

## MATHS

### BOOKS - CHHAYA PUBLICATION MATHS (BENGALI ENGLISH)

#### PROPERTIES OF TRIANGLE

##### Illustrative Examples

1. If the angles of a triangle are in the ratio  $1: 2: 3$  and the circumradius is 10 cm, find the lengths of its sides.



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2. In the triangle ABC, if  $a=5$ ,  $b=7$  and  $c=3$ , find the angle B and the circumradius R.





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3. If the radius ABC,  $C = \frac{\pi}{6}$ ,  $b = \sqrt{3}$  and  $a=1$ , find the other angles and the third side.



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4. (i) If  $a:b:c = 2:3:4$  and  $s=27$  inches, find the area of the triangle ABC.

- (ii) If in a triangle ABC,  $a=6$ ,  $b=3$  and  $\cos(A-B) = \frac{4}{5}$  then find its area.



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5. The triangle ABC is isosceles: If  $\angle A = 108^\circ$ , find the value of a:b.



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6. In the triangle ABC, if  $A = 60^\circ$ , show that,  $b + c = 2a \cos\left[\frac{B - C}{2}\right]$



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7. In any triangle ABC, prove that,  $c \sin\left(\frac{A - B}{2}\right) = (a - b)\cos\left(\frac{C}{2}\right)$



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8. In any triangle ABC, prove that,

$$(b^2 - c^2)\cot A + (c^2 - a^2)\cot B + (a^2 - b^2)\cot C = 0$$



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9. In any triangle ABC, prove that

$$\frac{a^2 \sin(B - C)}{\sin B + \sin C} + \frac{b^2 \sin(C - A)}{\sin C + \sin A} + \frac{c^2 \sin(A - B)}{\sin A + \sin B} = 0$$



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10. In any triangle ABC, prove that,

$$(b - c)\cot \frac{A}{2} + (c - a)\cot \frac{B}{2} + (a - b)\cot \frac{C}{2} = 0$$



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11. In any triangle ABC, show that,

$$(a + b - c) \left( \frac{\cot A}{2} + \frac{\cot B}{2} \right) = 2c \frac{\cot C}{2}$$

A. page no 460

B.

C.

D.

**Answer:**



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12. If the area of the triangle ABC be  $\Delta$ , show that,

$$b^2 \sin 2C + c^2 \sin 2B = 4 \Delta.$$

A. page no 460

B.

C.

D.

**Answer:**



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13. The sides of a triangle in cm are  $2a + 3$ ,  $a^2 + 3a + 3$  and  $a^2 + 2a$ , where  $a$  is a given positive quantity. Find the greatest angle of the triangle.



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**14.** If  $(a^2 + b^2)\sin(A - B) = (a^2 - b^2)\sin(A + B)$  then show that, the triangle is either isosceles or right angled.



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**15.** In any triangle ABC, prove that,

$$a^3 \cos(B - C) + b^3 \cos(C - A) + c^3 \cos(A - B) = 3abc.$$



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**16. (i)** If in a triangle ABC,  $a^4 + b^4 + c^4 - 2b^2c^2 - 2c^2a^2 = 0$ , then show that,  $C = 45^\circ$  or  $135^\circ$ .

**(ii)** In in a triangle ABC,

$$\sin^4 A + \sin^4 B + \sin^4 C = \sin^2 B \sin^2 C + 2 \sin^2 C \sin^2 A + 2 \sin^2 A \sin^2 B$$

, show that, one of the angles of the triangle is  $30^\circ$  or  $150^\circ$



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17. If  $C$  is a right angle in the triangle  $ABC$ , show that,  
 $\tan^{-1} \frac{a}{b+c} + \tan^{-1} \frac{b}{c+a} = \frac{\pi}{4}$ .



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18. If in any triangle  $ABC$ ,  $\cot A + \cot B + \cot C = \sqrt{3}$ , prove that, the triangle is equilateral.



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19. In triangle  $ABC$ ,  $A = 90^\circ$ ,  $B = 45^\circ$  and  $a = 5$ , then find  $b$ ?



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20. In any triangle  $ABC$ , if  $8R^2 = a^2 + b^2 + c^2$ , prove that, the triangle is right angled.



