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## MATHS

## BOOKS - KAPLAN INC MATHS (ENGLISH)

## QUADRATICS

## How Much Do You Know

1. Which of the following linear expression divides
evenly into $6 x^{2}+7 x-20$ ?
A. $3 x-10$
B. $3 x-5$
C. $3 x-4$
D. $3 x-2$

## Answer: C

## D Watch Video Solution

2. $x^{2}-10 x-7$

Which of the following expression is equivalent to
the expression above ?

$$
\text { A. }(x-5)^{2}-32
$$

$$
\begin{aligned}
& \text { B. }(x-5)^{2}+32 \\
& \text { C. }(x+5)^{2}-32 \\
& \text { D. }(x+5)^{2}+32
\end{aligned}
$$

## Answer: A

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3. In the equation above, $k$ is a constant. For which of the following values $f \mathrm{k}$ does the equation have at least one re3al solution ?
B. 3
C. 4
D. 5

Answer: A

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4. 

Which of the following could be the equation of
the graph shown?
A. $y=2 x+10$

$$
\begin{aligned}
& \text { В. } y=-x^{2} \frac{+3}{2}+10 \\
& \text { С. } y=-(x-2)(x+5) \\
& \text { D. } y=-(x+2)(x-5)
\end{aligned}
$$

## Answer: D

## D View Text Solution

5. The $x$-coordinates of the solutions to a system of equations are 3.5 and 6 . Which of the following could be the system ?

$$
\text { A. }\left\{\begin{array}{l}
y=x+3.5 \\
y=x^{2}+6
\end{array}\right.
$$

B. $\left\{\begin{array}{l}y=x-7 \\ y=-(x-6)^{2}\end{array}\right.$
C. $\left\{\begin{array}{l}y=\frac{1}{2} x+3 \\ y=-(x-5)^{2}+7\end{array}\right.$
D. $\left\{\begin{array}{l}y=\frac{1}{2} x+7 \\ y=-(x-6)^{2}+3.5\end{array}\right.$

Answer: C

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## Try On Your Own

1. Which of the following equivalent form of the expression $(6-5 x)(15 x-11)$ ?
A. $-75 x^{2}+35 x-66$
B. $-75 x^{2}+145 x-66$
C. $90 x^{2}-141 x+35$
D. $90 x^{2}+9 x+55$

Answer: B

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2. Which of the following is equivalent to

$$
\frac{x^{2}-10 x+25}{3 x^{2}-75} ?
$$

A. $\frac{3(x-5)}{(x+5)}$
B. $\frac{3(x+5)}{(x-5)}$
C. $\frac{(x-5)}{3(x+5)}$
D. $\frac{(x+5)}{3(x-5)}$

## Answer: C

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3. For what positive value of $x$ is the equation
$\frac{3}{2 x^{2}+4 x-6}=0$ underfined ?

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4. $3 x^{2}+9 x=54$

What is the sum of the roots of the equation above?
A. -6
B. -3
C. 3
D. 6

Answer: B

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5. Which of the following functions is equivalent to thte function above?
A. $f(x)=(x-5)^{2}$
B. $f(x)=x^{2}+10.28 x+5.42$
C. $f(x)=0.61 x^{2}+0.14 x+25$
D.

$$
f(x)=1.3(x-3)^{2}=0.69 x^{2}+0.14 x+9.79
$$

## Answer: A

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6. For all $a$ and $b$, what is the sum of

$$
(a-b)^{2} \text { and }(a+b)^{2} ?
$$

A. $2 a^{2}$
B. $2 a^{2}-2 b^{2}$
C. $2 s a^{2}+2 b^{2}$
D. $2 a^{2}+4 a b+2 b^{2}$

Answer: C

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7. What is the positive difference between the roots of the equation $y=\frac{1}{3} x^{2}-2 x+3$ ?

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8. $f(x) \frac{3}{(x-7)^{2}+6(x-7)+9}$

For which value of $x$ is the function $f(x)$ underfined ?

- Watch Video Solution

9. Suppose $a^{2}+2 a b+b^{2}=c^{2}$ and $c-b=4$.

Assuming $c>0$, which is the value of a ?

