



## MATHS

### BOOKS - ARIHANT MATHS (HINGLISH)

#### BIONOMIAL THEOREM

##### Examples

1. Expand  $\left(2a - \frac{3}{b}\right)^5$  by binomial theorem

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2. Evaluate the following:  $(x + \sqrt{x^2 - 1})^6 + (x - \sqrt{x^2 - 1})^6$

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3. In the expansion of  $(x + a)^n$  if the sum of odd terms is  $P$  and the sum of even terms is  $Q$ , then  $P^2 - Q^2 = (x^2 - a^2)^n$

$$4PQ = (x + a)^{2n} - (x - a)^{2n} \quad 2(P^2 + Q^2) = (x + a)^{2n} + (x - a)^{2n}$$

none of these

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4. Using binomial theorem, prove that  $(101)^{50} > (100^{50} + 99^{50})$ .

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5. If  $a_n = \sum_{r=0}^n \frac{1}{{}^n C_r}$ , find the

value of  $\sum_{r=0}^n \frac{r}{{}^n C_r}$

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6. Find the number of dissimilar terms in

the expansion of  $(1 - 3x + 3x^3 - x^3)^{33}$

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7. Find the sum of  $\sum_{r=1}^n \frac{r^n C_r}{n C_{r-1}}$ .

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8.

$(C_0 + C_1)(C_1 + C_2)(C_2 + C_3)(C_3 + C_4)\dots\dots\dots(C_{n-1} + C_n) = \frac{C_0 C_1 C_2 \dots C_n}{C_n}$

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9. find the sum of the series

$$\sum_{r=0}^n (-1)^r \cdot {}^n C_r$$

$\left[ \frac{1}{2^r} + \frac{3^r}{2^{2r}} + \frac{7^r}{2^{3r}} + \frac{15^r}{2^{4r}} \dots \text{up to } m \text{ terms} \right]$

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10. The seventh term in the expansion of  $\left(4x - \frac{1}{2\sqrt{x}}\right)^{13}$  is

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11. Find the coefficient of  $x^8$  in the expansion of  $\left(x^2 - \frac{1}{x}\right)^{10}$

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12. Find the coefficient of  $x^7$  in the expansion of  $\left(ax^2 + \frac{1}{bx}\right)^{11}$ . (ii) the coefficient of  $x^{-7}$  in the expansion of  $\left(ax + \frac{1}{bx^2}\right)^{11}$ . Also, find the relation between a and b, so that these coefficients are equal.

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13. Find the term independent of  $x$  in the

expansion of  $\left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^9$



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14. Find the 4th term from the end in the expansion of  $\left(\frac{x^3}{2} - \frac{2}{x^2}\right)^9$ .



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15. Find the  $(n+1)$ th term from the end in

the expansion of  $\left(2x - \frac{1}{x}\right)^{3n}$



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16. Find the number of terms in the

expansion of  $(\sqrt[2]{9} + \sqrt[2]{8})^{500}$  which are integers.



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17. The sum of all rational terms in the expansion of  $\left(3^{\frac{1}{5}} + 2^{\frac{1}{3}}\right)^{15}$  is

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18. The number of irrational terms in the expansion of

$(\sqrt[8]{5} + \sqrt[6]{2})^{100}$  is

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19. Let  $n$  be a positive integer . If the

coefficients of  $r$ th  $(r + 1)$  th and  $(r + 2)$ th terms in the expansion of  $(1 + x)^n$

are in AP, then find the relation between  $n$  and  $r$  .

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20. If  $a, b, c$  and  $d$  are any four consecutive

coefficients in the expansion of  $(1 + x)^n$ , then prove that

$$(i) \frac{a}{a+b} + \frac{c}{b+c} = \frac{2b}{b+c}$$

$$(ii) \left( \frac{b}{b+c} \right)^2 > \frac{ac}{(a+b)(c+d)}, \text{ if } x > 0.$$



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21. If the 2nd, 3rd and 4th terms in the

expansion of  $(x + y)^n$  are 240, 720 and 1080

respectively find  $x, y$  and  $n$ .



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22. Find the middle term in the expansion of:  $\left( \frac{a}{x} + bx \right)^{12}$



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23. Find the middle term (terms) in the expansion of

(i)  $\left(\frac{x}{a} - \frac{a}{x}\right)^{10}$  (ii)  $\left(3x - \frac{x^3}{6}\right)^9$



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24. Show that the middle term in the expansion of

$(1+x)^{2n}$  is  $\frac{(1 \cdot 3 \cdot 5 \cdots (2n-1))}{n!} 2^n x^n$ , where  $n$  is a positive integer.



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25. Find numerically greatest term in the expansion of  $(2+3x)^9$ , when  $x = 3/2$ .



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26. Find numerically the greatest term in

the expansion of  $(3-5x)^n$ , when  $x = \frac{1}{5}$



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27. Show that , if the greatest term in the expansion of  $(1 + x)^{2n}$  has also the greatest coefficient

then  $x$  lies between  $\frac{n}{n+1}$  and  $\frac{n+1}{n}$

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28. Find out the sum of the coefficients in the expansion of the binomial  $(5p - 4q)^n$ , where  $n$  is a +ive integer.

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29. In the expansion of  $\left(3^{-x/4} + 3^{5x/4}\right)^\pi$  the sum of binomial coefficient is 64 and term with the greatest binomial coefficient exceeds the third by  $(n - 1)$  , the value of  $x$  must be 0 b. 1 c. 2 d. 3

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30. Find the sum of  $\frac{1}{1!(n-1)!} + \frac{1}{3!(n-3)!} = \frac{1}{5!(n-5)!} + \dots$ ,

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31. Find the values of  $\frac{1}{12!} + \frac{1}{10!2!} + \frac{1}{8!4!} + \dots + \frac{1}{12!}$

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32. The sum of the coefficients of the polynomial  $(1 + x - 3x^2)^{2163}$  is .....

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33. If the sum of the coefficient in the expansion of  $(\alpha x^2 - 2x + 1)^{35}$  is equal to the sum of the coefficient of the expansion of  $(x - \alpha y)^{35}$ , then  $\alpha =$

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**34.** If  $(1 + x + 2x^2)^{20} = a_0 + a_1x + a_2x^2 + \dots + a_{40}x^{40}$ .

The value of  $a_0 + a_2 + a_4 + \dots + a_{38}$  is

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**35.** Show that the integral part of

$(5 + 2\sqrt{6})^n$  is odd where  $n$  is natural number

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**36.** Show that the integral part of

$(5\sqrt{5} + 11)^{2n+1}$  is even where  $n \in \mathbb{N}$ .

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37. Let  $(6\sqrt{6} + 14)^{2n+1} = R$ , if  $R$  be the fractional part of  $R$ , then prove that  $Rf = 20^{2n+1}$

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38. If  $(7 + 4\sqrt{3})^n + 5 + t$ , where  $n$  and  $s$  are positive integers and  $t$  is a proper fraction, show that  $(1 - t)(s + t) = 1$

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39. If  $x = (8 + 3\sqrt{7})^n$ , where  $n$  is a natural number, power that the integral part of  $x$  is an odd integer and also show that  $x - x^2 + x[x] = 1$ , where  $[.]$  denotes the greatest integer function.

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**40.** Show that

$1992^{1998} - 1955^{1998} - 1938^{1998} + 1901^{1998}$  is divisible by 1998



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**41.** Prove that  $2222^{5555} + 5555^{2222}$  is

divisible by 7 .



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**42.** If  $n$  is any positive integer , show that

$2^{3n+3} - 7n - 8$  is divisible by 49 .



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**43.** If  $10^n$  divides the number  $101^{100} - 1$  , find

the greatest value of  $n$



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44. If  $7^{103}$  is divided by 25, find the remainder.

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45. Find the remainder when  $x = 5^5 \wedge 5 \wedge 5$  (24 times 5) is divided by 24.

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46. If 7 divides  $32^{32^{32}}$ , then find the remainder

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47. The last two digits of  $3^{400}$  is

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48. If the number is  $17^{256}$ , find the last digit

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49. If the number is  $17^{256}$ , find the last digit

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50. Calculate last two digit; last three digit of  $(17)^{256}$

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51. Find the greater number is  $100^{100}$  and  $(300)!$ .

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52. Find the greater number in  $300!$  and

$$\sqrt{300^{\sqrt{300}}}$$



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53. If  $(1 + x)^n = C_0 + C_1x + C_2x^2$

$+ C_3x^3 + C_4x^4 + \dots$ , find the values of

(i)  $C_0 - C_2 + C_4 - C_6 + \dots$

(ii)  $C_1 - C_3 + C_5 - C_7 + \dots$

(iii)  $C_0 + C_3 + C_6 + \dots$



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54. Find the value of  ${}^{4n}C_0 + {}^{4n}C_4 + {}^{4n}C_8 + \dots + {}^{4n}C_{4n}$ .



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55. Find the coefficient of  $a^2b^3c^4d$  in the expansion of  $(a - b - c + d)^{10}$ .



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56. Find the coefficient of  $a^3b^4c^5$  in the expansion of  $(bc + ca + ab)^6$



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57. Find the total number of distinct or dissimilar terms in the expansion of  $(x + y + z + w)^n, n \in N$



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58. Find the greatest coefficient in the expansion of  $(a + b + c + d)^{15}$ .



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59. Find the coefficient of  $x^7$  in the expansion of  $(a + 3x - 2x^3)^{10}$ .

