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## MATHS

## BOOKS - KAPLAN INC MATHS (ENGLISH)

## LINEAR EQUATIONS AND GRAPHS

How Much Do You Know

1. Uniform cicular motion is used in physics to
describe the motion of an object traveling at a
constant speed in a circle. The speed of the object is called tangential velocity and it can be calculated using the formula abovce, where $r$ is the radius of the circle and $T$ is the time is
takes for the object to make one complete circle, called a peroid. WHich of the following formulas could be used to find the length of one period if you know the tengential velocity and the radius of the circle?

$$
\begin{aligned}
\text { A. } T & =\frac{v}{2 \pi r} \\
\text { B. } T & =\frac{2 \pi r}{v}
\end{aligned}
$$

$$
\text { C. } T=2 \pi r v
$$

$$
\text { D. } T=\frac{1}{2 \pi r v}
$$

## Answer: B

## - Watch Video Solution

2. The formula above is Newton's law of
universal gratitation, where $F$ is the attractive
force, $\gamma$ is the gravitational constnat, $m_{1}$ and $m_{2}$ are the masses of the particles, and $r$ is the distnace between their centres of
mass. Which of the following givers $r$ in terms of $F, \gamma, m_{1}, \quad$ and $m_{2}$ ?

$$
\begin{aligned}
& \text { A. } r=\sqrt{\frac{\left(m_{1}\right)\left(m_{2}\right)}{\gamma\left(m_{2}\right)}} \\
& \text { B. } r=\sqrt{\frac{F\left(m_{2}\right)}{\gamma\left(m_{1}\right)}} \\
& \text { C. } r=\sqrt{\frac{\gamma\left(m_{2}\right)}{F\left(m_{1}\right)}} \\
& \text { D. } r=\sqrt{\frac{\gamma\left(m_{1}\right)\left(m_{2}\right)}{F}}
\end{aligned}
$$

Answer: D

## D Watch Video Solution

3. Andrew rorks at a trabvel agency. He gets
paid $\$ 120$ for a day's work, plus a bonus of $\$ 25$
for each cruise he books. Which of the following equations represents the relationship between the total Andrew earns in a day, d, and the number of cruises he books, c ?

$$
\begin{aligned}
& \text { А. } c=26 d+120 \\
& \text { B. } c=120 d+25 \\
& \text { C. } d=120+25 c
\end{aligned}
$$

## D. $d=120 c+25$

## Answer: C

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4. Vera is on her school's track and field term.

In a partice long-jump competition against her temmates, she gets 5 points for landing over
the nearer line and 10 points for landing over
the more distant line. She gets a total of 7
jumps and lands $x$ times over the more distant
line and the rest of the times over the nearer
line. Which of the following equations represents the relationship between Vara's total score, $y$, and the number of times she lands over the more distant line, x ?
A. $y=10 x$
B. $y=5 x+35$
C. $y=10 x+5$

$$
\text { D. } y=70-5 x
$$

Answer: B

5.

A hardware store sells light bulbs in different quantities. The graph shows the cost of
various quantities. According to the graph, what is the cost of a single light bulb ?
A. $\$ 0.56$
B. $\$ 1.80$
C. $\$ 2.50$
D. $\$ 3.60$

Answer: B

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6. 

The graph shown represents which of the following equations ?
A. $y=-3 x+4$
B. $y=-\frac{1}{3} x+4$

$$
\begin{aligned}
& \text { C. } y=\frac{1}{3} x-4 \\
& \text { D. } y=3 x-4
\end{aligned}
$$

## Answer: C

## D Watch Video Solution

## Try Your Own

1. $3 y+2(y-2)=\frac{3 y}{2}+1$

What value of $y$ satisfies the equation above?

$$
\begin{aligned}
& \text { A. }-\frac{10}{7} \\
& \text { B. }-\frac{6}{13} \\
& \text { C. } \frac{7}{9} \\
& \text { D. } \frac{10}{7}
\end{aligned}
$$

## Answer: D

## - Watch Video Solution

2. $S=\frac{C-\frac{1}{4} I}{C+I}$

A techer uses the formula above to calculate
her students' scores, S, by subtracting $\frac{1}{4}$ of the number of equations the students answered incorrectly, I, from the number of questions they answered correctly, C, and dividing by the total number of questions.

