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## MATHS

# BOOKS - CHHAYA PUBLICATION MATHS (BENGALI ENGLISH) 

## SET THEORY

## Examples

1. Write down the following statements in set-theoretic notations:

3 is an element of a set A

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2. Write down the following statements in set-theoretic notations:

4 does not belong to a set B
3. Write down the following statements in set-theoretic notations:
$C$ is a subset of $D$

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4. Write down the following statements in set-theoretic notations:
$P$ and $Q$ are disjoint sets.

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5. Represent the following sets in tabular (or Roster) form :
set of factors of 30
6. Represent the following sets in tabular (or Roster) form : $X=\{a: a \in \mathbb{N}$ and $a$ is a perfect square and $2<a \leq 49\}$

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7. Represent the following sets in tabular (or Roster) form :
$Y=\{x: x$ is an even natural number greater than 20\}

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8. Represent the following sets in tabular (or Roster) form :
$\mathbb{Z}=\left\{x: x=\frac{n+2}{n^{2}-2}\right.$ where $2 \leq n \leq 5$ and $\left.n \in \mathbb{N}\right\}$.

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9. Write the following sets in set-builder form:
set of letters in the word 'Statistics'
10. Write the following sets in set-builder form:
$A=\{3,6,9,12,15, \ldots\}$

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11. Write the following sets in set-builder form:
set of integers either equal or greater than 3 but less than 25 .

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12. Which of the following sets is the null set $\phi$ ? Briefly say why?
$A=\{x: x$ is $>1$ and $x$ is $<1\}$

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13. Which of the following sets is the null set $\phi$ ? Briefly say why?
$B=\{x: x+3=3\}$

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14. Which of the following sets is the null set $\phi$ ? Briefly say why?
$C=\{\phi\}$

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15. Show the relationships among the following three sets in respect of subsets and supersets:
$\mathbb{Z}^{+}=\{\mathrm{x}: \mathrm{x}$ is a positive integer $\}$
$\mathbb{Z}=\{x: x$ is an integer $\}$
$\mathbb{R}=\{\mathrm{x}: \mathrm{x}$ is a real number $\}$

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16. State with reasons whether the sets defined in each of the following cases are equal :

$$
X=\phi, Y=\{\phi\}
$$

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17. State with reasons whether the sets defined in each of the following cases are equal :
$A=\left\{x: x^{2}-3 x+2=0\right\}, \mathrm{B}=\{\mathrm{x}: \mathrm{x}$ is a digit in the number 212$\}$

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18. State with reasons whether the sets defined in each of the following cases are equal :
$P=\{x: x$ is an integer and $-2 \leq x \leq 2\}, Q=\left\{x: x\left(x^{2}-1\right)\left(x^{2}-4\right)\right.$

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19. State whether each of the following sets is finite or infinite :
$A=\{x: x$ is an odd integer greater than 100 $\}$

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20. State whether each of the following sets is finite or infinite :
$\mathrm{B}=\{\mathrm{x}: \mathrm{x}$ is real and $-1 \leq x<1\}$

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21. State whether each of the following sets is finite or infinite :
$C=\{x: x$ is an odd negative integer greater than -140$\}$.

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22. Given, $A=\{2,3,4\}$, determine all the eight subsets of $A$.
23. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$\{x\} \in A$

## - Watch Video Solution

24. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$x \in A$

## Watch Video Solution

25. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$\{x\} \subset A$
26. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$y \subseteq A$

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27. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$\phi \in A$

## - Watch Video Solution

28. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$\phi \subseteq A$

## - Watch Video Solution

29. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:

$$
\{x, y, z\} \subseteq A
$$

## - Watch Video Solution

30. Given $A=\{x, y, z\}$, state with reasons which of the following statements are correct:
$\{z\} \in P(A)$

## - Watch Video Solution

31. Given $A=\{1,2,3\}, B=\{2,4\}, C=\{2,3,5\}$.

Find $A \cap B, A \cap C$ and $(A \cap B) \cup(A \cap C)$
32. Given $A=\{1,2,3\}, B=\{2,4\}, C=\{2,3,5\}$.
$B \cup C$ and $A \cap(B \cup C)$.
Hence, verify the result $A \cap(B \cup C)=(A \cap B) \cup(A \cap C)$.

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33. Let the sets A and B be given by, $A=\{1,2,3,4\}, B=\{2,4,6,8,10\}$ and the universal set $S=\{1,2,3,4,5,6,7,8,9,10\}$. Find $(A \cup B)^{\prime}$ and $(A \cap B)^{\prime}$

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34. Given $A=\{1,2,3,4\}, B=\{3,4,5\}$ and $C=\{1,4,5\}$,
verify the following statement :
$A-(B \cup C)=(A-B) \cap(A-C)$.

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35. If $S=\{a, b, c, d, e, f\}$ be the universal set and $A, B, C$ are three subsets of $S$, where $A=\{a, c, d, f\}, B \cap C=\{a, b, f\}, \quad$ find $(A \cup B) \cap(A \cup C)$ and $B^{\prime} \cup C^{\prime}$.

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36. For any two sets $A$ and $B$, if $P(A)=P(B)$, then show that $A=B$, here $P(A)$ is the power set of A .