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**21.** If the sides of a triangle are in A.P. and the greater and the least angles are  $\theta$  and  $\phi$  respectively, then show that,

$$4(1 - \cos \theta)(1 - \cos \phi) = \cos \theta + \cos \phi$$



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**22.** (i) If the cosines of two of the angles of a triangle, which is not isosceles, are inversely proportional to the corresponding opposite sides, show that the triangle is right angled.

(ii) In a triangle ABC, If  $A=2B$  then show that,  $a^2 - b^2 = bc$ .



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**23.** In triangle ABC , $A = 60^\circ$ ,  $B = 45^\circ$  and  $a = 2\sqrt{3}$ , then find b?



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24. If the lengths of the sides  $\overrightarrow{BC}$ ,  $\overrightarrow{CA}$  and  $\overrightarrow{AB}$  of the triangle ABC be a:b:c respectively and the lengths of perpendicular from the circumcenter upon  $\overrightarrow{BC}$ ,  $\overrightarrow{CA}$  and  $\overrightarrow{AB}$  be x, y, z respectively, then prove that,

$$\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = \frac{abc}{4xyz}.$$



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25. The perpendicular from the vertices A, B and C of a triangle ABC on the opposite sides meet at O. If OA=x, OB=y and OC=z, prove that,

$$\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = \frac{abc}{xyz}.$$



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26. Two chords of a circle are of lengths a cm and b cm and they subtend angles  $\theta$  and  $3\theta$  respectively at the center of the circl. If the radius of the circle by r cm, show that,

$$r = a \sqrt{\frac{a}{3a - b}} \text{ cm.}$$



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27. In any triangle ABC, if  $\frac{\cos B + 2 \cos A}{\cos B + 2 \cos C} = \frac{\sin C}{\sin A}$  then prove that, the triangle is either isosceles or right angled.



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28. In any triangle ABC if  $\cos A + 2 \cos B + \cos C = 2$ , show that the sides of the triangle are in A.P.



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29. In any triangle ABC, prove that

$$\frac{\sin A}{\sin B + \sin C} + \frac{\sin B}{\sin C + \sin A} + \frac{\sin C}{\sin A + \sin B} \geq \frac{3}{2}.$$



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**30.** In any triangle ABC, If  $b^2 = a(c + a)$ ,  $c^2 = b(a + b)$ , then prove that,

$$\cos A \cos B \cos C = -\frac{1}{8}.$$



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**31.** If in a triangle ABC,  $\cos^2 A + \cos^2 B + \cos^2 C = 1$ , then show that the triangle is right angled.



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**32.** In the triangle ABC, If  $\operatorname{cosec}^2 A + \operatorname{cosec}^2 B + \operatorname{cosec}^2 C = 4$ , show that the triangle is equilateral.



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**Exercise Multiple Choice Questions**

1. In an triangle, ABC, if  $A = 60^\circ$ ,  $B = 45^\circ$  and  $a = 2\sqrt{3}$  units then, b=

A.  $2\sqrt{2}$  units

B.  $3\sqrt{2}$  units

C. 1 unit

D. none of these

**Answer: A**



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2. If the sides of triangle be 15 units , 12 units and 9 units then the area (in sq. units) of the triangle is-

A. 45

B. 54

C. 50

D. 40

**Answer: B**



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**3.** If  $\sin^2 B + \sin^2 C = \sin^2 A$ , then the triangle ABC is-

A. isosceles

B. right angled

C. equilateral

D. none of these

**Answer: B**



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**4.** If  $a = \sqrt{3}$ ,  $b = 2$  and  $c=1$ , then the value of angle A is

A.  $30^\circ$

B.  $45^\circ$

C.  $60^\circ$

D.  $90^\circ$

**Answer: C**



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5. In any triangle ABC, which of the following is false?

A.  $a = b \cos C - c \cos B$

B.  $\sin A + \sin B > \sin C$

C.  $b^2 = c^2 + a^2 - 2ca \cos B$

D. The formula  $a^2 = b^2 - 2bc \cos A$  can be deduced using the formula

of the form  $a = b \cos C + c \cos B$

**Answer: A**



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**6.** In triangle ABC, state which of the following is the value of  $(bc \cos A + ca \cos B)$ ?

