



## MATHS

### BOOKS - TARGET MATHS (HINGLISH)

## VECTORS

#### Classical Thinking

1. If  $\vec{a} = \hat{i} - \hat{j}$  and  $\vec{b} = -2\hat{i} + m\hat{j}$  are two collinear vectors, then  $m =$

A. 4

B. 3

C. 2

D.  $\frac{1}{2}$

**Answer: C**



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2. The vectors  $\vec{a}$  and  $\vec{b}$  are non-collinear. The value of  $x$  for which the vectors  $\vec{c} = (x - 2)\vec{a} + \vec{b}$  and  $\vec{d} = (2x + 1)\vec{a} - \vec{b}$  are collinear, is

A. 1

B.  $\frac{1}{2}$

C.  $\frac{1}{3}$

D. 3

Answer: C



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3. If  $3i - 2j + 5k$  and  $-2i + pj - qk$  are collinear vectors, then

A.  $p = \frac{4}{3}, q = \frac{-10}{3}$

B.  $p = \frac{10}{3}, q = \frac{4}{3}$

$$C. p = \frac{-4}{3}, q = \frac{10}{3}$$

$$D. p = \frac{4}{3}, q = \frac{10}{3}$$

**Answer: D**



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4. The points  $A(\bar{a}), B(\bar{b}), C(\bar{c})$  will be collinear if

$$A. \bar{a} + \bar{b} + \bar{c} = \bar{0}$$

$$B. \bar{a} \times \bar{b} + \bar{b} \times \bar{c} + \bar{c} \times \bar{a} = \bar{0}$$

$$C. \bar{a} \cdot \bar{b} + \bar{b} \cdot \bar{c} + \bar{c} \cdot \bar{a} = \bar{0}$$

$$D. \bar{a} \times (\bar{b} + \bar{c}) + \bar{b} \times (\bar{c} + \bar{a}) + \bar{c} \times (\bar{a} + \bar{b}) = \bar{0}$$

**Answer: B**



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5. If  $\bar{a} = \hat{i} + \hat{j}$ ,  $\bar{b} = 2\hat{i} - \hat{j}$  and  $\bar{r} = 2\hat{i} - 4\hat{j}$ , then express  $\bar{r}$  as linear combination of  $\bar{a}$  and  $\bar{b}$

A.  $\bar{r} = 2\bar{a} + 2\bar{b}$

B.  $\bar{r} = -2\bar{a} + 2\bar{b}$

C.  $\bar{r} = 2\bar{a} - 2\bar{b}$

D.  $\bar{r} = -2\bar{a} - 2\bar{b}$

**Answer: B**



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6.

Let

$$\bar{A} = (x + 4y)\bar{a} + (2x + y + 1)\bar{b} \text{ and } \bar{B} = (y - 2x + 2)\bar{a} + (2x - 3y - 1)\bar{b}$$

, where  $\bar{a}$  and  $\bar{b}$  are non-collinear vectors, if  $3\bar{A} = 2\bar{B}$ , then

A.  $x = 1, y = 2$

B.  $x = 2, y = 1$

C.  $x = 2, y = -1$

D.  $x = -1, y = 2$

**Answer: C**



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7. A vector coplanar with the non-collinear vectors  $\vec{a}$  and  $\vec{b}$  is

A.  $\vec{a} \times \vec{b}$

B.  $\vec{a} + \vec{b}$

C.  $\vec{a} \cdot \vec{b}$

D.  $\vec{a} \times 3\vec{b}$

**Answer: B**



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8. The vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{a} + \vec{b}$  are

- A. Collinear
- B. Coplanar
- C. Non-coplanar
- D. Non-collinear

**Answer: B**



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9.  $\vec{p}$  and  $\vec{q}$  are position vectors of two points  $P$  and  $Q$ . The position vectors of a point which divides  $PQ$  internally in the ratio 2:5 is

- A.  $\frac{\vec{p} + \vec{q}}{7}$
- B.  $\frac{5\vec{p} + 2\vec{q}}{7}$
- C.  $\frac{2\vec{p} + 5\vec{q}}{7}$
- D.  $\frac{\vec{p} - \vec{q}}{7}$

**Answer: B**



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**10.** The co-ordinates of the points which divides line segment joining the point  $A(2, 3, -1)$  and  $B(3, 1, 4)$  internally in the ratio 2:3 are

A.  $\left(\frac{-12}{5}, \frac{-11}{5}, 1\right)$

B.  $\left(\frac{12}{5}, \frac{11}{5}, 1\right)$

C.  $\left(\frac{-12}{5}, \frac{-11}{5}, \frac{1}{5}\right)$

D.  $\left(\frac{12}{5}, \frac{11}{5}, \frac{1}{5}\right)$

**Answer: B**



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**11.** If O is origin and C is the mid - point of A (2, -1) and B ( -4, 3) . Then value of OC is

A.  $\hat{i} + \hat{j}$

B.  $\hat{i} - \hat{j}$

C.  $-\hat{i} + \hat{j}$

D.  $-\hat{i} - \hat{j}$

**Answer: C**



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**12.** If the position vectors of the points  $A$  and  $B$  are  $\hat{i} + 3\hat{j} - \hat{k}$  and  $3\hat{i} - \hat{j} - 3\hat{k}$ , then what will be the position vectors of the mid point of  $AB$

A.  $\hat{i} + 2\hat{j} - \hat{k}$

B.  $2\hat{i} + \hat{j} - 2\hat{k}$

C.  $\hat{i} + \hat{j} - \hat{k}$

D.  $\hat{i} + \hat{j} - 2\hat{k}$



**Answer: B**



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**13.** Position vectors of a point which divides line joining points  $A$  and  $B$  whose position vectors are  $2\hat{i} + \hat{j} - \hat{k}$  and  $\hat{i} - \hat{j} + 2\hat{k}$  externally in the ratio 5: 2 is

A.  $\frac{1}{3}(\hat{i} - 7\hat{j} + 12\hat{k})$

B.  $-\frac{1}{3}(\hat{i} + 7\hat{j} - 12\hat{k})$

C.  $\hat{i} - 7\hat{j} + 12\hat{k}$

D.  $\hat{i} + 7\hat{j} - 12\hat{k}$

**Answer: A**



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14. If  $P \equiv (2, -1, 4)$ ,  $Q \equiv (3, 2, 1)$  then the co-ordinates of the point which divides  $PQ$  externally in the ratio 2:1 are

- A.  $(4, 5, 2)$
- B.  $(-4, 5, -2)$
- C.  $(-4, -5, 2)$
- D.  $(4, 5, -2)$

**Answer: D**



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15. If the point  $A(5, a, -1)$ ,  $B(2, -7, k)$  and  $P\left(\frac{17}{4}, \frac{11}{4}, 0\right)$  are collinear, then the ratio in which P divides AB is

- A. 1:2
- B. 3:1
- C. 2:1

D. 1 : 3

**Answer: D**



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16. If  $A(2, 3, -4)$ ,  $B(m, 1, -1)$ ,  $C(3, 2, 2)$  and  $G(3, 2, n)$  is the centroid of  $\triangle ABC$ , then the values of  $m$  and  $n$  respectively are

A.  $-4, 1$

B.  $3, 4$

C.  $4, 3$

D.  $4, -1$

**Answer: D**



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17. If  $A(a, 2, 2)$ ,  $B(a, b, 1)$  and  $C(1, 2, -2)$  are the vertices of triangle  $ABC$  and  $G(2, 1, c)$  is centroid, then values of  $a$ ,  $b$  and  $c$  are

A.  $a = \frac{1}{2}, b = 1, c = 1$

B.  $a = \frac{5}{2}, b = -1, c = \frac{1}{3}$

C.  $a = -1, b = 1, c = \frac{3}{2}$

D.  $a = \frac{1}{2}, b = \frac{1}{2}, c = 1$

**Answer: B**



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18. If  $\hat{i}, \hat{j}, \hat{k}$  are the unit vectors and mutually perpendicular, then  $[\hat{i}\hat{k}\hat{j}]$  is equal to

A. 0

B. -1

C. 1

D. 2

**Answer: B**



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19. The scalar triple product of the vectors  $2\hat{i}$ ,  $3\hat{j}$  and  $-5\hat{k}$  is

A. 0

B. 10

C.  $-15$

D.  $-30$

**Answer: D**



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20. The value of  $(\hat{i} + \hat{j}) \cdot [(\hat{j} + \hat{k}) \times (\hat{k} + \hat{i})]$  is

A. 0

B. 1

C. -1

D. 2

**Answer: D**



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21. If  $\bar{a} = \hat{i} - \hat{j} + \hat{k}$ ,  $\bar{b} = \hat{i} + \hat{j} - 4\hat{k}$ ,  $\bar{c} = -\hat{i} + 2\hat{j} - \hat{k}$ , then

$$[\bar{a}\bar{b}\bar{c}] =$$

A. 2

B. 3

C. 6

D. 5

**Answer: D**

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22.

