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## MATHS

## BOOKS - PRINCETON MATHS (ENGLISH)

## ALGEBRA: CRACKING THE SYSTEM

## Example

1. If $2 x-15=25$, what is the value of $x$ ?
( Watch Video Solution
2. Suppose the evaporation rate of water in a
lake is given by the equation
$E=\frac{\frac{T_{a}-T_{b}}{700}-\frac{V}{T_{w}}}{h^{4}}$, where E is the evaporation
rate in gallons/day. $T_{a}$ is the air temperature,
$T_{d}$ is the dew point temperature, V is the volume of water in the table, $T_{w}$ is the water temperature, and h is the number of hours the water is exposed to sunlight. Which of the following expresses $T_{w}$ in terms $T_{a}, T_{b}, V, E$, and $h ?$

$$
\begin{aligned}
& \text { A. } T_{w}=\frac{E h^{4}}{\left(T_{a}-T_{b}\right) V} \\
& \text { B. } T_{w}=\frac{700}{T_{a}-T_{d}-E h^{4} V} \\
& \text { C. } T_{w}=\frac{V^{4}\left(T_{a}-T_{b}\right)}{E h^{4}} \\
& \text { D. } T_{w}=\frac{V}{\frac{T_{a}-T_{d}}{700}-E h^{4}}
\end{aligned}
$$

## Answer: D

## - Watch Video Solution

3. If $7 \sqrt{x}-24=11$, what is the value of $x$ ?
A. $\sqrt{5}$
B. $\sqrt{7}$
C. 5
D. 25

Answer: D

## - Watch Video Solution

4. If $\frac{18}{r+10}=\frac{3}{r}$, what is the value of $\frac{r}{3}$ ?
A. $\frac{2}{3}$
B. $\frac{3}{2}$
C. 2
D. 3

## Answer: A

## D Watch Video Solution

5. $\sqrt{t+4}=t-2$

Which of the following contains the solution
set to the equation above?
A. $\{0,5\}$
B. $\{0,4,5\}$
C. $\{0\}$
D. $\{5\}$

Answer: A

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6. If $4 x+2=4$, what is the value of $4 x-6$ ?
A. -6
B. -4
C. 4
D. 8

## Answer: B

## - Watch Video Solution

$$
\text { 7. If } \sqrt{5}=x-2 \text {, what is the value of }(x-2)^{2}
$$

## ?

A. $\sqrt{5}$
B. $\sqrt{7}$

## C. 5

D. 25

## Answer: C

## D Watch Video Solution

8. $3 a-7 b=4 d-9$
$-4 c+10 a=6 b+7$
$-2 a+3 c-4 d=10$

Given the system of equation above, what is
the value of $-10 a-2 b+2 c$ ?
A. -52
B. -26
C. 8
D. 26

Answer: A

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9. If $-3 x+6 \geq 18$, which of the following must be true?
A. $x \leq-4$
B. $x \leq 8$
C. $x \geq-4$
D. $x \geq-8$

Answer: A

D Watch Video Solution
10. Aubrie, Bera, and Kea are running a lemonade and snack stand to earn money.

They are sellling lemonade for $\$ 1.07$ a cup and
chocolate chip cookies for $\$ 0.78$ each. Their customers arrive on foot or by car. During a three hour period, they had 47 customers each buying only one item and made \$45.94.

Aubrie, Bera, and Kea need to determine if
they have enough supplies for tomorrow.

Solving which of the following system of equations will let them know many cups of
lemonade, $x$, and how many cookies, $y$, they sold today?

$$
\begin{aligned}
& \text { А. }\left\{\begin{array}{l}
x+y=45.94 \\
1.07 x+0.78 y=47
\end{array}\right. \\
& \text { B. }\left\{\begin{array}{l}
x+y=47 \\
1.07 x+0.78 y=45.94
\end{array}\right.
\end{aligned}
$$

C. $\left\{\begin{array}{l}x+y=47 \\ 0.78 x+1.07 y=45.94\end{array}\right.$
D. $\left\{\begin{array}{l}x+y=47 \\ 107 x+78 y=45.94\end{array}\right.$

Answer: B

## D View Text Solution

11. To save on helium costs, a balllon is inflated
with both helium and nitrogen gas. Between
the two gases, the ballon can be inflated up to
8 liters in volume. The density of helium is 0.20
gram per liter, and the density of nitrogen is
1.30 grams per liter. The ballon must be filled so that the volumetric average density of the ballon is lower than that of air, which has a density of 1.20 grams per liter. Which if the following system of inequalities best describes how the ballon will be filled, if x represent the number in liters of helium and $y$ represents the number of liters of nitrogen?

$$
\begin{aligned}
& \text { A. }\left\{\begin{array}{l}
x+y>8 \\
20 x+130 y>120
\end{array}\right. \\
& \text { B. }\left\{\begin{array}{l}
x+y=8 \\
\frac{0.2 x+1.30 y}{2}<1.20
\end{array}\right. \\
& \text { C. }\left\{\begin{array}{l}
x+y=47 \\
0.78 x+1.07 y=45.94
\end{array}\right.
\end{aligned}
$$

