

MATHS

BOOKS - SURA MATHS (TAMIL ENGLISH)

ALGEBRA



1. Solve the following system of linear equations in three variables

x + y + z = 5, 2x - y + z = 9, x - 2y + 3z = 16

2. Solve the following system of linear equations in three

variables

$$rac{1}{x}-rac{2}{y}+4=0, rac{1}{y}-rac{1}{z}+1=0, rac{2}{z}+rac{3}{x}=14$$

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3. Solve the following system of linear equations in three

variables

$$x+20=rac{3y}{2}+10=2z+5=110-(y+z)$$

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4. Discuss the nature of solutions of the following system is

equations

$$x+2y-z=6,\;-3x-2y+5z=\;-12,x-2z=3$$

5. Discuss the nature of solutions of the following system is

equations

$$2y+z=3(-x+1),\;-x+3y-z=-4,3x+2y+z=-rac{1}{2}$$

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6. Discuss the nature of solutions of the following system is equations y+z z+x x+y

$$rac{y+z}{4} = rac{z+x}{3} = rac{x+y}{2}, x+y+z = 27$$

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7. Vani, her father and her grand father have an average age of53. One-half of her grand father's age plus one-third of her

father's age plus one fourth of Vani's age is 65. Four years ago if Vani's grandfather was four times as old as Vani then how old are they all now?



8. The sum of the digits of a three-digit number is 11. If the digits are revesed, the new number is 46 more than five times the former number. If the hundreds digit plus twice the tens digit is equal to the units digits, then find the original three digit number?



9. There are 12 pieces of five, ten and twenty rupee currrencies whose total value is ₹105. When first 2 sorts are interchanged in

their numbers its value will be increased by ₹20. Find the number

of currencies in each sort.



3. Find the GCD of the given polynomials

 $3x^4 + 6x^3 - 12x^2 - 24x, 4x^4 + 14x^3 + 8x^2 - 8x$



4. Find the GCD of the given polynomials

 $3x^3 + 3x^2 + 3x + 3, 6x^3 + 12x^2 + 6x + 12$

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5. Find the LCM of the given expressions.

 $4x^2y, 8x^3y^2$

6. Find the LCM of the given expressions.



8. Find the LCM of the given expressions.

$$p^2-3p+2,\,p^2-4$$

9. Find the LCM of the given expressions.

$$2x^2 - 5x - 3, 4x^2 - 36$$



10. Find the LCM of the given expressions.

$$\left(2x^2-3xy
ight)^2$$
, (4x-6y)^(3), 8x^(3)-27y^(3)`

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1. Find the LCM and GCD for the following and verify that f(x) imes g(x) = LCM imes GCD21x^(2)y, 35xy^(2)` 2. Find the LCM and GCD for the following and verify that f(x) imes g(x)=LCM imes GCD $ig(x^3-1ig)(x+1), x^3+1$

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3. Find the LCM and GCD for the following and verify that f(x) imes g(x)=LCM imes GCD $ig(x^2y+xy^2ig),\,ig(x^2+xyig)$

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4. Find the LCM of each pair of the following polynomials

 $a^2+4a-12, a^2-5a+6$ whose GCD is a-2



7. Find the GCD for each pair of the following polynomials

$$ig(x^3+y^3ig),ig(x^4+x^2y^2+y^4ig)$$
 whose LCM is

$$ig(x^3+y^3ig)ig(x^2+xy+y^2ig)$$

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8. Given the LCM and GCD of the two polynomials p(x) and q(x)

find the unknownn polynomial in the following table

S. No	LCM*	GCD	p(x)	<i>q(x)</i>
(i)	$a^3 - 10a^2 + 11a + 70$	<i>a</i> – 7	$a^2 - 12a^2 + 35$	
(ii)	$(x^2 + y^2) (x^4 + x^2y^2 + y^4)$	(x^2-y^2)		$(x^4 - y^4) (x^2 + y^2 - xy)$

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Execrise 3 4

1. Reduce each of the following retional expression to its lowest

table form .

 $\frac{x^2-1}{x^2+x}$

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2. Reduce each of the following retional expression to its lowest

table form .

$$\frac{x^2 - 11x + 18}{x^2 - 4x + 4}$$

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3. Reduce each of the following retional expression to its lowest

table form .

$$\frac{9x^2 + 81x}{x^3 + 8x^2 - 9x}$$

4. Reduce each of the following retional expression to its lowest

table form .

$$\frac{p^2-3p-40}{2p^3-24p^2+64p}$$



5. Find the excluded values, if any of the following expressions

$$rac{y}{y^2-25}$$



6. Find the excluded values, if any of the following expressions

$$\frac{t}{t^2-5t+6}$$

7. Find the excluded values, if any of the following expressions

 $\frac{x^2+6x+8}{x^2+x-2}$

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8. Find the excluded values, if any of the following expressions

$$\frac{x^3 - 27}{x^3 + x^2 - 6x}$$

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Execrise 3 5

1. Simplify

$$rac{4x^2y}{2z^2} imesrac{6xz^3}{20y^4}$$



$$\left(rac{p^2-10p+21}{p-7} imesrac{p^2+p-12}{\left(p-3
ight)^2}
ight)$$

3. Simplify

 $\frac{5t^3}{4t-8}\times \frac{6t-12}{10t}$

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4. Simplify $\frac{2a^2 + 5a + 3}{2a^2 + 7a + 6} \div \frac{a^2 + 6a + 5}{-5a^2 - 35a - 50}$