If

$$\bar{a} = 3\hat{i} - 2\hat{j} + 2\hat{k}, \bar{b} = 6\hat{i} + 4\hat{j} - 2\hat{k} \text{ and } \bar{c} = 3\hat{i} - 2\hat{j} - 4\hat{k},$$

then  $\bar{a}(\bar{b} \times \bar{c})$  is

A. 122

B. -144

C. 120

D. -120

**Answer: B**

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23. Let  $\bar{a}$ ,  $\bar{b}$  and  $\bar{c}$  three vectors, Then scalar triple product  $[\bar{a}\bar{b}\bar{c}]$  is equal to

A.  $[\bar{b}, \bar{a}, \bar{c}]$

B.  $[\bar{a}, \bar{c}, \bar{b}]$

C.  $[\bar{c}, \bar{b}, \bar{a}]$

D.  $[\bar{b}, \bar{c}, \bar{a}]$

**Answer: D**



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24. If  $\bar{a}, \bar{b}, \bar{c}$  are three vectors, then  $[\bar{a}, \bar{b}, \bar{c}]$  is not equal to

A.  $[\bar{b}\bar{c}\bar{a}]$

B.  $[\bar{c}\bar{a}\bar{b}]$

C.  $-[\bar{b}\bar{a}\bar{c}]$

D.  $[\bar{b}\bar{a}\bar{c}]$

**Answer: D**



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25.  $[\hat{i} \hat{k} \hat{j}] + [\hat{k} \hat{j} \hat{i}] + [\hat{j} \hat{k} \hat{i}]$

A. 1

B. 3

C. -3

D. -1

**Answer: D**



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26. The scalar triple product of vectors is zero if \_\_\_\_\_

A. One of the vectors is zero vectors

B. Any two vectors are non-collinear

C. the three vectors are non-coplanar

D. All of the above

**Answer: A**



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27. If  $\bar{a}, \bar{b}, \bar{c}$  are non-coplanar vectors then  $[\bar{a} + 2\bar{b} \quad \bar{a} + \bar{c} \quad \bar{b}] =$

A. 0

B.  $[\bar{a}, \bar{b}, \bar{c}]$

C.  $-[\bar{a}, \bar{b}, \bar{c}]$

D.  $2[\bar{a}, \bar{b}, \bar{c}]$

**Answer: C**



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28. If  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar vectors, then three points with position vectors  $\vec{a} - 2\vec{b} + 3\vec{c}, 2\vec{a} + m\vec{b} - 4\vec{c}$  and  $-7\vec{b} + 10\vec{c}$  will be collinear if  $m$  equals

A. 2

B. 3

C. 0

D.  $-1$

**Answer: B**



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29. The vectors  $\hat{i} + 2\hat{j} + 3\hat{k}, \lambda\hat{i} + 4\hat{j} + 7\hat{k}$  and  $-3\hat{i} - 2\hat{j} - 5\hat{k}$  are collinear, if  $\lambda$  equals

A. 3

B. 4

C. 5

D. 6

**Answer: A**



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**30.** If  $\vec{a}, \vec{b}, \vec{c}$  are any vectors, then which of these sets of vectors are coplanar

A.  $\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}$

B.  $\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}$

C.  $\vec{a} - \vec{b}, \vec{b} - \vec{c}, \vec{c} - \vec{a}$

D.  $\vec{a} + 2\vec{b}, \vec{b} + 2\vec{c}, \vec{c} + 2\vec{a}$

**Answer: C**



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31. If  $\vec{a} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$  and  $\vec{c} = 3\hat{i} + p\hat{j} + 5\hat{k}$  are coplanar then the value of  $p$  will be

A.  $-6$

B.  $-2$

C.  $2$

D.  $6$

**Answer: A**



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32. If the vectors  $\hat{i} + 3\hat{j} - 2\hat{k}$ ,  $2\hat{i} - \hat{j} + 4\hat{k}$  and  $3\hat{i} + 2\hat{j} + x\hat{k}$  are coplanar, then the value of  $x$  is

A.  $-2$

B.  $2$

C.  $1$

D. 3

**Answer: B**



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33. If vectors  $\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{j} - \hat{i}$ ,  $\hat{i} + 2\hat{j} + a\hat{k}$  are coplanar, then  $a$  is equal to

A.  $\frac{3}{2}$

B. 3

C.  $-3$

D. 0

**Answer: A**



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34. For any vectors  $\vec{a}, \vec{b}, \vec{c}$  correct statement is

A.  $\vec{a} \cdot (\vec{b} \times \vec{c}) = (\vec{c} \times \vec{b}) \cdot \vec{a}$

B.  $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{b} \times (\vec{c} \times \vec{a})$

C.  $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \times \vec{b}) \times \vec{c}$

D.  $\vec{a} \cdot (\vec{b} \times \vec{c}) = \vec{b} \cdot (\vec{c} \times \vec{a})$

Answer: D



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35.  $[\vec{a} \quad \vec{b} \quad \vec{a} \times \vec{b}]$  is equal to

A.  $|\vec{a} \times \vec{b}|$

B.  $|\vec{a} \times \vec{b}|^2$

C. 0

D. None of these

**Answer: B**



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36. If  $\vec{a}$  and  $\vec{b}$  be parallel vectors, then  $[\vec{a} \quad \vec{c} \quad \vec{b}] =$

A. 0

B. 1

C. 2

D. 3

**Answer: A**



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37. If  $\vec{a}, \vec{b}, \vec{c}$  are any three coplanar unit vectors then

A.  $\vec{a} \cdot (\vec{b} \times \vec{c}) = 1$



B.  $\bar{a} \cdot (\bar{b} \times \bar{c}) = 3$

C.  $(\bar{a} \times \bar{b}) \cdot \bar{c} = 0$

D.  $(\bar{c} \times \bar{a}) \cdot \bar{b} = 1$

**Answer: C**



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38. If  $\bar{a} = \frac{11}{2} \hat{i}$ ,  $\bar{b} = 12 \hat{j}$  and  $\bar{c} = \frac{13}{3} \hat{k}$  represents the three co-terminus edges of a parallelepiped, then its volume is given by

A. 510

B. 145

C. 286

D. 268

**Answer: C**



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39. Three concurrent edges  $OA, OB, OC$  of a parallelepiped are represented by three vectors  $2\hat{i} + \hat{j} - \hat{k}$ ,  $\hat{i} + 2\hat{j} + 3\hat{k}$  and  $-3\hat{i} - \hat{j} + \hat{k}$  the volume of the solid so formed in cubic unit is

- A. 5
- B. 6
- C. 7
- D. 8

**Answer: A**

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40. If  $\bar{a} = -3\hat{i} + 7\hat{j} + 5\hat{k}$ ,  $\bar{b} = -3\hat{i} + 7\hat{j} - 3\hat{k}$  and  $c = 7\hat{i} - 5\hat{j} - 3\hat{k}$  are the three coterminus edges of a parallelepiped, then its volume is

A. 108

B. 210

C. 272

D. 308

**Answer: C**



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**41.** The volume of the tetrahedron whose vertices are  $A(1, -1, 10)$ ,  $B(-1, -3, 7)$ ,  $C(5, -1, 1)$  and  $D(7, -4, 7)$  is

A. 26

B. 29

C. 32

D. None of these

**Answer: B**

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42. The volume of the tetrahedron with vertices  $5\hat{i} - \hat{j} + \hat{k}$ ,  $7\hat{i} - 4\hat{j} + 7\hat{k}$ ,  $\hat{i} - 6\hat{j} + 10\hat{k}$  and  $-\hat{i} - 3\hat{j} + 7\hat{k}$  is

A. 7

B. 3

C. 15

D. 11

**Answer: D**

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43. The sum of the three vectors determined by the medians of triangle directed from the vertices is

A. 0

B. 1

C.  $-1$

D.  $\frac{1}{3}$

**Answer: A**



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### Critical Thinking

1. The points with respective position vectors  $60\hat{i} + 3\hat{j}$ ,  $40\hat{i} - 8\hat{j}$ ,  $x\hat{i} - 52\hat{j}$  are collinear if  $x$  is equal to

A.  $-40$

B. 40

C. 20

D.  $-20$

**Answer: A**



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2. If the vectors  $\hat{i} + 2\hat{k}$ ,  $\hat{j} + \hat{k}$  and  $\lambda\hat{i} + \mu\hat{j}$  collinear, then

A.  $\lambda = 2, \mu = 1$

B.  $\lambda = 2, \mu = -1$

C.  $\lambda = -1, \mu = 2$

D.  $\lambda = -1, \mu = -2$

**Answer: C**



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3. If the vectors  $-\hat{i} + 3\hat{j} + 2\hat{k}$ ,  $-4\hat{i} + 2\hat{j} - 2\hat{k}$  and  $5\hat{i} + \lambda\hat{j} + \mu\hat{k}$  are collinear then

A.  $\lambda = 5, \mu = 10$

B.  $\lambda = 2, \mu = -1$

C.  $\lambda = -5, \mu = 10$

D.  $\lambda = 5, \mu = -10$

**Answer: A**



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4. If three points A, B and C have position vectors  $(1, x, 3), (3, 4, 7)$  and  $(y, -2, -5)$ , respectively and if they are collinear, then find  $(x, y)$ .

