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## MATHS

# BOOKS - ARIHANT MATHS (HINGLISH) 

## AREA OF BOUNDED REGIONS

Examples

1. Mark the region represtented by $3 x+4 y \leq 12$.

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2. Sketch the curve $y=x^{3}$.
3. Sketch the curve $y=x^{3}-4 x$.

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4. Sketch the curve $y=(x-1)(x-2)(x-3)$.

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5. Sketch the graph for $y=x^{2}-x$.

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6. Sketch the curve $y=\sin 2 x$.

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7. Sketch the curve $y=\sin ^{2} x$.

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8. Construct the graph for $f(x)=\frac{x^{2}-1}{x^{2}+1}$.

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9. Construct the graph for $f(x)=x+\frac{1}{x}$.

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10. Construct the graph for $f(x)=\frac{1}{1+e^{1 / x}}$.

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11. Sketch the graph $y=|x+1|$. Evaluate $\int_{-4}^{2}|x+1| d x$. What does the value of the integral represents on the graph.
12. Find the area of the region bounded by the ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$

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13. The area bounded by the hyperbola $x^{2}-y^{2}=a^{2}$ between the straight-lines $x=a$ and $x=2 a$ is given by

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14. The area inside the parabola $5 x^{2}-y=0$ but outside the parabola $2 x^{3}-y+9=0$ is

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15. The area enclosed by $y=x(x-1)(x-2)$ and x -axis, is given by
16. The area between the curve $y=2 x^{4}-x^{2}$, the $x$-axis, and the ordinates of the two minima of the curve is

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17. Sketch the curves and identify the region bounded by the curves
$x=\frac{1}{2}, x=2, y=\log x a n y=2^{x}$. Find the area of this region.

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18. Find the area given by $x+y \leq 6, x^{2}+y^{2} \leq 6 y$ and $y^{2} \leq 8 x$

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19. Find the area of the region $\left\{(x, y): 0 \leq y \leq x^{2}+1,0 \leq y \leq x+1,0 \leq x \leq 2\right\}$
20. The area common to the region determined by $y \geq \sqrt{x}$ and $x^{2}+y^{2}<2$ has the value
A. $\pi$ sq units
B. $(2 \pi-1)$ sq units
C. $\left(\frac{\pi}{4}-\frac{1}{6}\right)$ sq units
D. None of these

## Answer: C

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21. Find the area of the figure enclosed by the curve $5 x^{2}+6 x y+2 y^{2}+7 x+6 y+6=0$.
22. If $f(x)=\left\{\begin{array}{ll}\sqrt{\{x\}} & x \notin Z \\ 1 & x \in Z\end{array}\right.$ and $g(x)=\{x\}^{2}$ then area bounded by $\mathrm{f}(\mathrm{x})$ and $\mathrm{g}(\mathrm{x})$ for $x \in[0,10]$ is
A. $\frac{5}{3}$ sq units
B. 5 sq units
C. $\frac{10}{3}$ sq units
D. None of these

## Answer: C

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23. Find the area of the region bounded by the curves $y=x^{2}, y=\left|2-x^{2}\right|$, andyl $=2$, which lies to the right of the line $x=1$.
24. The area enclosed by the curve $|y|=\sin 2 x$, where $x \in[0,2 \pi]$. is
A. 1 sq unit
B. 2 sq unit
C. 3 sq unit
D. 4 sq unit

## Answer: D

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25. Let $f(x)=x^{2}, g(x)=\cos x$ and $\alpha, \beta(\alpha<\beta)$ be the roots of the equation $18 x^{2}-19 \pi x+\pi^{2}=0$. Then the area bounded by the curves $u=\operatorname{fog}(x)$, the ordinates $x=\alpha, x=\beta$ and the X -asis is
A. $\frac{1}{2}(\pi-3)$ sq units
B. $\frac{\pi}{3}$ sq units
C. $\frac{\pi}{4}$ sq units
D. None of these

## Answer: D

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26. Find the area bounded by the curves $x^{2}+y^{2}=25,4 y=\left|4-x^{2}\right|$, and $x=0$ above the $x$-axis.

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27. Find area enclosed by $|x|+|y|=1$.

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28. Let $f(x)=\max \left\{\sin x, \cos x, \frac{1}{2}\right\}$, then determine the area of region bounded by the curves $y=f(x), \mathrm{X}$-axis, Y -axis and $x=2 \pi$.
29. If A denotes the area bounded by $f(x)=\left|\frac{\sin x+\cos x}{x}\right|, \mathrm{X}$-axis, $x=\pi$ and $x=3 \pi$,then
A. $1<A<2$
B. $0<A<2$
C. $2<A<2$
D. None of these

## Answer: B

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30. If $y=f(x)$ makes positive intercepts of 2 and 1 unit on x and y coordinates axes and encloses an area of $\frac{3}{4}$ sq unit with the axes, then $\int_{0}^{2} x f^{\prime}(x) d x$, is
A. $\frac{3}{4}$
B. 1
C. $\frac{5}{4}$
D. $-\frac{3}{4}$

## Answer: D

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31. The area of the region included between the regions satisfying $\min (|x|,|y|) \geq 1$ and $x^{2}+y^{2} \leq 5$ is
A. $\frac{5}{2}\left(\frac{\sin ^{-1}(2)}{\sqrt{5}}-\frac{\sin ^{-1}(q)}{\sqrt{5}}\right)-4$
B. $10\left(\frac{\sin ^{-1}(2)}{\sqrt{5}}-\frac{\sin ^{-1}(q)}{\sqrt{5}}\right)-4$
C. $\frac{2}{5}\left(\frac{\sin ^{-1}(2)}{\sqrt{5}}-\frac{\sin ^{-1}(q)}{\sqrt{5}}\right)-4$
D. $15\left(\frac{\sin ^{-1}(2)}{\sqrt{5}}-\frac{\sin ^{-1}(q)}{\sqrt{5}}\right)-4$

## Answer: B

32. The area of the region bounded by the curves $y=\sqrt{\frac{1+\sin x}{\cos x}}$ and $y=\sqrt{\frac{1-\sin x}{\cos x}}$ bounded by the lines $\mathrm{x}=0$ and $x=\frac{\pi}{4}$ is
A. $\int_{0}^{\sqrt{2}-1} \frac{t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$
B. $\int_{0}^{\sqrt{2}-1} \frac{4 t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$
C. $\int_{0}^{\sqrt{2}=1} \frac{4 t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$
D. $\int_{0}^{\sqrt{2}+1} \frac{t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$

## Answer: B

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33. Let T be the triangle with vertices $(0,0),\left(0, c^{2}\right)$ and $\left(c, c^{2}\right)$ and let R be the region between $y=c x$ and $y=x^{2}$ where $c>0$ then
A. Area $(R)=\frac{c^{3}}{6}$
B. Area of $R=\frac{c^{3}}{3}$
C. $c \rightarrow 0^{+} \frac{\operatorname{Area}(T)}{\operatorname{Area}(R)}=3$
D. $c \rightarrow 0^{+} \frac{\operatorname{Area}(T)}{\operatorname{Area}(R)}=\frac{3}{2}$

## Answer: A: C

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34. Suppose fis defined from $R \rightarrow[-1,1]$ as $f(x)=\frac{x^{2}-1}{x^{2}+1}$ where R is the set of real number .then the statement which does not hold is
A. $f$ is many-one onto
B. f increases for $x>0$ and decreases for $x<0$
C. minimum value is not attained even though $f$ is bounded
D. the area included by the curve $y-f(x)$ and the line $y=1$ is $\pi$ sq units

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35. Consider $f(x)=\left\{\begin{array}{ll}\cos x & 0 \leq x<\frac{\pi}{2} \\ \left(\frac{\pi}{2}-x\right)^{2} & \frac{\pi}{2} \leq x<\pi\end{array}\right.$ such that f is periodic with period $\pi$. Then which of the following is not true?
A. the range of f is $\left[0, \frac{\pi^{2}}{4}\right)$
B. $f$ is continuous for all real $x$, but not defferentiable for some real $x$
C. $f$ is continuous fo all real $x$
D. the area bounded by $y=f(x)$ and the X -axis for $x=n \pi$ to

$$
x=n \pi \text { is } 2 n\left(1+\frac{\pi^{2}}{24}\right) \text { for a given } n \in N
$$

## Answer: A::D

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36. Consider the functions $\mathrm{f}(\mathrm{x})$ and $\mathrm{g}(\mathrm{x})$, both defined from $R \rightarrow R$ and are defined as $f(x)=2 x-x^{2}$ and $g(x)=x^{n}$ where $n \in N$. If the area
between $f(x)$ and $g(x)$ is $1 / 2$, then the value of $n$ is
A. 12
B. 15
C. 20
D. 30

## Answer: B::C::D

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37. The area of the region bounded by the curve $y=e^{x}$ and lines $\mathrm{x}=0$ and $y=e$ is
A. $e-1$
B. $\int_{1}^{e} \operatorname{In}(e+1-y) d y$
C. $e-\int_{0}^{1} e^{x} d x$
D. $\int_{0}^{e} I n y d y$

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38. Number of positive integers $x$ for which
$f(x)=x^{3}-8 x^{2}+20 x-13$ is a prime number is $\qquad$ .
A. 1
B. 2
C. 3
D. 4

## Answer: C

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39. Consider the function $f(x)=x^{3}-8 x^{2}+20 x-13$