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60. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , prove that

$$C_1 + 2C_2 + 3C_3 + \dots + nC_n = n \cdot 2^{n-1}$$

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61. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , prove that

$$C_0 + 2C_1 + 3C_2 + \dots + (n + 1)C_n = (n + 2)2^{n-1}.$$

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62. If  $(1 + x)^n = c_0 + c_1x + c_2x^2 + \dots + c_nx^n$  then the value of  $c_0 + 3c_1 + 5c_2 + \dots + (2n + 1)c_n$  is-



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63. If  $(1 + x)^n = C_0 + C_1x + C_2x^2$

$+ \dots + C_nx^n$ , prove that  $1^2 \cdot C_1 + 2^2 \cdot C_2 = n(n + 1) \cdot 2^{n-2}$ .

$1^2 \cdot C_1 + 2^2 \cdot C_2 = n(n + 1) \cdot 2^{n-2}$ .

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64. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , prove that

$(1 \cdot 2)C_2 + (2 \cdot 3)$

$C_3 + \dots + \{(n - 1) \cdot n\}C_n = n(n - 1)2^{n-2}$ .

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65.  $(1 + x)^n = C_0 + C_1x + C_2x^2 + C_3x^3 + \dots + C_nx^n$ , prove

that  $C_0 - 2C_1 + 3C_2 - 4C_3 + \dots + (-1)^n(n + 1)C_n = 0$

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66.

If

$(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , us  $\in$  gderivativesprovethat

$$C_1 + 2C_2 + \dots + nC_n = n \cdot 2^{n-1}$$

$$C_1 - 2C_2 + 3C_3 + \dots + (-1)^{n-1}nC_n = 0$$

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67. Prove that :  $C_0 - 3C_1 + 5C_2 - \dots + (-1)^n(2n + 1)C_n = 0$

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68. सिध्द कीजिए कि  $C_0 + \frac{C_1}{2} + \frac{C_2}{3} + \dots + \frac{C_n}{n+1} = \frac{2^{n+1} - 1}{n+1}$

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69. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + C_3x^3 + \dots + C_nx^n$ , prove that

$$C_0 - \frac{C_1}{2} + \frac{C_2}{3} - \dots + (-1)^n \frac{C_n}{n+1} = \frac{1}{n+1}.$$

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70. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + C_3x^3 + \dots + C_nx^n$  prove that

$$\frac{C_0}{1} + \frac{C_2}{3} + \frac{C_4}{5} + \dots = \frac{2^n}{n+1}.$$

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71. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + C_3x^3$

$+ \dots + C_nx^n$ , prove that  $\frac{C_1}{2} + \frac{C_3}{4} + \frac{C_5}{6} + \dots = \frac{2^{n+1} - 1}{n+1}$ .

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72.  $3C_0 + 3^2 \frac{C_1}{2} + 3^3 \frac{C_2}{3} + \dots + 3^{n+1} \cdot \frac{C_n}{n+1}$  equal to

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73. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ ,

Show

that

$$\frac{2^2}{1 \cdot 2}C_0 + \frac{2^3}{2 \cdot 3}C_1 + \frac{2^4}{3 \cdot 4}C_2 + \dots + \frac{2^{n+2}C_n}{(n+1)(n+2)} = \frac{3^{n+2} - 2n - 5}{(n+1)(n+2)}$$

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74.

Prove

that

$$C_0C_r + C - 1C_{r+1} + C_2C_{r+2} + \dots + c_{n-r}C_n = \frac{(2n)!}{(n-r)!(n+r)!}$$

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75. यदि  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ . साबित कीजिए कि

$$C_0^2 + C_1^2 + C_2^2 + \dots + C_n^2 = \frac{(2n)!}{n!n!} = \frac{1.3.5 \dots (2n-1).2^n}{n!}$$

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76.

Prove

that

$$\binom{2n}{0}^2 - \binom{2n}{1}^2 + \binom{2n}{2}^2 - \dots + \binom{2n}{2n}^2 = (-1)^n \cdot 2^n C_n.$$


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77. If  $(1+x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , prove that

$$C_0^2 - C_1^2 + C_2^2 - \dots + (-1)^n \cdot C_n^2 = 0 \text{ or}$$

$$(-1)^{n/2} \cdot \frac{n!}{(n/2)!(n/2)!}, \text{ according as } n \text{ is odd or even}$$

Also, evaluate  $C_0^2 + C_1^2 + C_2^2 - \dots + (-1)^n \cdot C_n^2$  for  $n$

$n = 10$  and  $n = 11$ .


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78. If  $m, n, r$  are positive integers such that  $r < m, n$ , then

$${}^m C_r + {}^m C_{r-1} {}^n C_1 + {}^m C_{r-2} {}^n C_2 + \dots + {}^m C_1 {}^n C_{r-1} + {}^n C_r \text{ equals}$$


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79. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , prove that

$$C_0C_n - C_1C_{n-1} + C_2C_{n-2} - \dots + (-1)^n C_nC_0 = 0 \quad \text{or}$$

$$(-1)^{n/2} \frac{n!}{(n/2)!(n/2)!}, \text{ according as } n \text{ is odd or even.}$$



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80. If  $(1 + x)^n = C_0 + C_1x + C_2x^2$

$+ C_3x^3 + \dots + C_nx^n$ , prove that

$$C_1^2 + 2C_2^2 + 3C_3^2 + \dots + nC_n^2 = \frac{(2n - 1)!}{((n - 1)!)^2}$$



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81. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$  then the value of

$$(C_0)^2 + \frac{(C_1)^2}{2} + \frac{(C_2)^2}{3} + \dots + \frac{(C_n)^2}{n+1} \text{ is equal to}$$



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82. Evaluate  $\sum_{r=0}^n n+r C_n$ .

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83. Prove that  $\binom{n}{0} C_n - \binom{n}{1} C_1^{2n-2} C_n + \binom{n}{2} C_2^{2n-4} C_n \equiv 2^n$ .

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84. Prove that  $\binom{n}{0} C_0^{2n} C_n - \binom{n}{1} C_1^{2n-1} C_n + \binom{n}{2} C_2 \times^{2n-2} C_n + \dots + (-1)^n \binom{n}{n} C_n^n C_n = 1$ .

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85. If  $C_0, C_1, C_2, \dots, C_n$  denote the binomial coefficients in the expansion of  $(1+x)^n$ , then  $\sum_{r=0}^n \sum_{s=0}^n (C_r + C_s)$

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86. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , find the values of the following  $\sum_{i=0}^n \sum_{j=0}^n (i + j)C_iC_j$

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87. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , find the values of the following  $\sum_{0 \leq i < j \leq n} C_i$

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88. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , find the values of the following  $\left( \sum_{0 \leq i < j \leq n} \sum_{j} jC_i \right)$

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89. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ ,  
find the values of the following

$$\sum_{0 \leq i < j \leq n} j C_i$$

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90. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , find the values of the following  $\left( \sum \sum \right)_{0 \leq i \leq j \leq n} C_i C_j$

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91. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ ,

find the values of the following

$$\left( \sum \sum \right)_{0 \leq i \leq j \leq n} (i + j) (C_i \pm C_j)^2$$

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92. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ ,

find the values of the following

$$\left( \sum \sum \right)_{0 \leq i \leq j \leq n} (i + j) (C_i \pm C_j)^2$$



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93. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ ,

find the values of the following

$$\sum_{0 \leq i \leq j \leq n} C_i C_j$$



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94. If  $\binom{2n+1}{0} + \binom{2n+1}{3} + \binom{2n+1}{6} + \dots = 170$ , then n

equals

A. 2

B. 4

C. 6

D. 8

Answer: b



$$95. ({}^m C_0 + {}^m C_1 - {}^m C_2 - {}^m C_3) \\ + ({}^m C_4 + {}^m C_5 - {}^m C_6 - {}^m C_7) + \dots = 0$$

if and only if for some positive integer  $k$ ,  $m$  is equal to

- A.  $4k$
- B.  $4k + 1$
- C.  $4k - 1$
- D.  $4k + 2$

**Answer: c**



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96. The coefficient of  $x^n$  in  $(1 + x)^{101} (1 - x + x^2)^{100}$  is non zero, then  $n$  cannot be of the form

- A.  $3\lambda + 1$

B.  $3\lambda$

C.  $3\lambda + 2$

D. none of these

**Answer: C**



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97. The sum  $\sum_{i=0}^m {}^{10}C_i \times {}^{20}C_{m-i}$  (where  ${}^pC_q = 0$  if  $p < q$ )

is maximum, when m is

A. 5

B. 10

C. 15

D. 20

**Answer: c**



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98. If  ${}^{n-1}C_r = (k^2 - 3) \cdot {}^n C_{r+1}$ , then  $k$  belong to

A.  $(-\infty, -2]$

B.  $[2, \infty)$

C.  $[-\sqrt{3}, \sqrt{3}]$

D.  $(\sqrt{3}, 2]$

**Answer: D**



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99. If  $\left(x + \frac{1}{x} + 1\right)^6 = a_0 \left(a_1 x + \frac{b_1}{x}\right) + \left(a_2 x^2 + \frac{b_2}{x^2}\right) + \dots + \left(a_6 x^6 + \frac{b_6}{x^6}\right)$ ,

the value of  $a_0$  is

A. 121

B. 131

C. 141

D. 151

**Answer: C**



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**100.** The coefficient of  $x^{50}$  in the series

$$\sum_{r=1}^{101} r x^{r-1} (1+x)^{101-r} \text{ is}$$

A.  $^{100}C_{50}$

B.  $^{101}C_{50}$

C.  $^{102}C_{50}$

D.  $^{103}C_{50}$

**Answer: c**



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101. The largest integer  $\lambda$  such that  $2^\lambda$  divides

$3^{2^n} - 1, n \in N$  is

A.  $n - 1$

B.  $n$

C.  $n + 1$

D.  $n + 2$

**Answer:**



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102. If the last term in the binomial expansion of

$\left(2^{\frac{1}{3}} - \frac{1}{\sqrt{2}}\right)^n$  is  $\left(\frac{1}{3^{\frac{5}{3}}}\right)^{\log_3 8}$ , then 5th term from the beginning is 210 b.

