

## MATHS

### BOOKS - VK JAISWAL MATHS (HINGLISH)

### VECTOR & 3DIMENSIONAL GEOMETRY

#### Exercise 1 Single Choice Problems

1. If  $ax + by + cz = p$  , then minimum value of  $x^2 + y^2 + z^2$  is

$\left(\frac{p}{a+b+c}\right)^2$  (b)  $\frac{p^2}{a^2 + b^2 + c^2}$   $\frac{a^2 + b^2 + c^2}{p^2}$  (d)  $\left(\frac{a+b+c}{p}\right)^2$

A.  $\left(\frac{p}{a+b+c}\right)^2$

B.  $\frac{p^2}{a^2 + b^2 + c^2}$

C.  $\frac{a^2 + b^2 + c^2}{p^2}$

D. 0

**Answer: B**



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2. If the angle between the vectors  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{3}$  and the area of the triangle with adjacent sides parallel to  $\vec{a}$  and  $\vec{b}$  is 3 is

A.  $\sqrt{3}$

B.  $2\sqrt{3}$

C.  $4\sqrt{3}$

D.  $\frac{\sqrt{3}}{2}$

**Answer: B**



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3. A straight line L cuts the sides AB, AC, AD of a parallelogram ABCD at

$B_1, C_1, D_1$

respectively.

If

$\vec{AB}_1 = \lambda_1 \vec{AB}$ ,  $\vec{AD}_1 = \lambda_2 \vec{AD}$  and  $\vec{AC}_1 = \lambda_3 \vec{AC}$ , then  $\frac{1}{\lambda_3}$  equal to

A.  $\lambda_1, \lambda_3$  and  $\lambda_2$  are in AP

B.  $\lambda_1, \lambda_3$  and  $\lambda_2$  are in GP

C.  $\lambda_1, \lambda_3$  and  $\lambda_2$  are in HP

D.  $\lambda_1 + \lambda_2 + \lambda_3 = 0$

**Answer: C**



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4. Let  $\vec{a} = 2\hat{i} + \hat{j} - 2\hat{k}$  and  $\vec{b} = \hat{i} + \hat{j}$ . If  $\vec{c}$  is a vector such that  $\vec{a} \cdot \vec{c} = |\vec{c}|$ ,  $|\vec{c} - \vec{a}| = 2\sqrt{2}$  and the angle between  $\vec{a} \times \vec{b}$  and  $\vec{c}$  is  $30^\circ$  then  $\left| \left( \vec{a} \times \vec{b} \right) \times \vec{c} \right|$  is equal to :

A.  $\frac{2}{3}$

B.  $\frac{3}{2}$

C. 2

D. 3

**Answer: B**

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5. If acute angle between the line  $\vec{r} = \hat{i} + 2\hat{j} + \lambda(4\hat{i} - 3\hat{k})$  and  $xy$ -plane is  $\theta_1$  and acute angle between planes  $x + 2y = 0$  and  $2x + y = 0$  is  $\theta_2$ , then  $(\cos^2 \theta_1 + \sin^2 \theta_2)$  equals to :

A. 1

B.  $\frac{1}{4}$

C.  $\frac{2}{3}$

D.  $\frac{3}{4}$

**Answer: A**

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6. If  $a, b, c, x, y, z$  are real and  $a^2 + b^2 + c^2 = 25, x^2 + y^2 + z^2 = 36$  and  $ax + by + cz = 30$ , then  $\frac{a + b + c}{x + y + z}$  is equal to :
- A. 1
- B.  $\frac{6}{5}$
- C.  $\frac{5}{6}$
- D.  $\frac{3}{4}$

Answer: C

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7. If  $\vec{a}$  and  $\vec{b}$  are non-zero, non-collinear vectors such that  $|\vec{a}| = 2, \vec{a} \cdot \vec{b} = 1$  and angle between  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{3}$ . If  $\vec{r}$  is any vector such that  $\vec{r} \cdot \vec{a} = 2, \vec{r} \cdot \vec{b} = 8, \left(\vec{r} + 2\vec{a} - 10\vec{b}\right) \cdot \left(\vec{a} \times \vec{b}\right) = 4\sqrt{3}$  and satisfy to  $\vec{r} + 2\vec{a} - 10\vec{b} = \lambda\left(\vec{a} \times \vec{b}\right)$ , then  $\lambda$  is equal to :

A.  $\frac{1}{2}$

B. 2

C.  $\frac{1}{4}$

D. None of these

**Answer: D**



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8. Given  $\vec{a} = 3\hat{i} + 2\hat{j} + 4\hat{k}$ ,  $\vec{b} = 2(\hat{i} + \hat{k})$  and  $\vec{c} = 4\hat{i} + 2\hat{j} + 3\hat{k}$ .

Find for what number of distinct values of  $\alpha$  the equation  $x\vec{a} + y\vec{b} + z\vec{c} = \alpha(x\hat{i} + y\hat{j} + z\hat{k})$  has non-trivial solution  $(x, y, z)$ .

A. -1

B. 4

C. 7

D. 8

Answer: C



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9. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} - \hat{k}$ , then the value of

$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix} \text{ is equal to :}$$

A. 2

B. 4

C. 16

D. 64

Answer: C



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10.  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $|\vec{a}| = 1$ ,  $|\vec{b}| = 4$  and  $\vec{a} \cdot \text{Vecb} = 2$ . If  $\vec{c} = (2\vec{a} \times \vec{b}) - 3\vec{b}$  then find angle between  $\vec{b}$  and  $\vec{c}$ .

A.  $\frac{\pi}{6}$

B.  $\frac{\pi}{3}$

C.  $\frac{2\pi}{3}$

D.  $\frac{5\pi}{3}$

Answer: D



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11. If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors, then the value of  $|\vec{a} - 2\vec{b}|^2 + |\vec{b} - 2\vec{c}|^2 + |\vec{c} - 2\vec{a}|^2$  does not exceed to :

A. 9

B. 12



C. 18

D. 21

**Answer: D**



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12. The adjacent side vectors  $\vec{OA}$  and  $\vec{OB}$  of a rectangle OACB are  $\vec{a}$  and  $\vec{b}$  respectively, where O is the origin. If  $16|\vec{a} \times \vec{b}| = 3\left(|\vec{a}| + |\vec{b}|\right)^2$  and  $\theta$  be the acute angle between the diagonals OC and AB then the value of  $\cos(\theta/2)$  is :

A.  $\frac{1}{\sqrt{2}}$

B.  $\frac{1}{2}$

C.  $\frac{1}{\sqrt{3}}$

D.  $\frac{1}{3}$

**Answer: D**

13. The vectors  $\vec{AB} = 3\hat{i} + 4\hat{k}$  and  $\vec{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are the sides of a triangle ABC. The length of the median through A is (A)  $\sqrt{72}$  (B)  $\sqrt{33}$  (C)  $\sqrt{2880}$  (D)  $\sqrt{18}$