The function $f(x)$ defined for $R \rightarrow R$
A. is one-one onto
B. is many-one onto
C. has 3 real roots
D. is such that $f\left(x_{1}\right) \cdot f\left(x_{2}\right)<0$ where $x_{1}$ and $x_{2}$ are the roots of

$$
f^{\prime}(x)=0
$$

## Answer: B

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40. Consider the function $f(x)=x^{3}-8 x^{2}+20 x-13$

Area enclosed by $y=f(x)$ and the coordinate axes is
A. $65 / 12$
B. $13 / 12$
C. $71 / 12$
D. None of these

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41. Let $h(x)-f(x)-g(x)$ where $f(x)=\sin ^{4} \pi x$ and $g(x)=I n x$. Let $x_{0}, x_{1}, x_{2}, \ldots \ldots, x_{n-1}$ be the roots of $f(x)=g(x)$ in increasing oder.Then the absolute area enclosed by $y=f(x)$ and $y=g(x)$ is given by
A. $\sum_{r=0}^{n} \int_{x_{r}}^{x_{r+1}}(-1)^{r} h(x) d x$
B. $\sum_{r=0}^{n} \int_{x_{r}}^{x_{r+1}}(-1)^{r+1} h(x) d x$
C. $2 \sum_{r=0}^{n} \int_{x_{r}}^{x_{r+1}}(-1)^{r} h(x) d x$
D. $\frac{1}{2} \sum_{r=0}^{n} \int_{x_{r}}^{x_{r+1}}(-1)^{r+1} h(x) d x$

## Answer: A

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42. Let $h(x)=f(x)=f_{x}-g_{x}$, where $f_{x}=\sin ^{4} \pi x$ and $g(x)=\operatorname{In} x$. Let $x_{0}, x_{1}, x_{2}, \ldots ., x_{n+1}$ be the roots of $f_{x}=g_{x}$ in increasing order. In the above question, the value of $n$ is
A. 1
B. 2
C. 3
D. 4

## Answer: B

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43. Let $h(x)-f(x)-g(x)$ where $f(x)=\sin ^{4} \pi x$ and $g(x)=\operatorname{In} x$. Let $x_{0}, x_{1}, x_{2}, \ldots \ldots, x_{n-1}$ be the roots of $f(x)=g(x)$ in increasing oder.Then the absolute area enclosed by $y=f(x)$ and $y=g(x)$ is given by
A. $\frac{11}{8}$
B. $\frac{8}{3}$
C. 2
D. $\frac{13}{3}$

## Answer: A

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44. Consider the function defined implicitly by the equation $y^{3}-3 y+x=0$ on various intervals in the real line. If $x \in(-\infty,-2) \cup(2, \infty)$, the equation implicitly defines a unique realvalued defferentiable function $y=f(x)$. If $x \in(-2,2)$, the equation implicitly defines a unique real-valud diferentiable function $y-g(x)$ satisfying $g_{0}=0$. If $f(-10 \sqrt{2})=2 \sqrt{2}$, then $f^{\prime \prime}(-10 \sqrt{2})$ is equal to
A. $\frac{4 \sqrt{2}}{7^{3} 3^{2}}$
B. $-\frac{4 \sqrt{2}}{7^{3} 3^{2}}$
C. $\frac{4 \sqrt{2}}{7^{3} 3}$
D. $-\frac{4 \sqrt{2}}{7^{3} 3}$

## Answer: B

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45. Consider the function defined implicitly by the equation $y^{3}-3 y+x=0$ on various intervals in the real line. If $x \in(-\infty,-2) \cup(2, \infty)$, the equation implicitly defines a unique realvalued defferentiable function $y=f(x)$. If $x \in(-2,2)$, the equation implicitly defines a unique real-valud diferentiable function $y-g(x)$ satisfying $g_{0}=0$.

The area of the region bounded by the curve $y=f(x)$, the X -axis and the line $x=a$ and $x=b$, where $-\infty<a<b<-2$ is
A. $\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x+b y(b)-a f(a)$
B. $-\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x-b y(b)+a f(a)$
C. $\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x-b y(b)+a f(a)$
D. $-\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x+b y(b)=a f(a)$

## Answer: A

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46. Consider the function defined implicitly by the equation $y^{3}-3 y+x=0$ on various intervals in the real line. If $x \in(-\infty,-2) \cup(2, \infty)$, the equation implicitly defines a unique realvalued defferentiable function $y=f(x)$. If $x \in(-2,2)$, the equation implicitly defines a unique real-valud diferentiable function $y-g(x)$ satisfying $g_{0}=0$.

If $f(-10 \sqrt{2})=2 \sqrt{2}$, then $f(-10 \sqrt{2})$ is equal to
A. $2 g(-1)$
B. 0
C. $-2 g(1)$
D. $2 g(1)$

## Answer: D

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47. Find the total area bounded by the curve $y=\cos x-\cos ^{2} x$ and $y=x^{2}\left(x^{2}-\frac{\pi^{2}}{4}\right)$

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48. A curve $y=f(x)$ passes through point $P(1,1)$. The normal to the curve at $P$ is a $(y-1)+(x-1)=0$. If the slope of the tangent at any point on the curve is proportional to the ordinate of the point, then the equation of the curve is (a)
(b) $(c) y=(d) e^{(e)(f) K((g)(h) x-1(i))(j)}(k)(l) \quad$ (m)
$(n)(o) y=(p) e^{(q)(r) K e(s)}(t)(u)$
(d) $(e) y=(f) e^{(g)(h) K((i)(j) x-2(k))(l)}(m)(n)$ (o) (d) None of these
49. Sketch the region bounded by the curves $y=x^{2} a n d y=\frac{2}{1+x^{2}}$. Find the area.

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50. Find the area enclosed between the curves:
$y=\log _{e}(x+e), x=\log _{e}\left(\frac{1}{y}\right) \&$ the $x$-axis.

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51. Find the area of the region bounded by the curve $C: y=\tan x, \tan \geq n t d r a w n \rightarrow C$ at $x=\frac{\pi}{4}$, and the $x$-axis.

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52. Find all the possible values of $b>0$, so that the area of the bounded region enclosed between the parabolas $y=x-b x^{2} a n d y=\frac{x^{2}}{b}$ is maximum.

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53. Let $C_{1}$ and $C_{2}$, be the graph of the functions $y=x^{2}$ and $y=2 x, 0 \leq x \leq 1$ respectively. Let $C_{3}$, be the graph of a function $y-(f x), 0 \leq x \leq 1, f(0)=0$. For a point Pand $C_{2}$, let the lines through P , parallel to the axes, meet $C_{2}$ and $C_{3}$, at Q and R respectively. If for every position of P (on $C_{1}$ ), the areas of the shaded regions $O P Q$ and $O R P$ are equal, determine the function $f(x)$.

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54. The area of the region bounded by the curves $y=e x \log x$ and $y=\frac{\log x}{e x}$ is
55. Let $A_{n}$ be the area bounded by the curve $y=(\tan x)^{n}$ and the lines $x=0, y=0$, and $x=\frac{\pi}{4}$. Prove that for $n>2, A_{n}+A_{n-2}=\frac{1}{n-1}$ and deduce $1 /(2 n+2)$

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56. Consider a square with vertices at $(1,1),(-1,1),(-1,-1), \operatorname{and}(1,-1)$. Set $S$ be the region consisting of all points inside the square which are nearer to the origin than to any edge. Sketch the region $S$ and find its area.

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57. The area of the region included between the curves $x^{2}+y^{2}=a^{2}$ and $\sqrt{|x|}+\sqrt{|y|}=\sqrt{a}(a>0)$ is
58. Show that the area included between the parabolas $y^{2}=4 a(x+a)$ and $y^{2}=4 b(b-x)$ is $\frac{8}{3} \sqrt{a b}(a+b)$.

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59. Determine the area of the figure bounded by two branches of the curve $(y-x)^{2}=x^{3}$ and the straight line $x=1$.

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60. Prove that the areas $S_{0}, S_{1}, S_{2}$...bounded by the X-axis and half-waves of the curve $y=e^{-a x} \sin \beta x, x \mid 0$.from a geometric progression with the common ratio $g=e^{-\pi \alpha / \beta}$.

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61. Let $b \neq 0$ and for $j=0,1,2, \ldots, n$. Let $S_{j}$ be the area of the region bounded by $Y_{-}$axis and the curve $x \cdot e^{a y}=\sin b y, \frac{j \pi}{b} \leq y \leq \frac{(j+1) \pi}{b}$. Show that $S_{0}, S_{1}, S_{2}, \ldots S_{n}$ are in geometric progression. Also, find their sum for $a=-1$ and $b=\pi$.

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62. For any real $t, x=\frac{1}{2}\left(e^{t}+e^{-t}\right), y=\frac{1}{2}\left(e^{t}-e^{-t}\right)$ is a point on the hyperbola $x^{2}-y^{2}=1$ Show that the area bounded by the hyperbola and the lines joining its centre to the points corresponding to $t_{1}$ and $-t_{1}$ is $t_{1}$.

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63. Find the area enclosed by circle $x^{2}+y^{2}=4$, parabola $y=x^{2}+x+1$, the curve $y=\left[\frac{\sin ^{2} x}{4}+\frac{\cos x}{4}\right]$ and X -axis (where,[.] is the greatest integer function.
64. Let $f(x)=\operatorname{Ma\xi \mu m}\left\{x^{2},(1-x)^{2}, 2 x(1-x)\right\}$, where $0 \leq x \leq 1$. Determine the area of the region bounded by the curves $y=f(x), x-a \xi s, x=0$, and $x=1$.