$$rac{b^2+3b-28}{b^2+4b+4} \div rac{b^2-49}{b^2-5b-14}$$

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6. Simplify

$$rac{x+2}{4y} \div rac{x^2-x-6}{12y^2}$$

7. Simplify

$$rac{12t^2-22t+8}{3t} \div rac{3t^2+2t-8}{2t^2+4t}$$

$$rac{x(x+1)}{x-2} + rac{x(1-x)}{x-2}$$

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2. Simplify

$$rac{x+2}{x+3}+rac{x-1}{x-2}$$

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3. Simplify

$$\frac{x^3}{x-y} + \frac{y^3}{y-x}$$

$$\frac{(2x+1)(x-2)}{x-4}-\frac{\big(2x^2-5x+2\big)}{x-4}$$

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5. Simplify

4x	 x	+	1
$x^2 - 1$	x	_	1

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6. Subtract
$$\displaystyle rac{1}{x^2+2}$$
 from $\displaystyle rac{2x^3+x^2+3}{\left(x^2+2
ight)^2}$

7. Which rational expression should be subtracted from
$$\frac{x^2+6x+8}{x^3+8}$$
 to get $\frac{3}{x^2-2x+4}$.

8. If
$$A = rac{2x+1}{2x-1}, B = rac{2x-1}{2x+1}$$
 find $rac{1}{A-B} - rac{2B}{A^2-B^2}$

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9. If
$$A = \frac{x}{x+1}, B = \frac{1}{x+1}, provet^{((A+B)^{(2)+(A-1)})}$$

B)^(2))/(A÷B)=(2(x^(2)+1))/(x(x+1)^(2))`

10. Peri needs 4 hours to complete a work. His friend Yuvan needs 6 hours to complete the same work. How long will take to complete if they work together?



11. Iniya bought 50 kg of fruits consisting of apples and bananas.

She paid twice as much per kg for the apple as she did for the

banana. If Iniya bought ₹1800 worth of apples and ₹600 worth

bananas, then how many kg of each fruits did she buy?





1. Find the square root of the following rational expressions.

 $\frac{400x^4y^{12}z^{16}}{100x^8y^4z^4}$

2. Find the square root of the following rational expressions.

$$\frac{7x^2+2\sqrt{14}x+2}{x^2-\frac{1}{2}x+\frac{1}{16}}$$

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3. Find the square root of the following rational expressions.

$$rac{121 {(a + b)}^8 {(x + y)}^8 {(b - c)}^8}{81 {(b - c)}^4 {(a - b)}^{12} {(b - c)}^4}$$

4. Find the square root of the following

 $4x^2 + 20x + 25$

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5. Find the square root of the following

 $9x^2 - 24xy + 30xz - 40yz + 25z^2 + 16y^2$

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6. Find the square root of the following

$$1+rac{1}{x^6}+rac{2}{x^3}$$

7. Find the square root of the following

$$\left(4x^2-9x+2
ight) \left(7x^2-13x-2
ight) \left(28x^2-3x-1
ight)$$

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8. Find the square root of the following

$$\left(2x^2+rac{17}{6}x+1
ight)\left(rac{3}{2}x^2+4x+2
ight)\left(rac{4}{3}x^2+rac{11}{3}x+2
ight)$$

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1. Find the square root of the following polynomials by division method

$$x^4 - 12x^3 + 42x^2 - 36x + 9$$



2. Find the square root of the following polynomials by division

method

 $37x^2 - 28x^3 + 4x^4 + 42x + 9$



3. Find the square root of the following polynomials by division

method

 $16x^4 + 8x^2 + 1$

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4. Find the square root of the following polynomials by division

method

$$121x^4 - 198x^3 - 183x^2 + 216x + 144$$



6. Find the values of a and b if the following polynomials are

perfect squares

 $4x^4 - 12x^3 + 37x^2 + bx + a$



7. Find the values of a and b if the following polynomials are

perfect squares

 $ax^4 + bx^3 + 361ax^2 + 220x + 100$

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8. Find the values of m and n if the following expression are

perfect squares.

 $rac{1}{x^4} - rac{6}{x^3} + rac{13}{x^2} + rac{m}{x} + n$

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9. Find the values of m and n if the following expression are

perfect squares.

$$x^4 - 8x^3 + mx^2 + nx + 16$$





1. Determine the quadratic equations, whose sum and product of

roots are

-9, 20

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2. Determine the quadratic equations, whose sum and product of

roots are

 $\frac{5}{3}, 4$

3. Determine the quadratic equations, whose sum and product of

roots are

$$rac{-3}{2},\ -1$$

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4. Determine the quadratic equations, whose sum and product of

roots are

$$-(2-a)^2,(a+5)^2$$

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5. Find the sum and product of the roots for each of the following quadratic equations

$$x^2 + 3x - 28 = 0$$

6. Find the sum and product of the roots for each of the following quadratic equations

 $x^2+3x=0$

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7. Find the sum and product of the roots for each of the following quadratic equations

$$3 + \frac{1}{a} = \frac{10}{a^2}$$



8. Find the sum and product of the roots for each of the following quadratic equations

$$3y^2 - y - 4 = 0$$

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Execrise 3 10
1. Solve the following quadratic equations by factorization
method.
 $4x^2 - 7x - 2 = 0$
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2. Solve the following quadratic equations by factorization method.

$$3ig(p^2-6ig)=p(p+5)$$

3. Solve the following quadratic equations by factorization method.

$$\sqrt{a(a-7)}=3\sqrt{2}$$

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4. Solve the following quadratic equations by factorization method.

$$\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$$

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5. Solve the following quadratic equations by factorization method.

$$2x^2-x+\frac{1}{8}=0$$

6. The number of volleyball games that must be scheduled in a league with n teams is given by $G(n) = \frac{n^2 - n}{2}$ where each team plays with every other team exactly once. A league scheledules 15 games. How many teams are in the league?

