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## MATHS

## BOOKS - CHETAN MATHS (TAMIL

## ENGLISH)

## CIRCLE

## Practice Set 31

1. In the adjoining figure, the radius of a circle
with center $C$ is 6 cm . Line $A B$ is a tangent at $A$.

Answer the following question.
what is the measure of $\angle C A B$ ? Why?

What is the distance of point $C$ from line $A B$ ?

Why?
(iii) $d(A, B)=6 \mathrm{~cm}$, find $d(B, C)$.
(iv) What the measure of $\angle A B C$ ? Why ?

2. In the adjoining figure, $O$ is the centre of the circle. From point R, seg RM and RN are tangent segments drawn which touch the circle at $M, N$. If $\mathrm{OR}=10 \mathrm{~cm}$, radius of the circle $=5 \mathrm{~cm}$, then find
(i) the length of each tangent segment
(ii) Measure of $\angle M R O$
(iii) Measure of $\angle M R N$


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3. In the figure, seg RM and seg RN are tangent segments of a circle with centre O. Prove that seg OR divides $\angle M R N$ as well as $\angle M O \mathbb{N}$


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4. What is the distance between two parallel tangents of a circle having dradius 4.5 cm . Justify your answer

Given :
(i) A circle with center O and radius 4.5 cm .
(ii) Line I is tangent to the circle at point A
(iii) Line $m$ is tangent to the circle at point $B$


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Practice Set 32

1. Two circles having radii 3.5 cm and 4.8 cm touch each other internally. Find the distance between their centres .

## Given :

(i) Two circles with centres $A$ and $B$ touch each other internally at point $P$.
(ii) Radius of circle with centre $A$ is 4.8 cm .
(iii) Radius of circle with center $B$ is 3.5 cm .

To Find : AB


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2. Two circle having radii $5.5 \mathrm{~cm}, 4.2$ touch each other externally. Find distance between
their centres ?

Given :
(i) Two circles with centres $P$ and $Q$ touch each other extaranlly at point R .
(ii) Radius of circle with centre $P$ is 5.5 cm
(iii) Radius of circle with centre $Q$ is 4.2 cm

3. Draw two externally touching circles and internally touching circles with radii 4 cm and 2 .8 cm ,

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4. In the adjoining figure the circles with centers $P$ and $Q$ touch each other at $R$. A line passing through $R$ meets the circles at $A$ and $B$ respectively then

Prove that :
(i) $\operatorname{seg} A P|\mid \operatorname{seg} B Q$.
(ii) $\Delta A P R \sim \Delta R Q B$.
(iii) Find $\angle R Q B$ if $\angle P A R=35^{\circ}$


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5. In the adjoining figure, the circles with centres A and B touch each other at E Line I is a common tangent that touches the circles at C
and $D$ respectively. Find length of seg CD if the radii of the circles are $4 \mathrm{~cm}, 6 \mathrm{~cm}$ ?

## Construction :

Draw seg AE and seg EB.

Draw seg AF $\perp$ seg BD, B-F-D


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# 1. In the adjoining figure, G, D, E, F are concyclic 

 points of a circle with centre C. $\angle E C F=70^{\circ}$ $\mathrm{m}(\operatorname{arc} \mathrm{DGF})=200^{\circ}$ find(i) $m$ arc $D E$
(iii) m (arc DEF).


E

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2. In the adjoining figure, $\triangle Q R S$ is an equilateral triangle.
(1) are $R S \cong \operatorname{arc} Q S \cong \operatorname{arc} Q R$
(2) $\mathrm{m}(\operatorname{arc} \mathrm{QRS})=240^{\circ}$.