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37. For any two sets $A$ and $B$, prove that
$P(A) \cup P(B) \subseteq P(A \cup B)$

## - Watch Video Solution

38. For any two sets $A$ and $B$, prove that
$P(A \cap B)=P(A) \cap P(B)$
where $P(A)$ is the power set of $A$.

## - Watch Video Solution

39. If $A=\{x: 1 \leq x \leq 2\}$ and $B=\{x: 0<x \leq 4\}$, find $A \cup B$

## - Watch Video Solution

40. If $A=\{x: 1 \leq x \leq 2\}$ and $B=\{x: 0<x \leq 4\}$, find $A \cap B$
41. If $A=\{x: 1 \leq x \leq 2\}$ and $B=\{x: 0<x \leq 4\}$, find $A-B$ and
42. If $A=\{x: 1 \leq x \leq 2\}$ and $B=\{x: 0<x \leq 4\}$, find
$A \cup B-(A \cap B)$

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43. List the sets $A, B$ and $C$, given that,

$$
A \cup B=\{p, q, r, s\}, A \cup C=\{q, r, s, t\}, A \cap B=\{q, r\}, A \cap C=\{q, s\}
$$

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44. Let $A=\{1,2,3,4,5,6,7,8,9\}, B=\{2,4,6,8\}, C=\{1,3,5,7,9\}, D=\{3,4,5\}$ and $E=\{3,5\}$ which set can equal X , if we are given the following information ? $X$ and $B$ are disjoint

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45. Let $A=\{1,2,3,4,5,6,7,8,9\}, B=\{2,4,6,8\}, C=\{1,3,5,7,9\}, D=\{3,4,5\}$ and $E=\{3,5\}$ which set can equal $X$, if we are given the following information ? $X \subset A$ but $X \not \subset C$

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46. Let $A=\{1,2,3,4,5,6,7,8,9\}, B=\{2,4,6,8\}, C=\{1,3,5,7,9\}, D=\{3,4,5\}$ and $E=\{3,5\}$
which set can equal $X$, if we are given the following information ?
$X \subset D$ but $X \varnothing B$

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47. Let $A=\{1,2,3,4,5,6,7,8,9\}, B=\{2,4,6,8\}, C=\{1,3,5,7,9\}, D=\{3,4,5\}$ and $E=\{3,5\}$
which set can equal X , if we are given the following information ?
$X \subset C$ but $X \subset A$

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48. For any three sets $A, B$ and $C$, prove that,

$$
A \cap(B-C)=(A \cap B)-(A \cap C)
$$

## - Watch Video Solution

49. For any three sets $A, B$ and $C$, prove that,
$A-(B \cup C)=(A-B) \cap(A-C)$

## - Watch Video Solution

50. For any three sets $A, B$ and $C$, prove that,
$A-(B \cap C)=(A-B) \cup(A-C)$.

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51. $A=\{x:: x \in \mathbb{N}\}, B=\{x: x=2 n, n \in \mathbb{N}\}$ and $\mathbb{D}=\{\mathrm{x}: \mathrm{x}$ is a prime natural number\}.Find $A \cap B$.
52. If $B \subseteq A$, then prove that, $B-A=\phi$.

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53. Applying the laws of algebra of sets, prove that, $A-B=B^{c}-A^{c}$

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54. Applying the laws of algebra of sets, prove that,
$(A \cup B) \cap\left(A \cup B^{c}\right)=A$

## - Watch Video Solution

55. Applying the laws of algebra of sets, prove that,
$(A \cup B) \cap A=A$
56. Applying the laws of algebra of sets, prove that,
$A \cap(B-A)=\phi$

## - Watch Video Solution

57. Applying set algebra, show that,
$(A \cup B)-C=(A-C) \cup(B-C)$

- Watch Video Solution

58. Applying set algebra, show that,
$(A \cap B)-C=(A-C) \cap(B-C)$

- Watch Video Solution

59. Applying set algebra, show that,

$$
A-(B \cup C)=(A-B) \cap(A-C)
$$

## - Watch Video Solution

60. Applying set operations find the H.C.F. of the three numbers 15,40 and 105.

## - Watch Video Solution

61. Using set operations find the L.C.M. of the three numbers 12,15 and 20.

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62. Let $\mathbb{N}$ be the set of natural numbers and $a \in \mathbb{N}$. If $a \mathbb{N}=\{a x: x \in \mathbb{N}\}$ and $p \mathbb{N} \cap q \mathbb{N}=r \mathbb{N}$, where $p, q, r \in \mathbb{N}$, then show that $r$ is the LCM of $p$ and $q$.
63. Applying set operations, prove that, $2+3=5$.

## - Watch Video Solution

64. In an examination, $45 \%$ of the candidates have passed in English, $40 \%$ have passed in Bengali, while $30 \%$ have passed in both the subjects. Find the total number of candidates if 90 of them have failed in both the subjects.

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65. It is known that in a group of people, each of which speaks at least one of the languages English, Hindi and Bengali, 31 speak English, 36 speak Hindi and 27 speak Bengali. 10 speak both English and Hindi, 9 both English and Bengali and 11 both Hindi and Bengali. Using a Venn diagram
or otherwise, prove that the group contains at least 64 people and not more than 73 people.

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66. In a survey concerning the smoking habits of consumers it was found that $50 \%$ smoke cigarette A, $45 \%$ smoke B, $40 \%$ smoke C, $25 \%$ smoke A and $\mathrm{B}, 10 \%$ smoke B and $\mathrm{C}, 16 \%$ smoke C and $\mathrm{A}, 8 \%$ smoke all the three brands. What percentage do not smoke ?

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67. A factor inspector examined the defects in hardness, finishing and dimensions of an item. After examining 100 items he gave the following report:

All three defects 5, defect in hardness and finishing 10, defect in dimensions and finishing 8, defect in dimensions and hardness 20. Defect in finishing 30, in hardness 23 and in dimensions 50 . The inspector was fined, why?
68. Two finite sets have m and n elements. The number of elements in the power set of first set is 48 more than the total number of elements in the power set of the second set. Find the values of $m$ and $n$.

