

MATHS

BOOKS - CHHAYA PUBLICATION MATHS (BENGALI ENGLISH)

INTRODUCTION TO THREEDIMENSIONAL COORDINATE GEOMETRY

Example

1. Find the octants in which the following points lie:

(2,3,4)



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2. Find the octants in which the following points lie:

(2,3,-4)



3. Find the octants in which the following points lie:

$$(-1, -2, 3)$$



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4. Find the octants in which the following points lie:

$$(-3, -4, -5)$$



5. Find the octants in which the following points lie:

$$(-1,2,5)$$



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6. Find the octants in which the following points lie:

$$(2, -1, -3)$$



7. Find the octants in which the following points lie:

(1, -3, 4)



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8. Find the octants in which the following points lie:

(-2,-3,5)



9. Let P (a, b, c) be any point in space, state the signs of a, b and c if P lies on octant OXY'Z'



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10. Let P (a, b, c) be any point in space, state the signs of a, b and c if P lies on octant OX 'YZ



11. Let P (a, b, c) be any point in space, state the signs of a, b and c if P lies on octant OX ' Y' Z '



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12. Let P (a, b, c) be any point in space, state the signs of a, b and c if P lies on octant **OXYZ**



13. Let P (a, b, c) be any point in space, state the signs of a, b and c if P lies on octant OX'Y'Z



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14. Let P (a, b, c) be any point in space, state the signs of a, b and c if P lies on octant OXY'Z



15. Where do the following points lie?

$$(0, -2, -3)$$



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16. Where do the following points lie?

(0,0,-3)



17. Where do the following points lie?

(2,1,0)



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18. Where do the following points lie?

(2,0,0)



19. Where do the following points lie? (3,0,-4)



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20. find the distance of the point (2, 3, -4) from the origin. Unsing the same digits state the coordinates of the points having the same distance from the origin.



21. If the distance between the points (- 1, -3, c) and (2,1,-2) is $5\sqrt{2}$ unit, find c.



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22. Find the points on the z-axis which are at a distance of $\sqrt{29}$ unit from the point (2, -3, -2).



23. Show that the points (p , q , r) , (q , r , p) and (r , p , q) are the vertices of an equilateral triangle.



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24. Show that the points A (4, 7, -6), B (2, 5,

-4) and C (1,4,-3) are collinear.



25. Find the equation to the locus of a moving point which is always equidistant from the points (3, 4, -5) and (-2, 1, 4)



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26. Prove that the points (1, -3, 1), (0, 1, 2) and (2, -1, 3) are the vertices of a right angled isosceles triangle.



27. Find the perpendicular distances of the point (2,3,4) from the z coordinate axes.



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28. Find the point in yz-plane which is equidistant from the points (2,0,3), (3,2,0) and (1,0,2).



29. Find the point on the x-axis which is equidistant from the points (2, -1, 3) and (-3, 2, -4).



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30. The sum of the distances of a moving point from the points (5, 0, 0) and (-5, 0, 0) is always 20 unit . Find the equation to the locus of the moving point .



31. Find the coordinates of the point equidistant from the four points (2,1,2),(-1,1,3),(0,5,6) and (3,2,2).



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32. Show that the pointsO (0,0,0),P (a,a,0)
Q (a,0,a) and R (0,a,a) from regular tetrahedron.



33. Prove that the points A(-5, 1, 1), B(1, 3, 4), C(-1, 6, 10) and D(-7, 4, 7) taken in order are the vertices of a rhombus.



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34. Find the coordinates of the point which divides the line- segment joining A (2, -1, 3) and B (-3, 1, 4) (i) internally in the ratio 2: 3 (ii) externally in the ratio 4: 3



35. Find the ratio in which the line -segment joining the points (2,0,-4) and (-42,6) is divided by the xy - plane. Also find the coordinates of the point of division .



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36. Find the coordinates of the point of trisection of the line-segment joining the points (0,2,1) and (2,-1,5) that is nearer to (0,2,1).

