



India's Number 1 Education App

MATHS

BOOKS - VIKAS GUPTA MATHS (HINGLISH)

LIMIT

Exercise Single Choice Problems

1. $\lim_{x \rightarrow 0} \frac{\cos(\tan x) - \cos x}{x^4} =$

A. $\frac{1}{6}$

B. $-\frac{1}{3}$

C. $-\frac{1}{6}$

D. $\frac{1}{3}$

Answer: B



doubtnut | doubt, not out



Watch Video Solution

2. The value of $\lim_{x \rightarrow 0} \frac{(\sin x - \tan x)^2 - (1 - \cos 2x)^4 + x^5}{7(\tan^{-1} x)^7 + (\sin^{-1} x)^6 + 3\sin^5 x}$ equal to :
- A. 0
B. 1
C. 2
D. $\frac{1}{3}$

Answer: D



Watch Video Solution

3. Let $a = \lim_{x \rightarrow 0} \frac{\ln(\cos 2x)}{3x^2}$, $b = \lim_{x \rightarrow 0} \frac{\sin^2 2x}{x(1 - e^x)}$, $c = \lim_{x \rightarrow 1} \frac{\sqrt{x} - x}{\ln x}$
- A. $a < b < c$
B. $b < c < a$
C. $a < c < b$

D. $b < a < c$

Answer: D



Watch Video Solution

4. If $f(x) = \cot^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right)$ and $g(x) = \cos^{-1}\left(\frac{1 - x^2}{1 + x^2}\right)$, then
 $\lim_{x \rightarrow a} \frac{f(x) - f(a)}{g(x) - g(a)}$, $0 < a < \frac{1}{2}$ is

A. $\frac{3}{2(1 + a^2)}$

B. $\frac{3}{2}$

C. $\frac{-3}{2(1 + a^2)}$

D. $-\frac{3}{2}$

Answer: D



Watch Video Solution

5. $\lim_{x \rightarrow 0} \left(\frac{(1+x)^{\frac{2}{x}}}{e^2} \right)^{\frac{4}{\sin x}}$ is :

A. e^4

B. e^{-4}

C. e^8

D. e^{-8}

Answer: B



Watch Video Solution

6. $\lim_{x \rightarrow \infty} \frac{3}{x} \left[\frac{x}{4} \right] = \frac{p}{q}$ where $[.]$ denotes greatest integer function), then $p + q$ (where p,q are relative prime) is:

A. 2

B. 7

C. 5

D. 6

Answer: B



Watch Video Solution

7. $f(x) = \frac{x^n + \left(\frac{\pi}{3}\right)^n}{x^{n-1} + \left(\frac{\pi}{3}\right)^{n-1}}$, (n is an even number, then which of the following is correct

- A. If $f, \left[\frac{\pi}{3}, \infty\right) \rightarrow \left[\frac{\pi}{3}, \infty\right)$, then function is invertible
- B. $f(x) = f(-x)$ has infinite number of solutions
- C. $f(x) = |f(x)|$ has infinite number of solutions
- D. $f(x)$ is one-one function for all $x \in R$

Answer: D



Watch Video Solution

8. $\lim_{x \rightarrow 0} \frac{\sin(\pi \cos^2(\tan(\sin x)))}{x^2} =$

- A. π
- B. $\frac{\pi}{4}$
- C. $\frac{\pi}{2}$
- D. none of these

Answer: A



Watch Video Solution

9. if $f(x) = \frac{(e^{(x+3)\ln 27})^{\frac{x}{27}} - 9}{3^x - 27}, x < 3$ and

$f(x) = \lambda \frac{1 - \cos(x-3)}{(x-3)\tan(x-3)}$ if $\lim_{x \rightarrow 3} f(x)$ exist then lambda is

A. $\frac{9}{2}$

B. $\frac{2}{9}$

C. $\frac{2}{3}$

- D. none of these

Answer: C



Watch Video Solution

10. $\lim_{x \rightarrow \frac{\pi}{3}} \frac{\sin\left(\frac{\pi}{3} - x\right)}{2 \cos x - 1}$ is equal to:

A. $\frac{2}{\sqrt{3}}$

B. $\frac{1}{\sqrt{3}}$

C. $\sqrt{3}$

D. $\frac{1}{2}$

Answer: B



Watch Video Solution

11. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\sin x}{co^{-1}\left[\frac{1}{4}(3 \sin x - \sin 3x)\right]}$ where $[]$ denotes greatest integer function id:

A. $\frac{2}{\pi}$

B. 1

C. $\frac{4}{\pi}$

D. does not exist

Answer: A



Watch Video Solution

12. Let f be a continuous function on R such that

$$f\left(\frac{1}{4n}\right) = \frac{\sin e^n}{e^{n^2}} + \frac{n^2}{n^2 + 1} \text{ Then the value of } f(0) \text{ is}$$

