



# MATHS

## BOOKS - CALCUTTA BOOK HOUSE

### MATHS (BENGALI ENGLISH)

#### AREA OF CIRCLES

##### Examples Mcq

1. In the right-angled triangle  $ABC$ ,  $\angle ABC = 90^\circ$ . If the coordinates of A

and C be (0,4) and (3,0) respectively then the area of the  $\triangle ABC$  is

A. 12 Sq-units

B. 6 Sq-units

C. 24 Sq-units

D. 8 Sq-units

**Answer:**



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2. If the points  $(0,0)$ ,  $(4,-3)$  and  $(x,y)$  are collinear, then

A.  $x = 8, y = -6$

B.  $x = 8, y = 6$

C.  $x = 4, y = -6$

D.  $x = -8, y = -6$

**Answer:**



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3. If the area of the triangle, the vertices of which are  $(2,7)$ ,  $(5, 1)$  and  $(x,3)$  is 18 Sq-units, then the value of  $x$  is

A. 10

B. 2

C. -2

D. -10

**Answer:**



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4. If the points  $(-1,3)$ ,  $(2,h)$  and  $(5,-1)$  are collinear, then the value of  $h$  is

A. 1

B. 0

C. 2

D. None of these

**Answer:**



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## Examples Short Answer Type Question

1. Examine the collinearity of the point  $(2,3)$ ,  $(4,5)$ , and  $(6,5)$  .



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2. The centroid of a triangle is  $(6,9)$  and of two its vertices are  $(15,0)$  and  $(0,10)$ . Find the coordinates of the third vertex.



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3. If the points  $(a,0)$ ,  $(0,b)$  and  $(1,1)$  are collinear , then show that  $\frac{1}{a} + \frac{1}{b} = 1$ .



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4. The coordiantes of the centroid of the triangle fromed by the points  $(x - y, y - z)$ ,  $(-x, -y)$  and  $(y, z)$  are -



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5. For what value of  $k$  the points  $(1,-1)$ ,  $(2,-1)$  and  $(k,-1)$  are collinear ?



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6. Prove that the line segment obtained by joining the points  $(1,2)$  and  $(-2,-4)$  passes through the origin.



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7. Prove that the mid-point of the line segment obtained by joining the points  $(2,1)$  and  $(6,5)$  lies on the line obtained by joining the points  $(-4,-5)$  and  $(9,8)$ .



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8. Find the area of the quadrilateral formed by the Points  $(1,4)$ ,  $(-2,1)$ ,  $(2,-3)$  and  $(3,3)$ .



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**9.** The coordinates of the vertices A, B and C of a triangle ABC are (0,5), (-1,-2) and (11,7) respectively. Find the coordinates of the foot of the perpendicular from B on AC.



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**10.** The coordinates of A of the  $\triangle ABC$  are (2,5) and the coordinates of its centroid are (-2,1). Find the coordinates of the mid-point of BC.



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11. A (-1,5), B (3,1) and C (5,7) are the vertices of the  $\triangle ABC$ . D, E and F are the mid-points of BC, CA and AB respectively. Find the area of  $\triangle DEF$  and show that  $\triangle ABC = 4\triangle DEF$ .



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12. The coordinates of the points A,B,C,D are (0,-1),(-1,2),(15,2) and (4,-5) respectively . Find the ratio in which  $\overline{AC}$  divides  $\overline{BD}$ .



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13. The vertices of the triangle ABC are (3,0), B (0,6) and C (6,9). The sides  $\overline{AB}$  and  $\overline{AC}$  of  $\triangle ABC$  are intersected by  $\overline{DE}$  at D and E respectively into a ratio of 1:2

Prove by coordinates geometry that  $\Delta ABC = 9\Delta ADE$ .