37. Two vertces of a parallelogram are (2, 5, -3) and (3, 7, -5), it its diagonals meet at (4, 3, 3), find the coordinates of the other two vertices.



ABC with vertices A (-3, p, 2), B (2, -4, q) and

38. If (2, -3, 1) is the centroid of the triangle

C(r,3,5), find the values of p, q, r.



- **39.** Two vertices of triangle are (4, 3, -6), (3, -4
- , 4) and the coordinates of its centroid are (2 ,
- 2, 1), find the coordinates of the third vertex of the triangle.



40. Three vertices of triangle ABC are A (3 , 2 , -1) B (-1 , -1 , -1) and C (1, 5, 5) , if the internal bisector of $\angle BAC$ meets the opposite side \overline{BC} at D , then find the coordinates of D .



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41. Find the ratio in which the line-segment joining the points (2, 1, 3) and (1, -3, -4) is divided by the plane $3 \times 2y - 3z = 3$. Also find the coordinates of the point of division.

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- **42.** Find the image of the point
- (3, 2, -4) in the xy-plane



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- 43. Find the image of the point
- (3, 2, -4) in the yz plane



44. Find the image of the point

(3, 2, -4) in the zx-plane.



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45. The coordinates of the mid-points of the sides of a triangle are (4,3,4),(1,5,-1) and (0,4,-2), find the coordinates of the vertices of the triangle.



46. A point with y-coordinate 5 lies on the line-segment joining the points (1, 4, -3) and (4, 7, -6), find the coordinates of the point.



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47. Applying section formulae show that the points A(4,7,-6), B(2,5,-4) and C(1,4,-3) are collinear.



Multiple Choice Questions

1. The equation of zx - plane is _

$$A. x = 0$$

$$B. y = 0$$

$$\mathsf{C}.\,z=0$$

D. none of these

Answer: B



2. x=0,y=0 represent the equation of _

A. x - axis

B. y - axis

C. z - axis

D. none of these

Answer: C



3. The coordinates of any point in yz - plane are of the form_

A.
$$(x, 0, z)$$

B.
$$(x, y, 0)$$

D. none of these

Answer: C



4. y = b and z = c represent the equation of a line parallel to _

A. x - axis

B. y - axis

C. z - axis

D. none of these

Answer: A



5. x = a represents the equation of a plane parallel to _

A. xz - plane

B. xy-plane

C. yz-plane

D. none of these

Answer: C



6. (0, a, 0) are the coordinates of any point on

- A. x-axis
- B. y axis
- C. z axis
- D. none of these

Answer: B



7. The points (5,2,4), (6,-1,2) and (8,-7,

k) are collinear if k=

A. 3

B.-3

C. 2

D.-2

Answer: D



8. If the distance between the points (- 1, 1, c) and (2, 1, 1) is 3, then the value of C is _

A. 3

B. 2

C. 1

D. -1

Answer: C



9. The equation of xy-plane is _

A.
$$x = 0$$

$$B. y = 0$$

$$C. z = 0$$

D. none of these

Answer: C



10. The coordinates of any point on the line-segment joining the points (x_1,y_1,z_1) and (x_2,y_2,z_2) are $\left(\frac{x_1+kx_2}{k+1},\frac{y_1+ky_2}{k+1},\frac{z_1+kz_2}{k+1}\right)$, then the

value of k will be _

A. Positive integers

B. negative integers

C. real numbers

D. imaginary numbers

Answer: C

11. The ratio in which the line-segment joining the points (2, -3, 4) and (3, 4, -1) is divided by the zx-plane is _

A. 3:4

B. 4:3

C. -2:3

D. 1: 4

Answer: A

12. If the coordinates of two extremities of a diagonal of a square are (4,4,7) and (0,6,

3), then the length of a side is _

A. 3 unit

B. 4 unit

C. $3\sqrt{2}$ unit

D. $2\sqrt{6}$ unit

Answer: C

13. The equation of z-axis in three-dimensional space is _

A.
$$y = 0, z = 0$$

$$\mathtt{B.}\,x=0,y=0$$

C.
$$x = 0, z = 0$$

D. none of these

Answer: B



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14. YOZ-plane divides the line-segment joining the points (3, -2, -4) and (2, 4, -3) in the ratio

