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## MATHS

## BOOKS - KAPLAN INC MATHS

## (ENGLISH)

## EXPONENTS, RADICALS,

## POLYNOMIALS, AND RATIONAL

## EXPRESSIONS

1. Which expression is equivalent to
$2\left(-4 j^{3} k^{-4}\right)^{-3} ?$

$$
\begin{aligned}
& \text { A. }-\frac{k^{12}}{512 j^{9}} \\
& \text { B. }-\frac{k\left({ }^{\wedge} 12\right)}{32 j^{9}} \\
& \text { C. }-\frac{j^{9}}{32 j^{9}} \\
& \text { D. }-\frac{k^{12}}{128 j^{9}}
\end{aligned}
$$

Answer: B
2. $T=2 \pi \sqrt{\frac{L}{g}}$

The formula above was created by Italian scientist Galileo Galilei in the early 1600s to demonstrate that the time it takes for a pendulum to complete a swing-called its period, T-can be found using only the length of the pendulum, L, and the force of gravity, $g$ He proved that the mass of the pendulum did not affect its period. Based on the equation
above, which of the following equations could be used to find the length of the pendulum given its period?
A. $L=\frac{g T}{2 \pi}$
B. $L=\frac{g T^{2}}{4 \pi^{2}}$
C. $L=\frac{T^{2}}{4 \pi^{2} g}$
D. $L=\frac{g}{4 \pi^{2} T^{2}}$

Answer: B

## D Watch Video Solution

3. Which of the following represents $\frac{\sqrt[6]{x^{10} y^{12}}}{\sqrt[3]{x^{5} y^{6}}}$
written in simplest from, given that
A. 1
B. 2
C. $x^{2} y^{3} \sqrt{x}$
D. $x y^{2} \sqrt[3]{x^{2}}$

Answer: A
4. What is the result when $4 x^{3}-5 x^{2}+x-3$
is divided by $x-2$ ?

$$
\begin{aligned}
& \text { A. } 4 x+3+\frac{11}{x-2} \\
& \text { B. } 4 x^{2}+3 x-6 \\
& \text { C. } 4 x^{2}+3 x+18 \\
& \text { D. } 4 x^{2}+3 x+7+\frac{11}{x-2}
\end{aligned}
$$

## Answer: D

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5. The function $f$ is a parabolic function that intersects the $x$-axis. Which of the following statements must be true?
A. The function has at least one real root.
B. The function has no real roots.
C. The function intersects the positive $y$
axis.
D. The function has two zeros.

Answer: A
6.
$a x^{4}+b x^{3}+c x^{2}-d x=0, a, b, c$ and $d$ are constants. If the equations crosses the $x$-axis at $0,-2,3$, and 5 which of the following is
a factor of $a x^{4}+b x^{3}+c x^{2}-d x$ ?
A. $x-2$
B. $x+3$
C. $x-5$
D. $x+5$

## Answer: C

## D Watch Video Solution

7. $\frac{8 x}{3(x-5)}+\frac{2 x}{3 x-15}=\frac{50}{3(x-5)}$

What value (s) of $x$ satisfy the equation above
?
A. 0
B. 5
C. No solution
D. Any value such that $x \neq 5$

## Answer: C

## D Watch Video Solution

8. 

$\frac{6}{2 x-3}+6 a=\frac{10}{2 x-3}+4 b$ and $3 a-2 b=2$,
what is the value of $x$ ?
A. $\frac{1}{2}$
B. 2
C. No solution
D. The value cannot be determined from
the information given.