A.  $\sqrt{288}$

B.  $\sqrt{72}$

C.  $\sqrt{33}$

D.  $\sqrt{18}$

**Answer: C**

14. If  $\vec{a} = 2\hat{i} + \lambda\hat{j} + 3\hat{k}$ ,  $\vec{b} = 3\hat{i} + 3\hat{j} + 5\hat{k}$ ,  $\vec{c} = \lambda\hat{i} + 2\hat{j} + 2\hat{k}$  are linearly dependent vectors, then the number of possible values of  $\lambda$  is :

A. 0

B. 1

C. 2

D. More than 2

**Answer: C**



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15. The scalar triple product

$\left[ \vec{a} + \vec{b} - \vec{c} \quad \vec{b} + \vec{c} - \vec{a} \quad \vec{c} + \vec{a} - \vec{b} \right]$  is equal to :

A. 0

B.  $\left[ \vec{a} \vec{b} \vec{c} \right]$

C.  $2 \left[ \vec{a} \vec{b} \vec{c} \right]$

D.  $4 \left[ \vec{a} \vec{b} \vec{c} \right]$

**Answer: D**



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16. If  $\hat{a}$  and  $\hat{b}$  are unit vectors then the vector defined as  $\vec{V} = (\hat{a} \times \hat{b}) \times (\hat{a} + \hat{b})$  is collinear to the vector :

- A.  $\hat{a} + \hat{b}$
- B.  $\hat{b} - \hat{a}$
- C.  $2\hat{a} - \hat{b}$
- D.  $\hat{a} + 2\hat{b}$

**Answer: B**

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17. The sine of angle formed by the lateral face ADC and plane of the base ABC of the tetrahedron ABCD, where  $A = (3, -2, 1)$ ,  $B = (3, 1, 5)$ ,  $C = (4, 0, 3)$  and  $D = (1, 0, 0)$ , is :

- A.  $\frac{2}{\sqrt{29}}$

B.  $\frac{5}{\sqrt{29}}$

C.  $\frac{3\sqrt{3}}{\sqrt{29}}$

D.  $\frac{-2}{\sqrt{29}}$

**Answer: B**



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18. Let  $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}$ ,  $r = 1, 2, 3$  be three mutually

perpendicular unit vectors, then the value of  $\begin{vmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$  is equal to :

A. 0

B.  $\pm 1$

C.  $\pm 2$

D.  $\pm 4$

**Answer: B**



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19. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and  $\vec{r}$  be any arbitrary vector. Then

$(\vec{a} \times \vec{b}) \times (\vec{r} \times \vec{c}) + (\vec{b} \times \vec{c}) \times (\vec{r} \times \vec{a}) + (\vec{c} \times \vec{a}) \times (\vec{r} \times \vec{b})$  is always equal to  $\left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$  b.  $2 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$  c.  $3 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$  d. none of these

A.  $\left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$

B.  $2 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$

C.  $4 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$

D.  $\vec{0}$

**Answer: B**



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20. E and F are the interior points on the sides BC and CD of a parallelogram ABCD. Let  $\overrightarrow{BE} = 4\overrightarrow{EC}$  and  $\overrightarrow{CF} = 4\overrightarrow{FD}$ . If the line EF meets the diagonal AC in G, then  $\overrightarrow{AG} = \lambda\overrightarrow{AC}$ , where  $\lambda$  is equal to :

- A.  $\frac{1}{3}$
- B.  $\frac{21}{25}$
- C.  $\frac{7}{13}$
- D.  $\frac{21}{5}$

**Answer: B**



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21. If  $\hat{a}$ ,  $\hat{b}$  are unit vectors and  $\hat{c}$  is such that  $\hat{c} = \hat{a} \times \hat{c} + \hat{b}$ , then the maximum value of  $\left[ \begin{matrix} \hat{a} & \hat{b} & \hat{c} \end{matrix} \right]$  is :

- A. 1
- B.  $\frac{1}{2}$

C. 2

D.  $\frac{3}{2}$

**Answer: B**



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22. Consider the matrices  $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 1 & 2 \\ 1 & -1 & 1 \end{bmatrix}$   $B = \begin{bmatrix} 2 & 1 & 3 \\ 4 & 1 & -1 \\ 2 & 2 & 3 \end{bmatrix}$   
 $C = \begin{bmatrix} 14 \\ 12 \\ 2 \end{bmatrix}$   $D = \begin{bmatrix} 13 \\ 11 \\ 14 \end{bmatrix}$ . Now  $x = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$  is such that solutions of equation  $AX = C$  and  $BX = D$  represent two points L and M respectively in 3 dimensional space. If  $L'$  and  $M'$  are their reflections of L and M in the plane  $x+y+z=9$  then find coordinates of  $L, M, L', M'$

A. (3, 4, 2)

B. (5, 3, 4)

C. (7, 2, 3)

D. (1, 5, 6)



**Answer: A**



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23. The value of  $\alpha$  for which point  $M(\alpha\hat{i} + 2\hat{j} + \hat{k})$ , lie in the plane containing three points  $A(\hat{i} + \hat{j} + \hat{k})$  and  $C(3\hat{i} - \hat{k})$  is :

A. 1

B. 2

C.  $\frac{1}{2}$

D.  $-\frac{1}{2}$

**Answer: B**



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24. Q is the image of point P(1, -2, 3) with respect to the plane  $x - y + z = 7$ . The distance of Q from the origin is.

A.  $\sqrt{\frac{70}{3}}$

B.  $\frac{1}{2}\sqrt{\frac{70}{3}}$

C.  $\sqrt{\frac{35}{3}}$

D.  $\sqrt{\frac{15}{2}}$

**Answer: A**



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25.  $\hat{a}$ ,  $\hat{b}$  and  $\hat{a} - \hat{b}$  are unit vectors. The volume of the parallelepiped, formed with  $\hat{a}$ ,  $\hat{b}$  and  $\hat{a} \times \hat{b}$  as coterminous edges is :

A. 1

B.  $\frac{1}{4}$

C.  $\frac{2}{3}$

D.  $\frac{3}{4}$

**Answer: D**

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26. A line passing through  $P(3, 7, 1)$  and  $R(2, 5, 7)$  meet the plane  $3x + 2y + 11z - 9 = 0$  at  $Q$ . Then  $PQ$  is equal to :

- A.  $\frac{5\sqrt{41}}{59}$
- B.  $\frac{\sqrt{41}}{59}$
- C.  $\frac{50\sqrt{41}}{59}$
- D.  $\frac{25\sqrt{41}}{59}$