A. 1:2

B.-4:3

C. -2:3

D. -3:2

Answer: D

15. XOY-plane divides the join of (x,y,z) and (

-y,-z,-x) in the ratio

A. x: z

B.z:x

C. y: z

D. y: x

Answer: B



16. The coordinates of the vertices of a triangle are (4,6,0),(0,-3,7) and (-4,0,-1), then the coordinates of the centroid of the triangle are _

A. (0, 1, 2)

B. (-1, 1, 2)

 $\mathsf{C}.\,(0,2,1)$

D. none of these

Answer: A

17. The equation of yz-plane is _

A.
$$y + z = 0$$

$$\mathsf{B.}\,yz=0$$

$$C. y = 0$$

$$\mathsf{D}.\,x=0$$

Answer: D



18. The equation of a plane parallel to xy - plane is _

$$A. xy = a$$

$$\mathrm{B.}\,x+y=a$$

$$\mathsf{C}.\,z=c$$

D. none of these

Answer: C



Very Short Answer Type Questions

1. Find the octants in which the following points lie:

$$(3,4,-5)$$



2. Find the octants in which the following points lie:

$$(-2,1,5)$$



3. Find the octants in which the following points lie:



4. Find the octants in which the following points lie:

$$(1, -3, 2)$$



5. Find the octants in which the following points lie:

(2,2,2)



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6. Find the octants in which the following points lie:

(-3,-3,-2)



7. Find the octants in which the following points lie:

$$(-2, -3, 1)$$



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8. Find the octants in which the following points lie:

$$(2,-1,-2)$$



9. Find the octants in which the following points lie:

$$(-3,2,-1)$$



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10. Let P(x, y, z) be any point in threedimensional space, state the signs of x, y and zif P lies on octant

OX'YZ'



11. Let P(x, y, z) be any point in three-dimensional space, state the signs of x, y and zif P lies on octant

OX'Y'Z



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12. Let P(x, y, z) be any point in threedimensional space, state the signs of x, y and zif P lies on octant

OX 'YZ

13. Let P(x, y, z) be any point in three-dimensional space, state the signs of x, y and z if P lies on octant



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14. Let P (x, y, z) be any point in three-dimensional space, state the signs of x, y and

zif P lies on octant

OXY'Z'



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15. Let P(x, y, z) be any point in three-dimensional space, state the signs of x, y and z if P lies on octant

OX'Y'Z'



16. Let P(x, y, z) be any point in three-dimensional space, state the signs of x, y and zif P lies on octant OXY7'



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17. Let P(x, y, z) be any point in three-dimensional space, state the signs of x, y and z if P lies on octant OXY'Z

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18. Where do the following points lie?



(3,0,0)

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19. Where do the following points lie?

(0, -2, -3)



20. Where do the following points lie? (2,1,0)



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21. Where do the following points lie? (0, -4, 0)



22. Where do the following points lie? (3,0,4)

23. Where do the following points lie?

(0,0,-5)



24. Where do the following points lie?

(-4,0,0)



25. Where do the following points lie? (0,0,6)



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26. Find the distance of the point (-6, 2, -3) from the origin. State the coordinates of the points with same numerical values of x, y and z-coordinates.



27. Find the distance between the points (-1,2,4),(-1,-1,-2).



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28. Find the distance between the points (-4,3,7) and (-1,-2,3)



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29. Find the perpendicular distance of the point (1, -2, -3) from the coordinates axes.

30. Prove that the triangle formed by joining the points

(2,3,4),(3,4,2),(4,2,3) is an equilateral triangle.



31. Prove that the triangle formed by joining the points

(2,3,-1),(4,5,0),(2,6,2) is and isosceles triangle.



