



## MATHS

### BOOKS - TARGET MATHS (HINGLISH)

#### TRIGONOMETRIC FUNCTIONS OF COMPOUND ANGLES

##### Classical Thinking

1. The value of  $\cos 105^\circ$  is

A.  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$

B.  $\frac{\sqrt{3} - 1}{2\sqrt{2}}$

C.  $-\frac{\sqrt{3} + 1}{2\sqrt{2}}$

D.  $\frac{1 - \sqrt{3}}{2\sqrt{2}}$

Answer: D



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2.  $\tan 15^\circ =$

A.  $\frac{1}{3}$

B.  $\sqrt{3} - 2$

C.  $2 - \sqrt{3}$

D.  $2 + \sqrt{3}$

**Answer: C**



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3.  $\cos 38^\circ \cos 8^\circ + \sin 38^\circ \sin 8^\circ$  is equal to

A.  $\cos 30^\circ$

B.  $\cos 60^\circ$

C.  $\cos 45^\circ$

D.  $\cos 38^\circ$

**Answer: A**



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4.  $\frac{1}{3}(\sqrt{3}\cos 23^\circ - \sin 23^\circ) =$

A.  $\cos 43^\circ$

B.  $\cos 7^\circ$

C.  $\frac{1}{4}\cos 53^\circ$

D.  $\frac{2}{3}\cos 53^\circ$

**Answer: D**



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5. The value of  $\tan 5A - \tan 3A - \tan 2A$  is equal to

A.  $\tan 5A \tan 3A \tan 2A$

B.  $-\tan 5A \tan 3A \tan 2A$

C. 0

D. 1

**Answer: A**

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**6.** The value of

$\tan 57^\circ - \tan 12^\circ - \tan 57^\circ \tan 12^\circ$  is

A.  $\tan 69^\circ$

B.  $\tan 45^\circ$

C. 0

D.  $\tan 57^\circ$

**Answer: B**

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7.  $\frac{\cos 10^\circ + s \in 10^\circ}{\cos 10^\circ - s \in 10^\circ}$  is equal to  $\tan 55^\circ$  b.  $\cos 55^\circ$  c.  $-\tan 35^\circ$  d.  $-\cot 35^\circ$

A.  $\tan 55^\circ$

B.  $\cot 55^\circ$

C.  $-\tan 55^\circ$

D.  $-\cot 35^\circ$

**Answer: A**

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8. Find value of  $(\cos 8^\circ - \sin 8^\circ) / (\cos 8^\circ + \sin 8^\circ)$

A.  $\tan 53^\circ$

B.  $\tan 37^\circ$

C.  $\tan 82^\circ$

D.  $\tan 62^\circ$

**Answer: B**



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9. If  $\tan A = \frac{a}{a+1}$  and  $\tan B = \frac{1}{2a+1}$  then find the value of  $A+B$

A. 0

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{3}$

D.  $\frac{\pi}{4}$

**Answer: D**



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10. If  $\tan A - \tan B = x$  and  $\cot B - \cot A = y$ , then what is  $\cot (A - B)$  equal to ?

A.  $\frac{1}{x} + y$

B.  $\frac{1}{xy}$

C.  $\frac{1}{x} - \frac{1}{y}$

D.  $\frac{1}{x} + \frac{1}{y}$

**Answer: D**



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11. The value of  $\cos^2 48^\circ - \sin^2 12^\circ$  is

A.  $\frac{\sqrt{5} - 1}{4}$

B.  $\frac{\sqrt{5} + 1}{8}$

C.  $\frac{\sqrt{3} - 1}{4}$

D.  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$

**Answer: B**



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12.  $\frac{\cot^2 15^\circ - 1}{\cot^2 15^\circ + 1} =$

A.  $\frac{1}{2}$

B.  $\frac{\sqrt{3}}{2}$

C.  $\frac{3\sqrt{3}}{4}$

D.  $\sqrt{3}$

**Answer: B**



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13. The value of  $\tan(-945^\circ)$  is

A.  $-1$



B.  $-2$

C.  $-3$

D.  $-4$

**Answer: A**



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14.  $\sin\left(\frac{\pi}{10}\right)\sin\left(\frac{3\pi}{10}\right)$

A.  $\frac{1}{2}$

B.  $\frac{-1}{2}$

C.  $\frac{1}{4}$

D. 1

**Answer: C**



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15.  $\sin 15^\circ + \cos 105^\circ =$

A. 0

B.  $2\sin 15^\circ$

C.  $\cos 15^\circ + \sin 15^\circ$

D.  $\sin 15^\circ - \cos 15^\circ$

**Answer: A**



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16. If  $\tan A = \frac{1}{2}$ ,  $\tan B = \frac{1}{3}$ , then  $\cos 2A =$

A.  $\sin B$

B.  $\sin 2B$

C.  $\sin 3B$

D.  $-\sin 2B$

**Answer: B**



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17. If  $8\theta = \pi$ , then  $\cos 7\theta + \cos \theta$  is equal to

A. 0

B. 1

C.  $-1$

D. 7

**Answer: A**



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18. If ABCD is a cyclic quadrilateral, then  $\cos A + \cos B$  is equal to

A. 0

B.  $\cos C + \cos D$

C.  $-(\cos C + \cos D)$

D.  $\cos C - \cos D$

**Answer: C**



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19. If ABCD is a cyclic quadrilateral, then the value of  $\cos A - \cos B + \cos C - \cos D$  is

A. 0

B. 1

C.  $2(\cos B - \cos D)$

D.  $2(\cos A - \cos C)$

**Answer: A**



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20.  $\sin 10^\circ + \sin 20^\circ + \sin 30^\circ + \dots + \sin 360^\circ$  is equal to

A. 0

B. 1

C.  $-1$

D.  $\frac{1}{2}$

**Answer: A**



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21.  $\cos 1^\circ + \cos 2^\circ + \cos 3^\circ + \dots + \cos 180^\circ$  is equal to

A. 0

B. 1

C.  $-1$

D. 2

**Answer: C**



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**22.** Which of the following is the correct identity ?

A.  $\cos\left(\frac{\pi}{2} + A\right) = \tan A$

B.  $\sec\left(\frac{7\pi}{2} - A\right) = \csc A$

C.  $\sin(n\pi + A) = -\sin A$

D.  $\sin(\pi - A) = -\sin A$

**Answer: B**



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**23.** The value of  $\frac{\cot 54^\circ}{\tan 36^\circ} + \frac{\tan 20^\circ}{\cot 70^\circ}$  is

A. 0

B. 2

C. 3

D. 1

**Answer: B**



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**24. Prove that**

$$\frac{\cos(90^\circ + \theta)\sec(-\theta)\tan(180^\circ - \theta)}{\sec(360^\circ - \theta)\sin(180^\circ + \theta)\cot(90^\circ - \theta)} = -1$$

A. 2

B. 1

C. -1

D. 0

**Answer: C**



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25.  $\sin^2 25^\circ + \sin^2 65^\circ$  is equal to

A. 0

B. 1

C.  $\frac{1}{2}$

D. 2

**Answer: B**



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26. The value of :

$$\sin^2\left(\frac{\pi}{8}\right) + \sin^2\left(\frac{3\pi}{8}\right) + \sin^2\left(\frac{5\pi}{8}\right) + \sin^2\left(\frac{7\pi}{8}\right) \text{ is :}$$

A. 1

B. 2

C.  $\frac{3}{8}$



D.  $\frac{1}{8}$

**Answer: B**



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27.  $\cos 2\theta$  is not equal to

A.  $2 \cos^2 \theta - 1$

B.  $1 - 2 \sin^2 \theta$

C.  $\frac{1 + \tan^2 \theta}{1 - \tan^2 \theta}$

D.  $\frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$

**Answer: C**



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28.  $\sin 4\theta$  can be written as

A.  $4 \sin \theta (1 - 2 \sin^2 \theta) \sqrt{1 - \sin^2 \theta}$

B.  $2 \sin \theta \cos \theta \sin^2 \theta$

C.  $4 \sin \theta - 6 \sin^3 \theta$

D.  $4 \sin \theta + 6 \sin^2 \theta$

**Answer: A**

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**29.** If  $\tan \theta = t$ , then  $\tan 2\theta + \sec 2\theta =$

A.  $\frac{1+t}{1-t}$

B.  $\frac{1-t}{a+t}$

C.  $\frac{2t}{a-t}$

D.  $\frac{2t}{1+t}$

**Answer: A**

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30. If  $\sin A + \cos A = 1$ , then  $\sin 2A$  is equal to

A. 1

B. 2

C. 0

D.  $\frac{1}{2}$

**Answer: C**



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31. Find the value of:  $\sqrt{2 + \sqrt{2 + 2 \cos 4\theta}}$

A.  $\cos \theta$

B.  $\sin \theta$

C.  $2 \cos \theta$

D.  $2 \sin \theta$

**Answer: C**



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**32.**  $1 + \cos^2 2A$  is equal to

A.  $\sin^4 A + \cos^4 A$

B.  $\sin^2 2A$

C.  $2(\cos^4 A + \sin^4 A)$

D.  $2(\cos^4 A - \sin^4 A)$

**Answer: C**



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**33.**  $1 - 2 \sin^2 \left( \frac{\pi}{4} + \theta \right) =$

A.  $\cos 2\theta$

B.  $-\cos 2\theta$

C.  $\sin 2\theta$

D.  $-\sin 2\theta$

**Answer: D**

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**34.** The largest value of  $\sin \theta \cos \theta$  is

A. 1

B.  $\frac{1}{2}$

C.  $\frac{1}{\sqrt{2}}$

D.  $\frac{\sqrt{3}}{2}$

**Answer: B**

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35.  $(\sec 2A + 1)\sec^2 A =$