- A.  $a^2$
- B.  $b^2$
- C.  $c^2$
- D.  $a^2 + b^2$

**Answer:** C



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**7.** In triangle ABC, If  $B = 90^\circ$ , state which of the following is true?

- A.  $(a - b)^2 = c^2 - ab$
- B.  $(b - c)^2 = a^2 - bc$
- C.  $(c - a)^2 = b^2 - ca$

$$\text{D. } (c - a)^2 = b^2 - 2ca$$

**Answer: D**



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**8.** In triangle ABC, If  $\cos B = \frac{a}{2c}$ , then the triangle is-

A. equilateral

B. isosceles

C. right angled

D. scalene.

**Answer: B**



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**9.** The circumradius of triangle ABC is 10 units: If  $c = 10\sqrt{3}$  units, state which of the following is the value of the angle C?

A.  $60^\circ$

B.  $120^\circ$

C.  $30^\circ$

D.  $90^\circ$

**Answer:** A



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**10.** In triangle ABC, if  $(a+b+c)(b+c-a) = 3bc$ , state which of the following is the value of the angle A?

A.  $30^\circ$

B.  $60^\circ$

C.  $90^\circ$

D.  $120^\circ$

**Answer: B**



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11. In triangle ABC, if  $a=3$ ,  $b=5$  and  $c = 120^\circ$ , state which of the following is the value of  $c$ ?

A. 7

B. 6

C. 6.5

D. 7.5

**Answer: A**



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**12.** If in a  $\triangle ABC$ ,  $\angle A = 45^\circ$ ,  $\angle B = 60^\circ$ ,  $\angle C = 75^\circ$ , then the ratio of its sides is-

A.  $2:\sqrt{6}:\sqrt{3}+1$

B.  $\sqrt{6}:2:\sqrt{3}+1$

C.  $\sqrt{6}:\sqrt{3}+1:2$

D. none of these

**Answer:** A



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**13.** In a triangle,  $a=2b$  and  $A=3B$ . Mention which of the following is true?

A. The triangle is equilateral

B. The triangle is isosceles

C. The triangle is right angled

D. The existence of such a triangle is not possible.

**Answer: C**



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### Very Short Answer Type Questions

1. In a triangle the sides are in the ratio  $\sqrt{2}: 2: (\sqrt{3} + 1)$ . Find the possible values of the angles.



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2. If the angles of a triangle are in the ratio 2: 3: 7 and the circumradius is 10 cm, find the lengths of its sides.



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3. In  $\triangle ABC$   $\angle B = 60^\circ$ ,  $c = 2\sqrt{3}$ ,  $b = 3\sqrt{2}$  then find  $\angle A$ .



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4. In a triangle ABC the angle  $A = 60^\circ$  and  $b:c = (\sqrt{3} + 1) : 2$ . Find the other two angles B and C.



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5. If the two sides and the included angle are respectively  $a = \sqrt{3} + 1$ ,  $b = 2$ ,  $\angle C = 60^\circ$ , find the other angles and the third side.



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6. Find the angles of the triangle whose sides are  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$ ,  $\frac{\sqrt{3} - 1}{2\sqrt{2}}$  and  $\frac{\sqrt{3}}{2}$ .



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**7.** Find the area of the triangle if

(i)  $a = 13, b = 14, c = 15$

(ii)  $a:b:c = 3:4:5$  and  $s=48 \text{ cm}$

(iii)  $a = \frac{x}{y} + \frac{y}{z}, b = \frac{y}{z} + \frac{z}{x}$  and  $c = \frac{z}{x} + \frac{x}{y}$



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**8.** If in a triangle ABC,  $a=3, b=5$  and  $c=7$ , show that the triangle is obtuse angled.



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**9.** If  $\frac{\sin A}{3} = \frac{\sin B}{3} = \frac{\sin C}{4}$ , then prove that,  $\cos C = \frac{1}{9}$ .



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10. If in a triangle ABC,  $\frac{a - b + c}{2} = a \frac{b}{b + c - a}$  then prove that  $\angle C = 90^\circ$ .



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11. If  $a=3$ ,  $b=4$ ,  $c=5$ , find the value of  $\tan\left(\frac{B}{2}\right)$ .



