



MATHS

BOOKS - KUMAR PRAKASHAN KENDRA MATHS (GUJRATI ENGLISH)

STRAIGHT LINES

Exercise 10 1

1. Draw a quadrilateral in the Cartesian plane, whose vertices are $(-4, 5)$, $(0, 7)$, $(5, -5)$ and $(-4, -2)$. Also, find its area.

 [Watch Video Solution](#)

2. The base of an equilateral triangle with side $2a$ lies along the Y-axis such that the mid-point of the base is at the origin. Find vertices of the

triangle.

 [Watch Video Solution](#)

3. Find the distance between $P(x_1, y_1)$ and $Q(x_2, y_2)$ when (i) PQ is parallel to the Y-axis (ii) PQ is parallel to the X-axis.

 [Watch Video Solution](#)

4. Find a point on the X-axis, which is equidistant from the points $(7, 6)$ and $(-3, 4)$.

 [Watch Video Solution](#)

5. Find the slope of a line, which passes through the origin, and the midpoint of the line segment joining the points $P(0, -4)$ and $B(8, 0)$.

 [Watch Video Solution](#)

6. Without using the Pythagoras theorem, show that the points $(4, 4)$, $(3, 5)$ and $(-1, -1)$ are the vertices of a right angled triangle.

 [Watch Video Solution](#)

7. Find the slope of the line, which makes an angle of 30° with the positive direction of Y-axis measured anticlockwise.

 [Watch Video Solution](#)

8. Find the value of x for which the points $(x, -1)$, $(2, 1)$ and $(4, 5)$ are collinear.

 [Watch Video Solution](#)

9. Without using distance formula, show that points $(-2, -1)$, $(4, 0)$, $(3, 3)$ and $(-3, 2)$ are the vertices of a

parallelogram.

 [Watch Video Solution](#)

10. Find the angle between the X-axis and the line joining the points $(3, -1)$ and $(4, -2)$.

 [Watch Video Solution](#)

11. The slope of a line is double of the slope of another line. If tangent of the angle between them is $\frac{1}{3}$, find the slopes of the lines.

 [Watch Video Solution](#)

12. A line passes through (x_1, y_1) and (h, k) . If slope of the line is m , show that, $k - y_1 = m(h - x_1)$.

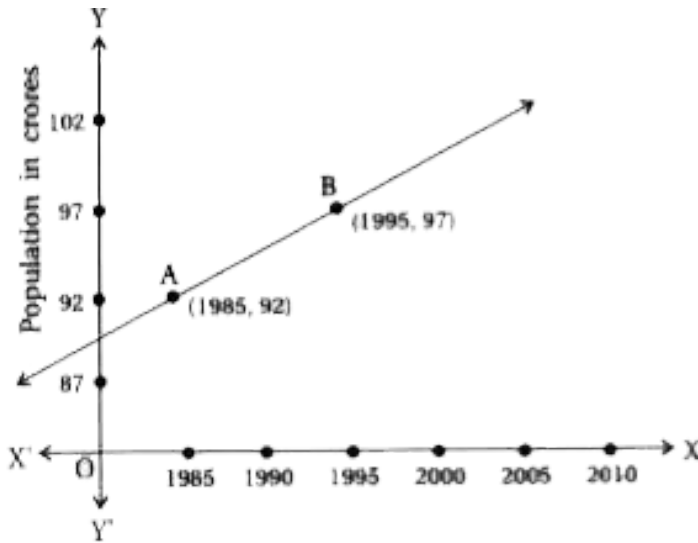
 [Watch Video Solution](#)

13. If three points $(h, 0)$, (a, b) and $(0, k)$ lie on a line, show that

$$\frac{a}{h} + \frac{b}{k} = 1.$$

 [Watch Video Solution](#)

14. Consider the following population and year graph, find the slope of the line AB and using it, find what will be the population in the year 2010?



 [Watch Video Solution](#)

1. Obtain Equation of line which satisfy given condition :

Write the equations for the X- and Y- axes.

 [Watch Video Solution](#)

2. Obtain Equation of line which satisfy given condition :

Passing through the point $(-4, 3)$ with slope $\frac{1}{2}$.

 [Watch Video Solution](#)

3. Obtain Equation of line which satisfy given condition :

Passing through $(0, 0)$ with slope m .

 [Watch Video Solution](#)

4. Obtain Equation of line which satisfy given condition :

Passing through $(2, 2\sqrt{3})$ and inclined with the X-axis at an angle of 75° .



 [Watch Video Solution](#)

5. Obtain Equation of line which satisfy given condition :

Intersecting the X -axis at a distance of 3 units to the left of origin with slope -2 .

 [Watch Video Solution](#)

6. Obtain Equation of line which satisfy given condition :

Intersecting the Y -axis at a distance of 2 units above the origin and making an angle of 30° with positive direction of the X -axis.

 [Watch Video Solution](#)

7. Obtain Equation of line which satisfy given condition :

Passing through the points $(-1, 1)$ and $(2, -4)$.

 [Watch Video Solution](#)

8. Obtain Equation of line which satisfy given condition :

Perpendicular distance from the origin is 5 units and the angle made by the perpendicular with the positive X -axis is 30° .



[Watch Video Solution](#)

9. The vertices of ΔPQR are $P(2, 1)$, $Q(-2, 3)$ and $R(4, 5)$. Find equation of the median through the vertex R.



[Watch Video Solution](#)

10. Find the equation of the line passing through $(-3, 5)$ and perpendicular to the line through the points $(2, 5)$ and $(-3, 6)$.



[Watch Video Solution](#)

11. A line perpendicular to the line segment joining the points $(1, 0)$ and $(2, 3)$ divides it in the ratio $1 : n$. Find the equation of the line.

 [Watch Video Solution](#)

12. Find the equation of a line that cuts off equal intercepts on the coordinate axes and passes through the point $(2, 3)$.

 [Watch Video Solution](#)

13. Find equation of the line passing through the point $(2, 2)$ and cutting off intercepts on the axes whose sum is 9.

 [Watch Video Solution](#)

14. Find equation of the line through the point $(0, 2)$ making an angle $\frac{2\pi}{3}$ with the positive X-axis. Also, find the equation of line parallel to it

and crossing the Y-axis at a distance of 2 units below the origin.



[Watch Video Solution](#)

15. The perpendicular from the origin to a line meets it at the point $(-2, 9)$, find the equation of the line.



[Watch Video Solution](#)

16. The length L (in centimetre) of a copper rod is a linear function of its Celsius temperature C . In an experiment, if $L = 124.942$ when $C = 20$ and $L = 125.134$ when $C = 110$, express L in terms of C .



[Watch Video Solution](#)

17. The owner of a milk store finds that, he can sell 980 litres of milk each week at Rs. 14/litre and 1220 litres of milk each week at Rs. 16/litre.

Assuming a linear relationship between selling price and demand, how many litres could he sell weekly at Rs. 17/litre ?

 [Watch Video Solution](#)

18. P (a, b) is the mid-point of a line segment between axes. Show that equation of the line is $\frac{x}{a} + \frac{y}{b} = 2$.

 [Watch Video Solution](#)

19. Point $R(h, k)$ divides a line segment between the axes in the ratio 1 : 2 . Find equation of the line.

 [Watch Video Solution](#)

20. By using the concept of equation of a line, prove that the three points $(3, 0)$, $(-2, -2)$ and $(8, 2)$ are collinear.