A. 1

B. 0

C. -1

D. $\frac{1}{6}$

Answer: A



Watch Video Solution

13. $\lim_{x \rightarrow 1^-} \frac{e^{\{x\}} - \{x\} - 1}{\{x\}^2}$ equal, where $\{.\}$ is fractional part function

and I is an integer, to :

A. $\frac{I}{2}$

B. $e - 2$

C. I

D. does not exist

Answer: B



Watch Video Solution

14. $\lim_{x \rightarrow \infty} (e^{11x} - 7x)^{\frac{1}{3x}}$

A. $\frac{11}{3}$

B. $\frac{3}{11}$

C. $e^{\frac{3}{11}}$

D. $e^{\frac{11}{3}}$

Answer: D



Watch Video Solution

15. The value of $\lim_{x \rightarrow 0} \left[(1 - 2x)^n \sum_{r=0}^n - r \left(\frac{x + x^2}{1 - 2x} \right)^r \right]^{\frac{1}{x}}$ is :

A. e^n

B. e^{-n}

C. e^{3n}

D. e^{-3n}

Answer: B



Watch Video Solution

16. For a certain value of 'c' $\lim_{x \rightarrow \infty} \left[(x^5 + 7x^4 + 2)^c - x \right]$ is finite and non-zero. Then the value of limit is :

A. $\frac{7}{5}$

B. 1

C. $\frac{2}{5}$

D. None of these

Answer: A



Watch Video Solution

17. The integer n for which $\lim_{x \rightarrow 0} \frac{(\cos x - 1)(\cos x - e^x)}{x^n}$ is a finite non-zero number is :

A. 1

B. 2

C. 3

D. 4

Answer: C



Watch Video Solution

18. The value of $\lim_{x \rightarrow 0} \left(\frac{\sin x}{x} \right)^{\frac{1}{1 - \cos x}}$:

A. $e^{-1/3}$

B. $e^{1/3}$

C. $e^{-1/6}$

D. $e^{1/6}$

Answer: A



Watch Video Solution

19. If $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 - x + 1} - ax - b \right) = 0$, then for

$$k \geq 2, (k \in N) \lim_{x \rightarrow \infty} \sec^{2n}(k!\pi b) =$$

A. a

B. $-a$

C. $2a$

D. b

Answer: A



Watch Video Solution

20. If f is a positive function such that

$$f(x + T) = f(x) (T > 0), \forall x \in R,$$

$$\lim_{n \rightarrow \infty} n \left(\frac{f(x + T) + 2f(x + 2T) + \dots + nf(x + nT)}{f(x + T) + 4f(x + 4T) + \dots + n^2 f(x + n^2 T)} \right) =$$

A. 2

B. $\frac{2}{3}$

C. $\frac{3}{2}$

D. none of these

Answer: C



Watch Video Solution

21. Let $f(x) = 3x^{10} - 7x^8 + 5x^6 - 21x^3 + 3x^2 - 7$

$$265 \left(\lim_{h \rightarrow 0} \frac{h^4 + 3h^2}{(f(1-h) - f(1))\sin 5h} \right) =$$

A. 1

B. 2

C. 3

D. -3

Answer: C



Watch Video Solution

22. $\lim_{x \rightarrow 0} \left(\frac{\cos x - \sec x}{x^2(x+1)} \right) =$

A. 0

B. $-\frac{1}{2}$

C. -1

D. -2

Answer: C



Watch Video Solution

23. Let $f(x)$ be a continuous and differentiable function satisfying

$f(x+y) = f(x)f(y) \forall x, y \in R$ if $f(x)$ can be expressed as

$f(x) = 1 + xP(x) + x^2Q(x)$ where

$\lim_{x \rightarrow 0} P(x) = a$ and $\lim_{x \rightarrow 0} Q(x) = b$, then $f'(x)$ is equal to :

A. $af(x)$

B. $bf(x)$

C. $(a + b)f(x)$

D. $(a + 2b)f(x)$

Answer: A



Watch Video Solution

24. The value of $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\left\{1 - \frac{\tan(x)}{2}\right\}\{1 - \sin x\}}{\left\{1 + \frac{\tan(X)}{2}\right\}(\pi - 2x)^3}$ equals

A. not exist

B. $\frac{1}{8}$

C. $\frac{1}{16}$

D. $\frac{1}{32}$

Answer: D



Watch Video Solution

25. $\lim_{x \rightarrow \infty} \left(\frac{x-3}{x+2} \right)^x$ is equal to

A. e

B. e^{-1}

C. e^{-5}

D. e^5

Answer: C



[Watch Video Solution](#)