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12. If  $a=2b$  and  $A=3B$ , find the angles of the triangle ABC.



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13. (i)  $(b + c)\cos A + (c + a)\cos B + (a + b)\cos C = a + b + c$



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$$14. \text{(ii)} (b - c)\sin A + (c - a)\sin B + (a - b)\sin C = 0$$



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$$15. \text{(iii)} a(b \cos C - c \cos B) = b^2 - c^2$$



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$$16. \quad \text{(iv)}$$

$$a^2(\cos^2 B - \cos^2 C) + b^2(\cos^2 C - \cos^2 A) + c^2(\cos^2 A - \cos^2 B) = 0$$



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$$17. \text{(v)} 2(bc \cos A + ca \cos B + ab \cos C) = a^2 + b^2 + c^2$$



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$$18. \text{(vi)} (a^2 - b^2 - c^2) \tan A + (a^2 - b^2 + c^2) \tan B = 0$$



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$$19. \text{(vii)} (b^2 + c^2 - a^2) \tan A = (a^2 - b^2 + c^2) \tan B$$



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$$20. \quad \text{(viii)}$$

$$(b + c - a) \tan\left(\frac{A}{2}\right) = (c + a - b) \tan\left(\frac{B}{2}\right) = (a + b - c) \frac{\tan C}{2}$$



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### Short Answer Type Questions

1. In triangle ABC,

$$\text{(i)} a \sin\left(\frac{A}{2} + B\right) = (b + c) \frac{\sin A}{2}$$



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$$2. \text{ (ii)} (b - c) \cos\left(\frac{A}{2}\right) = a \sin\left(\frac{B - C}{2}\right)$$



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$$3. \text{ (iii)} a \cos A + b \cos B + c \cos C = 4R \sin A \sin B \sin C$$



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$$4. \text{ (iv)} a \sin(B - C) + b \sin(C - A) + c \sin(A - B) = 0$$



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$$5. \text{ (v)} \frac{b^2 - c^2}{\cos B + \cos C} + \frac{c^2 - a^2}{\cos C + \cos A} + \frac{a^2 - b^2}{\cos A + \cos B} = 0$$



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$$6. \text{(vi)} a \cos B \cos C + b \cos C \cos A + c \cos A \cos B = \frac{abc}{4R^2}$$



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$$7. \text{(vii)} (b^2 - c^2) \cos 2A + (c^2 - a^2) \cos 2B + (a^2 - b^2) \cos 2C = 0$$



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$$8. \text{(viii)} (b^2 - c^2) \cos 2A + (c^2 - a^2) \cos 2B + (a^2 - b^2) \cos 2C = 0$$



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$$9. \text{(ix)} \frac{a^2 \sin(B - C)}{\sin A} + \frac{b^2 \sin(C - A)}{\sin B} + \frac{c^2 \sin(A - B)}{\sin C} = 0$$



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$$10. \text{(x)} \frac{a \sin(B - C)}{b^2 - c^2} = \frac{b \sin(C - A)}{c^2 - a^2} = \frac{c \sin(A - B)}{a^2 - b^2}$$



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$$11. \text{(xi)} \quad a^2 \sin 2B + b^2 \sin 2A = 4\Delta$$



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$$12. \text{(xii)} \quad (b + c - a) \left( \cot' \frac{B}{2} + \cot' \frac{C}{2} \right) = 2a \cot' \frac{A}{2}$$



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$$13. \text{(xiii)} \quad a^3 \sin(B - C) + b^3 \sin(C - A) + c^3 \sin(A - B) = 0$$



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$$14. \text{(xiv)} \quad a \cos A + b \cos B + c \cos C = \frac{abc}{2R^2}$$



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$$15. \text{ (xv)} a \cos(B - C) + b \cos(C - A) + c \cos(A - B) = \frac{4(\Delta)}{R}$$



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$$16. \text{ If } C = 60^\circ, \text{ show that, } 2a - b = 2c \cos B$$



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$$17. \text{ If } b + c = 2a, \text{ show that, } 2 \sin' \frac{A}{2}' = \sin\left(B + \frac{A}{2}\right)$$



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$$18. \text{ If } a \cos^2, \frac{C}{2}, + c \cos^2, \frac{A}{2}, = \frac{3b}{2} \text{ then show that the sides of the triangle are in A.P.}$$



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19. In any triangle ABC, if  $\frac{1}{a+c} + \frac{1}{b+c} = \frac{3}{a+b+c}$  then show that,  
 $C = 60^\circ$ .