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3. In the adjoining figure, chord $A B \cong$ chord $C D$. Prove that arc $A C \cong B D$


## Practice Set 34

1. In the abjoining figure, point $O$ is the centre of the circle. Length of chord $A B$ is equal to the radius of the circle. Find
(i) $\angle A O B$
(ii) $\angle A C B$
(iii) $\mathrm{nm}(\operatorname{arc} \mathrm{AB})$
(iv) $\mathrm{m}(\operatorname{arc} \mathrm{ACB})$


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2. In the adjoining figure, $\square P Q R S$ is a cyclic quadrilateral. Side $\mathrm{PQ} \cong$ side RQ .
$\angle P S R=110^{\circ}$. Find
(i) $\angle P Q R$
(ii) $m(\operatorname{arc} P Q R)$
(iii) $m(\operatorname{arc} Q R)$
(iv) $\angle P R Q$

3. In cyclic $\square M R P N$
$\angle R=(5 x-13)^{\circ}$ and $\angle N=(4 x+4)^{\circ}$. Find the measures of $\angle R$ and $\angle N$.

4. In the adjoining figure seg RS is the dianeter of the circle with centre ' O ' . Point T is in the exterior of the circle. Prove that $\angle R T S$ is an acute angle.

5. Prove that any rectangle is a cyclic quadrilateral.

Given : $\square P Q R S$ is rectangle

To prove : $\square P Q R S$ is cyclic quadrilateral ('\#\#CTN_MK_MAT_X_P2_GEO_CO3_EO4_005_Q01.png" width="80\%">

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6. In the adjoining figure, m (arc NS) $=125^{\circ}$ $\mathrm{m}(\operatorname{arcEF})=37^{\circ}$. Find $\mathrm{m} \angle N M S$.


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7. In the adjoining figure, chord $A C$ and and chord DE intersect at point B . If
$\angle A B E=108^{\circ}$ and $\mathrm{m}(\operatorname{arc} \mathrm{AE})=95^{\circ}$, then
find $m(\operatorname{arc} D C)$.


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Practice Set 35

## 1. In the adjoining figure, point $Q$ is the point of

 contact of tangent and circle . If $\mathrm{PQ}=12, \mathrm{PR}=8$, then find Ps and RS .
2. In the adjoining figure, point $B$ is the point of contact and point O is the centre of the circle.

Seg $O E \perp$ se $A D$, if $A B=12, A C=8$, then find
(i) $A D$
(ii) DC and
(iii) DE

3. In the adjoining figure, if $P Q=6, Q R=10, P S=$ 8, then find TS.


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4. In the adjoining figure, seg EF is the diameter of the circle with centre H . Line DF is tangent at point $F$. If $r$ is the radius of the circle, then prove that $D E \times G E=4 r^{2}$

To Prove : $D E \times G E=4 r^{2}$


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Problem Set 3

1. In the adjoining figure, $M$ is the centre of the
circle and seg KL is a tangent segment. If $\mathrm{MK}=$
$12, \mathrm{KL}=6 \sqrt{3}$, then
(i) Find radius of the circle.
(ii) Find measure of $\angle K$ and $\angle M$.


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2. In the adjoining figure, circle with centre $M$ touches the circle with center N at point T . Radius MR touches the smaller circle at S . Radii
of circles are 9 cm and 2.5 cm . Find the answers
to the following questions hence find the ratio

MS : SR.
(i) Find the lenght of seg MT
(ii) Find the length fo seg MN
(iii) Find measure of $\angle N S M$.


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3. In the adjoining fig. circles with centres $X, Y$ touch each other at Z . A secant passing through $Z$ meets the circles at $A$ and $B$ respectively. Prove that, radius $\mathrm{XA} \|$ radius YB .

Fill in the blanks and complete the proof.

4. In the adjoining figure, seg $A B$ is a diameter of a circle with centre C. Line PQ is a tangent, it touhces the circle at $T$. segs $A P$ and $B Q$ are perpendiculars to line $P Q$. Prove seg $C P \cong$ seg CQ.