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65. Find the ratio in which the curve, $y=\left[-0.01 x^{4}-0.02 x^{2}\right]$ [where, [.] denotes the greatest integer function) divides the ellipse ( $\left.3 x^{2}+4 y^{2}\right)=12$.

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66. Let

$$
f(x)= \begin{cases}-2 & -3 \leq x \leq 0 \\ x-2 & 0<x \leq 3\end{cases}
$$

where
$g(x)=\min \{f(|x|)+|f(x)|, f(|x|)-|f(x)|\}$. Find the area bounded by the curve $g(x)$ and the X -axis between the ordinates at $x=3$ and $x=-3$.

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67. Let $A B C$ be a triangle with vertices $A \equiv(6,2 \sqrt{3}+1))), B \equiv(4,2)$ and $C \equiv(8,2)$. Let R be the region consisting of all those points P inside $\triangle A B C$ which satisfyd $(P, B C) \geq \max \{d(P, A B) ; d(P, A C)\}$, where $\mathrm{d}(\mathrm{P}, \mathrm{L})$ denotes the distance of the point from the line $L$, then

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68. Let $O(0,0), A(2,0)$, $\operatorname{and} B\left(1 \frac{1}{\sqrt{3}}\right)$ be the vertices of a triangle. Let $R$ be the region consisting of all those points $P$ inside $O A B$ which satisfy $d(P, O A) \leq \min [d(p, O B), d(P, A B)]$, where $d$ denotes the distance from the point to the corresponding line. Sketch the region $R$ and find its area.

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69. A curve $y=f(x)$ passes through the origin. Through any point $(x, y)$ on the curve, lines are drawn parallel to the co-ordinate axes. If the curve divides the area formed by these lines and co-ordinates axes in the ratio $m: n$, find the curve.

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70. Find the ratio of the areas in which the curve $y=\left[\frac{x^{3}}{100}+\frac{x}{35}\right]$ divides the circle $x^{2}+Y^{2}-4 x+2 y+1=0$. (where, [.] denotes the greated integer function).

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71. Area bounded by the line $\mathrm{y}=\mathrm{x}$, curve $y=f(x),(f(x)>x, \forall x>1)$ and the lines $\mathrm{x}=1, \mathrm{x}=\mathrm{t}$ is $\left(t-\sqrt{1+t^{2}}-(1+\sqrt{2})\right)$ for all $t>1$. Find $f(x)$.
72. The area bounded by the curve $y=f(x), \mathrm{X}$-axis and ordinates $\mathrm{x}=1$ and $\mathrm{x}=\mathrm{b}$ is $(b-1) \sin (3 b+4)$, find $f(x)$.

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73. Find the area of region enclosed by the curve $\frac{(x-y)^{2}}{a^{2}}+\frac{(x+y)^{2}}{b^{2}}=2(a>b)$, the line $\mathrm{y}=\mathrm{x}$ and the positive X -axis.

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74. Let $\mathrm{f}(\mathrm{x})$ be a function which satisfy the equation $f(x y)=f(x)+f(y)$ for all $x>0, y>0$ such that $f^{\prime}(1)=2$. Find the area of the region bounded by the curves $y=f(x), y=\left|x^{3}-6 x^{2}+11 x-6\right|$ and $x=0$.

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75. Find the area of the region which is inside the parabola satisfying the condition $|x-2 y|+|x+2 y| \leq 8$ and $x y \geq 2$.

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76. Consider the function $f(x)=\left\{\begin{array}{ll}x-[x]-\frac{1}{2} & x \notin \\ 0 & x \in I\end{array}\right.$ where [.] denotes the fractional integral function and $I$ is the set of integers. Then find $g(x)$ max $\cdot\left[x^{2}, f(x),|x|\right\},-2 \leq x \leq 2$.

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77. Find the area of the region bounded by $y=f(x), y=|g(x)|$ and the lines $x=0, x=2$, where $\mathrm{f}, \mathrm{g}$ are continuous function satisfying
$f(x+y)=f(x)+f(y)-8 x y, \forall x, y \in R$ and
$g(x+y)=g(x)+g(y)+3 x y(x+y), \forall x, y \in R \quad$ also
$f^{\prime}(0)=8$ and $g^{\prime}(0)=-4$.
78. Find the area of the region bounded by the curves $y=x^{2}$ and $y=\sec ^{-1}\left[-\sin ^{2} x\right]$, where [.] denotes G.I.F.

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79. Draw a graph of the function $f(x)=\cos ^{-1}\left(4 x^{3}-3 x\right), x \in[-1,1]$ and find the ara enclosed between the graph of the function and the $x$ axis varies from 0 to 1 .

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80. Consider two curves $y^{2}=4 a(x-\lambda)$ and $x^{2}=4 a(y-\lambda)$, where $a>0$ and $\lambda$ is a parameter. Show that
(i) there is a single positive value of $\lambda$ for which the two curves have exactly one point of intersection in the 1st quadrant find it.
(ii) there are infinitely many nagetive values of $\lambda$ for which the two curves have exactly one points of intersection in the 1st quadrant.
(iii) if $\lambda=-a$, then find the area of the bounded by the two curves and the axes in the 1st quadrant.

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81. Let $f(x)$ be continuous function given by $f(x)=\left\{2 x,|x| \leq 1 x^{2}+a x+b,|x|>1\right\}$. Find the area of the region in the third quadrant bounded by the curves $x=-2 y^{2}$ andy $=f(x)$ lying on the left of the line $8 x+1=0$.

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82. Let $[x]$ denotes the greatest integer function. Draw a rough sketch of the portions of the curves $x^{2}=4[\sqrt{x}] y$ and $y^{2}=4[\sqrt{y}] x$ that lie within the square $\{(x, y) \mid 1 \leq x \leq 4,1 \leq y \leq 4\}$. Find the area of the part of the square that is enclosed by the two curves and the line $x+y=3$.
83. The value of the parameter $a(a \geq 1)$ for which the area of the figure bounded by the pair of staight lines $y^{2}-3 y+2=0$ and the curves $y=[a] x^{2}, y=\frac{1}{2}[a] x^{2}$ is greatest is (Here [.] denotes the greatest integer function). (A) $[0,1)$ (B) $[1,2)$ (C) $[2,3)$ (D) $[3,4)$

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84. Find the area in the $1^{*}$ quadrant bounded by $[x]+[y]=n$, where $n \in N$ and $y=k$ (where $k \in n \forall k \leq n+1$ ), where [.] denotes the greatest integer less than or equal to x .

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## Exercise For Session 1

1. Draw a rough sketch of $y=\sin 2 x$ and determine the area enclosed by
the curve. X-axis and the lines $x=\pi / 4$ and $x=3 \pi / 4$.

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2. Find the area under the curve $y=\left(x^{2}+2\right)^{2}+2 x$ between the ordinates $\mathrm{x}=0$ and $\mathrm{x}=2^{\text {` }}$
A. $\frac{236}{14}$ sq units
B. $\frac{136}{14}$ sq units
C. $\frac{430}{14}$ sq units
D. $\frac{436}{14}$ sq units

Answer: $\frac{436}{14}$ sq units

## - Watch Video Solution

3. Find by integration the area of the region bounded by the curve $y=2 x-x^{2}$ and the $x$-axis.
A. $\frac{1}{3}$ sq units
B. $\frac{2}{3}$ sq units
C. $\frac{4}{3}$ sq units
D. $\frac{5}{3}$ sq units

Answer: $\frac{4}{3}$ sq units

## - Watch Video Solution

4. Examples: Find the area of the region bounded by the curve $y^{2}=2 y-x$ and the $y$-axis.

## - Watch Video Solution

5. Find the area bounded by the curve $y=4-x^{2}$ and the line $y=0$ and $y=3$.

## - Watch Video Solution

6. Find the area bounded by $x=a t^{2}$ and $y=2 a t$ between the ordinates corresponding to $t=1$ and $t=2$.

## - Watch Video Solution

7. Find the area of the parabola $y^{2}=4 a x$ and the latusrectum.

## - Watch Video Solution

8. Find the area bounded by $y=1+2 \sin ^{2} x$, X -axis, $X=0$ and $x=\pi$.

## - Watch Video Solution

9. Sketch the graph of $y=\sqrt{x}+\operatorname{in}[0,4]$ and determine the area of the region enclosed by the curve, the axis of X and the lines $x=0, x=4$.