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1. Solve the following quadratic equation by completing the square method

 $9x^2 - 12x + 4 = 0$

2. Solve the following quadratic equation by completing the

square method

$$\frac{5x+7}{x-1} = 3x+2$$

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3. Solve the following quadratic equation by formula method

$$2x^2 - 5x + 2 = 0$$

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4. Solve the following quadratic equation by formula method

$$\sqrt{2}f^2-6f+2\sqrt{2}$$

5. Solve the following quadratic equation by formula method

$$3y^2 - 20y - 3 = 0$$



7. A garden measuring 12m by 16m is to have wide installed all the way around so that it incease the total area of $285m^2$. What is the width of the pathway?



1. If the difference between a number and its reciprocal is $\frac{24}{5}$, find the number.

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2. A garden measuring 12m by 16m is to have wide installed all the way around so that it incease the total area of $285m^2$. What is the width of the pathway?

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3. A bus covers a distance of 90km at a unform speed. Had the speed been 15km/hour more it would have taken 30 minutes less for the journey. Find the original speed of the bus.



4. A girl is twice as old as her sister. Five years hence, the product of their ages (in years) will be 375. Find their present ages.

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5. A pole has to be erected at a point on the boundary of a circular ground of diameter 20m in such a way that the difference of its distance form two diameterically opposite fixed gates P and Q on the boundary is 4 m. Is it possible to do so? If answer is yes at what distance from the two gates should the pole be erected?


6. From a group of black bees $2x^2$, square root of half of the group went to a tree. Again eightninth of th ebess went to the same tree. The remaining two got caught up in a fragrant lotus. How many bees were there in total?



7. Music is been played in two opposite galleries with certain group of people. In the first gallery a group of 4 singers were singing and in the second gallery 9 singers were singing. The two galleries are separate by the distance of 70m. Where should a person stand for hearing the same intensity of the singers voice? (Hit: The ratio of the sound intensity is equal to square of the ratio of their corresponding distances).



8. There is a square field whose side is 10 m. A square flower bed is prepared in its centre leaving a gravel path all round the flower bed. The total cost of the laying the flower bed and gravelling the path at ₹3 and ₹4 per square metre respectively is ₹364. Find the width of the gravel path.

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9. Two woman together took 100 eggs to a market, one had more than the other. Both sold tham for the same sum of the money. The first then said to the second, "If 1 had your eggs, I would have earned ₹15", to which the second replied: "If 1 had your eggs, I would have earned ₹ $6\frac{2}{3}$?. How many eggs did each had in the beginning?



10. The hypotenuse of a right angled triangle is 25cm an dits

perimeter 56 cm. Find the length of the smallest side.



equations

 $15x^2 + 11x + 2 = 0$

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2. Determine the nature of the roots for the following quadratic

equations

 $x^2-x-1=0$



3. Determine the nature of the roots for the following quadratic

equations

$$\sqrt{2}t^2-3t+3\sqrt{2}=0$$



4. Determine the nature of the roots for the following quadratic

equations

 $9y^2-6\sqrt{2}y+2=0$



5. Determine the nature of the roots for the following quadratic

equations

$$9a^2b^2x^2-24abcdx+16c^2d^2=0, a
eq 0, b
eq 0$$

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6. Find the value of 'k' for which the roots of the following equations are real and equal

 $(5k-6)x^2 + 2kx + 1 = 0$

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7. Find the value of 'k' for which the roots of the following equations are real and equal

$$kx^2 + (6k+2)x + 16 = 0$$

8. If the roots of $(a-b)x^2 + (b-c)x + (c-a) = 0$ are real

and equal, then prove that b, a, c are in arithmetic progression.

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9. If a, b are real then show that the roots of the equation

 $(a-b)x^2-6(a+b)x-9(a-b)=0$ are real and unequal.

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1. Write each of the following expressions in terms of

 $\alpha + \beta$ and $\alpha\beta$.



3. Write each of the following expressions in terms of $\alpha + \beta$ and $\alpha\beta$.

(3lpha-1)(3eta-1)

4. Write each of the following expressions in terms of

$$lpha+eta ext{ and } lphaeta. \ rac{lpha+3}{eta}+rac{eta+3}{lpha}$$

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5. The roots of the equation $2x^2 - 7x + 5 = 0$ are α and β .

Without solving the root find

$$\frac{1}{\alpha} + \frac{1}{\beta}$$

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6. The roots of the equation $2x^2 - 7x + 5 = 0$ are α and β .