Answer: B

- Watch Video Solution


## Try On Your Own

1. What is the vlaue of $\frac{3^{5} \times 27^{3}}{81^{3}}$ ?
2. $\frac{18 x^{4}+27 x^{3}-36 x^{2}}{9 x^{2}}$ If $x \neq 0$, which of the following is equivalent to the expression above?
A. $2 x^{2}+3 x-4$
B. $2 x^{2}+3 x-6$
C. $2 x^{4}+3 x^{3}-4 x^{2}$
D. $2 x^{6}+3 x^{5}-4 x^{4}$

## - Watch Video Solution

3. Human blood contains three primary cell types: red blood cells (RBC), white blood cells (WBC), and platelets. In an adult male, a single microliter $\left(1 \times 10^{-3}\right.$ milliliters) of blood contains approximately
$5.4 \times 10^{6} R B C, 7.5 \times 10^{3} \mathrm{WBC}$, and $3.5 \times 10^{5}$
platelets on average. What percentage of an adult male's total blood cell count is compresed of red blood cells ?
A. $1.30 \%$
B. $6.21 \%$
C. $60.79 \%$
D. $93.79 \%$

Answer: D

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4. If $n^{3}=-8$, what is the value of $\frac{\left(n^{2}\right)^{3}}{\frac{1}{n^{2}}}$ ?
5. If $r+s=6$, what is the value of t in the equation above?
A. 6
B. 12
C. 18
D. 30

Answer: B

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6. What do you need to do before squaring both sides ?

For what value of $x$ is the equation above true ?
A. -10
B. -2
C. 19
D. No solution

Answer: A
7. $3 x=x+14$
$\sqrt{3 z^{2}-11}+2 x=22$
If $z>0$, what is the value of $z$ ?
A. 1
B. 3
C. 5
D. 8

Answer: C
8. Which of the following expressions is equivalent to $-x^{\frac{1}{4}}$ ?

$$
\begin{aligned}
& \text { A. }-\frac{1}{4 x} \\
& \text { B. }-\frac{1}{x^{4}} \\
& \text { C. }-\sqrt[4]{x} \\
& \text { D. } \frac{1}{\sqrt[4]{-x}}
\end{aligned}
$$

## Answer: C

# 9. When simplified, $8^{\frac{4}{3}}$ is what number ? 

## - Watch Video Solution

10. $\sqrt{3 a+16}-3=a-1$

In the equation above, if $a>0$, which of the
following is a possible value of $a$ ?
A. 3
B. 2
C. 1
D. -4

Answer: A

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11. What is the sum of the polynomials

$$
6 a^{2}-17 a-9 \text { and }-5 a^{2}+8 a-2 ?
$$

A. $a^{2}-9 a-11$
B. $a^{2}-25 a-7$
C. $11 a^{2}-9 a-11$
D. $11 a^{2}-25 a-7$

Answer: A

## D Watch Video Solution

12. What is the difference when $3 x^{3}+7 x-5$ is subtracted from $8 x^{2}+4 x+10 ?$

$$
\begin{aligned}
& \text { A. } 5 x^{2}-3 x+15 \\
& \text { B. }-3 x^{3}-3 x+5
\end{aligned}
$$

$$
\text { C. } 3 x^{3}-8 x^{2}+3 x-15
$$

$$
\text { D. }-3 x^{3}+8 x^{2}-3 x+15
$$

## Answer: D

## - Watch Video Solution

13. 

$A=4 x^{2}+7 x-1$ and $B=-x^{2}-5 x+3$,
then what is $\frac{3}{2} A-2 B$ ?
A. $4 x^{2}+\frac{31}{2} x-\frac{9}{2}$
B. $4 x^{2}+\frac{41}{2} x-\frac{15}{2}$
C. $8 x^{2}+\frac{31}{2} x-\frac{9}{2}$
D. $8 x^{2}+\frac{41}{2} x-\frac{15}{2}$

## Answer: D

## - Watch Video Solution

14. If $x^{3}-9 x=9-x^{2}$, which of the following CANNOT be the value of $x$ ?
A. -3
B. -1
C. 1
D. 3

## Answer: C

## D Watch Video Solution

15. 