A.  $\sec A$

B.  $2 \sec A$

C.  $\sec 2A$

D.  $2 \sec 2A$

**Answer: D**



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36.  $\cos ecA - 2 \cot 2A \cos A =$

A.  $2 \sin A$

B.  $\sec A$

C.  $2 \cos A \cot A$

D.  $\cos A$

**Answer: A**



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37.  $\cos 20^\circ \cos 40^\circ \cos 80^\circ =$

A.  $\frac{1}{2}$

B.  $\frac{1}{4}$

C.  $\frac{1}{6}$

D.  $\frac{1}{8}$

**Answer: D**



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38.  $\frac{\sin \theta + \sin 2\theta}{1 + \cos \theta + \cos 2\theta} =$

A.  $\frac{1}{2} \tan \theta$

B.  $\frac{1}{2} \cot \theta$

C.  $\tan \theta$

D.  $\cot \theta$

**Answer: C**

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39. If  $\sin 2\theta = \frac{3}{4}$ , then  $\sin^3 \theta + \cos^3 \theta =$

A.  $\frac{\sqrt{5}}{8}$

B.  $\frac{\sqrt{7}}{8}$

C.  $\frac{\sqrt{11}}{8}$

D.  $\frac{5\sqrt{7}}{16}$

**Answer: D**

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40. If  $\cos 3\theta = \alpha \cos \theta + \beta \cos^3 \theta$ , then  $(\alpha, \beta) =$

A. (3, 4)

B. (4, 3)

C. (-3, 4)

D. 3, -4)

**Answer: C**



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41. If  $\tan A = \frac{1}{2}$ , then  $\tan 3A =$

A.  $\frac{9}{2}$

B.  $\frac{11}{2}$

C.  $\frac{7}{2}$

D.  $-\frac{1}{2}$

**Answer: B**



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42. If  $x + \frac{1}{x} = 2 \cos \theta$ , then  $\left(x^3 + \frac{1}{x^3}\right)$  is equal to-

A.  $\cos 3\theta$

B.  $2 \cos 3\theta$

C.  $\frac{1}{2} \cos 3\theta$

D.  $\frac{1}{3} \cos 3\theta$

**Answer: B**



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43. If  $\sin \alpha = \frac{-3}{5}$ , where  $\pi < \alpha < \frac{3\pi}{2}$ , then  $\cos\left(\frac{\alpha}{2}\right) =$

A.  $\frac{-1}{\sqrt{10}}$

B.  $\frac{1}{\sqrt{10}}$

C.  $\frac{3}{\sqrt{10}}$

D.  $\frac{-3}{\sqrt{10}}$

**Answer: A**



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44. If  $\tan \frac{\theta}{2} = t$ , then the value of  $\frac{1 - t^2}{1 + t^2}$  is

A.  $\cos \theta$

B.  $\sin \theta$

C.  $\sec \theta$

D.  $\cos 2\theta$

**Answer: A**



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45. If  $\tan \frac{A}{2} = \frac{3}{2}$ , then  $\frac{1 + \cos A}{1 - \cos A} =$

A.  $-5$

B.  $5$

C.  $\frac{9}{4}$

D.  $\frac{4}{9}$

**Answer: D**



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46.  $\tan \frac{A}{2}$  is equal to

A.  $\sqrt{\frac{1 - \sin A}{1 + \sin A}}$

B.  $\sqrt{\frac{1 + \sin A}{1 - \sin A}}$

C.  $\sqrt{\frac{1 - \cos A}{1 + \cos A}}$

D.  $\sqrt{\frac{1 + \cos A}{1 - \cos A}}$

**Answer: C**

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47. If  $\tan \beta = \cos \theta \tan \alpha$ , then prove that  $\tan^2 \frac{\theta}{2} = \frac{\sin(\alpha - \beta)}{\sin(\alpha + \beta)}$ .

A.  $\frac{\sin(\alpha + \beta)}{\sin(\alpha + \beta)}$

B.  $\frac{\cos(\alpha - \beta)}{\cos(\alpha + \beta)}$

C.  $\frac{\sin(\alpha - \beta)}{\sin(\alpha - \beta)}$

D.  $\frac{\cos(\alpha + \beta)}{\cos(\alpha - \beta)}$

**Answer: C**

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**Critical Thinking**

1. If  $\cos(A + B) = \alpha \cos A \cos B + \beta \sin A \sin B$ , then  $(\alpha, \beta)$  is

A.  $(-1, -1)$

B.  $(-1, 1)$

C.  $(1, -1)$

D.  $(1, 1)$

**Answer: C**



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2. If  $\sin A = \frac{4}{5}$  and  $\cos B = -\frac{12}{13}$ , where A and B lie in first and third quadrant respectively, then  $\cos(A + B) =$

A.  $\frac{56}{65}$

B.  $-\frac{56}{65}$

C.  $\frac{16}{65}$

D.  $-\frac{16}{56}$

**Answer: D**



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3. If  $\sin A = \frac{1}{\sqrt{10}}$  and  $\sin B = \frac{1}{\sqrt{5}}$ , where  $A$  and  $B$  are positive acute angles, then  $A + B$  is equal to

A.  $\pi$

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{3}$

D.  $\frac{\pi}{4}$

**Answer: D**



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4. If  $\tan \theta = 1/2$  and  $\tan \phi = 1/3$ , then  $\tan(2\theta + \phi)$

A. 1

B. 2

C. 3

D. 4

**Answer: C**

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5. If  $\theta$  lies in the first quadrant and  $\cos \theta = \frac{8}{17}$ , then find the value of  $\cos(30^\circ + \theta) + \cos(45^\circ - \theta) + \cos(120^\circ - \theta)$ .

A.  $\frac{23}{17} \left( \frac{\sqrt{3} - 1}{2} + \frac{1}{\sqrt{2}} \right)$

B.  $\frac{23}{17} \left( \frac{\sqrt{3} - 1}{2} + \frac{1}{\sqrt{2}} \right)$

C.  $\frac{23}{17} \left( \frac{\sqrt{3} + 1}{2} - \frac{1}{\sqrt{2}} \right)$

D.  $\frac{23}{17} \left( \frac{\sqrt{3} + 1}{2} - \frac{1}{\sqrt{2}} \right)$

**Answer: A**





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6. If  $A - B = \pi/4$ , then  $(1 + \tan A)(1 - \tan B)$  is equal to

A. 1

B. 2

C.  $\infty$

D. -2

Answer: B



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7. If  $A + B = 45^\circ$ , then  $(\cot A - 1)(\cot B - 1)$  is equal to

A. 0

B. 2

C. 1

D. 4

**Answer: B**



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8. If  $\cos(\theta - \alpha) = a$ ,  $\sin(\theta - \beta) = b$ , then  $\cos^2(\alpha - \beta) + 2ab \sin(\alpha - \beta)$  is equal to

A.  $4a^2b^2$

B.  $a^2 - b^2$

C.  $a^2 + b^2$

D.  $-a^2b^2$

**Answer: C**



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9. If  $x, y, z$  are any three real numbers, then  $\tan(x - y) + \tan(y - z) + \tan(z - x)$  is equal to

A. 1

B. 0

C.  $\tan(x - y)\tan(y - z)\tan(z - x)$

D.  $\tan(y - x)\tan(z - y)\tan(z - x)$  is equal to

**Answer: C**



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10. The value of  $\tan 3A - \tan 2A - \tan A$  is equal to (A)  $\tan 3A \tan 2A \tan A$  (B)  $-\tan 3A \tan 2A \tan A$  (C)  $\tan A \tan 2A - \tan 2A \tan 3A - \tan 3A \tan A$  (D) none of these

A.  $\tan 3A \tan 2A \tan A$

B.  $-\tan 3A \tan 2A \tan A$

C.  $\tan A \tan 2A - \tan 2A \tan 3A$

D.  $\tan 2A \tan 3A - \tan A \tan 2A$

**Answer: A**

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11.  $\tan 20^\circ + \tan 40^\circ + \sqrt{3} \cdot \tan 20^\circ \cdot \tan 40^\circ =$

A.  $\frac{1}{\sqrt{3}}$

B.  $\sqrt{3}$

C.  $-\frac{1}{\sqrt{3}}$

D.  $-\sqrt{3}$

**Answer: B**

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12.  $\tan \frac{2\pi}{5} - \tan \frac{\pi}{15} - \sqrt{3} \tan \frac{2\pi}{5} \tan \frac{\pi}{15}$  is equal to

A.  $-\sqrt{3}$

B.  $\frac{1}{\sqrt{3}}$

C. 1

D.  $\sqrt{3}$

**Answer: D**



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13. If  $\tan A = 2 \tan B + \cot B$ , then  $2 \tan(A - B)$  is equal to

A.  $\tan B$

B.  $2 \tan B$

C.  $\cot B$

D.  $2 \cos B$

**Answer: C**

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14. If  $\alpha, \beta, \gamma, \in \left(0, \frac{\pi}{2}\right)$ , then prove that  $\frac{\sin(\alpha + \beta + \gamma)}{\sin \alpha + \sin \beta + \sin \gamma} < 1$

A.  $< 1$

B.  $> 1$

C. 1

D. None of these

**Answer: A**

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15.  $\frac{1}{\tan 3A - \tan A} - \frac{1}{\cot 3A - \cot A} =$

A.  $\tan A$

B.  $\tan 2A$

C.  $\cot A$

D.  $\cot 2A$

**Answer: D**



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16. Show that  $\sin 150^\circ + \cos 105^\circ = \frac{1}{\sqrt{5}}$