 [Watch Video Solution](#)

Exercise 10 3

1. Reduce the following equations into slope intercept form and find their slopes and the y- intercepts.

(i) $x + 7y = 0$



[Watch Video Solution](#)

2. Reduce the following equations into slope intercept form and find their slopes and the y- intercepts.

(ii) $6x + 3y - 5 = 0$



[Watch Video Solution](#)

3. Reduce the following equations into slope intercept form and find their slopes and the y- intercepts.

(iii) $y = 0$



[Watch Video Solution](#)

4. Reduce the following equations in intercept form and find their intercepts on axis.

(i) $3x + 2y - 12 = 0$



[Watch Video Solution](#)

5. Reduce the following equations in intercept form and find their intercepts on axis.

(ii) $4x - 3y = 6$



[Watch Video Solution](#)

6. Reduce the following equations in intercept form and find their intercepts on axis.

(iii) $3y + 2 = 0$



[Watch Video Solution](#)

7. Reduce the following equation in normal form. Find their perpendicular distances from origin and between perpendicular distance with positive side of X- axis :

(i) $x - \sqrt{3}y + 8 = 0$

[Watch Video Solution](#)

8. Reduce the following equation in normal form. Find their perpendicular distances from origin and between perpendicular distance with positive side of X- axis :

(ii) $y - 2 = 0$

[Watch Video Solution](#)

9. Reduce the following equation in normal form. Find their perpendicular distances from origin and between perpendicular distance with positive

side of X- axis :

(iii) $x - y = 4$

 [Watch Video Solution](#)

10. Find the distance of the point $(-1, 1)$ from the line $12(x + 6) = 5(y - 2)$.

 [Watch Video Solution](#)

11. Find the points on the X-axis, whose distances from the line $\frac{x}{3} + \frac{y}{5} = 1$ are 4 units.

 [Watch Video Solution](#)

12. Find the distance between following pair of parallel lines :

(i) $15x + 8y - 34 = 0$ and $15x + 8y + 31 = 0$

 [Watch Video Solution](#)

13. Find the distance between following pair of parallel lines :

(ii) $l(x + y) + p = 0$ and $l(x + y) - r = 0$



Watch Video Solution

14. Find equation of the line parallel to the line $3x - 4y + 2 = 0$ and passing through the point $(-2, 3)$.



Watch Video Solution

15. Find equation of the line perpendicular to the line $x - 7y + 5 = 0$ and having x intercept 3.



Watch Video Solution

16. Find angles between the lines $\sqrt{3}x + y = 1$ and $x + \sqrt{3}y = 1$.

 [Watch Video Solution](#)

17. The line through the points $(h, 3)$ and $(4, 1)$ intersects the line $7x - 9y - 17 = 0$ at right angle. Find the value of h .

 [Watch Video Solution](#)

18. Prove that the line through the point (x_1, y_1) and parallel to the line $Ax + By + C = 0$ is $A(x - x_1) + B(y - y_1) = 0$.

 [Watch Video Solution](#)

19. Two lines passing through the point $(2, 3)$ intersects each other at an angle of 60° . If slope of one line is 2, find equation of the other line.

 [Watch Video Solution](#)

20. Find the equation of the right bisector of the line segment joining the points $(3, 4)$ and $(-1, 2)$.

 [Watch Video Solution](#)

21. Find the coordinates of the foot of perpendicular from the point $(-1, 3)$ to the line $3x - 4y - 16 = 0$.

 [Watch Video Solution](#)

22. The perpendicular from the origin to the line $y = mx + c$ meets it at the point $(-1, 2)$. Find the values of m and c .

 [Watch Video Solution](#)

23. If p and q are the lengths of perpendiculars from the origin to the lines $x \cos \theta - y \sin \theta = k \cos 2\theta$ and $x \sec \theta + y \csc \theta = k$

respectively, prove that $p^2 + 4q^2 = k^2$.

 [Watch Video Solution](#)

24. In the triangle ABC with vertices $A(2, 3)$, $B(4, 1)$ and $C(1, 2)$, find the equation and length of altitude from the vertex A.

 [Watch Video Solution](#)

25. If p is the length of perpendicular from the origin to the line whose intercepts on the axes are a and b , then show that $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$.

 [Watch Video Solution](#)

Exercise 10 4

1. Find equation of line passes from point of intersection of $3x + 4y = 7$ and $x - y + 2 = 0$. whose slope is 5.



[Watch Video Solution](#)

2. Find equation of the line passes from point of intersection of lines $x + 2y - 3 = 0$ and $4x - y + 7 = 0$. Whose is parallel to line $5x + 4y - 20 = 0$.



[Watch Video Solution](#)

3. Find equation of line passes from point of intersection at lines $2x + 3y - 4 = 0$ and $x - 5y = 7$ whose x-intercept is -4 .



[Watch Video Solution](#)

4. Find equation of line passes from point of intersection at lines $5x - 3y = 1$ and $2x + 3y - 23 = 0$ and perpendicular to line $5x - 3y = 1$.



[Watch Video Solution](#)

Exercise 10 5

1. Find the new coordinates of the point in each of the following cases if origin is shifted to the point $(-3, -2)$ by translation of axes.

(i) $(1, 1)$



[Watch Video Solution](#)

2. Find the new coordinates of the point in each of the following cases if origin is shifted to the point $(-3, -2)$ by translation of axes.

(ii) $(0, 1)$



[Watch Video Solution](#)

3. Find the new coordinates of the point in each of the following cases if origin is shifted to the point $(-3, -2)$ by translation of axes.

(iii) $(5, 0)$



Watch Video Solution

4. Find the new coordinates of the point in each of the following cases if origin is shifted to the point $(-3, -2)$ by translation of axes.

(iv) $(-1, -2)$



Watch Video Solution

5. Find the new coordinates of the point in each of the following cases if origin is shifted to the point $(-3, -2)$ by translation of axes.

(v) $(3, -5)$



Watch Video Solution

6. Find what the following equation becomes when origin is shifted of the point $(1, 1)$.

(i) $x^2 + xy - 3y^2 - y + 2 = 0$



Watch Video Solution

 Watch Video Solution

7. Find what the following equation becomes when origin is shifted of the point $(1, 1)$.

(ii) $xy - y^2 - x + y = 0$

 Watch Video Solution

8. Find what the following equation becomes when origin is shifted of the point $(1, 1)$.

(iii) $xy - x - y + 1 = 0$

 Watch Video Solution

Miscellaneous Exercise 10

1. Find the values of k for which the line $(k - 3)x - (4 - k^2)y + k^2 - 7k + 6 = 0$ is

(i) Parallel to the x-axis

$$\text{Line } (k - 3)x - (4 - k^2)y + k^2 - 7k + 6 = 0.$$



[Watch Video Solution](#)

2. Find the values of k for which the line

$$(k - 3)x - (4 - k^2)y + k^2 - 7k + 6 = 0 \text{ is}$$

(ii) Parallel to the y-axis.



[Watch Video Solution](#)

3. Find the values of k for which the line

$$(k - 3)x - (4 - k^2)y + k^2 - 7k + 6 = 0 \text{ is}$$

(iii) Passing through the origin.



[Watch Video Solution](#)

4. Find the values of θ and p , if the equation $x \cos \theta + y \sin \theta = p$ is the normal form of the line $\sqrt{3}x + y + 2 = 0$.

 [Watch Video Solution](#)

5. Find the equations of the lines, which cut-off intercepts on the axes whose sum and product are 1 and -6 , respectively.

 [Watch Video Solution](#)

6. What are the points on the Y- axis whose distance from the line $\frac{x}{3} + \frac{y}{4} = 1$ is 4 units.

 [Watch Video Solution](#)

7. Find perpendicular distance from the origin to the line joining the points $(\cos \theta, \sin \theta)$ and $(\cos \phi, \sin \phi)$.



[Watch Video Solution](#)

8. Find the equation of the line parallel to Y-axis and drawn through the point of intersection of the lines $x - 7y + 5 = 0$ and $3x + y = 0$.



[Watch Video Solution](#)

9. Find the equation of a line drawn perpendicular to the line $\frac{x}{4} + \frac{y}{6} = 1$ through the point, where it meets the Y-axis.



[Watch Video Solution](#)

10. Find the area of the triangle formed by the lines $y - x = 0$, $x + y = 0$ and $x - k = 0$.



[Watch Video Solution](#)

11. Find the value of p so that the three lines $3x + y - 2 = 0$, $px + 2y - 3 = 0$ and $2x - y - 3 = 0$ may intersect at one point.



[Watch Video Solution](#)

12. If three lines whose equations are $y = m_1x + c_1$, $y = m_2x + c_2$ and $y = m_3x + c_3$ are concurrent, then show that $m_1(c_2 - c_3) + m_2(c_3 - c_1) + m_3(c_1 - c_2) = 0$.



[Watch Video Solution](#)

13. Find the equation of the lines through the point $(3, 2)$ which make an angle of 45° with the line $x - 2y = 3$.



[Watch Video Solution](#)

14. Find the equation of the line passing through the point of intersection of the lines $4x + 7y - 3 = 0$ and $2x - 3y + 1 = 0$ that has equal intercepts on the axes.

 [Watch Video Solution](#)

15. Show that the equation of the line passing through the origin and making an angle θ with the line $y = mx + c$ is $\frac{y}{x} = \frac{m \pm \tan \theta}{1 \pm m \tan \theta}$.

 [Watch Video Solution](#)

16. In what ratio, the line joining $(-1, 1)$ and $(5, 7)$ is divided by the line $x + y = 4$?

 [Watch Video Solution](#)

17. Find the distance of the line $4x + 7y + 5 = 0$ from the point $(1, 2)$ along the line $2x - y = 0$.



Watch Video Solution

18. Find the direction in which a straight line must be drawn through the point $(-1, 2)$. So that its point of intersection with the line $x + y = 4$ may be at a distance of 3 units from this point.



