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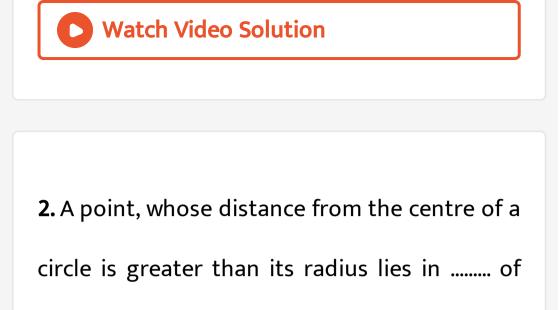
### MATHS

# BOOKS - KUMAR PRAKASHAN KENDRA MATHS (GUJRATI ENGLISH)

## CIRCLES

Exercise 10 1 Fill In The Blanks

**1.** The centre of a circle lies in ...... of the circle. (exterior/interior)



the circle. (exterior / interior)



3. The longest chord of a circle is a ...... of the

circle.



4. An arc is a ...... when its ends are the ends of

a diameter.



#### 5. Segment of a circle is the region between an

arc and ..... of the circle.

6. A circle divides the plane, on which it lies, in

..... parts.

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Exercise 10 1 True Or False

1. Line segment joining the centre to any point

on the circle is a radius of the circle

**2.** A cirecle has only finite number of equal chords.



**3.** If a circle is divided into three equal arcs,

each is a major arc.

4. A chord of a circle, which is twice as long as

its radius, is a diameter of the circle.



5. Sector is the region between the chord and

its corresponding arc.

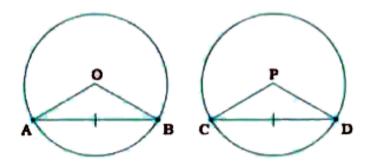


6. A circle is a plane figure.

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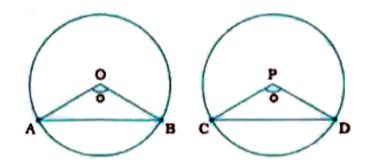
#### Exercise 10 2

**1.** Recall that two circles are congruent if they have the same radii. Proe that equal chords of congruent circles subtend equal angles at their centres.





**2.** Prove that if chords f congruent circles subtend equal angles at their centres, then the chords are equal.





#### Exercise 10 3

**1.** Draw different pairs of circles. How many points does each pair have in common ? What

is the maximum number of common points ?

Pairs of circles	No. of common points
$\bigcirc \bigcirc$	0
$\bigcirc\bigcirc$	1
$\bigcirc$	2
$\bigcirc$	1
$\bigcirc$	o

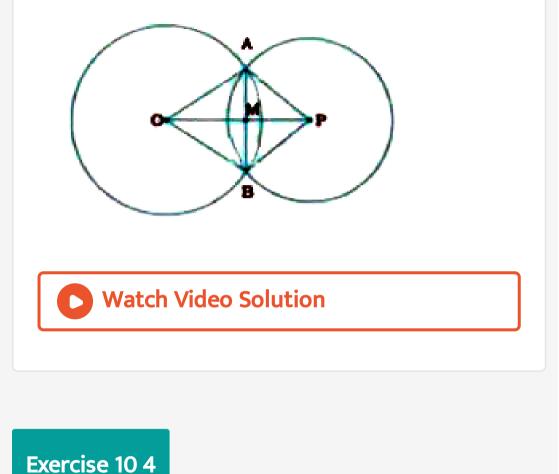


**2.** Suppose you ar given a circle. Give a construction to find its centre.

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**3.** If two circles intersect at two points, prove that their centres lie on the perpendicular

#### bisector of the common chord.



**1.** If the radii of two circles with centres o and  $O^{,}$  are 7 cm and 10 cm and the distance

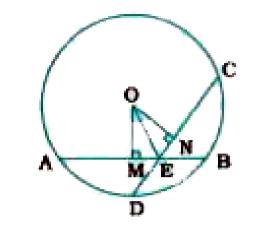
between their centres is 12 cm. In how many

point do the circle intersect?