A.  $\frac{1}{2}$

B. 1

C.  $\sqrt{2}$

D.  $\frac{1}{\sqrt{2}}$

**Answer: D**



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17. The value of

$\tan 81^\circ - \tan 63^\circ - \tan 27^\circ + \tan 9^\circ$  is equal to

A. 1

B. 2

C. 3

D. 4

**Answer: D**



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18. If  $\alpha + \beta = \frac{\pi}{2}$  and  $\beta + \gamma = \alpha$ , then  $\tan \alpha$  equals  $2(\tan \beta + \tan \gamma)$  (b)

$\tan \beta + \tan \gamma$  (c)  $\tan \beta + 2 \tan \gamma$  (d)  $2 \tan \beta + \tan \gamma$

A.  $2(\tan \beta + \tan \gamma)$

B.  $\tan \beta + \tan \gamma$

C.  $\tan \beta + 2 \tan \gamma$



$$D. 2 \tan \beta + \tan \gamma$$

**Answer: C**



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19.  $\tan\left(\frac{\pi}{4} + \theta\right)\tan\left(\frac{3\pi}{4} + \theta\right)$  is equal to

A.  $-2$

B.  $-1$

C.  $1$

D.  $0$

**Answer: B**



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20.  $\tan(100^\circ) + \tan(125^\circ) + \tan(100^\circ)\tan(125^\circ) =$

A. 0

B.  $\frac{1}{2}$

C.  $-1$

D. 1

**Answer: D**



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21. If  $A+B=225^\circ$  Find  $\cot A/(1+\cot A)*\cot B(1+\cot B)$

A. 1

B.  $-1$

C. 0

D.  $\frac{1}{2}$

**Answer: D**



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22. The value of  $\frac{\sin(-660^\circ)\tan(1050^\circ)\sec(420^\circ)}{\cos(225^\circ)\cos(315^\circ)\cos(510^\circ)}$  is:

A.  $\frac{\sqrt{3}}{4}$

B.  $\frac{\sqrt{3}}{2}$

C.  $\frac{2}{\sqrt{3}}$

D.  $\frac{4}{\sqrt{3}}$

**Answer: C**



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23.  $\cos^2\left(\frac{\pi}{4}\beta\right) - \sin^2\left(\alpha - \frac{\pi}{4}\right) =$

A.  $\sin(\alpha + \beta)\sin(\alpha - \beta)$

B.  $\cos(\alpha + \beta)\cos(\alpha - \beta)$

C.  $\sin(\alpha + \beta)\cos(\alpha + \beta)$

D.  $\sin(\alpha + \beta)\cos(\alpha - \beta)$

**Answer: D**



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24. The value of  $\cos^2\left(\frac{\pi}{12}\right) + \cos^2\left(\frac{\pi}{4}\right) + \cos^2\left(\frac{5\pi}{12}\right)$  is

A.  $\frac{2}{3 + \sqrt{3}}$

B.  $\frac{2}{3}$

C.  $\frac{3 + \sqrt{3}}{2}$

D.  $\frac{3}{2}$

**Answer: D**



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25.  $\tan \alpha = \frac{1}{7}$ ,  $\tan \beta = \frac{1}{3}$ , then  $\cos 2\alpha =$

A.  $\sin 2\beta$

B.  $\sin 4\beta$

C.  $\sin 3\beta$

D.  $\sin \beta$

**Answer: B**

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26. If  $\cos \theta = \frac{1}{2} \left( x + \frac{1}{x} \right)$  then  $\frac{1}{2} \left( x^2 + \frac{1}{x^2} \right) =$

A.  $\sin 2\theta$

B.  $\cos 2\theta$

C.  $\tan 2\theta$

D.  $\sec 2\theta$

**Answer: B**

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27. If  $\sin x + \cos x = \frac{1}{5}$  and  $0 \leq x \leq \pi$ , then  $\tan x$  is equal to

A.  $-\frac{4}{3}$

B.  $-\frac{3}{4}$

C.  $-\frac{2}{3}$

D.  $\frac{3}{2}$

**Answer: A**



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28. If  $0 < x < \pi$  and  $\cos x + \sin x = \frac{1}{2}$ , then  $\tan x$  is

A.  $\frac{1 - \sqrt{7}}{4}$

B.  $\frac{4 - \sqrt{7}}{3}$

C.  $-\frac{4 + \sqrt{7}}{3}$

D.  $\frac{\sqrt{7} + 1}{4}$

**Answer: C**



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29. If:  $\tan\left(\frac{\pi}{4} + \theta\right) - \tan\left(\frac{\pi}{4} - \theta\right) = m \cdot \tan(n\theta)$ , then

A.  $2 \tan 2\theta$

B.  $2 \cot 2\theta$

C.  $\tan 2\theta$

D.  $\cot 2\theta$

**Answer: A**



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30. If  $\sec 2\theta = p + \tan 2\theta$ , then the value of  $\sin^2 \theta$  in terms of  $p$  is

A.  $\frac{(p-1)^2}{2(p^2+1)}$

B.  $\frac{1}{2} \left( \frac{p-1}{p+1} \right)^2$

C.  $\frac{p^2-1}{2(p^2+1)}$

D.  $\frac{p^2-1}{2(P+1)^2}$

**Answer: A**



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31. If  $\theta$  and  $\phi$  are angles in first quadrant and  $\tan \theta = \frac{1}{7}$  and  $\sin \phi = \frac{1}{\sqrt{10}}$  then

A.  $\theta + 2\phi = 90^\circ$

B.  $\theta + 2\phi = 60^\circ$

C.  $\theta + 2\phi = 30^\circ$

D.  $\theta + 2\phi = 45^\circ$

**Answer: D**





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32. If  $\cos(\theta - \alpha) = a$  and  $\cos(\theta - \beta) = b$  then the value of  $\sin^2(\alpha - \beta) + 2ab \cos(\alpha - \beta)$

A.  $1 - a^2 - b^2$

B.  $a - 2a^2 - 2b^2$

C.  $2 + a^2 + b^2$

D.  $2 - a^2 - b^2$

Answer: B



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33. If  $\tan^2 \theta = 2 \tan^2 \varphi + 1$ , then  $\cos 2\theta + \sin^2 \varphi$  equals  $-1$  (b)  $0$  (c)  $1$  (d) none of these

A.  $-1$

B. 0

C. 1

D. 2

**Answer: B**



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34. If  $\tan \theta - \cot \theta = a$  and  $\sin \theta + \cos \theta = b(b^2 - 1)^2(a^2 + 4)$  is equal to

A. 2

B.  $-4$

C.  $\pm 4$

D. 4

**Answer: D**



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35. If  $\sin A \sin 2A = x$  and  $\cos A + \cos 2A = y$ , then  $(x^2 + y^2)(x^2 + y^2) =$

A.  $2y$

B.  $y$

C.  $3y$

D.  $4y$

**Answer: A**



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36.

If

$$\tan x = \frac{2b}{a - c}, a \neq c, y = a \cos^2 x + 2b \sin x \cdot \cos x + c \sin^2 x, z = a \sin^2 x$$

then

A.  $y = z$

B.  $y + z = a + c$

C.  $y - z = a + c$

D.  $y - z = (a - c)^2 + 4b^2$

**Answer: B**



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37.  $8 \cdot \sin\left(\frac{x}{8}\right) \cdot \cos\left(\frac{x}{2}\right) \cdot \cos\left(\frac{x}{4}\right) \cdot \cos\left(\frac{x}{8}\right) =$

A.  $8 \sin x$

B.  $\sin x$

C.  $\cos x$

D.  $8 \cos x$

**Answer: B**



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38. If  $x = \cos 10^\circ \cos 20^\circ \cos 40^\circ$ , then the value of  $x$  is

A.  $\frac{1}{4} \tan 10^\circ$

B.  $\frac{1}{8} \cos 10^\circ$

C.  $\frac{1}{8} \operatorname{cosec} 10^\circ$

D.  $\frac{1}{8} \sec 10^\circ$

**Answer: B**



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39. If  $\theta = \frac{\pi}{2^n + 1}$ , then

$\cos \theta \cos 2\theta \cos 2^2\theta \dots \cos 2^{n-1}\theta$  is equal to

A.  $\frac{1}{2^n}$

B.  $\cos \theta$

C. 2

D.  $2^n$

**Answer: A**



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40.  $\cos\left(\frac{\pi}{7}\right)\cos\left(\frac{2\pi}{7}\right)\cos\left(\frac{4\pi}{7}\right) =$

A. 0

B.  $\frac{1}{2}$

C.  $\frac{1}{4}$

D.  $-\frac{1}{8}$

**Answer: D**



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41. The value of  $\cos\frac{\pi}{5}\cos2\frac{\pi}{5}\cos4\frac{\pi}{5}\cos8\frac{\pi}{5} =$

A.  $\frac{1}{16}$

B. 0

C.  $\frac{-1}{8}$

D.  $\frac{-1}{16}$

**Answer: D**



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42. The value of  $\frac{1}{\sin 10^\circ} - \frac{\sqrt{3}}{\cos 10^\circ}$  is equal to

A. 1

B. 2

C. 4

D. 3

**Answer: C**



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43. If  $|\tan A| < 1$  and  $|A|$  is acute, then

$\frac{\sqrt{1 + \sin 2A} + \sqrt{1 - \sin 2A}}{\sqrt{1 + \sin 2A} - \sqrt{1 - \sin 2A}}$  is equal to

