



MATHS

BOOKS - VIKAS GUPTA MATHS (HINGLISH)

TRIGONOMETRIC EQUATIONS

Exercise 1 Single Choice Problems

1. Let x and y be 2 real numbers which satisfy the equations $(\tan^2 x - \sec^2 y) = \frac{5a}{6} - 3$ and $(-\sec^2 x + \tan^2 y) = a^2$, then the product of all possible value's of a can be equal to :

A. 0

B. $-\frac{2}{3}$

C. -1

D. $-\frac{3}{2}$

Answer: C



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2. The general solution of the equation

$\tan^2(x + y) + \cot^2(x + y) = 1 - 2x - x^2$ lie on the line is :

A. $x = -1$

B. $x = -2$

C. $y = -1$

D. $y = -2$

Answer: A



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3. General solution of the equation :

$\sin x + \cos x = \min_{a \in R} \{1, a^2 - 4a + 6\}$ is :

A. $\frac{n\pi}{2} + (-1)^n \frac{\pi}{4}$

B. $2n\pi + (-1)^n \frac{\pi}{4}$

C. $n\pi + (-1)^{n+1} \frac{\pi}{4}$

D. $n\pi + (-1)^n \frac{\pi}{4} - \frac{\pi}{4}$

Answer: D



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4. The number of solutions of the equation

$$\left(2 \sin\left(\frac{\sin x}{2}\right)\right) \left(\cos\left(\frac{\sin x}{2}\right)\right) \left(\sin\left(2 \tan \frac{x}{2} \cos^2 \frac{x}{2}\right) - 3\right) + 2 = 0$$
 in

$[0, 2\pi]$ is :

A. 0

B. 1

C. 2

D. 4

Answer: A



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5. Number of solution of $\tan(2x) = \tan(6x)$ in $(0, 3\pi)$ is :

A. 4

B. 5

C. 3

D. None of these

Answer: B



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6. The number of values of x in the interval $[0, 5\pi]$ satisfying the equation

$$3 \sin^2 x - 7 \sin x + 2 = 0$$
 is

A. 0

B. 2

C. 6

D. 8

Answer: C

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7. The number of different values of θ satisfying the equation $\cos \theta + \cos 2\theta = -1$, and at the same time satisfying the condition $0 < \theta < 360^\circ$ is :

A. 1

B. 2

C. 3

D. 4

Answer: D



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8. The total number of solution of the equation $\max(\sin x, \cos x) = \frac{1}{2}$ for $x \in (-2\pi, 5\pi)$ is equal to (A) 3 (B) 6 (C) 7 (D) 8

A. 3

B. 6

C. 7

D. 8

Answer: C



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9. The general value of x satisfying the equation

$$2 \cot^2 x + 2\sqrt{3} \cot x + 4 \operatorname{cosec} x + 8 = 0 \text{ is : (where } n \in I \text{)}$$

A. $n\pi - \frac{\pi}{6}$

B. $n\pi + \frac{\pi}{6}$

C. $2n\pi - \frac{\pi}{6}$

D. $2n\pi + \frac{\pi}{6}$

Answer: C



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10. The general solution of the equation $\sin^2 x + \cos^2 3x = 1$ is equal to :

(where $n \in I$)

A. $x = \frac{n\pi}{2}$

B. $x = n\pi + \frac{\pi}{4}$

C. $x = \frac{n\pi}{4}$

D. $x = n\pi + \frac{\pi}{2}$

Answer: C

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11. The values of x between 0 and 2π which satisfy the equation $\sin x \sqrt{8 \cos^2 x} = 1$ are in A.P. with common difference is

A. $\frac{\pi}{4}$

B. $\frac{\pi}{3}$

C. $\frac{\pi}{2}$

D. $\frac{2\pi}{3}$

Answer: A

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12. Number of solutions of $\sum_{r=1}^5 \cos rx = 5$ in the interval $[0, 4\pi]$ is

A. 0

B. 2

C. 3

D. 7

Answer: C



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13. The solution of

$$4 \sin^2 x + \tan^2 x + \sec^2 x + \cot^2 x - 6 = 0 \text{ is } (n \in \mathbb{Z}) \quad n\pi \pm \frac{\pi}{4} \quad (\text{b})$$

$$2n\pi \pm \frac{\pi}{4} \quad n\pi + \frac{\pi}{3} \quad (\text{d}) \quad n\pi - \frac{\pi}{6}$$