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the points (-4,9,6),(0,7,10),(-1,6,6) is an isosceles

32. Prove that the triangle formed by joining



right angled triangle.

33. Prove that the triangle formed by joining the points

(1,-3,1),(0,1,2),(2,-1,3) is a right angled triangle.



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34. Prove that the points (4 , 7 , - 6) , (2 , 5 , -4) and (1 , 4 , - 3) are collinear .



35. Find the coordiantes of the point in the xyplane which is equiistant from the points A (0 , 0 , 1) , B (2 , 0 , 3) and C (0 , 3 , 2) .



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36. If the distance between the points (x, -1, 2) and (-4, 1, 5) is 7 unit, then find the value of x.



37. Show that the points A (3,2,-4), B (5,4,

-6) and C (9,8,-10) are collinear. Also find the ratio in which C divides the line-segment AB .



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38. Find the coordinates of the points on y axis which are at a distance $\sqrt{41}$ unit from the point (3,2,-4).



39. Find the coordinates of the point in xy-plane which is equidistant from the points (1, -2, -3), (3, 0, 3) and (0, -2, -4).



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40. Find the coordinates of points on z-axis which are at a distance of 7 unit from the point (-3,-2,2).



41. Determined the equation to the locus of the point which is equidistant from the points (2,-2,-4) and (-3,1,2).



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42. Find the coordinates of the point which is equidistant from the points (0,0,0), (6,0,0), (0,-4,0) and (0,0,-2).



43. Find the equation to the locus of the point whose distance from the point (- 2, -3, 2) is 6 unit.



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44. Find the perimeter of the triangle whose vertices are (0,1,2),(2,0,4) and (-4,-2, 7).



45. Find the images of the point (3, -4, 6) with respect to yz-plane



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46. Find the images of the point (3, -4, 6) with respect to zx-plane



47. Find the images of the point (3, - 4, 6) with respect to xy - plane



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48. Prove that the points (4,7,6),(2,3,2), (-1,-2,-1) and (1,2,3) taken in order are the vertices of a parallelogram . Is the the parallelogram a rectangle?



49. Three consecutive vertices of a parallelogram are (1, 2, -4), (-1, 1, 2), (1, -2, 8), find the coordinates of fourth vertex.



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50. Two vertices of the parallelogram ABCD are A(8,14,12) and B(4,6,4) and its diagonals intersect at (3,5,5), find the coorinates of vertices C and D.



51. If $(x_1,y_1,z_1),$ $(x_2,y_2,z_2),$ (x_3,y_3,z_3) and (x_4,y_4,z_4) be the consecutive vertices of a parallelogram, show that $x_1+x_3=x_2+x_4,$ $y_1+y_3=y_2+y_4$ and $z_1+z_3=z_2+z_4.$



52. Determine the coordinates of the point which is equiistant from the points (0,00), (a,0,0) and (0,b,0) and (0,0,c).



53. Find the distance of the point (2 , 4 , 3) from the x-axis and from the XOY plane .



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54. Find the equation to the locus of a point the sum of the squares of whose distances from the points (0, -4, 3) and (0, 4, -3) is equal to 60 unit.

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55. Prove that the four points (1,1,1), (-2,4, 1), (-1, 5, 5) and (2, 2, 5) are the vertices of a square.



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56. Prove that the points (2, 3, 5), (-4, 7, -7) , (- 2 , 1 , -10) and (4 , - 3 , 2) are the vertices of a rectangle.



57. Show that the points (0 ,0,0) , (- 2 , 0, 0) , (0 , 2 , 0) and (0 , 0 , 4) lie on a sphere whose centre is (- 1, 1, 2).



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58. Find the coordinates of the points of trisection of the line-segment joining the points (2,1,-3) and (5,-8,3) that is nearer to (2,1,-3).

59. Prove that the points (- 1 , - 3, 4) , (1 , - 6, 10) , (7 , - 4 , 7) and (5 , - 1 , 1) are the vertices of the rhombus .