- A.  $\tan A$
- B.  $-\tan A$
- C.  $\cot A$
- D.  $-\cot A$

**Answer: C**



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44. If  $\tan x = \frac{b}{a}$  then  $\sqrt{\frac{a+b}{a-b}} + \sqrt{\frac{a-b}{a+b}} =$

- A.  $\frac{2 \sin x}{\sqrt{\sin 2x}}$
- B.  $\frac{2 \cos x}{\sqrt{\cos 2x}}$
- C.  $\frac{2 \cos x}{\sqrt{\sin 2x}}$



D.  $\frac{2 \sin x}{\sqrt{\cos 2x}}$

**Answer: B**



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45. Show that:  $\tan(60^\circ + \theta)\tan(60^\circ - \theta) = \frac{2 \cos 2\theta + 1}{2 \cos 2\theta - 1}$

A.  $\frac{2 \cos 2A + 1}{2 \cos 2A - 1}$

B.  $\frac{2 \cos 2A - 1}{2 \cos 2A + 1}$

C.  $\frac{\cos 2A + 21}{\cos 2A - 1}$

D.  $\frac{\cos 2A - 1}{\cos 2A + 21}$

**Answer: A**



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46. Maximum value of  $\sin^4 \theta + \cos^4 \theta$  is

A. 0, 2

B.  $1, \frac{1}{2}$

C.  $-1, 1$

D.  $1, -\frac{1}{2}$

**Answer: B**

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47. Let  $B = 2\sin^2 x - \cos 2x$ , then

A.  $-1 \leq B \leq 3$

B.  $0 \leq B \leq 2$

C.  $-1 \leq B \leq 1$

D.  $-2 \leq B \leq 2$

**Answer: A**

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48. If  $3 \sin 2\theta = 2 \sin 3\theta$  and  $0 < \theta < \pi$ , then  $\sin \theta =$

A. 0

B.  $\frac{\sqrt{15}}{4}$

C.  $-\frac{1}{4}$

D.  $\frac{1}{4}$

**Answer: B**



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49. If  $\sin 2A = \sin 3A$  and  $0 \leq A \leq 90^\circ$ , then A is equal to

A.  $45^\circ$

B.  $60^\circ$

C.  $0^\circ$  or  $36^\circ$

D.  $72^\circ$

**Answer: C**



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50. Solve that following equations :

$$\tan\theta + \tan\left(\theta + \frac{\pi}{3}\right) + \tan\left(\theta + \frac{2\pi}{3}\right) = 3$$

A.  $\tan 2\theta = 1$

B.  $\tan 3\theta = 1$

C.  $\tan^3 \theta = 1$

D.  $\tan^2 \theta = 1$

**Answer: B**



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51. If  $\sin \theta = -\frac{4}{5}$  and  $\theta$  lies in third quadrant, then the value of  $\cos\left(\frac{\theta}{2}\right)$  is

A.  $\frac{1}{\sqrt{5}}$

B.  $-\frac{1}{\sqrt{5}}$

C.  $\sqrt{\frac{2}{5}}$

D.  $-\sqrt{\frac{2}{5}}$

**Answer: B**



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52. If  $\sec \theta = 1\frac{1}{4}$ , then  $\tan \frac{\theta}{2} =$

A.  $\frac{1}{3}$

B.  $\frac{3}{4}$

C.  $\frac{1}{4}$

D.  $\frac{5}{4}$

**Answer: A**

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53. For  $f$  or  $A = 133^\circ$ ,  $2 \cos \frac{A}{2}$  is equal to

A.  $-\sqrt{1 + \sin A} - \sqrt{1 - \sin A}$

B.  $-\sqrt{1 + \sin A} + \sqrt{1 - \sin A}$

C.  $\sqrt{1 + \sin A} - \sqrt{1 - \sin A}$

D.  $\sqrt{1 + \sin A} + \sqrt{1 - \sin A}$

**Answer: C**

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54. If  $\cos \theta = \frac{3}{5}$  and  $\cos \phi = \frac{4}{5}$ , where  $\theta$  and  $\phi$  are positive acute angles, then  $\cos \frac{\theta - \phi}{2} =$

A.  $\frac{7}{\sqrt{2}}$

B.  $\frac{7}{5\sqrt{2}}$

C.  $\frac{7}{\sqrt{5}}$

D.  $\frac{7}{2\sqrt{5}}$

**Answer: B**



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55.  $(\cos \alpha + \cos \beta)^2 + (\sin \alpha + \sin \beta)^2 =$

A.  $4 \cos^2 \left( \frac{\alpha - \beta}{2} \right)$

B.  $4 \sin^2 \left( \frac{\alpha - \beta}{2} \right)$

C.  $4 \cos^2 \left( \frac{\alpha + \beta}{2} \right)$

$$D. 4 \sin^2 \left( \frac{\alpha + \beta}{2} \right)$$

**Answer: A**

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$$56. \frac{\sin 2A}{1 + \cos 2A} \cdot \frac{\cos A}{1 + \cos A} =$$

A.  $\tan \frac{A}{2}$

B.  $\cot \frac{A}{2}$

C.  $\sec \frac{A}{2}$

D.  $\operatorname{cosec} \frac{A}{2}$

**Answer: A**

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$$57. \frac{1 + \sin A - \cos A}{1 + \sin A + \cos A} =$$



A.  $\sin \frac{A}{2}$

B.  $\cos \frac{A}{2}$

C.  $\tan \frac{A}{2}$

D.  $\cot \frac{A}{2}$

**Answer: C**

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58.  $\frac{\tan A + \sec A - 1}{\tan A - \sec A + 1} = \frac{1 + \sin A}{\cos A}$

A.  $\frac{1 - \sin A}{\cos A}$

B.  $\frac{1 - \cos A}{\sin A}$

C.  $\frac{1 + \sin A}{\cos A}$

D.  $\frac{1 + \cos A}{\sin A}$

**Answer: C**

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59. If  $0 < \theta < \frac{\pi}{2}$  and  $\frac{y+1}{1-y} = \sqrt{\frac{1+\sin\theta}{1-\sin\theta}}$ , then  $y$  is equal to

A.  $\cot \frac{\theta}{2}$

B.  $\tan \frac{\theta}{2}$

C.  $\cot \frac{\theta}{2} + \tan \frac{\theta}{2}$

D.  $\cot \frac{\theta}{2} - \tan \frac{\theta}{2}$

**Answer: B**



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60. If  $\tan A$  &  $\tan B$  are the roots of the quadratic equation  $x^2 - ax + b = 0$ , then the value of  $\sin^2(A + B)$  is:

A.  $\frac{a^2}{a^2 + (1-b)^2}$

B.  $\frac{a^2}{a^2 + b^2}$

$$C. \frac{a^2}{(a+b)^2}$$

$$D. \frac{a^2}{b^2 + (1-a)^2}$$

**Answer: A**



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## Competitive Thinking

**1. Prove that**

$$(i) \cos \left( \frac{\pi}{4} + x \right) + \cos \left( \frac{\pi}{4} - x \right) = \sqrt{2} \cos x$$

$$(ii) \cos \left( \frac{3\pi}{4} + x \right) - \cos \left( \frac{3\pi}{4} - x \right) = -\sqrt{2} \sin x$$

A.  $\sqrt{2} \sin^2 x$

B.  $\sqrt{2} \sin x$

C.  $\sqrt{2} \cos^2 x$

D.  $\sqrt{2} \cos x$

**Answer: D**



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2. IF  $2 \sin\left(\theta + \frac{\pi}{3}\right) = \cos\left(\theta - \frac{\pi}{6}\right)$ , then  $\tan \theta =$

A.  $\sqrt{3}$

B.  $-\frac{1}{\sqrt{3}}$

C.  $\frac{1}{\sqrt{3}}$

D.  $-\sqrt{3}$

**Answer: D**



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3. The value of  $\cos 15^\circ - \sin 15^\circ$  is equal to

A.  $\frac{1}{\sqrt{2}}$

B.  $\frac{1}{2}$

C.  $-\frac{1}{\sqrt{2}}$

D. 0

**Answer: A**



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4. If  $\sin \theta = \frac{12}{13}$ ,  $\left(0 < \theta < \frac{\pi}{2}\right)$  and  $\cos \phi = -\frac{3}{5}$ ,  $\left(\pi < \phi < \frac{3\pi}{2}\right)$ .

Then,  $\sin(\theta + \phi)$  will be

A.  $\frac{-56}{61}$

B.  $\frac{-56}{65}$

C.  $\frac{1}{65}$

D.  $-56$

**Answer: B**



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5. If  $\frac{\pi}{2} < \alpha < \pi, \pi < \beta < 3\frac{\pi}{2}; \sin \alpha = \frac{15}{17}$  and  $\tan \beta = \frac{12}{5}$ , then the value of  $\sin(\beta - \alpha)$  is

A.  $\frac{-171}{221}$

B.  $\frac{21}{221}$

C.  $\frac{21}{221}$

D.  $\frac{171}{221}$

**Answer: D**

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6. If  $\tan(A + B) = p$  and  $\tan(A - B) = q$ , then write the value of  $\tan 2B$ .