A.  $2, -3$

B.  $-2, 3$

C.  $2, 3$

D.  $-2, -3$

**Answer: A**

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5. If the position vectors of the point  $A, B, C$  be  $\hat{i} + \hat{j}$ ,  $\hat{i} - \hat{j}$  and  $a\hat{i} + b\hat{j} + c\hat{k}$  respectively then the point  $A, B, C$  are collinear if

A.  $a = b = c = 1$

B.  $a = 1$ ,  $b$  and  $c$  are arbitrary scalars

C.  $a = b = c = 0$

D.  $c = 0$ ,  $a = 1$  and  $b$  is arbitrary scalar

**Answer: D**

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6. Three points whose position vectors are  $\bar{a} + \bar{b}$ ,  $\bar{a} - \bar{b}$  and  $\bar{a} + k\bar{b}$  are collinear, then the value of  $k$  is



- A. Zero
- B. Only negative real number
- C. Only positive real number
- D. Every real number

**Answer: D**

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7. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-zero vectors, no two of which are collinear. If the vectors  $\vec{a} + 2\vec{b}$  is collinear with  $\vec{c}$  and  $\vec{b} + 3\vec{c}$  is collinear with  $\vec{a}$ , then  $(\lambda$  being some non-zero scalar) $\vec{a} + 2\vec{b} + 6\vec{c}$  is equal to

- A.  $\lambda\vec{a}$
- B.  $\lambda\vec{b}$
- C.  $\lambda\vec{c}$
- D. 0

**Answer: D**



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8. If the points  $A, B, C$  and  $D$  have position vectors  $\bar{a}, 2\bar{a} + \bar{b}, 4\bar{a} + 2\bar{b}$  and  $5\bar{a} + 4\bar{b}$  respectively, then three collinear points are

A.  $A, B, D$

B.  $A, B, C$

C.  $B, C, D$

D.  $A, C, D$

**Answer: A**



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9.

If

$$\bar{a} = 2\bar{p} + 3\bar{q} - \bar{r}, \bar{b} = \bar{p} - 2\bar{q} + 2\bar{r} \text{ and } \bar{c} = -2\bar{p} + \bar{q} - 2\bar{r} \text{ and } \bar{R} = 3\bar{p}$$

where  $\bar{p}, \bar{q}, \bar{r}$  are non-coplanar vectors, then  $\bar{R}$  in terms of  $\bar{a}, \bar{b}, \bar{c}$  is

A.  $5\bar{a} + 2\bar{b} + 3\bar{c}$

B.  $3\bar{a} + 5\bar{b} + 2\bar{c}$

C.  $2\bar{a} + 5\bar{b} + 3\bar{c}$

D.  $5\bar{a} + 3\bar{b} + 2\bar{c}$

**Answer: C**[Watch Video Solution](#)

10. If  $\bar{a} + \bar{b} + \bar{c} = \lambda\bar{d}$  and  $\bar{b} + \bar{c} + \bar{d} = \mu\bar{a}$  and  $\bar{a}, \bar{b}, \bar{c}$  are non-coplanar, then  $\bar{a} + \bar{b} + \bar{c} + \bar{d}$  is equal to

A.  $\mu\bar{b}$

B.  $\lambda\bar{a}$

C.  $\vec{0}$

D.  $(\lambda | \mu)\vec{a}$

**Answer: C**



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11. A and B are two points. The position vector of A is  $6\vec{b}-2\vec{a}$ . A point P divides the line AB in the ratio 1:2. If  $\vec{a}-\vec{b}$  is the position vector of P, then the position vector of B is given by

A.  $7\vec{a} - 15\vec{b}$

B.  $7\vec{a} + 15\vec{b}$

C.  $15\vec{a} - 7\vec{b}$

D.  $15\vec{a} + 7\vec{b}$

**Answer: A**



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12. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are the position vectors of the points A, B, C respectively and  $2\vec{a} + 3\vec{b} - 5\vec{c} = \vec{0}$ , then find the ratio in which the point C divides line segment AB.

A. 2:3

B. 3:2

C. 3:5

D. 5:2

**Answer: B**



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13. If  $\vec{OA} = \hat{i} + 3\hat{j} - 2\hat{k}$  and  $\vec{OB} = 3\hat{i} + \hat{j} - 2\hat{k}$ , then the vectors  $\vec{OC}$  which bisects  $\angle AOB$  is equal to

A.  $\hat{i} - \hat{j} - \hat{k}$

B.  $2(\hat{i} + \hat{j} + \hat{k})$

C.  $-\hat{i} + \hat{j} - \hat{k}$

D.  $2(\hat{i} + \hat{j} - \hat{k})$

**Answer: D**



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14.  $\bar{a}$ ,  $\bar{b}$  are position vectors of points A and B. If P divides AB in the ratio 3: 1 and Q is the mid-point of AP, then position vectors of Q will be

A.  $\frac{1}{2}(\bar{a} - \bar{b})$

B.  $\frac{1}{2}(\bar{a} + \bar{b})$

C.  $\frac{1}{8}(5\bar{a} + 3\bar{b})$

D.  $\frac{1}{8}(5\bar{a} - 3\bar{b})$

**Answer: C**



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15. If  $2\bar{a} + \bar{b} = 3\bar{c}$ , then A divides BC in the ratio

A. 3: 1 externally

B. 3: 1 internally

C. 1: 3 externally

D. 1: 3 internally

**Answer: A**



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16. In  $\triangle ABC$ , P is the mid point of BC, Q divides CA internally in the ratio 2: 1 and R divides AB externally in the ratio 1: 2 then

A. R divides PQ externally in the ratio 2: 1

B. P, Q, R are collinear

C. P divides QR externally in the ratio 3: 2

D. Q divides PR internally in the ratio 3 : 2

**Answer: B**



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17. If  $\vec{a} = \hat{i} - \hat{k}$ ,  $\vec{b} = x\hat{i} + \hat{j} + (1 - x)\hat{k}$  and

$\vec{c} = y\hat{i} + x\hat{j} + (1 + x - y)\hat{k}$ . Then  $[\vec{a}, \vec{b}, \vec{c}]$  depends on

A. only x

B. only y

C. neither x nor y

D. both x and y

**Answer: C**



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18. If the points  $(1, 1, 2)$ ,  $(2, 1, p)$ ,  $(1, 0, 3)$  and  $(2, 2, 0)$  are co-planar then value of  $p$  is

A. 1

B. 2

C.  $-1$

D. 0

**Answer: A**



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19. If the points A, B, C and D with position vectors  $\hat{i} + \hat{j} + \hat{k}$ ,  $2\hat{i} + 3\hat{j} + \hat{k}$ ,  $\hat{i} + 2\hat{j} + 5\hat{k}$  and  $\lambda\hat{i} + 3\hat{j} + 4\hat{k}$  are coplanar then  $\lambda$  is equal to

A. 5

B. 7

C. 2

D.  $\frac{13}{8}$

**Answer: D**



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20. If  $a\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} - b\hat{j} + \hat{k}$ ,  $\hat{i} + \hat{j} - c\hat{k}$  are coplanar, then  $abc + 2$  is equal to

A.  $a + b - c$

B.  $a - b - c$

C.  $a + b + c$

D.  $a - b + c$

**Answer: B**



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21. If the given vectors  $(-bc, b^2 + bc, c^2 + bc)$ ,  $(a^2 + ac, -ac, c^2 + ac)$  and  $(a^2 + ab, b^2 + ab, c^2 + bc)$  are coplanar, where none of  $a$ ,  $b$  and  $c$  is zero then

A.  $a^2 + b^2 + c^2 = 1$

B.  $bc + ca + ab = 0$

C.  $a + b + c = 0$

D.  $a^2 + b^2 + c^2 = bc + ca + ab$

**Answer: B**



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22. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non-zero, non collinear vectors, then the vectors  $\vec{a} - \vec{b} + \vec{c}$ ,  $4\vec{a} - 7\vec{b} - \vec{c}$  and  $3\vec{a} + 6\vec{b} + 6\vec{c}$  are

A. collinear

B. Coplanar

C. both collinear and co-planar

D. neither collinear nor coplanar

**Answer: D**

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23. Given vectors  $\vec{a}, \vec{b}, \vec{c}$  such that  $\vec{a} \cdot (\vec{b} \times \vec{c}) = \lambda \neq 0$  the value of  $(\vec{b} \times \vec{c}) \cdot (\vec{a} + \vec{b} + \vec{c}) / \lambda$  is

A. 3

B. 1

C.  $-3\lambda$

D.  $\frac{3}{\lambda}$

**Answer: B**

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24. For any three vectors  $\bar{a}$ ,  $\bar{b}$  and  $\bar{c}$ ,  $(\bar{a} - \bar{b}) [(\bar{b} + \bar{c}) \times (\bar{c} + \bar{a})]$  is equal to:

A.  $2\bar{a} \cdot (\bar{b} \times \bar{c})$

B.  $[\bar{a} \ \bar{b} \ \bar{c}]$

C.  $[\bar{a} \ \bar{b} \ \bar{c}]^2$

D. 0

**Answer: D**



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25. If  $\bar{a}$ ,  $\bar{b}$  and  $\bar{c}$  are three non-coplanar vectors, then :

$$(\bar{a} + \bar{b} + \bar{c}) \cdot [(\bar{a} + \bar{b}) \times (\bar{a} + \bar{c})] =$$

A. 0

B.  $[\bar{a} \ \bar{b} \ \bar{c}]$

C.  $-[\bar{a}\bar{b}\bar{c}]$

$$D. 2[\bar{a}, \bar{b}, \bar{c}]$$

**Answer: C**



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26. If  $\bar{r} = l(\bar{b} \times \bar{c}) + m(\bar{c} \times \bar{a}) + n(\bar{a} \times \bar{b})$  and  $[\bar{a}\bar{b}\bar{c}] = 2$ , then  $l + m + n$  is equal to

