



## MATHS

# **BOOKS - KAPLAN INC MATHS (ENGLISH)**

# QUADRATICS

How Much Do You Know

**1.** Which of the following linear expression divides evenly into  $6x^2 + 7x - 20$  ?

A. 3x - 10

B. 3x - 5

C. 3x - 4

D. 3x-2

#### Answer: C

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**2.** 
$$x^2 - 10x - 7$$

Which of the following expression is equivalent to

the expression above ?

A. 
$$(x-5)^2 - 32$$

B. 
$$(x-5)^2 + 32$$
  
C.  $(x+5)^2 - 32$   
D.  $(x+5)^2 + 32$ 

#### Answer: A



**3.** In the equation above, k is a constant. For which of the following values f k does the equation have at least one re3al solution ?

B. 3

C. 4

D. 5

Answer: A

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Which of the following could be the equation of the graph shown ?

A. 
$$y = 2x + 10$$

B. 
$$y = -x^2 \, rac{+_3}{2} \, + 10$$

C. 
$$y = -(x-2)(x+5)$$

D. 
$$y = -(x+2)(x-5)$$

#### Answer: D

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**5.** The x-coordinates of the solutions to a system of equations are 3.5 and 6. Which of the following could be the system ?

A. 
$$egin{cases} y = x + 3.5 \ y = x^2 + 6 \end{cases}$$

B. 
$$\begin{cases} y = x - 7 \\ y = -(x - 6)^2 \\ y = \frac{1}{2}x + 3 \\ y = -(x - 5)^2 + 7 \\ y = \frac{1}{2}x + 7 \\ D. \begin{cases} y = \frac{1}{2}x + 7 \\ y = -(x - 6)^2 + 3.5 \end{cases}$$

#### Answer: C



**1.** Which of the following equivalent form of the expression (6 - 5x)(15x - 11) ?

A. 
$$-75x^2 + 35x - 66$$

$$\mathsf{B.} - 75x^2 + 145x - 66$$

 $C.90x^2 - 141x + 35$ 

D. 
$$90x^2 + 9x + 55$$

#### **Answer: B**

2. Which of the following is equivalent to
$$\frac{x^2 - 10x + 25}{3x^2 - 75}$$
?`
A.  $\frac{3(x-5)}{(x+5)}$ 

B. 
$$rac{3(x+5)}{(x-5)}$$
  
C.  $rac{(x-5)}{3(x+5)}$   
D.  $rac{(x+5)}{3(x-5)}$ 

#### Answer: C



# **3.** For what positive value of x is the equation $\frac{3}{2x^2+4x-6} = 0$ underfined ?

**4.**  $3x^2 + 9x = 54$ 

What is the sum of the roots of the equation above?

 $\mathsf{A.}-6$ 

 $\mathsf{B.}-3$ 

C. 3

D. 6

Answer: B

5. Which of the following functions is equivalent to

thte function above ?

A. 
$$f(x)=(x-5)^2$$

B.  $f(x) = x^2 + 10.28x + 5.42$ 

 $\mathsf{C.}\,f(x)=0.61x^2+0.14x+25$ 

D.

$$f(x) = 1.3(x-3)^2 = 0.69x^2 + 0.14x + 9.79$$



6. For all a and b, what is the sum of  $(a-b)^2$  and  $(a+b)^2$ ?

A.  $2a^2$ 

- $\mathsf{B.}\, 2a^2-2b^2$
- $\mathsf{C.}\, 2sa^2+2b^2$

D. 
$$2a^2 + 4ab + 2b^2$$

#### Answer: C



7. What is the positive difference between the roots of the equation  $y = rac{1}{3}x^2 - 2x + 3$  ?

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8. 
$$f(x) rac{3}{\left(x-7
ight)^2+6(x-7)+9}$$

#### For which value of x is the function f (x) underfined

?

**9.** Suppose  $a^2 + 2ab + b^2 = c^2$  and c - b = 4.

Assuming c > 0, which is the value of a ?