Watch Video Solution

19. The hypotenuse of a right angled triangle has its ends at the points $(1, 3)$ and $(-4, 1)$. Find an equation of the legs (perpendicular sides) of the triangle.



Watch Video Solution

20. Find the image of the point $(3, 8)$ with respect to the line $x + 3y = 7$ assuming the line to be a plane mirror.

 [Watch Video Solution](#)

21. If the lines $y = 3x + 1$ and $2y = x + 3$ are equally inclined to the line $y = mx + 4$, find the value of m .

 [Watch Video Solution](#)

22. If sum of the perpendicular distances of a variable point $P(x, y)$ from the lines $x + y - 5 = 0$ and $3x - 2y + 7 = 0$ is always 10. Show that P must move on a line.

 [Watch Video Solution](#)

23. Find equation of the line which is equidistant from parallel lines

$$9x + 6y - 7 = 0 \text{ and } 3x + 2y + 6 = 0.$$



Watch Video Solution

24. A ray of light passing through the point $(1, 2)$ reflects on the X-axis at point A and the reflected ray passes through the point $(5, 3)$. Find the coordinates of A.



Watch Video Solution

25. Prove that the product of the lengths of the perpendiculars drawn from the points $(\sqrt{a^2 - b^2}, 0)$ and $(-\sqrt{a^2 - b^2}, 0)$ to the line $\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1$ is b^2 .



Watch Video Solution

26. A person standing at the junction (crossing) of two straight paths represented by the equations $2x - 3y + 4 = 0$ and $3x + 4y - 5 = 0$ wants to reach the path whose equation is $6x - 7y + 8 = 0$ in the least time. Find equation of the path that he should follow.

 [Watch Video Solution](#)

Practice Work

1. Prove that $(0, -1)$, $(6, 7)$, $(-2, 3)$ and $(8, 3)$ are the vertices of a rectangle.

 [Watch Video Solution](#)

2. Find the area of the quadrilateral ABCD with vertices $A(1, 1)$, $B(7, -3)$, $C(12, 2)$ and $D(7, 21)$.

 [Watch Video Solution](#)

3. $A(6, 3)$, $B(-3, 5)$, $C(4, -2)$ and $D(x, 3x)$ are given points. Find x if $\frac{\text{Area at } \triangle DBC}{\text{Area at } \triangle ABC} = \frac{1}{2}$.

 [Watch Video Solution](#)

4. Find point on Y-axis which is at the equidistance from the given points $A(-4, 3)$ and $B(5, 2)$.

 [Watch Video Solution](#)

5. Find distance PQ between the points $P(a \cos \alpha, a \sin \alpha)$ and $Q(a \cos \beta, a \sin \beta)$.

 [Watch Video Solution](#)

6. Find x if the slope of the line passes from points $A(x, 2)$ and $B(6, -8)$ is $-\frac{5}{4}$.



[Watch Video Solution](#)

7. Without using Pythagoras theorem prove that $A(12, 8)$, $B(-2, 6)$ and $C(6, 0)$ are the vertices of right angled triangle.



[Watch Video Solution](#)

8. Using definition of slope prove that $P(4, 8)$, $Q(5, 12)$ and $R(9, 28)$ are collinear points.



[Watch Video Solution](#)

9. Find slope of the perpendicular line to the line passes from points $(0, 8)$ and $(-5, 2)$.



[Watch Video Solution](#)

10. Find y if the line passes from points $(3, y)$ and $(2, 7)$ is parallel to the line passes from points $(-1, 4)$ and $(0, 6)$.

 [Watch Video Solution](#)

11. Prove that line passes from the points $A(4, -6)$ and $B(-2, -5)$ makes obtuse angle with X-axis.

 [Watch Video Solution](#)

12. $A(-2, 1)$, $B(2, 3)$ and $C(-2, -4)$ are vertices of $\triangle ABC$. Find measure of $\angle B$.

 [Watch Video Solution](#)

13. Angle between two lines is 45° and slope of one line is 2 then find slope of second line.

 [Watch Video Solution](#)

14. $A(0, 2)$, $B(-2, -1)$, $C(4, 0)$ and $D(2, 3)$ are vertices of parallelogram ABCD. If angle between its diagonal is θ then prove that $\tan \theta = 3$.

 [Watch Video Solution](#)

15. Two lines pass through $(0, 0)$, $(2, 3)$ and $(2, -2)$, $(3, 5)$. Find measure of an angle between them.

 [Watch Video Solution](#)

16. Obtain the equation of the line which satisfying given condition :

(1) Passes from points $A(-1, 8)$ and $B(4, -2)$.

 [Watch Video Solution](#)

17. Obtain the equation of the line in Ex. (1) to (10) satisfying given condition :

Equation of perpendicular bisector of \overline{AB} joining $A(-2, 3)$ and $B(4, 5)$.

 [Watch Video Solution](#)

18. Obtain the equation of the line in Ex. (1) to (10) satisfying given condition :

Equation of the line whose X- intercept is 4 and slope $\frac{1}{2}$.

 [Watch Video Solution](#)

19. Obtain the equation of the line in Ex. (1) to (10) satisfying given condition :

Length of perpendicular from origin is 7 unit and slope -1 .

 [Watch Video Solution](#)

20. Obtain the equation of the line in Ex. (1) to (10) satisfying given condition :

Passes from point $(-4, 3)$ and parallel to Y-axis.



[Watch Video Solution](#)

21. Obtain the equation of the line in Ex. (1) to (10) satisfying given condition :

Equation of line with $p = 2$ and $\sin \theta = \frac{4}{5}$.



[Watch Video Solution](#)

22. Obtain the equation of the line in Ex. (1) to (10) satisfying given condition :

Passes from point $(1, -2)$ and makes equal intercepts on axes.



[Watch Video Solution](#)

23. Obtain the equation at the line in Ex. (1) to (10) satisfying given condition :

Equation of horizontal and vertical line passes from point $(-5, 6)$.

 [Watch Video Solution](#)

24. Obtain the equation at the line in Ex. (1) to (10) satisfying given condition :

Equation of line which is of the equidistance from the line $x = -2$ and $x = 6$.

 [Watch Video Solution](#)

25. Obtain the equation at the line in Ex. (1) to (10) satisfying given condition :

Length of perpendicular from origin is 7 unit and makes an angle $\frac{\pi}{6}$ with positive side of X-axis.

 [Watch Video Solution](#)

26. Prove that point $(4, 1)$ divides perpendicular line segment joining points $(6, 5)$ and $(2, -1)$ in ratio $8:5$ internally.

 [Watch Video Solution](#)

27. $A(5, 2)$, $B(2, 3)$ and $C(6, 5)$ are the vertices of $\triangle ABC$. Find equation of internal bisector of $\angle BAC$.

 [Watch Video Solution](#)

28. Find equation of line whose sum and product of intercepts on axis are 1 and -6 respectively.

 [Watch Video Solution](#)

29. Line makes right angled triangle with axis whose area is 6 unit and length of its hypoteneous is 5 unit. Find equation of line.

 [Watch Video Solution](#)

30. Find equation of line L whose length of perpendicular from origin is 2 unit with slope $\frac{5}{12}$.

 [Watch Video Solution](#)

31. In which ratio line $x + y = 4$ divides line segment joining points $(-1, 1)$ and $(5, 7)$?

 [Watch Video Solution](#)

32. Equation at sides of rectangle are $x = a, x = a', y = b$ and $y = b'$. Obtain equation of its diagonals.



Watch Video Solution

33. Find equation of line passes from point $P(1, -7)$ which intersects axis is at points A and B such that $4AP - 3BP = 0$.



Watch Video Solution

34. $A(1, 4)$, $B(2, -3)$ and $C(-1, -2)$ are the vertices at $\triangle ABC$ then find, (1) Equation of median from A. (2) Equation of perpendicular from A. (3) Equation of perpendicular bisector of \overline{BC} .



Watch Video Solution

35. Find the equation of line which makes a triangle with area $\frac{50}{\sqrt{3}}$ unit with axis and perpendicular from origin makes an angle $\frac{\pi}{6}$ with positive side of X-axis.



Watch Video Solution

36. A ray of light passing through the point $(1, 2)$ reflects on the X-axis at point A and the reflected ray passes through the point $(5, 3)$. Find the coordinates of A.