Without solving the root find

$$\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$$

7. The roots of the equation $2x^2 - 7x + 5 = 0$ are α and β .

Without solving the root find

 $\frac{\alpha+2}{\beta+2}+\frac{\beta+2}{\alpha+2}$

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8. The roots of the equation $x^2+6x-4=0$ are lpha,eta. Find the quadratic equation whose roots area $lpha^2$ and eta^2



9. The roots of the equation $x^2+6x-4=0$ are lpha,eta. Find the

quadratic equation whose roots area



 $\left(lpha^2 eta
ight)$ and $eta^2 lpha$

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11. If α, β are the roots of $7x^2 + ax + 2 = 0$ and if $\beta - \alpha = \frac{-13}{7}$. find the value of a.

12. If one root of the equation $2y^2 - ay + 64 = 0$ is twice the other then find the values of a.



 $x^2 - 9x + 20 = 0$



2. Graph the following quadratic equations and state their nature of solutions.

 $x^2 - 4x + 4 = 0$



3. Graph the following quadratic equations and state their nature of solutions.

$$x^2 + x + 7 = 0$$



4. Graph the following quadratic equations and state their nature of solutions.



6. Draw the graph of
$$y=x^2-4$$
 and hence solve $x^2-x-12=0.$

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7. Draw the graph of $y=x^2+x$ and hence solve $x^2+1=0.$

8. Draw the graph of $y = x^2 + 3x + 2$ and use it to solve

$$x^2 + 2x + 1 = 0.$$

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9. Draw the graph $y = x^2 + 3x - 4$ and hence use it to solve $x^2 + 3x - 4 = 0$.

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10. Draw the graph of $y = x^2 - 5x + 6$ and hence solve $x^2 - 5x - 14 = 0.$

11. Draw the graph of $y = 2x^2 - 3x - 5$ and hence solve $2x^2 - 4x - 6 = 0.$

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12. Draw the graph of
$$y = (x-1)(x+3)$$
 and hence solve $x^2 - x - 6 = 0.$

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Execrise 3 16

1. In the matrix
$$A=egin{bmatrix}8&9&4&3\\-1&\sqrt{7}&rac{\sqrt{3}}{2}&5\\1&4&3&0\\6&8&-11&1\end{bmatrix}$$
 , write

The number of elements.

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2. In the matrix
$$A = \begin{bmatrix} 8 & 9 & 4 & 3 \\ -1 & \sqrt{7} & \frac{\sqrt{3}}{2} & 5 \\ 1 & 4 & 3 & 0 \\ 6 & 8 & -11 & 1 \end{bmatrix}$$
, write

The order of the matrix.



3. In the matrix
$$A = \begin{bmatrix} 8 & 9 & 4 & 3 \\ -1 & \sqrt{7} & \frac{\sqrt{3}}{2} & 5 \\ 1 & 4 & 3 & 0 \\ 6 & 8 & -11 & 1 \end{bmatrix}$$
, write

Write the elements $a_{22}, a_{23}, a_{24}, a_{34}, a_{43}, a_{44}$,

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4. If the matrix has 18 elements, what are the possible orders it

can have? What if it has 6 elements?



5. Construct a 3 imes 3 matrix whose elements are given by

 $a_{ij} = \left|i-2j
ight|$

6. Construct a 3 imes 3 matrix whose elements are given by

$$a_{ij}=rac{\left(i+j
ight) ^{3}}{3}$$

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7. If
$$A = \begin{bmatrix} 5 & 4 & 3 \\ 1 & -7 & 9 \\ 3 & 8 & 2 \end{bmatrix}$$
 then find the transpose of A.

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8. If
$$A = \begin{bmatrix} \sqrt{7} & -3 \\ -\sqrt{5} & 2 \\ \sqrt{3} & -5 \end{bmatrix}$$
 then find the transpose of -A.

9. If
$$A = egin{bmatrix} 5 & 2 & 2 \ -\sqrt{17} & 0.7 & rac{5}{2} \ 8 & 3 & 1 \end{bmatrix}$$
 then verify $ig(A^Tig)^T = A.$



10. Find the values of x, y, and z from the following equations

 $\left[egin{array}{cc} 12 & 3 \ x & 5 \end{array}
ight] = \left[egin{array}{cc} y & z \ 3 & 5 \end{array}
ight]$

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11. Find the values of x, y, and z from the following equations

$$egin{bmatrix} x+y & 2 \ 5+z & xy \end{bmatrix} = egin{bmatrix} 6 & 2 \ 5 & 8 \end{bmatrix}$$

12. Find the values of x, y, and z from the following equations

 $egin{bmatrix} x+y+a \ x+z \ y+z \end{bmatrix} = egin{bmatrix} 9 \ 5 \ 7 \end{bmatrix}$

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Execrise 3 17

1. If
$$A = \begin{bmatrix} 1 & 9 \\ 3 & 4 \\ 8 & -3 \end{bmatrix}$$
, $B = \begin{bmatrix} 5 & 7 \\ 3 & 3 \\ 1 & 0 \end{bmatrix}$ then verify that $A + B = B + A$

2. If
$$A = \begin{bmatrix} 1 & 9 \\ 3 & 4 \\ 8 & -3 \end{bmatrix}, B = \begin{bmatrix} 5 & 7 \\ 3 & 3 \\ 1 & 0 \end{bmatrix}$$
 then verify that $A + (-A) = (-A) + A$

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3.