A. $n\pi \pm \frac{\pi}{4}$

B. $2n\pi \pm \frac{\pi}{4}$

C. $n\pi + \frac{\pi}{3}$

D. $n\pi - \frac{\pi}{6}$

Answer: A



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14. Smallest positive x satisfying the equation

$$\cos^3 3x + \cos^3 5x = 8 \cos^3 4x \cdot \cos^3 x \text{ is :}$$

A. 15°

B. 18°

C. 22.5°

D. 30°

Answer: B



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15. The general solution of the equation $\sin^{100} x - \cos^{100} x = 1$ is (where

$n \in \mathbb{I}$)

A. $2n\pi + \frac{\pi}{2}$

B. $n\pi + \frac{\pi}{2}$

C. $2n\pi - \frac{\pi}{2}$

D. $n\pi$

Answer:



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16. Number of solution (s) of equation $\sin \theta = \sec^2 4\theta$ in $[0, \pi]$ is/are :

A. 0

B. 1

C. 2

D. 3

Answer: B



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17. The number of solutions of the equation

$$4\sin^2 x + \tan^2 x + \cot^2 x + \operatorname{cosec}^2 x = 6 \text{ in } [0, 2\pi]$$

A. 1

B. 2

C. 3

D. 4

Answer: D



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18. One value of θ which satisfies the equation $\sin^4 \theta - 2\sin^2 \theta - 1$ lies between 0 and 2π .

A. 0

B. 2

C. 4

D. 8

Answer: A



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19. Find the smallest positive number p for which the equation $\cos(p \sin x) = \sin(p \cos x)$ has a solution $x \in [0, 2\pi]$.

A. $\frac{\pi}{\sqrt{2}}$

B. $\frac{\pi}{2}$

C. $\frac{\pi}{2\sqrt{2}}$

D. $\frac{3\pi}{2\sqrt{2}}$

Answer: C



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20. The total number of ordered pairs (x, y) satisfying $|x| + |y| = 2, \sin\left(\frac{\pi x^2}{3}\right) = 1$, is equal to 2 (b) 3 (c) 4 (d) 6

A. 2

B. 4

C. 6

D. 8

Answer: B



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21. The complete set of values of $x, x \in \left(-\frac{\pi}{2}, \pi\right)$ satisfying the inequality $\cos 2x > |\sin x|$ is :

A. $\left(-\frac{\pi}{6}, \frac{\pi}{6}\right)$

B. $\left(-\frac{\pi}{2}, \frac{\pi}{6}\right) \cup \left(\frac{\pi}{6}, \frac{5\pi}{6}\right)$

C. $\left(-\frac{\pi}{2}, -\frac{\pi}{6}\right) \cup \left(\frac{5\pi}{6}, \pi\right)$

D. $\left(-\frac{\pi}{6}, \frac{\pi}{6}\right) \cup \left(\frac{5\pi}{6}, \pi\right)$

Answer: D

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22. The total number of solution of the equation $\sin^4 x + \cos^4 x = \sin x \cos x$ in $[0, 2\pi]$ is :

A. 2

B. 4

C. 6

D. 8

Answer: A

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23. The number of solutions of equation $\sin \frac{5x}{2} - \sin \frac{x}{2} = 2$ in $[0, 2\pi]$ is

- A. 1
- B. 2
- C. 0
- D. Infinite

Answer: C



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24. In the interval $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ the equation $\log_{\sin \theta}(\cos 2\theta) = 2$ has

- A. No solution
- B. One solution
- C. Two solution
- D. Infinite solution

Answer: B



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25. If α and β are 2 distinct roots of equation $a \cos \theta + b \sin \theta = C$ then

$\cos(\alpha + \beta) =$

A. $\frac{2ab}{a^2 + b^2}$

B. $\frac{2ab}{a^2 - b^2}$

C. $\frac{a^2 + b^2}{a^2 - b^2}$

D. $\frac{a^2 - b^2}{a^2 + b^2}$

Answer: D



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Exercise 2 One Or More Than One Answer Is Are Correct

1. If $2 \cos \theta + 2\sqrt{2} = 3 \sec \theta$ where $\theta \in (0, 2\pi)$ then which of the following can be correct ?