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20. If  $2 \cos A = \frac{\sin B}{\sin C}$  then show that the triangle is isosceles.



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21. In triangle ABC , $a = 2$ ,  $b = \sqrt{3}$  and  $A = 90^\circ$ , then find B?



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22. In any triangle ABC, if  $\cos A \cos B + \sin A \sin B \sin C = 1$  then prove that  
the triangle is an isosceles right angled.



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**23.** In any triangle ABC, prove that

$$\cos A + \cos B + \cos C \leq \frac{3}{2}$$



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**24.** In any triangle ABC, show that  $\frac{a \sin C}{b - a \cos C} = \tan A$ .



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**25.** If  $B = 30^\circ$ ,  $b = 3\sqrt{2} - \sqrt{6}$ ,  $c = 6 - 2\sqrt{3}$ , solve the triangle.



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**26.** In any triangle ABC, if  $\cos A + \cos B + \cos C = \frac{3}{2}$ , then show that the triangle is equilateral.



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27. If  $A, B, C$  be the angles of a triangle then prove that

$$(\sin A + \sin B)(\sin B + \sin C)(\sin C + \sin A) > \sin A \sin B \sin C.$$



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28. In any triangle ABC, if  $\sin^2 A + \sin^2 B + \sin^2 C = \frac{9}{4}$ , show that the triangle is equilateral.



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### Long Answer Type Questions

1. The sides of a triangle ABC are  $(x^2 + x + 1)$ ,  $(2x + 1)$  and  $(x^2 - 1)$ .

Find the greatest angle of the triangle.



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2. In a triangle ABC, if  $(a^2 + b^2)\sin(A - B) = (a^2 - b^2)\sin(A + B)$  (where  $a \neq b$ ), prove that the triangle is right angled.



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3. If  $a^4 + b^4 + c^4 + a^2b^2 = 2c^2(a^2 + b^2)$  then show that,  $C = 60^\circ$  or  $120^\circ$



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4. A wire of length 2 metre is cut into three pieces so as to form the sides of a triangle. If the two angles of the triangle be  $35^\circ$  and  $85^\circ$ , find an metre the lengths of the sides. Given  $\sin 35^\circ = 0.5736$ ,  $\sin 60^\circ = 0.8660$  and  $\sin 85^\circ = 0.9962$ .



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5. The angles A, B, C of  $\triangle ABC$  are in A.P. and  $b:c = \sqrt{3}:\sqrt{2}$ . Find A.



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6. If in  $\triangle ABC$ ,  $\tan^{-1}\left(\frac{a}{b+c}\right) + \tan^{-1}\left(\frac{c}{a+b}\right) = \frac{\pi}{4}$ , then prove that, the triangle is right angled.



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7. If  $\frac{\sin A}{\sin C} = \frac{\sin(A - B)}{\sin(B - C)}$ , then show that,  $a^2, b^2, c^2$  are in A.P.



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8. In triangle ABC , $a = 3$ ,  $b = 3\sqrt{3}$  and  $A = 30^\circ$ , then find B?



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9. In any triangle ABC, if  $\sin A : \sin B : \sin C = 4:5:6$ , then prove that,  $\cos A : \cos B : \cos C = 12:9:2$

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10. In any triangle ABC, if  $\tan\left(\frac{A}{2}\right), \tan\left(\frac{B}{2}\right), \tan\left(\frac{C}{2}\right)$  are in A.P., prove that,  $\cos A, \cos B, \cos C$  are also in A.P.

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11. If h be the length of the perpendicular drawn from A on BC in the triangle ABC, show that,  $h = \frac{a \sin B \sin C}{\sin(B + C)}$ .

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12. If D is the mid-point of the side BC of a triangle ABC and  $\angle BAD = \theta, \angle CAD = \phi$ , then show that  $\cot \theta - \cot \phi = \cot B - \cot C$



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13. The sides of a triangle are 4,5,6 cm. Show that its smallest angle is half of its greatest angle.