5. Draw circles with centres $A, B, C$ each with radius 3 cm such that each circle touches the remaining two circles.

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6. Prove that any three points on a circle cannot be collinear.
7. In the adjoining figure, line PR touches the circle at point $Q$. Using the information given in the diagram, answer the following questions.
(i) What is the sum of $\angle T A Q$ and $\angle T S Q$ ?
(ii) Write names of angles congruent to $\angle A Q P$.
(iii) Write names of angles congruent to $\angle Q T S$
(iv) If $\angle T A S=65^{\circ}$, then find $\angle T Q S$ and arc TS.
(v) It $\angle A Q R=42^{\circ}$ and $\angle S Q R=58^{\circ}$, then
find $\angle A T S$.


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8. In a circle with centre 'O' chord PQ $\cong$ chord RS

IF $\mathrm{m} \angle P O R=70^{\circ}$ and $\mathrm{m}(\operatorname{arc} \mathrm{RS})=80^{\circ}$, then find
(1) $m(\operatorname{arc} P R)$
(2) m (arc QSR)
(3) m (arc QS)


# 9. In the adjoining figure, $\mathrm{m}(\operatorname{arc} \mathrm{WY})=44^{\circ} \mathrm{m}$ 

$(\operatorname{arc} Z X)=68^{\circ}$, then
(i) Find $\mathrm{m} \angle Z T X$.
(ii) If $\mathrm{I}(\mathrm{WT})=4.8, \mathrm{I}(\mathrm{TX})=8 \mathrm{I}(\mathrm{YT})=6.4$, then find

I(TZ)
(iii) If $I(W X)=25, I(Y T)=8 I(Y Z)=26$, then find


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10. In the adjoining figure,
(i) if $\mathrm{m}(\operatorname{arcCE})=54^{\circ}, \mathrm{m}(\operatorname{arcBD})=23^{\circ}$, then
find $\angle C A E$.
(ii) If $A B=4.2, B C=5.4, A E=12$, then find $A D$
(iii) If $A B 3.6, A C=9.0, A D=5.4$, then find AE.


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11. In the adjoining diagram, chord EF || chord GH. Prove that chord EG $\cong$ chord FE.
[Complete the following for the proof]

12. In the adjoining figure,seg $A B$ is a diameter of a circle with centre O. Bisector of inscribed
$\angle A C B$ intersects circle at point D. Complete the following proof by filling in the blanks.

Prove that : seg $A D \cong \operatorname{seg} B D$


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13. In the adjoining figure, seg MN is a chord of
a circle with centre $\mathrm{O} . \mathrm{I}(\mathrm{MN})=25$. Point L on
chord MN such that $\mathrm{I}(\mathrm{MN})=9$ and $\mathrm{I}(\mathrm{OL})=5$, then
find radius of the circle.


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14. In the adjoining figure, two circles intersect each other at points $M$ and $N$. Secants drawn from points $M$ and $N$ intersect cirecls at point $R, S, P$ and $Q$ as shown in the figure.

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15. In the adjoining figure, two circles intersect
each other at points $A$ and $E$. Their common
secant through E intersects the circle at points
$B$ and D. The tangents of the circles at point B and D intersect each other at point C. Prove
that $\square A B C D$ is cyclic .


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16. In the adjoining figure, seg $A D \perp$ side $B C$,
seg $B E \perp$ side $A C$, segCf $\perp$ side $A B$. Point $O$
is the orthocentre. Prove that, point O is the
incentre of $\triangle D E F$


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Problem Set 3 Mcqs

1. Two circles of radii 5.5 cm and 3.3 cm respectively touch each other. What is the distance between their centres ?
A. 4.4 cm
B. 8.8 cm
C. 2.2 cm
D. 8.8 or 2.2 cm

Answer: B::C
2. Two circles intersect each other such that each circle passes through the centre of the other. If the distance between their centres is 12 , what is the radius of each circle ?
A. 6 cm
B. 12 cm
C. 24 cm
D. can't say

Answer: A::B::C
3. A circle touches all sides of a parallelogram.