A. $\cos \theta = \frac{1}{\sqrt{2}}$

B. $\tan \theta = 1$

C. $\sin \theta = -\frac{1}{\sqrt{2}}$

D. $\cot \theta = -1$

Answer: A::B::C::D



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2. In a triangle ABC if $\tan C < 0$ then :

A. $\tan A \tan B < 1$

B. $\tan A \tan B > 1$

C. $\tan A + \tan B + \tan C < 0$

D. $\tan A + \tan B + \tan C > 0$

Answer: A::C

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3. The inequality $4 \sin 3x + 5 \geq 4 \cos 2x + 5 \sin x$ true for $x \in$

A. $\left[-\pi, \frac{3\pi}{2} \right]$

B. $\left[-\frac{\pi}{2}, \frac{\pi}{2} \right]$

C. $\left[\frac{5\pi}{8}, \frac{13\pi}{8} \right]$

D. $\left[\frac{23\pi}{14}, \frac{41\pi}{14} \right]$

Answer: A::B::C::D

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4. The least difference between the roots, in the first quadrant

$\left(0 \leq x \leq \frac{\pi}{2} \right)$, of the equation

$4 \cos x (2 - 3 \sin^2 x) + (\cos 2x + 1) = 0$, is

A. equal to $\frac{\pi}{2}$

B. $> \frac{\pi}{10}$

C. $< \frac{\pi}{2}$

D. $< \frac{\pi}{3}$

Answer: B::C::D

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5. General solution of the equation,

$$\cos x \cdot \cos 6x = -1 \text{ is } x =$$

A. has 50 solutions in $[0, 100\pi]$

B. has 3 solutions in $[0, 3\pi]$

C. has even number of solutions in $(3\pi, 13\pi)$

D. has one solution in $\left[\frac{\pi}{2}, \pi\right]$

Answer: A::C::D



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6. Identify the correct options :

A. $\frac{\sin 3\alpha}{\cos 2\alpha} > 0$ for $\alpha \in \left(\frac{3\pi}{8}, \frac{23\pi}{48} \right)$

B. $\frac{\sin 3\alpha}{\cos 2\alpha} < 0$ for $\alpha \in \left(\frac{13\pi}{48}, \frac{14\pi}{48} \right)$

C. $\frac{\sin 2\alpha}{\cos \alpha} < 0$ for $\alpha \in \left(-\frac{\pi}{2}, 0 \right)$

D. $\frac{\sin 2\alpha}{\cos \alpha} > 0$ for $\alpha \in \left(\frac{13\pi}{48}, \frac{14\pi}{48} \right)$

Answer: A::B::C::D



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7. The equation $\sin^4 x + \cos^4 x + \sin 2x + k = 0$ must have real solutions if :

A. $k = 0$

B. $|k| \leq \frac{1}{2}$

$$C. -\frac{3}{2} \leq k \leq \frac{1}{2}$$

$$D. -\frac{1}{2} \leq k \leq \frac{3}{2}$$

Answer: A::B::C



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8.

Let

$$f(\theta) = \left(\cos \theta - \cos \frac{\pi}{8}\right) \left(\cos \theta - \cos \frac{3\pi}{8}\right) \left(\cos \theta - \cos \frac{5\pi}{8}\right) \left(\cos \theta - \cos \frac{7\pi}{8}\right)$$

then :

A. maximum value of $f(\theta) \forall \theta \in R$ is $\frac{1}{4}$

B. maximum value of $f(\theta) \forall \theta \in R$ is $\frac{1}{8}$

C. $f(0) = \frac{1}{8}$

D. Number of principle solutions of $f(\theta) = 0$ is 8

Answer: B::C::D



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9. If $\frac{\sin^2 2x + 4 \sin^4 x - 4 \sin^2 x \cdot \cos^2 x}{4 - \sin^2 2x - 4 \sin^2 x} = \frac{1}{9}$ and $0 < x < \pi$. Then the value of x is :

A. $\frac{\pi}{3}$

B. $\frac{\pi}{6}$

C. $\frac{2\pi}{3}$

D. $\frac{5\pi}{6}$

Answer: B::D



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10. Solve $\sin^2 \theta \tan \theta + \cos^2 \theta \cot \theta - \sin 2\theta = 1 + \tan \theta + \cot \theta$