A.  $(\bar{a} + \bar{b} + \bar{c})\bar{r}$

B.  $\frac{1}{2}(\bar{a} + \bar{b} + \bar{c})\bar{r}$

C.  $\frac{1}{3}(\bar{a} + \bar{b} + \bar{c})(\bar{a} + \bar{b} + \bar{c})$

D.  $\frac{2}{3}(\bar{a} + \bar{b} + \bar{c})\bar{r}$

**Answer: B**



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27. The volume of parallelepiped with vector  $\vec{a} + 2\vec{b} - \vec{c}$ ,  $\vec{a} - \vec{b}$  and  $\vec{a} - \vec{b} - \vec{c}$  is equal to  $k[\vec{a}\vec{b}\vec{c}]$  then  $k =$

A.  $-3$

B.  $3$

C.  $2$

D.  $-2$

**Answer: B**



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28. If the volume of parallelepiped with coterminus edges  $-p\hat{i} + 5\hat{k}$ ,  $\hat{i} - \hat{j} + q\hat{k}$  and  $3\hat{i} - 5\hat{j}$  is 8 then

A.  $5pq + 18 = 0$

B.  $3pq - 18 = 0$

C.  $pq + 18 = 0$

D.  $pq - 18 = 0$

**Answer: A**



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29. If the volumes of tetrahedron where vertices  $(1, 2, 0)$ ,  $(2, 0, 4)$ ,  $(-1, 2, 0)$  and  $(-1, 1, \lambda)$  is  $\frac{2}{3}cu$ , unit, find the value of  $\lambda$

A. 0

B. 1

C. 4

D. -2

**Answer: B**



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30. If D is the mid-point of side AB of  $\triangle ABC$ , then  $\overline{AB} + \overline{BC} + \overline{AC} =$

A.  $2(\overline{AD} - \overline{BD})$

B.  $2(\overline{DC} - \overline{BD})$

C.  $2(\overline{BD} - \overline{CA})$

D.  $2(\overline{BD} - \overline{AC})$

**Answer: B**



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31. The vector  $\overline{AB} = 3\hat{i} + 4\hat{k}$  and  $\overline{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are the sides of a triangle ABC. The length of the median through A is

A.  $\sqrt{288}$

B.  $\sqrt{18}$

C.  $\sqrt{72}$

D.  $\sqrt{33}$

**Answer: D**



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**32.** If  $G$  and  $G'$  are the centroids of the triangle  $ABC$  and  $A'B'C'$ , then the value of  $\overline{AA'} + \overline{BB'} + \overline{CC'}$  equals

A.  $\overline{GG'}$

B.  $2\overline{GG'}$

C.  $3\overline{GG'}$

D.  $\frac{2}{3}\overline{GG'}$

**Answer: C**



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**33.** If  $S$  is circumcentre,  $O$  is orthocentre of  $\triangle ABC$ , then  $\overrightarrow{SA} + \overrightarrow{SB} + \overrightarrow{SC} =$

A.  $\overline{SO}$

B.  $2\overline{SO}$

C.  $\overline{OS}$

D.  $2\overline{OS}$

**Answer: A**

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**34.** If  $A(-3, -2, 0)$ ,  $B(3, -3, 1)$  and  $C(5, 0, 2)$  are three successive vertices of parallelogram  $ABCD$ , then its fourth vertex  $D$  is

A.  $(1, 1 - 1)$

B.  $(-1, 1, 1)$

C.  $(1, -1, 1)$

D.  $(2, -3, 5)$

**Answer: B**

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35. In a trapezium, if the vectors  $\overline{BC} = \lambda(\overline{AD})$ ,  $\overline{P} = \overline{AC} + \overline{BD}$  is collinear with  $\overline{AD}$  and  $\overline{P} = \mu\overline{AD}$ , then

A.  $\mu = \lambda + 1$

B.  $\lambda = \mu + 1$

C.  $\lambda + \mu = 1$

D.  $\mu = 2 + \lambda$

**Answer: A**

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### Competitive Thinking

1. If the point  $(1, 0)$ ,  $(0, 1)$  and  $(x, 8)$  are collinear, then the value of  $x$  is equal to

A. 5

B.  $-6$

C. 6

D.  $-7$

**Answer: D**



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2. The points with position vectors  $20\hat{i} + p\hat{j}$ ,  $5\hat{i} - \hat{j}$  and  $10\hat{i} - 13\hat{j}$  are collinear. The value of p is

A. 7

B.  $-37$

C.  $-7$

D. 37

**Answer: B**

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3. If the points  $P(\bar{a} + 2\bar{b} + \bar{c})$ ,  $Q(2\bar{a} + 3\bar{b})$  and  $R(\bar{b} + t\bar{c})$  are collinear, where  $\bar{a}$ ,  $\bar{b}$ ,  $\bar{c}$  are three non-coplanar vectors, then the value of  $t$  is

A.  $-2$

B.  $-\frac{1}{2}$

C.  $\frac{1}{2}$

D.  $2$

**Answer: D**

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4. If the position vectors of the points  $A, B, C$  are  $\bar{a}, \bar{b}$  and  $3\bar{a} - 2\bar{b}$  respectively, then the position  $A, B, C$  are

A. Collinear

B. Non-collinear

C. Forming a right angled triangle

D. None of these

**Answer: A**



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5. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are three non-zero vectors which are pairwise non-collinear. If  $\vec{a} + 3\vec{b}$  is collinear with  $\vec{c}$  and  $\vec{b} + 2\vec{c}$  is collinear with  $\vec{a}$ , then  $\vec{a} + 3\vec{b} + 6\vec{c}$  is

A.  $\vec{c}$

B.  $\vec{0}$

C.  $\vec{a} + \vec{c}$

D.  $\vec{a}$

**Answer: B**



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6. If the vectors  $3\hat{i} + 2\hat{j} - \hat{k}$  and  $6\hat{i} - 4x\hat{j} + y\hat{k}$  are parallel, then the value of  $x$  and  $y$  will be

A.  $-1, -2$

B.  $1, -2$

C.  $-1, 2$

D.  $1, 2$

**Answer: A**



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7. If the vectors  $3\hat{i} + \hat{j} - 5\hat{k}$  and  $a\hat{i} + b\hat{j} - 15\hat{k}$  are collinear, if

A.  $a = 3, b = 1$

B.  $a = 9, b = 1$



C.  $a = 3, b = 3$

D.  $a = 9, b = 3$

**Answer: D**



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8. If  $\vec{a}, \vec{b}$  are non-collinear vectors and  $x, y$  are scalars such that  $x\vec{a} + y\vec{b} = \vec{0}$ , then

A.  $x = 0$ , but  $y$  is not necessarily zero

B.  $y = 0$ , but  $x$  is not necessarily zero

C.  $x = 0, y = 0$

D. None of these

**Answer: C**



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9. If  $\vec{a}, \vec{b}, \vec{c}$  are non-collinear vectors such that for some scalar  $x, y, z$ ,  $x\vec{a} + y\vec{b} + z\vec{c} = 0$ , then

A.  $x = 0, y = 0, z = 0$

B.  $x \neq 0, y \neq 0, z = 0$

C.  $x = 0, y \neq 0, z \neq 0$

D.  $x \neq 0, y \neq 0, z \neq 0$

**Answer: A**



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10.  $\vec{a}$  and  $\vec{b}$  are two non collinear vectors then  $x\vec{a} + y\vec{b}$  (where  $x$  and  $y$  are scalars) represents a vector which is (A) parallel to  $\vec{b}$  (B) parallel to  $\vec{a}$  (C) coplanar with  $\vec{a}$  and  $\vec{b}$  (D) none of these

A. Parallel to  $\vec{b}$

B. Parallel to  $\vec{a}$

C. Coplanar with  $\bar{a}$  and  $\bar{b}$

D. None of these

**Answer: C**

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11. If

$$\bar{a} = \hat{i} + \hat{j} - 2\hat{k}, \bar{b} = 2\hat{i} - \hat{j} + \hat{k} \text{ and } \bar{c} = 3\hat{i} + \hat{k} \text{ and } \bar{c} = m\bar{a} + n\bar{b}$$

then  $m + n$

A. 0

B. 1

C. 2

D. -1

**Answer: C**

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12. The position vectors of the point which divides internally in the ratio 2:3 the join of the points  $2\bar{a} - 3\bar{b}$  and  $3\bar{a} - 2\bar{b}$ , is

A.  $\frac{12}{5}\bar{a} + \frac{13}{5}\bar{b}$

B.  $\frac{12}{5}\bar{a} - \frac{13}{5}\bar{b}$

C.  $\frac{3}{5}\bar{a} - \frac{2}{5}\bar{b}$

D.  $\frac{2}{5}\bar{a} = \frac{3}{5}\bar{b}$

**Answer: B**



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13. Let  $A(1, -1, 2)$  and  $B(2, 3, -1)$  be two points. If a point P divides AB internally in the ratio 2:3, then the position vector of P is

A.  $\frac{1}{\sqrt{5}}(\hat{i} + \hat{j} + \hat{k})$

B.  $\frac{1}{\sqrt{3}}(\hat{i} + 6\hat{j} + \hat{k})$

C.  $\frac{1}{\sqrt{3}}(\hat{i} + \hat{j} + \hat{k})$

D.  $\frac{1}{5}(7\hat{i} + 3\hat{j} + 4\hat{k})$

**Answer: D**



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**14.** If  $z_1$  and  $z_2$  are z co-ordinates of the point of trisection of the segment joining the points  $A(2, 1, 4)$ ,  $B(-1, 3, 6)$  then  $z_1 + z_2 =$

A. 1

B. 4

C. 5

D. 10

**Answer: D**



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15. If the position vector of a point A is  $\vec{a} + 2\vec{b}$  and  $\vec{a}$  divides AB in the ratio 2:3, then the position vector of B, is

A.  $\vec{a} + \vec{b}$

B.  $\vec{a}$

C.  $\vec{a} - 3\vec{b}$

D.  $\vec{b}$

**Answer: C**



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16. Assertion (A): If  $(-1, 3, 2)$  and  $(5, 3, 2)$  are respectively the orthocentre and circumcentre of a triangle, then  $(3, 3, 2)$  is its centroid.