So the parallelogram must be a
A. rectangle
B. rhombus
C. square
D. trapezium

Answer: B
4. Length of a tangent segment drawn from a point which is at a distance 12.5 cm from the centre of a circle is 12 cm find diameter of the circle.
A. 25 cm
B. 24 cm
C. 7 cm
D. 14 cm

Answer: C
5. If two circles are touching externally, how many common tangents of them can be drawn ?
A. One
B. Two
C. Three
D. Four

## Answer:

6. $\angle A C B$ is inscribed in area ACB of a circle with centre 0 . If $\angle A C B=65^{\circ}$, find m (arc ACB).
A. $65^{\circ}$
B. $130^{\circ}$
C. $295^{\circ}$
D. $230^{\circ}$

Answer: B::C
7. Chords $A B$ and $C D$ of a circle intersect inside the circle at point $E$. If $A E=5.6, E B=10, C E=$ 8,find ED.
A. 7
B. 8
C. 11.2
D. 9
8. In a cyclic $\square A B C D$, twice the measure of
$\angle A$ is thrice the measure of $\angle C$. Find the measure of $\angle C$.
A. 36
B. 72
C. 90
D. 108
9. Points $A, B, C$ are on a circle, such that $m$ (arc
$A B)=m(\operatorname{arc} B C)=120^{\circ}$. No point, except point $B$, is common to arcs. Which is the type of $\triangle A B C ?$
A. Equilateral triangle
B. Scalene triangle
C. Right angled triangle
D. Isosceles triangle

## Answer: A

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10. Seg $X Y$ is a diameter of a circle . Point $Y$ lies
in its interior. How many of the following statements are true ?
(i) It is not possible that $\angle X Y Z$ is an acute angle.
(ii) $\angle X Y Z$ can't be a right angle.
(iii) $\angle X Y Z$ is an obtuse angle.
(iv) Can't make a difinite statement for measure of $\angle X Y Z$
A. Only one
B. Only two
C. Only three
D. All

## Answer:

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1. $\angle Q P R=60^{\circ}$
$\therefore \angle A O B=$

A. $60^{\circ}$
B. $90^{\circ}$
C. $120^{\circ}$
D. $240^{\circ}$

## Answer: C

## D Watch Video Solution

2. Angle between external end point of radius and tangent is
A. $90^{\circ}$
B. an acute angle
C. an obtuse angle
D. $45^{\circ}$

## Answer:

## D Watch Video Solution

3. Point $P$ is on the circle. $A B$ is diameter of the
circle, $\angle A P B$ is
A. a Reflex angle
B. an acute angle
C. a Right angle
D. an obtuse angle

Answer: A

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4. MN is tangent at M and
AM is radius
Find
AM.
A. 6
B. 3
C. $3 \sqrt{3}$
D. 1

Answer: B

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5. $\angle A D C=80^{\circ}$, then
$\angle C B E=$ ?

A. $100^{\circ}$
B. $10^{\circ}$
C. $80^{\circ}$
D. $280^{\circ}$

Answer:
6. $\angle X Y Z=40^{\circ}, \angle A Y Z=20^{\circ}$ line Ay is
tangent at point $Y$.
$\therefore \mathrm{m}(\operatorname{arc} \mathrm{XY})=. . . . .$.

A. $80^{\circ}$
B. $40^{\circ}$

## C. $60^{\circ}$

D. $120^{\circ}$

Answer: C

## D Watch Video Solution

7. $A B$ is tangent at $B . A B=12, A P=6$
$\therefore P Q=\ldots . . .$.

A. 18
B. 6
C. 12
D. 20

Answer: A
8. Line PT is tangent at point $T$. Which of the following is true?

A. $\angle A B T \cong \angle A P T$
B. $\angle A B T \cong \angle B A T$

## C. $\angle B A T \cong \angle B T Q$

D. None of (A), (B), (C)

Answer: A::B

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9. $A$ circle with centre $P$. Line $A B$ and line $A C$ are tangents from point $A$ at points $B$ and $C$ respectively. Which of the following is/ are true

A. $\angle B P A \cong \angle C P A$
B. $\angle B A P \cong \angle C A P$
c. $\angle P B A \cong \angle P C A$
D. All of (A), (B), (C)

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10. In adjoining figure, $\mathrm{PQ}=\mathrm{QR} . \angle P=60^{\circ}$
$\therefore \mathrm{m}(\operatorname{arc} \mathrm{PR})=. . .$.