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14. ABC is a triangle and D is the middle point of BC. If AD is perpendicular to AC, prove that,  $\cos A \cos C = \left( 2 \frac{c^2 - a^2}{3ca} \right)$



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15. In any triangle ABC, if  $\frac{\cos A + 2 \cos C}{\cos A + 2 \cos B} = \frac{\sin B}{\sin C}$  then prove that, the triangle is either isosceles or right angled.



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16. If  $x, y, z$  are altitudes of the triangle  $ABC$ , through the vertices  $A, B, C$  respectively, then prove that,  $\frac{\cos A}{x} + \frac{\cos B}{y} + \frac{\cos C}{z} = \frac{1}{R}$  where  $R$  is the circumradius of the triangle.



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17. In any triangle  $PQR$ ,  $\angle R = \frac{\pi}{2}$ . If  $\tan' \frac{P}{2}$  and  $\tan' \frac{Q}{2}$  are the roots of the equation  $ax^2 + bx + c = 0 (a \neq 0)$ , then show that,  $a+b=c$ .



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18. In triangle  $ABC$ , if  $3\left(\tan' \frac{A}{2}, + \tan' \frac{C}{2}\right) = 2 \cot' \frac{B}{2}$  then show that, its sides  $a, b, c$  are in A.P.



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**19.** In the triangle ABC if

$$\frac{2 \cos A}{a} + \frac{\cos B}{b} + \frac{2 \cos C}{c} = \frac{a}{bc} + \frac{b}{ca} \text{ find the angle A.}$$



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**20.** If in the triangle ABC,  $C = \frac{\pi}{2}$  and  $\tan' \frac{A}{2}'$ ,  $\tan' \frac{B}{2}'$  are two roots of the equation  $px^2 + qx + r = 0 (p \neq 0)$  then show that  $p+q=r$ .



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**21.** In the triangle ABC, if  $\frac{b+c}{11} = \frac{c+a}{12} = \frac{a+b}{13}$ , prove that  $\frac{\cos A}{7} = \frac{\cos B}{19} = \frac{\cos C}{25}$ .



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**22.** In the triangle ABC, two sides b,c and angle B are given, side a has two values  $a_1$  and  $a_2$ . Show that  $|(a_1 - a_2)| = 2\sqrt{b^2 - c^2 \sin^2 B}$ .



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## Sample Questions For Competitive Exams

1. In triangle ABC if  $a^4 + b^4 + c^4 = 2a^2b^2 + 2b^2c^2$  then the values of B will be-

A.  $45^\circ$

B.  $135^\circ$

C.  $120^\circ$

D.  $60^\circ$

**Answer: A::B**



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2. The sides of a  $\triangle ABC$  satisfy the equation  $2a^2 + 4b^2 + c^2 = 4ab + 2ac$ , then-

A. the triangle is isoceles

B. the triangle is obtuse

C.  $B = \frac{\cos^{-1} 7}{8}$

D.  $A = \frac{\cos^{-1} 1}{4}$

**Answer: A::C::D**



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3. If the sides of right angled triangle are in G.P then the cosines of the acute angle of the triangle are-

A.  $\frac{\sqrt{5} - 1}{2}$

B.  $\frac{\sqrt{5} + 1}{2}$

C.  $\frac{\sqrt{\sqrt{5} - 1}}{2}$

D.  $\frac{-(\sqrt{5}) - 1}{2}$

**Answer: A::C::D**



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4. In  $\triangle ABC$ , if  $\cos \frac{A}{2} = \sqrt{\frac{b+c}{2c}}$ , then-

- A. Area of triangle is  $\frac{1}{2}ab$
- B. Circumradius is equal to  $\frac{1}{2}c$
- C. Area of triangle is  $\frac{1}{2}bc$
- D. Circumradius is equal to  $\frac{1}{2}a$

**Answer: A::B**



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5.