$$A = egin{bmatrix} 4 & 3 & 1 \ 2 & 3 & -8 \ 1 & 0 & -4 \end{bmatrix}, B = egin{bmatrix} 2 & 3 & 4 \ 1 & 9 & 2 \ -7 & 1 & -1 \end{bmatrix}, C = egin{bmatrix} 8 & 3 & 4 \ 1 & -2 & 3 \ 2 & 4 & -1 \end{bmatrix}$$

lf

then verify that A + (B + C) = (A + B) + c

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4. Find the X and Y if
$$X+Y=\left[egin{array}{cc}7&0\\3&5\end{array}
ight] ext{ and } X-Y=\left[egin{array}{cc}3&0\\0&4\end{array}
ight]$$

5. If
$$A = \begin{bmatrix} 0 & 4 & 9 \\ 8 & 3 & 7 \end{bmatrix}$$
, $B = \begin{bmatrix} 7 & 3 & 8 \\ 1 & 4 & 9 \end{bmatrix}$ find the value of B-5A

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6. If
$$A = \begin{bmatrix} 0 & 4 & 9 \\ 8 & 3 & 7 \end{bmatrix}$$
, $B = \begin{bmatrix} 7 & 3 & 8 \\ 1 & 4 & 9 \end{bmatrix}$ find the value of 3A-9B



7. Find the value of x, y, z if

$$egin{pmatrix} x-3 & 3x-z \ x+y+7 & x+y+z \end{pmatrix} = egin{pmatrix} 1 & 0 \ 1 & 6 \end{pmatrix}$$

8. Find the value of x, y, z if

$$egin{bmatrix} x & y-z & z+3 \end{bmatrix} + egin{bmatrix} y & 4 & 3 \end{bmatrix}$$

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9. Find x and y if
$$x \begin{pmatrix} 4 \\ -3 \end{pmatrix} x + y \begin{pmatrix} -2 \\ 3 \end{pmatrix} = \begin{pmatrix} 4 \\ 6 \end{pmatrix}$$
.

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10. Find the non-zero values of x satisfying the matrix equation

$$xiggl[egin{array}{ccc} 2x & 2 \ 3 & x \ \end{bmatrix}, 2iggl[egin{array}{ccc} 8 & 5x \ 4 & 4x \ \end{bmatrix} = 2iggl[egin{array}{ccc} x^2+8 & 24 \ 10 & 6x \ \end{bmatrix}$$

11. Solve for x, y,
$$egin{bmatrix} x^2 \\ y^2 \end{bmatrix} + 2 egin{bmatrix} -2x \\ -y \end{bmatrix} = egin{bmatrix} 5 \\ 8 \end{bmatrix}$$





3. Find the order of the product matrix AB is

	(i)	(ii)	(iii)	(iv)	(v)
Orders of A	3×3	4×3	4×2	4×5	1×1
Orders of B ·	3×3	3×2	2×2	5×1	1×3

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4. If
$$A = \begin{bmatrix} 2 & 5 \\ 4 & 3 \end{bmatrix}, B = \begin{bmatrix} 1 & -3 \\ 2 & 5 \end{bmatrix}$$
 find AB, BA and check if

AB=BA?

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5. Given that

$$A = \begin{bmatrix} 1 & 3 \\ 5 & -1 \end{bmatrix}, B = \begin{bmatrix} 1 & -1 & 2 \\ 3 & 5 & 2 \end{bmatrix}, C = \begin{bmatrix} 1 & 3 & 2 \\ -4 & 1 & 3 \end{bmatrix}$$
 verify

that A(B+C) = AB + AC.

6. Show that the matrices $A = \begin{bmatrix} 1 & 2 \\ 3 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 1 & -2 \\ -3 & 1 \end{bmatrix}$ satisfy commutative property AB=BA.

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7. Let
$$A = \begin{bmatrix} 1 & 2 \\ 1 & 3 \end{bmatrix}, B = \begin{bmatrix} 4 & 0 \\ 1 & 5 \end{bmatrix}, C = \begin{bmatrix} 2 & 0 \\ 1 & 2 \end{bmatrix}$$
 show that $A(BC) = (AB)C$

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8. Let
$$A = \begin{bmatrix} 1 & 2 \\ 1 & 3 \end{bmatrix}$$
, $B = \begin{bmatrix} 4 & 0 \\ 1 & 5 \end{bmatrix}$, $C = \begin{bmatrix} 2 & 0 \\ 1 & 2 \end{bmatrix}$ show that $(A - B)C = AC - BC$

9. Let
$$A = \begin{bmatrix} 1 & 2 \\ 1 & 3 \end{bmatrix}$$
, $B = \begin{bmatrix} 4 & 0 \\ 1 & 5 \end{bmatrix}$, $C = \begin{bmatrix} 2 & 0 \\ 1 & 2 \end{bmatrix}$ show that $(A - B)^T = A^T - B^T$

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10. If
$$A = \begin{pmatrix} \cos \theta & 0 \\ 0 & \cos \theta \end{pmatrix}$$
, $B = \begin{pmatrix} \sin \theta & 0 \\ 0 & \sin \theta \end{bmatrix}$ then show that $A^2 + B^2 = I$.