**Answer: D**

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27. Let  $\vec{a}, \vec{b}, \vec{c}$  be three non-zero non coplanar vectors and  $\vec{p}, \vec{q}$  and  $\vec{r}$  be three vectors given by  $\vec{p} = \vec{a} + \vec{b} - 2\vec{c}$ ,  $\vec{q} = 3\vec{a} - 2\vec{b} + \vec{c}$  and  $\vec{r} = \vec{a} - 4\vec{b} + 2\vec{c}$

If the volume of the parallelopiped determined by  $\vec{a}, \vec{b}$  and  $\vec{c}$  is  $V_1$  and

that of the parallelepiped determined by  $\vec{a}$ ,  $\vec{q}$  and  $\vec{r}$  is  $V_2$ , then

$$V_2 : V_1 =$$

- A. 10
- B. 15
- C. 20
- D. None of these

**Answer: B**



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28. If the two lines represented by  $x + ay = b, z + cy = d$  and  $x = a'y + b', z = c'y + d'$  be perpendicular to each other, then the value of  $aa' + cc'$  is :

- A. 1
- B. 2
- C. 3

D. 4

**Answer: A**

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**29.** The distance between the line

$\vec{r} = 2\hat{i} - 2\hat{j} + 3\hat{k} + \lambda(\hat{i} - \hat{j} + 4\hat{k})$  and the plane

$\vec{r} \cdot (\hat{i} + 5\hat{j} + \hat{k}) = 5$  is

A.  $\frac{10}{9}$

B.  $\frac{10}{3\sqrt{3}}$

C.  $\frac{3}{10}$

D.  $\frac{10}{3}$

**Answer: B**

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30. If  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$ , where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are any three vectors such that  $\vec{a} \cdot \vec{b} \neq 0$ ,  $\vec{b} \cdot \vec{c} \neq 0$ , then  $\vec{a}$  and  $\vec{c}$  are :

A. Inclined at an angle of  $\frac{\pi}{3}$

B. Inclined at an angle of  $\frac{\pi}{6}$

C. Perpendicular

D. Parallel

**Answer: D**



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31. Let  $\vec{r}$  be position vector of variable point in cartesian plane OXY such that  $\vec{r} \cdot (\vec{r} + 6\hat{j}) = 7$  cuts the co-ordinate axes at four distinct points, then the area of the quadrilateral formed by joining these points is :

A.  $4\sqrt{7}$

B.  $6\sqrt{7}$

C.  $7\sqrt{7}$

D.  $8\sqrt{7}$

**Answer: D**

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32. If  $|\vec{a}| = 2$ ,  $|\vec{b}| = 5$  and  $\vec{a} \cdot \vec{b} = 0$ , then

$\vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \vec{b} \right) \right) \right) \right) \right) \right) \right)$  is equal to :

A.  $64\vec{a}$

B.  $64\vec{b}$

C.  $-64\vec{a}$

D.  $-64\vec{b}$

**Answer: D**

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33. If O (origin) is a point inside the triangle PQR such that  $\vec{OP} + k_1\vec{OQ} + k_2\vec{OR} = 0$ , where  $k_1, k_2$  are constants such that  $\frac{\text{Area}(\Delta PQR)}{\text{Area}(\Delta OQR)} = 4$ , then the value of  $k_1 + k_2$  is :

- A. 2
- B. 3
- C. 4
- D. 5

**Answer: B**



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34. Let PQ and QR be diagonals of adjacent faces of a rectangular box, with its centre at O. If  $\angle QOR, \angle ROP$  and  $\angle POQ$  are  $\theta, \phi$  and  $\Psi$  respectively then the value of ' $\cos \theta + \cos \phi + \cos \Psi$ ' is :

- A. -2



B.  $-\sqrt{3}$

C. -1

D. 0

Answer: C



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35. The value of  $\begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{p} & \vec{b} \cdot \vec{p} & \vec{c} \cdot \vec{p} \\ \vec{a} \cdot \vec{q} & \vec{b} \cdot \vec{q} & \vec{c} \cdot \vec{q} \end{vmatrix}$  is equal to :

A.  $(\vec{p} \times \vec{q}) \left[ \vec{a} \times \vec{b} \quad \vec{b} \times \vec{c} \quad \vec{c} \times \vec{a} \right]$

B.  $2(\vec{p} \times \vec{q}) \left[ \vec{a} \times \vec{b} \quad \vec{b} \times \vec{c} \quad \vec{c} \times \vec{a} \right]$

C.  $4(\vec{p} \times \vec{q}) \left[ \vec{a} \times \vec{b} \quad \vec{b} \times \vec{c} \quad \vec{c} \times \vec{a} \right]$

D.  $(\vec{p} \times \vec{q}) \sqrt{\left[ \vec{a} \times \vec{b} \quad \vec{b} \times \vec{c} \quad \vec{c} \times \vec{a} \right]}$

Answer: D



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36.

If

$$\vec{r} = a(\vec{m} \times \vec{n}) + b(\vec{n} \times \vec{l}) + c(\vec{l} \times \vec{m}) \text{ and } \left[ \vec{l} \vec{m} \vec{n} \right] = 4, \text{ find}$$

:

A.  $\frac{1}{4}$

B.  $\frac{1}{2}$

C. 1

D. 2

Answer: A



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37. The volume of tetrahedron, for which three co-terminus edges are

$$\vec{a} - \vec{b}, \vec{b} + 2\vec{c} \text{ and } 3\vec{a} - \vec{c} \text{ is :}$$

A. 6k

B. 7k

C. 30k

D. 42k

**Answer: D**



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**38.** The equation of a plane passing through the line of intersection of the planes :

$x + 2y + z - 10 = 0$  and  $3x + y - z = 5$  and passing through the origin is :

A.  $5x + 3z = 0$

B.  $5x - 3z = 0$

C.  $5x + 4y + 3z = 0$

D.  $5x - 4y + 3z = 0$

**Answer: B**



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**39.** Find the locus of a point whose distance from x-axis is twice the distance from the point  $(1, -1, 2)$  :

A.  $y^2 + 2x - 2y - 4z + 6 = 0$

B.  $x^2 + 2x - 2y - 4z + 6 = 0$

C.  $x^2 - 2x + 2y - 4z + 6 = 0$

D.  $z^2 - 2x + 2y - 4z + 6 = 0$

**Answer: C**



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**Exercise 2 One Or More Than One Answer Is Are Correct**

1. If equation of three lines are :

$$\frac{x}{1} = \frac{y}{2} = \frac{z}{3}, \frac{x}{2} = \frac{y}{1} = \frac{z}{3} \text{ and } \frac{x-1}{1} = \frac{2-y}{1} = \frac{z-3}{0}, \text{ then}$$

which of the following statement(s) is/are correct ?