In

a

triangle

$$\sin^4 A + \sin^4 B + \sin^4 C = \sin^2 B \sin^2 C + 2 \sin^2 C \sin^2 A + 2 \sin^2 A \sin^2 B$$

, then its angle A is equal to-

- A.  $30^\circ$

B.  $120^\circ$

C.  $150^\circ$

D.  $60^\circ$

**Answer: A::C**



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**Integer Answer Type**

1. ABC is a right angled triangle, then the value of  $\sin^2 A + \sin^2 B + \sin^2 C$  will be-



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2. In  $\triangle ABC$ , if  $3a = b+c$  then the value of  $\cot' \frac{B}{2} \cot' \frac{C}{2}$  will be-



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3. A triangle ABC is inscribed in a circle. If half the sum of the square of its three sides is equal to twice the square of the diameter of the circle, then the value of  $\sin^2 A + \sin^2 B + \sin^2 C$  will be-



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4. In  $\triangle ABC$ ,  $\angle A = 60^\circ$ ,  $b = \sqrt{3} + 1$  and  $c = \sqrt{3} - 1$  then the value of  $\tan\left(\frac{B - C}{2}\right)$  is-



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5. In  $\triangle ABC$ ,  $\angle A = 60^\circ$ , then the value of  $\left(1 + \frac{a}{c} + \frac{b}{c}\right)\left(1 + \frac{c}{b} - \frac{a}{b}\right)$  will be-



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Comprehension Type

**1.** ABC is a triangle where  $a=6$ ,  $b=3$  and  $\cos(A - B) = \frac{4}{5}$

(i) Area of the triangle ABC (in sq. units) is-

A. 9

B. 12

C. 11

D. 10

**Answer:** A



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**2.** ABC is a triangle where  $a=6$ ,  $b=3$  and  $\cos(A - B) = \frac{4}{5}$

Value of angle C is-

A.  $\frac{3\pi}{4}$

B.  $\frac{\pi}{4}$

C.  $\frac{\pi}{2}$

D.  $\frac{\pi}{3}$

**Answer: C**



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3. ABC is a triangle where  $a=6$ ,  $b=3$  and  $\cos(A - B) = \frac{4}{5}$

A.  $\frac{1}{2\sqrt{5}}$

B.  $\frac{1}{\sqrt{3}}$

C.  $\frac{1}{\sqrt{5}}$

D.  $\frac{2}{\sqrt{5}}$

**Answer: D**



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**4.**  $P_1, P_2, P_3$  are altitudes of a triangle ABC from the vertices A, B, C and

$\Delta$  is the area of the triangle,

The value of  $\frac{1}{P_1^2} + \frac{1}{P_2^2} + \frac{1}{P_3^2}$  is equal to-

A.  $\frac{a+b+c}{\Delta}$

B.  $\frac{a^2+b^2+c^2}{4\Delta^2}$

C.  $\frac{a^2+b^2+c^2}{\Delta^2}$

D. none of these

**Answer:** B



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**5.**  $P_1, P_2, P_3$  are altitudes of a triangle ABC from the vertices A, B, C and

$\Delta$  is the area of the triangle,

The value of  $P_1^{-1} + P_2^{-1} + P_3^{-1}$  is equal to-

A.  $\frac{2S}{\Delta}$

B.  $\frac{2}{r}$

C.  $\frac{8R}{abc}$

D. none of these

**Answer:** D



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**6.**  $P_1, P_2, P_3$  are altitudes of a triangle ABC from the vertices A, B, C and  $\Delta$  is the area of the triangle,

The value of  $\frac{\cos A}{P_1} + \frac{\cos B}{P_2} + \frac{\cos C}{P_3}$  is equal to-

A.  $\frac{1}{R}$

B.  $\frac{a^2 + b^2 + c^2}{2R}$

C.  $\frac{\Delta}{2R}$

D. none of these

**Answer:** A



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## Assertion Reason Type

1. Statement-I: In  $\triangle ABC$ ,  $\sin A + \sin B > \sin C$

Statement-II: In  $\triangle ABC$ , sum of two sides is always greater than the third side.

- A. Statement-I is true, statement-II is true and statement-II is a correct explanation for statement- I.
- B. Statement-I is true, Statement-II is true but Statement-II is not a correct explanation of Statement-I.
- C. Statement-I is true, Statement-II is false.
- D. Statement-I is false, Statement-II is true.

**Answer: A**



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2. Prove that  $(b - c)\sin A + (c - a)\sin B + (a - b)\sin C = 0$



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