A. $120^{\circ}$

B. $60^{\circ}$

C. $90^{\circ}$
D. $240^{\circ}$

Answer: A

## (D) Watch Video Solution

Problems For Practice Based On Parctice Set 31

1. In the adjoining figure, point $P$ is the centre of the circle and line $A B$ is the tangent to the circle at T . The radius of the circle is 6 cm . Find PB if $\angle T P B=60^{\circ}$


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2. In the adjoining figure point $A$ is the centre of the circle $. \mathrm{AN}=10 \mathrm{~cm}$. Line NM is tangent at $M . M N=5 \mathrm{~cm}$. Find the radius .

3. Two tangents TP and TQ are drawn to a circle with centre O from an external point T . Prove that $\angle P T Q=2 \angle O P Q$

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4. In the adjoining figure, $O$ is the centre and $\operatorname{seg} A B$ is a diameter. At point $C$ on the circle,
the tangent $C D$ is drawn. Line $B D$ is tangent at
B. Prove that seg OD \| seg AC.


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Problems For Practice Based On Parctice Set 32

1. Two circles of radii 5 cm and 3 cm touch externally. Find the distance between them.

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2. Find the distance between two internally
touching circles whose radii are 10 cm and 2
cm.
3. The circles which are not congruent touch externally. The sum of their areas is $130 \pi \mathrm{~cm}^{2}$ and distance between their centres is 14 cm . Find the radii of the two circles.

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4. In the adjoining figure circles with centres $A$ and $C$ touch internally at point $T$. Line $A B$ is tangent to the smaller circle at point $P$. Point $B$
lies on the bigger circle. Radii are 16 cm and 6
cm . Find AP.


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5. The radii of two circles are 25 cm and 9 cm .

The distance between their centres is 34 cm .

Find the length of the common tangent segmentto these circles .

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## Problems For Practice Based On Parctice Set 33

1. In the adjoining figure, a circle with centre ' O '
are $P Q=\operatorname{arc} Q R=\operatorname{arc} P R$. Find measure of each
arc


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2. A circle with centre ' O '. Chord $P Q \cong$ chord RS . $M(\operatorname{arc} P X Q)=260^{\circ}$. Then find $m(\operatorname{arc} R X S)$.


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3. $A$ circle with centre $P$. arc $A B=\operatorname{arc} B C$ and $\operatorname{arc}$
$A X C=2 \operatorname{arc} A B$. Find measure of $\operatorname{arc} A B, \operatorname{arc} B C$
and arc AXC . Prove that chord $A B \cong$ chord BC


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4. In the adjoining figure, chord $A D \cong$ chord $B C . M(\operatorname{arc} A D C)=100^{\circ} \mathrm{m}(\operatorname{arc} C D)=60^{\circ}$

Find $m(\operatorname{arc} A B)$ and $m(\operatorname{arc} B C$.


Problems For Practice Based On Parctice Set 34

1. If $\mathrm{m}(\operatorname{arc} \mathrm{APC})=60^{\circ}$ and $\angle B A C=80^{\circ}$. Find (a) $\angle A B C$ (b) $\mathrm{m}(\operatorname{arc} \mathrm{BQC})$

2. chords $A B$ and $C D$ of a circle intersect in point $Q$ in the interior of a circle of a shown in the figure. If $\mathrm{m}(\operatorname{arc} A D)=20^{\circ}$, and $\mathrm{m}(\mathrm{ARC} \mathrm{BC})$
$=36^{\circ}$ then find $\angle B Q C$

3. Secants containing chords RS and PQ of a circle intersect each other in point $A$ in the exterior of a circle. If $\mathrm{m}(\operatorname{arc} \mathrm{PCR})=26^{\circ} \mathrm{m}(\operatorname{arc}$

QDS $=48^{\circ}$, then find (1) $\angle A Q R$ (2) $\angle S P Q$
(3) $\angle R A Q$.