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**10.** 
$$2x^2 - 28x + 98 = a(x - b)^2$$

In the expression above, a > 1 and both a and b are constants. Which of the following could be the value of b ?

A. -7

C. 14

D. 49

**Answer: B** 

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11. Which of the following is a value of x that satisfies the equation  $x^2 + 2x - 5 = 0$  ?

A. -1

B.  $1 - \sqrt{6}$ 

 $\mathsf{C.}\,1+\sqrt{6}$ 

D. 
$$-1 - \sqrt{6}$$

#### Answer: D

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**12.** 
$$a^4 - 12aa^2 - 72 = 0$$

Which of the following is the greatest possible value of a ?

A. 
$$\sqrt{6+\sqrt{3}}$$
  
B.  $\sqrt{6ig(1+\sqrt{3}ig)}$ 

C. 12

D. 
$$6(1+\sqrt{3})$$

#### **Answer: B**

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13. 
$$x^2 - (6\sqrt{5})x = -40$$

What is the sum of the possible values of x given

the above equation ?

A. 15

B.  $5\sqrt{5}$ C.  $6\sqrt{5}$ 

D. 60

#### Answer: C

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## 14. $x^2 + 7x + 1 = 2x^2 - 4x + 3$

Which of the following is a value of x that is valid in the above equation ?

A. 
$$5.5-\sqrt{28.25}$$

 $\mathrm{B.}\,\sqrt{5.5}$ 

D. 
$$5.5+\sqrt{30.25}$$

#### Answer: A

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**15.** Given the equation  $2x^2 + 8x + 4 + 2z = 0$ ,

for what value of z is there exactly one solution for

х?



16. The product of all the solutions to the equation

 $3y^2 + 4v - 2 = 0$  is M. What is the value of M ?

A. 
$$-3$$
  
B.  $-\frac{2}{3}$   
C.  $-\frac{1}{3}$   
D.  $\frac{4}{3}$ 

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Answer: B



17. What are the solution to the equation  $4x^2 - 24x + 16 = 0$ ? A.  $x=3\pm\sqrt{5}$ B.  $x=4\pm\sqrt{6}$ C.  $x=5\pm\sqrt{3}$ D.  $x=5\pm 2\sqrt{2}$ 



18. 
$$3x^2 = m(5x + v)$$

What are the values of x that satisgy the equation above, where m and v are constants ?

$$\begin{array}{l} \mathsf{A.} \, x = \, - \, \frac{5m}{6} \pm \frac{\sqrt{25m^2 + 12mv}}{6} \\ \mathsf{B.} \, x = \, \frac{5m}{6} \pm \, \frac{\sqrt{25m^2 + 12mv}}{6} \\ \mathsf{C.} \, x = \, - \, \frac{5m}{3} \pm \, \frac{\sqrt{12m^2 + 12mv}}{3} \\ \mathsf{D.} \, x = \, \frac{5m}{3} \pm \, \frac{\sqrt{25m^2 + 12mv}}{3} \end{array}$$

#### **Answer: B**



**19.** x(dx + 10) = -3

The equation above, where d is a constant, has no real solutions. The value of d could be which of the following?

A. - 12

B.4

C. 8

D. 10

Answer: D



**20.** Which of the following equations does NOT have any solutions that are real numbers ?

A. 
$$x^2 + 8x - 12 = 0$$

B. 
$$x^2 - 8x + 12 = 0$$

C. 
$$x^2 - 9x + 21 = 0$$

D. 
$$x^2 + 100x - 1 = 0$$

#### Answer: C



The following quadratinos are all representations of the graph above. Which equation clearly represents the exact values of the x-intercepts of the graph ?