## - Watch Video Solution

10. The area of the region bounded by the curve $x y-3-2 y-10=0$, X -axis and the lines $x=3, x=4$, is

## Watch Video Solution

## Exercise For Session 2

1. The area of the region bounded by $y^{2}=2 x+1$ and $x-y-1=0$ is
A. $2 / 3$
B. $4 / 3$
C. $8 / 3$
D. $16 / 3$

Answer: D
2. The area of the region bounded by the curve $y=2 x-x^{2}$ and the line $y=x$ is
A. $9 / 2$
B. $43 / 6$
C. $35 / 6$
D. None of these

## Answer: A

## - Watch Video Solution

3. The area bounded by the curve $y=x|x|, \mathrm{x}$-axis and the ordinates $x=1, x=-1$ is given by
A. 0
B. $1 / 3$
C. $2 / 3$
D. None of these

## Answer: C

## - Watch Video Solution

4. Area of the region bounded by the curves
$y=2^{x}, y=2 x-x^{2}, x=0$ and $x=2$ is given by :
A. $\frac{3}{\log 2}-\frac{4}{3}$
B. $\frac{3}{\log 2}+\frac{4}{3}$
C. $3 \log 2-\frac{4}{3}$
D. None of these

Answer: D

## - Watch Video Solution

5. What is the area bounded by the curves $y=e^{x}, y=e^{-x}$ and the straight line $x=1$ ?
A. $e+\frac{1}{e}$
B. $e-\frac{1}{e}$
C. $e+\left(\frac{1}{e}\right)-2$
D. None of these

## Answer: A

## - Watch Video Solution

6. Area (in square units) of the region bounded by the curve $y^{2}=4 x, y$ axis and the line $y=3$, is
A. 2
B. $\frac{9}{4}$
C. $6 \sqrt{3}$
D. None of these

## Answer: B

## - Watch Video Solution

7. The area of the region bounded by $y=\sin x, y=\cos x$ in the first quadrant is
A. $2(\sqrt{2-1})$
B. $\sqrt{3}+1$
C. $2(\sqrt{3}-1)$
D. None of these

## Answer: A

## - Watch Video Solution

8. The area bounded by the curves $y=x e^{x}, y=x e^{-x}$ and the line $x=1$ is $\frac{2}{e}$ squinits (b) $1-\frac{2}{e}$ squinits $\frac{1}{e}$ sqünits (d) $1-\frac{1}{e}$ squinits
A. $\frac{2}{e}$
B. $1-\frac{2}{e}$
C. $\frac{1}{e}$
D. $1-\frac{1}{e}$

## Answer: A

## - Watch Video Solution

9. The figure into which the curve $y^{2}=6 x$ divides the circle $x^{2}+y^{2}=16$ are in the ratio
A. $\frac{2}{3}$
B. $\frac{4 \pi-\sqrt{3}}{8 \pi+\sqrt{3}}$
C. $\frac{4 \pi+\sqrt{3}}{8 \pi-\sqrt{3}}$
D. None of these

## Answer: C

## - Watch Video Solution

10. Find the area bounded by the $y$-axis,
$y=\cos x, a n d y=\sin x w h e n 0 \leq x \leq \frac{\pi}{2}$.
A. $2(\sqrt{2-1})$
B. $\sqrt{2}-1)$
C. $(\sqrt{2}+1)$
D. $\sqrt{2}$

## Answer: B

## - Watch Video Solution

11. The area bounded by the curve $y=\frac{3}{|x|}$ and $y+|2-x|=2$ is
A. $\frac{4-\log 27}{3}$
B. $2-\log ^{3}$
C. $2+\log ^{3}$
D. None of these

## Answer: D

## Watch Video Solution

12. The area bounded by the curves $y=-x^{2}+2$ and $y=2|x|-x$ is
A. $2 / 3$
B. $8 / 3$
C. $4 / 3$
D. None of these

## - Watch Video Solution

13. The are bounded by the curve $y^{2}=4 x$ and the circle $x^{2}+y^{2}-2 x-3=0$ is
A. $2 \pi+\frac{8}{3}$
B. $4 \pi+\frac{8}{3}$
C. $\pi+\frac{8}{3}$
D. $\pi-\frac{8}{3}$

## Answer: A

## - Watch Video Solution

14. A point $P$ moves inside a triangle formed by $A(0,0), B\left(1, \frac{1}{\sqrt{3}}\right), C(2,0)$ such that $\min \{P A, P B, P C)=1$, then
the area bounded by the curve traced by P , is
A. $3 \sqrt{3}-\frac{3 \pi}{2}$
B. $\sqrt{3}+\frac{\pi}{2}$
C. $\sqrt{3}-\frac{\pi}{2}$
D. $3 \sqrt{3}+\frac{3 \pi}{2}$

## Answer: C

## - View Text Solution

15. The graph of $y^{2}+2 x y+40|x|=400$ divides the plane into regions.

Then the area of the bounded region is 200squinits (b) 400squnits 800squinits (d) 500squinits
A. 400
B. 800
C. 600
D. None of these

## Answer: B

## - Watch Video Solution

16. The aera of the region defined by $||x|-|y|| \leq 1$ and $x^{2}+y^{2} \leq 1$ in the xy plane is
A. $\pi$
B. $2 \pi$
C. $3 \pi$
D. 1

## Answer: A

17. The area of the region defined by $1 \leq|x-2|+|y+1| \leq 2$ is (a) 2
(b) 4 (c) 6 (d) non of these
A. 2
B. 4
C. 6
D. None of these

## Answer: C

## - Watch Video Solution

18. The area of the region enclosed by the curve $|y|=-(1-|x|)^{2}+5$, is
A. $\frac{8}{3}(7+5 \sqrt{5})$ sq units
B. $\frac{2}{3}(7+5 \sqrt{5})$ sq units
C. $\frac{2}{3}(5 \sqrt{5}-7)$ sq units
D. None of these

## Answer: A

## - Watch Video Solution

19. The area bounded by the
curve
$f(x)=||\tan x+\cot x|-|\tan x-\cot x||$ between the lines
$x=0, x=\frac{\pi}{2}$ and the X -axis is
A. $\log 4$
B. $\log \sqrt{2}$
C. $2 \log 2$
D. $\sqrt{2} \log 2$

## Answer: A

## - Watch Video Solution

20. If $f(x)=\max \left\{\sin x, \cos x, \frac{1}{2}\right\}$, then the area of the region bounded by the curves $y=f(x), \mathrm{x}$-axis, Y -axis and $x=\frac{5 \pi}{3}$ is
A. $\left(\sqrt{2}-\sqrt{3}+\frac{5 \pi}{12}\right)$ sq units
B. $\left(\sqrt{2}+\frac{\sqrt{3}}{2}+\frac{5 \pi}{2}\right)$ sq units
C. $\left(\sqrt{2}+\sqrt{3}+\frac{5 \pi}{2}\right)$ sq units
D. None of these

## Answer: B

## - Watch Video Solution

## Exercise Single Option Correct Type Questions

1. A point $P(x, y)$ moves such that $[x+y+1]=[x]$. Where [.] denotes greatest intetger function and $x \in(0,2)$, then the area represented by all the possible position of $P$, is
A. $\sqrt{2}$
B. $2 \sqrt{2}$
C. $4 \sqrt{2}$
D. 2

## Answer: D

## - Watch Video Solution

2. If $f:[-1,1] \rightarrow\left[-\frac{1}{2}, \frac{1}{2}\right], f(x)=\frac{x}{1+x^{2}}$, then find the area bounded by $y=f^{-1}(x), x$ axis and lines $x=\frac{1}{2}, x=-\frac{1}{2}$.
A. $\frac{1}{2} \log e$
B. $\log \left(\frac{e}{2}\right)$
C. $\frac{1}{2} \frac{\log e}{3}$
D. $\frac{1}{2} \log \left(\frac{e}{2}\right)$

## Answer: B

3. If the length of latusrectum of ellipse
$E_{1}: 4(x+y+1)^{2}+2(x-y+3)^{2}=8$ and
$E_{2}=\frac{x^{2}}{p}+\frac{y^{2}}{p^{2}}=1,(0<p<1)$ are equal , then area of ellipse $E_{2}$, is
A. $\frac{\pi}{2}$
B. $\frac{\pi}{\sqrt{2}}$
C. $\frac{\pi}{2 \sqrt{2}}$
D. None of these

## Answer: B

## - Watch Video Solution

4. The area of bounded by the curve
$4\left|x-2017^{2017}\right|+5\left|y-2017^{2017}\right| \leftarrow 20$, is
A. 60
B. 50
C. 40
D. 30

## Answer: C

## - Watch Video Solution

5. If the area bounded by the corve $y=x^{2}+1, y=x$ and the pair of lines $x^{2}+y^{2}+2 x y-4 x-4 y+3=0$ is K units, then the area of the region bounded by the curve $y=x^{2}+1, y=\sqrt{x-1}$ and the pair of lines $(x+y-1)(x+y-3)=0$ is
A. K
B. 2 K
C. $\frac{K}{2}$
D. None of these

## D Watch Video Solution

6. Suppose $y=f(x)$ and $y=g(x)$ are two continuous functiond whose graphs intersect at the three points $(0,4),(2,2)$ and $(4,0)$ with $f(x)>g(x)$ for $0<x<2$ and $f(x)<g(x)$ for $2<x<4$. If $\int_{0}^{4}[f(x)-g(x)] d x=10$ and $\int_{2}^{4}[g(x)-f(x)] d x=5 \quad$ the $\quad$ area between two curves for $0<x<2$,is (A) 5 (B) 10 (C) 15 (D) 20
A. 5
B. 10
C. 15
D. 20

## Answer: C

7. Let 'a' be a positive constant number. Consider two curves $C_{1}: y=e^{x}, C_{2}: y=e^{a-x}$. Let S be the area of the part surrounding by $C_{1}, C_{2}$ and the $y$ axis, then $\operatorname{Lim}_{a \rightarrow 0} \frac{s}{a^{2}}$ equals (A) 4 (B) $\frac{1}{2}$ (C) 0 (D) $\frac{1}{4}$
A. 4
B. $\frac{1}{2}$
C. 0
D. 1.4

## Answer: D

## - Watch Video Solution

8. 3 point $\mathrm{O}(0,0), P\left(a, a^{2}\right), Q\left(-b, b^{2}\right)(a>0, b>0)$ are on the parabola $y=x^{2}$. Let $S_{1}$ be the area bounded by the line PQ and parabola let $S_{2}$ be the area of the $\triangle O P Q$, the minimum value of $S_{1} / S_{2}$ is
A. $2 / 3$
B. $5 / 3$
C. 2
D. 73

