



## MATHS

### BOOKS - NCERT MATHS (ENGLISH)

## CIRCLES

#### Exercise 10.1

1. AD is a diameter of a circle and AB is a chord. If  $AD = 34\text{cm}$ ,  $AB = 30\text{cm}$ , the distance of AB from the centre of the circle is

A. 17 cm

B. 15 cm

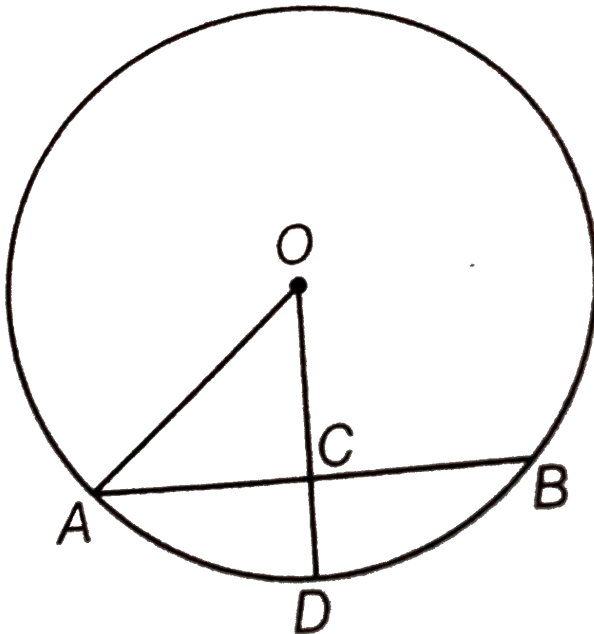
C. 4 cm

D. 8 cm

Answer: D

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2. In figure, if  $OA=5\text{cm}$ ,  $AB=8\text{ cm}$  and  $OD$  is perpendicular to  $AB$ , then  $CD$  is equal to



A. 2 cm

B. 3 cm

C. 4 cm

D. 5 cm

**Answer: A**



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3. If  $AB = 12\text{cm}$ ,  $BC = 16\text{ cm}$  and  $AB$  is perpendicular to  $BC$ , then the radius of the circle passing through the points  $A$ ,  $B$  and  $C$  is

A. 6 cm

B. 8 cm

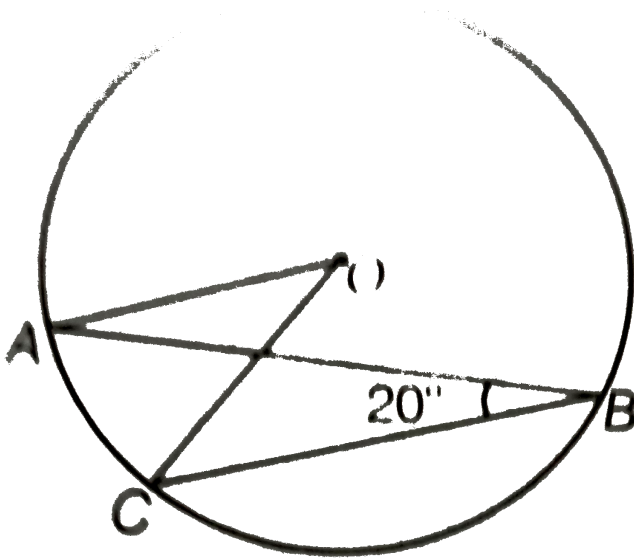
C. 10 cm

D. 12 cm

Answer: C

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4. If figure, if  $\angle ABC = 20^\circ$ , then  $\angle AOC$  is equal to



A.  $20^\circ$

B.  $40^\circ$

C.  $60^\circ$

D.  $10^\circ$

**Answer: B**



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5. If  $AOB$  is a diameter of the circle and  $AC=BC$ , then  $\angle CAB$  is equal to