A. 
$$y = 4x^2 - x - 3$$
  
B.  $y = (4x + 3)(x - 1)$   
C.  $y = 4(x - 0.125)^2 - 3.0625$   
D.  $y + 3.0625 = 4(x - 0.125)^2$ 

**Answer: B** 



22. Which equation represents the Axis of symmetry for the graph of the quadratic function  $f(x) = -rac{11}{3}x^2 + 17x - rac{43}{13}$  ? A.  $x = -\frac{102}{11}$ B.  $x = -\frac{51}{22}$ C.  $x = \frac{51}{22}$  $\mathsf{D}.\,x=\frac{102}{11}$ 

#### Answer: C

**23.** How many times do the parabolas given by the equation

 $f(x) = 3x^2 - 24x + 52$  and  $g(x) = x^2 + 12x - 110$ intersect ?

A. Never

B. Once

C. Twice

D. More than twice

Answer: B



24. What is the positive difference between the xintercepts of the parabola given by the equatin  $g(x) = -2.5x^2 + 10x - 7.5$ ?



**25.** A toy rocket is fired from ground level. The height of the rocket with respect to time can be represented by a quadratic function. If the toy rocket reaches a maximum height of 34 feet 3 seconds after it was fired, which of the following

functions could represent the height, h, of the rocket t seconds after it was fired ?

A. 
$$h(t) = -16(t-3)^2 + 34$$
  
B.  $h(t) = -16(t+3)^2 + 34$   
C.  $h(t) = 16(t-3)^2 + 34$   
D.  $h(t) = 16(t+3)^2 + 34$ 



26. 
$$\left\{egin{array}{l} a=b^2+4b-12\ a=-12+b \end{array}
ight.$$

The ordered pair (a,b) satisfies the system of equatin above. What is one possible value of b ?

**A.** − 6

B.-3

C. 2

D. 3

#### Answer: B

27. In the xy-coordinate plane, the graph of  $y = 5x^2 - 12x$  intersects the grphs of y = -2 at points (0,0) and (a,b). What is the value of a ?

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**28.** How many real solutions are there to the system of equations above ?

A. Exactly 4 real solutions

B. Exactly 2 real solutions

C. Exactly 1 real solutions

D. No real solutions

#### Answer: B





The graph of the function f, dedined by  $f(x) = -2(x-3)^2 - 4$ , is shown in the xyplane above. The function g (not shown) is defined by g(x) = 2x - 10. If  $f^{C} = g^{C}$ , what is one possible value of c?

$$A. - 6$$

C. 2

D. 4

#### Answer: C

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**30.** On the xy-plane, points P and Q are the two points where the parabola with the equation  $y = 3x^2 + \frac{14}{3}x - \frac{73}{3}$  and the line with thte equation  $y = -\frac{4}{3}x - \frac{1}{3}$  meet. What is the

distance between point P and point Q ?

A. 5

B. 8

C. 10

D. 12

#### Answer: C



the two functions intersect are (z,0) and (-z, 0).

What is the value of z ?

 $\mathsf{A.}\,0.5$ 

B. 1.0

 $\mathsf{C.}\,2.5$ 

 $\mathsf{D.}\,4.0$ 

Answer: C



**32.** The equation  $\frac{1}{4}(4x^2 - 8x - k) = 30$  has two solutions: x = -5 and x = 7. What is the value of 2k ?



## 33. 戻

The maximum value of the data shown in the scatterplot above occurs at x = 25. It the data is modeled using a quadratic regression and the correlation coefficient is 1.0 (the fit is exact), then what is the y-value when x = 35?

A. 10

B. 15

C. 22

D. 27

#### Answer: D



**34.** The height of a boulder launched from a Roman catap can be described as a function of time according to the following quadratic equation:  $h(t) = -16t^2 + 224t + 240$ . What is the maximum height that the boulder attains ?

A. 240

B. 784

C. 1024

D. 1696

Answer: C



35. The height of a boulder launched from a Roman catap can be described as a function of time according to the following quadratic equation:  $h(t) = -16t^2 + 224t + 240$ . How much time elapese between the moment the boulder is launched and the moment it hits the ground, assuming that the ground is at a height of 0?

A. 7

B. 12

C. 14

D. 15

#### Answer: D





If the function shown in the graph is represented by  $f(x) = a(x - h)^2 + k$ , which of the following statements is NOT true ?

