



# MATHS

## BOOKS - VIKAS GUPTA MATHS (HINGLISH)

### PARABOLA

#### Exercise 1 Single Choice Problems

1. Let PQ be the latus rectum of the parabola  $y^2 = 4x$  with vertex A. Minimum length of the

projection of PQ on a tangent drawn in  
portion of Parabola PAQ is

A. 2

B. 4

C.  $2\sqrt{3}$

D.  $2\sqrt{2}$

**Answer: D**



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2. A normal is drawn to the parabola  $y^2 = 9x$  at the point  $P(4, 6)$ . A circle is described on  $SP$  as diameter, where  $S$  is the focus. The length of the intercept made by the circle on the normal at point  $P$  is :

A.  $\frac{17}{4}$

B.  $\frac{15}{4}$

C. 4

D. 5

**Answer: B**



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3. A trapezium is inscribed in the parabola  $y^2 = 4x$ , such that its diagonal pass through the point  $(1, 0)$  and each has length  $\frac{25}{4}$ . If the area of the trapezium be  $P$ , then  $4P$  is equal to :

A. 70

B. 71

C. 80

D. 75

**Answer: D**



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4. The length of normal chord of parabola  $y^2 = 4x$ , which subtends an angle of  $90^\circ$  at the vertex is :

A.  $6\sqrt{3}$

B.  $7\sqrt{2}$

C.  $8\sqrt{2}$

D.  $9\sqrt{2}$

**Answer: A**



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5. If  $b$  and  $c$  are lengths of the segments of any focal chord of the parabola  $y^2 = 4ax$ , then write the length of its latus rectum.

A.  $\frac{bc}{b+c}$

B.  $\frac{2bc}{b+c}$

C.  $\frac{b+c}{2}$

D.  $\sqrt{bc}$

**Answer: B**



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**6.** The length of the shortest path that begins at the point  $(-1, 1)$ , touches the  $x$ -axis and then ends at a point on the parabola  $(x - y)^2 = 2(x + y - 4)$ , is :

A.  $3\sqrt{2}$

B. 5

C.  $4\sqrt{10}$

D. 13

**Answer: A**



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7. If the normals at P, Q, R of the parabola  $y^2 = 4ax$  meet in O and S be its focus, then  $. SP. SQ. SR =$



A.  $2^3$

B.  $a^2(SO')$

C.  $a(SO')^2$

D. None of these

**Answer: C**



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8. A and B are two points on the parabola  $y^2 = 4ax$  with vertex O. if OA is perpendicular

to OB and they have lengths  $r_1$  and  $r_2$

respectively, then the value of  $\frac{r_1^{4/3} r_2^{4/3}}{r_1^{2/3} + r_2^{2/3}}$  is

A.  $16a^2$

B.  $a^2$

C.  $4a$

D. None of these

**Answer: A**



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9. Length of the shortest chord of the parabola  $y^2 = 4x + 8$ , which belongs to the family of lines  $(1 + \lambda)y + (\lambda - 1)x + 2(1 - \lambda) = 0$  is

A. 6

B. 5

C. 8

D. 2

**Answer: C**



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10. If locus of mid point of any normal chord of the parabola :

$$y^2 = 4x \text{ is } x - a = \frac{b}{y^2} + \frac{y^2}{c},$$

where  $a, b, c \in N$ , then  $(a + b + c)$  equals to :

A. 5

B. 8

C. 10

D. None of these

**Answer: B**



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**11.** Let tangents at P and Q to curve  $y^2 - 4x - 2y + 5 = 0$  intersect at T. If S(2, 1) is a point such that  $(SP)(SQ) = 16$ , then the length ST is equal to :

A. 3

B. 4

C. 5

D. None of these

**Answer: B**



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**12.** Abscissa of two points P and Q on parabola

$y^2 = 8x$  are roots of equation

$x^2 - 17x + 11 = 0$ . Let Tangents at P and Q

meet at point T, then distance of T from the

focus of parabola is :

A. 7

B. 6

C. 5

D. 4

**Answer: A**



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**13.** If  $Ax + By = 1$  is a normal to the curve  $ay = x^2$ , then :

A.  $4A^2(1 - aB) = aB^3$

$$\text{B. } 4A^2(2 + aB) = aB^3$$

$$\text{C. } 4A^2(1 + aB) + aB^3 = 0$$

$$\text{D. } 2A^2(2 - aB) = aB^3$$

**Answer: D**



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**14.** The equation of a curve which passes through the point  $(3, 1)$ , such the segment of any tangent between the point of tangency



and the x-axis is bisected at its point of intersection with y-axis, is :

A.  $x = 3y^2$

B.  $x^2 = 9y$

C.  $x = y^2 + 2$

D.  $2x = 3y^2 + 3$

**Answer: A**



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15. The parabola  $y = 4 - x^2$  has vertex P. It intersects x-axis at A and B. If the parabola is translated from its initial position to a new position by moving its vertex along the line  $y = x + 4$ , so that it intersects x-axis at B and C, then abscissa of C will be :