A.  $30^\circ$

B.  $60^\circ$

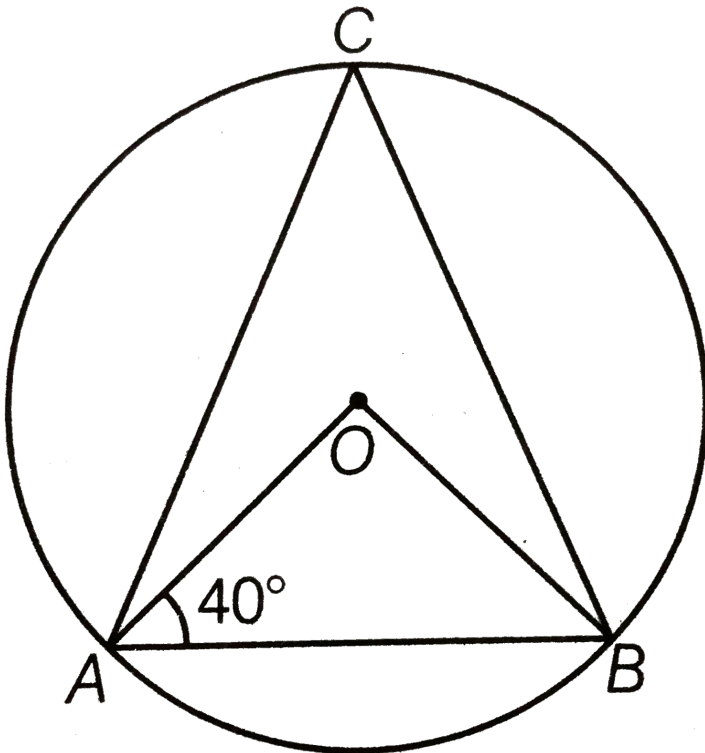
C.  $90^\circ$

D.  $45^\circ$

Answer: B

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6. In figure, if  $\angle OAB = 40^\circ$ , then  $\angle ACB$  is equal to



A.  $50^\circ$

B.  $40^\circ$

C.  $60^\circ$

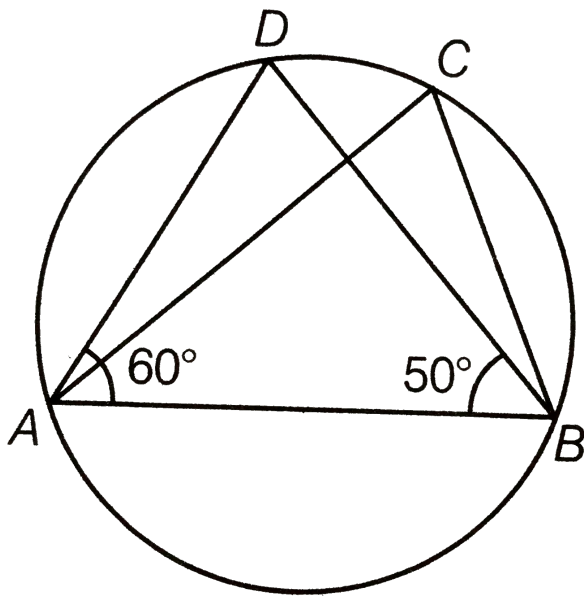
D.  $70^\circ$

**Answer: A**



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7. In figure, if  $\angle DAB = 60^\circ$ ,  $\angle ABD = 50^\circ$ , then  $\angle ACB$  is equal to



A.  $60^\circ$

B.  $50^\circ$

C.  $70^\circ$

D.  $80^\circ$

**Answer: C**



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8. ABCD is a cyclic quadrilateral such that AB is a diameter of the circle circumscribing it and  $\angle ADC = 140^\circ$ , then  $\angle BAC$  is equal to

A.  $80^\circ$

B.  $50^\circ$

C.  $40^\circ$

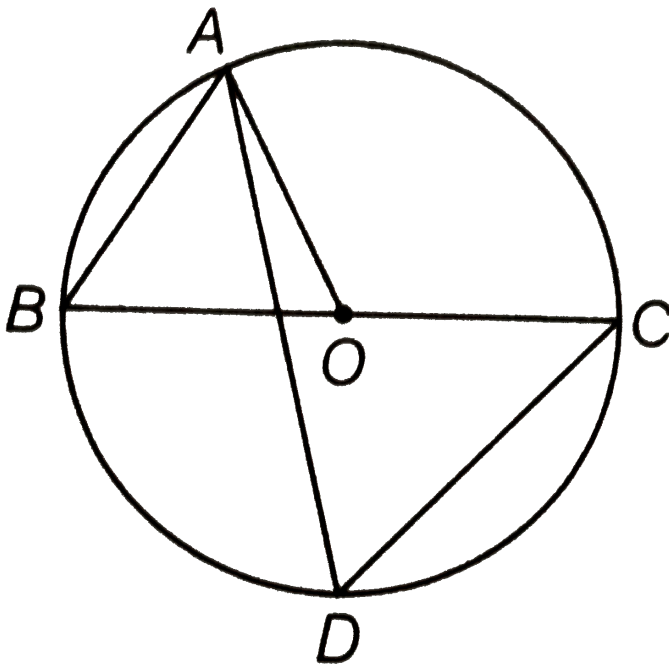
D.  $30^\circ$

**Answer: B**



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9. In figure, BC is a diameter of the circle and  $\angle BAO = 60^\circ$ . Then,  $\angle ADC$  is equal to