A. The value of a is negative.

B. f (x) is symmetrical across the line y = 3.

C. The function  $g(x) = rac{2x}{3}$  intersects f (x) at

its vertex.

D. The value of h is positive.

Answer: B

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37. If (x,y) is a solution to the system of equations

above, what is the value of  $x^2$  ?

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**38.** What are the x-intercepts of the parabolic function  $f(x) = x^2 - 7x + rac{81}{4}$  ?

A. 1 and 
$$8\frac{1}{4}$$
  
B.  $1\frac{1}{4}$  and  $5\frac{3}{4}$   
C.  $1\frac{1}{4}$  and  $5\frac{3}{4}$   
D.  $1\frac{1}{2}$  and  $5\frac{1}{2}$ 

#### Answer: D



**39.** If 
$$g(x) = (x-2)^2 - 5$$
, which of the following

statements is true ?

A. The function g (x) is increasing over the entire domain. B. The functin g(x) is decreasing over the entire domain. C. The function g (x) is increasing for x < 2and decreasing for x > 2. D. The function g (x) is decreasing for x < 2and increasing for x > 2.

Answer: D

40. What is the sum of the solutions of $(6x+5)^2-(3x-2)^2=0$ ? A.  $-rac{8}{3}$ 

B. 
$$-\frac{1}{6}$$
  
C.  $\frac{7}{3}$ 



**41.** If the equation above is true, then what is the positive value of the expression  $10\sqrt{x} - 15$  ?

A. 20

B.25

C. 30

D. 35



**42.** In the equation  $x-2=rac{3}{x-2},\,$  which of the

following is a possible value of x - 2 ?

- A.  $\sqrt{3}$
- B. 1
- $\mathsf{C.}\,2+\sqrt{3}$
- D. 3



**43.** If  $rac{z^{x^2+y^2}}{z^{-2xy}}=(z^3),$  x and y are positive

integers, and x > y, what is the value of x - y?

A. 1

B. 2

C. 3

D. 8

Answer: A



Solving Quadratics By Factoring

1. If  $x^2 - 7x = 30$  and x > 0, what is the value of x - 5?

A. 5

B. 6

C. 10

D. 25

Answer: A

**1.** Which of the following expressions is equivalent to  $25x^2y^4 - 1$  ?

A. 
$$5ig(x^2y^4-1ig)$$

$$\mathsf{B.}-5\big(xy^2+1\big)$$

$$\mathsf{C}.\,(5xy-1)(5xy+1)$$

D. 
$$\left(5xy^2-1
ight)\left(5xy^2+1
ight)$$

#### Answer: D

1. Which of the following equations has the same solutions as the equation  $40 - 6x = x^2 - y$  ?

A. 
$$y=\left(x-6
ight)^2-40$$

B. 
$$y=\left(x-6
ight)^2+40$$

C. 
$$y=\left(x+3
ight)^2-49$$

D. 
$$y=\left(x+3
ight)^2+49$$

#### Answer: C

1. Which of the following are the real values of x that satisfy the equation  $2x^2 - 5x - 2 = 0$ ?

A.1 and 4

$$B. -\frac{5}{4} + \frac{\sqrt{41}}{4} \text{ and } \frac{5}{4} - \frac{\sqrt{41}}{4}$$
$$C. \frac{5}{4} + \frac{\sqrt{41}}{4} \text{ and } \frac{5}{4} - \frac{\sqrt{41}}{4}$$

D. No real solutions

#### Answer: C

**1.** Given the equatin  $y = -(2x-4)^2 + 7$ , which

of the following statements is NOT true ?

A. The vertex is (4,7).

B. The y-intercept is (0, -9).

C. The parabola opens diownward.

D. The graph crosses the x-axis at least one

time.

Answer: A

#### Systems Of Quadratic And Linear Equations

1. In the xy-plane, the graph of  $y + 3x = 5x^2 + 6$  and y - 6 = 2x intersect at points (0,6) and (a,b). What is the value of b ?