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11. If
$$A=egin{pmatrix}\cos heta&\sin heta\-\sin heta&\cos heta\end{pmatrix}$$
 prove that $orall^T=A$

12. Verify that
$$A^2=I$$
 when $A=egin{pmatrix} 5&-4\6&-5 \end{pmatrix}$



13. If
$$A = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$
 and $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ show that

$$A^2-(a+d)A=(bc-ad)I_2.$$

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14. If
$$A = \begin{bmatrix} 5 & 2 & 9 \\ 1 & 2 & 8 \end{bmatrix}, B = \begin{bmatrix} 1 & 7 \\ 1 & 2 \\ 5 & -1 \end{bmatrix}$$
 verify that

$$(AB)^T = B^T A^T.$$

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15. if
$$A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$
, show that $A^2 - 5A + 7I = 0$.

1. A system of three linear equations in three variables is inconsistent if their planes.

A. intersect only at a point

B. intersect in a line

C. coincides with each other

D. do not intersect

Answer:



2. The solution of the system

$$x + y - 3z = -6, -7y + 7z = 7, 3z = 9$$
 is
A. $x = 1, y = 2, z = 3$
B. $x = -1, y = 2, z = 3$
C. $x = -1, y = -2, z = 3$
D. $x = 1, y = 2, z = 3$

Answer:

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3. If (x-6) is the HCF of $x^2 - 2x - 24$ and $x^2 - kx - 6$ then the value of k is.

C. 6

D. 8

Answer:



4.
$$\frac{3y-3}{y} \div \frac{7y-7}{3y^2}$$
 is
A. $\frac{9y}{7}$
B. $\frac{9y^3}{21y-21}$
C. $\frac{21y^2-42y+21}{3y^3}$
D. $\frac{7y^2-2y+1}{y^2}$

Answer:

5.
$$y^2 + rac{1}{y^2}$$
 is not equal to
A. $rac{y^4+1}{y^2}$
B. $\left(y+rac{1}{y}
ight)^2$
C. $\left(y-rac{1}{y}
ight)^2+2$
D. $\left(y+rac{1}{y}
ight)^2-2$

Answer:

6.
$$rac{x}{x^2-25}-rac{8}{x^2+6x+5}$$
 gives
A. $rac{x^2-7x+40}{(x+5)(x-5)}$

B.
$$rac{x^2 - 7x + 40}{(x+5)(x-5)(x+1)}$$

C. $rac{x^2 - 7x + 40}{(x^2 - 25)(x+1)}$
D. $rac{x^2 + 10}{(x^2 - 25)(x+1)}$

Answer:



7. The square root of
$$\frac{256x^8y^4z^{10}}{25x^6y^6z^6}$$
 is equal to
A. $\frac{16}{5} \left| \frac{x^2z^4}{y^2} \right|$
B. $16 \left| \frac{y^2}{x^2z^4} \right|$
C. $\frac{16}{5} \left| \frac{y}{xz^3} \right|$
D. $\frac{16}{5} \left| \frac{xz^3}{y} \right|$

Answer:



D. None of these

Answer:



10. The values of a and b if $4x^4 - 24x^3 + 76x^2 + ax + b$ is a perfect square are

A. 100, 120

B. 10, 12

C. - 120, 100

D. 12, 10

Answer:



11. Graph of a linear polynomial is a

A. straight line

B. circle

C. parabola hyperbola

D. hyperbola

Answer:



12. The number of points of intersection of the quadratic polynomial $x^2 + 4x + 4$ with the X axis.

A. 0

B. 1

C.0 or 1

D. 2
Answer:





- A. $\Delta \times J$
- $\text{B.} 3\times 2$
- ${\sf C.3} imes 4$
- D. 4 imes 3

Answer:



14. If A is a 2 imes 3 matrix and B is 3 imes 4 matrix, how many columns

does AB have

A. 3 B. 4 C. 2

D. 5

Answer: 4



15. If number of columns and rows are not equal in a matrix then

it is said to be a

A. diagonal matrix

B. rectangular matrix

C. square matrix

D. identity matrix

Answer: rectangular matrix



16. Transpose of a columns matrix is

A. unit matrix

B. diagonal matrix

C. column matrix

D. row matrix

Answer:



17. Find the matrix X if $2X + \begin{bmatrix} 1 & 3 \\ 5 & 7 \end{bmatrix} = \begin{bmatrix} 5 & 7 \\ 9 & 5 \end{bmatrix}$

A.
$$\begin{pmatrix} -2 & -2 \\ 2 & -1 \end{pmatrix}$$

B.
$$\begin{pmatrix} 2 & 2 \\ 2 & -1 \end{pmatrix}$$

C.
$$\begin{pmatrix} 1 & 2 \\ 2 & 2 \end{pmatrix}$$

D.
$$\begin{pmatrix} 2 & 1 \\ 2 & 2 \end{pmatrix}$$

Answer:



18. Which of the following can be caluculated from the given

matrices

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}, B = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$
(i) A^2 (ii) B^2

(iii)AB (iv)BA

A. (i) and (ii) only

B. (ii) and (iii) only

C. (ii) and (iv) only

D. all of these

Answer: 3

19. If
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{bmatrix}$$
, $B = \begin{bmatrix} 1 & 0 \\ 2 & -1 \\ 0 & 2 \end{bmatrix}$ and $C = \begin{bmatrix} 0 & 1 \\ -2 & 5 \end{bmatrix}$
which of the following statements are correct? (i)

$$AB + C = \begin{bmatrix} 5 & 5\\ 5 & 5 \end{bmatrix}$$
(ii) $BC = \begin{bmatrix} 0 & 1\\ 2 & -3\\ -4 & 10 \end{bmatrix}$ (iii)
$$BA + C = \begin{bmatrix} 2 & 5\\ 3 & 0 \end{bmatrix}$$
(iv) $(AB)C = \begin{bmatrix} -8 & 20\\ -8 & 13 \end{bmatrix}$