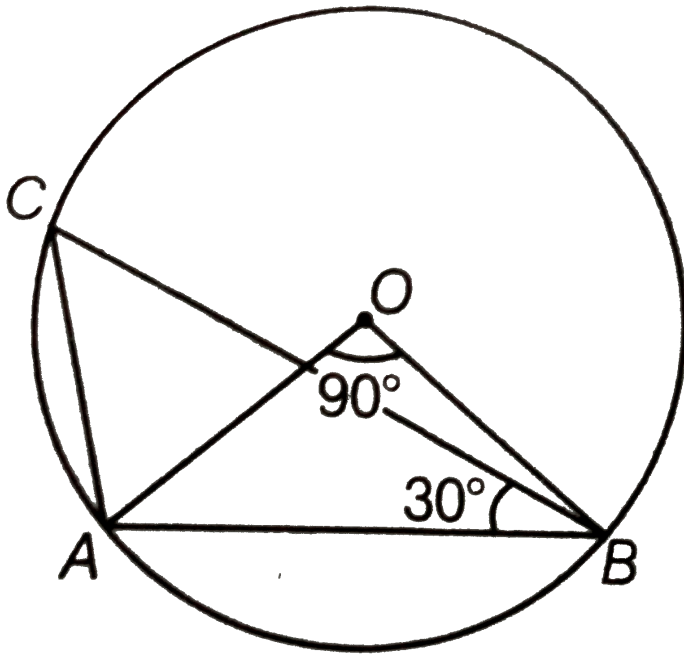
- A.  $60^\circ$
- B.  $45^\circ$
- C.  $50^\circ$
- D.  $120^\circ$

**Answer: A**



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10. In figure, if  $\angle AOB = 90^\circ$  and  $\angle ABC = 30^\circ$ , then  $\angle CAO$  is equal to



A.  $30^\circ$

B.  $45^\circ$

C.  $90^\circ$

D.  $60^\circ$

**Answer: D**



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## Exercise 10 2

1. Two chords AB and CD of a circle are each at distances 4 cm from the centre. Then,

A.  $AB=CD$ .

B. AB is not equal to CD.

C. AB there is no relation between CD.

D. AB is greater than CD.

**Answer: A**



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2. Two chords  $AB$  and  $AC$  of a circle with centre  $O$  are on the opposite sides of  $OA$ . Then,  $\angle OAB = \angle OAC$ .



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3. The congruent circles with centres  $O$  and  $O'$  intersect at two points  $A$  and  $B$ . Then,  $\angle AOB = \angle AO'B$ .



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4. Through three collinear points a circle can be draw.



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5. A circle of radius 3 cm can be drawn through two points A, B such that  $AB=6$  cm. State true or false



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6. If  $AOB$  is a diameter of a circle and  $C$  is a point on the circle, then  $AC^2 + BC^2 = AB^2$ .



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7.  $ABCD$  is a cyclic quadrilateral such that  $\angle A = 90^\circ$ ,  $\angle B = 70^\circ$ ,  $\angle C = 95^\circ$  and  $\angle D = 105^\circ$ .



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8. If A, B, C and D are four points such that  $\angle BAC = 30^\circ$  and  $\angle BDC = 60^\circ$ , then D is the centre of the circle through A, B and C.