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## Multiple Choice Questions

1. The number of subsets in a set consisting of four distinct elements is $\qquad$
A. 4
B. 8
C. 16
D. 64

## Answer: C

## D Watch Video Solution

2. The number of proper subsets in a set consisting of five distinct elements is $\qquad$
A. 5
B. 10
C. 32
D. 31

## Answer: D

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3. If $x \in A \Rightarrow x \in B$ then
A. $A=B$
B. $A \subset B$
C. $A \subseteq B$
D. $B \subseteq A$

## Answer: C

## D Watch Video Solution

4. If $A \subseteq B$ and $B \subseteq A$ then $\qquad$
A. $A=\phi$
B. $A \cap B=\phi$
C. $A=B$
D. none of these

## Answer: C

5. For two sets if $A \cup B=A \cap B$ then $\qquad$
A. $A \subseteq B$
B. $B \subseteq A$
C. $A=B$
D. none of these

## Answer: C

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6. $A-B=\phi$ if
A. $A \neq B$
B. $A \subset B$
C. $B \subset A$
D. $A \cap B=\phi$

Answer: B

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7. If $A \cap B=B$ then $\qquad$
A. $A \subseteq B$
B. $B \subseteq A$
C. $A=B$
D. $A=\phi$

## Answer: B

## - Watch Video Solution

8. If A and B are two disjoint sets then $n(A \cup B)=$
A. $n(A)+n(B)$
B. $n(A)-n(B)$
C. 0
D. none of these

## Answer: A

## - Watch Video Solution

9. For any two set A and $\mathrm{B}, n(A)+n(B)-n(A \cap B)=$
A. $n(A \cup B)$
B. $n(A)-n(B)$
C. $\phi$
D. none of these

## Answer: A

10. The dual of $A \cup U=U$ is $\qquad$
A. $A \cup U=U$
B. $A \cup \phi=\phi$
C. $A \cup \phi=A$
D. $A \cap \phi=\phi$

## Answer: D

## - Watch Video Solution

11. The dual of $A \cup(B \cap C)=(A \cup B) \cap(A \cup C)$ is
A. $(A \cap B) \cup(A \cap C)$
B. $(A \cup B) \cup(A \cup C)$
C. $(A \cap B) \cap(A \cap C)$
D. $(A \cup B) \cap(A \cup C)$

## Answer: A

## - Watch Video Solution

12. State which of the following statement is true?
A. Subset of an infinite set is an infinite set.
B. The set of even integers greater than 889 is an infinite set.
C. The set of odd negative integers greater than (-150) is an infinite set.
D. $A=\{x: x$ is real and $0<x \leq 1\}$ is a singleton set.

## Answer: B

13. State which of the following statement is not true?
A. If $a \in A$ and $a \in B$ then $A \subseteq B$.
B. If $A \subseteq B$ and $B \subseteq C$ then $A \subseteq C$.
C. If $A \subseteq B$ and $B \subseteq A, \quad$ then $A=B$.
D. For any set A, if $A \cup \phi=\phi$ ( $\phi$ being the null set) then $A=\phi$.

## Answer: A

## - Watch Video Solution

14. State which of the following is the set of factors of the number 12
A. $\{2,3,4,6\}$
B. $\{2,3,4,6,12\}$
C. $\{2,3,4,8,6\}$
D. $\{1,2,3,4,6,12\}$

## - Watch Video Solution

15. State which of the following is a null set?
A. $\{0\}$
B. $\{\phi\}$
C. $\{x: x$ is an integer and $1<x<2\}$
D. $\{x: x$ is a real number and $1<x<2\}$

## Answer: C

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16. If $B$ be power set of $A$, state which of the following is true?
A. $A \supset B$
B. $B \supset A$
C. $A \in B$
D. $A=B$

## Answer: C

## - Watch Video Solution

17. If $x \in A \cup B$, state which of the following is true?
A. $x \in A$
B. $x \in B$
C. $x \in A \vee x \in B$
D. $x \in A \wedge x \in B$

## Answer: C

18. If $x \in A \cap B$, state which of the following is true?
A. $x \in A \wedge x \in B$
B. $x \in B$
C. $x \in A \vee x \in B$
D. $x \notin A$

## Answer: A

## - Watch Video Solution

19. If $A=\{2,4,6,8\}$, state which of the following is true?
A. $\{2,4\} \in A$
B. $\{2,4\} \subseteq A$
C. $\{2,4\} \subset A$
D. $\{2,4\} \in A^{c}$

## - Watch Video Solution

20. State which of the following statements is true?
A. $\{a\} \in\{a, b, c\}$
B. $a \notin\{a, b, c\}$
C. $a \subset\{a, b, c\}$
D. $\{a\} \subset\{a, b, c\}$

## Answer: D

## Watch Video Solution

21. State which two of the following four sets are equal?
A. $A=\{0\}$
B. $B=\{\phi\}$
C. $C=\{x: x$ is a perfect square and $2 \leq x \leq 6\}$
D. $D=\{x: x$ is an integer and $-1<x<1\}$

## Answer: A and D

## - Watch Video Solution

22. Some well-defined sets are given below. Identify the null set:
A. $A=\{x: x$ is the cube of an integer and $2 \leq x \leq 7\}$
B. $B=\{0\}$
C. $C=\{\phi\}$
D. $D=\{x: \quad \mathrm{x}$ is an integer and $2<x \leq 3\}$

## Answer: A

23. State which of the following sets is an infinite set?
A. $A=\{x: x$ is an integer and $-1 \leq x<1\}$
B. $B=$ set of negative even integers greater than (-100)
C. C=set of positive integers less than 100
D. $D=\{x: x$ is real and $-1 \leq x<1\}$

## Answer: D

## - Watch Video Solution

## Very Short Answer Type Questions

1. Define with examples:

Finite and infinite sets
2. Define with examples:

Null set

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3. Define with examples:

Universal set

## - Watch Video Solution

4. Define with examples:

Singleton set

## - Watch Video Solution

5. Define with examples:

Equal sets
6. Define with examples:

Subset and proper subset

## - Watch Video Solution

7. Define with examples:

Union of two sets

## - Watch Video Solution

8. Define with examples:

Intersection of two sets
9. Define with examples:

Disjoint sets

## Watch Video Solution

10. Define with examples:

Complement of a set

## - Watch Video Solution

11. Define with examples:

Difference of two sets

## - Watch Video Solution

12. Define with examples:

Power set
13. Distinguish :

Null set and universal set

## - Watch Video Solution

14. Distinguish :

Union and intersection of two sets

## - Watch Video Solution

15. Distinguish :

Subset and proper subset
16. Distinguish :

Union and difference of two sets

## Watch Video Solution

17. Distinguish :

Universal set and complement of a set

## - Watch Video Solution

18. Write short notes on:

Power set

## - Watch Video Solution

19. Write short notes on:
null set
20. If ${ }^{\wedge} A=\{a, b, c\}$, name
the subsets of A ,

## - Watch Video Solution

21. If ${ }^{\prime} A=\{a, b, c\}$,
write the proper subsets of $A$.

## - Watch Video Solution

22. Define power set of a set A . Find the power set of $A=\{\{1\},\{2,3\}\}$.

## - Watch Video Solution

23. If $A=\{1,2,3,4\}, B=\{2,4,5,8\}$ and $C=\{3,4,5,6,7\}$, find $A \cup B$

## - Watch Video Solution

24. If $A=\{1,2,3,4\}, B=\{2,4,5,8\}$ and $C=\{3,4,5,6,7\}$, find $B \cap C$

## - Watch Video Solution

25. If $A=\{1,2,3,4\}, B=\{2,4,5,8\}$ and $C=\{3,4,5,6,7\}$, find $A \cup(B \cup C)$

## - Watch Video Solution

26. If $A=\{1,2,3,4\}, B=\{2,4,5,8\}$ and $C=\{3,4,5,6,7\}$, find $A \cup(B \cap C)$.
27. If $P=\{a, b, c, d, e\}$ and $Q=\{a, e, i, o, u\}$, prove that $P \subset P \cup Q$

## - Watch Video Solution

28. If $P=\{a, b, c, d, e\}$ and $Q=\{a, e, i, o, u\}$, prove that $P \cap Q \subset P$.

## - Watch Video Solution

29. If $A \subseteq B$ and $B \subseteq C$, prove that $A \subseteq C$.

## - Watch Video Solution

30. If $A \cup B=B$, show that, $A \subseteq B$.
31. If $A \subseteq B, \quad$ prove that, $A-B=\phi$.

## - Watch Video Solution

32. For any two sets A and B , if $A \cup B=A \cap B$, show that $\mathrm{A}=\mathrm{B}$.

## - Watch Video Solution

33. Represent the set in Roster form:
$A=\{(x, y):(x, y)$ is the co or dinate of point of intersection of line $y=x$

## - View Text Solution

## Short Answer Type Questions

1. Write short notes :

Union, intersection and difference of two sets.

## Watch Video Solution

2. Write short notes :

Universal set and subset.

## - Watch Video Solution

3. Write short notes :

The three set operations (union, intersection and complementation).

## - Watch Video Solution

4. State De Morgan's law of sets.
5. State the laws of algebra of sets.

## - Watch Video Solution

6. If $A$ is a finite set and contains $n$ elements, prove that the power set of A has $2^{n}$ elements.

## - Watch Video Solution

7. 

$A=\{a, b, c\}, B=\{a, b\}, C=\{a, b, d\}, D=\{c, d\}$ and $E=\{d\}$.
State which of the following statements are correct and give reasons:
$B \subset A$

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8. 

$A=\{a, b, c\}, B=\{a, b\}, C=\{a, b, d\}, D=\{c, d\}$ and $E=\{d\}$.
State which of the following statements are correct and give reasons:


## - Watch Video Solution

9. 

$A=\{a, b, c\}, B=\{a, b\}, C=\{a, b, d\}, D=\{c, d\}$ and $E=\{d\}$.
State which of the following statements are correct and give reasons:
$D \subset B$

## - Watch Video Solution

10. 

$A=\{a, b, c\}, B=\{a, b\}, C=\{a, b, d\}, D=\{c, d\}$ and $E=\{d\}$.
State which of the following statements are correct and give reasons:
$\{a\} \subset A$

## (D) Watch Video Solution

11. 

Let
$A=\{a, b, c, d, e, f, g, h, i\}, B=\{b, d, f, h\}, C=\{a, c, e, g, i\}, D=\{c, d$
Which set can equal X if we are given the following information?
$X$ and $B$ are disjoint

## - Watch Video Solution

12. 

Let
$A=\{a, b, c, d, e, f, g, h, i\}, B=\{b, d, f, h\}, C=\{a, c, e, g, i\}, D=\{c, d$
Which set can equal X if we are given the following information?
$X \subset A$ but $X \subset C$

## - Watch Video Solution

13. 

Let
$A=\{a, b, c, d, e, f, g, h, i\}, B=\{b, d, f, h\}, C=\{a, c, e, g, i\}, D=\{c, d$

Which set can equal X if we are given the following information?
$X \subset D$ but $X \subset B$

## - Watch Video Solution

14. 

$A=\{a, b, c, d, e, f, g, h, i\}, B=\{b, d, f, h\}, C=\{a, c, e, g, i\}, D=\{c, d$
.Which set can equal X if we are given the following information?
$X \subset C$ but $X \not \subset A$

## - Watch Video Solution

15. If $A=\{a, b, c, d, e\}, B=\{a, c, e, g\}$ and $C=\{b, c, f, g\}$, verify that
$(A \cup B) \cap C=(A \cap C) \cup(B \cap C)$

- Watch Video Solution

16. If $A=\{a, b, c, d, e\}, B=\{a, c, e, g\}$ and $C=\{b, c, f, g\}$, verify that

$$
(A \cap B) \cup C=(A \cup C) \cap(B \cup C) .
$$

## - Watch Video Solution

17. Let $S=\{1,2,3,4,5\}$ be the universal set and let $A=\{3,4,5\}$ and $B=\{1,4,5\}$ be two of its subsets. Verify : $(A \cup B)^{\prime}=A^{\prime} \cap B^{\prime}($ dash denotes complement).