## Answer: A

## - Watch Video Solution

9. Area enclosed by the graph of the function $y=\operatorname{In}^{2} x-1$ lying in the $4^{\text {th }}$ 'quadrant is
A. $\frac{2}{e}$
B. $\frac{4}{e}$
C. $2\left(e+\frac{1}{e}\right)$
D. $4\left(e-\frac{1}{e}\right)$

## Answer: B

10. The area bounded by $y=2-|2-x|$ and $y=\frac{3}{|x|}$ is
A. $\frac{4-3 \ln 3}{2}$
B. $\frac{4+3 \ln 3}{2}$
C. $\frac{3}{2}+I n 3$
D. $\frac{1}{2}+I n 3$

## Answer: A

## - Watch Video Solution

11. Suppose $g(x)=2 x+1$ and $h(x)=4 x^{2}+4 x+5 \quad$ and $h(x)=(f o g)(x)$. The area enclosed by the graph of the function $y=f(x)$ and the pair of tangents drawn to it from the origin, is
A. $8 / 3$
B. $16 / 3$
C. $32 / 3$
D. None of these

## Answer: B

## - Watch Video Solution

12. The area bounded by the curves $y=-\sqrt{-x}$ and $x=-\sqrt{-y}$ where $x, y \leq 0$
A. cannot be determined
B. is $\frac{1}{3}$
C. is $\frac{2}{3}$
D. is same as that of the figure bounded by the curves

$$
y=\sqrt{-x}, x \leq 0 \text { and } x=\sqrt{-y}, y \leq 0
$$

## Answer: B

13. $y=f(x)$ is a function which satisfies $f(0)=0, f^{\prime \prime}(x)=f^{\prime}(x)$ and $f^{\prime}(0)=1$ then the area bounded by the graph of $y=f(x)$, the lines $x=0, x-1=0$ and $y+1=0$ is
A.e
B. e-2
C. e-1
D. $\mathrm{e}+1$

## Answer: C

## - Watch Video Solution

14. Aea of the region nclosed between the curves $x=y^{2}-1$ and $x=|y| \sqrt{1-y^{2}}$ is
A. 1
B. $4 / 3$
C. $2 / 3$
D. 2

## Answer: D

## - Watch Video Solution

15. The area bounded by the curve $y=x e^{-x} ; x y=0$ and $x=c$ where c is the $x$-coordinate of the curve's inflection point, is
A. $1-3 e^{-2}$
B. $1-2 e^{-2}$
C. $1-e^{-2}$
D. 1

## Answer: A

16. If $(a, 0)$, agt 0 , is the point where the curve $y=\sin 2 x-\sqrt{3} \sin x$ cuts the $x$-axis first, $A$ is the area bounded by this part of the curve, the origin and the positive $x$-axis. Then
A. $4 A+8 \cos a=7$
B. $4 A+8 \sin a=7$
C. $4 A-8 \sin a=7$
D. $4 A-8 \cos a=7$

## Answer: A

## - Watch Video Solution

17. The curve $y=a x^{2}+b x+c$ passes through the point $(1,2)$ and its tangent at origin is the line $y=x$. The area bounded by the curve, the ordinate of the curve at minima and the tangent line is
A. $\frac{1}{24}$
B. $\frac{1}{12}$
C. $\frac{1}{8}$
D. $\frac{1}{6}$

## Answer: A

## - Watch Video Solution

18. A function $y=f(x)$ satisfies the differential equation $\frac{d y}{d x}-y=\cos x-\sin x$ with initial condition that y is bounded when $x>\infty$. The area enclosed by $y=f(x), y=\cos x$ and the $y$-axis is
A. $\sqrt{2}-1$
B. $\sqrt{2}$
C. 1
D. $1 / \sqrt{2}$

## - Watch Video Solution

19. If the area bounded between X -axis and the graph of $y=6 x-3 x^{2}$ between the ordinates $x=1$ and $\mathrm{x}=\mathrm{a}$ ' is 10 sq units, then 'a' can take the value
A. 4 or -2
B. two values are in $(2,3)$ and one in $(-1,0)$
C. two values are in $(3,4)$ and one in $(-2,-1)$
D. None of the above

## Answer: C

20. Area bounded by $y=f^{-1}(x)$ and tangent and normal drawn to it at points with abscissae $\pi$ and $2 \pi$, where $f(x)=\sin x-x$ is
A. $\frac{\pi^{2}}{2}-1$
B. $\frac{\pi^{2}}{2}-2$
C. $\frac{\pi^{2}}{2}-4$
D. $\frac{\pi^{2}}{2}$

## Answer: B

## - View Text Solution

21. If $f(x)=x-1$ and $g(x)=|f|(x)|-2|$, then the area bounded by $y=g(x)$ and the curve $x^{2}=4 y+8=0$ is equal to
A. $\frac{4}{3}(4 \sqrt{2}-5)$
B. $\frac{4}{3}(4 \sqrt{2}-3)$
C. $\frac{8}{3}(4 \sqrt{2}-3)$
D. $\frac{8}{3}(4 \sqrt{2}-5)$

## Answer: A

## - Watch Video Solution

22. 

Let
$S=\left\{(x, y): \frac{y(3 x-1)}{x(3 x-2)}<0\right\}, S^{\prime}=\{(x, y) \in A \times B:-1 \leq A \leq 1,-$ SnnS" is
A. 1
B. 2
C. 3
D. 4

## Answer: B

23. The area of the region bounded between the curves $y=e| | x \mid$ In $|x| \quad \mid, x^{2}+y^{2}-2(|x|+|y|)+1 \geq 0$ and X -axis where $|x| \leq 1$, if $\alpha$ is the $x$-coordinate of the point of intersection of curves in 1st quadrant, is
A. $4\left[\int_{0}^{\alpha} e x \operatorname{Inx} d x+\int_{\alpha}^{1}\left(1-\sqrt{1-(x-1)^{2}}\right) d x\right]$
B. $4\left[\int_{0}^{\alpha} e x \operatorname{In} x d x+\int_{1}^{\alpha}\left(1-\sqrt{1-(x-1)^{2}}\right) d x\right]$
C. $4\left[-\int_{0}^{\alpha} e x \operatorname{Inx} d x+\int_{\alpha}^{1}\left(1-\sqrt{1-(x-1)^{2}}\right) d x\right]$
D. $2\left[\int_{0}^{\alpha} e x \operatorname{Inx} d x+\int_{\alpha}^{1}\left(1-\sqrt{1-(x-1)^{2}}\right) d x\right]$

## Answer: D

## - Watch Video Solution

24. A point P lying inside the curve $y=\sqrt{2 a x-x^{2}}$ is moving such that its shortest distance from the curve at any position is greater than its distance from $X$-axis. The point $P$ enclose a region whose area is equal to
A. $\frac{\pi a^{2}}{2}$
B. $\frac{a^{2}}{3}$
C. $\frac{2 a^{2}}{3}$
D. $\left(\frac{3 \pi-4}{6}\right) a^{2}$

## Answer: C

## - Watch Video Solution

Exercise More Than One Correct Option Type Questions

1. The triangle formed by the normal to the curve $f(x)=x^{2}-a x+2 a$ at the point $(2,4)$ and the coordinate axes lies in second quadrant, if its area is 2 sq units, then a can be
A. 2
B. $17 / 4$
C. 5
D. None of these

## - Watch Video Solution

2. Let f and g be continuous function on $a \leq x \leq b$ and set $p(x)=\max \{f(x), g(x)\}$ and $q(x)=\min \{f(x), g(x)$, then the area bounded by the curves $y=p(x), y=q(x)$ and the ordinates $x=a$ and $x=b$ is given by
A. $\int_{a}^{b}|f(x)-g(x)| d x$
B. $\int_{a}^{b}|p(x)-q(x)| d x$
C. $\int_{a}^{b}\{f(x)-g(x)\} d x$
D. $\int_{a}^{b}\{p(x)-a(x)\} d x$

## Answer: A::B::D

## - View Text Solution

3. The area bounded by the parabola $y=x^{2}-7 x+10$ and X -axis
A. $9 / 2$ sq units
B. $1 / 6$ sq units
C. $5 / 6$ sq units
D. None of these

## Answer: A

## - Watch Video Solution

4. Area bounded by the ellipse $\frac{x^{2}}{4}+\frac{y^{2}}{9}=1$ is equal to
A. $6 \pi$ sq units
B. $3 \pi$ sq units
C. $12 \pi \mathrm{sq}$ units
D. area bounded by the ellipse $\frac{x^{2}}{9}+\frac{y^{2}}{4}=1$

## - Watch Video Solution

5. There is curve in which the length of the perpendicular from the orgin to tangent at any point is equal to abscissa of that point. Then,
A. $x^{2}+y^{2}=2$ is one such curve
B. $y^{2}=4 x$ is one such curve
C. $x^{2}+y^{2}=2 c x$ (c parameters) are such curve
D. there are no such curves

## Answer: A: C

## - Watch Video Solution

1. Statement I - The area of the curve $y=\sin ^{2} x$ from 0 to $\pi$ will be more than that of the curve $y=\sin x$ from 0 to $\pi$.