- A. Triangle formed by the line is equilateral
- B. Triangle formed by the lines is isosceles
- C. Equation of the plane containing the lines is  $x + y = z$
- D. Area of the triangle formed by the lines is  $\frac{3\sqrt{3}}{2}$

**Answer: B::C::D**



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2.

If

$$\vec{a} = \hat{i} + 6\hat{j} + 3\hat{k}, \vec{b} = 3\hat{i} + 2\hat{j} + \hat{k} \text{ and } \vec{c} = (\alpha + 1)\hat{i} + (\beta - 1)\hat{j} + \hat{k}$$

are linearly dependent vectors and  $|\vec{c}| = \sqrt{6}$ , then the possible value(s)

of  $(\alpha + \beta)$  can be :

A. 1

B. 2

C. 3

D. 4

**Answer: A:C**



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3. Consider the lines:

$$L_1: \frac{x-2}{1} = \frac{y-1}{7} = \frac{z+2}{-5}, L_2: x-4 = y+3 = -z$$

Then which of the following is/are correct ? (A) Point of intersection of

$L_1$  and  $L_2$  is  $(1, -6, 3)$

A. Point of intersection of  $L_1$  and  $L_2$  is  $(1, -6, 3)$

B. Equation of plane containing  $L_1$  and  $L_2$  is  $x + 2y + 3z + 2 = 0$

C. Acute angle between  $L_1$  and  $L_2$  is  $\cot^{-1}\left(\frac{13}{15}\right)$

D. Equation of plane containing  $L_1$  and  $L_2$  is  $x + 2y + 2z + 3 = 0$

Answer: A::B::C



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4. Let  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  be three unit vectors such that  $\hat{a} = \hat{b} + (\hat{b} \times \hat{c})$ , then the possible value(s) of  $|\hat{a} + \hat{b} + \hat{c}|^2$  can be :

A. 1

B. 4

C. 16

D. 9

Answer: A::D



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5. The value(s) of  $\mu$  for which the straight lines

$\vec{r} = 3\hat{i} - 2\hat{j} - 4\hat{k} + \lambda_1(\hat{i} - \hat{j} + \mu\hat{k})$  and

$\vec{r} = 5\hat{i} - 2\hat{j} + \hat{k} + \lambda_2(\hat{i} + \mu\hat{j} + 2\hat{k})$  are coplanar is/are :

A.  $\frac{5 + \sqrt{33}}{4}$

B.  $\frac{-5 + \sqrt{33}}{4}$

C.  $\frac{5 - \sqrt{33}}{4}$

D.  $\frac{-5 - \sqrt{33}}{4}$

**Answer: A::C**



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**6.**

If

$$\hat{i} \times [(\vec{a} - \hat{j}) \times \hat{i}] + \hat{j} \times [(\vec{a} - \hat{k}) \times \hat{j}] + \hat{k} \times [(\vec{a} - \hat{i}) \times \hat{k}] = 0 \text{ and}$$

, then :

A.  $x + y = 1$

B.  $y + z = \frac{1}{2}$

C.  $x + z = 1$



D. None of these

Answer: A::C

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7. The value of expression  $\left[ \vec{a} \times \vec{b} \quad \vec{c} \times \vec{d} \quad \vec{e} \times \vec{f} \right]$  is equal to :

A.  $\left[ \vec{a} \ \vec{b} \ \vec{d} \right] \left[ \vec{c} \ \vec{e} \ \vec{f} \right] - \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \left[ \vec{d} \ \vec{e} \ \vec{f} \right]$

B.  $\left[ \vec{a} \ \vec{b} \ \vec{e} \right] \left[ \vec{f} \ \vec{c} \ \vec{d} \right] - \left[ \vec{a} \ \vec{b} \ \vec{f} \right] \left[ \vec{e} \ \vec{c} \ \vec{d} \right]$

C.  $\left[ \vec{c} \ \vec{d} \ \vec{a} \right] \left[ \vec{b} \ \vec{e} \ \vec{f} \right] - \left[ \vec{c} \ \vec{d} \ \vec{b} \right] \left[ \vec{a} \ \vec{e} \ \vec{f} \right]$

D.  $\left[ \vec{b} \ \vec{c} \ \vec{d} \right] \left[ \vec{a} \ \vec{e} \ \vec{f} \right] - \left[ \vec{b} \ \vec{c} \ \vec{f} \right] \left[ \vec{a} \ \vec{e} \ \vec{d} \right]$

Answer: A::B::C

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8. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  &  $\vec{d}$  are position vector of point A,B,C and D respectively in 3-D space no three of A,B,C,D are collinear and satisfy the relation  $3\vec{a} - 2\vec{b} + \vec{c} - 2\vec{d} = 0$  then

A. A, B, C and D are coplanar

B. The line joining the points B and D divides the line joining the point A and C in the ratio of 2: 1

C. The line joining the points A and C divides the line joining the points B and D in the ratio of 1: 1

D. The four vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are linearly dependent .

**Answer: A::C::D**



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9. If OAB is a tetrahedron with edges and  $\hat{p}$ ,  $\hat{q}$ ,  $\hat{r}$  are unit vectors along bisectors of

$\vec{OA}, \vec{OB}, \vec{OC}, \vec{OA}$ 

respectively

and

$$\hat{a} = \frac{\vec{OA}}{|\vec{OA}|}, \hat{b} = \frac{\vec{OB}}{|\vec{OB}|}, \hat{c} = \frac{\vec{OC}}{|\vec{OC}|}, \text{ then :}$$

$$\text{A. } \frac{[\hat{a}\hat{b}\hat{c}]}{[\hat{p}\hat{q}\hat{r}]} = \frac{3\sqrt{3}}{2}$$

$$\text{B. } \frac{[\hat{a} + \hat{b} \quad \hat{b} + \hat{c} \quad \hat{c} + \hat{a}]}{[\hat{p} + \hat{q} \quad \hat{q} + \hat{r} \quad \hat{r} + \hat{p}]} = \frac{3\sqrt{3}}{4}$$

$$\text{C. } \frac{[\hat{a} + \hat{b} \quad \hat{b} + \hat{c} \quad \hat{c} + \hat{a}]}{[\hat{p}\hat{q}\hat{r}]} = \frac{3\sqrt{3}}{2}$$

$$\text{D. } \frac{[\hat{a}\hat{b}\hat{c}]}{[\hat{p} + \hat{q} \quad \hat{q} + \hat{r} \quad \hat{r} + \hat{p}]} = \frac{3\sqrt{3}}{4}$$

**Answer: A:D**



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10. Let  $\hat{a}$  and  $\hat{c}$  are unit vectors and  $|\vec{b}| = 4$ . If the angle between  $\hat{a}$  and  $\hat{c}$  is  $\cos^{-1}\left(\frac{1}{4}\right)$ , and  $\hat{b} - 2\hat{c} = \lambda\hat{a}$ , then the value of  $\lambda$  can be :