A. (i) and (ii) only

B. (ii) and (iii) only

C. (ii) and (iv) only

D. all of these

Answer:



Unit Exercise 3

1. Solve
$$rac{1}{3}(x+y-5)=y-z=2x-11=9-(x+2z).$$

2. One hundred and fifty students are admitted to a school. They are distributed over three sections A, B, C. If 6 students are shifted from section A to Sections C, the students will have equal number of students. If 4 times of students of section C exceeds the number of students of setion A by the number of students in sectionB, find the number of students in the sections.

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3. In a three-digit number, when the tens and the hundreds digit are interchanged the new number is 54 more than three times the original number. If 198 is added three times the original number. If 198 is added to the number, the digits are reversed. The tests difit exceeds the hundreds digit by twice as that of the tens digit exceeds the unit digit. Find the original number.



6. Reduce the given Rational expression to its lowest form

 $\frac{x^{3a}-8}{x^{2a}+2x^a+4}$



7. Reduce the given Rational expression to its lowest form

$$rac{10x^3-25x^2+4x-10}{-4-10x^2}.$$

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8. Simplify
$$\frac{\frac{1}{p} + \frac{1}{q+r}}{\frac{1}{p} - \frac{1}{q+r}} \times \left[1 + \frac{q^2 + r^2 - p^2}{2pr}\right]$$
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9. Arul, Ravi, and Ram working together can clean a store in 6 hours. Working alone, Ravi takes twice as long to clean the store as Arul does. Ram needs three times as long as Arul does. How long would it take each if they are working alone?



12. A boat takes 1.6 hours longer to go 36kms up a river than down the river. If the speed of the water current is 4 km per hr, what is the speed of the boat in still water?



13. Is it possible to design a rectangular park of perimeter 320m and area $4800m^2$? If so find its length and breadth.



14. At t minutes past 2pm, the time needed to 3 pm is 3minutes less than $\frac{t^2}{4}$ find t.

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15. The number of seats in a row is equal to the total number of rows in a hall. The total number of seats in the hall will increase by 375 if the number of rows is doubled and the number of seats in each row is reduced by 5. Find the number of rows in the hall at the beginning.



16. If a and b are the roots of the polynomial $f(x) = x^2 - 2x + 3$, find the polynomial whose roots are `(alpha+2),(beta+2)'

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17. If a and b are the roots of the polynomial $f(x)=x^2-2x+3$, find the polynomial whose roots are $rac{lpha-1}{lpha+1},rac{eta-1}{eta+1}$

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18. If -4 is a root of the equation $x^2 + px - 4 = 0$ and if the equation $x^2 + px + q = 0$ are equal roots, find the values of p



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19. Two farmers and Ravi cultivates three varieties of grains namely rice, wheat and ragi. If the sale (in ₹) of three varieties of grains by both the farmers in the month of April is given by the matrix.

April sale in ₹ $A = \begin{bmatrix} rice & Wheat & ragi \\ 500 & 1000 & 1500 \\ 2500 & 1500 & 500 \end{bmatrix}$ Senthil
Ravi

and the May

month sale (in ₹) is exactly twice as that of the April month sale

for each variety.

What is the average sales of the months April and May.



20. Two farmers and Ravi cultivates three varieties of grains namely rice, wheat and ragi. If the sale (in ₹) of three varieties of grains by both the farmers in the month of April is given by the matrix.



and the May

month sale (in \mathbf{P}) is exactly twice as that of the April month sale for each variety.

If the sales continue to increase in the same way in the successive months, what will be sales in the month of August?



21. If
$$\cos \theta \begin{bmatrix} \cos theata & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} + \sin \theta \begin{bmatrix} x & -\cos \theta \\ \cos \theta & x \end{bmatrix} = I_2.$$

Find x.

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22. Given
$$A = \begin{bmatrix} p & 0 \\ 0 & 2 \end{bmatrix}$$
, $B = \begin{bmatrix} 0 & q \\ 1 & 0 \end{bmatrix}$, $C = \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$ and If $BA = C^2$, find p and q.

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23.
$$A = \begin{bmatrix} 3 & 0 \\ 4 & 5 \end{bmatrix}, B = \begin{bmatrix} 6 & 3 \\ 8 & 5 \end{bmatrix}, C = \begin{bmatrix} 3 & 6 \\ 1 & 1 \end{bmatrix}$$
 find the matrix D, such that $CD - AB = 0$.

1. Product of the roots of the quadratic equation $x^2 + 3x = 0$ is

A. X B. 3 C. 0 D. 1

Answer:

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2. The no-diagonal elements is any unit matrix are ____.

B. 1

C.0

D. n

Answer: C





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4. If $lpha \,$ and $\,eta$ are the roots of $x^2+6x-4=0$, find the value of

$$\left(lpha -eta
ight) ^{2}.$$



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6. If $lpha, eta$ are the roots of the equation $2x^2 - x - 1 = 0$ then form the equation whose roots are $lpha^2 eta$?
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7. Find two consecutive positive integers, sum of whose squares

is 365.