Statement II $-x^{2}>x, \quad$ if $x>1$.
A. Statement I is true, Statement II is also true, Statement II is the correct explanation of Statement I.
B. Statement I is true, Statement II is also true, Statement II is not the correct explanation of Statement I.
C. Statement I is true , Statement II is false
D. Statement I is false , Statement II is true

## Answer: D

## - Watch Video Solution

2. Statement I - The area of bounded by the curves $y=x^{2}-3$ and $y=k x+2$ is least if $k=0$.

Statement II- The area bounded by the curves $y=x^{2}-3$ and $y=k x+2 i s \sqrt{k^{2}+20}$.
A. Statement I is true, Statement II is also true, Statement II is the correct explanation of Statement I.
B. Statement I is true, Statement II is also true, Statement II is not the correct explanation of Statement I.
C. Statement I is true , Statement II is false
D. Statement I is false , Statement II is true

## Answer: C

## - Watch Video Solution

3. Statement 1 - The area of region bounded parabola $y^{2}=4 x$ and $x^{2}=4 y$ is $\frac{32}{3}$ sq units.

Statement II- The area of region bounded by parabola $y^{2}=4 a x$ and $x^{2}=4 b y$ is $\frac{16}{3} a b$.
A. Statement I is true, Statement II is also true, Statement II is the correct explanation of Statement I.
B. Statement I is true, Statement II is also true, Statement II is not the correct explanation of Statement I.
C. Statement I is true, Statement II is false
D. Statement I is false, Statement II is true

## Answer: D

## D Watch Video Solution

4. Statement I- The area by region $|x+y|+|x-y| \leq 2$ is 4 sq units. Statement II- Area enclosed by region $|x+y|+|x-y| \leq 2$ is symmetric about X-axis.
A. Statement I is true, Statement II is also true, Statement II is the correct explanation of Statement I.
B. Statement I is true, Statement II is also true, Statement II is not the correct explanation of Statement I.
C. Statement I is true, Statement II is false
D. Statement I is false, Statement II is true

## Answer: B

## D Watch Video Solution

5. Statement I- Area bounded by $y=x(x-1)$ and $y=x(1-x)$ is $\frac{1}{3}$. Statement II- Area bounded by $y=f(x)$ and $y=g(x)$ "is" $\left|\int_{a}^{b}(f(x)-g(x)) d x\right|$ is true when $f(x)$ and $g(x)$ lies above X-axis. (Where a and b are intersection of $y=f(x)$ and $y=g(x)$ ).
A. Statement I is true, Statement II is also true, Statement II is the correct explanation of Statement I.
B. Statement I is true, Statement II is also true, Statement II is not the
C. Statement I is true, Statement II is false
D. Statement I is false, Statement II is true

## Answer: C

## - Watch Video Solution

## Exercise Passage Based Questions

1. Let $f(x)=\frac{a x^{2}+b x+c}{x^{2}+1}$ such that $\mathrm{y}=-2$ is an asymptote of the curve $y=f(x)$. The curve $y=f(x)$ is symmetric about Y-axis and its maximum values is 4. Let $h(x)=f(x)-g(x)$,where $\quad f(x)=\sin ^{4} \pi x$ and $g(x)=\log _{e} x$. Let $x_{0}, x_{1}, x_{2} \ldots x_{n+1}$ be the roots of $f(x)=g(x)$ in increasing order

Then, the absolute area enclosed by $y=f(x)$ and $y=g(x)$ is given by
A. $\sum_{r=0}^{n} \int_{x_{r}}^{x_{r+1}}(-1)^{r} \cdot h(x) d x$
B. $\sum_{r=0}^{n} \int_{x_{1}}^{x_{r+1}}(-1)^{r+1} \cdot h(x) d x$
C. $2 \sum_{r=0}^{n} \int_{x_{r}}^{x_{r-r}+1}(-1)^{r} \cdot h(x) d x$
D. $\frac{1}{2} \cdot \sum_{r=0}^{n} \int_{x_{1}}^{x_{r+1}}(-1)^{r+1} \cdot h(x) d x$

## Answer: A

## - View Text Solution

2. Let $f(x)=\frac{a x^{2}+b x+c}{x^{2}+1}$ such that $\mathrm{y}=-2$ is an asymptote of the curve $y=f(x)$. The curve $y=f(x)$ is symmetric about $Y$-axis and its maximum values is 4. Let $h(x)=f(x)-g(x)$, where $\quad f(x)=\sin ^{4} \pi x \quad$ and $g(x)=\log _{e} x$. Let $x_{0}, x_{1}, x_{2} \ldots x_{n+1}$ be the roots of $f(x)=g(x)$ in increasing order

In above inquestion the value of $n$, is
A. 1
B. 2
C. 3
D. 4

## Answer: B

## D View Text Solution

3. Let $f(x)=\frac{a x^{2}+b x+c}{x^{2}+1}$ such that $\mathrm{y}=-2$ is an asymptote of the curve $y=f(x)$. The curve $y=f(x)$ is symmetric about Y -axis and its maximum values is 4. Let $h(x)=f(x)-g(x)$,where $\quad f(x)=\sin ^{4} \pi x$ and $g(x)=\log _{e} x$. Let $x_{0}, x_{1}, x_{2} \ldots x_{n+1}$ be the roots of $f(x)=g(x)$ in increasing order

The whole area bounded by $y=f(x), y=g(x) x=0$ is
A. $\frac{11}{8}$
B. $\frac{8}{3}$
C. 2
D. $\frac{13}{3}$

## Answer: A

4. Consider the function $f:(-\infty, \infty) \rightarrow(-\infty, \infty)$ defined by $f(x)=\frac{x^{2}-a x+1}{x^{2}+a x+1} ; 0<a<2$. which of the following is true ?
A. $(2-a)^{2} f(1)+(2-a)^{2} f(-1)=0$
B. $(2-a)^{2} f(1)-(2-\mathrm{a})^{\wedge}(2) \mathrm{f}(-1)=0$
C. $f^{\prime}(1) f^{\prime}(-1)=(2-a)^{2}$
D. $f^{\prime}(1) f^{\prime}(-1)=-(2+a)^{2}$

## Answer: A

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5. Consider the function $f:(-\infty, \infty) \rightarrow(-\infty, \infty)$ defined by $f(x)=\frac{x^{2}-a x+1}{x^{2}+a x+1} ; 0<a<2$. which of the following is true ?
A. $f(x)$ is decreasing on $(-1,1)$ and has a local minimum at $x=1$
B. $f(x)$ is increasing on $(-1,1)$ and has maximum at $x=1$
C. $f(x)$ is increasing on ( $-1,1$ ) but has neither a local maximum nor a local minimum at $\mathrm{x}=1^{`}$
D. $f(x)$ is decreasing on $(-1,1)$ but has neither a local maximum nor a local minimum at $\mathrm{x}=1$.

## Answer: A

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6. Consider the function $f:(-\infty, \infty) \rightarrow(-\infty, \infty)$ defined by $f(x)=\frac{x^{2}-a x+1}{x^{2}+a x+1}, 0<a<2$, and let $g(x)=\int_{0}^{e^{x}} \frac{f^{\prime}(t) d t}{1+t^{2}}$. Which of the following is true? (A) $g^{\prime}(x)$ is positive on $(-\infty, 0)$ and negative on $(0, \infty)$ (B) $g^{\prime}(x)$ is negative on $(-\infty, 0)$ and positive on $(0, \infty)$ $g^{\prime}(x)$ changes sign on both $(-\infty, 0)$ and $(0, \infty)$ (D) $g^{\prime}(x)$ does not change sign on $(-\infty, \infty)$
A. $g^{\prime}(x)$ is positive on $(-\infty, 0)$ and negative on $(0, \infty)$
B. $g^{\prime}(x)$ is negative on $(-\infty, 0)$ and positive on $(0, \infty)$
C. $g^{\prime}(x)$ change sign on both $(-\infty, 0)$ and $(0, \infty)$
D. $g^{\prime}(x)$ does not change sign on $(-\infty, \infty)$.

## Answer: B

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7. Computing area with parametrically represented boundaries

If the boundary of a figure is represented by parametric equations $x=x(t)$
, $y=y(t)$, then the area of the figure is evaluated by one of the three formulae
$S=-\int_{\alpha}^{\beta} y(t) x^{\prime}(t) d t, S=\int_{\alpha}^{\beta} x(t) y^{\prime}(t) d t$
$S=\frac{1}{2} \int_{\alpha}^{\beta}\left(x y^{\prime}-y x^{\prime}\right) d t$
where $\alpha$ and $\beta$ are the values of the parameter t corresponding respectively to the beginning and the end of traversal of the contour .
The area enclosed by the astroid $\left(\frac{x}{a}\right)^{\frac{2}{3}}+\left(\frac{y}{a}\right)^{\frac{2}{3}}=1$ is
A. $\frac{3}{4} a^{2} \pi$
B. $\frac{3}{18} \pi a^{2}$
C. $\frac{3}{8} \pi a^{2}$
D. $\frac{3}{4} a \pi$

## Answer: C

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8. Computing area with parametrically represented boundaries: If the boundary of a figure is represented by parametric equation, i.e., $x=x(t), y=(t)$, then the area of the figure is evaluated by one of the three formulas :
$S=-\int_{\beta}^{\beta} y(t) x^{\prime}(t) d t$,
$S=\int_{\alpha} x(t) y^{\prime}(t) d t$,
$S=\frac{1}{2} \int_{\alpha}^{\beta}\left(x y^{\prime}-y x^{\prime}\right) d t$,
Where $\alpha$ and $\beta$ are the values of the parameter t corresponding respectively to the beginning and the end of the traversal of the curve
corresponding to increasing t .