26. $\lim_{x \rightarrow \frac{\pi}{2}} (\cos x)^{\cos x}$ is :

A. 1

B. 0

C. $\frac{1}{e}$

D. $\frac{2}{e}$

Answer: A



Watch Video Solution

27. If $\lim_{x \rightarrow c^-} \{\ln x\}$ and $\lim_{x \rightarrow c^+} \{\ln x\}$ exist finitely but they are not equal (where $\{\cdot\}$ denotes fractional part function), then:

A. c' can take only rational values

B. c' can take only irrational values

C. c' can take infinite values in which only one is irrational

D. c' can take infinite values in which only one is rational

Answer: D



Watch Video Solution

28. $\lim_{x \rightarrow 0} \left(1 + \frac{a \sin bx}{\cos x}\right)^{\frac{1}{x}}$, where a, b are non zero constants is equal to :

A. $e^{a/b}$

B. ab

C. e^{ab}

D. $e^{b/e}$

Answer: C



Watch Video Solution

29. the value of $\lim_{x \rightarrow 0} \left\{ (\cos x)^{\frac{1}{\sin^2 x}} + \frac{\sin 2x + 2 \tan^{-1} 3x + 3x^2}{\ln(1 + 3x + \sin^2 x) + xe^x} \right\}$

A. $\sqrt{e} + \frac{3}{2}$

B. $\frac{1}{\sqrt{e}} + \frac{3}{2}$

C. $\sqrt{e} + 2$

D. $\frac{1}{\sqrt{e}} + 2$

Answer: D



Watch Video Solution

30.

let

$$a = \lim_{x \rightarrow 1} \left(\frac{x}{\ln x} - \frac{1}{x \ln x} \right), b = \lim_{x \rightarrow 0} \left(\frac{x^3 - 16x}{4x + x^2} \right), c = \lim_{x \rightarrow 0} \frac{\ln(1 + \sin x)}{x}$$

$$\text{and } d = \lim_{x \rightarrow -1} \frac{(x+1)^3}{3[\sin(x+1) - (x+1)]} \text{ then the matrix } \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

A. Idempotent

B. Involuntary

C. Non-singular

D. Nilpotent

Answer: D

Watch Video Solution

31. The integral value of n so that $\lim_{x \rightarrow 0} f(x)$ where

$$f(x) = \frac{(\sin x - x)(2 \sin x - \ln\left(\frac{1+x}{1-x}\right))}{x^n}$$

is a finite non-zero number

A. 2

B. 4

C. 6

D. 8

Answer: C



Watch Video Solution

32. Consider the function $f(x) = \begin{cases} \max\left(x, \frac{1}{x}\right), & \text{If } x \neq 0 \\ \min\left(x, \frac{1}{x}\right) & \\ 1, & \text{if } x = 0 \end{cases}$, then

$$\lim_{x \rightarrow 0^-} \{f(x)\} + \lim_{x \rightarrow 1^-} \{f(x)\} + \lim_{x \rightarrow 1^-} [f(x)] =$$

(where $\{.\}$ denotes fraction part function and $[.]$ denotes greatest integer function)

A. 0

B. 1

C. 2

D. 3

Answer: A



Watch Video Solution

$$33. \lim_{x \rightarrow \frac{1}{\sqrt{2}}^+} \frac{\cos^{-1}(2x\sqrt{1-x^2})}{\left(x - \frac{1}{\sqrt{2}}\right)} - \lim_{x \rightarrow \frac{1}{\sqrt{2}}^-} \frac{\cos^{-1}(2x\sqrt{1-x^2})}{\left(x - \frac{1}{\sqrt{2}}\right)}$$

A. $\sqrt{2}$

B. $2\sqrt{2}$

C. $4\sqrt{2}$

D. 0

Answer: C



Watch Video Solution

34.

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left((\sin) \frac{\pi}{2k} - (\cos) \frac{\pi}{2k} - (\sin) \left(\frac{\pi}{2(k+2)} + (\cos) \frac{\pi}{2(k+2)} \right) \right) =$$

A. 0

B. 1

C. 2

D. 3

Answer: D



Watch Video Solution

35. $\lim_{x \rightarrow 0} [1 + [x]]^{\frac{2}{x}}$, where $[::]$ is greatest integer function, is equal to

A. 0

B. 1

C. e^2

D. Does not exist

Answer: B



Watch Video Solution

36. If m and n are positive integers, then $\lim_{x \rightarrow 0} \frac{(\cos x)^{\frac{1}{m}} - (\cos x)^{\frac{1}{n}}}{x^2}$ equal to :

A. $m - n$

B. $\frac{1}{n} - \frac{1}{m}$

C. $\frac{n - m}{2mn}$

D. none of these

Answer: C



Watch Video Solution

37. $\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1$ then

A. $\left(-\frac{5}{2}, -\frac{3}{2} \right)$

B. $\left(\frac{5}{2}, \frac{3}{2} \right)$

C. $\left(-\frac{5}{2}, \frac{3}{2} \right)$

D. $\left(\frac{5}{2}, -\frac{3}{2} \right)$

Answer: A



Watch Video Solution

38. What is the value of $a + b$, if $\lim_{x \rightarrow 0} \frac{\sin(ax) - \ln(e^x \cos x)}{x \sin(bx)} = \frac{1}{2}$?