A. 2

B. -3

C. 3

D. -4

**Answer: C::D**



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11. Consider the lines  $x = y = z$  and line

$2x + y + z - 1 = 0 = 3x + y + 2z - 2$ , then

A. The shortest distance between the two lines is  $\frac{1}{\sqrt{2}}$

B. The shortest distance between the two lines is  $\sqrt{2}$

C. Plane containing the line  $L_2$  and parallel to line  $L_1$  is

$$z - x + 1 = 0$$

D. Perpendicular distance of origin from plane containing line  $L_2$  and

parallel to line  $L_1$  is  $\frac{1}{\sqrt{2}}$

**Answer: A::D**

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12. If  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = h\vec{a} + k\vec{b} = r\vec{c} + s\vec{d}$ , where  $\vec{a}, \vec{b}$  are non-collinear and  $\vec{c}, \vec{d}$  are also non-collinear then :

A.  $\pi^2$

B.  $\frac{5\pi^2}{4}$

C.  $\frac{35\pi^2}{4}$

D.  $\frac{37\pi^2}{4}$

**Answer: B::D**

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13. If  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = h\vec{a} + k\vec{b} = r\vec{c} + s\vec{d}$ , where  $\vec{a}, \vec{b}$  are non-collinear and  $\vec{c}, \vec{d}$  are also non-collinear then :

A.  $h = \begin{bmatrix} \vec{a} & \vec{c} & \vec{d} \\ \vec{b} & \vec{c} & \vec{d} \end{bmatrix}$

$$B. k = \begin{bmatrix} \vec{a} & \vec{c} & \vec{d} \end{bmatrix}$$

$$C. r = \begin{bmatrix} \vec{a} & \vec{b} & \vec{d} \end{bmatrix}$$

$$D. s = - \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix}$$

Answer: B::C::D



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14. Let  $a$  be a real number and  $\vec{\alpha} = \hat{i} + 2\hat{j}$ ,  $\vec{\beta} = 2\hat{i} + a\hat{j} + 10\hat{k}$ ,  $\vec{\gamma} = 12\hat{i} + 20\hat{j} + a\hat{k}$  be three vectors, then  $\vec{\alpha}$ ,  $\vec{\beta}$  and  $\vec{\gamma}$  are linearly independent for :

A.  $a > 0$

B.  $a < 0$

C.  $a = 0$

D. No value of  $a$

Answer: A::B::C

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15. The volume of a right triangular prism  $ABCA_1B_1C_1$  is equal to 3. If the position vectors of the vertices of the base ABC are  $A(1, 0, 1)$ ,  $B(2, 0, 0)$  and  $C(O, 1, 0)$ , then position vectors of the vertex  $A_1$ , can be

A. (2, 2, 2)

B. (0, 2, 0)

C. (0, -2, 2)

D. (0, -2, 0)

**Answer: A:D**

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16. If  $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$ ,  $\vec{b} = y\hat{i} + z\hat{j} + x\hat{k}$ , and  $\vec{c} = z\hat{i} + x\hat{j} + y\hat{k}$ , then  $\vec{a} \times (\vec{b} \times \vec{c})$  is :

A. Parallel to  $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$

B. Orthogonal to  $\hat{i} + \hat{j} + \hat{k}$

C. Orthogonal to  $(y + z)\hat{i} + (z + x)\hat{j} + (x + y)\hat{k}$ ,

D. Orthogonal to  $x\hat{i} + y\hat{j} + z\hat{k}$

**Answer: A::B::C::D**

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17. If a line has a vector equation,  $\vec{r} = 2\hat{i} + 6\hat{j} + \lambda(\hat{i} - 3\hat{j})$  then which of the following statements holds good ?

A. the line is parallel to  $2\hat{i} + 6\hat{j}$

B. the line passes through the point  $3\hat{i} + 3\hat{j}$

C. the line passes through the point  $\hat{i} + 9\hat{j}$

D. the line is parallel to xy plane

**Answer: B::C::D**



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18. Let M, N, P and Q be the mid points of the edges AB, CD, AC and BD respectively of the tetrahedron ABCD. Further, MN is perpendicular to both AB and CD and PQ is perpendicular to both AC and BD. Then which of the following is/are correct:

A.  $AB = CD$

B.  $BC = DA$

C.  $AC = BD$

D.  $AN = BN$

**Answer: A::B::C::D**

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19. The solution vectors  $\vec{r}$  of the equation  $\vec{r} \times \hat{i} = \hat{j} + \hat{k}$  and  $\vec{r} \times \hat{j} = \hat{k} + \hat{j}$  represent two straight lines which

are :

- A. Intersecting
- B. Non coplanar
- C. Coplanar
- D. Non intersecting

**Answer: B::D**

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20. Which of the following statement(s) is/are incorrect ?

A. The lines

$$\frac{x - 4}{-3} = \frac{y + 6}{-1} = \frac{z + 6}{-1} \text{ and } \frac{x - 1}{-1} = \frac{y - 2}{-2} = \frac{z - 3}{2} \text{ are}$$

orthogonal

B. The planes  $3x - 2y - 4z = 3$  and the plane  $x - y - z = 3$  are

orthogonal

C. The function  $f(x) = \ln(e^{-2} + e^x)$  is monotonic increasing

$$\forall x \in \mathbb{R}$$

D. If  $g$  is the inverse of the function,

$$f(x) = \ln(e^{-2} + e^x) \text{ then } g(x) = \ln(e^x - e^{-2})$$

**Answer: A:B**

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21. The lines with vector equations are,

$$\vec{r}_1 = 3\hat{i} + 6\hat{j} + \lambda(-4\hat{i} + 3\hat{j} + 2\hat{k}) \text{ and } \vec{r}_2 = -2\hat{i} + 7\hat{j} + \mu(-4\hat{i} +$$

are such that :

A. they are coplanar

B. they do not intersect

C. they are skew

D. the angle between them is  $\tan^{-1}(3/7)$

Answer: B::C::D



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### Exercise 3 Comprehension Type Problems

1. The vertices of  $\Delta ABC$  are  $(2, 0, 0)$ ,  $B(0, 1, 0)$ ,  $C(0, 0, 2)$ . Its orthocentre is H and circumcentre is S. P is a point equidistant from A, B, C and the origin O.

Q. The z-coordinate of H is :

A. 1

B.  $1/2$

C.  $1/6$

D.  $1/3$

Answer: D



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2. The vertices of  $\Delta ABC$  are  $(2, 0, 0)$ ,  $B(0, 1, 0)$ ,  $C(0, 0, 2)$ . Its orthocentre is H and circumcentre is S. P is a point equidistant from A, B, C and the origin O.