[Watch Video Solution](#)

37. Prove that line segment joining mid points of the two sides of the triangle is parallel to third side.



[Watch Video Solution](#)

38. The Fahrenheit temperature F and absolute temperature K satisfy a linear equation. Given that $K = 273$ when $F = 32$ and that $K = 373$ when $F = 212$.

Express K in terms of F and find the value of F , when $K = 0$.



[Watch Video Solution](#)

39. $L: 3x + 2y - 7 = 0$

(1) Reduce the above equation in slope intercept form. Find their slope and y -intercept.

(2) Reduce the equation into intercept form. Find their intercepts on axis.

(3) Reduce the equation in normal form and find perpendicular distance from origin and measure of an angle made by perpendicular with positive side of X -axis.

 [Watch Video Solution](#)

40. Find points on line $x + y + 3 = 0$ whose distance from line $x + 2y + 2 = 0$ is $\sqrt{5}$ unit.

 [Watch Video Solution](#)

41. Length of perpendicular from origin to the line $\frac{x}{a} + \frac{y}{b} = 1$ is p . If a^2, p^2 and b^2 are in A.P. then prove that $a^4 + b^4 = 0$.

 [Watch Video Solution](#)

42. Find perpendicular distance from point $(3, -1)$ to the line $12x - 5y - 7 = 0$.

 [Watch Video Solution](#)

43. If two sides of the quadrilateral are along the lines $x + 2y + 3 = 0$ and $x + 2y = 5$. Find its area.

 [View Text Solution](#)

44. Find equation of parallel line to line $2x + 3y + 11 = 0$ and whose sum of intercept is 15.

 [Watch Video Solution](#)

45. Find equation of line at the distance 3 from origin and perpendicular to the line $\sqrt{3}x - y + 5 = 0$.

 [Watch Video Solution](#)

46. Find equation of line whose y-intercept is $\frac{4}{3}$ and perpendicular to the line $3x - 4y + 11 = 0$.

 [Watch Video Solution](#)

47. Prove that lines $3x + y + 4 = 0$, $3x + 4y = 20$ and $24x - 7y + 5 = 0$ are sides of an equilateral triangle.

 [Watch Video Solution](#)

48. One side and are vertex of the equilateral triangle is $2x + 2y - 5 = 0$ and $(1, 2)$ respectively. Find equation of other sides.

 [Watch Video Solution](#)

49. Find equation of lines which bisects the quadrants.

 [Watch Video Solution](#)

50. Prove that the product of the lengths of the perpendiculars drawn from the points $(\sqrt{a^2 - b^2}, 0)$ and $(-\sqrt{a^2 - b^2}, 0)$ to the line $\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1$ is b^2 .

 [Watch Video Solution](#)

51. Find equation of line passes from middle of two parallel lines $9x + 6y - 7 = 0$ and $3x + 2y + 6 = 0$.



[Watch Video Solution](#)

52. Find length of perpendicular from origin to the lines passes from points $(\cos \theta, \sin \theta)$ and $(\cos \phi, \sin \phi)$.

[Watch Video Solution](#)

53. Find foot of perpendicular from point $(2, 3)$ on the line $x + y + 1 = 0$.

[Watch Video Solution](#)

54. Find the equation at line passes from point of intersection at lines $x + 2y = 5$ and $3x + 7y = 12$. which is perpendicular to line $3x + 4y = 10$.

[Watch Video Solution](#)

55. Find equation of line passes from point of intersection at lines $4x - 3y - 1 = 0$ and $2x - 5y + 3 = 0$ which makes equal angle with axis.



[Watch Video Solution](#)

56. Find equation of line passes from point of intersection at lines $x - y - 1 = 0$ and $2x - 3y + 1 = 0$. Which is (i) Parallel to X- axis. (ii) Parallel to Y- axis and (iii) Parallel to line $3x + 4y = 14$.



[Watch Video Solution](#)

57. If origin is shifted to point $(1, -2)$ then find the new transformed form of the following equation.

(i) $2x^2 + y^2 - 4x + 4y = 0$

(ii) $y^2 - 4x + 4y + 8 = 0$



[Watch Video Solution](#)

58. At which origin will be shifted so, that new coordinate at point $(4, 5)$ will be $(-3, 9)$?

 [Watch Video Solution](#)

59. On which point we shift origin so that new transformed form of the equation $y^2 + 4y + 8x - 2 = 0$ does not contain constant term and term does not contain y ?

 [Watch Video Solution](#)

60. Prove that area at triangle will remain same by shifting origin at any point.

 [Watch Video Solution](#)

61. By shifting origin at $(-2, 3)$ find new transformed form at the equation $y + 3x = 2$.



Watch Video Solution

62. Find equation of line passes from $(\sqrt{3}, -1)$ whose perpendicular distance is $\sqrt{2}$ from origin.



Watch Video Solution

63. Two opposite vertices of rectangle are $(-3, 1)$ and $(1, 1)$. Also equation of one side is along the line $4x + 7y + 5 = 0$. Find equation of other sides of rectangle.



Watch Video Solution

64. Lines $3x + 4y + 5 = 0$ and $4x - 3y - 10 = 0$ intersects at point A. B is the point on line $3x + 4y + 5 = 0$ and point C lies on line $4x - 3y - 10 = 0$. such that $AB = AC$. Find equation of \overleftrightarrow{BC} passes from point $(1, 2)$.



Watch Video Solution

 [View Text Solution](#)

65. Find image of point $(-8, 12)$ with respect to line $4x + 7y + 13 = 0$.

 [Watch Video Solution](#)

66. Two sides of the triangle are along the lines $3x - 2y + 6 = 0$ and $4x + 5y - 20 = 0$. If ortho centre of the triangle is $(1, 1)$. Find the equation of third side of the triangle.

 [Watch Video Solution](#)

67. $A(0, -1, -2)$, $B(3, 1, 4)$ and $C(5, 7, 1)$ are vertices of $\triangle ABD$ then find the measure of $\angle A$.

 [Watch Video Solution](#)

68. Point $(2, 1)$ has reflection as simple mirror $(5, 2)$. Find equation of line.

 [Watch Video Solution](#)

69. Base of the equilateral triangle is along the line $x + y - 2 = 0$ and its one vertex is $(2, -1)$. Find area of triangle.

 [Watch Video Solution](#)

70. Find equation of line passess from point $(2, 3)$ and cuts line segment of length $\frac{2\sqrt{2}}{3}$. between the lines $2x + y = 3$ and $2x + y = 5$.

 [View Text Solution](#)

71. Find equation of line whose sum and product of intercepts on axis are 7 and 12 respectively.

 [Watch Video Solution](#)

72. Without finding point of intersection obtain the equation of line passes from point of intersection of lines $5x + y + 4 = 0$ and $2x + 3y - 1 = 0$. which is parallel to the line $4x - 2y - 1 = 0$.

 [Watch Video Solution](#)

73. Two adjacent sides of the parallelogram are $4x + 5y = 0$ and $7x + 2y = 0$ one diagonal of the parallelogram is along line $11x + 7y = 9$. Then find equation of other diagonal.

 [Watch Video Solution](#)

74. If m_1 and m_2 are the roots of the equation $x^2 + (\sqrt{3} + 2)x + \sqrt{3} - 1 = 0$ then prove that area of the triangle formed by the lines $y = m_1x$, $y = m_2x$ and $y = c$ is $\frac{c^2}{4}(\sqrt{33} + \sqrt{11})$.



Watch Video Solution

75. Find distance from point $(3, 5)$ to the line $2x + 3y = 14$ and the distance to the line parallel to $x - 2y = 1$.



Watch Video Solution

76. If the lines $ax + y + 1 = 0$, $x + by + 1 = 0$ and $x + y + c = 0$ are concurrent then prove that,

$$\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = .$$



Watch Video Solution

Text Based Mcqs

1. is the equation of line passes from point $A\left(2, -\frac{3}{2}\right)$ and parallel to X- axis.