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10. $2 x^{2}-28 x+98=a(x-b)^{2}$

In the expression above, $a>1$ and both a and b are constants. Which of the following could be the value of $b$ ?
A. -7
B. 7
C. 14
D. 49

Answer: B

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11. Which of the following is a value of $x$ that
satisfies the equation $x^{2}+2 x-5=0$ ?
A. -1
B. $1-\sqrt{6}$
C. $1+\sqrt{6}$
D. $-1-\sqrt{6}$

Answer: D

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12. $a^{4}-12 a a^{2}-72=0$

Which of the following is the greatest possible value of a?
A. $\sqrt{6+\sqrt{3}}$
B. $\sqrt{6(1+\sqrt{3})}$
C. 12
D. $6(1+\sqrt{3})$

Answer: B

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13. $x^{2}-(6 \sqrt{5}) x=-40$

What is the sum of the possible values of $x$ given the above equation?
A. 15
B. $5 \sqrt{5}$
C. $6 \sqrt{5}$
D. 60

## Answer: C

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14. $x^{2}+7 x+1=2 x^{2}-4 x+3$

Which of the following is a value of $x$ that is valid in the above equation?
A. $5.5-\sqrt{28.25}$
B. $\sqrt{5.5}$
C. $\sqrt{30.25}$

```
D. \(5.5+\sqrt{30.25}\)
```

Answer: A

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15. Given the equation $2 x^{2}+8 x+4+2 z=0$,
for what value of $z$ is there exactly one solution for
$x$ ?

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16. The product of all the solutions to the equation $3 y^{2}+4 v-2=0$ is $M$. What is the value of $M$ ?
A. -3
B. $-\frac{2}{3}$
C. $-\frac{1}{3}$
D. $\frac{4}{3}$

Answer: B

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17. What are the solution to the equation $4 x^{2}-24 x+16=0 ?$
A. $x=3 \pm \sqrt{5}$
B. $x=4 \pm \sqrt{6}$
C. $x=5 \pm \sqrt{3}$
D. $x=5 \pm 2 \sqrt{2}$

Answer: A

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18. $3 x^{2}=m(5 x+v)$

What are the values of $x$ that satisgy the equation above, where m and v are constants ?

$$
\begin{aligned}
& \text { A. } x=-\frac{5 m}{6} \pm \frac{\sqrt{25 m^{2}+12 m v}}{6} \\
& \text { B. } x=\frac{5 m}{6} \pm \frac{\sqrt{25 m^{2}+12 m v}}{6} \\
& \text { C. } x=-\frac{5 m}{3} \pm \frac{\sqrt{12 m^{2}+12 m v}}{3} \\
& \text { D. } x=\frac{5 m}{3} \pm \frac{\sqrt{25 m^{2}+12 m v}}{3}
\end{aligned}
$$

Answer: B
19. $x(d x+10)=-3$

The equation above, where $d$ is a constant, has no real solutions. The value of $d$ could be which of the following?
A. -12
B. 4
C. 8
D. 10

Answer: D

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20. Which of the following equations does NOT have any solutions that are real numbers ?
A. $x^{2}+8 x-12=0$
B. $x^{2}-8 x+12=0$
C. $x^{2}-9 x+21=0$
D. $x^{2}+100 x-1=0$

Answer: C

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21. 

The following quadratinos are all representations of the graph above. Which equation clearly represents the exact values of the x-intercepts of the graph ?

$$
\begin{aligned}
& \text { А. } y=4 x^{2}-x-3 \\
& \text { B. } y=(4 x+3)(x-1) \\
& \text { C. } y=4(x-0.125)^{2}-3.0625 \\
& \text { D. } y+3.0625=4(x-0.125)^{2}
\end{aligned}
$$

Answer: B
22. Which equation represents the Axis of symmetry for the graph of the quadratic function $f(x)=-\frac{11}{3} x^{2}+17 x-\frac{43}{13} ?$

$$
\begin{aligned}
& \text { A. } x=-\frac{102}{11} \\
& \text { B. } x=-\frac{51}{22} \\
& \text { C. } x=\frac{51}{22} \\
& \text { D. } x=\frac{102}{11}
\end{aligned}
$$