## - Watch Video Solution

18. The set $S=\{1,2,3, \ldots, 12\}$ is to be partitioned into three sets $\mathrm{A}, \mathrm{B}, \mathrm{C}$ of equal size. Thus $A \cup B \cup C=S, A \cap B=B \cap C=C \cap A=\phi$.

Find the number of ways to partition S .

## - Watch Video Solution

19. If $A=\{1,2,3,4\}, B=\{2,3,4,5\}, C=\{1,3,4,5,6,7\}$. Find A-B

## - Watch Video Solution

20. If $A=\{1,2,3,4\}, B=\{2,3,4,5\}, C=\{1,3,4,5,6,7\}$. Find $A-C$ and hence verify that,
$A-(B \cap C)=(A-B) \cup(A-C)$

## - Watch Video Solution

21. If $S=\{1,2,3,4,8,16,32\}$ be the universal set and $A=\{1,2,8,32\}, B=\{4,8,32\}$ be two of its subsets, verify that, $\left(A^{c}\right)^{c}=A$
22. If $S=\{1,2,3,4,8,16,32\}$ be the universal set and $A=\{1,2,8,32\}, B=\{4,8,32\}$ be two of its subsets, verify that, $(A \cap B)^{c}=A^{c} \cup B^{c}$

## - Watch Video Solution

23. If $S=\{1,2,3,4,8,16,32\}$ be the universal set and
$A=\{1,2,8,32\}, B=\{4,8,32\}$ be two of its subsets, verify that, $(A \cup B)^{c}=A^{c} \cap B^{c}$

## - Watch Video Solution

24. 

$P=\{a, b, c, d, e, f\}$ and $Q=\{a, c, e, f\}$, prove that $(P-Q) \cup(P \cap C$

## - Watch Video Solution

25. If $P=\{\theta: \sin \theta-\cos \theta=\sqrt{2} \cos \theta\}$ and
$Q=\{\theta: \sin \theta+\cos \theta=\sqrt{2} \sin \theta\}$, then show that
$P=Q$.

## - Watch Video Solution

26. Given $A=\{1,2,3,4,5\}$ and $B \cup C=\{3,4,6\}$, find $(A \cap B) \cup(A \cap C)$

## - Watch Video Solution

27. Given $A=\{1,2,3,4,5\}$ and $B \cup C=\{3,4,6\}$, find $(A-B) \cap(A-C)$

## - Watch Video Solution

28. Define three sets $P, Q$ and $R$ such that $P \cap Q \neq \phi, Q \cap R \neq \phi, R \cap P \neq \phi$ but $P \cap Q \cap R=\phi$.

## - Watch Video Solution

29. Let $\mathrm{A}, \mathrm{B}$ and C be three sets. If $A \in B$ and $B \subset C$, is it true that $A \subset C$ ? Justify your answer by an example.

## - Watch Video Solution

30. Let $S=\{a, b, c, d, e\}$ be the universal set and let $A=\{a, b, d\}$ and $B=\{b, d, e\}$ be two of its subsets. Find $(A \cap B)^{\prime}$ and $(A \cup B)^{\prime}$.

## - Watch Video Solution

31. Let $S=\{1,2,3,4,5,6\}$ be the universal set. Let $A \cup B=\{2,3,4\}$, find $A^{c} \cap B^{c}$ where $A^{c}, B^{c}$ are complements of A and B respectively.

## - Watch Video Solution

32. If $a \mathbb{N}=\{a x: x \in \mathbb{N}\}$, describe $3 \mathbb{N} \cap 7 \mathbb{N}$ where $\mathbb{N}$ is the set of natural numbers.

## - Watch Video Solution

33. Let $A, B$ and $C$ be three sets. Show by means of examples that each of the following statements is true:
if $B \in A$ and $x \in B$ then $x \in A$

## - Watch Video Solution

34. Let $A, B$ and $C$ be three sets. Show by means of examples that each of the following statements is false:
if $B \subset A$ and $A \in C$ then $B \in C$

## - Watch Video Solution

35. Let $A, B$ and $C$ be three sets. Show by means of examples that each of the following statements is false: if $A \varnothing B$ and $B \varnothing C$ then $A \varnothing C$

## - Watch Video Solution

36. For any two sets $A$ and $B$, prove the following :
$(B-A) \cap A=\phi$

## ( Watch Video Solution

37. For any two sets A and B , prove the following :

$$
A^{c}-B^{c}=B-A
$$

## Watch Video Solution

38. For any two sets A and B , prove the following :
$A-B=A-(A \cap B)$

## - Watch Video Solution

39. For any two sets $A$ and $B$, prove the following :
$A-B=A \cap B^{\prime}$

- Watch Video Solution

40. For any two sets A and B , prove the following :
$B-A^{c}=A \cap B$
41. For any two sets A and B, prove the following :
$B \subseteq(A-B)^{c}$

## - Watch Video Solution

42. For any two sets A and B , prove the following :
$(A \cup B)-(A \cap B)=(A-B) \cup(B-A)$

## - Watch Video Solution

43. For any two sets A and B, prove the following :
$(A-B) \cup(A \cap B)=A$

## - Watch Video Solution

44. Let $\mathbb{Z}$ be the set of integers and $A=\{x: x=6 n, n \in \mathbb{Z}\}, B=\{x: x=4 n, n \in \mathbb{Z}\}$, find $A \cap B$.

## - Watch Video Solution

45. Using set operations find the H.C.F. of the numbers 12,15 and 18 .

## - Watch Video Solution

46. Applying set operations find the L.C.M. of the numbers 15,25 and 30 .

## - Watch Video Solution

47. If $r, s, t$ are prime numbers and $p, q$ are the positive integers such that LCM of $\mathrm{p}, \mathrm{q}$ is $r^{2} t^{4} s^{2}$, then find the number of ordered pair ( $\mathrm{p}, \mathrm{q}$ ).