420 c. 105 d. none of these

A.  ${}^{10}C_6$

B.  $2^{10}C_4$

C.  $\frac{1}{2} \cdot {}^{10}C_4$

D. None of the above

**Answer:**



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103. If  $f(x) = \sum_{r=1}^n \{r^2({}^nC_r - {}^nC_{r-1}) + (2r+1){}^nC_r\}$

and  $f(30) = 30(2)^\lambda$ , then the value of  $\lambda$  is

A. 3

B. 4

C. 5

D. 6

**Answer:**



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104. Let  $a_n = \left(1 + \frac{1}{n}\right)^n$ . Then for each  $n \in \mathbb{N}$

A.  $a_n \geq 2$

B.  $a_n < 3$

C.  $a_n < 4$

D.  $a_n < 2$

Answer: a, b, c

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105. Prove that  $\sum_{k=0}^n {}^n C_k \sin Kx \cdot \cos(n - K)x = 2^{n-1} \sin nx$

A.  $S_5\left(\frac{\pi}{2}\right) = 16$

B.  $S_7\left(\frac{-\pi}{2}\right) = 64$

C.  $S_{50}(\pi) = 0$

D.  $S_{51}(-\pi) = -2^{50}$

**Answer: a, b, c**



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**106.** If  $a + b = k$ , when  $a, b > 0$  and

$$S(k, n) = \sum_{r=0}^n r^2 \binom{n}{r} a^r \cdot b^{n-r}, \text{ then}$$

A.  $S(1, 3) = 3(3a^2 + ab)$

B.  $S(2, 4) = 16(4a^2 + ab)$

C.  $S(3, 5) = 25(5a^2 + ab)$

D.  $S(4, 6) = 36(6a^2 + ab)$

**Answer: a, b**



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107. The value of  $x$ , for which the ninth term in the

expansion of  $\left\{ \frac{\sqrt{10}}{(\sqrt{x})^{5 \log_{10} x}} + x \cdot x^{\frac{1}{2 \log_{10} x}} \right\}^{10}$

is 450 is equal to

A. 10

B.  $10^2$

C.  $\sqrt{10}$

D.  $10^{-2/5}$

Answer: b, d



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108. For a positive integer  $n$ , if the expansion of

$\left( \frac{5}{x^2} + x^4 \right)^n$  has a term independent of  $x$ , then  $n$  can be

A. 18

B. 27

C. 36

D. 45

**Answer: a, b, c, d**



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109. Consider  $(1 + x + x^2)^n = \sum_{r=0}^n a_r x^r$ , where  $a_0, a_1, a_2, \dots, a_{2n}$  are real number and  $n$  is positive integer.

If  $n$  is even, the value of  $\sum_{r=0}^{n/2-1} a_{2r}$  is

A.  $\frac{9^n - 2a_{2n} - 1}{4}$

B.  $\frac{9^n - 2a_{2n} + 1}{4}$

C.  $\frac{9^n + 2a_{2n} - 1}{4}$

D.  $\frac{9^n + 2a_{2n} + 1}{4}$

**Answer: b**



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110. Consider  $(1 + x + x^2)^n = \sum_{r=0}^n a_r x^r$ , where  $a_0, a_1, a_2, \dots, a_{2n}$  are real number and n is positive integer.

If n is odd, the value of  $\sum_{r=1}^2 a_{2r-1}$  is

A.  $\frac{9^n - 1}{2}$

B.  $\frac{9^n - 1}{4}$

C.  $\frac{9^n + 1}{2}$

D.  $\frac{9^n + 1}{4}$

Answer: b



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111. Consider  $(1 + x + x^2)^n = \sum_{r=0}^{2n} a_r x^r$ , where  $a_0, a_1, a_2, \dots, a_{2n}$  are real numbers and n is a positive integer.

The value of  $a_2$  is

A.  ${}^{4n+1}C_2$

B.  ${}^{3n+1}C_2$

C.  ${}^{2n+1}C_2$

D.  ${}^{n+1}C_2$

Answer: c



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112. Let  $S = \sum_{r=1}^{30} \frac{{}^{30+r}C_r(2r-1)}{{}^{30}C_r(30+r)}$ ,  $K = \sum_{r=0}^{30} ({}^{30}C_r)^2$

and  $G = \sum_{r=0}^{60} (-1)^r ({}^{60}C_r)^2$

The value fo (G-S)is

A. 0

B. 1

C.  $2^{30}$



D.  $2^{60}$

Answer: b



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113. Let  $S = \sum_{r=1}^{30} \frac{{}^{30+r}C_r(2r-1)}{{}^{30}C_r(30+r)}$ ,  $K = \sum_{r=0}^{30} ({}^{30}C_r)^2$

and  $G = \sum_{r=0}^{60} (-1)^r ({}^{60}C_r)^2$

The value  $(SK - SG)$  is

A. 0

B. 1

C.  $2^{30}$

D.  $2^{60}$

Answer: a



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114. Let  $S = \sum_{r=1}^{30} \frac{{}^{30+r}C_r(2r-1)}{{}^{30}C_r(30+r)}$ ,  $K = \sum_{r=0}^{30} ({}^{30}C_r)^2$

and  $G = \sum_{r=0}^{60} (-1)^r ({}^{60}C_r)^2$

The value of  $K + G$  is

A.  $2S - 2$

B.  $2S - 1$

C.  $2S + 1$

D.  $2S + 2$

Answer: d



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115. The digit at units place in  $2^9 \wedge 100$  is (A) 2 (B) 4 (C) 6 (D) 8



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116. If  $(1 + x)^n = \sum_{r=0}^n a_r x^r$  &  $b_r = 1 + \frac{a_r}{a_{r-1}}$  &  $\prod_{r=1}^n b_r = \frac{(101)^{100}}{100!}$ , then

equals to: 99 (b) 100 (c) 101 (d) None of these



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117. Statement-1 (Assertion) and Statement-2 (Reason)

Each of the these examples also has four alternative choices , only one of which is the correct answer. You have to select the correct choice as given below .

$(7^9 + 9^7)$  is divisible by 16

Statement-2  $(x^y + y^x)$  is divisible by  $(x + y)$ ,  $\forall x, y$ .

A. Statement-1 is true ,Statement-2 is true, Statement-2 is a correct explanation for Statement-1

B. Statement-1 is true ,Statement-2 is true, Statement-2 is not a correct explanation for Statement-1

C. Statement-1 is true ,Statement-2 is false

D. Statement-1 is true ,Statement-2 is ture

**Answer: c**

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**118.** Statement-1 (Assertion) and Statement-2 (Reason)

Each of the these examples also has four laternative choices ,  
only one of which is the correct answer. You have to select the correct  
choice as given below .

Number of distincet terms in the

sum of expansion  $(1 + ax)^{10} + (1 - ax)^{10}$  is 22.

A. Statement-1 is ture ,Statement-2 is treu, Statement-2 is a correct  
explanation for Statement-1

B. Statement-1 is ture ,Statement-2 is treu, Statement-2 is not a correct  
explanation for Statement-1

C. Statement-1 is true ,Statement-2 is false

D. Statement-1 is true ,Statement-2 is ture

Answer: d

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119. Find the term independent of  $x$  in the expansion of

$$(1 + x + 2x)^3 \left( \frac{3}{2}x^2 - \frac{1}{3x} \right)^9.$$

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120.  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n,$

show that  $\sum_{r=0}^n C_r^3$  is equal to the coefficient of  $x^n y^n$  in the

expansion of  $\{(1 + x)(1 + y)(x + y)\}^n.$

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121. Let  $(1 + x^2)^2 \cdot (1 + x)^n = \sum_{k=0}^{n+4} a_k \cdot x^k$  If  $a_1, a_2$  and  $a_3$  are in  $AP$ ,

find  $n$ .

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122. if  $(1 - x^3)^n = \sum_{r=0}^n a_r x^r (1 - x)^{3n-2r}$ , where  $n \in \mathbb{N}$  then find  $a_r$ .

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123. If  $a_0, a_1, a_2, \dots, a_{2n}$  are the coefficients in the expansion of  $(1 + xx^2)^n$  in ascending of  $x$  show

that  $a_0^2 - a_1^2 - a_2^2 - \dots + a_{2n}^2 = a_n$ .

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124. Show that no three consecutive binomial coefficients can be in (i) G.P.,  
(ii) H.P.



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125. Show that no three consecutive binomial coefficients can be in (i) G.P.,  
(ii) H.P.



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126. Evaluate  $\sum_{i=0}^n \sum_{j=0}^n {}^n C_j \cdot {}^j C_i, i \leq j$ .



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127. Find the remainder when  $27^{40}$  is divided by 12.



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128. show that  $\left[ (\sqrt{3} + 1)^{2n} \right] + 1$  is divisible by  $2^{n+1}$

$\forall n \in \mathbb{N}$ , where  $[.]$  denote the greatest integer function .



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129. Find number of rational terms in  $(\sqrt{2} + 3^{\frac{1}{3}} + 5^{\frac{1}{6}})^{10}$



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130. Find the remainder when  $1690^{2608} + 2608^{1690}$  is divided by 7.