4. In the adjoining figure, $O$ is the centre of the
circle . Find the value of $\angle A B P$ if
$\angle P O B=90^{\circ}$

5. If two consecutive angles of cyclic quadrilateral are congruent, then prove that one pair of opposite sides is congruent and other is parallel.

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6. $\square A B C D$ is a parallelogram . Side BC intersects circle at point $P$. Prove that DC = DP .


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7. In the adjoining figure, chord Pq and chord
$A B$ intersect at point $M$. If $P M=A M$, then prove
that $B M=Q M$.


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Problems For Practice Based On Parctice Set 35

1. Seg $A B$ and seg $A D$ are the chords of the circle . C is a point on tangent of the circle at point $A$. If $m(a r c ~ A P B)=80^{\circ}$ and $\angle B A D=30^{\circ}$ The find (i) $\angle B A C$ (ii) m (arc BQD).

2. Secant $A C$ and secnat $A E$ intersects in point $A$
. Points of intersections of the circle and secants are $B$ and $D$ respectively. If $C B=5, A B=$ 7, EA = 20 . Determine ED - AD


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3. In the adjoining figure line PA is tangent at point $A$. Line $P B C$ is a secant. If $A P=15$ and $B P=$ 10 , find $B C$.


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4. $\square A B C D$ is a rectangle. Taking AD as a diameter, a simicircle AXD is drawn which intersects the diagonal $B D$ at $X$. If $A B=12 \mathrm{~cm}$,
$A D=9 \mathrm{~cm}$, then find values of $B D$ and $B X$.

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5. In the adjoining figure point $O$ is the centre of the circle. Line PB is a tangent and line PAC is a secnt. Find $P a \times \mathrm{PC}$ if $\mathrm{OP}=25$ and radius is
6. 



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Assignment 3 A Solve The Following Sub
Questions

1. Two circles with diameters 6 cm and 9 cm touch each other externally. Find the distance between their centres.

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Assignment 3 B Solve Any One Of The Following
Questions

1. Line PA os a tamgemt at point $A$. Line $P B C$ is a
secant $A P=15, B P=10$, find $B C$.


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## Assignment 3 Solve Any One Of The Following Questions

1. Measure of a major arc of a circle is four
times the measure of corresponding minor arc.

Find the measure of each arc.

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2. Line PA and line PB are tangents to the circle at points A and B . If $\angle A P B=60^{\circ}$ then find $m(\operatorname{arc} A X B)$.


## Assignment 3 Solve The Following Sub Questions

 Any Two1. Two circles with centres $P$ and $Q$ touch each other at point A. $\angle B P A=60^{\circ}$. Find $\angle Q C A$ and $\angle C Q P$


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2. Line $P Q$ is a tangent to the circle at point $A B$ $\cong$ arc AC. Complete the following activity to prove $\triangle A B C$ as isosceles triangle.


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3. Two circles intersect each other in point $A$ and $B$. Secants through $A$ and $B$ intersect circles in C, D and $M, N$ as shown in the figure prove that: $C M|\mid D N$


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Assignment 3 Solve Any Two Of The Following

## Questions

1. A circle with centre ' $O$ ' is incircle of
$\triangle A B C . \Delta B C A=90^{\circ}$. Radius of the circle is
r.

Prove that: $2 r=a+b-c$.


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2. In the adjoining figure line PA is a tangent to
the circle at point A. Secant PQZ intersects
chord $A Y$ in point $X$, such that $A P=P X=X Y$. If $P Q$
$=1$ and $Q Z=8$. Find $A X$.

(D) Watch Video Solution

## 3. In the adjoining figure, $O$ is the centre of the

circle $X Y$ is a diameter. $O Y=Y R, O-Y-R, R Z$ is a
tangent through Z.A thangent through the point $Y$ intersects $R Z$ in $Q$ and $X Z$ in $P$
prove that : $\triangle P Q Z$ is an equilateral triangle.


