



## MATHS

### BOOKS - TELUGU ACADEMY MATHS (TELUGU ENGLISH)

#### INVERSE TRIGONOMETRIC FUNCTIONS

Spq

1. Prove that  $\sin^{-1} \frac{3}{5} + \cos^{-1} \frac{12}{13} = \cos^{-1} \frac{33}{65}$ .

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2. P.T  $\tan^{-1} \frac{1}{7} + \tan^{-1} \frac{1}{13} - \tan^{-1} \frac{2}{9} = 0$

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3. If  $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \pi$  then prove that  $x + y + z = xyz$ .



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4. If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \pi$ , then prove that  $x^4 + y^4 + z^4 + 4x^2y^2z^2 = 2(x^2y^2 + y^2z^2 + z^2x^2)$ .



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### Saq 1 D Star Q

1. Prove that  $\sin^{-1} \left( \frac{4}{5} \right) + \frac{\sin^{-1} 7}{25} = \frac{\sin^{-1} 117}{125}$ .



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2. Prove that  $\sin^{-1} \frac{3}{5} + \sin^{-1} \frac{8}{17} = \cos^{-1} \frac{36}{85}$

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3. P.T.  $\cos^{-1} \left( \frac{4}{5} \right) + \sin^{-1} \left( \frac{3}{\sqrt{34}} \right) = \tan^{-1} \left( \frac{27}{11} \right)$ .

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4. Find the value of  $\sin \left( \frac{\cos^{-1} 3}{5} + \frac{\cos^{-1} 12}{13} \right)$

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5. Find  $\cos \left( \frac{\sin^{-1} 3}{5} + \frac{\sin^{-1} 5}{13} \right)$

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6. Find the value of  $\tan\left(\frac{\sin^{-1} 3}{5} + \frac{\cos^{-1} 5}{\sqrt{34}}\right)$ .

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7. Find the value of  $\tan\left(\frac{\cos^{-1} 4}{5} + \frac{\tan^{-1} 2}{3}\right)$

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8. Show that  $\cot\left(\sin^{-1} \sqrt{\frac{13}{17}}\right) = \sin\left(\tan^{-1} \frac{2}{3}\right)$ .

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9. Show that  $\cos\left(2 \tan^{-1} \frac{1}{7}\right) = \sin\left(2 \tan^{-1} \frac{3}{4}\right)$

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10. Prove that  $\cos\left(2\frac{\tan^{-1} 1}{7}\right) = \sin\left(4\frac{\tan^{-1} 1}{3}\right)$

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11. Prove that  $\tan^{-1}\left(\frac{1}{2}\right) + \tan^{-1}\left(\frac{1}{5}\right) + \tan^{-1}\left(\frac{1}{8}\right) = \frac{\pi}{4}$

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12. Show that  $\frac{\tan^{-1} 3}{4} + \frac{\tan^{-1} 3}{5} - \frac{\tan^{-1} 8}{19} = \frac{\pi}{4}$ .

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13. Show that  $\frac{\tan^{-1} 1}{7} + \frac{\tan^{-1} 1}{8} = \frac{\cot^{-1} 201}{43} + \cot^{-1} 18$

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14. Prove that  $\cot^{-1} 9 + \operatorname{cosec}^{-1} \frac{\sqrt{41}}{4} = \frac{\pi}{4}$ .

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15. Prove that  $\sin^{-1} \frac{4}{5} + \sin^{-1} \frac{5}{13} + \sin^{-1} \left( \frac{16}{65} \right) = \frac{\pi}{2}$

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16. Prove that  $\sin^{-1} \left( \frac{4}{5} \right) + 2 \tan^{-1} \left( \frac{1}{3} \right) = \frac{\pi}{2}$ .

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17. Prove that  $\sin \left[ \frac{\cot^{-1}(2x)}{1-x^2} + \cos^{-1} \left( \frac{1-x^2}{1+x^2} \right) \right] = 1$ .

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18. Show that  $\tan \left[ 2 \tan^{-1} \left( \frac{\sqrt{5} - 1}{2} \right) \right] = 2$

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19. If  $\sin^{-1} x - \cos^{-1} x = \frac{\pi}{6}$  then find x.

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20. If  $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \frac{\pi}{2}$ , then prove that  $xy + yz + zx = 1$

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21. If  $\sin^{-1}(x) + \sin^{-1}(y) + \sin^{-1}(z) = \pi$ , prove that  $x\sqrt{1-x^2} + y\sqrt{1-y^2} + z\sqrt{1-z^2} = 2xyz$ .

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22. If  $\cos^{-1} p + \cos^{-1} q + \cos^{-1} r = \pi$  then,

*P. T.*  $p^2 + q^2 + r^2 = 2pqr = 1$

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Saq 2 D Hard Q 3 D Mis Q

1. Prove that  $\cos [\tan^{-1} \{ \sin(\cot^{-1} x) \}] = \sqrt{\frac{x^2 + 1}{x^2 + 2}}$

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2. If  $\frac{\sin^{-1}(2p)}{1 + p^2} - \cos^{-1} \left( \frac{1 - q^2}{1 + q^2} \right) = \frac{\tan^{-1}(2x)}{1 - x^2}$ , then prove that  $x = \frac{p - q}{1 + pq}$

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3. If  $a, b, c$  are distinct non-zero real numbers having the same sign.

Prove that

$$\cot^{-1}\left(\frac{ab+1}{a-b}\right) + \cot^{-1}\left(\frac{bc+1}{b-c}\right) + \cot^{-1}\left(\frac{ca+1}{c-a}\right) = \pi \text{ ( or ) } 2\pi$$

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4. Solve :  $\sin^{-1}\left(\frac{5}{x}\right) + \sin^{-1}\left(\frac{12}{x}\right) = \frac{\pi}{2}$

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5. Solve  $\sin^{-1} x + \sin^{-1} 2x = \frac{\pi}{3}$ .

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6. Prove that

$$\tan\left\{\frac{\pi}{4} + \frac{1}{2}\cos^{-1}\left(\frac{a}{b}\right)\right\} + \tan\left\{\left(\frac{\pi}{4} - \frac{1}{2}\frac{\cos^{-1}a}{b}\right)\right\} = \frac{2b}{a}.$$

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7. Solve

$$3\sin^{-1}\left(\frac{2x}{1+x^2}\right) - 4\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right) + 2\tan^{-1}\left(\frac{2x}{1-x^2}\right) = \frac{\pi}{3}$$

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8. Show that  $\sec^2(\tan^{-1} 2) + \operatorname{cosec}^2(\cot^{-1} 2) = 10$

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9. Prove that  $2\sin^{-1}\left(\frac{3}{5}\right) - \cos^{-1}\frac{5}{13} = \cos^{-1}\left(\frac{323}{325}\right)$ .

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10. If  $\alpha = \tan^{-1} \left( \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \right)$  then prove that  $x^2 = \sin 2\alpha$ .

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11. Solve  $\sin^{-1} \frac{3x}{5} + \sin^{-1} \frac{4x}{5} = \sin^{-1} x$

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