A. 1

B. 2

C. 3

D. $-\frac{1}{2}$

Answer: B



Watch Video Solution

39. Let $\alpha = \lim_{n \rightarrow \infty} \frac{(1^3 - 1^2) + (2^3 - 2^2) + \dots + (n^3 - n^2)}{n^4}$, then α

is equal to :

A. $\frac{1}{3}$

B. $\frac{1}{4}$

C. $\frac{1}{2}$

D. None existent

Answer: B



Watch Video Solution

40. The value of $\lim_{x \rightarrow 0} \frac{\cos(\sin x) - \cos x}{x^4}$ is equal to :

A. $\frac{1}{5}$

B. $\frac{1}{6}$

C. $\frac{1}{4}$

D. $\frac{1}{12}$

Answer: D



Watch Video Solution

41. $\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1$ then

A. $\left(-\frac{5}{2}, -\frac{3}{2} \right)$

B. $\left(\frac{5}{2}, \frac{3}{2} \right)$

C. $\left(-\frac{5}{2}, \frac{3}{2} \right)$

D. $\left(\frac{5}{2}, \frac{3}{2} \right)$

Answer: A



Watch Video Solution

42. Consider the sequence $u_n = \sum_{r=1}^n \frac{r}{2^r}$, $n \geq 1$ then the $\lim_{it_n \rightarrow \infty} u_n$

A. 1

B. e

C. $\frac{1}{2}$

D. 2

Answer: D



Watch Video Solution

43. the value of $\lim_{x \rightarrow 0} \left\{ (\cos x)^{\frac{1}{\sin^2 x}} + \frac{\sin 2x + 2 \tan^{-13} x + 3x^2}{\ln(1 + 3x + \sin^2 x) + xe^x} \right\}$

A. $\sqrt{e} + \frac{3}{2}$

B. $\frac{1}{\sqrt{e}} + \frac{3}{2}$

C. $\sqrt{e} + 2$

D. $\frac{1}{\sqrt{e}} + 2$

Answer: D



Watch Video Solution

44. For $n \in N$, let

$$f_n(x) = \tan \frac{x}{2} (1 + \sec x)(1 + \sec 2x)(1 + \sec 4x) \dots \dots (1 + \sec 2^n x),$$

the $\lim_{x \rightarrow 0} \frac{f_n(x)}{2x}$ is equal to :

A. 0

B. 2^n

C. 2^{n-1}

D. 2^{n+1}

Answer: C



Watch Video Solution

45. The value of $\lim_{x \rightarrow \frac{\pi}{4}} (1 + [x])^{1/\ln(\tan x)}$ (where $[.]$ denote the greatest integer function) is equal to

A. 0

B. 1

C. e

D. $\frac{1}{e}$

Answer: B



[Watch Video Solution](#)

46. If $(\lim)_{x \rightarrow 0} \frac{\{(a - n)nx - \tan x\}\sin nx}{x^2} = 0$, where n is nonzero real number, the a is
(a) 0 (b) $\frac{n+1}{n}$ (c) n (d) $n + \frac{1}{n}$

A. 0

B. $1 + \frac{1}{n}$

C. π

$$\text{D. } n + \frac{1}{n}$$

Answer: D



Watch Video Solution

47. The value of $\lim_{x \rightarrow \infty} \left(\frac{n!}{n^n} \right)^{\frac{3n^3+4}{4n^4-1}}$, $n \in N$ is equal to:

A. $\left(\frac{1}{e} \right)^{3/4}$

B. $e^{3/4}$

C. e^{-1}

D. 0

Answer: A



Watch Video Solution

48. The value of $\lim_{x \rightarrow \infty} \frac{ax^2 + bx + c}{dx + e}$ ($a, b, c, d, e \in R - \{0\}$) depends on the sign of :

- A. a only
- B. d only
- C. a and d only
- D. a,b and d only

Answer: C



Watch Video Solution

49. If $f(x) = \lim_{n \rightarrow \infty} \tan^{-1} \left(4n^2 \left(1 - \cos \left(\frac{x}{n} \right) \right) \right)$ and $g(x) = \lim_{n \rightarrow \infty} \frac{n^2}{2} \ln \cos \left(2 \frac{x}{n} \right)$ then $\lim_{x \rightarrow 0} \frac{e^{-2g(x)} - e^{f(x)}}{x^6}$ equals