Which of the following expresses the number of questions answered incorrectly in terms of the other variables?

$$
\begin{aligned}
& \text { A. } \frac{C(1-4 S)}{4 S+1} \\
& \text { B. } \frac{C(1+4 S)}{4 S-1} \\
& \text { C. } \frac{4 C(1-S)}{4 S+1}
\end{aligned}
$$

D. $\frac{4 C(1+S)}{4 S-1}$

## Answer: C

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3. What value of $n$ satisfies the equation $\frac{7}{8}(n-6)=\frac{21}{2} ?$

D Watch Video Solution
4. If $b \neq 0$ and $\frac{3 a+b}{b}=\frac{11}{2}$, which of the following could be the value of $\frac{a}{b}$ ?
A. $\frac{3}{2}$
B. $\frac{7}{2}$
C. $\frac{9}{2}$
D. It is not possible to determine a value of

$$
\frac{a}{b} .
$$

Answer: A

$$
\text { 5. } \frac{4+z-(3+2 z)}{6}=\frac{-z-3(5-2)}{7}
$$

What is the value of $z$ in the equation above?
A. -61
B. $-\frac{61}{27}$
C. $\frac{61}{27}$
D. 61

## Answer: D

6. A local restaurant is hosing a dance-a-thon
for charity. Each couple must dance a minimum of three hours before earning any money for the charity. After the first three hours, couples earn $\$ 50$ per half-hour of continous dancing. Which expression represents the total amount earned by a couple who dance $h$ hours, assuming they dance at least three hours?
A. 25 h
B. 100 h
C. $50(h-3)$
D. $100 h-300$

## Answer: D

## - Watch Video Solution

7. The final value, $v$, in a four-digit lock code is determined by multiplying the second value by two, subtracting that expression from the first value, and dividing the resulting expression by half of the third value. The first value is $f$, the
is the final value, $v$, in terms of $f$ and $t$ ?

$$
\begin{aligned}
& \text { A. } \frac{f-2}{t} \\
& \text { B. } \frac{2 f-4}{t} \\
& \text { C. } \frac{t}{2 f-4} \\
& \text { D. } \frac{2 t-4}{f}
\end{aligned}
$$

Answer: B
8. A pizzeria's top-selling pizzas are The Works
and The Hawaiian. The Works sells for $\$ 17$,
and The Hawaiian sells for $\$ 13$. Ingredient
costs for the works are $\$ 450$ per week, and ingreading costs for The Hawaiian are $\$ 310$ per week. If $x$ represents the number of each type of pizza sold in one week, and the weekly profit from the sale of each type of pizza is the same, what is the values of $x$ ?
A. 30
B. 35
C. 140
D. 145

Answer: B

## D Watch Video Solution

9. A student opens a checking account when
she starts a new job so that her paychecks can
be directly deposited into the account. Her balance can be computed using the expression $10 n w+50 m$ where n is the
number of hours she works every week and w is the number of weeks that she has worked so
far. Assuming she does not withdraw any money from her account, which of the terms in
the expressin most logically will change if the student geets a raise ?
A. 10
B. n
C. w
D. The expression will not change if the student gets a raise.

Answer: A

## D Watch Video Solution

10. Milk starts a job at which his starting salary
is $\$ 25500$ per year. He expects that his salary
will increase by a constnat dollar amount annually. In 12 years, his salary will be doulb ehis starting salary. Assuming salary increases
take place only at the eand of a full year, how many years must Malik wait until his salary is at least $\$ 40,000$ annually?

## - Watch Video Solution

11. Line A passes through the cooredinate points $\left(-\frac{2}{5}, 0\right)$ and $(0,1)$. Which of the following lines will line A never intersect ?

C.