A. $\frac{\pi}{4}$

B. π

C. $\frac{7\pi}{12}$

D. None of these

Answer: C

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11. If $\sin \theta + \sqrt{3} \cos \theta = 6y - y^2 - 11$, $\theta \in [0, 4\pi]$, $y \in \mathbb{R}$ holds for

A. no values of x and θ

B. one value of x and two values of θ

C. two values of x and two values of θ

D. two pairs of values of (x, θ)

Answer: B::D

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Exercise 3 Comprehension Type Problems

1. Consider f, g and h be three real valued function defined on \mathbb{R} .

Let $f(x) = \sin 3x + \cos x, g(x) = \cos 3x + \sin x$ and

$$h(x) = f^2(x) + g^2(x)$$

Q. General solution of the equation $h(x) = 4$, is :

[where $n \in \mathbb{I}$]

A. $\frac{\pi}{8}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{6}$

D. $\frac{\pi}{2}$

Answer: B



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2. Consider f, g and h be three real valued function defined on \mathbb{R} .

Let $f(x) = \sin 3x + \cos x, g(x) = \cos 3x + \sin x$ and

$$h(x) = f^2(x) + g^2(x)$$

Q. General solution of the equation $h(x) = 4$, is :

[where $n \in I$]

A. $(4n + 1) \frac{\pi}{8}$

B. $(8n + 1) \frac{\pi}{8}$

C. $(2n + 1) \frac{\pi}{4}$

D. $(7n + 1) \frac{\pi}{4}$

Answer: A



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3. Consider f , g and h be three real valued function defined on \mathbb{R} . Let

$$f(x) = \sin 3x + \cos x, g(x) = \cos 3x + \sin x \quad \text{and}$$

$$h(x) = f^2(x) + g^2(x). \text{ Then,}$$

Number of point (s) where the graphs of the two function, $y=f(x)$ and

$y=g(x)$ intersects in $[0, \pi]$, is

A. 2

B. 3

C. 4

D. 5

Answer: C

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Exercise 5 Subjective Type Problems

1. Find the number of solutions of the equations

$$(\sin x - 1)^3 + (\cos x - 1)^3 + (\sin x)^3 = (2 \sin x + \cos x - 2)^3 \quad \text{in} \\ (0, 2\pi).$$

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2. If $x + \sin y = 2014$ and $x + 2014 \cos y = 2013$, $0 \leq y \leq \frac{\pi}{2}$, then find the value of $[x + y] - 2005$

(where $[.]$ denotes greatest integer function)



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3. The complete set of values of x satisfying $\frac{2 \sin 6x}{\sin x - 1} < 0$ and $\sec^2 x - 2\sqrt{2}\tan x \leq 0$ in $(0, \frac{\pi}{2})$ is $[a, b) \cup (c, d]$, then find the value of $\left(\frac{cd}{ab}\right)$.



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4. The range of value's of k for which the equation $2 \cos^4 x - \sin^4 x + k = 0$ has atleast one solution is $[\lambda, \mu]$. Find the value of $(9\mu + \lambda)$.



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5. Find the coodinates of the point of intersection of the curves $y = \cos x, y = \sin 3x$ if $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

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6. Find the number of solutions of the equation $2 \sin^2 x + \sin^2 2x = 2$, $\sin 2x + \cos 2x = \tan x$ in $[0, 4\pi]$ satisfying the condition $2 \cos^2 x + \sin x \leq 2$.

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7. If the sum of all the solutions of the equation $3 \cot^2 \theta + 10 \cot \theta + 3 = 0$ in $[0, 2\pi]$ is $k\pi$ where $k \in I$, then find the value of k .

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8. If the sum of all values of θ , $0 \leq \theta \leq 2\pi$ satisfying the equation $(8 \cos 4\theta - 3)(\cot \theta + \tan \theta - 2)(\cot \theta + \tan \theta + 2) = 12$ is $k\pi$, then k is equal to :

A. 2

B. 4

C. 12

D. 8

Answer: D



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9. Find the number of solutions of the equation $2 \sin^2 x + \sin^2 2x = 2$, $\sin 2x + \cos 2x = \tan x$ in $[0, 4\pi]$ satisfying the condition $2 \cos^2 x + \sin x \leq 2$.



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