$\left(2 x^{2}+3 x-4\right)(3 x+2)=6 x^{3}+a x^{2}-6 x-8$
In the above equation, $a$ is a constant. If the
equation is true for all value of $x$, what is the

## value of a ?

A. 4
B. 9
C. 13
D. 16

Answer: C
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16. Which of the following is equivalent to $\frac{2 a^{2}-5 a-1}{a-3}$ ?
A. $2 a-2$
B. $2 a+1-\frac{2}{a-3}$
C. $2 a+\frac{2}{a-3}$
D. $2 a+1+\frac{2}{a-3}$

Answer: D

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17. $\frac{6 x^{2}+19 x+10}{2 x+5}$

If $a x+b$ represents the simplified from of the expression above, then what is the value of $a+b$ ?
A. 2
B. 3
C. 5
D. 6

Answer: C
18. Which of the following is equivalent to
$\frac{4 x^{2}-6 x}{2 x+2} ?$

$$
\begin{aligned}
& \text { A. } 2 x-\frac{10}{2 x+2} \\
& \text { B. } 2 x-5+\frac{10}{2 x+2} \\
& \text { C. } 2 x-3 \\
& \text { D. } 2 x+5-\frac{10}{2 x+2}
\end{aligned}
$$

Answer: B

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19.

The
equation
$\frac{36^{2}+16 x-21}{t x-4}=-9 x+5-\frac{1}{t x-4}$
true for all values of x for which $x \neq \frac{4}{t}$, where $t$ is a constant. What is the value of $t$ ?
A. -20
B. -4
C. 4
D. 12

Answer: B
20. If the polynomial $f(x)$ is evently divisible by
$x-5$ and the polynomial $g(x)=f(x)+4$, what is the value of $g(5) ?$
A. -4
B. 0
C. 4
D. 9
21. If function $f$ has exactly two distinct real zeros, which of the following graphs could be the complete graph of $f(x)$ ?
A.
B.
c.
D.

## - Watch Video Solution

22. The graph of $f(x)=-(x-3)^{2}+9$ above approximates the trajectory of a water bolloon shot from a cannon at ground level. In terms of the trajectory what information is represented by a root of this runction?
A. The maximum height achieved by the ballloon.
B. The total horizontal distance traveled by
the balloon.
C. The maximum speed of the balloon.
D. The initial acceleration of the balloon.

## Answer: B

## D Watch Video Solution

23. The manager of a health club determines
that the club's membership has increased at a
rate of 16 percent per year for the past four
years. The club currently has 42 members. If
this trend continues, how many years will it take for the club's membership to exceed 100 membgers ?
A. 4 years
B. 5 years
C. 6 years
D. 7 years

## Answer: C

24. Radioactive carbon dating can determine how long ago an organism lived by measuring how much of thte ${ }^{14} C$ in the sample has decayed. ${ }^{14} C$ is an isotope of carbon that has
a half-life of 5,600 years. Half-life is the amount of time it takes for half of the original amount to decay. If a sample of a petrified tree contains 6.25 percent of its original ${ }^{14} C$, how long ago did the tree die?
A. 22,400 years
B. 28,000 years
C. 35,000 years
D. 89,600 years

## Answer: A

## D Watch Video Solution

25. Penelope receives the same amount of money each month for her allowance. Each month she spends half of her allowance and puts the rest in a piggy bank. On penelope's

8th birthday, the piggy bank contains $\$ 40$. If the piggy bank contains $\$ 244$ after 2 years, what is her monthly allowance? (Ignore the dollar sign when gridding your response.)

## - Watch Video Solution

26. At a certain bank, month held in account $X$
earns a monthly interest equal to 2 percent of
the original investment, while account $Y$ earns
a monthly interest equal to 2 reprecent of the
current value of the account. If $\$ 500$ is
invested into each account, what is the positive difference between the value of account $X$ and account $Y$ after three years ?
(Round you answer to the nearest dollar and ignore the dollar sign when gridding you response.)