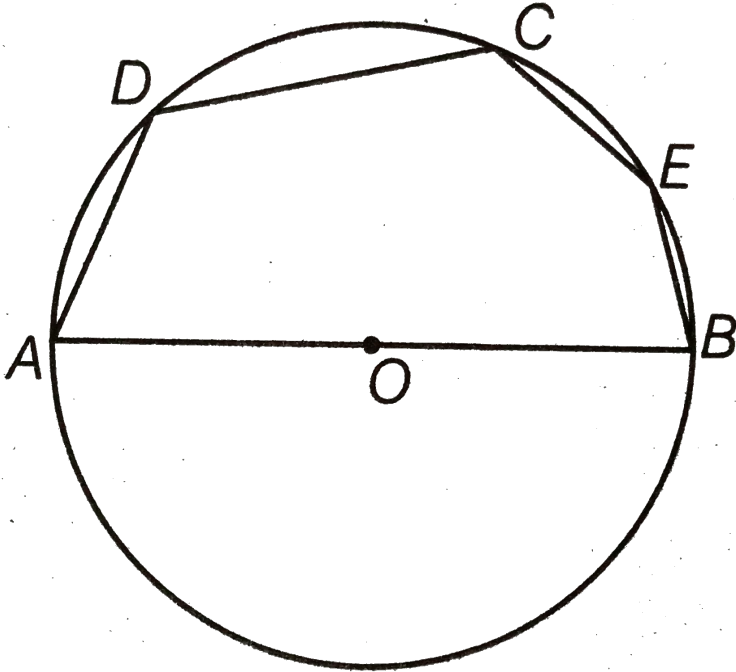
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9. If A, B, C and D are four points such that  $\angle BAC = 45^\circ$  and  $\angle BDC = 45^\circ$ , then A, B, C and D are concyclic.



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10. In figure, if  $AOB$  is a diameter and  $\angle ADC = 120^\circ$ , then  $\angle CAB = 30^\circ$ .



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1. If two arcs of a circle (or of congruent circles) are congruent, then corresponding chords are equal.

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2. If the perpendicular bisector of a chord  $AB$  of a circle  $PXAQBY$  intersects the circle at  $P$  and  $Q$ , prove that arc  $PXA \cong$  arc  $PYB$ .

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3.  $A$ ,  $B$  and  $C$  are three points on a circle. Prove that the perpendicular bisectors of  $AB$ ,  $BC$  and  $CA$  are concurrent.

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4. Two chords  $AB$  and  $AC$  of a circle are equal. Prove that the centre of the circle lies on the angle bisector of  $\angle BAC$ .

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5. If a line segment joining mid-points of two chords of a circle passes through the centre of the circle, prove that the two chords are parallel.

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6.  $ABCD$  is such a quadrilateral that  $A$  is the centre of the circle passing through  $B, C$  and  $D$ . Prove that  $\angle CBD + \angle CDB = \frac{1}{2} \angle BAD$ .

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7. If  $O$  is the circumcentre of a  $ABC$  and  $OD \perp BC$ , prove that  $\angle BOD = \angle a$ .

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8. On a common hypotenuse  $AB$ , two right angled triangles,  $ACB$  and  $ADB$  are situated on opposite sides. Prove that  $\angle BAC = \angle BDC$ .

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9. Two chords  $AB$  and  $AC$  of a circle subtends angles equal to  $90^\circ$  and  $150^\circ$ , respectively at the centre. Find  $\angle BAC$ , if  $AB$  and  $AC$  lie on the opposite sides of the centre.



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10. If  $BM$  and  $CN$  are the perpendiculars drawn on the sides  $AC$  and  $BC$  of the  $\triangle ABC$ , prove that the points  $B, C, M$  and  $N$  are concyclic.



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11. If a line is drawn parallel to the base of an isosceles triangle to intersect its equal sides, prove that the quadrilateral, so formed is cyclic.



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12. If the two sides of a pair of opposite sides of a cyclic quadrilateral are equal, prove that its diagonals are equal.

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13. The circumcentre of the  $\triangle ABC$  is O. Prove that  $\angle OBC + \angle BAC = 90^\circ$ .

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14. A chord of a circle is equal to the radius of the circle find the angle subtended by the chord at a point on the minor arc and also at a point on the major arc.