A. $\frac{8}{3}$

B. $\frac{7}{3}$

C. $\frac{5}{3}$

D. $\frac{2}{3}$

Answer: A



Watch Video Solution

50. If $f(x)$ be a cubic polynomial and $\lim_{x \rightarrow 0} \frac{\sin^2 x}{f(x)} = \frac{1}{3}$ then $f(1)$ can not be equal to :

A. 0

B. - 5

C. 3

D. - 2

Answer: C



Watch Video Solution

51. $\lim_{x \rightarrow 0} \frac{2e^{\sin x} - e^{-\sin x} - 1}{x^2 + 2x}$

A. $\frac{3}{2}$

B. $e^{3/2}$

C. 2

D. e^2

Answer: A



Watch Video Solution

52. If $x_1, x_2, x_3, \dots, x_n$ are the roots of the equation $x^n + ax + b = 0$,
the value of

$(x_1 - x_2)(x_1 - x_3)(x_1 - x_4) \dots \dots (x_1 - x_n)$ is

A. $nx_1 + b$

B. $nx_1^{n-1} + a$

C. nx_1^{n-1}

D. nx_1^{n-1}

Answer: B



Watch Video Solution

53. $\lim_{x \rightarrow 0} \frac{\sqrt[3]{1 + \sin^2 x} - \sqrt[4]{1 - 2 \tan x}}{\sin x + \tan^2 x}$ is equal to:

A. -1

B. 1

C. $\frac{1}{2}$

D. $-\frac{1}{2}$

Answer: C



Watch Video Solution

54. if $f(x) = \begin{vmatrix} x \cos x & 2x \sin x & x \tan x \\ 1 & x & 1 \\ 1 & 2x & 1 \end{vmatrix}$ find $\lim_{x \rightarrow 0} \frac{f(x)}{x^2}$

- A. 0
- B. 1
- C. -1
- D. Does not exist

Answer: C



Watch Video Solution

Exercise One Or More Than One Answer Is Are Correct

1. if $\lim_{x \rightarrow 0} (p \tan qx^2 - 3 \cos^2 x + 4)^{\frac{1}{3x^2}} = e^{\frac{5}{3}}$

- A. $p = \sqrt{2}, q = \frac{1}{2\sqrt{2}}$
- B. $= \frac{1}{\sqrt{2}}, q = 2\sqrt{2}$

C. $p = 1, q = 2$

D. $p = 2, q = 4$

Answer: B::C



Watch Video Solution

2. $\lim_{x \rightarrow \infty} 2\left(\sqrt{25x^2 + x} - 5x\right)$ is:

A. $\lim_{x \rightarrow 0} \frac{2x - \log_e(1+x)^2}{5x^2}$

B. $\lim_{x \rightarrow 0} \frac{e^{-x} - 1 + x}{x^2}$

C. $\lim_{x \rightarrow 0} \frac{2(1 - \cos x^2)}{5x^4}$

D. $\lim_{(x \rightarrow 0)} \frac{\sin \frac{\pi}{5}}{x}$

Answer: A::C::D



Watch Video Solution

3. Let $\lim_{x \rightarrow \infty} (2^x + a^x + e^x)^{1/x} = L$ which of the following statement(s) is (are) correct ?

- A. if $L = a(a > 0)$, then the range of a is $[e, \infty)$
- B. if $L = 2e(a > 0)$, then the range of a is $\{2e\}$
- C. if $L = e(a > 0)$, then the range of a is $(0, e]$
- D. if $L = 2a(a > 1)$, then the range of a is $\left(\frac{e}{2}, \infty\right)$

Answer: A::B::C



Watch Video Solution

4. Let $\tan \alpha \cdot x + \sin \alpha \cdot y = \alpha$ and $\alpha \cdot \cos ec \alpha \bullet x + \cos \alpha \cdot y = 1$ be two variable straight lines, α being the parameter. Let P be the point of intersection of the lines. In the limiting position when $a \rightarrow 0$, the point P lies on the line :

- A. $x = 2$

B. $x = -1$

C. $y + 1 = 0$

D. $y = 2$

Answer: A::C::D



Watch Video Solution

5. Let $f: R \rightarrow [-1, 1]$ be defined as $f(x) = \cos(\sin x)$, then which of the following is(are) correct ?

A. f is periodic with fundamental period 2π

B. Range of $f = [\cos 1, 1]$

C. $\lim_{x \rightarrow \frac{\pi}{2}} \left(f\left(\frac{\pi}{2} - x\right) + f\left(\frac{\pi}{2} + x\right) \right) = 2$