The area of the region bounded by an are of the cycloid $x=a(t-\sin t), y=a(1-\cos t)$ and the $x$-axis is
A. $6 \pi a^{2}$
B. $3 \pi a^{2}$
C. $4 \pi a^{2}$
D. None of these

## Answer: B

## D Watch Video Solution

9. Computing area with parametrically represented boundaries: If the boundary of a figure is represented by parametric equation, i.e., $x=x(t), y=(t)$, then the area of the figure is evaluated by one of the three formulas:
$S=-\int_{\alpha}^{\beta} y(t) x^{\prime}(t) d t$
$S=\int_{\alpha} x(t) y^{\prime}(t) d t$,
$S=\frac{1}{2} \int_{\alpha}^{\beta}\left(x y^{\prime}-y x^{\prime}\right) d t$,
Where $\alpha$ and $\beta$ are the values of the parameter t corresponding respectively to the beginning and the end of the traversal of the curve corresponding to increasing t .

The area of the loop described as
$x=\frac{t}{3}(6-t), y=\frac{t^{2}}{8}(6-t)$ is
A. $\frac{27}{5}$
B. $\frac{24}{5}$
C. $\frac{27}{6}$
D. $\frac{21}{5}$

## Answer: A

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1. Consider $f(x)=x^{2}-3 x+2$ The area bounded by $|y|=|f(|x|)|, x \geq 1$ is A , then find the value of $3 A+2$.

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2. If $S$ is the sum of cubes of possible value of $c$ for which the area of the figure bounded by the curve $y=8 x^{2}-x^{5}$, then straight lines $x=1 a n d x=c$ and the abscissa axis is equal to $\frac{16}{3}$, then the value of [ $S$ ], where[.] denotest the greatest integer function, is $\qquad$

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3. The area bounded by $y=2-|2-x|, y=\frac{3}{|x|} i s \frac{k-3 \text { In } 3}{2}$, then k is equal to ......

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4. Using the method of integration find the area of the triangle $A B C$, coordinates of whose vertices are $A(2,0), B(4,5)$ and $C(6,3)$.

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5. A point ' P ' moves in xy plane in such a way that $[|x|]+[|y|]=1$ where [.] denotes the greatest integer function. Area of the region representing all possible positions of the point ' $P$ ' is equal to:

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6. Let $f:[0,1] \rightarrow\left[0, \frac{1}{2}\right]$ be a function such that $f(x)$ is a polynomial of 2nd degree, satisfty the following condition :
(a) $f(0)=0$
(b) has a maximum value of $\frac{1}{2} a t x=1$.

If A is the area bounded by $y=f(x)=f^{-1}(x)$ and the line $2 x+2 y-3=0$ in 1st quadrant, then the value of 24 A is equal to .......
7. Let $f(x)=\min \left\{\sin ^{-1} x, \cos ^{-1} x, \frac{\pi}{6}\right\}, x \in[0,1]$. If area bounded by $y=f(x)$ and X -axis, between the lines $x=0$ and $x=1 i s \frac{a-X}{b(\sqrt{3}+1)}$. Then , (a-b) is ........

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8. Let $f(x)$ be a real valued function satisfying the relation $f\left(\frac{x}{y}\right)=f(x)-f(y)$ and $\lim _{x \rightarrow 0} \frac{f(1+x)}{x}=3$. The area bounded by the curve $y=f(x), y$-axis and the line $y=3$ is equal to

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## Exercise Subjective Type Questions

1. Find the continuous function $f$ where
$\left(x^{4}-4 x^{2}\right) \leq f(x) \leq\left(2 x^{2}-x^{3}\right)$ such that the area bounded by $y=f(x), y=x^{4}-4 x^{2}$. then $y$-axis, and the line $x=t$, where $(0 \leq t \leq 2) \quad$ is $\quad k \quad$ times the area bounded by $y=f(x), y=2 x^{2}-x^{3}, y-a \xi s$, and line $x=t(w h e r e 0 \leq t \leq 2)$.

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2. Let $f(t)=|t-1|-|t|+|t+1|, \forall t \in R$.

Find
$g(x)=\max \{f(t): x+1 \leq t \leq x+2\}, \forall x \in R$. Find $g(x)$ and the area bounded by the curve $y=g(x)$, the X -axis and the lines $x=-3 / 2$ and $x=5$.

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3. Let $\mathrm{f}(\mathrm{x})=$ minimum $\left\{e^{x}, 3 / 2,1+e^{-x}\right\}, 0 \leq x \leq 1$. Find the area bounded by $y=f(x), \mathrm{X}$-axis and the line $\mathrm{x}=1$.
4. Find t5he area bounded by $y=f(x)$ and the curve $y=\frac{2}{1+x^{2}}$ satisfying the condition
$f(x), f(y)=f(x y) \forall x, y \in R$ and $f^{\prime}(1)=2, f(1)=1$,

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5. The value of

$$
\int_{0}^{\sin ^{2} x} \sin ^{-1} \sqrt{t} d t+\int_{0}^{\cos ^{2} x} \cos ^{-1} \sqrt{t} d t \text {, is }
$$

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6. Let T be an acute triangle Inscribe a pair R,S of rectangle in T as shown:

Let $A(x)$ denote the area of polygon X find the maximum value (or show that no maximum exists), of $\frac{A(R)+A(S)}{A(T)}$, where T ranges over all
triangles and R,S over all rectangle as above.


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7. Find the maximum area of the ellipse that can be inscribed in an isoceles triangles of area $A$ and having one axis lying along the perpendicular from the vertex of the triangles to its base.

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8. In the adjacent figure the graph of two function $y=f(x)$ and $y=\sin x \quad$ are given $\quad y=\sin \quad x$ intersects, $y=f(x) \quad$ at $\quad A(a, f(a))$, $B(\pi, 0)$ and $C(2 \pi, 0)$.
$A_{i}(i=1,2,3) \quad$ is the area bounded by the curves $y=f(x)$ and $y=\sin x$ between $\mathrm{x}=0$ and $\mathrm{x}=\mathrm{a}, \mathrm{i}=1$ between $\mathrm{x}=\mathrm{a}$ and $x=\pi, i=2 \quad$ between $\quad x=\pi \quad$ and $\quad x=2 \pi, i=3$. $A_{1}=1-\sin a+(a-1) \cos \mathrm{a}$, determine the function $\mathrm{f}(\mathrm{x})$. Hence, determine a and $A_{1}$. Also, calculate $A_{2}$ and $A_{3}$.


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9. Find the area of the region bounded by curve $y=25^{x}+16$ and the curve $y=b .5^{x}+4$, whose tangent at the point $\mathrm{x}=1$ make an angle $\tan ^{-1}$ ( $40 \ln 5$ ) with the X -axis.
10. If the circles of the maximum area inscriabed in the region bounded by the curves $y=x^{2}-2 x-3$ and $y=3+2 x-x^{2}$, then the area of region $y-x^{2}+2 x+3 \leq 0, y+x^{2}-2 x-3 \leq 0$ and $s \leq 0$.

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11. Find limit of the ratio of the area of the triangle formed by the orgin and intersection points of the parabola $y-4 x^{2}$ and the line $y=a^{2}$,to the area between the parabola and the line as a approaches to zero.

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12. Find the area of curve enclosed by $|x+y|+|x-y| \leq 4,|x| \leq 1, y \geq \sqrt{x^{2}-2 x+1}$.

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13. Calculate the area enclosed by the curve $4 \leq x^{2}+y^{2} \leq 2(|x|+|y|)$.

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14. Find the area enclosed by the curve $[x]+[y]-4$ in 1st quadrant (where [.] denotes greatest integer function).

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15. Sketch the region and find the area bounded by the curves $|y+x| \leq 1,|y-x| \leq 1$ and $2 x^{2}+2 y^{2} \geq 1$.

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16. Find the area of the region bounded by the curve $2^{|x|}|y|+2^{|x|-1} \leq 1$, with in the square formed by the lines $|x| \leq 1 / 2,|y| \leq 1 / 2$.
17. The value of the parameter $a(a \geq 1)$ for which the area of the figure bounded by the pair of staight lines $y^{2}-3 y+2=0$ and the curves $y=[a] x^{2}, y=\frac{1}{2}[a] x^{2}$ is greatest is (Here [.] denotes the greatest integer function). (A) $[0,1)$ (B) $[1,2)$ (C) $[2,3)$ (D) $[3,4)$

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## Exercise Questions Asked In Previous 13 Years Exam

1. Area of region
$\left\{(x, y) \in R^{2}: y \geq \sqrt{|x+3|}, 5 y \leq x+9 \leq 15\right\}$
A. $\frac{1}{6}$
B. $\frac{4}{3}$
C. $\frac{3}{2}$
D. $\frac{5}{3}$

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2. Let $F(x)=\int_{x}^{x^{2}+\frac{\pi}{6}}\left[2 \cos ^{2} t . d t\right] \quad$ for $\quad$ all $\quad x \in R \quad$ and $f:\left[0, \frac{1}{2}\right] \rightarrow[0, \infty)$ be a continuous function.For $a \in\left[0, \frac{1}{2}\right]$, if $\mathrm{F}^{\prime}(\mathrm{a})+2$ is the area of the region bounded by $x=0, y=0, y=f(x)$ and $x=a$, then $f(0)$ is

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3. The common tangents to the circle $x^{2}+y^{2}=2$ and the parabola $y^{2}=8 x$ touch the circle at $P, Q$ andthe parabola at $R, S$. Then area of quadrilateral $P Q R S$ is
A. 3
B. 6
C. 9
D. 15

Answer: D

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4. The area enclosed by the curves
$y=\sin x+\cos x$ and $y=|\cos x-\sin x|$ over the interval $\left[0, \frac{\pi}{2}\right]$
A. $4(\sqrt{2}-1)$
B. $2 \sqrt{2}(\sqrt{2}-1)$
C. $2(\sqrt{2}+1)$
D. $2 \sqrt{2}(\sqrt{2}+1)$