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131. If  $C_0, C_1, C_2, \dots, C_n$  are the binomial coefficients

in the expansion of  $(1 + x)^n$ , prove that

$$(C_0 + 2C_1 + C_2)(C_1 + 2C_2 + C_3) \dots (C_{n-1} + 2C_n + C_{n+1})$$

$$\frac{(n-2)^n}{(n+1)!} \prod_{r=1}^n (C_{r-1} + C_r).$$



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132. If  $\sum_{r=0}^{2n} a_r(x-2)^r = \sum_{r=0}^{2n} b_r(x-3)^r$  and  $a_k = 1$  for all  $k \geq n$ , then show that  $b_n = {}^{2n+1}C_{n+1}$ .

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133. If  $n$  is an odd natural number, then  $\sum_{r=0}^n \frac{(-1)^r}{{}^nC_r}$  is equal to

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134. If  $n$  is an even natural number, then  $\sum_{r=0}^n \frac{(-1)^r}{{}^nC_r}$  equals

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135. If  $(1+x)^n = C_0 + C_1x + C_2x^2 + C_3x^3 + \dots + C_nx^n$ , show that  $C_1 - \frac{C_2}{2} + \frac{C_3}{3} - \dots + (-1)^{n-1} \frac{C_n}{n} = 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$ .

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**136.** If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + C_3x^3 + \dots + C_nx^n$ , find the sum of the seriesd

$$\frac{C_0}{2} - \frac{C_1}{6} + \frac{C_2}{10} + \frac{C_3}{14} - \dots + (-1)^n \frac{C_n}{4n + 2}.$$

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**137.** If  $(1 + x)^n = \sum_{r=0}^n C_r x^r$ , then prove that

$$\left( \sum \sum \right)_{0 \leq i < j \leq n} \left( \frac{i}{C_i} + \frac{j}{C_j} \right) = \frac{n^2}{2} \sum_{r=0}^n \frac{1}{C_r}.$$

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**138.** If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + c_3x^3 + \dots + C_nx^n$ , show that

$$\frac{\sum_{r=0}^n \frac{C_r 3^{r+4}}{(r+1)(r+2)(r+3)(r+4)}}{(n+1)(n+2)(n+3)(n+4)} \left( 4^{n+4} - \sum_{t=0}^3 {}^{n+4}C_{t^t} \right).$$

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139. Prove that  $\sum_{k=0}^9 x^k$  divides  $\sum_{k=0}^9 x^{kkkk}$

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140. Prove that  $\sum_{r=1}^k (-3)^{r-1} C(3n, 2r-1) = 0$ , where  $k = \frac{3n}{2}$  and  $n$  is an even positive integer.

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141. Prove that

$${}^n C_3 + {}^n C_7 + {}^n C_{11} + \dots = \frac{1}{2} \left\{ 2^{n-1} - 2^{n/2} \sin \frac{n\pi}{4} \right\}$$

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142. Evaluate  $\sum_{i=0}^{n-1} \sum_{j=1+i}^{n+1} {}^n C_i {}^{n+1} C_j$ .

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**143.** If  $(9 + 4\sqrt{5})^n = I + f$ ,  $n$  and  $I$  being positive integers and  $f$  is a proper fraction, show that  $(I - 1)f + f^2$  is an even integer.

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**144.** If  $P_r$  is the coefficient of  $x^{\mathbb{R}}$  in the expansion of

$(1 + x)^2 \left(1 + \frac{x}{2}\right)^2 \left(1 + \frac{x}{2^2}\right)^2 \left(1 + \frac{x}{2^3}\right)^2 \dots$  prove that

$$P_r = \frac{2^2}{(2^r - 1)} (P_{r-1} + P_{r-2}) \text{ and } P_4 = \frac{1072}{315} .$$

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**Jee Type Solved Example Matching Type Questions**

Column I		Column II	
(A)	If $m$ and $n$ are the numbers of rational terms in the expansions of $(\sqrt{2} + 3^{1/5})^{10}$ and $(\sqrt{3} + 5^{1/8})^{256}$ respectively, then	(p)	$n - m = 6$
(B)	If $m$ and $n$ are the numbers of irrational terms in the expansions of $(2^{1/2} + 3^{1/5})^{40}$ and $(5^{1/10} + 2^{1/6})^{100}$ respectively, then	(q)	$m + n = 20$
(C)	If $m$ and $n$ are the numbers of rational terms in the expansions of $(1 + \sqrt{2} + 3^{1/3})^6$ and $(1 + \sqrt[3]{2} + \sqrt[3]{3})^{15}$ respectively, then	(r)	$n - m = 31$
		(s)	$m + n = 35$
		(t)	$n - m = 39$

1.



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Column I		Column II	
(A)	If $S = \sum_{r=0}^n \lambda C_r$ and values of $S$ are $a, b, c$ for $\lambda = 1, r, r^2$ respectively, then	(p)	$a = b + c$
(B)	If $S = \sum_{r=0}^n (-1)^r \lambda C_r$ and values of $S$ are $a, b, c$ for $\lambda = 1, r, r^2$ respectively, then	(q)	$a + b = c + 2$
(C)	If $S = \sum_{r=0}^n \frac{\lambda C_r}{(r+1)}$ and values of $S$ are $a, b, c$ for $\lambda = 1, r, r^2$ respectively, then	(r)	$a^3 + b^3 + c^3 = 3abc$
		(s)	$b^{c-a} + (c-a)^b = 1$
		(t)	$a + c = 4b$

2.



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## Exercise For Session 1

1. The value of  $\sum_{r=0}^{10} r^{10} C_r 3^r (-2)^{10-r}$  is 20 b. 10 c. 300 d. 30

A. 10

B. 20

C. 30

D. 300

**Answer: c**



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2. The number of distinct terms in the expansion of  $\left(x + \frac{1}{x} + \frac{1}{x^2}\right)^{15}$  is/are (with respect to different power of  $x$ ) 255 b. 61 c. 127 d. none of these

A. 61

B. 121

C. 255

D. 16

**Answer: a**



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3. The expression  $\left[ x + (x^3 - 1)^{\frac{1}{2}} \right]^5 + \left[ x - (x^3 - 1)^{\frac{1}{2}} \right]^5$  is a polynomial of degree

A. 5

B. 6

C. 6

D. 8

**Answer: c**



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4.  $(\sqrt{2} + 1)^6 - (\sqrt{2} - 1)^6$  is equal to

A. 101

B.  $70\sqrt{2}$

C.  $140\sqrt{2}$

D.  $120\sqrt{2}$

Answer: c



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5. The total number of dissimilar terms in the expansion of  $(x + a)^{100} + (x - a)^{100}$  after simplification will be

A. 202

B. 51



C. 50

D. 101

**Answer: b**



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6. Find the number of nonzero terms in the expansion of  $(1 + 3\sqrt{2}x)^9 + (1 - 3\sqrt{2}x)^9$ .

A. 0

B. 5

C. 9

D. 10

**Answer: b**



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7. If  $(1+x)^n = \sum_{r=0}^n C_r x^r, \left(1 + \frac{C_1}{C_0}\right) \left(1 + \frac{C_2}{C_1}\right) \dots \left(1 + \frac{C_n}{C_{n-1}}\right)$  is

equal to

- A.  $\frac{n^{n-1}}{(n-1)!}$
- B.  $\frac{(n+1)^{n-1}}{(n-1)!}$
- C.  $\frac{(n+1)^n}{n!}$
- D.  $\frac{(n+1)^{n+1}}{n!}$

**Answer: c**



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8. If  ${}^{n+1}C_{r+1} : {}^n C_r : {}^{n-1}C_{r-1} = 11 : 6 : 3$ , find the values of n and r.

- A. 20
- B. 30
- C. 0
- D. 50

**Answer: c**



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## Exercise For Session 2

1. If the  $r$ th term in the expansion of  $(1 + x)^{20}$  has its coefficient equal to that of the  $(r + 4)$ th term, find  $r$

A. 7

B. 9

C. 11

D. 13

**Answer: b**



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2. If the fourth term in the expansion of  $\left(px + \frac{1}{x}\right)^n$  is  $\frac{5}{2}$ , then  $(n, p) =$

A.  $\frac{9}{2}$

B.  $\frac{11}{2}$

C.  $\frac{13}{2}$

D.  $\frac{15}{2}$

**Answer: c**



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3. In  $\left(33 + \frac{1}{33}\right)^n$  if the ratio of 7th term from the beginning to the 7th term from the end is  $\frac{1}{6}$ , then find the value of  $n$ .

A. 3

B. 5

C. 7

D. 9

**Answer: d**



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4. Find the number of integral terms in the expansion of  $\left(5^{\frac{1}{2}} + 7^{\frac{1}{8}}\right)^{1024}$ .

A. 128

B. 129

C. 130

D. 131

**Answer: b**



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5. In the expansion of  $\left(7^{\frac{1}{3}} + 11^{\frac{1}{9}}\right)^{6561}$ , the number of terms free from radicals is:

- A. 715
- B. 725
- C. 730
- D. 750

**Answer: c**



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6. If the coefficients of three consecutive terms in the expansion of  $(1 + x)^n$  are 165,330 and 462 respectively, the value of n is

- A. 7
- B. 9
- C. 11

D. 13

**Answer: c**



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7. If the coefficients of 5th, 6th , and 7th terms in the expansion of  $(1 + x)^n$  are in A.P., then  $n =$  a. 7 only b. 14 only c. 7 or 14 d. none of these

A. 7only

B. 14 only

C. 7 or 14

D. None of these

**Answer: c**



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8. If the middle term in the expansion of  $(x^2 + 1/x)^n$  is  $924x^6$ , then find the value of  $n$ .