D. f is neither even nor odd function

Answer: B::C



Watch Video Solution

6. Let $f(x) = x + \sqrt{x^2 + 2x}$ and $g(x) = \sqrt{x^2 + 2x} - x$, then:

- A. $\lim_{x \rightarrow \infty} g(x) = 1$
- B. $\lim_{x \rightarrow \infty} f(x) = 1$
- C. $\lim_{x \rightarrow -\infty} f(x) = -1$
- D. $\lim_{x \rightarrow \infty} g(x) = -1$

Answer: A::C::D



Watch Video Solution

7. Which of the following limits does not exist ?(a)

$$\lim_{x \rightarrow \infty} \cos ec^{-1} \left(\frac{x}{x+7} \right) \text{(B)} \quad \lim_{x \rightarrow 1} \sec^{-1} (\sin^{-1} x) \text{(C)} \quad \lim_{x \rightarrow 0^+} x^{\frac{1}{x}} \text{(D)}$$
$$\lim_{x \rightarrow 0} \left(\tan \left(\frac{\pi}{8} + x \right) \right)^{\cot x}$$

A. $\lim_{x \rightarrow \infty} \cos ec^{-1} \left(\frac{x}{x+7} \right)$

B. $\lim_{x \rightarrow 1} \sec^{-1} (\sin^{-1} x)$

C. $\lim_{x \rightarrow 0^+} x^{\frac{1}{x}}$

D. $\lim_{x \rightarrow 0} \left(\tan\left(\frac{\pi}{8} + x\right) \right)^{\cot x}$

Answer: A::D



Watch Video Solution

8. If $f(x) = (\lim)_{n \rightarrow \infty} \left(\frac{3}{2} + [\cos x] \left(\sqrt{n^2 + 1} - \sqrt{n^2 - 3n + 1} \right) \right)$

where $[y]$ denotes largest integer \leq , then identify the correct statement(s). $(\lim)_{n \rightarrow \infty} f(x) = 0$ $(\lim)_{n \xrightarrow{\frac{\pi}{2}}} f(x) = \frac{3\pi}{4}$

$$f(x) = \frac{3x}{2} \forall x \in \left[0, \frac{\pi}{2}\right] f(x) = 0 \forall x \in \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$$

A. $\lim_{x \rightarrow 0} f(x) = 0$

B. $\lim_{x \xrightarrow{\frac{\pi}{2}}} f(x) = \frac{3\pi}{4}$

C. $f(x) = \frac{3\pi}{2} \forall x \in \left[0, \frac{\pi}{2}\right]$

D. $f(x) = 0 \forall x \in \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

Answer: A::C::D



9.

Let

$$f: R \rightarrow R; f(x) = \begin{cases} (-1)^n & \text{if } x = \frac{1}{2^{2^n}}, n = 1, 2, 3, \dots \dots \dots \text{ and } 0 \\ & \text{otherwise} \end{cases}$$

otherwise then identify the correct statement (s).

- A. $\lim_{x \rightarrow 0} f(x)f(2x) = 0$
- B. $\lim_{x \rightarrow 0} f(x)$ does not exist
- C. $\lim_{x \rightarrow 0} f(x)f(2x) = 0$
- D. $\lim_{x \rightarrow 0} f(x)(2x)$ does not exist

Answer: B::C



Watch Video Solution

10. If $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} [f(x)]$ ($[.]$ denotes the greatest integer function) and $f(x)$ is non-constantcontinuous function, then :

- A. $\lim_{x \rightarrow 0} f(x)$ is an integer
- B. $\lim_{x \rightarrow 0} f(x)$ is non-integer
- C. $f(x)$ has local maximum at $x = a$
- D. $f(x)$ has local minimum at $x = a$

Answer: A::D



Watch Video Solution

11. let $f(x) = \frac{\cos^{-1}(1 - \{x\})\sin^{-1}(1 - \{x\})}{\sqrt{2\{x\}(1 - \{x\})}}$ where $\{x\}$ denotes the fractional part of x then

- A. $\lim_{x \rightarrow 0^+} f(x) = \frac{\pi}{4}$
- B. $\lim_{x \rightarrow 0^+} f(x) = \sqrt{2} \lim_{x \rightarrow 0^-} f(x)$
- C. $\lim_{x \rightarrow 0^-} f(x) = \frac{\pi}{4\sqrt{2}}$
- D. $\lim_{x \rightarrow 0^-} f(x) = \frac{\pi}{2\sqrt{2}}$

Answer: B::D



Watch Video Solution

12. $\lim_{x \rightarrow 0} \frac{\sin(\sin x) - \sin x}{ax^3 + bx^5 + c} = -\frac{1}{12}$ then

- A. $a = 2$
- B. $a = -2$
- C. $c = 0$
- D. $b \in R$

Answer: A::C



Watch Video Solution

13. If $f(x) = \lim_{n \rightarrow \infty} \left(n \left(x^{1/n} - 1 \right) \right)$ for $x > 0$, then which of the following is/are true?