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60. The coordinates of the points A, B, C and D are (1,1,1), (-2,4,1), (-1,5,5) and (2,2,5), prove that ABCD is a square.



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Short Answer Type Questions

1. Find the coordinates of the point which divides the join of (2,-3,5) and (3,-2,4) in the ratio 3:4



2. Find the coordinates of the point which divides the join of (2, -3, 5) and (3, -2, 4) in the ratio 3:4



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3. The straight line joining the points (3,4,3) and (2,1,5) intersects the plane 2x + 2y - 2z = 1 at P, find the coordinates of P.



4. Find the ratios in which the line-segment joining the points (4,3,2) and (1,2,-3) is divided by the coordinate planes.



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5. If a line is perpendicular to z-axis and makes an angle 40° with y-axis then find the angle it makes with x - axis .



6. The coordinates of the mid-points of the sides of a triangle are (3,-1,-1), (1,3,-4) and (0,1,-2), find the coordinates of the vertices.



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7. Find the ratio in which the line segment joining A (2,4,5) and B (3,5,4) divided by the yz-plane.



8. Let A (2 , - 4 , - 3) and B (- 4 , 2 , 3) be two given points if the points C and D trisect the line-segment \overline{AB} , then find the coordinates of C and D.



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9. Find the coordinates of the point in zx-plane which is equidistant from the points (-1,1,2) (1, -3, -8) and (-3, 3, -2).



10. Find the coordinates of the points on z-axis which are at a distance $\sqrt{29}$ unit from the point (2,-3,-1).



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11. A (1 , 3 , 0) , B (2 , 2 , 1) and C (5 , -1 , 4) are the vertices of the triangle ABC , if the bisector of $\angle BAC$ meets its side \overline{BC} at D , then find the coordinates of D .

12. IF the z-coordinates of a point C on the line
- segment joining the points A(2, 2, 1) and B (
5, 1, - 2) is -10, then find the x - coordinate of
C.



13. If A (1 , y , z) lies on the line through the points b (3 , 2 , - 1) and c (- 4 , 6 , 3) , then find the values of y and z .

14. Find the coordinates of the centriod of the triangle whose vertices are $(a_1,b_1,c_1),\,(a_2,b_2,c_2)$ and $(a_3,b_3,c_3).$



15. Using section formula, show that the points A (3, 2, -4), b (5, 4, -6) and C (9, 8,

-10) are collinear. Also find the ratio in which the point B divides the line-segment \overline{AC} .



- **16.** The line-segment joining the points A (1, 2,
- 3) and b (3, 4, -5) intersects the xy-plane at
- P , find the value of \overline{AP} : \overline{PB} .



17. Prove that the xy-plane divides the linesegment joining the points A(2, 1, 3) and B(1,

- 3, -4) in the ratio 3 : 4 at the point

$$\left(\frac{11}{7},\;-\frac{5}{7},0\right)$$



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18. If (- 4 , 7 , 5) , (2 , - 6 , - 3) and (8 , 2 , - 5) are the coordinates of the mid-points of the sides of a triangle, then find the coordinates of the centroid of the triangle.

19. Find the consine of the angle B of the triangle formed by joining the points A(6, 11, 2), B(1,-1,2) and C(1,2,6).



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20. If the point C(x , y , -14) lies on the line-segment \overline{AB} produced where the coordinates of A and B are (2 , - 3 , 4) and (3 , 1 , -2) respectively, then find te values of x and y.

21. Prove that the plane ax + by + cz + d = 0 divides the line-segment joining the points (x_1,y_1,z_1) and (x_2,y_2,z_2) in the ratio $-\frac{ax_1+by_1+cz_1+d}{ax_2+by_2+cz_2+d}$



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22. The coordinates of the centroid of the triangle ABC are (1,1,1), if the coordinates of

B and C are (1, 1, 2) and (-1, 7, -6) respectively , then find the coordiantes of the vertex A.