A. 8

B. 12

C. 16

D. 20

**Answer: b**



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9. If the sum of the binomial coefficients in the expansion of  $\left(x^2 + \frac{2}{x^3}\right)^n$  is 243, the term independent of  $x$  is equal to

A. 40

B. 30

C. 20



D. 10

**Answer: a**



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10. In the expansion of  $(1 + x)(1 + x + x^2) \dots (1 + x + x^2 + \dots + x^{2n})$ , the sum of the coefficients is

A. 1

B.  $2n!$

C.  $2n!+1$

D.  $(2n + 1)!$

**Answer: d**



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## Exercise For Session 3

1. If  $R = (7 + 4\sqrt{3})^{2n} = 1 + f$ , where  $I \in \mathbb{N}$  and

$0 < f < 1$ , then  $R(1 - f)$  equals

A. 1

B. 0

C. -1

D. even integer

**Answer: a**

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2. If  $(5 + 2\sqrt{6})^n = I + f$ , where  $I \in \mathbb{N}$ ,  $n \in \mathbb{N}$  and

$0 \leq f \leq 1$ , then  $I$  equals

A.  $\frac{1}{f} - f$

B.  $\frac{1}{1+f} - f$

C.  $\frac{1}{1-f} - f$

D.  $\frac{1}{1+f} + f$

**Answer: c**



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3. If  $n > 0$  is an odd integer and

$x = (\sqrt{2} + 1)^n$ ,  $f = x - [x]$ , then  $\frac{1-f^2}{f}$  is

- A. an irrational number
- B. a non-integer rational number
- C. an odd number
- D. an even number

**Answer: d**



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4. Integral part of  $(\sqrt{2} + 1)^6$  is

- A. 196
- B. 197
- C. 198
- D. 199

**Answer: b**



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5.  $(103)^{86} - (86)^{103}$  is divisible by

- A. 7
- B. 13
- C. 17
- D. 23

**Answer: c**



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6. fractional part of  $\frac{2^{78}}{31}$  is:

A.  $\frac{2}{31}$

B.  $\frac{4}{31}$

C.  $(8)/(31)'$

D.  $(16)/(31)'$

**Answer: c**



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7. The unit digit of  $17^{1983} + 11^{1983}$  is

A. 4

B. 2

C. 3

D. 0

**Answer: a**



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8. The last two digits of the number  $(23)^{14}$  are 01 b. 03 c. 09 d. none of these

A. 1

B. 3

C. 9

D. 27

**Answer: c**



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9. The last four digits of the natural number  $3^{100}$  are

A. 2001

B. 3211

C. 1231

D. 1

**Answer: a**



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10. The remainder when  $23^{23}$  is divided by 53 is

A. 17

B. 21

C. 30

D. 47

Answer: c



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### Exercise For Session 4

1. The coefficient of  $a^8b^4c^9d^9$  in  $(abc + abd + acdd + bcd)^{10}$  is  $10!$  b.

$\frac{10!}{8!4!9!9!}$  c. 2520 d. none of these

A.  $10!$

B.  $\frac{10!}{4!8!9!9!}$

C. 2520

D. None of these

Answer: c



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2. If  $(1 + 2x + 3x^2)^{10} = a_0 + a_1x + a_2x^2 + \dots + a_{20}x^{20}$ , then  $a_1$  equals

10 b. 20 c. 210 d. none of these

A. 210

B. 20

C. 10

D. None of these

**Answer: b**



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3. If  $(1 + x + x^2 + x^3)^5 = a_0 + a_1x + a_2x^2 + \dots + a_{15}x^{15}$ , then  $a_{10}$

equals to

A. 99

B. 100

C. 101

**Answer: c****Watch Video Solution**

4. Coefficient of  $x^{15}$  in  $(1 + x + x^3 + x^4)^n$  is

A.  $\sum_{r=0}^5 {}^n C_{5-r} \cdot {}^n C_{3r}$

B.  $\sum_{r=0}^5 {}^n C_{5r}$

C.  $\sum_{r=0}^5 {}^n C_{2r}$

D.  $\sum_{r=0}^5 {}^n C_{3-r} \cdot {}^n C_{5r}$

**Answer: a****Watch Video Solution**

5. The number of terms in the expansion of  $\left(x^2 + 1 + \frac{1}{x^2}\right)^n$ ,  $n \in N$ , is:

A.  ${}^{n+2}C_2$

B.  ${}^{n+3}C_2$

C.  ${}^{2n+1}C_{2n}$

D.  ${}^{3n+1}C_{3n}$

**Answer: a**



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6. If  $(1 + x)^{10} = a_0 + a_1x + a_2x^2 + \dots + a_{10}x^{10}$ , then value of  $(a_0 - a_2 + a_4 - a_6 + a_8 - a_{10})^2 + (a_1 - a_3 + a_5 - a_7 + a_9)^2$  is

A.  $2^9$

B.  $3^9$

C.  $2^{10}$

D.  $3^{10}$

**Answer: c**

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7. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , then

the sum  $C_0 + (C_0 + C_1) + \dots + (C_0 + C_1 + \dots + C_{n-1})$  is equal to

A.  $n \cdot 2^n$

B.  $n \cdot 2^{n-1}$

C.  $n \cdot 2^{n-2}$

D.  $n \cdot 2^{n-3}$

Answer: b

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8.  $\frac{C_0}{1} \cdot 3 - \frac{C_1}{2} \cdot 3 + \frac{C_2}{3} \cdot 3 - \frac{C_3}{4} \cdot 3 + \dots + (-1)^n \frac{C_n}{(n+1) \cdot 3}$  01+23+

$(-1)^1 \cdot 3 \quad 2 \cdot 3 \quad 3 \cdot 3 \quad 4 \cdot 3$

A.  $\frac{3}{n+1}$

B.  $\frac{n+1}{3}$

C.  $\frac{1}{3(n+1)}$

D. None of these

**Answer: c**



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9. The value of  $\binom{50}{0}\binom{50}{1} + \binom{50}{1}\binom{50}{2} + \dots + \binom{50}{49}\binom{50}{50}$

is

A.  $\binom{100}{50}$

B.  $\binom{100}{51}$

C.  $\binom{50}{25}$

D.  $\binom{50}{25}^2$

**Answer: b**



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10. If  $c_r = nC_r$  then  $\frac{C_1}{2} - \frac{C_2}{3} + \frac{C_3}{4} - \dots - \frac{C_{100}}{101}$  is equal to

A.  $C_1$

B.  $C_2$

C.  $C_3$

D.  $C_4$

Answer: b



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11. The sum  $\sum_{r=0}^n (r+1)(C_r)^2$  is equal to :

A.  $\frac{(n+2)(2n-1)!}{n!(n-1)!}$

B.  $\frac{(n+2)(2n+1)!}{n!(n-1)!}$

C.  $\frac{(n+2)(2n+1)!}{n!(n+1)!}$

D.  $\frac{(n+2)(2n-1)!}{n!(n+1)!}$

Answer: a



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12.  $\sum_{r=1}^n \left\{ \sum_{r_1=0}^{r-1} {}^n C_r {}^n C_{r_1} 2^r 1 \right\}$  is equal to

A.  $4^n - 3^n + 1$

B.  $4^n - 3^n - 1$

C.  $4^n - 3^n + 2$

D.  $4^n - 3^n$

Answer: d



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13. The value of the expression  $\left( \sum_{r=0}^{10} {}^{10} C_r \right) \left( \sum_{k=0}^{10} (-1)^k \frac{{}^{10} C_k}{2^k} \right)$  is :

A. 1

B.  $2^5$

C.  $2^{10}$

D.  $2^{20}$

**Answer: a**



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14. The value of  $\left(\sum \sum \sum \sum\right)_{0 \leq i < j < k < l \leq n}$  2 is equal to

A.  $2(n + 1)^3$

B.  $2 \cdot {}^{n+1}C_4$

C.  $2(n + 1)^4$

D.  $2 \cdot {}^{n+2}C_3$

**Answer: b**



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## Exercise Single Option Correct Type Questions

1.  $\sum_{r=0}^n (-1)^r C(n, r) \left( \left( \frac{1}{2^r} \right) + \left( \frac{3^r}{2^{2r}} \right) + \left( \frac{7^r}{2^{3r}} \right) + \dots \right)$  is equal to

A. -6

B. -3

C. 3

D. Cannot be determined

**Answer: d**



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2. The coefficient of  $(x^3 \cdot b^6 \cdot C^8 \cdot d^9 \cdot e \cdot f)$  in the expansion of  $(a + b + c - d - e - f)^{31}$  is

A. 12632

B. 23110

C. 3110

D. None of these

**Answer: d**



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**3. Find the number of rational terms and also find**

the sum of rational terms in  $(\sqrt{2} + \sqrt[3]{3} + \sqrt[6]{5})^{10}$

A. 12632

B. 1260

C. 126

D. None of these

**Answer: a**



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4. If  $(1 + x - 3x^2)^{2145} = a_0 + a_1x + a_2x^2 + \dots$  then  $a_0 - a_1 + a_2 - \dots$

ends with

A. 1

B. 3

C. 7

D. 9

**Answer: b**



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5. In the expansion of  $\left(\sqrt{\frac{q}{p}} + \sqrt[10]{\frac{p^7}{q^3}}\right)^n$ , there is a term

similar to  $pq$ , then that term is equal to

A.  $45pq$

B.  $120pq$

C. 210 pq

D. 252 pq

**Answer: d**



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6. If  $(5 + 2\sqrt{6})^n = I + f$ , where  $I \in \mathbb{N}$ ,  $n \in \mathbb{N}$  and

$0 \leq f < 1$ , then  $I$  equals

A. a natural number

B. a negative integer

C. a prime number

D. an irrational number

**Answer: b**



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7. If  $x + \frac{1}{x} = 1$  and  $p = x^{4000} + \frac{1}{x^{4000}}$  and  $q$  is the digit at unit place in the number  $2^{2^n} + 1$ ,  $n \in \mathbb{N}$  and  $n > 1$ , then  $p + q$  is .