## Answer: B

## - View Text Solution

12. In the xy-plane, the point $(4,7)$ lies on the
line $t$, which is perpendicular to the line
$y=-\frac{4}{3} x+6$. What is the equation of line t?

$$
\begin{aligned}
& \text { A. } y=\frac{3}{4} x+4 \\
& \text { B. } y=-\frac{4}{3} x+4 \\
& \text { C. } y=\frac{3}{4} x+7 \\
& \text { D. } y=-\frac{3}{4} x+4
\end{aligned}
$$

Answer: A

D Watch Video Solution

Snowy Tree Cricket Temperature Prediction


The graph shows the correlation between ambient air temperature, $t$, in degress

Fahrenheit and the number of chirps, c, per minute that a snowy tree cricket makes at that temperature. Which of the following equations represents the line shown in the graph ?
A. $c=4 t-160$
B. $c=\frac{1}{4} t-160$
C. $c=\frac{1}{2} t-40$
D. $c=4 t+160$

Answer: A

- Watch Video Solution


14. 

Weight (in pounds)

A freight airline charges a flat fee to airmil a
box, plus an additional charge for each pound
the box weights. The graph above shows the relationship between the weitht of the box
and the total cost to airmail it. Based on the graph, how much would it cost in dollars to airmail a 40-pound box

## D Watch Video Solution



Xia is charging her laptop. She records the battery charge for the first 30 minutes after she plugs it in to get an idea of when it will be completely charged. The table above shows
the results. If $y$ is the percent battery charge
on Xia's laptop, which linear equation
represents the correct relationship between y
and $x$ ?

$$
\begin{aligned}
& \text { A. } y=1.5 x+19 \\
& \text { B. } y=2 x+14 \\
& \text { C. } y=2.5 x+9 \\
& \text { D. } y=10 x+34
\end{aligned}
$$

Answer: A

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16. Remember that the SAT doesn't ask you to
show your work. If you find the algeba in a question challenging, there is often another
way to get to the answer. Try this question
first using algebra and then using the picking numbers startegy you alermed in chapter 3.

Time yourself. Which approach fo you find easier? Which onw was faster ? Did you get the correct answer both times ? Remamber
you per-ferred approach and try it first if you see a questin like this on test day.

$$
\frac{2(a-3)}{b}=\frac{4}{7}
$$

If the equation above is true, whihc of the following must NOT be true ?

$$
\begin{aligned}
& \text { A. } \frac{b}{a-3}=\frac{7}{2} \\
& \text { B. } \frac{2 a}{b}=-\frac{10}{7} \\
& \text { C. } 14 a-4 b=42 \\
& \text { D. } \frac{a-3}{b}=\frac{2}{7}
\end{aligned}
$$

Answer: B
17. Which value of $x$ makes the equation $\frac{8}{5}\left(x+\frac{33}{12}\right)=16$ true ?
A. 7.25
B. 8.75
C. 12.75
D. 13.25

Answer: A
(D) Watch Video Solution


Number of Songs Purchased
18.

The graph above shows the cost of joining and buying music from a music subsciption service.

What does the $y$-intercept of the line most
likely represent?
A. The cost per song
B. The cost to join the service
C. The cost of buying 20 sings
D. The cost of 20 subscriptions to the service

Answer: B

- Watch Video Solution

19. If $\frac{3}{4} y=6-\frac{1}{3} c$, then what is the value of
$2 x+\frac{9}{2} y ?$
20. Three years ago, Madison High School started charging an admission fee for basketball games to raise money for new bleachers. The initial price was $\$ 2$ per person, the school raised the price of admission to $\$ 2.50$ this year. Assuming this tread continuse, which of the following equations can be used to describe $c$, the cost of admission, y years after the school began charging for admission to games ?
A. $c=6 y+2$
B. $c=\frac{y}{6}+2.5$
C. $c=\frac{y}{6}+2$
D. $c=\frac{y}{2}+2$

Answer: C

- Watch Video Solution

| Price of One <br> Pound | Projected Number <br> of Pounds Sold |
| :---: | :---: |
| $\$ 1.20$ | 15,000 |
| $\$ 1.40$ | 12,500 |
| $\$ 1.60$ | 10,000 |
| $\$ 1.80$ | 7,500 |
| $\$ 2.00$ | 5,000 |
| 21. | 2,20 |

Which of the following equations best, describes the linear relationship shown in the table, where $g$ represents the number of pounds of grain sold and $d$ represnets the price in dollars of one pound of grain?

$$
\text { A. } g=1.2 d+12.500
$$

$$
\text { B. } g=12,500 d+15,000
$$

## C. $g=-12,500 d+17,500$

D. $g=-12,500 d+30,000$

Answer: D
(D) Watch Video Solution

22.