A.  $\frac{p + q}{p - q}$

B.  $\frac{p - q}{1 + pq}$

C.  $\frac{p + q}{1 - pq}$

D.  $\frac{1 + pq}{1 - p}$

**Answer: C**



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7. If  $\cos(\alpha + \beta) = \frac{4}{5}$ ;  $\sin(\alpha - \beta) = \frac{5}{13}$  and  $\alpha, \beta$  lie between  $0$  &  $\frac{\pi}{4}$  then

find the value of  $\tan 2\alpha$

A.  $\frac{16}{63}$

B.  $\frac{56}{33}$

C.  $\frac{28}{33}$

D. None of these

**Answer: B**



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8. If  $\cos(A - B) = \frac{3}{5}$  and  $\tan A \tan B = 2$  then

A.  $\cos A \cos B = \frac{1}{5}$

B.  $\sin A \sin B = -\frac{2}{5}$

C.  $\cos A \cos B = -\frac{1}{5}$

D.  $\sin A \sin B = -\frac{1}{5}$

**Answer: A**



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9. If  $\sin \theta = 3 \sin(\theta + 2\alpha)$ , then the value of  $\tan(\theta + \alpha) + 2 \tan \alpha$  is

A. 3

B. 2

C. -1

D. 0



**Answer: D**



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10. If  $\tan\beta = \frac{n \sin \alpha \cos \alpha}{1 - n \sin^2 \alpha}$ , show that  $\tan(\alpha - \beta) = (1 - n)\tan\alpha$ .

A.  $n \tan \alpha$

B.  $(1 - n)\tan \alpha$

C.  $(1 + n)\tan \alpha$

D.  $\frac{\tan \alpha}{n}$

**Answer: B**



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11. If  $y = (1 + \tan A)(1 - \tan B)$ , where  $A - B = \frac{\pi}{4}$  then  $(y + 1)^{y+1}$  is equal to

A. 9

B. 4

C. 27

D. 81

**Answer: C**

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12.  $\cot\left(\frac{\pi}{4} + \theta\right)\cot\left(\frac{\pi}{4} - \theta\right)$  is

A. 0

B. -1

C. 1

D. -2

**Answer: C**

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13. A positive acute angle is divided into two parts whose tangents are

$\frac{1}{2}$  and  $\frac{1}{3}$ . Then the angle is

A.  $\frac{\pi}{4}$

B.  $\frac{\pi}{5}$

C.  $\frac{\pi}{3}$

D.  $\frac{\pi}{6}$

**Answer: A**



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14. If  $\cos P = \frac{1}{7}$  and  $\cos Q = \frac{13}{14}$ , where P and Q both are acute angles.

Then the value of P-Q is

A.  $30^\circ$

B.  $60^\circ$

C.  $45^\circ$

D.  $75^\circ$

**Answer: B**



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15. If  $\sin \alpha = \frac{1}{\sqrt{5}}$  and  $\sin \beta = \frac{3}{5}$ , then  $\beta - \alpha$  lies in

A.  $\left(0, \frac{\pi}{4}\right)$

B.  $\left(\frac{\pi}{2}, \frac{3\pi}{4}\right)$

C.  $[0, \pi]$

D.  $\left(\pi, \frac{5\pi}{4}\right)$

**Answer: A**



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16. if  $\tan \theta_1 = k \cot \theta_2$  then find  $\frac{\cos(\theta_1 - \theta_2)}{\cos(\theta_1 + \theta_2)} =$

A.  $\frac{1+k}{1-k}$

B.  $\frac{1-k}{1+k}$

C.  $\frac{k+1}{k-1}$

D.  $\frac{k-1}{k+1}$

**Answer: B**



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17.  $\frac{\cos 17^\circ + \sin 17^\circ}{\cos 17^\circ - \sin 17^\circ} =$

A.  $\tan 62^\circ$

B.  $\tan 56^\circ$

C.  $\tan 54^\circ$

D.  $\tan 73^\circ$

**Answer: A**



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**18. Prove that**

$$\frac{\cos 9^\circ + \sin 9^\circ}{\cos 9^\circ - \sin 9^\circ} = \tan 54^\circ$$

A.  $\tan 54^\circ$

B.  $\tan 36^\circ$

C.  $\tan 18^\circ$

D.  $\tan 73^\circ$

**Answer: A**



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**19. If  $\tan \theta = \frac{\sin \alpha - \cos \alpha}{\sin \alpha + \cos \alpha}$ , then**

A.  $\sqrt{2} \cos \theta, \sqrt{2} \sin \theta$

B.  $-\sqrt{2} \sin \theta, -\sqrt{2} \cos \theta$

C.  $\sqrt{2} \sin \theta, \sqrt{2} \sin \theta$

D.  $\sqrt{2} \cos \theta, \sqrt{2} \cos \theta$

**Answer: A**

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20.  $\cos^2 45^\circ - \sin^2 15^\circ =$

A.  $\frac{\sqrt{3}}{2}$

B.  $\frac{\sqrt{3}}{4}$

C.  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$

D.  $\frac{\sqrt{3} - 1}{2\sqrt{2}}$

**Answer: B**

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21. The value of  $\cos^2\left(\frac{\pi}{6} + \theta\right) - \sin^2\left(\frac{\pi}{6} - \theta\right)$  is

A.  $\frac{1}{2} \cos 2\theta$

B. 0

C.  $-\frac{1}{2} \cos 2\theta$

D.  $\frac{1}{2}$

**Answer: A**



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22. The maximum value of  $\sin\left(\theta + \frac{\pi}{6}\right) + \cos\left(\theta + \frac{\pi}{6}\right)$  is attained at

$\theta \in \left(0, \frac{\pi}{2}\right)$

A.  $x = \frac{\pi}{3}$

B.  $x = \frac{\pi}{12}$

C.  $x = \frac{\pi}{6}$



$$D. x = \frac{\pi}{2}$$

**Answer: B**



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**23.** What is the value of  $\sin 15^\circ$  ?

A.  $\frac{\sqrt{3} - 1}{2\sqrt{2}}$

B.  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$

C.  $\frac{1 - \sqrt{3}}{2\sqrt{2}}$

D.  $\frac{1 + \sqrt{3}}{\sqrt{2}}$

**Answer: A**



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**24.**  $\sin 75^\circ =$

A.  $\frac{2 - \sqrt{3}}{2}$

B.  $\frac{\sqrt{3} + 1}{2\sqrt{2}}$

C.  $\frac{\sqrt{3} - 1}{-2\sqrt{2}}$

D.  $\frac{\sqrt{3} - 1}{2\sqrt{2}}$

**Answer: B**



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25.  $\sin 765^\circ$

A. 1

B. 0

C.  $\frac{\sqrt{3}}{2}$

D.  $\frac{1}{\sqrt{2}}$

**Answer: D**



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26. The value of  $\tan\theta \sin\left(\frac{\pi}{2} + \theta\right) \cos\left(\frac{\pi}{2} - \theta\right)$  is -1 b. 1 c.  $\frac{1}{2}\sin 2\theta$  d.

none of these

A. 1

B. 0

C.  $\cos^2 \theta$

D.  $\sin^2 \theta$

**Answer: D**



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27.  $\cot(45 + \theta)\cot(45 - \theta) =$

A. -1

B. 0

C. 1

D.  $\infty$

**Answer: C**



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28.  $\tan 75^\circ - \cot 75^\circ =$

A.  $2\sqrt{3}$

B.  $2 + \sqrt{3}$

C.  $2 - \sqrt{3}$

D.  $-2\sqrt{3}$

**Answer: A**



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29. Prove that  $\tan 70^\circ = \tan 20^\circ + 2\tan 50^\circ$

A.  $\tan 20^\circ + \tan 50^\circ$

B.  $\tan 20^\circ + \tan 50^\circ$

C.  $\tan 20^\circ + 2\tan 50^\circ$

D.  $2\tan 20^\circ + 2\tan 50^\circ$

**Answer: C**

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**30.**  $\sec 50^\circ + \tan 50^\circ$  is equal to

A.  $\tan 20^\circ + \tan 50^\circ$

B.  $2\tan 20^\circ + 2\tan 50^\circ$

C.  $\tan 20^\circ + 2\tan 50^\circ$

D.  $2\tan 20^\circ + 2\tan 50^\circ$

**Answer: C**

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31. If  $2 \sec 2\alpha = \tan \beta + \cot \beta$ , then one of the values of  $\alpha + \beta$  is

A.  $\frac{\pi}{4}$

B.  $\frac{\pi}{2}$

C.  $\pi$

D.  $2\pi$

**Answer: A**



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32. The value of  $\sin(\pi + \theta)\sin(\pi - \theta)\cos ec^2\theta$  is equal to

A. 1

B. -1

C.  $\sin \theta$

D.  $-\sin \theta$

**Answer: B**



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**33.** If  $A, B, C, D$  are angles of a cyclic quadrilateral, then prove that

$$\cos A + \cos B + \cos C + \cos D = 0$$

A.  $2(\cos A + \cos C)$

B.  $2(\cos A + \cos B)$

C.  $2(\cos A + \cos D)$

D. 0

**Answer: D**



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34. The value of  $\cos(270^\circ + \theta)\cos(90^\circ + \theta) - \sin(270^\circ - \theta)\cos \theta$  is

A. 0

B.  $-1$

C.  $\frac{1}{2}$

D. 1

**Answer: D**



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35. If  $A = \frac{\pi}{2}$ ,  $\cos A + \sin(270^\circ - A) + \cos(180^\circ + A) =$

A.  $-1$

B. 0

C. 1

D.  $\frac{1}{2}$



**Answer: B**



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36.  $\tan A + \cot(180^\circ + A) + \cot(90^\circ + A) + \cot(360^\circ - A) =$

A. 0

B.  $2 \tan A$

C.  $2 \cot A$

D.  $2(\tan A - \cot A)$

**Answer: A**



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37. The value of

$\sin 1^\circ + \sin 2^\circ + \dots + \sin 359^\circ$  is equal to

A. 1

B. 180

C. 0

D.  $-1$

**Answer: C**



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**38.** The value of

$\sin 600^\circ \cos 330^\circ + \cos 120^\circ \sin 150^\circ$  is

A.  $-1$

B. 1

C.  $\frac{1}{\sqrt{2}}$

D.  $\frac{\sqrt{3}}{2}$

**Answer: A**

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39. At  $x = \frac{5\pi}{6}$ , the value of  $2 \sin 3x + 3 \cos 3x$  is