Reason (R): Centroid of a triangle divides the line segment joining the orthocentre and the circumcentre in the ratio 1:2,

A. A and R are true and R is correct explanation to A.

B. A and R are true but R is not the correct explanation to A.

C. A is true, R is false.

D. A is false. R is true.

**Answer: C**



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17. If the orthocentre and centroid of a triangle are  $(-3, 5, 2)$  and  $(3, 3, 4)$  respectively, then its circumcentre is

A.  $(6, 2, 5)$

B.  $(6, 2, -5)$

C.  $(6, -2, 5)$

D.  $(6, -2, -5)$

**Answer: A**



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18. L and M are two points with position vectors  $2\vec{a} - \vec{b}$  and  $\vec{a} + 2\vec{b}$ , respectively. The position vector of the point N which divides the line segment LM in the ratio 2:1 externally is

A.  $3\vec{b}$

B.  $4\vec{b}$

C.  $5\vec{b}$

D.  $3\vec{a} + 4\vec{b}$

**Answer: C**



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19. The position vector of a point R which divides the line joining two points P and Q whose position vectors are  $\hat{i} + 2\hat{j} - \hat{k}$  and  $-\hat{i} + \hat{j} - \hat{k}$  respectively, in the ratio 2:1 externally is



A.  $-3\hat{i} - \hat{k}$

B.  $3\hat{i} + \hat{k}$

C.  $2\hat{i} + \hat{j} - \hat{k}$

D. None of these

**Answer: A**

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20. If  $3\overline{P} + 2\overline{R} - 5\overline{Q} = \overline{0}$ , then

A.  $P, Q, R$  are collinear

B.  $P, Q, R$  vertices of a  $\Delta$

C.  $Q$  divides  $PR$  externally

D. None of these

**Answer: A**

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21. If three points A,B,C are collinear, whose position vectors are  $\hat{i} - 2\hat{j} - 8\hat{k}$ ,  $5\hat{i} - 2\hat{k}$  and  $11\hat{i} + 3\hat{j} + 7\hat{k}$  respectively, then the ratio in which B divides AC is

A. 1:2

B. 2:3

C. 2:1

D. 1:1

**Answer: B**



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22. Let  $\square PQRS$  be a quadrilateral. If M and N are the mid-points of the sides PQ and RS respectively, then  $PS+QR=$

A.  $3\overline{MN}$

B.  $4\overline{MN}$

C.  $2\overline{MN}$

D.  $2\overline{NM}$

**Answer: C**



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23. In  $\triangle ABC$ ,  $L, M, N$  are points on  $BC, CA, AB$  respectively, dividing them in the ratio  $1:2, 2:3, 3:5$ , if the point  $K$  divides  $AB$  in the ratio  $5:3$ ,

then  $\frac{|\overline{AL} + \overline{BM} + \overline{CN}|}{|\overline{CK}|} =$

A.  $\frac{1}{15}$

B.  $\frac{2}{5}$

C.  $\frac{5}{8}$

D.  $\frac{3}{5}$

**Answer: A**



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24. Let  $G$  be the centroid of a triangle  $ABC$  and  $O$  be any other point, then

$\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC}$  is equal to

A.  $\vec{0}$

B.  $\overrightarrow{OG}$

C.  $3\overrightarrow{OG}$

D. None of these

Answer: C



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25. If  $A, B, C$  are the vertices of a triangle whose position vectors are

$\vec{a}, \vec{b}, \vec{c}$  and  $G$  is the centroid of the  $\triangle ABC$ , then

$$\overrightarrow{GA} + \overrightarrow{GB} + \overrightarrow{GC} =$$

A.  $\bar{0}$

B.  $\bar{a} + \bar{b} + \bar{c}$

C.  $\frac{\bar{a} + \bar{b} + \bar{c}}{3}$

D.  $\frac{\bar{a} + \bar{b} - \bar{c}}{3}$

**Answer: A**



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26. If  $\bar{a} = 2\hat{i} + \hat{j} - \hat{k}$ ,  $\bar{b} = \hat{i} + 2\hat{j} + \hat{k}$  and  $\bar{c} = \hat{i} - \hat{j} + 2\hat{k}$ , then

$\bar{a} \cdot (\bar{b} \times \bar{c}) =$

A. 6

B. 10

C. 12

D. 24

**Answer: C**



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27.

If

$$\bar{a} = \hat{i} + \hat{j} + \hat{k}, \bar{b} = 2\hat{i} + \lambda\hat{j} + \hat{k}, \bar{c} = \hat{i} - \hat{j} + 4\hat{k} \text{ and } \bar{a} \cdot (\bar{b} \times \bar{c}) =$$

, then  $\lambda$  is equal to

A. 6

B. 7

C. 9

D. 10

Answer: A



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28. If  $\bar{a}$  is perpendicular to  $\bar{b}$  and  $\bar{c}$ ,  $|\bar{a}| = 2$ ,  $|\bar{b}| = 3$ ,  $|\bar{c}| = 4$  and the angle between  $\bar{b}$  and  $\bar{c}$  is  $\frac{2\pi}{3}$ . then  $[\bar{a} \ \bar{b} \ \bar{c}]$  is equal to

A.  $4\sqrt{3}$

B.  $6\sqrt{3}$

C.  $12\sqrt{3}$

D.  $18\sqrt{3}$

**Answer: C**



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29. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are mutually perpendicular vectors having magnitudes 1, 2, 3 respectively, then  $[\vec{a} + \vec{b} + \vec{c}, \vec{b} - \vec{a}, \vec{c}] =$

A. 0

B. 6

C. 12

D. 18

**Answer: C**

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30. The value of  $[\bar{a} - \bar{b}, \bar{b} - \bar{c}, \bar{c} - \bar{a}]$ , where  $|\bar{a}| = 1$ ,  $|\bar{b}| = 5$  and  $|\bar{c}| = 3$  is

A. 0

B. 1

C. 2

D. 4

Answer: A

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31. The value of  $(\bar{a} - \bar{b}) \cdot [(\bar{b} - \bar{c}) \times (\bar{c} - \bar{a})]$  is

A. 0

B.  $2[\bar{a} \ \bar{b} \ \bar{c}]$



C.  $3[\bar{a} \ \bar{b} \ \bar{c}]$

D. None of these

**Answer: A**



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32. If a vector  $\bar{\alpha}$  lie in plane  $\bar{\beta}$  and  $\bar{\gamma}$  then which is correct

A.  $[\bar{\alpha}, \bar{\beta}, \bar{\gamma}] = 0$

B.  $[\bar{\alpha}, \bar{\beta}, \bar{\gamma}] = 1$

C.  $[\bar{\alpha}, \bar{\beta}, \bar{\gamma}] = 3$

D.  $[\bar{\beta}, \bar{\gamma}, \bar{\alpha}] = 1$

**Answer: A**



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33. If  $\vec{a}, \vec{b}, \vec{c}$  are three coplanar vectors, then  $[\vec{a} + \vec{b} \quad \vec{b} + \vec{c} \quad \vec{c} + \vec{a}] =$

A.  $[\vec{a}\vec{b}\vec{c}]$

B.  $2[\vec{a}\vec{b}\vec{c}]$

C.  $3[\vec{a}\vec{b}\vec{c}]$

D. 0

**Answer: D**



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34. If  $\vec{a}, \vec{b}, \vec{c}$  be any three non-coplanar vectors, then

$$[\vec{a} + \vec{b} \quad \vec{b} + \vec{c} \quad \vec{c} + \vec{a}] =$$

A.  $[\vec{a} \quad \vec{b} \quad \vec{c}]$

B.  $2[\vec{a} \quad \vec{b} \quad \vec{c}]$

C.  $[\vec{a} \quad \vec{b} \quad \vec{c}]^2$

D.  $2[\vec{a} \quad \vec{b} \quad \vec{c}]^2$

**Answer: B**



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35. Let  $\bar{A} = \hat{i} + \hat{j} + \hat{k}$ ,  $\bar{B} = \hat{i}$ ,  $\bar{C} = C_1\hat{i} + C_2\hat{j} + C_3\hat{k}$  if  $C_2 = -1$  and  $C_3 = 1$ , then make three vectors coplanar

A.  $C_1 = 0$

B.  $C_1 = 1$

C.  $C_1 = 2$

D. No value of  $C_1$  can be found

**Answer: D**



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36. If the vectors  $2\hat{i} - \hat{j} + \hat{k}$ ,  $\hat{i} + 2\hat{j} - 3\hat{k}$  and  $3\hat{i} + \lambda\hat{j} + 5\hat{k}$  be coplanar, then  $\lambda =$

A.  $-1$

B.  $-2$

C.  $-3$

D.  $-4$

**Answer: D**



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37. If the vectors  $\lambda \hat{i} + \hat{j} + 2\hat{k}$ ,  $\hat{i} + \lambda \hat{j} - \hat{k}$  and  $2\hat{i} - \hat{j} + \lambda \hat{k}$  are coplanar if