## - Watch Video Solution

48. Using a Venn diagram or otherwise, solve the following problem: In a class of 70 students, each student has taken either English or Hindi or both. 45 students have taken English and 30 students have taken Hindi. How many students have taken both English and Hindi?

## - Watch Video Solution

49. Use a Venn diagram to solve the following problem:

In a statistical investigation of 1003 families of Kolkata it was found that
63 families had neither a radio nor a T.V., 794 families had a radio and 187 a television. How many families in that group had both a radio and a T.V.?

## - Watch Video Solution

50. A market research group conducted a survey of 1000 consumers and reported that 720 consumers liked product A and 450 consumers liked product $B$. What is the least number that must have liked both products?
51. In a town $60 \%$ red magazine A, $25 \%$ do not read magazine A but read magazine B. Calculate the percentage of those who do not read any magazine. Also find the highest and lowest possible figures of those who read magazine B.

## - Watch Video Solution

52. Two finite sets $A$ and $B$ have respectively $p$ and $q$ elements. If the total number of subsets of $A$ is 56 more than the total number of subsets of $B$, then find the values of $p$ and $q$.

## - Watch Video Solution

53. Two finite sets $A$ and $B$ have $m$ and $n$ elements respectively. Find the maximum and minimum elements are in $A \cup B$.

## Long Answer Type Questions

1. For a finite set $A$, the number of elements in $A$ is denoted by $n(A)$. Use a

Venn diagram (or otherwise) to prove that, for any two sets $A, B$
$n(A \cup B)=n(A)+n(B)-n(A \cap B)$

## - Watch Video Solution

2. Given, $A=\{x: 0<x \leq 2\}$ and $B=\{x: 1<x<3\}$, find $A \cap B$

## - Watch Video Solution

3. Given, $A=\{x: 0<x \leq 2\}$ and $B=\{x: 1<x<3\}$, find
$A \cup B$
4. Given, $A=\{x: 0<x \leq 2\}$ and $B=\{x: 1<x<3\}$, find $A-B$

## - Watch Video Solution

5. Given, $A=\{x: 0<x \leq 2\}$ and $B=\{x: 1<x<3\}$, find
$(A \cup B)-(A \cap B)$

## - Watch Video Solution

6. Let $A=\{x: 2 \leq x<5\}$ and $B=\{x: 3<x<7\}$ be two subsets of the universal set, $S=\{x: 0<x \leq 10\}$, verify that, $(A \cup B)^{c}=A^{c} \cap B^{c}$

- Watch Video Solution

7. If $P=\{p, q, r, s, t, u\}$ and $Q \cap R=\{q, r, v, w\}$, find $(P \cup Q) \cap(P \cup R)$

## - Watch Video Solution

8. If $P=\{p, q, r, s, t, u\}$ and $Q \cap R=\{q, r, v, w\}$, find
$(P-Q) \cup(P-R)$

## - Watch Video Solution

9. If $A, B, C$ be three subsets of the universal set $S$ where
$S=\{1,2,3,4,5,6,7\}, A=\{1,3,5,6\}$ and $B \cap C=\{1,2,6\}, \quad$ find $(A \cup B) \cap(A \cup C)$ and $B^{c} \cup C^{c}$.

## - Watch Video Solution

10. If $U=\{a, b, c, d, e, f\}$ be the universal set and $\mathrm{A}, \mathrm{B}, \mathrm{C}$ are three subsets of U , where $A=\{a, c, d\}$ and $B \cup C=\{a, d, c, f\}$, find $(A \cap B) \cup(A \cap C)$ and

## - Watch Video Solution

11. If $U=\{a, b, c, d, e, f\}$ be the universal set and $\mathrm{A}, \mathrm{B}, \mathrm{C}$ are three subsets of U , where $A=\{a, c, d\}$ and $B \cup C=\{a, d, c, f\}$, find $\left(B^{\prime} \cap C^{\prime}\right)$

## - Watch Video Solution

12. 

Given

$$
X \cup Y=\{1,2,3,4\}, X \cup Z=\{2,3,4,5\}, X \cap Y=\{2,3\} \text { and } X \cap Z=
$$

, find $X, Y$ and $Z$.
13. Verify the following relations using Venn diagrams:
$(A \cup B) \cap(A \cup C)=A \cup(B \cap C)$

## - Watch Video Solution

14. Verify the following relations using Venn diagrams:

$$
A \cap(B \cup C)=(A \cap B) \cup(A \cap C)
$$

## - Watch Video Solution

15. Verify the following relations using Venn diagrams:
$(A \cup B)^{c}=A^{c} \cap B^{c}$

## - Watch Video Solution

16. Verify the following relations using Venn diagrams:
$(A \cap B)^{c}=A^{c} \cup B^{c}$
17. Verify the following relations using Venn diagrams:
$A-(B \cap C)=(A-B) \cup(A-C)$

## - Watch Video Solution

18. Verify the following relations using Venn diagrams:
$A-(B \cup C)=(A-B) \cap(A-C)$

- Watch Video Solution

19. Verify the following relations using Venn diagrams:
$(A-C) \cap(B-C)=(A \cap B)-C$

- Watch Video Solution

20. Draw a Venn diagram of three non-empty sets A , B and C such that $A \subset B, C \varnothing B, A \cap C=\phi$

## - Watch Video Solution

21. If $A, B$ and $C$ are three non-empty subsets of the universal set $S$, draw a

Venn diagram to illustrate the following case :
$A \subset B, B \cap C \neq \phi, A \cap C=\phi, C \subset B$