A. $x = 2$

B. $2x - 3 = 0$

C. $2y - 3 = 0$

D. $2y + 3 = 0$

Answer: D



Watch Video Solution

2. Line $x + y = 4$ divides \overline{AB} joining $A(-2, 3)$ and $B(1, 5)$ in ratio

1: λ from A then $\lambda = \dots\dots$

A. 3:2

B. 2:3

C. 1:3

D. -2:3

Answer: B

 [Watch Video Solution](#)

3. Perpendicular distance from origin to line $3x + 4y + 10 = 0$ is

A. -2

B. $\frac{2}{5}$

C. $\frac{1}{5}$

D. 2

Answer: D

 [Watch Video Solution](#)

4. $(1, 2), (2, 1), \left(\frac{3 + \sqrt{3}}{2}, \frac{3 + \sqrt{3}}{2} \right)$ are vertices of triangle. Then

distance between circumcentre and orthocentre is

A. 0

B. $\sqrt{2}$

C. $3 + \sqrt{3}$

D. None of these

Answer: A



Watch Video Solution

5. Two medians are drawn from the vertices of an acute angles of the isosceles right angled triangle then angle between them is

A. $\cos^{-1} \left(\frac{2}{3} \right)$

B. $\cos^{-1} \left(\frac{3}{4} \right)$

C. $\cos^{-1} \left(\frac{4}{5} \right)$

D. $\cos^{-1} \left(\frac{5}{6} \right)$

Answer: C



Watch Video Solution

6. is the y intercept of the line passes from point $(2, 2)$ and perpendicular to $3x + y = 3$.

A. $\frac{1}{3}$

B. $\frac{2}{3}$

C. 1

D. $\frac{4}{3}$

Answer: D



Watch Video Solution

7. Area of the triangle with vertices $(-4, 1)$, $(1, 2)$ and $(4, -3)$ is

A. 17

B. 16

C. 15

D. None of these

Answer: A



[Watch Video Solution](#)

8. In ratio Y -axis divides line segment joining points $(-3, -4)$ and $(1, -2)$.

A. 1:3

B. 2:3

C. 3:1

D. 3:2

Answer: C



[Watch Video Solution](#)

9. P_1 and P_2 are the length of perpendicular from origin to the line $x \sec \theta + y \csc \theta = a$ and $x \cos \theta - y \sin \theta = a \cos 2\theta$ then of the

following is valid.

A. $4P_1^2 + P_2^2 = a^2$

B. $P_1^2 + 4P_2^2 = a^2$

C. $P_1^2 + P_2^2 = a^2$

D. None of these

Answer: A



Watch Video Solution

10. If $a + b + c = 0$ then line $3ax + by + c = 0$ passes fromof the following point.

A. $\left(2, \frac{2}{3}\right)$

B. $\left(\frac{2}{3}, 2\right)$

C. $\left(-2, \frac{2}{3}\right)$

D. None of these

Answer: B



[Watch Video Solution](#)

11. Lines $ax \pm by \pm c = 0$ represents of the following.

A. Rectangle

B. Square

C. Rhombus

D. None of these

Answer: C



[Watch Video Solution](#)

12. $(5, 2)$ is the mid point of the line segment intercepted between axes then equation of line is.....

A. $5x + 2y = 20$

B. $2x + 5y = 20$

C. $5x - 2y = 20$

D. $2x - 5y = 20$

Answer: B

 [Watch Video Solution](#)

13. $P - \alpha$ form of the line $x + \sqrt{3}y - 4 = 0$ is.....

A. $x \frac{\cos(\pi)}{6} + y \frac{\sin(\pi)}{6} = 2$

B. $x \frac{\cos(\pi)}{3} + y \frac{\sin(\pi)}{3} = 2$

C. $x \cos\left(-\frac{\pi}{3}\right) + y \sin\left(-\frac{\pi}{3}\right) = 2$

D. $x \cos\left(-\frac{\pi}{6}\right) + y \sin\left(-\frac{\pi}{6}\right) = 2$

Answer: B

 [Watch Video Solution](#)

14. If the lines $x \cos \alpha + y \sin \alpha = P$ and $x - \sqrt{3}y + 1 = 0$ are mutually perpendicular then $\alpha = \dots\dots$

A. $\frac{\pi}{2}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{3}$

D. $\frac{\pi}{3}$

Answer: C



[Watch Video Solution](#)

15. Perpendicular distance between

$3x + 4y - 5 = 0$ and $6x + 8y - 15 = 0$ is

A. 1

B. $\frac{1}{2}$

C. $\frac{22}{10}$

D. 2

Answer: B



Watch Video Solution

16. Lines $3x + 4y = 5$, $5x + 4y = 4$ and $\lambda x + 4y = 6$ passes from unique point then value of $\lambda = \dots$

A. 2

B. 1

C. 3

D. 4

Answer: B



Watch Video Solution

17. $(2, 7)$ is the centroid of the triangle with vertices $(4, 8)$ and $(-2, 6)$
then its third vertex is

A. $(0, 0)$

B. $(4, 7)$

C. $(7, 4)$

D. $(7, 7)$

Answer: B



[Watch Video Solution](#)

18. $A(0, b)$, $B(0, 0)$ and $C(a, 0)$ are vertices of $\triangle ABC$. If the medians \overline{AD} and \overline{BE} are mutually perpendicular then of the following is true.

A. $a = \frac{b}{2}$

B. $b = \frac{a}{2}$

C. $ab = 1$

$$D. a = \pm \sqrt{2b}$$

Answer: D



Watch Video Solution

19. is the foot of perpendicular from point $(-2, 3)$ to the line $2x - y - 3 = 0$.

A. $(-2, 3)$

B. $(2, 1)$

C. $(3, 2)$

D. $(1, 2)$

Answer: B



Watch Video Solution

20. of the following is the line joining the point of intersection $y - x + 7 = 0$ and $y + 2x - 2 = 0$ and origin.

A. $3x + 3y = 0$

B. $3x - 4y = 0$

C. $4x - 3y = 0$

D. $4x + 3y = 0$

Answer: D



[Watch Video Solution](#)

21. Angle between the intersecting lines

$2x - y + 3 = 0$ and $x + 2y + 3 = 0$.

A. 90°

B. 60°

C. 45°

D. 30°

Answer: A



[Watch Video Solution](#)

22. Is the line passes from point $(1, 2)$ and perpendicular to the line $x + y + 7 = 0$.

A. $x + y + 3 = 0$

B. $x - y + 1 = 0$

C. $y - x + 1 = 0$

D. $2x - y = 0$

Answer: B



[Watch Video Solution](#)

23. Lines $ax + by = c$ and $a'x + b'y = c'$ are mutually perpendicular then of the following is valid.

A. $aa' = 1$

B. $aa' + 1 = 0$

C. $aa' - 1 = 0$

D. $ab' + a'b = 0$

Answer: B



Watch Video Solution

24. Angle between the lines $\frac{x}{a} + \frac{y}{b} = 1$ and $\frac{x}{a} - \frac{y}{b} = 1$ is

A. $\tan^{-1} \left(\frac{2ab}{a^2 - b^2} \right)$

B. $\tan^{-1} \left(\frac{2ab}{a^2 + b^2} \right)$

C. $\tan^{-1} \left(\frac{a + b}{a - b} \right)$

D. $\tan^{-1} \left(\frac{2ab}{a + b} \right)$

Answer: A



Watch Video Solution

25. If the lines $mx + (2m + 3)y + m + 6 = 0$ and $(2m + 1)x + (m - 1)y + m - 9 = 0$ intersects on Y-axis then $m = \dots\dots$

A. -1 OR 21

B. 1 OR 21

C. -1 OR -21

D. $-\frac{1}{2}$ OR $-\frac{3}{2}$

Answer: D



Watch Video Solution

1. Line passess from fixed point $(2, 3)$ intersects axis of points P and Q. If

O is origin and OPRQ will be rectangle then locus of point R is

A. $3x + 2y = 6$

B. $2x + 3y = xy$

C. $3x + 2y = xy$

D. $3x + 2y = 6xy$

Answer: C



[Watch Video Solution](#)

Textbook Illustrations For Practice Work

1. Find the slope of the lines :

(a) Passing through the points $(3, -2)$ and $(-1, 4)$,



[Watch Video Solution](#)

2. Find the slope of the lines :

(b) Passing through the points $(3, -2)$ and $(7, -2)$,

 [Watch Video Solution](#)

3. Find the slope of the lines :

(c) Passing through the points $(3, -2)$ and $(3, 4)$,

 [Watch Video Solution](#)

4. Find the slope of the lines :

(d) Making inclination of 60° with the positive direction of x-axis.

 [Watch Video Solution](#)

5. If the angle between two lines is $\frac{\pi}{4}$ and slope of one of the lines is $\frac{1}{2}$,

find the slope of the other line.



[Watch Video Solution](#)

6. Line through the points $(-2, 6)$ and $(4, 8)$ is perpendicular to the line through the points $(8, 12)$ and $(x, 24)$. Find the value of x .



[Watch Video Solution](#)

7. Three points $P(h, k)$, $Q(x_1, y_1)$ and $R(x_2, y_2)$ lie on a line. Show that,
 $(h - x_1)(y_2 - y_1) = (k - y_1)(x_2 - x_1)$.