**2.** If two equal chords of a circle intersect within the circle, prove that the segments of one chord are equal to correspondig

#### segments of the other chord.

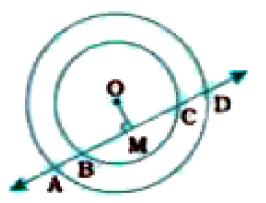




**3.** If two equal chords of a circle intersect within the circle, prove that the line joining the point of intersection to the centre makes equal angles with the chords.

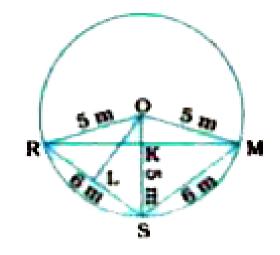


4. If a line intersects two concentric circles (circles with the same centre) with centre O at A,B,C and D), prove that AB = CD



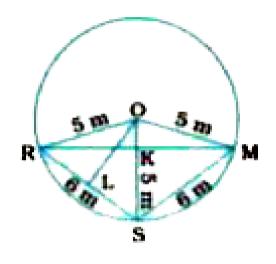
**5.** Three girls Reshma, Salma and Mandip are playing a game by standing on a circle of radius 5m drawn in a park. Reshma throws a ball to Salma, Salma to Mandip, Mandip to Reshma. If the distance between Reshma and Salma and between Salma and Mandip is 6 m each, what is the distance between Reshma

#### and Mandip?





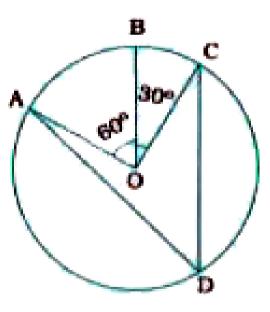
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#### Exercise 10 5

**1.** In the given figure, A, B and C are three points on a circle with centre O such that  $\angle BOC = 30^{\circ}$  and  $\angle AOB = 60^{\circ}$ . If D is a point on the circle other than the are ABC, find  $\angle ADC$ .



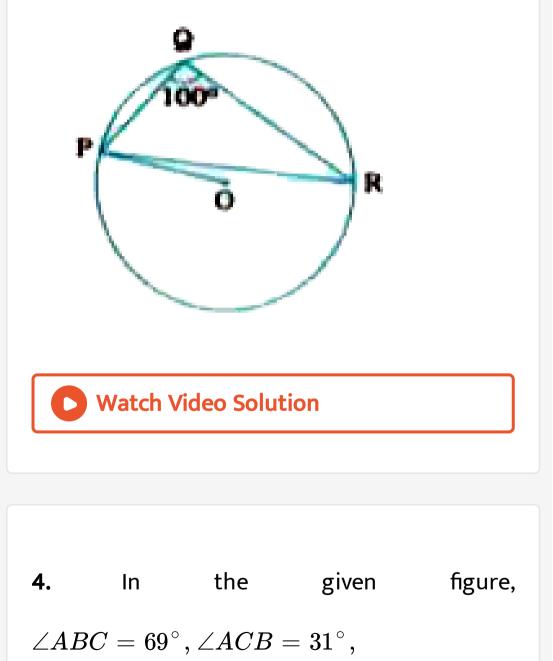


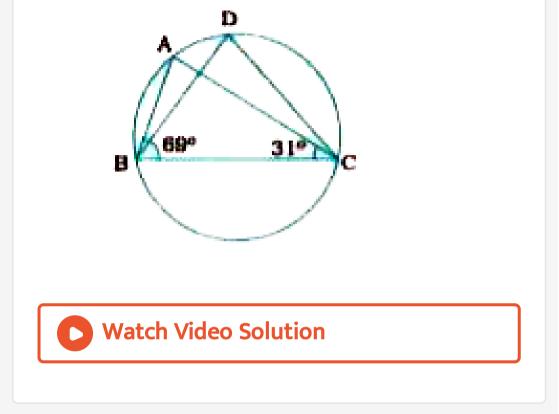
**2.** A chord of a circle is equal to the radius of the circle. Find the angle subtended by the chord at a point on the minor arc and also at a point on the major arc.