Q. The y-coordinate of S is :

A.  $5/6$

B.  $1/3$

C.  $1/6$

D.  $1/2$

**Answer: C**



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3. The vertices of  $\Delta ABC$  are  $(2, 0, 0)$ ,  $B(0, 1, 0)$ ,  $C(0, 0, 2)$ . Its orthocentre is H and circumcentre is S. P is a point equidistant from A, B, C and the

origin O.

Q. PA is equal to :

A. 1

B.  $\sqrt{2}$

C.  $\sqrt{\frac{3}{2}}$

D.  $\frac{3}{2}$

**Answer: D**

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4. Consider a plane  $\pi: \vec{r} \cdot \vec{n} = d$  (where  $\vec{n}$  is not a unit vector). There are two points  $A(\vec{a})$  and  $B(\vec{b})$  lying on the same side of the plane.

Q. If foot of perpendicular from A and B to the plane  $\pi$  are P and Q respectively, then length of PQ be :

A. 
$$\frac{\left| \left( \vec{b} - \vec{a} \right) \cdot \vec{n} \right|}{\left| \vec{n} \right|}$$

B.  $\left| \left( \vec{b} - \vec{a} \right) \cdot \vec{n} \right|$

C.  $\frac{\left| \left( \vec{b} - \vec{a} \right) \times \vec{n} \right|}{\left| \vec{n} \right|}$

D.  $\left| \left( \vec{b} - \vec{a} \right) \times \vec{n} \right|$

**Answer: C**



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5. Consider a plane  $\pi: \vec{r} \cdot \vec{n} = d$  (where  $\vec{n}$  is not a unit vector). There are two points  $A(\vec{a})$  and  $B(\vec{b})$  lying on the same side of the plane.

Q. If foot of perpendicular from A and B to the plane  $\pi$  are P and Q respectively, then length of PQ be :

A.  $\vec{a} + \frac{2}{(\vec{n})^2} (d - \vec{a} \cdot \vec{n}) \vec{n}$

B.  $\vec{a} - \frac{1}{(\vec{n})^2} (d - \vec{a} \cdot \vec{n}) \vec{n}$

C.  $\vec{a} + \frac{2}{(\vec{n})^2} (d + \vec{a} \cdot \vec{n}) \vec{n}$

$$D. \vec{a} + \frac{2}{(\vec{n})^2} \vec{n}$$

**Answer: A**

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6. Consider a plane  $\pi: \vec{r} \cdot \vec{n} = d$  (where  $\vec{n}$  is not a unit vector). There are two points  $A(\vec{a})$  and  $B(\vec{b})$  lying on the same side of the plane.

Q. If foot of perpendicular from A and B to the plane  $\pi$  are P and Q respectively, then length of PQ be :

A.  $\frac{\left| (\vec{a} - \vec{b}) \cdot \vec{n} \right|}{|\vec{n}|}$

B.  $\left| (\vec{a} - \vec{b}) \cdot \vec{n} \right|$

C.  $\left| (\vec{a} - \vec{b}) \times \vec{n} \right|$

D.  $\frac{\left| (\vec{a} - \vec{b}) \times \vec{n} \right|}{|\vec{n}|}$

**Answer: A**





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7. Consider a plane  $\Pi: \vec{r} \cdot (2\hat{i} + \hat{j} - \hat{k}) = 5$ , a line  $L_1: \vec{r} = (3\hat{i} - \hat{j} + 2\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - \hat{k})$  and a point  $a(3, -4, 1) \cdot L_2$  is a line passing through A intersecting  $L_1$  and parallel to plane  $\Pi$ .

Q. Equation of  $L_2$  is :

A.  $\vec{r} = (1 + \lambda)\hat{i} + (2 - 3\lambda)\hat{j} + (1 - \lambda)\hat{k}, \lambda \in R$

B.  $\vec{r} = (3 + \lambda)\hat{i} - (4 - 2\lambda)\hat{j} + (1 + 3\lambda)\hat{k}, \lambda \in R$

C.  $\vec{r} = (3 + \lambda)\hat{i} - (4 + 3\lambda)\hat{j} + (1 - \lambda)\hat{k}, \lambda \in R$

D. None of the above

Answer: C



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8. Consider a plane  $\Pi : \vec{r} \cdot (2\hat{i} + \hat{j} - \hat{k}) = 5$ , a line  $L_1 : \vec{r} = (3\hat{i} - \hat{j} + 2\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - \hat{k})$  and a point  $a(3, -4, 1) \cdot L_2$  is a line passing through A intersecting  $L_1$  and parallel to plane  $\Pi$ .

Q. Plane containing  $L_1$  and  $L_2$  is :

- A. parallel to yz-plane
- B. parallel to x-axis
- C. parallel to y-axis
- D. passing through origin

**Answer: B**

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9. Consider a plane  $\Pi : \vec{r} \cdot (2\hat{i} + \hat{j} - \hat{k}) = 5$ , a line  $L_1 : \vec{r} = (3\hat{i} - \hat{j} + 2\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - \hat{k})$  and a point  $a(3, -4, 1) \cdot L_2$  is a line passing through A intersecting  $L_1$  and parallel

to plane  $\Pi$ .

Q. Line  $L_1$  intersects plane  $\Pi$  at Q and xy-plane at R the volume of tetrahedron OAQR is :

(where 'O' is origin)

A. 0

B.  $\frac{14}{3}$

C.  $\frac{3}{7}$

D.  $\frac{7}{3}$

**Answer: D**

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10. Consider three planes :

$$2x + py + 6z = 8, x + 2y + qz = 5 \text{ and } x + y + 3z = 4$$

Q. Three planes intersect at a point if :

A.  $p = 2, q \neq 3$

B.  $p \neq 2, q \neq 3$

C.  $p \neq 2, q = 3$

D.  $p = 2, q = 3$

**Answer: B**



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**11. Consider three planes :**

$$2x + py + 6z = 8, x + 2y + qz = 5 \text{ and } x + y + 3z = 4$$

**Q. Three planes do not have any common point of intersection if :**

A.  $p = 2, q \neq 3$

B.  $p \neq 2, q \neq 3$

C.  $p \neq 2, q = 3$

D.  $p = 2, q = 3$

**Answer: C**

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12. The points A, B and C with position vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  respectively lie on a circle centered at origin O. Let G and E be the centroid of  $\triangle ABC$  and  $\triangle ACD$  respectively where D is mid point of AB.