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27. Given the equation $\frac{6}{x}=\frac{3}{k+2}$ and the constraints $x \neq 0$ and $k \neq-2$, what is x in terms of k ?
A. $x=2 k+4$
B. $x=2 k+12$
C. $x=2 k-\frac{1}{4}$
D. $x=\frac{1}{4} k+12$

Answer: A

## D Watch Video Solution

28. $\frac{3 a+9}{(a-3)^{2}}+\frac{-9}{3 a-9}$

In the expression above, $(a-3)^{2}=6$. What
is the value of the expression?

## D Watch Video Solution

29. If $a>6$, which of the following is
equivalent to $\frac{\frac{2}{a}}{\frac{1}{a-2}+\frac{1}{a-6}}$ ?
A. $2 a^{2}-16 a+24$
B. $a(2 a-8)$
C. $\frac{a^{2}-8 a+12}{a^{2}-4 a}$
D. $\frac{2 a-80}{a^{2}-8 a+12}$

## Answer: C

## D Watch Video Solution

30. If $\frac{5}{x+2}=\frac{2}{x+1}+\frac{1}{2}$ and $x>1$, what is the value of $x$ ?
A. 2
B. 3
C. 6
D. 9

Answer: B

## D Watch Video Solution

31. If $\frac{16}{7 x+4}+A$ is equivalent to $\frac{49 x^{2}}{7 x+4}$, what is $A$ in terms of $x$ ?
A. $7 x+4$
B. $7 x-4$
C. $49 x^{2}$
D. $49 x^{2}+4$

Answer: B

## D Watch Video Solution

32. $\frac{c+5}{6 c}+\frac{2}{2 c-4}=0$

The equation above is true for all values of $c$
such that $c \neq-6$ and $c \neq 2$. if $c<0$, what is the value of $c$ ?
A. -20
B. -10
C. 1

## D. 10

## Answer: B

## D Watch Video Solution

33. The expression $\frac{3 x-1}{x-4}$ is equivalent to which of the following ?

$$
\begin{aligned}
& \text { A. } \frac{1}{2} \\
& \text { B. } 3 x-\frac{1}{x-4} \\
& \text { С. } 3-\frac{11}{x-4}
\end{aligned}
$$

$$
\text { D. } 3+\frac{11}{x-4}
$$

## Answer: D

## D Watch Video Solution

34. An object lauched upwards at an angle has
parabolic motion. The height $h$, of a projectile
at time $t$ is given by the equation $h=\frac{1}{2} a t^{2}+v_{y} t+h_{0}, \quad$ where $\quad \mathrm{a}$ is the acceleration due to gravity, $v_{v}$ is the vertical component of the velocity, and $h_{0}$ is the initial
height. Which of the following equations correctly represents the object's acceleration due to gravity in terms of the other variables?

$$
\begin{aligned}
& \text { A. } a=\frac{h-v_{v} t-h_{0}}{t} \\
& \text { B. } a=\frac{h-v_{v} t-h_{0}}{2 t^{2}} \\
& \text { C. } a=\frac{2\left(h-v_{v} t-h_{0}\right)}{t^{2}} \\
& \text { D. } a=t \sqrt{2\left(h-v_{v} t-h_{0}\right)}
\end{aligned}
$$

Answer: C

## D Watch Video Solution

35. If $\left(16^{3 x}\right)\left(32^{x}\right)\left(8^{3 x}\right)=\frac{\left(4^{6 x}\right)\left(32^{3 x}\right)}{4}$, then what is the value of $x$ ?
A. -2
B. -1
C. 1
D. 2

Answer: D

D Watch Video Solution
36.

Given
that
$\frac{y}{\sqrt{x}-3}=\frac{\sqrt{x}+3}{3}$ and $2 x+42=9 x-63$, what is the value of $y$ ?