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**Exercise 3 Mcq**

1. The area of the triangle produced by the straight line  $5x + 6y = 15$  and the coordinate axes is

A.  $\frac{15}{4}$  Sq-units

B.  $\frac{25}{4}$  Sq-units

C. 15 Sq-units

D. 20 Sq-units

**Answer:**



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2. The area of the triangle with vertices A (5,2), B (-4,1) and C (0,-6) is

A.  $\frac{57}{2}$  Sq-units

B.  $\frac{67}{2}$  Sq-units

C.  $\frac{37}{2}$  Sq-units

D.  $\frac{77}{2}$  Sq-units

**Answer:**



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3. The centroid of a triangle is  $(6,4)$  and two of its vertices are  $(6,1)$  and  $(2,7)$ . The third vertex of the triangle is

A.  $(10,4)$

B.  $(10,-4)$

C.  $(4,10)$

D.  $(-4,10)$

**Answer:**



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### Exercise 3 Short Answer Type Question

1. Show that the line segment obtained by joining the points  $(5,6)$  and  $(-10,-12)$  passes through the origin.



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2. Prove that the mid-point of the line segments obtained by joining the points  $(2,1)$  and  $(6,5)$  lies on the line obtained by joining the points  $(-4,-5)$  and  $(9,8)$ .





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3. The area of the triangle with vertices  $(-1, m)$ ,  $(3, 4)$  and  $(m-2, m)$  is 1 sq. units, then find the value of  $m$ .



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4. Find the area of the triangle with vertices  $(at_1^2, 2at_1)$ ,  $(at_2^2, 2at_2)$  and  $(at_3^2, 2at_3)$



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5. Prove that the points  $(a, bc - a^2)$ ,  $(b, ca - b^2)$ ,  $(c, ab - c^2)$  are collinear.



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6. Prove that the points  $(p, p^2)$ ,  $(q, q^2)$  and  $(r, r^2)$  ( $p \neq q \neq r$ ) can never be collinear.



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### Exercise 3 Long Answer Type Question

1. Find the area of the triangle with vertices at  $\left(a, \frac{1}{a}\right)$ ,  $\left(b, \frac{1}{b}\right)$  and  $\left(c, \frac{1}{c}\right)$ .



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2. Find the length of the perpendicular drawn from P to  $\overline{QR}$  of the triangle with vertices at P (5,6), Q(-9,1) and R (-3,-1). If A be the mid-point of  $\overline{QR}$ , show that

$$PQ^2 + PR^2 = 2(AP^2 + AQ^2).$$

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3. The coordinates of A, B and C of the  $\triangle ABC$  are (3,1), (9,7) and (-3,7) respectively. If D, E and F are the mid-point of the sides  $\overline{BC}$ ,  $\overline{CA}$  and  $\overline{AB}$  respectively, then find the area of the  $\triangle DEF$ . Also show that  $\triangle ABC = 4\triangle DEF$ .

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4. If the coordinates of A, B , C and D are (6,3), (-3,5), (4,-2) and (x,3x) respectively and if

$$\frac{\Delta DBC}{\Delta ABC} = \frac{1}{2}, \text{ then show that } x = \frac{11}{8} \text{ or } \frac{3}{8}.$$



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5. If the points (a,b), (a',b') and (a-a',b-b') are collinear, then prove that  $ab' = a'b$ .



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6. Prove that  $(a,b+c)$ ,  $(b,a+c)$  and  $(c,a+b)$  are collinear.



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7. If  $P (-2,3)$ ,  $Q (4,-5)$  and  $R (-3,1)$  are the three consecutive vertices of a parallelogram, then find its area.



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**8.** Four vertices of a quadrilateral are  $(-5,5)$ ,  $(2,-4)$ ,  $(3,2)$  and  $(-2,3)$ . Find the area of the quadrilateral.



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**9.** Four vertices of a quadrilateral are  $(1,2)$ ,  $(-5,6)$ ,  $(7,-4)$  and  $(k,-2)$  and its area is zero. Find the value of  $k$ .



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**10.** The area of a quadrilateral is 28 square unit.

If the coordinates of its angular points be  $(-1,6)$

$(-2,-4)$  ,  $(3,-2)$  and  $(a,b)$  , then show that ,  $2a+b=6$

or ,  $2a+b=2$



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