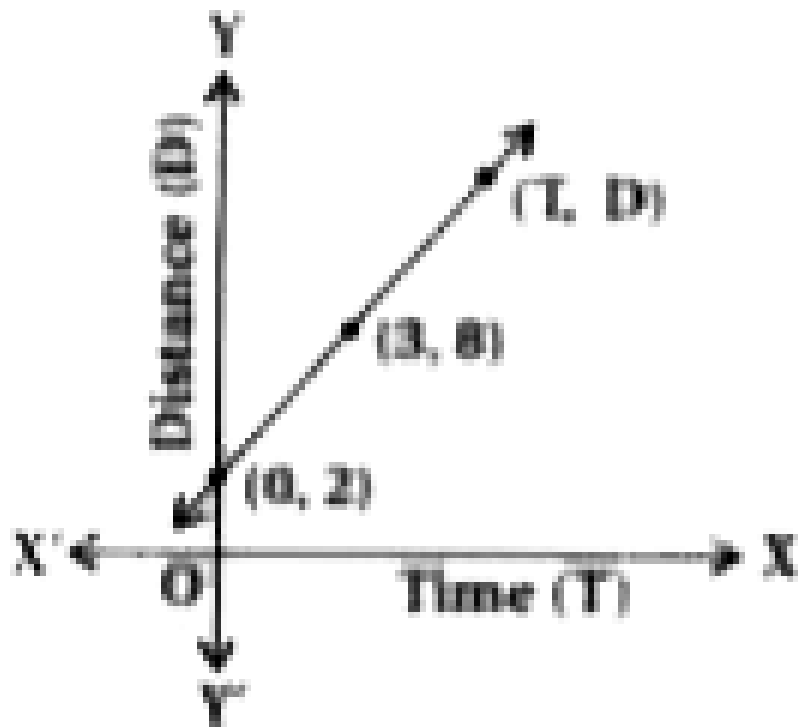


[Watch Video Solution](#)

8. In Figure, time and distance graph of a linear motion is given.

Two positions of time and distance are recorded as, when $T = 0$, $D = 2$ and when $T = 3$, $D = 8$. Using the concept of slope, find law of motion,

i.e., how distance depends upon time.



[▶ Watch Video Solution](#)

9. Find the equations of the lines parallel to axes and passing through $(-2, 3)$.

[▶ Watch Video Solution](#)

10. Find the equation of the line through $(-2, 3)$ with slope -4 .

 [Watch Video Solution](#)

11. Write the equation of the line through the points $(1, -1)$ and $(3, 5)$.

 [Watch Video Solution](#)

12. Write the equation of the lines for which $\tan \theta = \frac{1}{2}$, where θ is the

(i) y-intercept is $= -\frac{3}{2}$

 [Watch Video Solution](#)

13. Write the equation of the lines for which $\tan \theta = \frac{1}{2}$, where θ is the

(ii) x intercept is $= 4$.

 [Watch Video Solution](#)

14. Find the equation of the line, which makes intercepts -3 and 2 on the x – and y – axes respectively.



[Watch Video Solution](#)

15. Find the equation of the line whose perpendicular distance from the origin is 4 units and the angle which the normal makes with positive direction of x -axis is 15° .



[Watch Video Solution](#)

16. The fahrenheit temperature F and absolute temperature K satisfy the linear equation. Given that $K = 273$ when $F = 32$ and that $K = 373$ when $F = 212$. Express K in terms of F also find value of F when $K = 0$.



[Watch Video Solution](#)

17. Equation of a line is $3x - 4y + 10 = 0$. Find its

(i) slope,

 [Watch Video Solution](#)

18. Equation of a line is $3x - 4y + 10 = 0$. Find its

(ii) x -intercepts and y -intercepts.

 [Watch Video Solution](#)

19. Reduce the equation $\sqrt{3}x + y - 8 = 0$ into normal form. Find the value of p and ω .

 [Watch Video Solution](#)

20. Find the angle between the lines

$y - \sqrt{3}x - 5 = 0$ and $\sqrt{3}y - x + 6 = 0$.





Watch Video Solution

21. Show that two lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$,

where $b_1, b_2 \neq 0$ are

(i) Parallel if $\frac{a_1}{b_1} = \frac{a_2}{b_2}$ and



Watch Video Solution

22. Show that two lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$,

where $b_1, b_2 \neq 0$ are Perpendicular if $a_1a_2 + b_1b_2 = 0$.



Watch Video Solution

23. Find the equation of a line perpendicular to the line $x - 2y + 3 = 0$

and passing through the point $(1, -2)$.



Watch Video Solution

24. Find the distance of the point $(3, -5)$ from the line $3x - 4y - 26 = 0$.

 [Watch Video Solution](#)

25. Find the distance between the parallel lines $3x - 4y + 7 = 0$ and $3x - 4y + 5 = 0$.

 [Watch Video Solution](#)

26. Find the equation of line parallel to the Y-axis and drawn through the point of intersection of $x - 7 + 5 = 0$ and $3x + y - 7 = 0$.

 [Watch Video Solution](#)

27. Find the new coordinates of point $(3, -4)$ if the origin is shifted to $(1, 2)$ by a translation.

 [Watch Video Solution](#)

28. Find the transformed equation of the straight line $2x - 3y + 5 = 0$, when the origin is shifted to the point $(3, -1)$ after translation of axes.

 [Watch Video Solution](#)

29. If the lines $2x + y - 3 = 0$, $5x + ky - 3 = 0$ and $3x - y - 2 = 0$ are concurrent, find the value of k .

 [Watch Video Solution](#)

30. Find the distance of the line $4x - y = 0$ from the point $P(4, 1)$ measured along the line making an angle of 135° with the positive x -axis.

 [Watch Video Solution](#)

31. Assuming that straight lines work as the plane mirror for a point, find the image of the point $(1, 2)$ in the line $x - 3y + 4 = 0$.

 [Watch Video Solution](#)

32. Show that the area of the triangle formed by the lines $y = m_1x + c_1$, $y = m_2x + c_2$ and $x = 0$ is $\frac{(c_1 - c_2)^2}{2|m_1 - m_2|}$.

 [Watch Video Solution](#)

33. A line is such that its segment between the lines $5x - y + 4 = 0$ and $3x + 4y - 4 = 0$ is bisected at the point $(1, 5)$. Obtain its equation.

 [Watch Video Solution](#)

34. Show that the path of a moving point such that its distances from two lines $3x - 2y = 5$ and $3x + 2y = 5$ are equal is a straight line.

 [Watch Video Solution](#)

Solutions Of Ncert Exemplar Problems Short Answer Type Questions

1. Find the equation of the straight line which passes through the point $(1, -2)$ and cuts off equal intercepts from axes.

 [Watch Video Solution](#)

2. Find the equation of the line passing through the point $(5, 2)$ and perpendicular to the line segment joining the points $(2, 3)$ and $(3, -1)$.

 [Watch Video Solution](#)

3. Find the angle between the lines

$$l_1: y = (2 - \sqrt{3})(x + 5) \text{ and}$$

$$l_2: y = (2 + \sqrt{3})(x - 7).$$

Thinking Process : If the angle between the lines having the slope

m_1 and m_2 is θ then $\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$. Use this formula to solve the

above problem.



[Watch Video Solution](#)

4. Find the equation of the lines which passes through the point (3, 4)

and cuts off intercepts from the coordinate axes such that their sum is

14.



[Watch Video Solution](#)

5. Find the points on the line $x + y = 4$ which lie at a unit distance from

the line $4x + 3y = 10$.



[Watch Video Solution](#)

6. Show that the tangent of an angle between the lines

$$\frac{x}{a} + \frac{y}{b} = 1 \text{ and } \frac{x}{a} - \frac{y}{b} = 1 \text{ is } \frac{2ab}{a^2 - b^2}.$$



[Watch Video Solution](#)

7. Find the equation of lines passing through $(1, 2)$ and making angle 30° with Y- axis.

Thinking Process : Equation of a line passing through the point (x_1, y_1) and having slope m is $y - y_1 = m(x - x_1)$.



[Watch Video Solution](#)

8. Find the equation of the line passing through the point of intersection of $2x + y = 5$ and $x + 3y + 8 = 0$ and parallel to the line $3x + 4y = 7$.

Thinking Process : First find point of intersection of given lines and take slope m of intersection of given lines and take slope m of $y - y_1 = m(x - x_1)$.