A. 8

B. 6

C. 7

D. None of these

Answer: b



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8. If the number of terms in  $\left(x + 1 + \frac{1}{x}\right)^n$  ( $n \in I^+$  is 401, then  $n$  is greater than

A. 201

B. 200

C. 199

D. None of these

Answer: d

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9. The value of  $\sum_{r=0}^{n-1} \left( \frac{C_r}{{}^nC_r + {}^nC_{r+1}} \right)$  is equal to

A.  $\frac{n}{2}$

B.  $\frac{n+1}{2}$

C.  $\frac{n(n+1)}{2}$

D.  $\frac{n(n-1)}{2(n+1)}$

Answer: a

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10. The largest term in the expansion of  $\left( \frac{b}{2} + \frac{b}{2} \right)^{100}$  is

A.  $b^{100}$

B.  $\left(\frac{b}{2}\right)^{100}$

C.  ${}^{100}C_{50} \left(\frac{b}{2}\right)^{100}$

D.  ${}^{100}C_{50} b^{100}$

**Answer: c**



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11. If the fourth term of  $\left(\frac{1}{x^{1+(\log)_{10}x} + x^{12}}\right)^6$  is equal to 200 and  $x > 1$ , then  $x$  is equal to  $10\sqrt{2}$  (2) 10 (3)  $10^4$  (4) 100

A.  $10\sqrt{2}$

B. 10

C.  $10^4$

D.  $\frac{10}{\sqrt{2}}$

**Answer: b**



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12. Coefficient of  $x^m$  in

$(1+x)^m + (1+x)^{m+1} + \dots + (1+x)^n, m < n$  is

A.  ${}^{n+1}C_{m+1}$

B.  ${}^{n-1}C_{m-1}$

C.  ${}^nC_m$

D.  ${}^nC_{m+1}$

Answer: a



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13. The number of values of 'r' satisfying the equation

$${}^{39}C_{3r-1} - {}^{39}C_{r^2} = {}^{39}C_{r^2-1} - {}^{39}C_{3r} \text{ is}$$

A. 1



B. 2

C. 3

D. 4

**Answer: b**



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**14.** The sum  $S = {}^{20}C_2 + 2 \cdot {}^{20}C_3 + 3 \cdot {}^{20}C_4 + \dots + 19 \cdot {}^{20}C_{20}$  is equal to

A.  $1 + 5 \cdot 2^{20}$

B.  $1 + 2^{21}$

C.  $1 + 9 \cdot 2^{20}$

D.  $2^{20}$

**Answer: c**



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15. The remainder, if  $1 + 2 + 2^2 + 2^3 + \dots + 2^{1999}$  is divided by 5, is

A. 0

B. 1

C. 2

D. 3

**Answer: a**



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16. Coefficient of  $\frac{1}{x}$  in the expansion of  $(1 + x)^n(1 + 1/x)^n$  is

A.  $\frac{n!}{(n-1)!(n+1)!}$

B.  $\frac{2n!}{(n-1)!(n+1)!}$

C.  $\frac{n!}{(2n-1)!(1n+1)!}$

D.  $\frac{2n!}{(2n-1)!(1n+1)!}$

**Answer: b**



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17. The last two digits of the number  $19^{94}$  is

A. 19

B. 29

C. 39

D. 81

**Answer: a**



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18. If the second term in the expansion of  $\left(\sqrt[3]{a} + \frac{a}{\sqrt{a^{-1}}}\right)^n$  is

$14a^{5/2}$  then value of  $\frac{{}^nC_3}{{}^nC_2}$  is

A. 19

B. 29

C. 39

D. 81

**Answer: a**



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19. If  $6^{83} + 8^{83}$  is divided by 49, the remainder is

A. 0

B. 14

C. 35

D. 42

**Answer: c**



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20. The sum of all rational terms in the expansion of

$$\left(3^{1/4} + 4^{1/3}\right)^{12} \text{ is}$$

A. 91

B. 251

C. 273

D. 283

**Answer: d**



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21. Sum of last three digits of the number  $N = 7^{100} - 3^{100}$  is.

A. 2000

B. 4000

C. 6000

D. 8000

**Answer: d**



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22. If  $5^{99}$  is divided by 13, the remainder is

A. 2

B. 4

C. 6

D. 8

**Answer: d**



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23. The value of  $\left\{ \frac{3^{2003}}{28} \right\}$  is

A.  $17/28$

B.  $19/28$

C.  $23/28$

D.  $2/28$

**Answer: b**



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24. The value of  $\sum_{r=0}^{20} r(20-r) \binom{20}{r}^2$  is equal to  $400^{39}C_{20}$  b.  $400^{40}C_{19}$  c.  $400^{39}C_{19}$  d.  $400^{38}C_{20}$

A.  $400^{37}C_{20}$

B.  $400^{40}C_{19}$

C.  $400^{38}C_{19}$

D.  $400^{38}C_{20}$

**Answer: d**



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25. If  $(3 + x^{2008} + x^{2009})^{2010} = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$ , then the value of  $a_0 - \frac{1}{2}a_1 - \frac{1}{2}a_2 + a_3 - \frac{1}{2}a_4 - \frac{1}{2}a_5 + a_6 - \dots$  is

A. 1

B.  $2^{2010}$

C.  $5^{2010}$

D.  $3^{2010}$

Answer: B



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26. The total number of terms which depend on the value of  $x$  in the expansion of  $\left(x^2 - 2 + \frac{1}{x^2}\right)^n$  is

A.  $2n + 1$



B.  $2n$

C.  $n + 1$

D.  $n$

**Answer: b**



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27. The coefficient of  $x^{10}$  in the expansion of

$(1 + x^2 - x^3)^8$ , is

A. 420

B. 476

C. 532

D. 588

**Answer: b**



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28. The number of real negative terms in the binomial expansion of  $(1 + ix)^{4n-2}$ ,  $n \in \mathbb{N}$ ,  $n > 0$ ,  $I = \sqrt{-1}$ , is

- A.  $n$
- B.  $n + 1$
- C.  $n - 1$
- D.  $2n$

**Answer: a**



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29.  $\sum_{p=1}^n \sum_{m=p}^n \binom{n}{m} \binom{m}{p}$  is equal to

- A.  $3^n$
- B.  $2^n$
- C.  $3^2 + 2^n$

D.  $3^n - 2^n$

**Answer: D**



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**30.** The largest real value of  $x$ , such that

$$\sum_{r=0}^4 \left( \frac{5^{4-r}}{(4-r)!} \right) \left( \frac{x^r}{r!} \right) = \frac{8}{3} \text{ is}$$

A.  $2\sqrt{2} - 5$

B.  $2\sqrt{2} + 5$

C.  $-2\sqrt{3} - 5$

D.  $-2\sqrt{2} + 5$

**Answer: a**



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## Exercise More Than One Correct Option Type Questions

1. If in the expansion of  $(1 + x)^m(1 - x)^n$ , the coefficients of  $x$  and  $x^2$  are 3 and -6 respectively, the value of  $m$  and  $n$  are

- A. 3
- B. 6
- C. 9
- D. 12

**Answer:** c,d



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2. If the coefficients of  $r$ th,  $(r + 1)$ th and  $(r + 2)$ th terms in the expansion of  $(1 + x)^{1/4}$  are in AP, then  $r$  is /are

- A. 5

B. 9

C. 10

D. 12

**Answer: a,b**



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3. If  $n$  is a positive integer and  $(3\sqrt{3} + 5)^{2n+1} = l + f$  where  $l$  is an integer and  $0 < f < 1$ , then

A.  $\alpha$  is an even integer

B.  $(\alpha + \beta)^2$  is divisible by  $2^{2n+1}$

C. the integer just below  $(3\sqrt{3} + 5)^{2n+1}$  divisible by 3

D.  $\alpha$  is divisible by 10

**Answer: a,d**



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4. If  $(8 + 3\sqrt{7})^n = P + F$ , where P is an integer and F is a proper fraction, then

A. P is an odd integer

B. P is an even integer

C.  $F(P + F) = 1$

D.  $(1 - F)(P + F) = 1$

**Answer: a,d**

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5. The value of  $x$  for which the sixth term in the expansion of

$\left[ 2^{\log_2} - 2\sqrt{9^{(x-1)+7}} + \frac{1}{\frac{2^1}{5}(\log)_2(3^{(x-1)+1})} \right]^7$  is 84 is 4 b. 1 or 2 c.