Q. If OE and CD are mutually perpendicular, then which of the following will be necessarily true ?

A.  $\left| \vec{b} - \vec{a} \right| = \left| \vec{c} - \vec{a} \right|$

B.  $\left| \vec{b} - \vec{a} \right| = \left| \vec{b} - \vec{c} \right|$

C.  $\left| \vec{c} - \vec{a} \right| = \left| \vec{c} - \vec{b} \right|$

D.  $\left| \vec{b} - \vec{a} \right| = \left| \vec{c} - \vec{a} \right| = \left| \vec{b} - \vec{c} \right|$

**Answer: A**

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13. The points A, B and C with position vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  respectively lie on a circle centered at origin O. Let G and E be the centroid of  $\Delta ABC$  and  $\Delta ACD$  respectively where D is mid point of AB.

Q. If GE and CD are mutually perpendicular, then orthocenter of  $\Delta ABC$  must lie on :

- A. median through A
- B. median through C
- C. angle bisector through A
- D. angle bisector through B

**Answer: B**



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14. The points A, B and C with position vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  respectively lie on a circle centered at origin O. Let G and E be the centroid of  $\Delta ABC$  and  $\Delta ACD$  respectively where D is mid point of AB.

Q. If  $\left[ \overrightarrow{AB} \overrightarrow{AC} \overrightarrow{AB} \times \overrightarrow{AC} \right] = \lambda \left[ \overrightarrow{AE} \overrightarrow{AG} \overrightarrow{AE} \times \overrightarrow{AG} \right]$ , then the value of  $\lambda$

is :

A. -18

B. 18

C. -324

D. 324

**Answer: D**



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15. Consider a tetrahedron  $D - ABC$  with position vectors if its angular points as

$A(1, 1, 1)$ ,  $B(1, 2, 3)$ ,  $C(1, 1, 2)$

and centre of tetrahedron  $\left( \frac{3}{2}, \frac{3}{4}, 2 \right)$ .

Q. Shortest distance between the skew lines AB and CD :

A.  $\frac{1}{2}$

B.  $\frac{1}{3}$

C.  $\frac{1}{4}$

D.  $\frac{1}{5}$

**Answer: B**



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**16.** Consider a tetrahedron  $D - ABC$  with position vectors of its angular points as

$$A(1, 1, 1), B(1, 2, 3), C(1, 1, 2)$$

and centre of tetrahedron  $\left(\frac{3}{2}, \frac{3}{4}, 2\right)$ .

**Q.** If  $N$  be the foot of the perpendicular from point  $D$  on the plane face  $ABC$  then the position vector of  $N$  are :

A.  $(-1, 1, 2)$

B.  $(1, -1, 2)$

C.  $(1, 1, -2)$



D. (-1, -1, 2)

**Answer: B**



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17. In a triangle AOB, R and Q are the points on the side OB and AB respectively such that  $3OR = 2RB$  and  $2AQ = 3QB$ . Let OQ and AR intersect at the point P (where O is origin).

Q. If the point P divides OQ in the ratio of  $\mu : 1$ , then  $\mu$  is :

A.  $\frac{2}{19}$

B.  $\frac{2}{17}$

C.  $\frac{2}{15}$

D.  $\frac{10}{9}$

**Answer: D**



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18. In a triangle AOB, R and Q are the points on the side OB and AB respectively such that  $3OR = 2RB$  and  $2AQ = 3QB$ . Let OQ and AR intersect at the point P (where O is origin).

Q. If the ratio of area of quadrilateral PQBR and area of  $\triangle OPA$  is  $\frac{\alpha}{\beta}$  then  $(\beta - \alpha)$  is (where  $\alpha$  and  $\beta$  are coprime numbers) :

A. 1

B. 9

C. 7

D. 0

**Answer: D**



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**Exercise 4 Matching Type Problems**

Column-I	Column-II
(A) Lines $\frac{x-1}{-2} = \frac{y+2}{3} = \frac{z}{-1}$ and $\vec{r} = (3\hat{i} - \hat{j} + \hat{k}) + t(\hat{i} + \hat{j} + \hat{k})$ are	(P) Intersecting
(B) Lines $\frac{x+5}{1} = \frac{y-3}{7} = \frac{z+3}{3}$ and $x - y + 2z - 4 = 0 = 2x + y - 3z + 5$ are	(Q) Perpendicular
(C) Lines $(x = t - 3, y = -2t + 1, z = -3t - 2)$ and $\vec{r} = (t + 1)\hat{i} + (2t + 3)\hat{j} + (-t - 9)\hat{k}$ are	(R) Parallel
(D) Lines $\vec{r} = (\hat{i} + 3\hat{j} - \hat{k}) + t(2\hat{i} - \hat{j} - \hat{k})$ and $\vec{r} = (-\hat{i} - 2\hat{j} + 5\hat{k}) + s(\hat{i} - 2\hat{j} + \frac{3}{4}\hat{k})$ are	(S) Skew
	(T) Coincident

1.

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Column-I	Column-II
(A) If $\vec{a}$ , $\vec{b}$ and $\vec{c}$ are three mutually perpendicular vectors where $ \vec{a}  =  \vec{b}  = 2$ , $ \vec{c}  = 1$ , then $[\vec{a} \times \vec{b} \quad \vec{b} \times \vec{c} \quad \vec{c} \times \vec{a}]$ is	(P) -12
(B) If $\vec{a}$ and $\vec{b}$ are two unit vectors inclined at $\frac{\pi}{3}$ , then $16[\vec{a} \quad \vec{b} + (\vec{a} \times \vec{b}) \quad \vec{b}]$ is	(Q) 0
(C) If $\vec{b}$ and $\vec{c}$ are orthogonal unit vectors and $\vec{b} \times \vec{c} = \vec{a}$ then $[\vec{a} + \vec{b} + \vec{c} \quad \vec{a} + \vec{b} \quad \vec{b} + \vec{c}]$ is	(R) 16
(D) If $[\vec{x} \quad \vec{y} \quad \vec{a}] = [\vec{x} \quad \vec{y} \quad \vec{b}] = [\vec{a} \quad \vec{b} \quad \vec{c}] = 0$ , each vector being a non-zero vector, then $[\vec{x} \quad \vec{y} \quad \vec{c}]$ is	(S) 1
	(T) 4

2.

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Column-I		Column-II	
(A)	The number of real roots of equation $2^x + 3^x + 4^x - 9^x = 0$ is $\lambda$ , then $\lambda^2 + 7$ is divisible by	(P)	2
(B)	Let $ABC$ be a triangle whose centroid is $G$ , orthocenter is $H$ and circumcentre is the origin ' $O$ '. If $D$ is any point in the plane of the triangle such that not three of $O, A, B, C$ and $D$ are collinear satisfying the relation $\vec{AD} + \vec{BD} + \vec{CD} + 3\vec{HG} = \lambda\vec{HD}$ , then $\lambda + 4$ is divisible by	(Q)	3
(C)	If $A(\text{adj } A) = \begin{bmatrix} 10 & 0 \\ 0 & 10 \end{bmatrix}$ , then $5 A  - 2$ is divisible by	(R)	4
(D)	$\vec{a}, \vec{b}, \vec{c}$ are three unit vector such that $\vec{a} + \vec{b} = \sqrt{2}\vec{c}$ , then $ 6\vec{a} - 8\vec{b} $ is divisible by	(S)	6
		(T)	10

3.