[Watch Video Solution](#)

9. For what values of a and b the intercepts cut off on the coordinate axes by the line $ax + by + 8 = 0$ are equal in length but opposite in signs to those cut off by the line $2x - 3y + 6 = 0$ on the axes?



[Watch Video Solution](#)

10. If the intercept of a line between the coordinate axes is divided by the point $(-5, 4)$ in the ratio $1:2$, then find the equation of the line.

Thinking Process : Coordinates of the point which divides line segment

joining (x_1, y_1) and (x_2, y_2) in ratio

$$(m_1 : m_2) \left(\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right).$$



[Watch Video Solution](#)

11. Find the equation of a straight line on which length of perpendicular from the origin is four units and the line makes an angle of 120° with the positive direction of X -axis.

Thinking Process : Equation of line which makes an angle α with positive side of X axis and whose length of perpendicular from origin p is given by

$$x \cos \alpha + y \sin \alpha = p.$$



[Watch Video Solution](#)

12. Find the equation of one of the sides of an isosceles right angled triangle whose hypotenuse is given by $3x + 4y = 4$ and the opposite vertex of the hypotenuse is $(2, 2)$.



[Watch Video Solution](#)

1. If the equation of the base of an equilateral triangle is $x + y = 2$ and the vertex is $(2, -1)$, then find the length of the side of the triangle.

 [Watch Video Solution](#)

2. A variable line passes through a fixed point P. The algebraic sum of the perpendiculars drawn from the points $(2, 0)$, $(0, 2)$ and $(1, 1)$ on the line is zero. Find the coordinates of the point P.

 [Watch Video Solution](#)

3. In what direction should a line be drawn through the point $(1, 2)$ so that its point of intersection with the line $x + y = 4$ is at a distance $\frac{\sqrt{6}}{3}$ from the given point ?

 [Watch Video Solution](#)

4. A straight line moves so that the sum of the reciprocals of its intercepts made on axes is constant. Show that the line passes through a fixed point.

Thinking Process : For line which makes intercepts on axis $\frac{x}{a} + \frac{y}{b} = 1$ If

$\frac{1}{a} + \frac{1}{b} = \text{constant} \left(\frac{1}{k} \right)$ then $\frac{k}{a} + \frac{k}{b} = 1$ and we say it passes through point (k, k) .



[Watch Video Solution](#)

5. Find the equation of the line which passes through the point $(-4, 3)$ and the portion of the line intercepted between the axes is divided internally in the ratio 5:3 by this point.



[Watch Video Solution](#)

6. Find the equations of the lines through the point of intersection of the lines $x - y + 1 = 0$ and $2x - 3y + 5 = 0$ and whose distance from the point $(3, 2)$ is $\frac{7}{5}$.



Watch Video Solution

7. If the sum of the distances of a moving point in a plane from the axes is 1, then find the locus of the point.

Thinking Process : Given that $|x| + |y| = 1$ which gives four sides of a square.



Watch Video Solution

8. P_1, P_2 are points on either of the two lines $y - \sqrt{3}|x| = 2$ at a distance of 5 units from their point of intersection. Find the coordinates of the foot of perpendiculars drawn from P_1, P_2 on the bisector of the angle between the given lines.

Thinking Process : Here, equation $y - \sqrt{3}|x| = 2$ represents two different lines for $x > 0$ and $x < 0$ and they are bisector of Y -axis.

P_1 and P_2 are points at a distance 5 unit from point of intersection. The y coordinate of the foot of perpendicular on Y-axis is $2 + 5 \cos(30^\circ)$.



Watch Video Solution

9. If p is the length of perpendicular from the origin on the line

$$\frac{x}{a} + \frac{y}{b} = 1 \text{ and } a^2, p^2 \text{ and } b^2 \text{ are in A.P., then show that } a^4 + b^4 = 0.$$

 [Watch Video Solution](#)

Solutions Of Ncert Exemplar Problems Objective Type Questions

1. A line cutting off intercept -3 from the Y-axis and the tangent at angle to the X-axis is $\frac{3}{5}$, its equation is,

A. $5y - 3x + 15 = 0$

B. $3y - 5x + 15 = 0$

C. $5y - 3x - 15 = 0$

D. None of these

Answer: A

 [Watch Video Solution](#)

2. Slope of a line which cuts off intercepts of equal lengths on the axes is

.....

A. -1

B. 0

C. 2

D. $\sqrt{3}$

Answer: A



Watch Video Solution

3. The equation of the straight line passing through the point $(3, 2)$ and perpendicular to the line $y = x$ is,

A. $x - y = 5$

B. $x + y = 5$

C. $x + y = 1$

D. $x - y = 1$

Answer: B



Watch Video Solution

4. The equation of the line passing through the point $(1, 2)$ and perpendicular to the line $x + y + 1 = 0$ is

A. $y - x + 1 = 0$

B. $y - x - 1 = 0$

C. $y - x + 2 = 0$

D. $y - x - 2 = 0$

Answer: B



Watch Video Solution

5. The tangent of angle between the lines whose intercepts on the axes are a , $-b$ and b , $-a$, respectively, is

A. $\frac{a^2 - b^2}{ab}$

B. $\frac{b^2 - a^2}{2}$

C. $\frac{b^2 - a^2}{2ab}$

D. None of these

Answer: C



Watch Video Solution

6. If the line $\frac{x}{a} + \frac{y}{b} =$ passes through the points $(2, -3)$ and $(4, -5)$ then (a, b) is

A. $(1, 1)$

B. $(-1, 1)$

C. $(1, -1)$

D. $(-1, -1)$

Answer: D



[Watch Video Solution](#)

7. The distance of the point of intersection of the lines $2x - 3y + 5 = 0$ and $3x + 4y = 0$ from the line $5x - 2y = 0$ is

A. $\frac{130}{17\sqrt{29}}$

B. $\frac{13}{7\sqrt{29}}$

C. $\frac{130}{7}$

D. None of these

Answer: A



[Watch Video Solution](#)

8. The equations of the lines which pass through the point $(3, -2)$ and are inclined at 60° to the line $\sqrt{3}x + y = 1$ is

A. $y + 2 = 0, \sqrt{3}x - y - 2 - 3\sqrt{3} = 0$

B. $x - 2 = 0, \sqrt{3}x - y + 2 + 3\sqrt{3} = 0$

C. $\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$

D. None of these

Answer: D



Watch Video Solution

9. The equations of the lines passing through the point $(1, 0)$ and at a distance $\frac{\sqrt{3}}{2}$ from the origin, are

A. $\sqrt{3}x + y - \sqrt{3} = 0, \sqrt{3}x - y - \sqrt{3} = 0$

B. $\sqrt{3}x + y + \sqrt{3} = 0, \sqrt{3}x - y + \sqrt{3} = 0$

C. $x + \sqrt{3}y - \sqrt{3} = 0, \sqrt{3}y - \sqrt{3} = 0$

D. None of these

Answer: A



Watch Video Solution

10. The distance between the lines $y = mx + c_1$ and $y = mx + c_2$ is

A. $\frac{c_1 - c_2}{\sqrt{m^2 + 1}}$

B. $\frac{|c_1 - c_2|}{\sqrt{1 + m^2}}$

C. $\frac{|c_1 - c_2|}{\sqrt{1 + m^2}}$

D. 0

Answer: B



Watch Video Solution

11. The coordinates of the foot of perpendiculars from the point $(2, 3)$ on the line $y = 3x + 4$ is given by,

A. $\left(\frac{37}{10}, \frac{-1}{10}\right)$

B. $\left(-\frac{1}{10}, \frac{37}{10}\right)$

C. $\left(\frac{10}{37}, -10\right)$

D. $\left(\frac{2}{3}, -\frac{1}{3}\right)$

Answer: B



[Watch Video Solution](#)

12. If the coordinates of the middle point of the portion of a line intercepted between the coordinate axes is $(3, 2)$, then the equation of the line will be

A. $2x + 3y = 12$

B. $3x + 2y = 12$

C. $4x - 3y = 12$

D. $5x - 2y = 10$

Answer: A



Watch Video Solution

13. Equation of the line passing through $(1, 2)$ and parallel to the line $y = 3x - 1$ is

A. $y + 2 = x + 1$

B. $y + 2 = 3(x + 1)$

C. $y - 2 = 3(x - 1)$

D. $y - 2 = x - 1$

Answer: C



Watch Video Solution

14. Equations of diagonals of the square formed by the lines $x = 0, y = 0, x = 1$ and $y = 1$ are

A. $y = x, y + x = 1$

B. $y = x, x + y = 2$

C. $2y = x, y + x = \frac{1}{3}$

D. $y = 2x, y + 2x = 1$

Answer: A



[Watch Video Solution](#)