- A. 0
- B. 1
- C.  $-1$
- D. None of these

**Answer: D**

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40.  $\frac{1 - \tan 2^\circ \cot 62^\circ}{\tan 152^\circ - \cot 88^\circ} =$

- A.  $\sqrt{3}$
- B.  $-\sqrt{3}$
- C.  $\sqrt{2} - 1$

D.  $1 - \sqrt{2}$

**Answer: B**



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41.  $\frac{\cos 12^\circ - \sin 12^\circ}{\cos 12^\circ + \sin 12^\circ} + \frac{\sin 147^\circ}{\cos 147^\circ} =$

A. 1

B. -1

C. 0

D.  $\sqrt{3}$

**Answer: C**



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42. If  $\tan 20^\circ = \lambda$ , then  $\frac{\tan 160^\circ - \tan 110^\circ}{1 + (\tan 160^\circ)(\tan 110^\circ)} =$

A.  $\frac{1 + \lambda^2}{2\lambda}$

B.  $\frac{1 + \lambda^2}{\lambda}$

C.  $\frac{1 - \lambda^2}{\lambda}$

D.  $\frac{1 - \lambda^2}{2\lambda}$

**Answer: D**

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**43.**  $\sin^2 17.5^\circ + \sin^2 72.5^\circ$  is equal to

A.  $\cos^2 90^\circ$

B.  $\tan^2 45^\circ$

C.  $\cos^2 30^\circ$

D.  $\sin^2 45^\circ$

**Answer: B**

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44. Find the value of the expression

$$3 \left[ \sin^4 \left( \frac{3\pi}{2} - \alpha \right) + \sin^4 (3\pi + \alpha) \right] - 2 \left[ \sin^6 \left( \frac{\pi}{2} + \alpha \right) + \sin^6 (5\pi - \alpha) \right]$$

A. 0

B. 1

C. 3

D.  $\sin 4\alpha + \sin 6\alpha$

**Answer: B**



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45.  $\sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \dots + \sin^2 85^\circ + \sin^2 90^\circ =$

A. 7

B. 8

C. 9

D.  $9\frac{1}{2}$

**Answer: D**



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**46.**  $\cos 15^\circ$

A.  $\sqrt{\frac{1 + \cos 30^\circ}{2}}$

B.  $\sqrt{\frac{1 - \cos 30^\circ}{2}}$

C.  $\pm \sqrt{\frac{1 + \cos 30^\circ}{2}}$

D.  $\pm \sqrt{\frac{1 - \cos 30^\circ}{2}}$

**Answer: A**



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47. Which one of the following number (s) is/are rational?

A.  $\sin 15^\circ$

B.  $\cos 15^\circ$

C.  $\sin 15^\circ \cos 15^\circ$

D.  $\sin 15^\circ \cos 75^\circ$

Answer: C



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48. The value of  $\frac{1}{8}(3 - 4 \cos 2\theta + \cos 4\theta)$  is

A.  $\cos 4\theta$

B.  $\sin 4\theta$

C.  $\sin^4 \theta$

D.  $\cos^4 \theta$



**Answer: C**



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49. If  $0 < x < \frac{\pi}{4}$ , then  $\sec 2x - \tan 2x =$

A.  $\tan\left(x - \frac{\pi}{4}\right)$

B.  $\tan\left(\frac{\pi}{4} - x\right)$

C.  $\tan\left(x + \frac{\pi}{4}\right)$

D.  $\tan^2\left(x + \frac{\pi}{4}\right)$

**Answer: B**



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50.  $\sqrt{3} \csc 20^\circ - \sec 20^\circ =$

$$\frac{\sqrt{3}}{\sin(20^\circ)} - \frac{1}{\cos(20^\circ)} =$$

A. 2

B.  $\frac{2\sin 20^\circ}{\sin 40^\circ}$

C. 4

D.  $\frac{4\sin 20^\circ}{\sin 40^\circ}$

**Answer: C**

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51. The value of  $\tan(1^\circ) + \tan(89^\circ)$  is

A.  $\frac{2}{\sin(1^\circ)}$

B.  $\frac{1}{\sin(1^\circ)}$

C.  $\frac{1}{\sin(2^\circ)}$

D.  $\frac{2}{\sin(2^\circ)}$

**Answer: D**

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52. If  $\cot \frac{2x}{3} + \tan\left(\frac{x}{3}\right) = \sec \frac{kx}{3}$ , then the value of  $k$  is

- A. 1
- B. 2
- C. 3
- D. -1

**Answer: B**



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53. If  $2 \sin^2\left(\left(\frac{\pi}{2}\right)\cos^2 x\right) = 1 - \cos(\pi \sin 2x)$ ,  $x \neq (2n + 1)\pi/2$ ,  $n \in I$ ,

then  $\cos 2x$  is equal to

- A.  $\frac{1}{5}$
- B.  $\frac{3}{5}$
- C.  $\frac{4}{5}$

D. 1

**Answer: B**



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54. If  $8 \cos 2\theta + 8 \sec 2\theta = 65, 0 < \theta < \frac{\pi}{2}$ , then the value of  $4 \cos 4\theta$  is equal to

A.  $-\frac{33}{8}$

B.  $-\frac{31}{8}$

C.  $-\frac{31}{32}$

D.  $-\frac{33}{32}$

**Answer: B**



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55. If  $5(\tan^2 x - \cos^2 x) = 2 \cos 2x + 9$ , then the value of  $\cos 4x$  is

A.  $-\frac{7}{9}$

B.  $-\frac{3}{5}$

C.  $\frac{1}{3}$

D.  $\frac{2}{9}$

**Answer: A**



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56.  $x + \frac{1}{x} = 2 \cos \alpha$  then  $x^n + \frac{1}{x^n} =$

A.  $2^n \cos \alpha$

B.  $2^n \cos n\alpha$

C.  $2i \sin n\alpha$

D.  $2 \cos n\alpha$

**Answer: D**



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57. If  $\sin x + \cos x = \frac{1}{5}$ , then  $\tan 2x$  is

A.  $\frac{25}{17}$

B.  $\frac{7}{26}$

C.  $\frac{25}{7}$

D.  $\frac{24}{7}$

**Answer: D**



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58. If  $A$  lies in the third quadrant and  $3 \tan A - 4 = 0$ , then  $5 \sin 2A + 3 \sin A + 4 \cos A$  is equal to

A. 0

B.  $\frac{-24}{5}$

C.  $\frac{24}{5}$

D.  $\frac{48}{5}$

**Answer: A**



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59. If  $a \tan \theta = b$ , then  $a \cos 2\theta + b \sin 2\theta =$

A.  $a$

B.  $b$

C.  $-a$

D.  $-b$

**Answer: A**



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60. If  $a \cos 2\theta + b \sin 2\theta = c$  has  $\alpha$  and  $\beta$  as its solution, then the value of  $\tan \alpha + \tan \beta$  is

A.  $\frac{c + a}{2b}$

B.  $\frac{2b}{c + a}$

C.  $\frac{c - a}{2b}$

D.  $\frac{b}{c + a}$

**Answer: B**



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61. If  $\alpha, \beta$  are solutin of  $6 \cos \theta + 8 \sin \theta = 9$ , then  $\sin(\alpha + \beta) =$

A.  $\frac{3}{5}$

B.  $\frac{4}{5}$

C.  $\frac{24}{25}$



D.  $\frac{12}{13}$

**Answer: C**



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62. If  $\alpha$  is a root of  $25 \cos^2 \theta + 5 \cos \theta - 12 = 0$ ,  $\frac{\pi}{2} < \alpha < \pi$  the  $\sin 2\alpha$  is equal to:

A.  $\frac{24}{25}$

B.  $\frac{-24}{25}$

C.  $\frac{13}{18}$

D.  $\frac{-13}{18}$

**Answer: B**



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63.  $2 \cos^2 \theta - 2 \sin^2 \theta = 1$ , then  $\theta =$

A.  $15^\circ$

B.  $30^\circ$

C.  $45^\circ$

D.  $60^\circ$

**Answer: B**



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64.  $2 \sin A \cos^3 A - 2 \sin^3 A \cos A =$

A.  $\sin 4A$

B.  $\frac{1}{2} \sin 4A$

C.  $\frac{1}{4} \sin 4A$

D.  $\frac{1}{8} \sin 4A$

**Answer: B**



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$$65. \sin^4 \frac{\pi}{8} + \sin^4 \frac{3\pi}{8} + \sin^4 \frac{5\pi}{8} + \sin^4 \frac{7\pi}{8} =$$

A.  $\frac{1}{2}$

B.  $\frac{1}{4}$

C.  $\frac{2}{3}$

D.  $\frac{3}{4}$

**Answer: C**



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$$66. 3(\sin x - \cos x)^4 + 6(\sin x + \cos x)^2 + 4(\sin^6 x + \cos^6 x) =$$

A. 14

B. 11

C. 12

D. 13

**Answer: D**



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67. If  $\sin 2\theta + \sin 2\phi = \frac{1}{2}$  and  $\cos 2\theta + \cos 2\phi = \frac{3}{2}$ , then  $\cos^2(\theta - \phi) =$

A.  $\frac{3}{8}$

B.  $\frac{5}{8}$

C.  $\frac{3}{4}$

D.  $\frac{5}{4}$

**Answer: B**



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68. If  $n = 1, 2, 3, \dots$ , then  $\cos \alpha \cos 2\alpha \cos 4\alpha \dots \cos 2^{n-1}\alpha$  is equal to