0 or 1 d. 3

A. 4

B. 3

C. 2

D. 1

**Answer: c,d**



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6. Consider the binomial expansion of  $\left(\sqrt{x} + \left(\frac{1}{2x^{\frac{1}{4}}}\right)\right)^n$   $n \in \mathbb{N}$ , where the terms of the expansion are written in decreasing powers of  $x$ . If the coefficients of the first three terms form an arithmetic progression then the statement(s) which hold good is(are) (A) total number of terms in the expansion of the binomial is 8 (B) number of terms in the expansion with integral power of  $x$  is 3 (C) there is no term in the expansion which is independent of  $x$  (D) fourth and fifth are the middle terms of the expansion

A. Total number of terms in the expansion of the binomial is 8

B. Number of terms in the expansion with integral power of  $x$  is 3

C. There is no term in the expansion which is independent of  $x$

D. Fourth and fifth are the middle terms of the expansion

**Answer: b,c**



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7. Let  $(1 + x^2)^2(1 + x)^n = a_0 + a_1x + a_2x^2 + \dots$  if

$a_1, a_2$  and  $a_3$  are in A.P, the value of  $n$  is

A. 2

B. 3

C. 4

D. 7

**Answer: b,c**



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8. 10th term of  $\left(3 - \sqrt{\frac{17}{4} + 3\sqrt{2}}\right)^{20}$  is

- A. an irrational number
- B. a rational number
- C. a positive integer
- D. a negative integer

**Answer: a,d**



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9. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + C_3x^3 + \dots + C_nx^n$ , then

$C_0 - (C_0 - C_1) + (C_0 + C_1 + C_2) - (C_0 + C_1 + C_2 + C_3) + \dots + (-1)^n$

$(C_0) + C_1 + C_2 + \dots + C_{n-1}$ , when n is even integer is

- A. a positive value
- B. a negative value

C. divisible by  $2^{n-1}$

D. divisible by  $2^n$

**Answer: b,c**



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10. If  $f(m) = \sum_{i=0}^m \binom{30}{30-i} \binom{20}{m-i}$  where  $\binom{p}{q} = {}^pC_q$ , then (A) maximum value of  $f(m)$  is  $50C_{25}$  (B)  $f(0) + f(1) + \dots + f(50) = 2^{50}$  (C)  $f(m)$  is always divisible by 50 ( $1 \leq m \leq 49$ ) (D)  $\sum_{m=0}^{50} (f(m))^2 = 100C_{50}$

A. maximum value of  $f(m)$  is  ${}^{50}C_{25}$

B.  $f(0) + f(1) + f(2) + \dots + f(50) = 2^{50}$

C.  $f(m)$  is always divisible by 50

D.  $f^2(0) + f^2(1) + f^2(2) + \dots + f^2(50) = 100C_{50}$

**Answer: a,b,d**



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11. Number of values of  $r$  satisfying the equation

$${}^{69}C_{3r-1} - {}^{69}C_{r^2} = {}^{69}C_{r^2-1} - {}^{69}C_{3r} \text{ is}$$

A. 1

B. 2

C. 3

D. 7

Answer: c,d



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12. If the middle term of  $\left(x + \frac{1}{x} \sin^{-1} x\right)^8$  is equal to  $\frac{630}{16}$ ,

the value of  $x$  is/are

A.  $-\frac{\pi}{3}$

B.  $-\frac{\pi}{6}$

C.  $\frac{\pi}{6}$

D.  $\frac{\pi}{3}$

**Answer: a,d**



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13. If  $ac < b^2$  then the sum of the coefficient in the expansion of  $(a\alpha^2 x^2 + 2b\alpha x + c)^n$  is  $(a, b, c, \alpha \in R$  and  $n \in N)$

A. +ve, if  $a > 0$

B. +ve, if  $c > 0$

C. -ve, if  $a < 0$ ,  $n$  is odd

D. +ve, if  $c < 0$ ,  $n$  is even

**Answer: a,b,c,d**



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14. The number of terms in the expansion of  $\left(x^2 + 1 + \frac{1}{x^2}\right)^n$ ,  $n \in N$ ,

is:

A. number of term =  $2n + 1$

B. term independent of  $x = 2^{n-1}$

C. coefficient of  $x^{2n-2} = n$

D. coefficient of  $x^2 = n$

**Answer: a,c,**



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15. The coefficient of the  $(r + 1)$ th term of  $\left(x + \frac{1}{x}\right)^{20}$ , when

expanded in the descending power of  $x$ , is equal to the

coefficient of the 6th term of  $\left(x^2 + 2 + \frac{1}{x^2}\right)$  when

expanded in ascending power of  $x$ . The value of  $r$  is

A. 5

B. 6

C. 14

D. 15

**Answer: ad**



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### Exercise Passage Based Questions

1. Consider  $(1 + x + x^2)^n = \sum_{r=0}^n a_r x^r$ , where  $a_0, a_1, a_2, \dots, a_{2n}$  are real number and n is positive integer.

The value of  $\sum_{r=0}^{n-1} a_r$  is

A.  $\frac{-3^n - a_n}{2}$

B.  $\frac{3^n - a_n}{2}$

C.  $\frac{a_n - 3^n}{2}$

D.  $\frac{3^n + a_n}{2}$

Answer: b



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2. Consider  $(1 + x + x^2)^n = \sum_{r=0}^n a_r x^r$ , where  $a_0, a_1, a_2, \dots, a_{2n}$  are real number and n is positive integer.

If n is even, the value of  $\sum_{r=0}^{n/2-1} a_{2r}$  is

A.  $\frac{3^n - 1 + a_n}{2}$

B.  $\frac{3^n - 1 - a_n}{4}$

C.  $\frac{3^n + 1 + a_n}{2}$

D.  $\frac{3^n + 1 - 2a_n}{4}$

Answer: D



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3. Consider  $(1 + x + x^2)^n = \sum_{r=0}^n a_r x^r$ , where  $a_0, a_1, a_2, \dots, a_{2n}$  are real number and  $n$  is positive integer.

If  $n$  is odd, the value of  $\sum_{r=1}^2 a_{2r-1}$  is

A.  $\frac{3^n - 1 + 2a_n}{2}$

B.  $\frac{3^n - 1 + 2a_n}{4}$

C.  $\frac{3^n + 1 + 2n_n}{2}$

D.  $\frac{3^n + 1 - 2a_n}{4}$

Answer: b



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4. If  $(1 + x + 2x^2)^{20} = a_0 + a_1x + a_2x^2 + \dots + a_{40}x^{40}$ .

The value of  $a_0 + a_2 + a_4 + \dots + a_{38}$  is

A.  $2^{19}(2^{19} - 1)$

B.  $2^{20}(2^{19} - 1)$



C.  $2^{19}(2^{20} - 1)$

D.  $2^{20}(2^{20} - 19)$

**Answer: C**



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5. If  $(1 + x + 2x^2)^{20} = a_0 + a_1x + a_2x^2 + \dots + a_{40}x^{40}$ .

The value of  $a_0 + a_2 + a_4 + \dots + a_{38}$  is

A.  $2^{19}(2^{19} - 20)$

B.  $2^{19}(2^{20} - 21)$

C.  $2^{19}(2^{19} - 21)$

D.  $2^{19}(2^{19} - 19)$

**Answer: b**



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6. If  $(1 + x + 2x^2)^{20} = a_0 + a_1x + a_2x^2 + \dots + a_{40}x^{40}$ .

The value of  $\frac{a_{39}}{a_{40}}$ , is

A.  $2^{20}$

B.

C. 10

D. 1

Answer: c



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7. Suppose  $m$  divided by  $n$ , then quotient  $q$  and remainder  $r$   $n \mid m \Rightarrow m = nq + r$  or

$m = nq + r, \forall m, n, q, r \in \mathbb{Z}$  and  $n \neq 0$  If  $a$  is the remainder when  $5^{40}$  is divided by 11 and  $b$  is the remainder when  $2^{2011}$  is divided by 17, the value of  $a + b$  is

A. 7

B. 8

C. 9

D. 10

**Answer: c**



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8. Suppose  $m$  divided by  $n$ , then quotient  $q$  and remainder  $r$

$m = nq + r$

—

—

$r$

or  $m = nq + r, \forall m, n, q, r \in \mathbb{Z}$  and  $n \neq 0$

If  $13^{99}$  is divided by 81, the remainder is

A. 8

B. 4

C. 1

D. 0

**Answer: d**



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9. Suppose  $m$  divided by  $n$ , then quotient  $q$  and remainder  $r$

$n \overline{)m} (q$

—

—

$r$

or  $m = nq + r, \forall m, n, q, r \in \mathbb{Z}$  and  $n \neq 0$

If  $13^{99}$  is divided by 81, the remainder is

A. 13

B. 23

C. 39

D. 55

**Answer: d**



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**10.** Consider the binomial expansion of  $R = (1 + 2x)^n = I + f$ , where  $I$  is the integral part of  $R$  and  $f$  is the fractional part of  $R$ ,  $n \in \mathbb{N}$ .

Also, the sum of coefficient of  $R$  is 2187.

The value of  $(n + Rf)$  for  $x = \frac{1}{\sqrt{2}}$  is

A. 7

B. 8

C. 9

D. 10

**Answer: B**



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11. Consider the binomial expansion of  $R = (1 + 2x)^n = I + f$ , where  $I$  is the integral part of  $R$  and  $f$  is the fractional part of  $R$ ,  $n \in \mathbb{N}$ .

Also, the sum of coefficient of  $R$  is 2187.

If  $i$ th term is the greatest term for  $x = 1/3$ , then  $i$  equal

A. 4

B. 5

C. 6

D. 7

**Answer: a**



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12. Consider the binomial expansion of  $R = (1 + 2x)^n = I + f$ , where  $I$  is the integral part of  $R$  and  $f$  is the fractional part of  $R$ ,  $n \in \mathbb{N}$ .

Also, the sum of coefficient of  $R$  is 2187.

If  $k$ th term is having greatest coefficient, the sum of all possible value of  $k$ , is

A. 7

B. 9

C. 11

D. 13

Answer: b



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13.