- A. $f\left(\frac{1}{x}\right) = 0$
- B. $f\left(\frac{1}{x}\right) = \frac{1}{f(x)}$

C. $f\left(\frac{1}{x}\right) = -f(x)$

D. $f(xy) = f(x) + f(y)$

Answer: C::D



Watch Video Solution

14. $\lim_{n \rightarrow \infty} \cos^2\left(\pi\left(3\sqrt{n^3 + n^2 + 2n} - n\right)\right)$ where n is an integer, equals

A. $\frac{1}{3}$

B. $\frac{1}{2}$

C. $\frac{1}{4}$

D. $\frac{1}{9}$

Answer: A::B::C



Watch Video Solution

15. If $\alpha, \beta \in \left(-\frac{\pi}{2}, 0\right)$ such that
 $(\sin \alpha + \sin \beta) + \frac{\sin \alpha}{\sin \beta} = 0$ and $(\sin \alpha + \sin \beta) \frac{\sin \alpha}{\sin \beta} = -1$ and $\lambda = \lim_{n \rightarrow \infty}$

then :

A. $\alpha = \frac{\pi}{6}$

B. $\lambda = 2$

C. $\alpha = -\frac{\pi}{3}$

D. $\lambda = 1$

Answer: B



Watch Video Solution

16. Let $f(x) = \begin{cases} |x-2| + a^2 - 6a + 9, & x < 2 \\ 5 - 2x, & x \geq 2 \end{cases}$ If $\lim_{x \rightarrow 2} [f(x)]$ existsn the possible values a can take is/are (where $[.]$ represents the greatest integer function)

A. 2

B. $\frac{5}{2}$

C. 3

D. $\frac{7}{2}$

Answer: B



Watch Video Solution

17. A circular disk of unit radius is filled with a number of smaller circular disks arranged in the form of hexagon. Let A_n denotes a stack of disks arranged in the shape of a hexagon having 'n' disks on a side. The figure shows the configuration A_3 . If A be the area of large disk, S_n be the number of disks in A_n configuration and r_n be the radius of each disk in A_n configuration, then $\lim_{n \rightarrow \infty} \frac{S_n}{n^2} = \lim_{n \rightarrow \infty} nr_n$

A. $\frac{1}{3}$

B. $\frac{1}{2}$

C. $\frac{1}{4}$

D. $\frac{1}{11}$

Answer: B



Watch Video Solution

18.

Let

$$f(x) = [(x + 3, , -2 < x < 0), (4, x = 0), (2x + 5, , 0 < x < 1)],$$

then

$$\lim_{x \rightarrow 0^-} f([x - \tan]) \text{ is : } [.] \text{ denotes greatest integer function}$$

A. 2

B. 4

C. 5

D. none of these

Answer: B



Watch Video Solution

19.

Let

$$f(x) = [(x + 3, , -2 < x < 0), (4, x = 0), (2x + 5, , 0 < x < 1)],$$

then

$$\lim_{x \rightarrow 0} f\left(\left\{ \frac{x}{\tan x} \right\}\right) \text{ is: } (\{\cdot\} \text{ denotes fractional part of function})$$

A. 4

B. 5

C. 7

D. none of these

Answer: C



Watch Video Solution

20. A certain function $f(x)$ has the property that $f(3x) = \alpha f(x)$ for all positive real values of x and $f(x) = 1 - |x - 2|$ for $1 \leq x \leq 3$,

$$\lim_{x \rightarrow 2} (f(x))^{\cos ec\left(\frac{\pi x}{2}\right)} \text{ is}$$

A. $\frac{2}{\pi}$

B. $-\frac{2}{\pi}$

C. $e^{2/\pi}$

D. none of these

Answer: D



Watch Video Solution

21. A certain function $f(x)$ has the property that $f(3x) = \alpha f(x)$ for all positive real values of x and $f(x) = 1 - |x - 2|$ for $1 \leq x \leq 3$. If the total area bounded by $y = f(x)$ and x-axis in $[1, \infty)$ converges to a finite quantity, then the range of α is:

A. $(-1, 1)$

B. $\left(-\frac{1}{2}, \frac{1}{2}\right)$

C. $\left(-\frac{1}{3}, \frac{1}{3}\right)$

D. $\left(-\frac{1}{4}, \frac{1}{4}\right)$

Answer: C



Watch Video Solution

22. Consider the limit $\lim_{x \rightarrow 0} \frac{1}{x^3} \left(\frac{1}{\sqrt{1+x}} - \frac{(1+ax)}{(1+bx)} \right)$ exists, finite and

has the value equal to l (where a,b are real constants), then :

a=

A. 1

B. $\frac{3}{4}$

C. $\frac{1}{2}$

D. $\frac{1}{4}$

Answer: D



Watch Video Solution

23. Consider the limit $\lim_{x \rightarrow 0} \frac{1}{x^3} \left(\frac{1}{\sqrt{1+x}} - \frac{(1+ax)}{(1+bx)} \right)$ exists, finite and

has the value equal to l (where a,b are real constants), then:

$$a + b =$$

A. $\frac{3}{4}$

B. $\frac{1}{2}$

C. 1

D. 0

Answer: C



Watch Video Solution

24. Consider the limit $\lim_{x \rightarrow 0} \frac{1}{x^3} \left(\frac{1}{\sqrt{1+x}} - \frac{(1+ax)}{(1+bx)} \right)$ exists, finite and

has the value equal to l (where a,b are real constants), then :

$$\left| \frac{b}{a} \right| =$$

A. 38

B. 16

C. 72

D. 3

Answer: D



Watch Video Solution

25. For the curve $\sin x + \sin y = 1$ lying in first quadrant. If $\lim_{x \rightarrow 0} x^\alpha \frac{d^2y}{dx^2}$ exists and non-zero than $2\alpha =$

A. $\frac{1}{2}$

B. $\frac{1}{\sqrt{2}}$

C. $\frac{3}{2}$

D. 2

Answer: C



Watch Video Solution

26. For the curve $\sin x + \sin y = 1$ lying in the first quadrant there exists

a constant α for which $\lim_{x \rightarrow 0} x^\alpha \frac{d^2y}{dx^2} = I$, (not zero)

The value of L:

A. $\frac{1}{2}$

B. 1

C. $\frac{1}{2\sqrt{2}}$

D. $\frac{1}{2\sqrt{3}}$

Answer: C



[Watch Video Solution](#)

Exercise Comprehension Type Problems

1. A circular disk of unit radius is filled with a number of smaller circular disks arranged in the form of hexagon. Let A_n denotes a stack of disks

arranged in the shape of a hexagon having 'n' disks on a side. The figure shows the configuration A_3 . If A be the area of large disk, S_n be the number of disks in A_n configuration and r_n be the radius of each disk in A_n configuration, then $\lim_{n \rightarrow \infty} \frac{S_n}{n^2} = \lim_{n \rightarrow \infty} nr_n$

A. 3

B. 4

C. 1

D. 11

Answer: A



Watch Video Solution

Exercise Matching Type Problems

1. Solve for x: $\lim_{x \rightarrow -4} \left[\frac{x^2 - x - 20}{x + 4} \right]$



View Text Solution

Exercise Subjective Type Problems

1. If $\lim_{x \rightarrow 0} \frac{\ln \cot\left(\frac{\pi}{4} - \beta x\right)}{\tan \alpha x} = 1$, then $\frac{\alpha}{\beta} = \dots$.



Watch Video Solution

2. If $\lim_{x \rightarrow 0} \frac{f(x)}{\sin^2 x} = 8$, $\lim_{x \rightarrow 0} \frac{g(x)}{2 \cos x - xe^x + x^3 + x - 2} = \lambda$ and $\lim_{x \rightarrow 0} (1 + 2f(x))^{\frac{1}{g(x)}} = \frac{1}{e}$, then

The value of λ is



Watch Video Solution

3. If α, β are two distinct real roots of the equation $ax^3 + x - 1 - a = 0 (a \neq -1, 0)$, none of which is equal to unity. If the value of $\lim_{x \rightarrow \frac{1}{\alpha}} \frac{(1+a)x^3 - x^2 - a}{(e^{1-\alpha x} - 1)(x-1)}$ is $\frac{al(k\alpha - \beta)}{\alpha}$ the value of $k + l$



Watch Video Solution

4. The value of

$$\lim_{x \rightarrow 0} \frac{(140)^x - (35)^x - (28)^x - (20)^x + 7^x + 5^x + 4^x - 1}{x \sin^2 x}$$
$$= 2 \ln 2 \ln k \ln 7, \text{ then } k =$$



Watch Video Solution

5. If $\lim_{x \rightarrow 0} \frac{a \cos x}{x^2} + \frac{b}{x^2} = \frac{1}{3}$, then $b - a =$



Watch Video Solution

6. Find the value of $\lim_{x \rightarrow \infty} \left(x + \frac{1}{x} \right) e^{1/x} - x.$



Watch Video Solution

7. Find $\lim_{x \rightarrow \alpha^+} \left[\frac{\min(\sin x, \{x\})}{x - 1} \right]$ where alpha is the root of the equation $\sin x + 1 = x$. Here $[.]$ represents greatest integer function and

{.} represents fractional part function



Watch Video Solution