A.  $\frac{\sin 2n\alpha}{2n \sinh \alpha}$

B.  $\frac{\sin 2^n \alpha}{2^n \sin 2^{n-1} \alpha}$

C.  $\frac{\sin 4^{n-1} \alpha}{4^{n-1} \sin \alpha}$

D.  $\frac{\sin 2^n \alpha}{2^n \sin \alpha}$

**Answer: D**



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69.  $\cos \frac{2\pi}{15} \cos \frac{4\pi}{15} \cos \frac{8\pi}{15} \cos \frac{16\pi}{15} =$

A.  $\frac{1}{2}$

B.  $\frac{1}{4}$

C.  $\frac{1}{8}$

D.  $\frac{1}{16}$

**Answer: D**



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70. If  $K = \sin\left(\frac{\pi}{18}\right)\sin\left(\frac{5\pi}{18}\right)\sin\left(\frac{7\pi}{18}\right)$ , then the numerical value of  $K$  is \_\_\_\_\_

A.  $\frac{1}{4}$

B.  $\frac{1}{8}$

C.  $\frac{1}{16}$

D.  $\frac{1}{32}$

**Answer: B**



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71. The value of  $\frac{\sin \pi}{14} \frac{\sin(3\pi)}{14} \frac{\sin(5\pi)}{14} \frac{\sin(7\pi)}{14} \frac{\sin(9\pi)}{14} \frac{\sin(11\pi)}{14} \frac{\sin(13\pi)}{14}$  is equal to \_\_\_\_\_

A.  $\frac{1}{8}$

B.  $\frac{1}{16}$

C.  $\frac{1}{32}$

D.  $\frac{1}{64}$

**Answer: D**



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72. The value of  $\sin \frac{31}{3}\pi$  is

A.  $\frac{\sqrt{3}}{2}$

B.  $\frac{1}{\sqrt{2}}$

C.  $\frac{-\sqrt{3}}{2}$

D.  $\frac{-1}{\sqrt{2}}$

**Answer: A**



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73. Find the value  $\tan\left(\frac{\pi}{5}\right) + 2 \tan\left(\frac{2\pi}{5}\right) + 4 \cot\left(\frac{4\pi}{5}\right)$ .

A.  $\cot \frac{\pi}{51}$

B.  $\cot \frac{2\pi}{5}$

C.  $\cot \frac{4\pi}{5}$

D.  $\cot \frac{3\pi}{5}$

**Answer: A**



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74. The value of  $\frac{\cot x - \tan x}{\cot 2x}$  is



A. 1

B. 2

C. -1

D. 4

**Answer: B**

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75.  $\frac{\sec 8A - 1}{\sec 4A - 1} =$

A.  $\frac{\tan 2A}{\tan 8A}$

B.  $\frac{\tan 8A}{\tan 2A}$

C.  $\frac{\cot 8A}{\cot 2A}$

D.  $\frac{\tan 6A}{\tan 2A}$

**Answer: B**

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76. If  $2 \tan A = 3 \tan B$ , then  $\frac{\sin 2B}{5 - \cos 2B}$  is equal to

A.  $\tan A - \tan B$

B.  $\tan(A - B)$

C.  $\tan(A + B)$

D.  $\tan(A + 2B)$

**Answer: B**



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77.  $\cos 2\alpha = \frac{3 \cos 2\beta - 1}{3 - \cos 2\beta}$ , then  $\tan \alpha =$

A.  $\sqrt{2} \tan \beta$

B.  $\frac{\tan \beta}{\sqrt{2}}$

C.  $\frac{\tan^2 \beta}{\sqrt{2}}$

D.  $\tan \beta$

**Answer: A**



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78. If  $\cos \theta = \frac{1}{2} \left( a + \frac{1}{a} \right)$ , then the value of  $\cos 3\theta$  is

A.  $\frac{1}{8} \left( a^3 + \frac{1}{a^3} \right)$

B.  $\frac{3}{2} \left( a + \frac{1}{a} \right)$

C.  $\frac{1}{2} \left( a^3 + \frac{1}{a^3} \right)$

D.  $\frac{1}{3} \left( a^3 + \frac{1}{a^3} \right)$

**Answer: C**



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79.  $\cos^3 110^\circ + \cos^3 10^\circ + \cos^3 130^\circ =$

A.  $\frac{3}{4}$

B.  $\frac{3}{8}$

C.  $\frac{3\sqrt{3}}{8}$

D.  $\frac{3\sqrt{3}}{4}$

**Answer: C**



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**80.** If  $\sin 6\theta = 32 \cos^2 \theta \sin \theta - 32 \cos^3 \theta \sin \theta + 3x$ , then  $x =$

A.  $\cos \theta$

B.  $\cos 2\theta$

C.  $\sin \theta$

D.  $\sin 2\theta$

**Answer: D**



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81.  $\tan\left(\frac{\pi}{4} + \frac{\theta}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\theta}{2}\right)$  is equal to

A.  $\sec \theta$

B.  $2 \sec \theta$

C.  $\sec \frac{\theta}{2}$

D.  $\sin \theta$

**Answer: B**



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82. If  $\tan x = \frac{3}{4}$ ,  $\pi < x < \frac{3\pi}{2}$ , then the value of  $\cos \frac{x}{2}$  is

A.  $-\frac{1}{\sqrt{10}}$

B.  $\frac{3}{\sqrt{10}}$

C.  $\frac{1}{\sqrt{10}}$

D.  $-\frac{3}{\sqrt{10}}$

**Answer: A**



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83. If  $90^\circ < A < 180^\circ$  and  $\sin A = \frac{4}{5}$ , then  $\tan \frac{A}{2}$  is equal to

A.  $\frac{1}{2}$

B.  $\frac{3}{5}$

C.  $\frac{3}{2}$

D. 2

**Answer: D**



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84. If  $\theta$  is an acute angle and  $\sin\left(\frac{\theta}{2}\right) = \sqrt{\frac{x-1}{2x}}$ , then  $\tan \theta$  is equal to

A.  $x^2 - 1$

B.  $\sqrt{x^2 - 1}$

C.  $\sqrt{x^2 + 1}$

D.  $x^2 + 1$

**Answer: B**



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85. If  $\tan\left(\frac{x}{2}\right) = \cos ecx - \sin x$  then the value of  $\tan^2\left(\frac{x}{2}\right)$  is

A.  $2 - \sqrt{5}$

B.  $\sqrt{5} - 2$

C.  $\sqrt{5} + 2$

D.  $9 - 4\sqrt{5}$

**Answer: B**



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86. If  $\cos \theta = \frac{\cos \alpha - \cos \beta}{1 - \cos \alpha \cos \beta}$ , then one of the values of  $\tan\left(\frac{\theta}{2}\right)$  is

A.  $\cot \frac{\beta}{2} \tan \frac{\alpha}{2}$

B.  $\tan \alpha \tan \frac{\beta}{2}$

C.  $\tan \frac{\beta}{2} \cot \frac{\alpha}{2}$

D.  $\tan^2 \frac{\alpha}{2} \tan^2 \frac{\beta}{2}$

**Answer: A**



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87. If  $\theta \in \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$ , then the value of

$\sqrt{4 \cos^4 \theta + \sin^2 2\theta} + 4 \cot \theta \cos^2\left(\frac{\pi}{4} + \frac{\theta}{2}\right)$  is

A.  $-2 \cot \theta$

B.  $2 \cot \theta$



C.  $2 \cos \theta$

D.  $2 \sin \theta$

**Answer: B**



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88.  $(m + 2)\sin \theta + (2m - 1)\cos \theta = 2m + 1$  then  $\tan \theta$  is

A.  $\frac{4}{3}$  or  $\frac{2m}{m^2 - 1}$

B.  $\frac{3}{4}$  or  $\frac{2m}{m^2 + 1}$

C.  $\frac{4}{3}$  or  $\frac{2m + 1}{m^2}$

D.  $\frac{3}{4}$  or  $\frac{m^2}{2m + 1}$

**Answer: A**



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89. Given that  $\cos\left(\frac{\alpha - \beta}{2}\right) = 2 \cos\left(\frac{\alpha + \beta}{2}\right)$ , then  $\tan \frac{\alpha}{2} \tan \frac{\beta}{2}$  is equal to

A.  $\frac{1}{2}$

B.  $\frac{1}{3}$

C.  $\frac{1}{4}$

D.  $\frac{1}{8}$

**Answer: B**



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90. What is  $\tan\left(7\frac{1}{2}\right)^\circ$  equal to ?