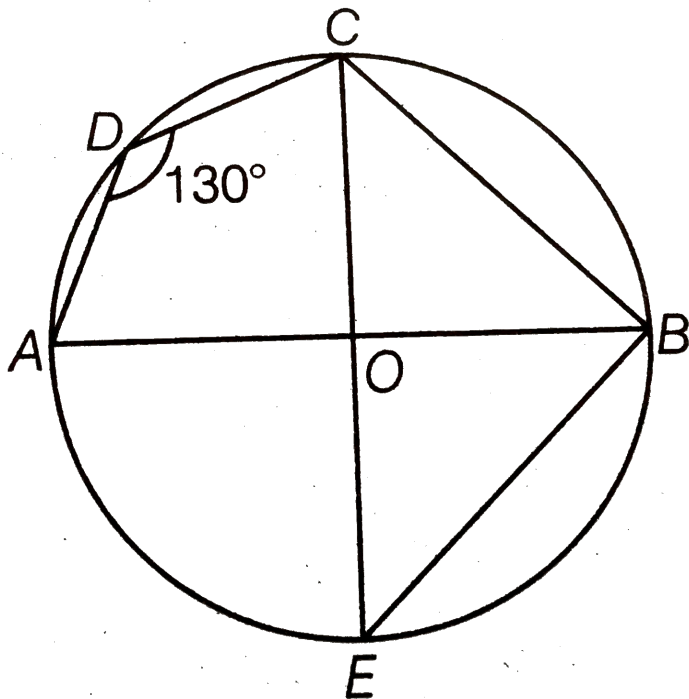
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15.

In

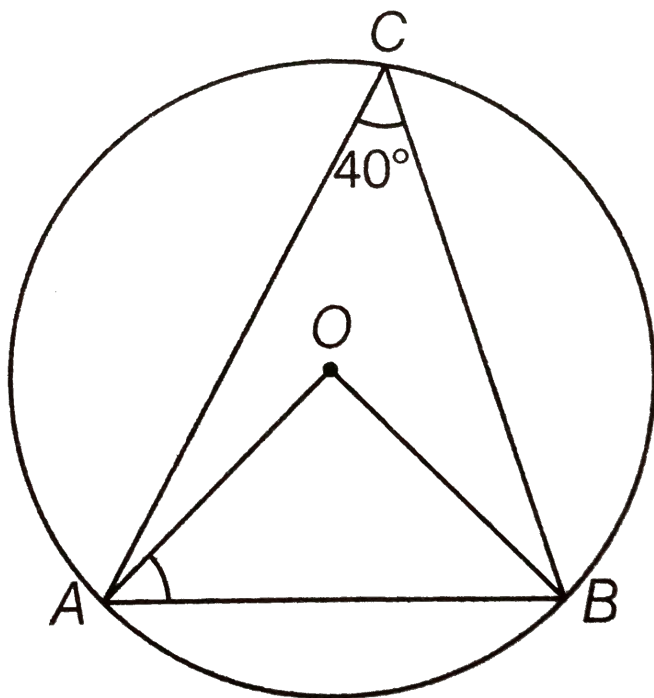
figure,

$\angle ADC = 130^\circ$  and chord  $BC = \text{chord } BE$ . Find  $\angle CBE$ .



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16. In figure,  $\angle ACB = 40^\circ$ . Find  $\angle OAB$ .



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17. In Figure,  $ABCD$  is a cyclic quadrilateral whose side  $AB$  is a diameter of the circle through  $A, B, C, D$ . If  $(\angle ADC) = 130^\circ$ , find  $\angle BAC$



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**18.** Two circles whose centres are  $O$  and  $O'$  intersect at  $P$ . Through  $P$ , a line  $l$  parallel to  $OO'$  intersecting the circles at  $C$  and  $D$  is drawn. Prove that  $CD = 2 OO'$

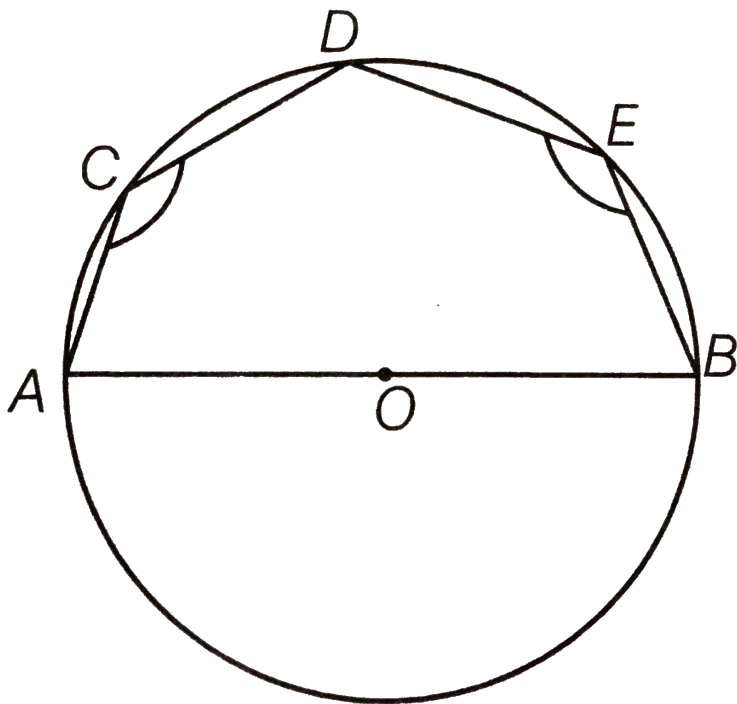


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**19.** In figure,  $AOB$  is a diameter of the circle and  $C, D, E$  are any three points on the semi-circle. Find the value of