Answer: C

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23. How many times do the parabolas given by the equation $f(x)=3 x^{2}-24 x+52$ and $g(x)=x^{2}+12 x-110$ intersect?
A. Never
B. Once
C. Twice
D. More than twice

Answer: B
24. What is the positive difference between the $x$ intercepts of the parabola given by the equatin $g(x)=-2.5 x^{2}+10 x-7.5 ?$

## - Watch Video Solution

25. A toy rocket is fired from ground level. The height of the rocket with respect to time can be represented by a quadratic function. If the toy rocket reaches a maximum height of 34 feet 3 seconds after it was fired, which of the following
functions could represent the height, $h$, of the rocket t secnds after it was fired?

$$
\begin{aligned}
& \text { A. } h(t)=-16(t-3)^{2}+34 \\
& \text { B. } h(t)=-16(t+3)^{2}+34 \\
& \text { C. } h(t)=16(t-3)^{2}+34 \\
& \text { D. } h(t)=16(t+3)^{2}+34
\end{aligned}
$$

Answer: A

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26. $\left\{\begin{array}{l}a=b^{2}+4 b-12 \\ a=-12+b\end{array}\right.$

The ordered pair ( $a, b$ ) satisfies the system of equatin above. What is one possible value of $b$ ?
A. -6
B. -3
C. 2
D. 3

Answer: B

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27. In the xy-coordinate plane, the graph of $y=5 x^{2}-12 x$ intersects the grphs of $y=-2$ at points $(0,0)$ and $(a, b)$. What is the value of a ?

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28. How many real solutions are there to the system of equations above?
A. Exactly 4 real solutions
B. Exactly 2 real solutions
C. Exactly 1 real solutions
D. No real solutions

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29. 



The graph of the function f, dedined by $f(x)=-2(x-3)^{2}-4$, is shown in the $x y$ plane above. The function $g$ (not shown) is defined by $g(x)=2 x-10$. If $f ®=g ®$, what is one possible value of $c$ ?

$$
\text { A. }-6
$$

B. -4
C. 2
D. 4

## Answer: C

## D View Text Solution

30. On the xy-plane, points $P$ and $Q$ are the two points where the parabola with the equation $y=3 x^{2}+\frac{14}{3} x-\frac{73}{3}$ and the line with thte equation $y=-\frac{4}{3} x-\frac{1}{3}$ meet. What is the distance between point $P$ and point $Q$ ?
A. 5
B. 8
C. 10
D. 12

Answer: C

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31. 

The
function
$f(x)=4 x^{2}-25$ and $g(x)=-4 x^{2}+25 \quad$ are
graphed in the $x y$-plane above. The point where
the two functions intersect are $(z, 0)$ and $(-z, 0)$.
What is the value of $z$ ?
A. 0.5
B. 1.0
C. 2.5
D. 4.0

Answer: C
32. The equation $\frac{1}{4}\left(4 x^{2}-8 x-k\right)=30$ has two solutions: $x=-5$ and $x=7$. What is the value of $2 k$ ?

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33. 

The maximum value of the data shown in the scatterplot above occurs at $x=25$. It the data is modeled using a quadratic regression and the correlation coefficient is 1.0 (the fit is exact), then what is the $y$-value when $x=35$ ?
A. 10
B. 15
C. 22
D. 27

Answer: D

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34. The height of a boulder launched from a Roman catap can be described as a function of time according to the following quadratic equation: $h(t)=-16 t^{2}+224 t+240$.

What is the maximum height that the boulder attains?
A. 240
B. 784
C. 1024
D. 1696

Answer: C
35. The height of a boulder launched from a Roman catap can be described as a function of time according to the following quadratic
equation: $h(t)=-16 t^{2}+224 t+240$.
How much time elapese between the moment the
boulder is launched and the moment it hits the ground, assuming that the ground is at a height of

0 ?
A. 7
B. 12
C. 14
D. 15

## Answer: D

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36. 

If the function shown in the graph is represented
by $f(x)=a(x-h)^{2}+k$, which of the following statements is NOT true ?
A. The value of $a$ is negative.
B. $\mathrm{f}(\mathrm{x})$ is symmetrical across the line $y=3$.
C. The function $g(x)=\frac{2 x}{3}$ intersects $\mathrm{f}(\mathrm{x})$ at its vertex.
D. The value of $h$ is positive.