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**3.** In the given figure,  $\angle PQR = 100^{\circ}$ , where P, 9 and R are points on a circle with centre O.

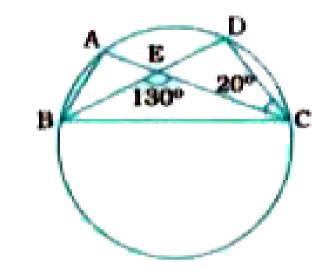
#### Find $\angle OPR$ .





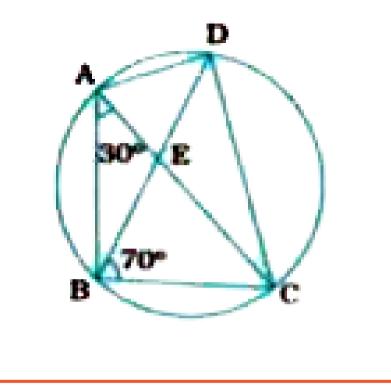
5. In the given figure, A, B, C and D are four points on a circle. AC and BD intersect at a point E such that  $\angle BEC = 130^{\circ}$  and  $\angle ECD = 20^{\circ}$ . Find

#### $\angle BAC.$





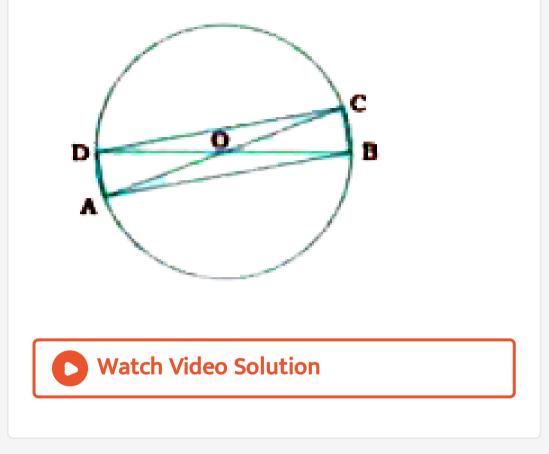
6. ABCD is a cyclic quadrilateral whose diagonals intersect at a point E. If  $\angle DBC = 70^{\circ}, \angle BACis30^{\circ},$  find  $\angle BCD$ . Further, if AB = BC, find  $\angle ECD$ .





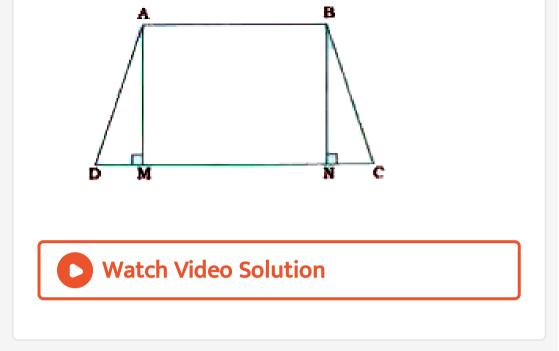
**7.** If diagonals of a cyclic quadrilateral are diameters of the circle through the vertices of

#### the quadrilateral, prove that it is a rectangle.



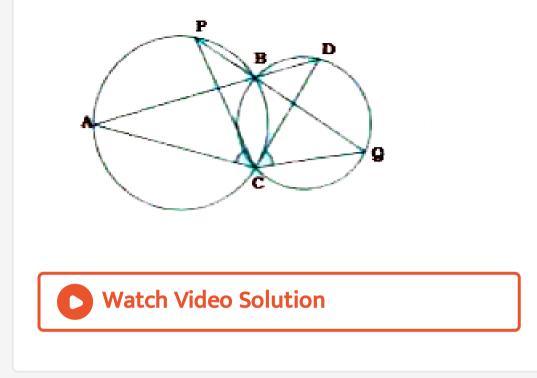
**8.** If the non-parallel sides of a trapezium are

equal, prove that it is cyclic.