## Answer: B

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5. Let $S$ be the area of the region enclosed by $y=e^{-x} \wedge 2, y=0, x=0, a n d x=1$. Then $S \geq \frac{1}{e}$ (b) $S \geq 1=\frac{1}{e}$ $S \leq \frac{1}{4}\left(1+\frac{1}{\sqrt{e}}\right)$ (d) $S \leq \frac{1}{\sqrt{2}}+\frac{1}{\sqrt{e}}\left(1-\frac{1}{\sqrt{2}}\right)$
A. $S \geq \frac{1}{e}$
B. $S \geq 1-\frac{1}{e}$
C. $S \leq \frac{1}{4}\left(1+\frac{1}{\sqrt{e}}\right)$
D. $S \leq \frac{1}{\sqrt{2}}+\frac{1}{\sqrt{e}}\left(1-\frac{1}{\sqrt{2}}\right)$

## Answer: B::D

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6. Let $f:[-1,2] \overrightarrow{0, \infty}$ be a continuous function such that $f(x)=f(1-x) f$ or all $x \in[-1,2]$. Let $R_{1}=\int_{-1}^{2} x f(x) d x$, and $R_{2}$ be the area of the region bounded by $y=f(x), x=-1, x=2$, and the $x-a \xi s$. Then $R_{1}=2 R_{2}$ (b) $R_{1}=3 R_{2} 2 R_{1}$ (d) $3 R_{1}=R_{2}$
A. $R_{1}=2 R_{2}$
B. $R_{1}=3 R_{2}$
C. $2 R_{1}=R_{2}$
D. $3 R_{1}=R_{2}$

## Answer: C

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7. Let the straight line $x=b$ divide the area enclosed by $y=(1-x)^{2}, y=0$, and $x=0 \quad$ into two parts $R_{1}(0 \leq x \leq b)$ and $R_{2}(b \leq x \leq 1)$ such that $R_{1}-R_{2}=\frac{1}{4}$. Then b equals
A. $\frac{3}{4}$
B. $\frac{1}{2}$
C. $\frac{1}{3}$
D. $\frac{1}{4}$

## Answer: B

## D Watch Video Solution

8. Area of the region bounded by the curve $y=e^{x}$ and lines $x=0$ and $y=e$ is
A. $e-1$
B. $\int_{1}^{e} \operatorname{In}(e+1-y) d y$
C. $e-\int_{0}^{1} e^{x} d x$
D. $\int_{0}^{e} \operatorname{Inyd} y$

## Answer: B::C

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9. The area of the region bounded by the curves $y=\sqrt{\frac{1+\sin x}{\cos x}}$ and $y=\sqrt{\frac{1-\sin x}{\cos x}}$ bounded by the lines $\mathrm{x}=0$ and $x=\frac{\pi}{4}$ is
A. $\int_{0}^{\sqrt{2}-1} \frac{t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$
B. $\int_{0}^{\sqrt{2}-1} \frac{4 t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$
C. $\int_{0}^{\sqrt{2}=1} \frac{4 t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$
D. $\int_{0}^{\sqrt{2}+1} \frac{t}{\left(1+t^{2}\right) \sqrt{1-t^{2}}} d t$

## Answer: B

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10. Consider the function defined implicitly by the equation $y^{3}-3 y+x=0$ on various intervals in the real line. If $x \in(-\infty,-2) \cup(2, \infty)$, the equation implicitly defines a unique realvalued defferentiable function $y=f(x)$. If $x \in(-2,2)$, the equation implicitly defines a unique real-valud diferentiable function $y-g(x)$ satisfying $g_{0}=0$.

If $f(-10 \sqrt{2})=2 \sqrt{2}$, then $f(-10 \sqrt{2})$ is equal to
A. $\frac{4 \sqrt{2}}{7^{3} 3^{2}}$
B. $-\frac{4 \sqrt{2}}{7^{3} 3^{2}}$
C. $\frac{4 \sqrt{2}}{7^{3} 3}$
D. $-\frac{4 \sqrt{2}}{7^{3} 3}$

## Answer: B

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11. Consider the function defined implicitly by the equation $y^{3}-3 y+x=0$ on various intervals in the real line. If $x \in(-\infty,-2) \cup(2, \infty)$, the equation implicitly defines a unique realvalued defferentiable function $y=f(x)$. If $x \in(-2,2)$, the equation implicitly defines a unique real-valud diferentiable function $y-g(x)$ satisfying $g_{0}=0$.

The area of the region bounded by the curve $y=f(x)$, the X -axis and the line $x=a$ and $x=b$, where $-\infty<a<b<-2$ is

$$
\text { A. } \int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x+b y(b)-a f(a)
$$

B. $-\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x-b y(b)+a f(a)$
C. $\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x-b y(b)+a f(a)$
D. $-\int_{a}^{b} \frac{x}{3\left[\{f(x)\}^{2}-1\right]} d x+b y(b)=a f(a)$

## Answer: A

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12. Consider the function defined implicitly by the equation $y^{3}-3 y+x=0$ on various intervals in the real line. If $x \in(-\infty,-2) \cup(2, \infty)$, the equation implicitly defines a unique realvalued defferentiable function $y=f(x)$. If $x \in(-2,2)$, the equation implicitly defines a unique real-valud diferentiable function $y-g(x)$ satisfying $g_{0}=0$.
$\int_{-1}^{1} g^{\prime}(x) d x$ is equal to
A. $2 g(-1)$
B. 0
C. $-2 g(1)$
D. $2 g(1)$

## Answer: D

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13. The area (in sqaure units) of the region $\left\{(x, y): x \geq 0, x+y \leq 3, x^{2} \leq 4 y\right.$ and $\left.y \leq 1+\sqrt{x}\right\}$ is
A. $\frac{5}{2}$
B. $\frac{59}{12}$
C. $\frac{3}{2}$
D. $\frac{7}{3}$

## Answer: A

14. The area (in sq units) of the region $\left\{(x, y): y^{2} \geq 2 x\right.$ and $\left.x^{2}+y^{2} \leq 4 x, x \geq 0, y \geq 0\right\}$ is
A. $\pi-\frac{4}{3}$
B. $\pi-\frac{8}{3}$
C. $\pi-\frac{4 \sqrt{2}}{3}$
D. $\frac{\pi}{2}-\frac{2 \sqrt{2}}{3}$

## Answer: B

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15. The area (in sq units) of the region described by $\left\{(x, y): y^{2} \leq 2 x\right.$ and $\left.y \geq 4 x-1\right\}$ is
A. $\frac{7}{32}$
B. $\frac{5}{64}$
C. $\frac{15}{64}$
D. $\frac{9}{32}$

## Answer: D

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16. The area (in sq. units) of the quadrilateral formed by the tangents at the end points of the latera recta to the ellipse $\frac{x^{2}}{9}+\frac{y^{2}}{5}=1$, is: (1) $\frac{27}{4}$ (2) 18 (3) $\frac{27}{2}(4) 27$
A. $\frac{27}{4}$
B. 18
C. $\frac{27}{2}$
D. 27

## Answer: D

17. The area of the region described by $A=\left\{(x, y): x^{2}+y^{2} \leq 1\right.$ and $\left.y^{2} \leq 1-x\right\}$ is
A. $\frac{\pi}{2}+\frac{4}{3}$
B. $\frac{\pi}{2}-\frac{4}{3}$
C. $\frac{\pi}{2}-\frac{2}{3}$
D. $\frac{\pi}{2}+\frac{2}{3}$

## Answer: A

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18. The area (in square units) bounded by the curves $y=\sqrt{x}, 2 y-x+3=0, x$-axis, and lying in the first quadrant is
A. 9
B. 36
C. 1
D. $\frac{27}{4}$

## Answer: A

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19. The area bounded between the parabola $x^{2}=\frac{y}{4}$ and $x^{2}=9 y$ and the straight line $y=2$ is
A. $20 \sqrt{2}$
B. $\frac{10 \sqrt{2}}{3}$
C. $\frac{20 \sqrt{2}}{3}$
D. $10 \sqrt{2}$

## Answer: C

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20. The area of the region enclosed by the curves $y=x, x=e, y=\frac{1}{x}$ and the positive $x$-axis is
A. 1 sq unit
B. $\frac{3}{2}$ sq units
C. $\frac{5}{2}$ sq units
D. $\frac{1}{2}$ sq unit

## Answer: B

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21. The area bounded by the curves $y=\cos x$ and $y=\sin x$ between the ordinates $x=0$ and $x=\frac{3 \pi}{2}$ is
A. $(4 \sqrt{2}-2)$ sq units
B. $(4 \sqrt{2}+2)$ sq units
C. $(4 \sqrt{2}-1)$ sq units
D. $(4 \sqrt{2}+1)$ sq units

## Answer: A

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22. The area of the region bounded by the parabola $(y-2)^{2}=x-1$, the tangent to the parabola at the point $(2,3)$ and the $x$-axis is
A. 6 sq units
B. 9 sq units
C. 12 sq units
D. 3 sq units

## Answer: B

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23. The area of the plane region bounded by the curves $x+2 y^{2}=0$ and $x+3 y^{2}=1$ is equal to (1) $\frac{5}{3}$ (2) $\frac{1}{3}$ (3) $\frac{2}{3}$ (4) $\frac{4}{3}$
A. $\frac{5}{3}$ sq units
B. $\frac{1}{3}$ sq unit
C. $\frac{2}{3}$ sq unit
D. $\frac{4}{3}$ sq units

## Answer: D

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