## - Watch Video Solution

22. For any three sets A , B and C prove the followings:
$A \cup(B \cap C)=(A \cup B) \cap(A \cup C)$

## - Watch Video Solution

23. For any three sets A , B and C prove the followings:

$$
A \cap(B \cup C)=(A \cap B) \cup(A \cap C)
$$

## - Watch Video Solution

24. For any three sets A , B and C prove the followings :
$A \cup(B \cup C)=(A \cup B) \cup C$

## - Watch Video Solution

25. For any three sets A , B and C prove the followings:

$$
A \cap(B \cap C)=(A \cap B) \cap C
$$

## - Watch Video Solution

26. For any three sets A , B and C prove the followings :
$(A \cup B)^{c}=A^{c} \cap B^{c}$
27. For any three sets A, B and C prove the followings :
$(A \cap B)^{c}=A^{c} \cup B^{c}$

## - Watch Video Solution

28. For any three sets $\mathrm{A}, \mathrm{B}$ and C prove the followings:
$A-(B \cup C)=(A-B) \cap(A-C)$

## - Watch Video Solution

29. For any three sets A , B and C prove the followings:
$A-(B \cap C)=(A-B) \cup(A-C)$

- Watch Video Solution

30. For any three sets $A, B$ and $C$ prove the followings:

$$
(A \cap B)-C=(A-C) \cap(B-C)
$$

## - Watch Video Solution

31. For any three sets $A, B$ and $C$ prove the followings:
$(A \cup B)-C=(A-C) \cup(B-C)$

- Watch Video Solution

32. Applying Set Algebra, prove the :
$A \cap(B-A)=\phi$

## - Watch Video Solution

33. Applying Set Algebra, prove the :
$A \cup(B-A)=A \cup B$
34. Applying Set Algebra, prove the :

$$
(A \cap B)-C=(A-C) \cap(B-C)
$$

## - Watch Video Solution

35. Applying Set Algebra, prove the :
$(A \cup B)-C=(A-C) \cup(B-C)$

## - Watch Video Solution

36. In an engineering college, 80 students get chance for Computer Science, 75 for information Technology, 72 for Electronics. If 60 students get chance in 1st and 2nd, 50 in 2nd and 3rd, 40 in 1st and 3 rd and 30 get chance in all three branches, how many seats are there in the engineering college? [The college has only three disciplines.]
37. In a survey of college students it was found that $40 \%$ use their own books, $50 \%$ use library books, $30 \%$ use borrowed books, $20 \%$ use both their own books and library books. $15 \%$ use their own books and borrowed books, $10 \%$ use library books and borrowed books, and $4 \%$ use their own books, library books and borrowed books. Calculate the percentage of students who do not use a book at all.

## - Watch Video Solution

38. A company studies the product preferences of 300 consumers. It was found that 226 liked product A, 51 liked product B, 54 liked product C,21 liked products A and B, 54 liked products A and C, 39 liked products B and C and 9 liked all the three products. Prove that, the study results are not correct. [ Assume that each consumer likes at least one of the three products.]
39. In a city three daily newspapers $X, Y, Z$ are published, $65 \%$ of the citizens read $\mathrm{X}, 54 \%$ read $\mathrm{Y}, 45 \%$ read $\mathrm{Z}, 38 \%$ read X and $\mathrm{Y}, 32 \%$ read Y and $\mathrm{Z}, 28 \%$ read X and $\mathrm{Z}, 12 \%$ do not read any one of these three papers. If the total number of people in the city be 1000000 find the number of citizens who read all the three newspapers. [You may use a Venn diagram or a standard formula for the enumeration of elements of sets.]

## - Watch Video Solution

40. Out of 1000 students in a college, 540 played football, 465 played cricket and 370 played volleyball, of the total 325 played both football and cricket. 260 played football and volleyball, 234 played cricket and volleyball, 125 played all the three games. How many students did not play any game

## - Watch Video Solution

41. Out of 1000 students in a college, 540 played football, 465 played cricket and 370 played volleyball, of the total 325 played both football and cricket. 260 played football and volleyball, 234 played cricket and volleyball, 125 played all the three games. How many students played only one game?

## - Watch Video Solution

42. Out of 1000 students in a college, 540 played football, 465 played cricket and 370 played volleyball, of the total 325 played both football and cricket. 260 played football and volleyball, 234 played cricket and volleyball, 125 played all the three games. How many students played just two games?

## - Watch Video Solution

43. A group consists of a number of students and each students and each student of the group can speak at least one of the languages Bengali,

Hindi and English. 65 can speak Bengali, 54 Hindi and 37 English, 31 can speak both Bengali and Hindi, 17 both Hindi and English, and 18 both Bengali and English. Determine the greatest and least number of students in the group.

## - Watch Video Solution

44. Using set operations show that the numbers 231 and 260 are prime to each other.

## - Watch Video Solution

45. suppose $A_{1}, A_{2}, \ldots, A_{30}$ are thirty sets each with five elements and $B_{1}, B_{2}, \ldots, B_{n}$ are n sets each with three elements.

Let $A_{1} \cup A_{2} \cup \ldots \cup A_{30}=B_{1} \cup B_{2} \cup \ldots \cup B_{n}=S$.
Assume that each element of S belongs to exactly ten of the A's and to exactly nine of the B's. Find $n$.
46. At a certain conference of 100 people, there are 29 Indian women and 23 Indian men. Of these Indian people 4 are doctors and 24 are either men or doctors. There are no foreign doctors. How many foreigners are attending the conference? How many women doctors are their in the conference?

## - Watch Video Solution

47. If two sets $A$ and $B$ are having 99 elements in common, then find the number of elements common to each of the sets $A \times B$ and $B \times A$.