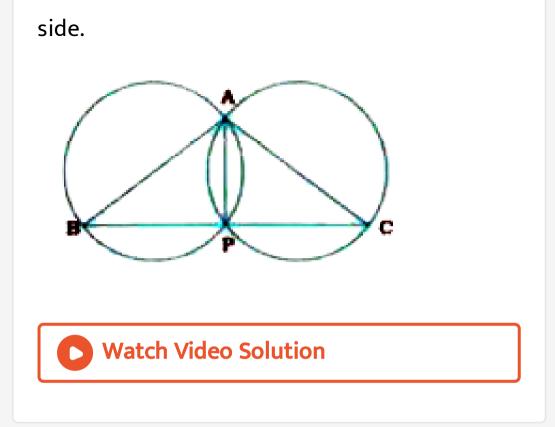


**9.** Two circles intersect at two points B and c. Through B, two line segments ABD and PBQ are drawn to intersect the circles at A, D and P, Q respectively (see the given figure). Prove

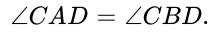
#### that $\angle ACP = \angle QCD$ .

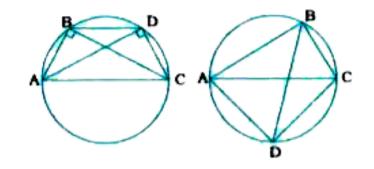


**10.** If circles are drawn taking two sides of a triangle as diameters, prove that the point of intersection of these circles lie on the third



# **11.** ABC and ADC are two right triangles with common hypotenuse AC. Prove that

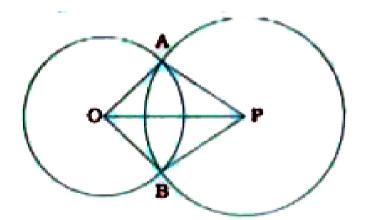






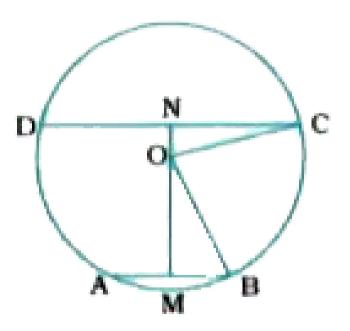
# **12.** Prove that a cyclic parallelogram is a rectangle.

**1.** Prove that the line segment joining the centres of two intersecting circles subtends equal angles at the two points of intersection.



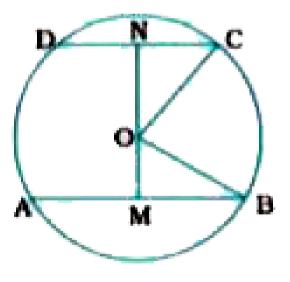


**2.** Two chords AB and CD of lengths 5 cm and 11 cm respectively of a circle are parallel to each other and are on opposite sides of its centre. If the distance between AB and CD is 6 cm, find the radius of the circle.





**3.** The lengths of two parallel chords of a circle are 6 cm and 8 cm. If the smaller chords is at distance 4 cm from the centre, what is the distance of the other chord from the centre ?







**1.** AB is a chord of a circle with centre o and diameter 20 cm. If AB = 12 cm, find the distance of AB from O.

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2. AB and CD are chords of a circle with centre

O. AB = 48 cm and its distance from centre o is

10 cm. If the distance of CD from centre O is 24

cm, find the length of CD.



**3.** In a circle with centre O. AB and CD are parallel chords lying on opposite sides of a diameter parallel to them. If AB = 30 cm, CD -48 cm and the distance between AB and CD is 27 cm, find the radius of the circle.

4. ABCD is a cyclic quadrilateral. If  $AD \mid \mid BC \text{ and } \angle B = 70^{\circ}$ , find the other angles of ABCD.