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### Exercise 5 Subjective Type Problems

1. A straight line  $L$  intersects perpendicularly both the lines :

$$\frac{x + 2}{2} = \frac{y + 6}{3} = \frac{z - 34}{-10} \quad \text{and} \quad \frac{x + 6}{4} = \frac{y - 7}{-3} = \frac{z - 7}{-2},$$

then the square of perpendicular distance of origin from  $L$  is



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2. If  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  are non-coplanar unit vectors such that  $[\hat{a}\hat{b}\hat{c}] = [\hat{b} \times \hat{c} \quad \hat{c} \times \hat{a} \quad \hat{a} \times \hat{b}]$ , then find the projection of  $\hat{b} + \hat{c}$  on  $\hat{a} \times \hat{b}$ .



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3. Let OA, OB, OC be coterminous edges of a cuboid. If l, m, n be the shortest distances between the sides OA, OB, OC and their respective skew body diagonals to them, respectively, then find

$$\frac{\left(\frac{1}{l^2} + \frac{1}{m^2} + \frac{1}{n^2}\right)}{\left(\frac{1}{OA^2} + \frac{1}{OB^2} + \frac{1}{OC^2}\right)}.$$



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4. Let OABC be a tetrahedron whose edges are of unit length. If  $\vec{OA} = \vec{a}$ ,  $\vec{OB} = \vec{b}$ , and  $\vec{OC} = \alpha(\vec{a} + \vec{b}) + \beta(\vec{a} \times \vec{b})$ , then  $(\alpha\beta)^2 = \frac{p}{q}$  (where p & q are relatively prime to each other). then the value of  $\left[\frac{q}{2}p\right]$  is



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5. Let  $\vec{v}_0$  be a fixed vector and  $\vec{v}_0 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ . Then for  $n \geq 0$  a sequence is

defined  $\vec{v}_{n+1} = \vec{v}_n + \left(\frac{1}{2}\right)^{n+1} \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}^{n+1} \vec{v}_0$  then

$\lim_{n \rightarrow \infty} \vec{v}_n = \begin{bmatrix} \alpha \\ \beta \end{bmatrix}$ . Find  $\frac{\alpha}{\beta}$ .



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6. If  $a$  is the matrix  $\begin{bmatrix} 1 & -3 \\ -1 & 1 \end{bmatrix}$ , then

$A - \frac{1}{3}A^2 + \frac{1}{9}A^3 \dots \dots \dots + \left(-\frac{1}{3}\right)^n A^{n+1} + \dots \dots \dots \infty = \frac{3}{13} \begin{bmatrix} 1 & a \\ b & 1 \end{bmatrix}$

. Find  $\left|\frac{a}{b}\right|$ .



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7. A sequence of  $2 \times 2$  matrices  $\{M_n\}$  is defined as follows

$M_n = \begin{bmatrix} \frac{1}{(2n+1)!} & \frac{1}{(2n+2)!} \\ \sum_{k=0}^n \frac{(2n+2)!}{(2k+2)!} & \sum_{k=0}^n \frac{(2n+1)!}{(2k+1)!} \end{bmatrix}$  then

$\lim_{n \rightarrow \infty} \det. (M_n) = \lambda - e^{-1}$ . Find  $\lambda$ .

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8. Let  $|\vec{a}| = 1$ ,  $|\vec{b}| = 1$  and  $|\vec{a} + \vec{b}| = \sqrt{3}$ . If  $\vec{c}$  be a vector such that  $\vec{c} = \vec{a} + 2\vec{b} - 3(\vec{a} \times \vec{b})$  and  $p|\left(\vec{a} \times \vec{b}\right) \times \vec{c}|$ , then find  $[p^2]$ .  
(where  $[ ]$  represents greatest integer function).

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9. Let  $\vec{r} = (\vec{a} \times \vec{b}) \sin x + (\vec{b} \times \vec{c}) \cos y + 2(\vec{c} \times \vec{a})$ , where  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non-zero and non-coplanar vectors. If  $\vec{r}$  is orthogonal to  $\vec{a} + \vec{b} + \vec{c}$ , then find the minimum value of  $\frac{4}{\pi^2}(x^2 + y^2)$ .

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10. The plane denoted by  $P_1: 4x + 7y + 4z + 81 = 0$  is rotated through a right angle about its line of intersection with plane

$P_2: 5x + 3y + 10z = 25$ . If the plane in its new position be denoted by P, and the distance of this plane from the origin is d, then the value of  $\left[ \frac{k}{2} \right]$  (where [.] represents greatest integer less than or equal to k) is....

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11. ABCD is a regular tetrahedron, A is the origin and B lies on x-axis. ABC lies in the xy-plane  $\left| \overrightarrow{AB} \right| = 2$  Under these conditions, the number of possible tetrahedrons is :

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12. If  $\vec{a}$  and  $\vec{b}$  are non zero, non collinear vectors and  $\vec{a}_1 = \lambda \vec{a} + 3 \vec{b}$ ,  $\vec{b}_1 = 2 \vec{a} + \lambda \vec{b}$ ,  $\vec{c}_1 = \vec{a} + \vec{b}$ . Find the sum of all possible real values of  $\lambda$  so that points  $A_1, B_1, C_1$  whose position vectors are  $\vec{a}_1, \vec{b}_1, \vec{c}_1$  respectively are collinear is equal to.

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13. Let P and Q are two points on curve  $y = \log_{\frac{1}{2}}\left(x - \frac{1}{2}\right) + \log_2 \sqrt{4x^2 - 4x + 1}$  and P is also on  $x^2 + y^2 = 10$ . Q lies inside the given circle such that its abscissa is integer. Find the smallest possible value of  $\overrightarrow{OP} \cdot \overrightarrow{OQ}$  where 'O' being origin.

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14. In above problem find the largest possible value of  $\left| \overrightarrow{PQ} \right|$ .

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15. If  $a, b, c, l, m, n \in \mathbb{R} - \{0\}$  such that  $al + bm + cn = 0, bl + cm + an = 0, cl + am + bn = 0$ . If a, b, c are distinct and  $f(x) = ax^3 + bx^2 + cx + 2$ . Find  $f(1)$  :

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16. Let  $\vec{u}$  and  $\vec{v}$  be unit vectors such that  $\vec{u} \times \vec{v} + \vec{u} = \vec{w}$  and  $\vec{w} \times \vec{u} = \vec{v}$ . Find the value of  $[\vec{u} \vec{v} \vec{w}]$ .



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