A.  $\lambda = -2$

B.  $\lambda = 0$

C.  $\lambda = 2$

D.  $\lambda = 1$

**Answer: A**

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38. If the vectors  $4\hat{i} + 11\hat{j} + m\hat{k}$ ,  $7\hat{i} + 2\hat{j} + 6\hat{k}$  and  $\hat{i} + 5\hat{j} + 4\hat{k}$  are coplanar, then  $m$  is equal to

A. 38

B. 0

C. 10

D.  $-10$

**Answer: C**

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39. If the vectors  $2\hat{i} + 2\hat{j} + 6\hat{k}$ ,  $2\hat{i} + \lambda\hat{j} + 6\hat{k}$ ,  $2\hat{i} - 3\hat{j} + \hat{k}$  are coplanar, then the value of  $\lambda$  is

A.  $-10$

B. 1

C. 0

D. 2

**Answer: D**



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40. If the four points with position vectors  $-2\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{j} - \hat{k}$  and  $\lambda\hat{j} + \hat{k}$  are coplanar, then  $\bar{\lambda} =$

A. 1

B. 2

C. -1

D. 0

**Answer: A**

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41. If the vectors

$$\bar{a} = \hat{i} + \hat{j} + \hat{k}, \bar{b} = \hat{i} - \hat{j} - 2\hat{k} \text{ and } \bar{c} = x\hat{i} + (x - 2)\hat{j} - \hat{k} \text{ are}$$

coplanar, then  $x =$

A. 1

B. 2

C. 0

D. -2

**Answer: D**

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42. If the point having the position vectors

$$3\hat{i} - 2\hat{j} - \hat{k}, 2\hat{i} + 3\hat{j} - 4\hat{k}, -\hat{i} + \hat{j} + 2\hat{k} \text{ and } 4\hat{i} + 5\hat{j} + \lambda\hat{k}$$

are coplanar then  $\lambda =$

A.  $-8$

B.  $8$

C.  $\frac{146}{17}$

D.  $\frac{-146}{17}$

**Answer: D**

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**43.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar vectors and the four points with position vectors  $2\vec{a} + 3\vec{b} - \vec{c}$ ,  $\vec{a} - 2\vec{b} + 3\vec{c}$ ,  $3\vec{a} + 4\vec{b} - 2\vec{c}$ ,  $k\vec{a} - 6\vec{b} + 6\vec{c}$  are coplanar, then  $k$

A.  $0$

B.  $1$

C.  $2$

D.  $3$



**Answer: B**



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44. If the vectors  $a\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} + b\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} + c\hat{k}$  are coplanar ( $a \neq b \neq c \neq 1$ ), then the value of  $abc - (a + b + c) =$

A. 2

B. -2

C. 0

D. -1

**Answer: B**



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45. The number of distinct real value of  $\lambda$ , for which the vector  $-\lambda^2\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} - \lambda^2\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} - \lambda^2\hat{k}$  are coplanar, is

A. Zero

B. One

C. Two

D. Three

**Answer: C**



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**46.** The number of distinct real values of  $\lambda$  for which the vectors  $\bar{a} = \lambda^3 \hat{i} + \hat{k}$ ,  $\bar{b} = \hat{i} - \lambda^3 \hat{j}$  and  $\bar{c} = \hat{i} + (2\lambda - \sin \lambda) \hat{j} - \lambda \hat{k}$  are coplanar is

A. 0

B. 1

C. 2

D. 3

**Answer: B**



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47. If  $\vec{a}, \vec{b}, \vec{c}$  are non coplanar vectors and  $\lambda$  is a real number then the vectors  $\vec{a} + 2\vec{b} + 3\vec{c}, \lambda\vec{b} + 4\vec{c}$  and  $(2\lambda - 1)\vec{c}$  are non coplanar for (A) all values of lamda (B) non value of lamda (C) all except two values of lamda (D) all except one vau of lamda

- A. No value of  $\lambda$
- B. all except one value of  $\lambda$
- C. all except two values of  $\lambda$
- D. all values of  $\lambda$

**Answer: C**



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48. If the origin and the point  $p(2, 3, 4), q(1, 2, 3)R(x, y, z)$  are coplanar then

A.  $x - 2y - z = 0$

B.  $x + 2y + z = 0$

C.  $x - 2y + z = -0$

D.  $2x - 2y + z = 0$

**Answer: C**



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49. A vector perpendicular to  $2\hat{i} + \hat{j} + \hat{k}$  and coplanar with  $\hat{i} + 2\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} + 2\hat{k}$  is

A.  $5(\hat{j} - \hat{k})$

B.  $\hat{i} + 7\hat{j} - \hat{k}$

C.  $5(\hat{j} + \hat{k})$

$$D. 2\hat{i} - 7\hat{j} - \hat{k}$$

**Answer: A**



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50. Given three arbitrary vectors  $\bar{a}, \bar{b}, \bar{c}$ , then vectors

$$\bar{\alpha} = 5\bar{a} + 6\bar{b} + 7\bar{c}, \beta = 7\bar{a} - 8\bar{b} + 9\bar{c}, \bar{\gamma} = 3\bar{a} + 20\bar{b} + 5\bar{c} \text{ are}$$

- A. collinear
- B. Coplanar
- C. Non-coplanar
- D. None of these

**Answer: B**



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51. If  $\vec{x} \cdot \vec{a} = 0$ ,  $\vec{x} \cdot \vec{b} = 0$  and  $\vec{x} \cdot \vec{c} = 0$  for some non-zero vectors  $\vec{x}$ , then the TRUE statement is

A.  $[\vec{a} \ \vec{b} \ \vec{c}] = 0$

B.  $[\vec{a} \ \vec{b} \ \vec{c}] \neq 0$

C.  $[\vec{a} \ \vec{b} \ \vec{c}] = 1$

D. None of these

**Answer: A**



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52. which of the following expression are meaningful?

A.  $\vec{u} \cdot (\vec{v} \times \vec{w})$

B.  $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$

C.  $(\vec{u} \cdot \vec{v}) \times \vec{w}$

D.  $\vec{u} \times (\vec{v} \cdot \vec{w})$

**Answer: A**



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**53.** Out of the following which one is not true?

A.  $\bar{a} \cdot (\bar{b} \times \bar{c})$

B.  $(\bar{b} \times \bar{c}) \cdot \bar{a}$

C.  $(\bar{a} \times \bar{b}) \cdot \bar{c}$

D.  $(\bar{a} \cdot \bar{c}) \times \bar{b}$

**Answer: D**



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**54.** For three vectors  $\vec{u}$ ,  $\vec{v}$ ,  $\vec{w}$  which of the following expressions is not equal to any of the remaining three?

A.  $\bar{u} \cdot (\bar{v} \times \bar{w})$

B.  $(\bar{v} \times \bar{w}) \cdot \bar{u}$

C.  $\bar{v} \cdot (\bar{u} \times \bar{w})$

D.  $(\bar{u} \times \bar{v}) \cdot \bar{w}$

**Answer: C**



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55.  $\bar{a} \cdot (\bar{a} \times \bar{b}) =$

A.  $\bar{b} \cdot \bar{b}$

B.  $\overline{a^2} \cdot \bar{b}$

C. 0

D.  $\bar{a}^2 + \bar{a} \cdot \bar{b}$

**Answer: C**



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56. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non-coplanar vectors, then

$$\frac{\vec{a} \cdot \vec{b} \times \vec{c}}{\vec{c} \times \vec{a} \cdot \vec{b}} + \frac{\vec{b} \cdot \vec{a} \times \vec{c}}{\vec{c} \cdot \vec{a} \times \vec{b}} =$$

- A. 0
- B. 2
- C.  $-2$
- D. None of these

Answer: A



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57. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar, then the value of

$$\vec{a} \cdot \left\{ \frac{\vec{b} \times \vec{c}}{3\vec{b} \cdot (\vec{c} \times \vec{a})} \right\} - \vec{b} \cdot \left\{ \frac{\vec{c} \times \vec{a}}{2\vec{c} \cdot (\vec{a} \times \vec{b})} \right\} \text{ is}$$

- A.  $\frac{-1}{2}$
- B.  $\frac{-1}{3}$

C.  $\frac{-1}{6}$

D.  $\frac{1}{6}$

**Answer: C**



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58.  $\bar{a} \cdot [\bar{b} + \bar{c}] \times (\bar{a} + \bar{b} + \bar{c})$  is equal to

A.  $[\bar{a} \ \bar{b} \ \bar{c}]$

B.  $2[\bar{a} \ \bar{b} \ \bar{c}]$

C.  $3[\bar{a} \ \bar{b} \ \bar{c}]$

D. 0

**Answer: D**



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59.  $(\bar{a} + \bar{b}) \cdot (\bar{b} + \bar{c}) \times (\bar{a} + \bar{b} + \bar{c}) =$

A.  $-\bar{a} \bar{b} \bar{c}$

B.  $\bar{a} \bar{b} \bar{c}$

C. 0

D.  $2\bar{a} \bar{b} \bar{c}$

**Answer: B**



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60. If  $\bar{a} = \frac{1}{\sqrt{10}}(3\hat{i} + \hat{k})$ ,  $\bar{b} = \frac{1}{7}(2\hat{i} + 3\hat{j} - 6\hat{k})$ , then the value of  $(2\bar{a} - \bar{b}) \cdot \{(\bar{a} \times \bar{b}) \times (\bar{a} + 2\bar{b})\}$  is