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23. The coordinates of the vertex A of the triangle ABC are (-3,-4,-2), if the coordinates of its centroid are (1, -2, 2), then find the coordinates of the mid - point of the side BC



24. Using section formula show tht the points A (9,8,-10), B (3,2,-4) and C (5,4,-6) are collinear.



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25. The coordinates of the centroid of the triangle formed by joining the points (x, -1, -2), (-2, y, 8) and (2, -4, z) are (1, 0, 30, find the values of x, y and z.



26. Prove that the plane ax - by + cz + d = 0 divides the line-segment joining the points

 $A(x_1,y_1,z_1)$ and $B(x_2,y_2,z_2)$ in the ratio

$$-rac{ax_1+by_1+cz_1+d}{ax_2=by_2+cz_2+d}.$$



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Sample Questions For Competitive Exams A M C Q

1. If OABC be a regular tetrahedron such that

$$OA^2+BC^2=OB^2+CA^2=OC^2+AB^2$$
then

- A. OA is perpendicular on BC
- B. OB is perpendicular on CA
- C. OC is perpendicular on AB
- D. AB is perpendicular on BC

Answer: A::B::C



2. The ratio in which the line segment joining the points (1, -2, 3) and (4, 2, -1) is divided by the XOY plane is _

A. 1:3

B. 3:1

C. line segment is bisected by the plane

D. 4:1

Answer: B::C



3. If $A(2,\beta,3), B(\alpha,-5,1)$ and C(-1,11,9) are coolinear then which of the following is/are ture?

A.
$$\alpha=3$$

B.
$$\beta=3$$

$$C. \alpha = -1$$

D.
$$\beta = -1$$

Answer: A::D



4. E is the mid point of side OB of triangle OAB

. D is a point on AB such that AD: DB = 2:1. If

OD and AE intersect at P, then -

A.
$$OP : PD = 3:2$$

B.
$$OP:PD = 2:5$$

C. P intersects OD internally

D. P intersects OD externally

Answer: A::C



5. P divides the line segment joining the points A(1,2,5) and B(6,7,-5) in ratio 2:3. If Q be the mid point of line segment AB then the coordinates of P and Q will be

A.
$$(3, 4, 9)$$

$$\mathsf{B.}\left(\frac{7}{2},\frac{9}{2},0\right)$$

$$\mathsf{C.}\left(\frac{7}{2},\frac{9}{2},1\right)$$

D.
$$(3, 4, 0)$$

Answer: A::B



Sample Questions For Competitive Exams B Integer Answer Type

1. The coordinates of the vertices of a regular tetrahedred are (3,2,3),(0,3,4),(6,1,4) and (6,3,2), the area (sq. units) of the tetrahedron is _



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2. $(-1,\lambda,-3)$ is the coordinate of centroid of the triangle formed by the points (3,2,-5),(-3,8,-5) and (-3,2,1). Then the value of λ is



3. The least distance of the point (2 soin t , 2 cos t , 3t) from the origin is _



4. If the projection of a triangle formed by the points A(-1,1,1), B(1,-1,-1) and C(1,1,-1) on the xy plane then the area of projected triangle on xy plane is _



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5. The z-coordinate of a point equidistant from the points (0,0,0), (2,0,0), (0,4,0) and (0,0,6) is



Sample Questions For Competitive Exams C **Matrix Match Type**

1. The point (3,7,5) lies on which octant?



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2. The point (-2,-6,7) lies on which octant?



Sample Questions For Competitive Exams D Comprehension Type

1. The point (2,3,4) lies on octant

A. OXYZ'

B. OXY'Z

C. OXYZ

D. OX'Y'Z

Answer: C



2. The point (-1,-4,-3) lies on octant

A. OXY'Z

B. OX'YZ

C. OX'Y'Z

D. OX'Y'Z'

Answer:



3. The point (2, -1,5) lies on octant

A. OXYZ'

B. OXYZ

C. OXY'Z

D. OX'YZ

Answer: C



4. The point (- 3, -4, -5) lies on octant

A. OXYZ'

B. OX'YZ'

C. OX'YZ

D. OX'Y'Z'

Answer: D