A.  $\sqrt{6} + \sqrt{3} + \sqrt{2} - 2$

B.  $\sqrt{6} - \sqrt{2} + \sqrt{2} - 2$

C.  $\sqrt{6} + \sqrt{3} + \sqrt{2} - 2$

D.  $\sqrt{6} - \sqrt{3} - \sqrt{2} - 2$

**Answer: B**



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91.  $\sqrt{2} + \sqrt{3} + \sqrt{4} + \sqrt{6}$  is equal to

A.  $\cot\left(7\frac{1}{2}\right)^\circ$

B.  $\text{si}\left(7\frac{1}{2}\right)^\circ$

C.  $\sin 15^\circ$

D.  $\cos 15^\circ$

**Answer: A**



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92. If  $\alpha = 22^\circ 30'$ , then  $(1 + \cos \alpha)(1 + \cos 3\alpha)(1 + \cos 5\alpha)(1 + \cos 7\alpha)$  equals

A.  $\frac{1}{8}$

B.  $\frac{1}{4}$

C.  $\frac{1 + \sqrt{2}}{2\sqrt{2}}$

D.  $\frac{\sqrt{2} - 1}{\sqrt{2} + 1}$

**Answer: A**



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93. If  $\tan A = \frac{1 - \cos B}{\sin B}$ , then  $\tan 2A$  is equal to

A.  $\tan B$

B.  $\tan^2 B$

C.  $\tan^2 B + 2 \tan B$

D.  $\tan B + 2 \tan B$

**Answer: A**



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94. If  $\cos ec\theta = \frac{p+q}{p-q}$ , then  $\cot(\pi/4 + \theta/2) =$

A.  $\sqrt{\frac{p}{q}}$

B.  $\sqrt{\frac{q}{p}}$

C.  $\sqrt{pq}$

D.  $pq$

**Answer: B**



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95.  $\frac{\sqrt{2} - \sin \alpha - \cos \alpha}{\sin \alpha - \cos \alpha} =$

A.  $\sec\left(\frac{\alpha}{2} - \frac{\pi}{8}\right)$

B.  $\cos\left(\frac{\pi}{8} - \frac{\alpha}{2}\right)$

C.  $\tan\left(\frac{\alpha}{2} - \frac{\pi}{8}\right)$

D.  $\cot\left(\frac{\alpha}{2} - \frac{\pi}{2}\right)$

**Answer: C**



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96.  $\cos 2(\theta + \phi) + 4 \cos(\theta + \phi) \sin \theta \sin \phi + 2 \sin^2 \phi =$

A.  $\cos 2\theta$

B.  $\cos 3\theta$

C.  $\sin 2\theta$

D.  $\sin 3\theta$

**Answer: A**



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97. If  $\sin \theta + \sin \phi = a$  and  $\cos \theta + \cos \phi = b$ , find the value of  $\tan\left(\frac{\theta - \phi}{2}\right)$

A.  $\sqrt{\frac{a^2 + b^2}{4 - a^2 - b^2}}$

B.  $\sqrt{\frac{4 - a^2 - b^2}{a^2 + b^2}}$

C.  $\sqrt{\frac{a^2 + b^2}{4 + a^2 + b^2}}$

D.  $\sqrt{\frac{4 + a^2 + b^2}{a^2 + b^2}}$

**Answer: B**



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98. The value of expression

$$\frac{1 + \sin 2\alpha}{\cos(2\alpha - 2\pi)\tan\left(\alpha - \frac{3\pi}{4}\right)} - \frac{1}{2}\sin 2\alpha \left( \cot \frac{\alpha}{2} + \cot \left( \frac{3\pi}{2} + \frac{\alpha}{2} \right) \right) \text{ is}$$

A. 0

B. 1

C.  $\sin^2 \frac{\alpha}{2}$

D.  $\sin^2 \alpha$

**Answer: D**



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99. Let  $f: (-1, 1) \rightarrow \mathbb{R}$  be such that  $f(\cos 4\theta) = \frac{2}{2 - \sec^2 \theta}$  for  $\theta \in \left(0, \frac{\pi}{4}\right) \cup \left(\frac{\pi}{4}, \frac{\pi}{2}\right)$ . Then the value(s) of  $f\left(\frac{1}{3}\right)$  is/are

A.  $1 \pm \sqrt{\frac{3}{2}}$

B.  $1 \pm \sqrt{\frac{2}{3}}$

C.  $1 \pm \sqrt{\frac{1}{3}}$

D.  $1 \pm \sqrt{\frac{1}{2}}$

**Answer: A**



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100.

Let

$$f_n(\Theta) = \left( \tan\left(\frac{\Theta}{2}\right) \right) (1 + \sec(\Theta))(1 + \sec(2\Theta)) \dots (1 + \sec(2^n \Theta))..$$

then

A.  $f_2\left(\frac{\pi}{16}\right) = 1$

B.  $f_3\left(\frac{\pi}{32}\right) = 1$

C.  $f_4\left(\frac{\pi}{64}\right) = 1$

D.  $f_5\left(\frac{\pi}{128}\right) = -1$

**Answer: D**

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101. The sum of the series  $\sum_{n=1}^{\infty} \sin\left(\frac{n! \pi}{720}\right)$  is

A.  $\sin\left(\frac{\pi}{180}\right) + \sin\left(\frac{\pi}{360}\right) + \sin\left(\frac{\pi}{540}\right)$

B.  $\sin\left(\frac{\pi}{6}\right) + \sin\left(\frac{\pi}{30}\right) + \sin\left(\frac{\pi}{120}\right) + \sin\left(\frac{\pi}{360}\right)$

C.  $\sin\left(\frac{\pi}{6}\right) + \sin\left(\frac{\pi}{30}\right) + \sin\left(\frac{\pi}{120}\right) + \sin\left(\frac{\pi}{360}\right) + \sin\left(\frac{\pi}{720}\right)$

$$D. \sin\left(\frac{\pi}{180}\right) + \sin\left(\frac{\pi}{360}\right)$$

**Answer: C**



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## Evaluation Test

1. If  $x \cos \theta = y \cos\left(\theta + \frac{2\pi}{3}\right) = z \cos\left(\theta + \frac{4\pi}{3}\right)$ , then write the value of  $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$ .

A. 1

B. 2

C. 0

D.  $3 \cos \theta$

**Answer: C**



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2.  $\tan 70^\circ - \tan 20^\circ - 2\tan 40^\circ =$

A.  $2\tan 20^\circ$

B.  $\tan 40^\circ$

C.  $4\tan 10^\circ$

D.  $\tan 10^\circ$

**Answer: C**



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3. If  $\sqrt{x} + \frac{1}{\sqrt{x}} = 2 \cos \theta$ , then  $x^6 + x^{-6} =$

A.  $2 \cos 6\theta$

B.  $2 \cos 12\theta$

C.  $2 \cos 3\theta$

D.  $2 \sin 3\theta$

**Answer: B**



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**4.** The value of

$\cos^3 \theta + \cos^3(\theta + 120^\circ) + \cos^3(\theta - 120^\circ)$  is

A.  $\frac{\sqrt{3}}{2} \cos 3\theta$

B.  $\frac{3}{4} \sec^3 \theta$

C.  $\frac{3}{2} \tan^3 \theta$

D.  $\frac{3}{4} \cos 3\theta$

**Answer: D**



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**5.** If  $\tan \alpha = \frac{1}{5}$ ,  $\tan \beta = \frac{1}{239}$ , then the value of  $\tan(4\alpha - \beta)$  is

A. 0

B.  $-1$

C. 1

D. None of these

**Answer: C**



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6. Suppose  $\theta$  and  $\phi (\neq 0)$  are such that  $\sec(\theta + \phi)$ ,  $\sec \theta$  and  $\sec(\theta - \phi)$  are in A.P. If  $\cos \theta = k \cos\left(\frac{\phi}{2}\right)$  for some  $k$ , then  $k$  is equal to

A.  $\pm 1$

B.  $\pm 2$

C.  $\pm \sqrt{2}$

D.  $\pm \frac{1}{\sqrt{2}}$

**Answer: C**



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7. The maximum value of the expression  $\frac{1}{\sin^2 \theta + 3 \sin \theta \cos \theta + 5 \cos^2 \theta}$  is.....

A. 2

B. 3

C. 4

D. 6

**Answer: A**



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8. Let  $\alpha, \beta$  be such that it  $\pi < \alpha - \beta < 3\pi$ . if  $\sin \alpha + \sin \beta = -\frac{21}{65}$  and  $\cos \alpha + \cos \beta = -\frac{27}{65}$  then the value of  $\cos\left(\frac{\alpha - \beta}{2}\right)$  is

A.  $-\frac{6}{65}$

B.  $\frac{3}{\sqrt{130}}$

C.  $\frac{6}{65}$

D.  $-(3)\sqrt{130}$

**Answer: D**

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9. If  $\tan \alpha = (1 + 2^{-x})^{-1}$ ,  $\tan \beta = (1 + 2^{x+1})^{-1}$  then  $\alpha + \beta$  equals

A.  $\frac{\pi}{6}$

B.  $\frac{\pi}{4}$

C.  $\frac{\pi}{3}$

D.  $\frac{\pi}{2}$

**Answer: B**

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10. A and B are positive acute angles satisfying the equation

$$3 \cos^2 A + 2 \cos^2 B = 4, \frac{3 \sin A}{\sin B} = \frac{2 \cos B}{\cos A} \text{ then } A + 2B \text{ is}$$

A.  $\frac{\pi}{3}$

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{6}$

D.  $\frac{\pi}{4}$

**Answer: B**



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11. If  $\frac{\sin^4 A}{a} + \frac{\cos^4 A}{b} = \frac{1}{a+b}$ , then the value of  $\frac{\sin^8 A}{a^3} + \frac{\cos^8 A}{b^3}$  is equal to (A)  $\frac{1}{(a+b)^3}$  (B)  $\frac{a^3 b^3}{(a+b)^3}$  (C)  $\frac{a^2 b^2}{(a+b)^2}$  (D) none of these

A.  $\frac{1}{(a+b)^3}$

B.  $\frac{a^3 b^3}{(a+b)^3}$



C.  $\frac{a^2b^2}{(a+b)^2}$

D. None of these

**Answer: A**



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12. If  $\sin(\pi \cos \theta) = \cos(\pi \sin \theta)$ , then of the value  $\cos\left(\theta \pm \frac{\pi}{4}\right)$  is

A.  $\sqrt{2}$

B.  $\frac{1}{\sqrt{2}}$

C.  $-\frac{1}{2\sqrt{2}}$

D.  $\frac{1}{2\sqrt{2}}$

**Answer: D**



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