A. -5

B. -3

C. 5

D. 2

Answer: A



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61. If  $\vec{p} = \frac{\vec{b} \times \vec{c}}{\vec{a} \cdot \vec{b} \cdot \vec{c}}$ ,  $\vec{q} = \frac{\vec{c} \times \vec{a}}{\vec{a} \cdot \vec{b} \cdot \vec{c}}$ ,  $\vec{r} = \frac{\vec{a} \times \vec{b}}{\vec{a} \cdot \vec{b} \cdot \vec{c}}$ , where  $\vec{a}, \vec{b}, \vec{c}$  are three non-coplanar vectors, then the value of  $(\vec{a} + \vec{b} + \vec{c}) \cdot (\vec{p} + \vec{q} + \vec{r})$  is given by

A. 3

B. 2

C. 1

D. 0

Answer: A



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62. If  $\vec{u}, \vec{v}, \vec{w}$  are three non-coplanar vectors, the  $(\vec{u} + \vec{v} - \vec{w}) \cdot (\vec{u} - \vec{v}) \times (\vec{v} - \vec{w})$  equals

- A. 0
- B.  $\vec{u} \cdot (\vec{v} \times \vec{w})$
- C.  $\vec{u} \cdot (\vec{w} \times \vec{v})$
- D.  $3\vec{u} \cdot (\vec{v} \times \vec{w})$

**Answer: B**



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63. If  $\vec{a}, \vec{b}, \vec{c}$  are three non-coplanar vectors and  $\vec{p}, \vec{q}, \vec{r}$  are defined by the

relations 
$$\vec{p} = \frac{\vec{b} \times \vec{c}}{\vec{a}\vec{b}\vec{c}}, \vec{q} = \frac{\vec{c} \times \vec{a}}{\vec{a}\vec{b}\vec{c}}, \vec{r} = \frac{\vec{a} \times \vec{b}}{\vec{a}\vec{b}\vec{c}}$$
 then

$(\vec{a} + \vec{b}) \cdot \vec{p} + (\vec{b} + \vec{c}) \cdot \vec{q} + (\vec{c} + \vec{a}) \cdot \vec{r} =$

- A. 0
- B. 1

C. 2

D. 3

**Answer: D**



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**64.** If  $a, b$  and  $c$  are non-coplanar vectors and  $d = \lambda a + \mu b + \nu c$ , then  $\lambda$  is equal to

A.  $\frac{[dbc]}{[bac]}$

B.  $\frac{[bcd]}{[bca]}$

C.  $\frac{[bdc]}{[abc]}$

D.  $\frac{[cbd]}{[abc]}$

**Answer: B**



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65. If  $\vec{u}, \vec{v}, \vec{w}$  are non-coplanar vectors and  $p, q$ , are real numbers then the equality

$$\left[ 3\vec{u} \ p \ \vec{v} \ p\vec{w} \right] - \left[ p \ \vec{v} \ \vec{w} \ q \ \vec{u} \right] - \left[ 2\vec{w} - q \ \vec{v} \ q \ \vec{u} \right] = 0 \text{ holds for}$$

- A. exactly one value of  $(p, q)$
- B. exactly two value of  $(p, q)$
- C. more than two but not all values of  $(p, q)$
- D. all values of  $(p, q)$

**Answer: A**



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66. If  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar vectors and  $\lambda$  is a real numbers then

$$\left[ \lambda(\vec{a} + \vec{b}) \ \lambda^2 \vec{b} \ \lambda \vec{c} \right] = \left[ \vec{a} \ \vec{b} + \vec{c} \ \vec{b} \right] \text{ for}$$

- A. exactly three values of  $\lambda$
- B. exactly two values of  $\lambda$

C. exactly one value of  $\lambda$

D. no value of  $\lambda$

**Answer: D**



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67. If the vectors  $2\hat{i} - 3\hat{j}$ ,  $\hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelepiped, then the volume of parallelepiped is

A. 8

B. 10

C. 4

D. 14

**Answer: C**



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68. The volumes of the parallelopiped whose edges are represented by

$$\bar{a} = 2\hat{i} - 3\hat{j} + \hat{k}, \bar{b} = \hat{i} - \hat{j} + 2\hat{k}, \bar{c} = 2\hat{i} + \hat{j} - \hat{k} \text{ is}$$

A. 14 cu. Units

B. 16 cu. Units

C. 18 cu. Units

D. 20 cu. Units

**Answer: A**



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69. If the volume of the tetrahedron formed by the coterminus edges

$\bar{a}$ ,  $\bar{b}$  and  $\bar{c}$  is 4, then the volume of the parallelopiped formed by the

coterminous edges  $\bar{a} \times \bar{b}$ ,  $\bar{b} \times \bar{c}$  and  $\bar{c} \times \bar{a}$  is

A. 144

B. 16

C. 48

D. 576

**Answer: D**



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70. The volume of a parallelepiped whose edges are represented by  $-12\bar{i} + \lambda\bar{k}$ ,  $3\bar{j} - \bar{k}$  and  $2\bar{i} + \bar{j} - 15\bar{k}$  is 546 then  $\lambda = \_ \_$

A. 3

B. 2

C.  $-3$

D.  $-2$

**Answer: C**



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71. If the three co-terminous edges of a parallelepiped are represented by  $\bar{a} - \bar{b}$ ,  $\bar{b} - \bar{c}$ ,  $\bar{c} - \bar{a}$ , then its volume is

- A.  $[\bar{a}\bar{b}\bar{c}]$
- B.  $2[\bar{a}\bar{b}\bar{c}]$
- C.  $[\bar{a}\bar{b}\bar{c}]^2$
- D. 0

**Answer: D**



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72.

If

$$\bar{a} = 2\hat{i} - 3\hat{j} + 5\hat{k}, \bar{b} = 3\hat{i} - 4\hat{j} + 5\hat{k} \text{ and } \bar{c} = 5\hat{i} - 3\hat{j} - 2\hat{k},$$

then the volume of the parallelepiped with co-terminus edges

$$\bar{a} + \bar{b}, \bar{b} + \bar{c}, \bar{c} + \bar{a} \text{ is}$$

A. 1

B. 5

C. 8

D. 16

**Answer: D**



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**73.** The volume of a tetrahedron (in cubic units) whose vertices are

$4\hat{i} + 5\hat{j} + \hat{k}$ ,  $-\hat{j} + \hat{k}$ ,  $3\hat{i} + 9\hat{j} + 4\hat{k}$  and  $-2\hat{i} + 4\hat{j} + 4\hat{k}$  is

A.  $\frac{14}{3}$

B. 5

C. 6

D. 30

**Answer: B**

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74. The vectors  $\overline{AB} = 3\hat{i} + 5\hat{j} + 4\hat{k}$  and  $\overline{AC} = 5\hat{i} - 5\hat{j} + 2\hat{k}$  are sides of a triangle  $ABC$ . The length of the median through A is

A.  $\sqrt{13}$  units

B.  $2\sqrt{5}$  units

C. 5 units

D. 10 units

**Answer: C**

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75.  $A(4, 3, 5)$ ,  $B(0, -2, 2)$  and  $C(3, 2, 1)$  are three points. The coordinates of the point in which the bisector of  $\angle BAC$  meets the side  $\overline{BC}$  is

A.  $\left(\frac{15}{8}, \frac{4}{8}, \frac{11}{8}\right)$

B.  $\left(\frac{12}{7}, \frac{2}{7}, \frac{10}{7}\right)$

C.  $\left(\frac{9}{5}, \frac{2}{5}, \frac{7}{5}\right)$

D.  $\left(\frac{3}{2}, 0, \frac{3}{2}\right)$

**Answer: A**



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76. If  $4\vec{i} + 7\vec{j} + 8\vec{k}$ ,  $2\vec{i} + 3\vec{j} + 4\vec{k}$  and  $2\vec{i} + 5\vec{j} + 7\vec{k}$  are the position vectors of the vertices of A, B and C of a triangle ABC, then the position vector of the point where the bisector of  $\angle A$  meets BC

A.  $\frac{1}{3}(6\hat{i} + 13\hat{j} + 18\hat{k})$

B.  $\frac{3}{2}(6\hat{i} + 12\hat{j} - 8\hat{k})$

C.  $\frac{1}{3}(-6\hat{i} - 8\hat{j} - 9\hat{k})$

D.  $\frac{2}{3}(-6\hat{i} - 12\hat{j} + 8\hat{k})$

**Answer: A**



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77. consider the points  $A, B, C$  and  $D$  with position vector  $7\vec{i} - 4\vec{j} + 7\vec{k}$ ,  $\vec{i} - 6\vec{j} + 10\vec{k}$ ,  $-\vec{i} - 3\vec{j} + 4\vec{k}$  and  $5\vec{i} - \vec{j} + \vec{k}$  respectively then  $ABCD$  is

- A. parallelogram but not a rhombus
- B. square
- C. rhombus
- D. rectangle

**Answer: C**



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78. In a right angled triangle ABC, the hypotenuse AB = p, then  $\vec{AB} \cdot \vec{AC} + \vec{BC} \cdot \vec{BA} + \vec{CA} \cdot \vec{CB}$  is equal to:

A.  $3p^2$

B.  $\frac{3p^2}{2}$

C.  $p^2$

D.  $\frac{p^2}{2}$

Answer: C



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79. Let  $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$  and a unit vectors  $\vec{c}$  be coplanar. If  $\vec{c}$  is perpendicular to  $\vec{a}$ , then  $\vec{c} =$