$$\angle ACD + \angle BED.$$



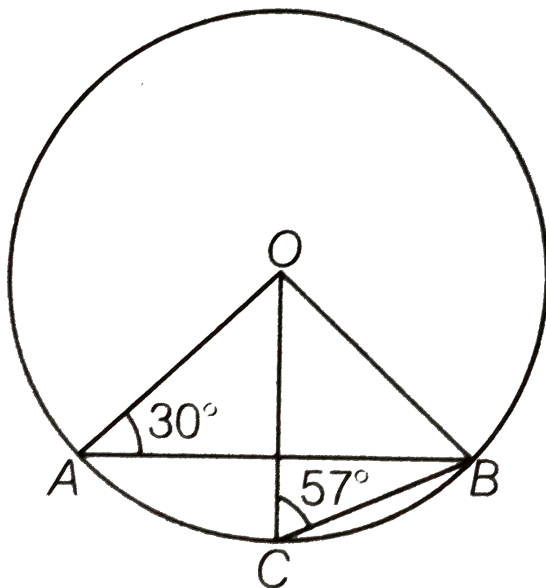
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20.

In

figure,

$\angle OAB = 30^\circ$  and  $\angle OCB = 57^\circ$ . Find  $\angle BOC$  and  $\angle AOC$



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### Exercise 10 4

1. If two equal chords of a circle intersect within the circle, prove that the segments of one chord are equal to corresponding segments of the other chord.



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2. If the non-parallel sides of a trapezium are equal, prove that it is cyclic.



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3.  $P$ ,  $Q$  and  $R$  are, respectively, the mid points of sides  $BC$ ,  $CA$  and  $AB$  of a triangle  $ABC$



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4.  $ABCD$  is a parallelogram. A circle through  $A$ ,  $B$  is so drawn that it intersects  $AD$  at  $P$  and  $BC$  at  $Q$ . Prove that  $P$ ,  $Q$ ,  $C$  and  $D$  are concyclic.



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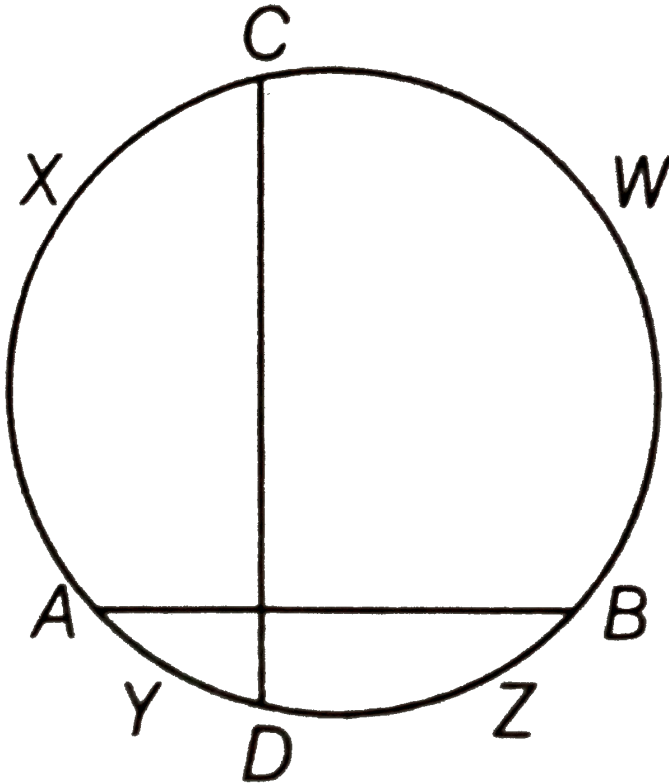
5. Prove that If the bisector of any angle of a triangle and the perpendicular bisector of its opposite side intersect, they will intersect on the circumcircle of the triangle.