8. Solve the qudratic equation $5x^2 - 6x - 2 = 0$ by completing

the square method.

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9. Find the square root of the expressions

$$\frac{x^2}{y^2} - 10\frac{x}{y} + 27 - 10\frac{y}{x} + \frac{y^2}{x^2}$$
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10. If $9x^4 + 12x^3 + 28x^2 + ax + b$ is a perfect squares. Find the

value of a and b.

11. A motor boat whose speed is 18km/hr in still water takes 1hour more to go 24km upstream than to the return downstream to the same spot. Find the speed of the stream.

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12. Draw the graph $y = x^2 + x - 2$ $x^2 + x - 2 = 0.$	and	hence	solve
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Additional Questions Answers

1. Find the values of k for which the following equation has equal

to roots. (k-12)x² + 2(k-12)x+2=0

2. A chess board contains 64 equal squares and the area of each square is $6.25cm^2$. A border round the board is 2cm wide find its side.



3. Find the consecutive natural numbers whose product is 20.



4. Solve the following system of the linear equations in three varaibles.

$$x + y + z = 6, 2x + 3y + 4z = 20, 3x + 2y + 5z = 22$$

5. Using quadratic formula solve the following equations.

$$p^2x^2 + ig(p^2-q^2ig)x - q^2 = 0$$

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6. Using quadratic formula solve the following equations.

$$9x^2 - 9(a+b)x + \left(2a^2 + 5ab + 2b^2
ight) = 0$$

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7. Prove that the equation
$$x^2(a^2b^2)+2x(ac+bd)+(c^2+d^2)=0$$
 has no real root if $ad \neq bc.$

8. The sum of two numbers is 15. If the sum of their reciprocals is $\frac{3}{10}$, find the numbers.



9. A two digit numbers is such that the product of its digits is 12. When 36 is added to the number the digits interchange their places. Find the number.



10. Seven year ago, Varun's age was five times the square of swati's age. Three years hence Swati's age will be two fifth of Varun's age. Find their present ages.

11. A two digit number is such that the product of its digits is 18, When 63 is subtracted to the number the digits interchange their places. Find the number.

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Unit Test

1. A system of three linear equations in three variables is inconsistent if their planes.

A. intersect only at a point

B. intersect in a line

C. coincides with each other

D. do not intersect

Answer:

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2. The solution of
$$(2x-1)^2 = 9$$
 is equal to

 $\mathsf{A.}-1$

 $\mathsf{B.}\,2$

C. -1, 2

D. None of these

Answer: -1, 2



3. If number of columns and rows are not equal in a matrix then

it is said to be a

A. diagonal matrix

B. rectangular matrix

C. square matrix

D. identity matrix

Answer:

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4. Transpose of a columns matrix is

A. unit matrix

B. diagonal matrix

C. column matrix

D. row matrix

Answer: row matrix

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5. If (x-6) is the HCF of $x^2 - 2x - 24$ and $x^2 - kx - 6$ then the

value of k is.

A. 3

B. 5

C.6

D. 8

Answer:



6. There are 12 pieces of five, ten and twenty rupee currencies whose total value is ₹105. When first 2 sorts are interchanged in their numbers its value will be increased by ₹20. Find the number of currencies in each sort.



7. Iniya bought 50 kg of fruits consisting of apples and bananas. She paid twice as much per kg for the apple as she did for the banana. If Iniya bought ₹1800 worth of apples and ₹600 worth bananas, then how many kg of each fruits did she buy?



8. A ball rolls down a slope and travels a distance $d = t^2 - 0.75t$ feet in t seconds. Find the time when the distance traveled by the ball is 11.25feet.



9. A garden measuring 12m by 16m is to have wide installed all the way around so that it incease the total area of $285m^2$. What is the width of the pathway?

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10. Find the LCM of each pair of the following polynomials

 $a^2+4a-12, a^2-5a+6$ whose GCD is a-2

11. Find the square root of the following rational expressions.

 $\frac{400x^4y^{12}z^{16}}{100x^8y^4z^4}$



12. Find the square root of the following polynomials by division

method

 $x^4 - 12x^3 + 42x^2 - 36x + 9$



13. Find the square root of the following polynomials by division

method

$$37x^2 - 28x^3 + 4x^4 + 42x + 9$$

14. Find the square root of the following polynomials by division

method

 $16x^4 + 8x^2 + 1$

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15. Find the square root of the following polynomials by division

method

 $121x^4 - 198x^3 - 183x^2 + 216x + 144$

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16. Find the LCM and GCD for the following and verify that f(x) imes g(x)=LCM imes GCD $21x^2y, 35xy^2$



17. Find the LCM and GCD for the following and verify that f(x) imes g(x)=LCM imes GCD $ig(x^3-1ig)(x+1), x^3+1$



18. Find the LCM and GCD for the following and verify that f(x) imes g(x)=LCM imes GCD $ig(x^2y+xy^2ig), ig(x^2+xyig)$



19. Draw the graph of $y = x^2 - 4$ and hence solve $x^2 - x - 12 = 0.$

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20. Draw the graph of $y = x^2 + x$ and hence solve $x^2 + 1 = 0$.