A.  $\frac{1}{\sqrt{2}}(-\hat{j} + \hat{k})$

B.  $\frac{1}{\sqrt{3}}(-\hat{i} - \hat{j} - \hat{k})$

C.  $\frac{1}{\sqrt{5}}(\hat{i} - 2\hat{j})$



$$D. \frac{1}{\sqrt{3}}(\hat{i} - \hat{j} - \hat{k})$$

**Answer: A**



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## Evaluation Test

1. Given  $\bar{a}, \bar{b}, \bar{c}$  are three non-zero vectors, no two of which are collinear. If the vector  $(\bar{a} + \bar{b})$  is collinear with  $\bar{c}$  and  $(\bar{b} + \bar{c})$  is collinear with  $\bar{a}$ , then  $\bar{a} + \bar{b} + \bar{c} =$

- A. a unit vectors
- B. a null vectors
- C. equally inclined to  $\bar{a}, \bar{b}, \bar{c}$
- D. None of these

**Answer: B**



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2. If  $\bar{a}, \bar{b}, \bar{c}$  are three non-coplanar vectors such that  $\bar{r}_1 = \bar{a} - \bar{b} + \bar{c}, \bar{r}_2 = \bar{b} + \bar{c} - \bar{a}, \bar{r}_3 = \bar{c} + \bar{a} + \bar{b}, \bar{r} = 2\bar{a} - 3\bar{b} + 4\bar{c}$ , if  $\bar{r} = \lambda_1\bar{r}_1 + \lambda_2\bar{r}_2 + \lambda_3\bar{r}_3$ , then

A.  $\lambda_1 = 7$

B.  $\lambda_1 + \lambda_3 = 3$

C.  $\lambda_1 + \lambda_2 + \lambda_3 = 5$

D.  $\lambda_3 + \lambda_2 = 2$

Answer: B



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3. Let  $a, b, c$  be distinct non-negative numbers. If the vectors  $a\hat{i} + a\hat{j} + c\hat{k}, \hat{i} + \hat{k}$  and  $c\hat{i} + c\hat{j} + b\hat{k}$  lie in a plane then  $c$  is

A. The arithmetic mean of  $a$  and  $b$

B. The geometric mean of a and b

C. The harmonic mean of a and b

D. Equal to zero

**Answer: B**



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4. The edges of a parallelepiped are of unit length and are parallel to non-coplanar unit vectors  $\vec{a}, \vec{b}, \vec{c}$  such that  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a} = 1/2$ . Then, the volume of parallelepiped is

A.  $\frac{1}{\sqrt{2}}$  cubic units

B.  $\frac{1}{2\sqrt{2}}$  cubic units

C.  $\frac{\sqrt{3}}{2}$  cubic units

D.  $\frac{1}{\sqrt{3}}$  cubic units

**Answer: A**

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5. If the vectors  $a\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} + b\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} + c\hat{k}$  ( $a \neq b \neq c \neq 1$ ) are coplanar, then the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} =$

A.  $-1$

B.  $-\frac{1}{2}$

C.  $\frac{1}{2}$

D.  $1$

**Answer: D**

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6. The value of  $a$  so that volume of parallelepiped formed by vectors  $\hat{i} + a\hat{j} + \hat{k}$ ,  $\hat{j} + a\hat{k}$ ,  $a\hat{i} + \hat{k}$  becomes minimum is

A.  $\sqrt{3}$

B. 2

C.  $\frac{1}{\sqrt{3}}$

D. 3

**Answer: C**



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7. If  $\bar{a} \cdot \bar{b} = \bar{b} \cdot \bar{c} = \bar{c} \cdot \bar{a} = 0$  then the value of  $[\bar{a} \quad \bar{b} \quad \bar{c}]$  is equal to

A. 1

B. -1

C.  $|\bar{a}| |\bar{b}| |\bar{c}|$

D. 0

**Answer: C**



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8. Let  $\bar{a} = -\hat{i} - \hat{k}$ ,  $\bar{b} = -\hat{i} + \hat{j}$  and  $\bar{c} = \hat{i} + 2\hat{j} + 3\hat{k}$  be three given vectors. If  $\bar{r}$  is a vector such that  $\bar{r} \times \bar{b} = \bar{c} \times \bar{b}$  and  $\bar{r} \cdot \bar{a} = 0$ , then the value of  $\bar{r} \cdot \bar{b}$  is

A. 4

B. 8

C. 6

D. 9

**Answer: D**



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9. If  $\bar{a}$  and  $\bar{b}$  are vectors such that

$$|\bar{a} + \bar{b}| = \sqrt{29} \text{ and } \bar{a} \times (2\hat{i} + 3\hat{j} + 4\hat{k}) = (2\hat{i} + 3\hat{j} + 4\hat{k}) \times \bar{b},$$

then a possible value of  $(\bar{a} + \bar{b}) \cdot (-7\hat{i} + 2\hat{j} + 3\hat{k})$  is

A. 0

B. 3

C. 4

D. 8

**Answer: C**



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10. If the vectors  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar and  $l, m, n$  are distinct scalars such that

$$\left[ l\vec{a} + m\vec{b} + n\vec{c} \quad l\vec{b} + m\vec{c} + n\vec{a} \quad l\vec{c} + m\vec{a} + n\vec{b} \right] = 0 \text{ then}$$

A.  $lm + mn + nl = 0$

B.  $l + m + n = 0$

C.  $l^2 + m^2 + n^2 = 0$

D.  $l^3 + m^3 + n^3 = 0$

**Answer: B**



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11. P is any point on the circumference of the circumcircle of  $\triangle ABC$ . H is the orthocentre, M is the midpoint of PH and D is the midpoint of BC.

Then

- A. DM is parallel to AC
- B. DM is perpendicular to AP
- C. DM is perpendicular to AB
- D. None of these

**Answer: B**



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12. The three vectors  $10\hat{i} + 13\hat{j} + 16\hat{k}$ ,  $30\hat{i} + 33\hat{j} + 36\hat{k}$  and  $47\hat{i} + 50\hat{j} + 53\hat{k}$  are

- A. Collinear
- B. Coplanar
- C. Non-coplanar
- D. Mutually perpendicular

**Answer: B**



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13. If the volume of parallelepiped whose concurrent edges are  $3\hat{i} - \hat{j} + 4\hat{k}$ ,  $2\hat{i} + \lambda\hat{j} - \hat{k}$  and  $-5\hat{i} + 2\hat{j} + \lambda\hat{k}$  is 110 cu. units, then the value of  $\lambda$  is

- A. 3
- B. 5

C. 0

D.  $\frac{31}{3}$

**Answer: A**



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14. If the vectors  $5\hat{i} - x\hat{j} + 3\hat{k}$  and  $-3\hat{i} + 2\hat{j} - y\hat{k}$  are parallel, the value of  $x$  and  $y$  respectively are

A.  $\frac{10}{3}, \frac{9}{5}$

B.  $-\frac{10}{3}, -\frac{9}{5}$

C.  $\frac{9}{5}, \frac{10}{3}$

D.  $-\frac{9}{5}, -\frac{10}{3}$

**Answer: A**



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15. If the position vector of  $p$  is  $3\bar{p} + \bar{q}$  and  $\bar{p}$  divides  $PQ$  internally in the ratio 3: 4, the position vector of  $Q$  is

A.  $\frac{1}{3}(5\bar{p} + 4\bar{q})$

B.  $\frac{1}{3}(4\bar{p} + 5\bar{q})$

C.  $\frac{-1}{3}(5\bar{p} + 4\bar{q})$

D.  $\frac{-1}{3}(4\bar{p} + 5\bar{q})$

**Answer: C**



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16.

$$A(\bar{a}) = 3\hat{i} + 2\hat{j}, B(\bar{b}) = 5\hat{i} + 3\hat{j} + 2\hat{k}, C(\bar{c}) = -9\hat{i} + 6\hat{j} - 3\hat{k}$$

are vectors of triangle  $ABC$ , if  $AD$  is the angle bisector of angle  $BAC$ , then the co-ordinates of the point  $D$  are

A.  $\left(-\frac{19}{8}, \frac{57}{16}, \frac{17}{16}\right)$

B.  $\left(\frac{19}{8}, \frac{57}{16}, \frac{17}{16}\right)$

C.  $\left(\frac{19}{8}, \frac{57}{16}, \frac{17}{16}\right)$

D.  $\left(\frac{19}{8}, \frac{57}{16}, \frac{17}{16}\right)$

**Answer: D**



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17. In  $\triangle ABC$  the mid points of the sides AB, BC and CA are  $(l, 0, 0)$ ,  $(0, m, 0)$  and  $(0, 0, n)$  respectively. Then,  $\frac{AB^2 + BC^2 + CA^2}{l^2 + m^2 + n^2}$

is equal to

A. 2

B. 4

C. 8

D. 16

**Answer: C**

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18. Find the coordinates of the foot of the perpendicular drawn from point  $A(1, 0, 3)$  to the join of points  $B(4, 7, 1)$  and  $C(3, 5, 3)$ .

A.  $\left(\frac{5}{3}, \frac{7}{3}, \frac{17}{3}\right)$

B.  $(5, 7, 17)$

C.  $\left(\frac{5}{7}, -\frac{7}{3}, \frac{17}{3}\right)$

D.  $\left(-\frac{5}{7}, \frac{7}{3}, \frac{17}{3}\right)$

**Answer: A**

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