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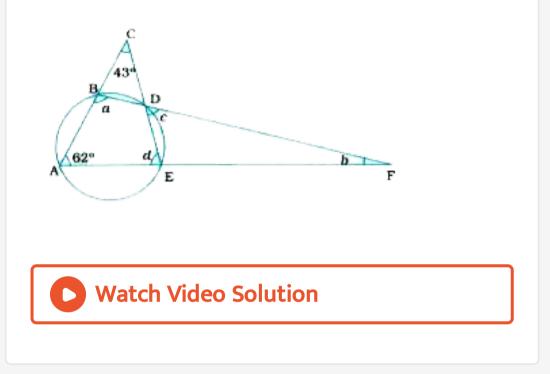
5. In cyclic quadrilateral ABCD. Diagonals AC and BD intersect at P. If  $\angle DBC = 70^{\circ}$  and  $\angle BAC = 30^{\circ}$ , find  $\angle BCD$ .

6. In a circle with centre O, AB is a diameter and ABCD is a cylical quadrilateral. If  $\angle ADC = 140^{\circ}$ , find  $\angle BAC$ .

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7. In the given figure,  $\angle BCD = 43^{\circ}$  and  $\angle BAE = 62^{\circ}$ . Find the

#### values of a,b,c and d.



#### Multiple Choice Questions Mcq S

**1.** In a circle with centre P. AB and CD are congruent chords. If  $ANGLEpab = 40^{\circ}$ ,

## THEN $ANGECPD = \dots$

A.  $40^{\circ}$ 

B.  $80^{\circ}$ 

C.  $100^{\circ}$ 

D.  $50^{\,\circ}$ 

Answer: C

**2.** In a circle with radius 5 cm, the length of a chord lying at distance 4 cm from the centre is ....... cm.

A. 3

B. 6

C. 12

D. 15

Answer: B



**3.** In a circle with radius 13 cm, the length of a chord is 24 cm. Then, the distance of the chord from the centre is ...... cm.

A. 10

B. 5

C. 12

D. 6.5

Answer: B



4. In a circle with radius 7 cm, the length of a

minor arc is always less than ...... cm.

A. 11

B. 22

C. 15

D.  $\pi$ 

**Answer: B** 

5. In a circle with centre P, AB is a minor arc. Point Ris a point other than A and B on major arc  $iFANGLEapb = 150^{\circ}$ . then  $\angle ARB =$ 

A.  $150^{\,\circ}$ 

B.  $75^{\circ}$ 

C.  $50^{\circ}$ 

D.  $100^{\,\circ}$ 

Answer: B

6. In a circle with centre P, AB is a minor arc. Point Ris a point other than A and B on major arc AB. If  $\angle ARB = 80^{\circ}$ , then  $\angle APB = \dots$ 

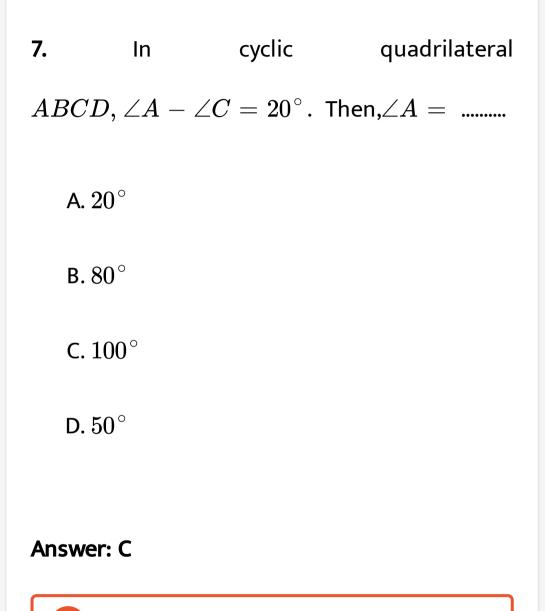
A.  $40^{\,\circ}$ 

B.  $80^{\circ}$ 

C.  $160^{\circ}$ 

D.  $60^{\,\circ}$ 

Answer: C



8. In cyclic quadrilateral PORS,  $7\angle P = 2\angle R$ .

Then,  $\angle P = \dots$ 

A.  $20^{\circ}$ 

B.  $40\,^\circ$ 

C.  $140^{\circ}$ 

D.  $100^{\circ}$ 

**Answer: B** 

**9.** The measures of two angles of a cyclic quadrilateral are  $40^{\circ}$  and  $110^{\circ}$  Then, the measures of other two angles of the quadrilateral are ......