A. 3

B. 4

C. 5

D. 8

**Answer: D**



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**16.** A focal chord for parabola  $y^2 = 8(x + 2)$  is inclined at an angle of  $60^\circ$  with positive x-axis and intersects the parabola at P and Q. Let perpendicular bisector of the chord PQ intersects the x-axis at R, then the distance of R from focus is :

A.  $\frac{8}{3}$

B.  $\frac{16\sqrt{3}}{3}$

C.  $\frac{16}{3}$

D.  $8\sqrt{3}$

**Answer: C**



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**17. v34**

A. 10

B. 11

C. 12

D. None of these

**Answer: C**



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**18.** The chord of contact of a point  $A(x_A, y_A)$  of  $y^2 = 4x$  passes through  $(3, 1)$  and point A lies on  $x^2 + y^2 = 5^2$ . Then :

A.  $5x_A^2 + 24x_A + 11 = 0$

B.  $13x_A^2 + 8x_A - 21 = 0$

C.  $5x_A^2 + 24x_A + 61 = 0$

D.  $13x_A^2 + 21x_A - 31 = 0$

**Answer: A**



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**Exercise 2 One Or More Than One Answer Is Are Correct**

1. PQ is a double ordinate of the parabola  $y^2 = 4ax$ . If the normal at P intersect the line passing through Q and parallel to axis of x at G, then locus of G is a parabola with -

A. vertex at  $(4a, 0)$

B. focus at  $(5a, 0)$

C. directrix as the line  $x - 3a = 0$

D. length of latus rectum equal to  $4a$

**Answer: A::B::C::D**



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## Exercise 3 Comprehension Type Problems

1. Consider the following lines :

$$L_1: x - y - 1 = 0$$

$$L_2: x + y - 5 = 0$$

$$L_3: y - 4 = 0$$

Let  $L_1$  is axis to a parabola,  $L_2$  is tangent at the vertex to this parabola and  $L_3$  is another tangent to this parabola at some point P.

Let 'C' be the circle circumscribing the triangle



formed by tangent and normal at point P and axis of parabola. The tangent and normals at normals at the extremities of latus rectum of this parabola forms a quadrilateral ABCD.

Q. The equation of the circle 'C' is :

A.  $x^2 + y^2 - 2x - 31 = 0$

B.  $x^2 + y^2 - 2y - 31 = 0$

C.  $x^2 + y^2 - 2x - 2y - 31 = 0$

D.  $x^2 + y^2 + 2x + 2y = 31$

**Answer: A**



2. Consider the following lines :

$$L_1 : x - y - 1 = 0$$

$$L_2 : x + y - 5 = 0$$

$$L_3 : y - 4 = 0$$

Let  $L_1$  is axis to a parabola,  $L_2$  is tangent at the vertex to this parabola and  $L_3$  is another tangent to this parabola at some point P.

Let 'C' be the circle circumscribing the triangle formed by tangent and normal at point P and axis of parabola. The tangent and normals at

normals at the extremities of latus rectum of this parabola forms a quadrilateral ABCD.

Q. The given parabola is equal to which of the following parabola ?

A.  $y^2 = 16\sqrt{2}x$

B.  $x^2 = -4\sqrt{2}y$

C.  $y^2 = -\sqrt{2}x$

D.  $y^2 = 8\sqrt{2}x$

**Answer: D**



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**3.** Consider the following lines :

$$L_1 : x - y - 1 = 0$$

$$L_2 : x + y - 5 = 0$$

$$L_3 : y - 4 = 0$$

Let  $L_1$  is axis to a parabola,  $L_2$  is tangent at the vertex to this parabola and  $L_3$  is another tangent to this parabola at some point P.

Let 'C' be the circle circumscribing the triangle formed by tangent and normal at point P and axis of parabola. The tangent and normals at normals at the extremities of latus rectum of

this parabola forms a quadrilateral ABCD.

Q. The area of the quadrilateral ABCD is :

A. 16

B. 8

C. 64

D. 32

**Answer: C**



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1. Points  $A$  and  $B$  lie on the parabola  $y = 2x^2 + 4x - 2$ , such that origin is the mid-point of the line segment  $AB$ . If  $l$  be the length of the line segment  $AB$ , then find the unit digit of  $l^2$ .



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2. For the parabola  $y = -x^2$ , let  $a < 0$  and  $b > 0$ ,  $P(a, -a^2)$  and  $Q(b, -b^2)$ . Let  $M$  be the mid-point of  $PQ$  and  $R$  be the

point of intersection of the vertical line through M, with the parabola. If the ratio of the area of the region bounded by the parabola and the line segment PQ to the area of the triangle PQR be  $\frac{\lambda}{\mu}$ , where  $\lambda$  and  $\mu$  are relatively prime positive integers, then find the value of  $(\lambda + \mu)$ :



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**3.** The chord AC of the parabola  $y^2 = 4ax$  subtends an angle of  $90^\circ$  at points B and D on

the parabola. If points A, B, C and D are represented by  $(at_i^2, 2at_i)$ ,  $i = 1, 2, 3, 4$  respectively, then find the value of  $\left| \frac{t_2 + t_4}{t_1 + t_3} \right|$ .



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