Answer: B

## - View Text Solution

37. If $(x, y)$ is a solution to the system of equations above, what is the value of $x^{2}$ ?

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38. What are the x-intercepts of the parabolic function $f(x)=x^{2}-7 x+\frac{81}{4}$ ?
A. 1 and $8 \frac{1}{4}$
B. $1 \frac{1}{4}$ and $5 \frac{3}{4}$
C. $1 \frac{1}{4}$ and $5 \frac{3}{4}$
D. $1 \frac{1}{2}$ and $5 \frac{1}{2}$

## Answer: D

## - Watch Video Solution

39. If $g(x)=(x-2)^{2}-5$, which of the following
statements is true?
A. The function $\mathrm{g}(\mathrm{x})$ is increasing over the entire domain.
B. The functin $g(x)$ is decreasing over the entire domain.
C. The function $\mathrm{g}(\mathrm{x})$ is increasing for $x<2$ and decreasing for $x>2$.
D. The function $\mathrm{g}(\mathrm{x})$ is decreasing for $x<2$ and increasing for $x>2$.
40. What is the sum of the solutions of

$$
(6 x+5)^{2}-(3 x-2)^{2}=0 ?
$$

A. $-\frac{8}{3}$
B. $-\frac{1}{6}$
C. $\frac{7}{3}$
D. 3

Answer: A
( Watch Video Solution
41. If the equation above is true, then what is the positive value of the expression $10 \sqrt{x}-15$ ?
A. 20
B. 25
C. 30
D. 35

Answer: A

- Watch Video Solution

42. In the equation $x-2=\frac{3}{x-2}$, which of the following is a possible value of $x-2$ ?
A. $\sqrt{3}$
B. 1
C. $2+\sqrt{3}$
D. 3

Answer: A

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43. If $\frac{z^{x^{2}+y^{2}}}{z^{-2 x y}}=\left(z^{3}\right), \mathrm{x}$ and y are positive integers, and $x>y$, what is the value of $x-y$ ?
A. 1
B. 2
C. 3
D. 8

Answer: A
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Solving Quadratics By Factoring

1. If $x^{2}-7 x=30$ and $x>0$, what is the value of $x-5$ ?
A. 5
B. 6
C. 10
D. 25

Answer: A

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1. Which of the following expressions is equivalent to $25 x^{2} y^{4}-1$ ?
A. $5\left(x^{2} y^{4}-1\right)$
B. $-5\left(x y^{2}+1\right)$
C. $(5 x y-1)(5 x y+1)$
D. $\left(5 x y^{2}-1\right)\left(5 x y^{2}+1\right)$

Answer: D

Completing The Square

1. Which of the following equations has the same solutions as the equation $40-6 x=x^{2}-y$ ?

$$
\begin{aligned}
& \text { A. } y=(x-6)^{2}-40 \\
& \text { B. } y=(x-6)^{2}+40 \\
& \text { С. } y=(x+3)^{2}-49 \\
& \text { D. } y=(x+3)^{2}+49
\end{aligned}
$$

Answer: C

1. Which of the following are the real values of $x$ that satisfy the equation $2 x^{2}-5 x-2=0$ ?
A. 1 and 4
B. $-\frac{5}{4}+\frac{\sqrt{41}}{4}$ and $\frac{5}{4}-\frac{\sqrt{41}}{4}$
C. $\frac{5}{4}+\frac{\sqrt{41}}{4}$ and $\frac{5}{4}-\frac{\sqrt{41}}{4}$
D. No real solutions

Answer: C

1. Given the equatin $y=-(2 x-4)^{2}+7$, which of the following statements is NOT true?
A. The vertex is $(4,7)$.
B. The $y$-intercept is $(0,-9)$.
C. The parabola opens diownward.
D. The graph crosses the $x$-axis at least one time.

Answer: A

## Systems Of Quadratic And Linear Equations

1. In the xy-plane, the graph of
$y+3 x=5 x^{2}+6$ and $y-6=2 x$ intersect at
points $(0,6)$ and $(a, b)$. What is the value of $b$ ?

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