- A.  $400^{\circ}$  and  $110^{\circ}$
- B.  $50^\circ\,$  and  $100^\circ\,$
- C. 140  $^\circ~$  and 70  $^\circ$
- D.  $20^{\circ}$  and  $120^{\circ}$

## Answer: C

10. In cyclic quadrilateral PQRS, $\angle SQR = 60^\circ ext{ and } \angle QPR = 20^\circ.$  Then, $\angle QRS$ =......

A.  $40^{\,\circ}$ 

B.  $60^{\circ}$ 

C.  $80^{\circ}$ 

D.  $100^{\,\circ}$ 

#### Answer: D

11. In cyclic quadrilateral ABCD,  $\angle CAB = 30^{\circ} \text{ and } \angle ABC = 100^{\circ}.$  Then,  $\angle ADB = ......$ 

A.  $50^{\,\circ}$ 

B.  $100^{\circ}$ 

C.  $75^{\circ}$ 

D.  $60^{\circ}$ 

#### **Answer: A**



**12.** Equilateral  $\Delta$  ABC is inscribed in a circle with centre P. Then,  $\angle BPC =$  .....

A.  $60^{\circ}$ 

B.  $90^{\circ}$ 

C.  $120^{\circ}$ 

D.  $75^{\,\circ}$ 

#### Answer: C



**13.** A ABC is inscribed in a circle with centre o and radius 5 cm and AC is a diameter of the circle. If AB = 8 cm, then BC = ...... cm.

A. 10

B. 8

C. 6

D. 15

#### Answer: C

14. In cyclic quadrilateral ABCD,  $\angle A = 70^{\circ}$  and  $\angle B + \angle X = 160^{\circ}$ . Then,  $\angle B =$  ......

A.  $35^{\,\circ}$ 

B.  $25^{\,\circ}$ 

C.  $50^{\circ}$ 

D.  $130^{\,\circ}$ 

#### Answer: C





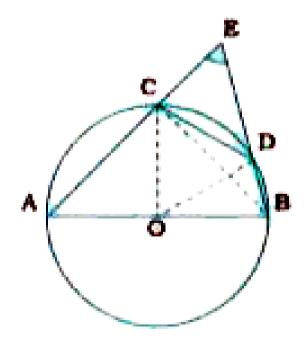
## Sum To Enrich Remamber

# 1. Give an arc of a circle, complete the circle,

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**2.** If two intersecting chords of a circle make equal angles with the diameter passing through their point of intersection, prove that the chords are equal.

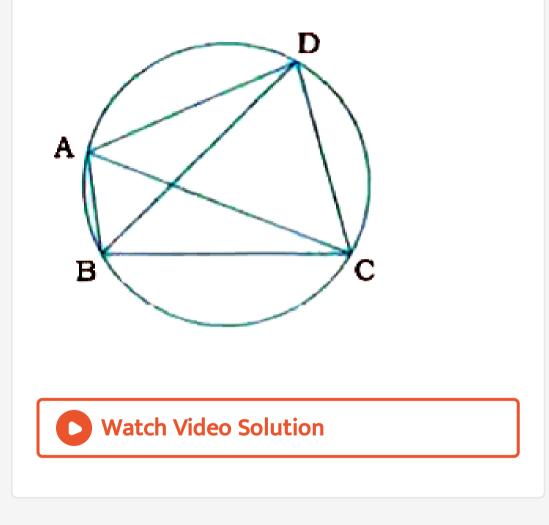
**3.** In the given figure, AB is a diameter of the circle, CD is chord equal to the radius of the circle, AC and BD when extended intersect at a point E. Prove that  $\angle AEB = 60^{\circ}$ .



4. In the given figure ABCD is a cyclic quadrilateral in which AC and BD are its diagonals.

 ${} \angle DBC = 55^\circ ~~{
m and} ~~{} \angle BAC = 45^\circ, ~~{
m find}$ 





**5.** Two circles intersect at two points A and B AD and AC are diameters to the two circles

Prove that B lies on the line segment DC.