Brain and Jared live in the same apartment comlex and both bike to and from work every day. The figure above shows a typical commute home for each of them. Based on the figure, which of the following statemetns is true?
A. It takes Brain longer to bike home
because his work is farther away.
B. It takes Jared longer to bike home
because his work is farther away.
C. Jared and Brain arrive home at the same
time, so they must bike at about the
same rate.
D. Jared bikes a longer distance than Brain
in the same amount of time, so Jared must bike at a faster rate.

## Answer: D

## D Watch Video Solution

23. When graphing a linear equation that is written in the form $y=m x+b$, the variable $m$ represents the slope of the line and $b$ represents the $y$-intercept. Assuming that $b>0$, which of the following best describes how reversing the sign of $b$ will affect the graph ?
A. The new line will be shifted down $b$ units.
B. The new line will be shifted down $2 b$ units.
C. the new line will be perfect reflection across the $x$-axis.
D. The new line will be a perfect reflection across the $y$-axis.

## Answer: B

24. The graph of a line in the $x y$-plane passes
through the points $(5,4)$ and $\left(3, \frac{1}{2}\right)$.
Which of the following equations describes
the line?

$$
\begin{aligned}
& \text { A. } y=\frac{7}{4} x+\frac{19}{4} \\
& \text { B. } y=-\frac{7}{4} x-\frac{19}{4} \\
& \text { C. } y=\frac{7}{4} x-\frac{19}{4} \\
& \text { D. } y=\frac{4}{6} x+\frac{8}{7}
\end{aligned}
$$

## Answer: C

## D Watch Video Solution

25. Line $f$ in th exy-plane passes through the origin and has a slope of $-\frac{2}{5}$. Line z is perpendicular to line $f$ and passes through the point $(6,2)$. Which of the following is the equation of line $z$ ?

$$
\begin{aligned}
& \text { А. } y=-\frac{1}{5} x \\
& \text { В. } y=-\frac{2}{5} x-13
\end{aligned}
$$

$$
\begin{aligned}
& \text { C. } y=\frac{5}{2} x \\
& \text { D. } y=\frac{5}{2} x-13
\end{aligned}
$$

## Answer: D

## D Watch Video Solution

26. $V=\frac{1}{3} \pi\left(\frac{d}{2}\right)^{2} h$

A circle of rubber with a constant diameter $d$
is placed on a table, its perimeter is anchored to the table and a string is attached to its centre. When the string is pulled upwards, a
cone is formed with height h and volume V .

The relationship between d , h , and V is represented above. Which of the following statements must be true?
I. As the volume of the cone decreases, the height also decreases.
II. If the diameter of the base of the cone is 6 centimeters, the height can be determined by dividing the volume by $3 \pi$.
III. If the height of the conc triples, the volume must also triple.
A. I only

## B. I and II only

## C. II and III only

D. I, II, and III

## Answer: D

## D Watch Video Solution

## Solving Equations

1. $\frac{1}{2}(3 X+14)=\frac{1}{6}(7 X-10)$

Which value of $x$ satisfies the equation above?
A. -26
B. 2
C. 8
D. 16

Answer: A

- Watch Video Solution


## Word Problems

1. A laser tag arean sells two types of memberships. One package costs $\$ 325$ for one
year of membership with an unilimated number of visits. The second package has a
\$125 enrollment fee, includes five free visits, and costs and additional $\$ 8$ per visit after the
first five. How many visits over a one-year period would a person who purchase the second package need to use for th cost to equal that of the one-year membership ?
A. 20
B. 25
C. 30
D. 40

Answer: C

## - Watch Video Solution

## Linear Graph

1. What is the equation of the line that pases
through the points $(-3,1)$ and $(1,3) ?$
A. $y=-x+2$
B. $y=-x-2$
C. $y=x-2$
D. $y=x+2$

Answer: D

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