15. For specifying a straight line, how many geometrical parameters should be known ?

A. 1

B. 2

C. 4

D. 3

Answer: B



[Watch Video Solution](#)

16. The point $(4, 1)$ undergoes the following two successive transformations :

(i) Reflection about the line $y = x$

(ii) Translation through a distance 2 units along the positive X -axis

Then the final coordinates of the point are

A. $(4, 3)$

B. $(3, 4)$

C. $(1, 4)$

D. $\left(\frac{7}{2}, \frac{7}{2}\right)$

Answer: B



[Watch Video Solution](#)

17. A point equidistant from the lines

$4x + 3y + 10 = 0$, $5x - 12y + 26 = 0$ and $7x + 24y - 50 = 0$ is,

A. $(1, -1)$

B. $(1, 1)$

C. $(0, 0)$

D. $(0, 1)$

Answer: C



[Watch Video Solution](#)

18. A line passes through $(2, 2)$ and is perpendicular to the line

$3x + y = 3$. Its y-intercept is

A. $\frac{1}{3}$

B. $\frac{2}{3}$

C. 1

D. $\frac{4}{3}$

Answer: D



[Watch Video Solution](#)

19. The ratio in which the line $3x + 4y + 2 = 0$ divides the distance between the lines $3x + 4y + 5 = 0$ and $3x + 4y - 5 = 0$ is

A. 1 : 2

B. 3 : 7

C. 2 : 3

D. 2 : 5

Answer: B



[Watch Video Solution](#)

20. One vertex of the equilateral triangle with centroid at the origin and one side as $x + y - 2 = 0$ is

A. $(-1, -1)$

B. $(2, 2)$

C. $(-2, -2)$

D. $(2, -2)$

Answer: C



[Watch Video Solution](#)

Solutions Of Ncert Exemplar Problems Fillers

1. If a, b and c are in AP then the straight lines $ax + by + c = 0$ will always pass through.



[Watch Video Solution](#)

2. The line which cuts off equal intercept from the axes and pass through the point $(1, -2)$ is

 [Watch Video Solution](#)

3. Equations of the lines through the point $(3, 2)$ and making an angle of 45° with the line $x - 2y + 3 = 0$ are

 [Watch Video Solution](#)

4. The points $(3, 4)$ and $(2, -6)$ are situated on the of the line $3x - 4y - 8 = 0$.

 [Watch Video Solution](#)

5. A point moves so that square of its distance from the point $(3, -2)$ is numerically equal to its distance from the line $5x - 12y = 3$. The

equation of its locus is

 [Watch Video Solution](#)

6. Locus of the mid-points of the portion of the line $x \sin \theta + y \cos \theta = p$ intercepted between the axes is.....

 [Watch Video Solution](#)

7. If the vertices of a triangle have integral coordinates, then the triangle can not be equilateral.

 [Watch Video Solution](#)

8. The points $A(-2, 1)$, $B(0, 5)$, $C(-1, 2)$ are collinear.

 [Watch Video Solution](#)

9. Equation of the line passing through the point $(a \cos^3 \theta, a \sin^3 \theta)$ and perpendicular to the line $x \sec \theta + y \csc \theta = a$ is $x \cos \theta - y \sin \theta = \cos 2\theta$.

 [Watch Video Solution](#)

10. The straight line $5x + 4y = 0$ passes through the point of intersection of the straight lines $x + 2y - 10 = 0$ and $2x + y + 5 = 0$. True or False.

 [Watch Video Solution](#)

11. The vertex of an equilateral triangle is $(2, 3)$ and the equation of the opposite side is $x + y = 2$. Then the other two sides are $y - 3 = (2 \pm \sqrt{3})(x - 2)$.

 [Watch Video Solution](#)

12. The equation of the line joining the point $\{3, 5\}$ to the point of intersection of the lines $4x + y - 1 = 0$ and $7x - 3y - 35 = 0$ is equidistant from the points $(0, 0)$ and $(8, 34)$.

 [Watch Video Solution](#)

13. The line $\frac{x}{a} + \frac{y}{b} = 1$ moves in such a way that $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c^2}$, where c is a constant. The locus of the foot of the perpendicular from the origin on the given line is $x^2 + y^2 = c^2$

 [Watch Video Solution](#)

14. The lines $ax + 2y + 1 = 0$, $bx + 3y + 1 = 0$ and $cx + 4y + 1 = 0$ are concurrent if a, b, c are in A.P.

 [Watch Video Solution](#)

15. Line joining the points $(3, -4)$ and $(-2, 6)$ is perpendicular to the line joining the points $(-3, 6)$ and $(9, -18)$.



[Watch Video Solution](#)

Solutions Of Ncert Exemplar Problems Matching The Columns

1. Match Column - I and Column - II.

Column - I

- (i) The coordinates of the points P and Q on the line $x + 5y = 13$ which are
- (ii) The coordinates of the point on the line $x + y = 4$, which are at a unit d
- (iii) The coordinates of the point on the line joining A(-2, 5) and B(3, 1) su



[View Text Solution](#)

2. The value of the λ , if the lines $(2x + 3y + 4) + \lambda(6x - y + 14) = 0$ are

Column - I

(i) Parallel to Y -axis is

(ii) Perpendicular to $7x + y - 4 = 0$ is

(iii) Passes through (1, 2) is

(iv) parallel to X -axis is

Column - II

(a) $\lambda = \frac{-3}{4}$

(b) $\lambda = \frac{-1}{3}$

(c) $\lambda = \frac{-17}{41}$

(d) $\lambda = 3$



Watch Video Solution

3. The equation of the line through the intersection of the lines

$2x - 3y = 0$ and $4x - 5y = 2$ and

Column - I

(i) through the point (2, 1) is

(ii) perpendicular to the line $x + 2y + 1 = 0$ is

(iii) parallel to the line $3x - 4y + 5 = 0$ is

(iv) equally inclined to the axis is

Column - II

(a) $(2x - y = 4)$

(b) $x + y - 5 = 0$

(c) $x - y - 1 = 0$

(d) $3x - 4y - 1 = 0$



Watch Video Solution

Question Of Module Knowledge Test

1. Find distance between the points $A(3, 4)$ and $B(-4, 3)$.



Watch Video Solution

2. Obtain co-ordinates of mid-point of \overline{AB} joining $A(1, 2)$, $B(7, 8)$.

 [Watch Video Solution](#)

3. Find area of triangle with vertices $A(2, 3)$, $B(-1, 4)$ and $C(-2, -1)$.

 [Watch Video Solution](#)

4. Find slope of \overline{AB} joining points $A(4, 5)$, $B(-3, 4)$.

 [Watch Video Solution](#)

5. If line makes an angle of 45° with the positive side of X-axis then write its slope.

 [Watch Video Solution](#)

6. If line makes an angle 45° with X -axis then write its slopes.

 [Watch Video Solution](#)

7. Find measure of an angle between the lines $x + y = 3$ and $2x + 5y - 7 = 0$.

 [Watch Video Solution](#)

8. Find measure of an angle between the lines $x = 3$ and $2x - y - 5 = 0$

 [Watch Video Solution](#)

9. Y intercept of line $24x - 10 = 0$ is

 [Watch Video Solution](#)

10. is equation of line with slope $-\sqrt{3}$ and X- intercept 5.

 [Watch Video Solution](#)

11. Y-intercept of line $y = 0$ is

 [Watch Video Solution](#)

12. Find a if line $(a + 1)x + (a^2 + a - 2)y + a = 0$ is parallel to Y-axis.

 [Watch Video Solution](#)

13. Find k if lines $5x - ky - 7 = 0$ and $2x + 3y + 5 = 0$ are mutually perpendicular.

 [Watch Video Solution](#)

14. Find equation of line passes from points $(5, 6)$ and $(-3, 6)$.

 [Watch Video Solution](#)

15. Find P and α by converting equation $x + y = 1$ in $x \cos \alpha + y \sin \alpha = P$ form.

 [Watch Video Solution](#)

16. Find perpendicular distance from point $(2, 3)$ to the line $3x + 4y - 5 = 0$.

 [Watch Video Solution](#)

17. Find perpendicular distance between the lines $3x - 4y + 7 = 0$ and $6x - 8y + 1 = 0$.

 [Watch Video Solution](#)

18. Find k if the perpendicular distance between lines $5x + 12y = 1$ and $5x + 12y + k = 0$ is 25 unit.



[Watch Video Solution](#)