D. $\left[\begin{array}{l}x+y \leq 8 \\ 0.20 x+1.30 y<1.20\end{array}\right.$

## Answer: C

## D View Text Solution

12. Which of the following is equivalent to $\frac{f^{2}}{g}+f ?$
A. $\frac{f}{g}(f+g)$
B. $f\left(\frac{f}{g}+f\right)$
C. $f^{2}\left(\frac{1}{g}-\frac{1}{f}\right)$

$$
\text { D. } f^{2}\left(\frac{1}{g}+1\right)
$$

## Answer: A

## D Watch Video Solution

13. In the expressions $x^{2}+k x+12, \mathrm{k}$ is a negative integer. Which of the following is a possible value of $k$ ?

$$
\text { A. }-13
$$

$$
\text { B. }-12
$$

C. -6
D. 7

Answer: A

D Watch Video Solution
14. If $2 x-3 y=5$, what is the value of
$4 x^{2}-12 x y+9 y^{2} ?$

D Watch Video Solution
15. If $3-\frac{3}{x}=x+7$ and $\mathrm{xne0} 0^{\prime}$, which of the following is a possible value for $x$ ?
A. -7
B. -1
C. 1
D. 3

Answer: B

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16. What is the product all the solutions to the equation $3 z^{2}-12 z+6=0$ ?
A. $\sqrt{2}$
B. 2
C. 4
D. $4 \sqrt{2}$

Answer: B

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17. For $i=\sqrt{-1}$, what is the result of subtracting $(2+4 i)$ from $(-5+6 i)$ ?
A. $-7+2 i$
B. $-3-10 i$
C. $3+2 i$
D. $7-10 i$

Answer: A

D Watch Video Solution
18. If $i=\sqrt{-1}$, which of the following is equivalent to $\frac{14}{2-\sqrt{10} i}$ ?
A. $2+\sqrt{10} i$
B. $2-\frac{\sqrt{10}}{14} i$
C. $\frac{2-\sqrt{10} i}{14}$
D. $28-14 \sqrt{10} i$

Answer: A

- Watch Video Solution

19. $|x+2|=6$
$|y-2|=7$

For the equations shown above, which of the
folllowing is a possible value of $x-y$ ?
A. -14
B. -5
C. -2
D. 14

Answer: B

## Algebra Drill 1 No Calculator Section

1. $y=3 x+1$
$\frac{1}{2} y+x=1$
In the system of equations above, if $(x, y)$ is
the solution to the system, what is the value

$$
\text { of } \frac{y}{x} ?
$$

A. $\frac{3}{8}$
B. $\frac{2}{5}$
C. 8
D. $\frac{4}{3}$

## Answer: C

## D Watch Video Solution

2. For the equation $\sqrt{m x-5}=x+3$,the
value of $m$ is -3 . What is the solution set for
the equation?

$$
\text { A. }\{-3,3\}
$$

B. $\{-2\}$
C. $\{-2,-7\}$
D. $\{3,6\}$

Answer: B

## - Watch Video Solution

3. If $i=\sqrt{-1}$, what is the product of
$(4+7 i)$ and $\left(\frac{1}{2}-2 i\right) ?$

$$
\text { A. } 16-\frac{9}{2} i
$$

B. $14+\frac{9}{2} i$
C. $2-8 i-14 i^{2}$
D. $i\left(8+\frac{9}{2}\right)$

Answer: A

D Watch Video Solution
4. $r x^{2}=\frac{1}{s} x+3$

A quadratic equation is provided above, where
$r$ and $s$ are constants. What are the solutions
for $x$ ?

$$
\begin{aligned}
& \text { A. } x=\frac{1}{2 s r} \pm \frac{\sqrt{\frac{1}{s^{2}}+12 r}}{2 r} \\
& \text { B. } x=\frac{s}{2 r} \pm \frac{\sqrt{\frac{1}{s^{2}}-12 r}}{2 s r} \\
& \text { C. } x=\frac{s}{2 r} \pm \frac{\sqrt{\frac{1}{s^{2}}-12 r}}{2 r} \\
& \text { D. } x=\frac{s}{2 r} \pm \frac{\sqrt{s^{2}-12 s r}}{2 s r}
\end{aligned}
$$

Answer: A

## D Watch Video Solution

## Algebra Drill 2 Calculator Permitted Section

1. If $x+6>0$ and $1-2 x>-1$,which of the following values oof $x$ is NOT solutions?
A. -6
B. -4
C. 0
D. $\frac{1}{2}$

Answer: A
( Watch Video Solution
2. If $\frac{2 x}{x^{2}+1}=\frac{2}{x+2}$, what is the value of $x$ ?
A. $\frac{-1}{4}$
B. $\frac{1}{2}$
C. 0
D. 2

Answer: B
3. If the product of x and y is 76 , and x is twice the square of $y$, which of the following pairs of equations could be used to determine the values of $x$ and $y$ ?
A. $x y=76, x=2 y^{2}$
B. $x y=76, x=(2 y)^{2}$
C. $x+y=76: x=4 y^{2}$
D. $x y=76, x=2 y$

Answer: A
4. If $-6<-4 r+10 \leq 2$, what is the least possible value of $4 r+3$ ?
A. 2
B. 5
C. 8
D. 11

Answer: D

- Watch Video Solution

5. How many solutions exist to the equation

$$
|x|=|2 x-1| ?
$$

A. 0
B. 1
C. 2
D. 3

Answer: C

- Watch Video Solution

6. The sum of three numbers $a, b$, and $c$ is 400 .

One of the numbers, $a$, is 40 percent less than
the sum $b$ and $c$. What is the value of $b+c$ ?
A. 40
B. 60
C. 150
D. 250

Answer: D

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