## - Watch Video Solution

## Multiple Correct Answer Type

1. If $A$ be a set, then $\qquad$
A. $A \cap \phi=\phi$
B. $A \cap \phi=A$
C. $A \cup \phi=A$
D. $A \cup \phi=\phi$

## Answer: A,C

## - Watch Video Solution

2. If $A=\{a, b, c, d\}$ and $B=\{b, c, d, e\}$ be two sets then $\qquad$
A. $A-B=\{a\}$
B. $B-A=\{e\}$
C. $A-B=\{b, c, d\}$
D. $B-A=\{b, c, d\}$

## Answer: A,B

3. If $A, B$ and $C$ are three finite sets,
$n(A)=10, n(B)=15, n(C)=20, n(A \cap B)=8$ and $n(B \cap C)=9$, then the value of $n(A \cup B \cup C)$ will be $\qquad$
A. 26
B. 27
C. 28
D. none of these

## Answer: A,B,C

## - Watch Video Solution

4. Given $A, B, C$ are three sets. State which of the followings are true $\qquad$
A. $A \cup B=B \cup A$
B. $A \cap B=B \cap A$
C. $A \cup(B \cap C)=(A \cup B) \cap(A \cap C)$
D. $(A \cap B) \cap C=A \cap(B \cap C)$

## Answer: A,B,C

## - Watch Video Solution

5. State which of the followings are null set?
A. $\left\{x \in \mathbb{R}: x^{2}+1=0\right\}$
B. $\{x \in \mathbb{C}: x>x\}$
C. $\left\{x \in \mathbb{R}: x^{2}+x=0\right\}$
D. $\left\{x \in \mathbb{R}: x^{2}+2=0\right\}$

## Answer: A,B

## - Watch Video Solution

1. If $a \mathbb{N}=\{a x: x \in \mathbb{N}\}$ then $3 \mathbb{N} \cap 7 \mathbb{N}=3 P \mathbb{N}$ what will be the value of P?

## - Watch Video Solution

2. If $A$ and $B$ are two sets such that $n(A)=70, n(B)=60$ and $n(A \cup B)=110, \quad$ then $n(A \cap B)=5 K$. What will be the value of $K$ ?

## - Watch Video Solution

3. If $n(A)=3, n(B)=6$ and $A \subseteq B$, then find $n(A \cup B)$.

## - Watch Video Solution

4. If $A=\{2,4,5\}$ and $B=\{7,8,9\}$ then find $n(A \times B)$.
5. Let $S=\{0,1,5,4,7\}$, number of subsets of S is $32 \mathbb{Q}$, then find the value of $\mathbb{Q}$.

## - Watch Video Solution

## Comprehension Type

1. In a class there are 115 students of which 65 like cricket, 45 like football and 42 like hockey, 20 like both football and cricket, 25 like both cricket and hockey and 15 like both hockey and football. Further 8 of the students like all the three games.

Number of students who like at least one of these three games
A. 98
B. 99
C. 100
D. 101

## Answer: C

## - Watch Video Solution

2. In a class there are 115 students of which 65 like cricket, 45 like football and 42 like hockey, 20 like both football and cricket, 25 like both cricket and hockey and 15 like both hockey and football. Further 8 of the students like all the three games.

Number of students who like exactly one game
A. 50
B. 55
C. 54
D. 56

## Answer: D

3. In a class there are 115 students of which 65 like cricket, 45 like football and 42 like hockey, 20 like both football and cricket, 25 like both cricket and hockey and 15 like both hockey and football. Further 8 of the students like all the three games.

Number of students who like exactly two games
A. 34
B. 36
C. 35
D. 37

## Answer: B

## D Watch Video Solution

4. 

$$
A=\{x: x \in \mathbb{N}\}, B=\{x: x \in 2 n, n \in \mathbb{N}\}, C=\{x: x=2 n-1, n \in \mathbb{N}\} \text { a }
$$

$D=\{x: x$ is a prime number $\}$ then $\qquad$
$A \cap C$ is
A. A
B. C
C. D
D. $\{2\}$

## Answer: B

## - Watch Video Solution

5. 

$A=\{x: x \in \mathbb{N}\}, B=\{x: x \in 2 n, n \in \mathbb{N}\}, C=\{x: x=2 n-1, n \in \mathbb{N}\}$ a
$D=\{x: x$ is a prime number $\}$ then
$B \cap C$ is
A. $\phi$
B. $\{2\}$
C. B
D. D

## Answer: A

## - Watch Video Solution

6. 

$A=\{x: x \in \mathbb{N}\}, B=\{x: x \in 2 n, n \in \mathbb{N}\}, C=\{x: x=2 n-1, n \in \mathbb{N}\}$ $D=\{x: x$ is a prime number $\}$ then $\qquad$
$C \cap D$ is

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## Assertion Reason Type

1. Let $A=\{1,2,3\}$ and $B=\{3,8\}$

Statement-I : $(A \cup B) \times(A \cap B)=\{(1,3),(2,3),(3,3),(8,3)\}$

Statement-II : $(A \times B) \cap(B \times A)=\{(3,3)\}$
A. Statement-I is true, Statement-II is true and Statement-II is a correct explanation for statement-l.
B. Statement-I is true, Statement-II is true but Statement-II is not a correct explanation of Statement-I.
C. Statement-I is true, Statement-II is false.
D. Statement-I is false,Statement-II is true.

## Answer: B

## - Watch Video Solution

2. Let $X$ and $Y$ be two sets

Statement-I: $X \cap(Y \cup X)^{\prime}=\phi$
Statement-II : If $\quad n(X \cup Y)=P$ and $n(X \cap Y)=\phi \quad$ then
$n(X \Delta Y)=P-Q[$ where $X \Delta Y=(A-B) \cup(B-A)]$
A. Statement-I is true, Statement-II is true and Statement-II is a correct
explanation for statement-I.
B. Statement-I is true, Statement-II is true but Statement-II is not a correct explanation of Statement-I.
C. Statement-I is true, Statement-II is false.
D. Statement-I is false,Statement-II is true.

## Answer: B

## - View Text Solution