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6. If two chords AB and CD of a circle AYDZBWCX intersect at right angles, then prove that  $\text{arc CXA} + \text{arc DZB} = \text{arc AYD} + \text{arc BWC}$ .

BWC = semi-circle.



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7. If ABC is an equilateral triangle inscribed in a circle and P be any point on the minor arc BC which does not coincide with B or C, then prove that PA is angle bisector of  $\angle BPC$ .



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8. In the figure, AB and CD are two chords of a circle, intersecting each other at a point E. Prove that  $\angle AEC = \frac{1}{2}(\text{angle subtended by arc CXA at the centre} + \text{angle subtended by arc DYB at the centre})$ .



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9. If bisectors of opposite angles of a cyclic quadrilateral ABCD intersect the circle, circumscribing it at the points P and Q, prove that PQ is a diameter of the circle.



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10. A circle has radius  $\sqrt{2}$ cm it is divided into 2 segments by a chord of length 2cm prove that angle subtended by the chord at a point in major segment is  $45^\circ$

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11.  $AB$  and  $CD$  are equal chords of a circle whose centre is  $O$ , when produced these chords meet at  $E$ , Prove that  $EB = ED$ .

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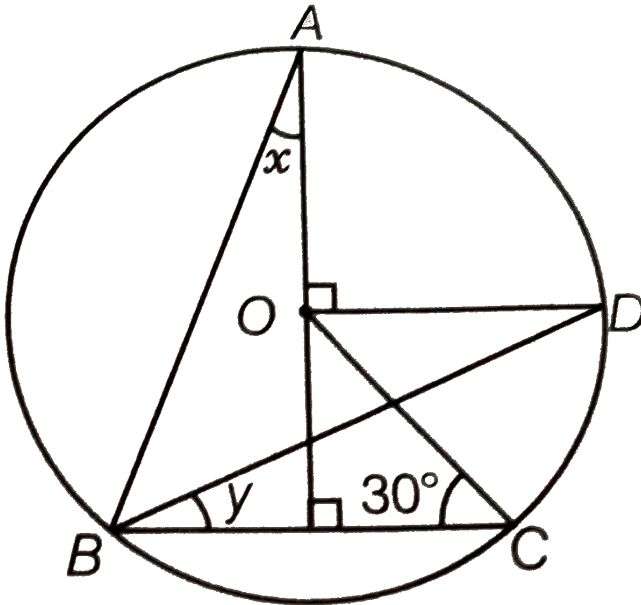
12.  $AB$  and  $AC$  are two chords of a circle of radius  $r$  such that  $AB=2AC$ . If  $p$  and  $q$  are the distances of  $AB$  and  $AC$  from the centre Prove that  $4q^2 = p^2 + 3r^2$ .



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13. In figure,  $O$  is the centre of the circle  $\angle BCO = 30^\circ$ . Find

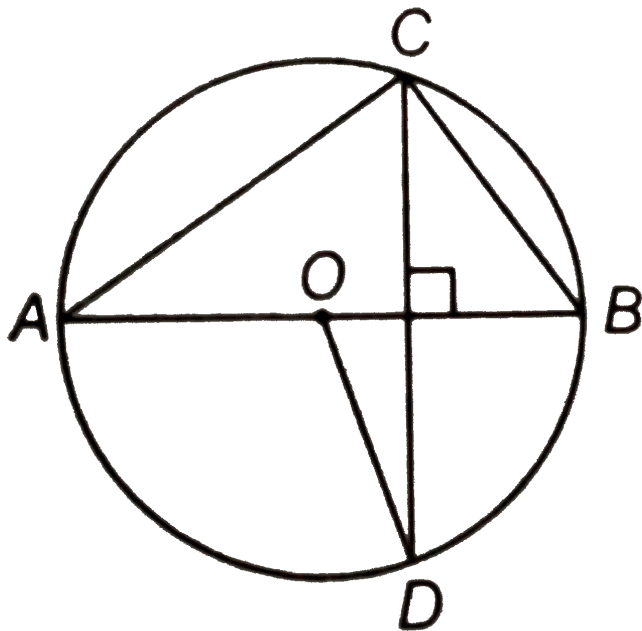
$x$  and  $y$ .



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14. If figure,  $O$  is the centre of the circle,  $BD = OD$  and  $CD \perp AB$ . Find  $\angle CAB$ .



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