## - Watch Video Solution

37. $y=\frac{3 x^{2}+7}{x-3}$

Which of the following expressions is
equivalent to $y$ ?

$$
\text { A. } 3 x+9-\frac{20}{x-3}
$$

$$
\text { B. } 3 x+9+\frac{34}{x-3}
$$

C. $3 x+43$
D. $3 x^{2}+\frac{9}{x-3}$

Answer: B

## D Watch Video Solution

38. $z=15 x^{2}+10 x y-6 x-4 y$

For which of the ordered pairs, $(x, y)$, below is
$z \neq 0 ?$
A. $(-3,2)$
B. $(-2,3)$
C. $\left(\frac{2}{5}, 0\right)$
D. $\left(\frac{2}{5}, 10\right)$

Answer: A

## D Watch Video Solution

39. $\sqrt{27^{\frac{2}{3}}+128^{\frac{4}{7}}}=$

- Watch Video Solution

40. Which of the following is equivalent to
$\frac{4 x^{2}-8}{2 x+3} ?$
A. $2 x-3+\frac{1}{2 x+3}$
B. $2 x-2$
C. $2 x+3-\frac{1}{2 x+3}$
D. $2 x+4$

Answer: A
( Watch Video Solution
41. $g(x) \frac{2}{2 x^{3}-12 x^{2}-14 x}$

For Which of the following values of x is the function $\mathrm{g}(\mathrm{x})$ dewfined ?
A. -1
B. 0
C. 1
D. 7

## Answer: C

## - Watch Video Solution

42. $x^{3}+4=3 x^{2}-7 x+25$

For what real value of $x$ is the above equation
valid ?
A. 0
B. 3
C. 4
D. 7

Answer: B

D Watch Video Solution
43. Which of the following equations has a graph for which all roots are greater than 0 ?

$$
\begin{aligned}
& \text { A. } y=4|x| \\
& \text { B. } y=x^{2}-4 \\
& \text { C. } y=(x-2)^{2} \\
& \text { D. } y=x(x-2)^{2}
\end{aligned}
$$

Answer: C

## - Watch Video Solution

44. A marketing team conducted a study on
the use of smartphones. In a certain metropolitan area, there were 1.6 million smartphone users at the end of 2018. The marketing team predicted that the number of smartphone users would increase by 35 percent each year beginning in 2019. If $y$ represents the number of smartphone users in this metropolitan area after x years, then which of the following equations best models the number of smartphone users in this area over time?
А. $y=1,600,000(1.35)^{x}$
B. $y=1,600,000(35)^{x}$
C. $y=35+1,600,000$
D. $y=1.35 x+1,600,000$

Answer: A

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## Exponents

1. The expression $x\left(x^{3} y^{2}\right)^{-4}$ is equivalent to which of the following

> A. $\frac{1}{y^{2}}$
> B. $\frac{1}{x^{4}}$
> C. $\frac{1}{x^{11} y^{8}}$
> D. $\frac{1}{x^{16} y^{8}}$

Answer: C

## D Watch Video Solution

1. If $-2 x^{2}+5 x-8$ is multiplied by $4 x-9$, what is the coefficient of $x$ in the resulting polynomial?
A. -77
B. -45
C. -32
D. -13

## Polynomial Division

1. Which of the following is equivalent to

$$
\frac{x^{2}+3 x+7}{x+4} ?
$$

A. $\frac{3+7}{4}$
B. $x+\frac{3}{4}$
C. $3+\frac{7}{x+4}$
D. $x-1+\frac{11}{x+4}$

## Answer: D

## D View Text Solution

## Modeling Growth And Decay

1. A certain car costs $\$ 20,000$. If the car loses

15 percent of its value each year, approximately how much will the car be worth after 5 years?
A. $\$ 5,000$
B. $\$ 8,900$
C. $\$ 11,200$
D. $\$ 15,000$

Answer: B
( Watch Video Solution

Rational Expressions And Equations

1. $\frac{5 y+7}{(y+4)^{2}}-\frac{5}{(y+4)}$
if the expression above the equal to $-b$
$\frac{-b}{(y+4)^{2}}$, where b is a positive constatn and $(y+4)^{2}$,
$y \neq-4$, what is the value of b ?
A. 4
B. 7
C. 13
D. 27

Answer: C

