



MATHS

BOOKS - TELUGU ACADEMY MATHS (TELUGU ENGLISH)

SOLVED MODEL PAPER - 4

Very Short Answer Questions

1. Find the value of k , if the straight lines $y - 3kx + 4 = 0$ and $(2k - 1)x + (8k - 1)y - 6 = 0$ are perpendicular.

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2. Find the equation of the straight line passing through the point $(-2, 4)$ and making intercepts, whose sum is zero.

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3. Find the ratio in which the point $C(6, -17, -4)$ divides the line segment joining the points $A(2, 3, 4)$ and $B(3, -2, 2)$.

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4. Reduce the equation $x + 2y - 3z - 6 = 0$ of the plane to the normal form.

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5. Evaluate $\lim_{x \rightarrow 0} \frac{\cos ax - \cos bx}{x^2}$

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6. Compute $\lim_{x \rightarrow \infty} (\sqrt{x+1} - \sqrt{x})$

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7. If $y = \log(\cosh 2x)$, then find $\frac{dy}{dx}$.

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8. Find the derivative of $\tan^{-1}\left(\frac{a-x}{1+ax}\right)$

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9. If $y = x^2 + x$, $x = 10$, $\Delta x = 0.1$, then find Δy and dy

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10. State Rolle's Theorem.



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Short Answer Questions

1. Find the equation of locus of P if

$$A = (4, 0), B(-4, 0) \text{ and } |PA - PB| = 4$$



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2. When the axes rotated through an angle $\frac{\pi}{4}$,
find the transformed equation of
 $3x^2 + 10xy + 3y^2 = 9$.

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3. If the straight lines $ax + by + c = 0$, $bx + cy + a = 0$
and $cx + ay + b = 0$ are concurrent, then prove that
 $a^3 + b^3 + c^3 = 3abc$.

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4. If f is given by $f(x) = \begin{cases} k^2x - k & \text{if } x \geq 1 \\ 2 & \text{if } x < 1 \end{cases}$ is a

continuous function on \mathbb{R} , then find k .



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5. Find the derivative of $\sin 2x$ from the first principles.



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6. Show that at any point (x, y) on the curve $y = b^{\frac{x}{a}}$, the length of the subtangent is a constant and the

length of the subnormal is $\frac{y^2}{a}$.



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7. A container is in the shape of an inverted cone has height 8m and radius 6m at the top. If it is filled with water at the rate of $2m^3/\text{minute}$, how fast is the height of water changing when the level is 4m?



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Long Answer Questions

1. Find the circumcentre of the triangle whose sides are given by

$$x + y + 2 = 0, 5x - y - 2 = 0 \text{ and } x - 2y + 5 = 0$$



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2. If $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$ represents two parallel lines then prove that $h^2 = ab$.



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3. If $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$

represents two parallel lines then prove that

$$af^2 = bg^2.$$



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4. If $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$

represents two parallel lines then prove that the

distance between the parallel lines is

$$2\sqrt{\frac{g^2 - ac}{a(a + b)}} \quad \text{or} \quad 2\sqrt{\frac{f^2 - bc}{b(a + b)}}.$$



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5. Find the value if k , if the lines joining the origin with the points of intersection of the curve $2x^2 - 2xy + 3y^2 + 2x - y - 1 = 0$ and the $x + 2y = k$ are mutually perpendicular .



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6. If a line makes angles $\alpha, \beta, \lambda, \delta$ with the four diagonals of a cube, then show that $\cos^2 \alpha + \cos^2 \beta + \cos^2 \lambda + \cos^2 \delta = \frac{4}{3}$.



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7. Find the derivative $\frac{dy}{dx}$ of the function

$$y = \frac{(1 - 2x)^{2/3}(1 + 3x)^{-3/4}}{(1 - 6x)^{5/6}(1 + 7x)^{-6/7}}.$$



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8. Find the angle between the curves

$$x + y + 2 = 0 \text{ and } x^2 + y^2 - 10y = 0$$



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9. A window is in the shape of a rectangle surmounted by a semi-circle. If the perimeter of the

window be 20 feet then find the maximum area.



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