If

$$(x + a_1)(x + a_2)(x + a_3) \dots (x + a_n) = x^n + S_1 x^{n-1} + S_2 x^{n-2} + \dots + S_n$$

$$\text{where } S_1 = \sum_{i=1}^n a_i, S_2 = \sum_{1 \leq i < j \leq n} a_i a_j, S_3 = \sum_{1 \leq i < j < k \leq n} a_i a_j a_k$$

and so on .

Coefficient of  $x^7$  in the expansion of

$$(1 + x)^2(3 + x)^3(5 + x)^4 \text{ is}$$

A.  $n \cdot 2^n$

B.  $(n + 1) \cdot 2^n$

C.  $n \cdot 2^{n+1}$

D.  $n \cdot 2^n + 1$

**Answer: b**



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**14.**

If

$$(x + a_1)(x + a_2)(x + a_3) \dots (x + a_n) = x^n + S_1x^{n-1} + S_2x^{n-2} + \dots + S_n$$

where

$$S_1 = \sum_{i=1}^n a_i, S_2 = \left( \sum \sum \right)_{1 \leq i < j \leq n} a_i a_j, S_3 = \left( \sum \sum \sum \right)_{1 \leq i < j < k \leq n} a_i a_j a_k$$

and so on .

If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$  the

coefficient of  $x^n$  in the expansion of

$$(x + C_0)(x + C_1)(x + C_2) \dots (x + C_n)$$
 is



A.  $2^{2n-1} - \frac{1}{2} {}^{2n}C_{n-1}$

B.  $2^{2n-1} - \frac{1}{2} {}^{2n}C_n$

C.  $2^{2n-1} - \frac{1}{2} {}^{2n+1}C_n$

D.  $2^{2n-1} - \frac{1}{2} {}^{2n+1}C_{n-1}$

**Answer: b**



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**15.**

If

$$(x + a_1)(x + a_2)(x + a_3) \dots (x + a_n) = x^n + S_1 x^{n-1} + S_2 x^{n-2} + \dots + S_n$$

where

$$S_1 = \sum_{i=1}^n a_i, S_2 = \left( \sum \sum \right)_{1 \leq i < j \leq n} a_i a_j, S_3 = \left( \sum \sum \sum \right)_{1 \leq i < j < k \leq n} a_i a_j a_k$$

and so on .

Coefficient of  $x^7$  in the expansion of

$$(1 + x)^2 (3 + x)^3 (5 + x)^4 \text{ is}$$

A. 112

B. 224

C. 342

D. 416

**Answer: d**



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16.  $A = \left(\frac{5}{2} + \frac{x}{2}\right)^n$ ,  $B = (1 + 3x)^m$

Sum of coefficients of expansion of B is 6561 . The difference of the coefficient of third to the second term in the expansion of A is equal to 117 .

The value of m is

A. 4

B. 5

C. 6

D. 7

**Answer: c**



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17. Sum of coefficients of expansion of B is 6561 . The difference of the coefficient of third to the second term in the expansion of A is equal to 117 .

If  $n^m$  is divided by 7 , the remainder is

A. 1

B. 2

C. 3

D. 5

**Answer: a**



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18. Sum of coefficients of expansion of B is 6561 . The difference of the coefficient of third to the second term in the expansion of A is equal to 117 .

The ratio of the coefficient of second term from the beginning and the end in the expansion of B , is

- A. 125
- B. 625
- C. 3125
- D. 15625

**Answer: d**



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19. Let us consider the binomial expansion  $(1 + x)^n = \sum_{r=0}^n a_r x^r$

where  $a_4, a_5$  and  $a_6$  are in AP , (  $n < 10$  ). Consider another

binomial expansion of  $A = \sqrt[3]{2} + (\sqrt[4]{3})^{13n}$  , the expansion of A

contains some rational terms  $T_{a_1}, T_{a_2}, T_{a_3}, \dots, T_{a_m}$

$$(a_1 < a_2 < a_3 < \dots < a_m)$$

The value of  $\sum_{i=1}^n a_i$  is

A. 63

B. 127

C. 255

D. 511

**Answer: b**



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20. Let us consider the binomial expansion  $(1 + x)^n = \sum_{r=0}^n a_r x^r$

where  $a_4, a_5$  and  $a_6$  are in AP, ( $n < 10$ ). Consider another

binomial expansion of  $A = \sqrt[3]{2} + (\sqrt[4]{3})^{13n}$ , the expansion of A

contains some rational terms  $T_{a_1}, T_{a_2}, T_{a_3}, \dots, T_{a_m}$

$$(a_1 < a_2 < a_3 < \dots < a_m)$$

The value of  $a_m$  is

A. 87

B. 88

C. 89

D. 90

**Answer: c**



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21. Let us consider the binomial expansion  $(1 + x)^n = \sum_{r=0}^n a_r x^r$

where  $a_4, a_5$  and  $a_6$  are in AP, ( $n < 10$ ). Consider another

binomial expansion of  $A = \sqrt[3]{2} + (\sqrt[4]{3})^{13n}$ , the expansion of A

contains some rational terms  $T_{a_1}, T_{a_2}, T_{a_3}, \dots, T_{a_m}$

$$(a_1 < a_2 < a_3 < \dots < a_m)$$

The common difference of the arithmetic progression

$a_1, a_2, a_3, \dots, a_m$  is

A. 6

B. 8

C. 10

D. 12

**Answer: d**

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## Exercise Single Integer Answer Type Questions

1. If  $(1 + x + x^2 + x^3)^n = \sum_{r=0}^{3n} b_r x^r$  and  $\sum_{r=0}^{3n} b_r = k$ , then  $\sum_{r=0}^{3n} r b_r$  is

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2. The number of rational terms in the expansion of

$$\left( \sqrt[3]{4} + \frac{1}{\sqrt[4]{6}} \right)^{20} \text{ is}$$



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3. If  $2^{2006} + 2006$  is divided by 7, the remainder is



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4. The last two digits of the number  $19^{94}$  is



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5. If 
$$\frac{{}^nC_r + 4 \cdot {}^nC_{r+1} + 6 \cdot {}^nC_{r+2} + 4 \cdot {}^nC_{r+3} + {}^nC_{r+4}}{[{}^nC_r + 3 \cdot {}^nC_{r+1} + 3 \cdot {}^nC_{r+2} + {}^nC_{r+3}]} = \frac{n + \lambda}{r + \lambda}$$

the value of  $\lambda$  is



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6. The value of  $99^{50} - 99 \cdot 98^{50} + \frac{99 \cdot 98}{1 \cdot 2} (97)^{50} - \dots + 99$  is



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7. If the greatest term in the expansion of  $(1+x)^2 n$  has the greatest coefficient if and only if  $x \in \left(\frac{10}{11}, \frac{11}{10}\right)$  and the fourth term in the expansion of  $\left(kx + \frac{1}{x}\right)^m$  is  $\frac{n}{4}$  then find the value of  $mk$ .

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8. If the value of

$$(n+2) \cdot {}^n C_0 \cdot 2^{n+1} - (n+1) \cdot {}^n C_1 \cdot 2^n + n \cdot {}^n C_2 \cdot 2^{n-1} - \dots$$

is equal to  $k(n+1)$ , the value of  $k$  is .

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9. If  $(1+x+x^2+\dots+x^9)^4 (x+x^2+x^3+\dots+x^9)$

$$= \sum_{r=1}^{45} a_r x^r \text{ and the value of } a_2 + a_6 + a_{10} + \dots + a_{42} \text{ is } \lambda$$

the sum of all digits of  $\lambda$  is .

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## Exercise Statement I And II Type Questions

1. Statement-1 Greatest coefficient in the expansion of

$$(1 + 3x)^6 \text{ is } {}^6C_3 \cdot 3^3.$$

Statement-2 Greatest coefficient in the expansion of

$$(1 + x)^{2n} \text{ is the middle term.}$$

- A. Statement I is True, Statement II is True, Statement II is a correct explanation for statement I
- B. Statement I is True, Statement II is True, Statement II is NOT a correct explanation for Statement I
- C. Statement I is True, Statement II is False
- D. Statement I is False, Statement II is True.

**Answer: d**



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2. Statement-1 The term independent of  $x$  in the

expansion of  $\left(x^2 + \frac{1}{x^2} + 2\right)^{25}$  is  ${}^{50}C_{25}$ .

Statement-2 In a binomial expansion middle term is independent of  $x$ .



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3. Statement-I : In the expansion of  $(1+x)^n$  if coefficient of  $31^{st}$  and  $32^{nd}$  terms are equal then  $n = 61$  Statement -II : Middle term in the expansion of  $(1+x)^n$  has greatest coefficient.



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4. Statement-1 The number of terms in the expansion of

$\left(x + \frac{1}{x} + 1\right)^n$  is  $(2n + 1)$

Statement-2 The number of terms in the expansion of

$(x_1 + x_2 + x_3 + \dots + x_m)^n$  is  ${}^{n+m-1}C_{m-1}$ .



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5. Statement-1  $4^{101}$  when divided by 101 leaves the remainder 4.

Statement-2  $(n^p - n)$  when divided by 'p' leaves

remainder zero when  $n \geq 2, n \in \mathbb{N}$  is a prime number .

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6. Statement-1:  $11^{25} + 12^{25}$  when divided by 23 leaves the remainder

zero. Statement-2:  $(a + b)^n$  is divisible by  $(a + b)$  for all values of  $n \in \mathbb{N}$

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7. Statement-1 The maximum value of the term

independent of  $x$  in the expansion of  $(ax^{1/6} + bx^{1/3})^9$  is 84

Statement-2  $2a^2 + b = 2$

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## Exercise Subjective Type Questions

1. If the third term in the expansion of  $\left(\frac{1}{x} + {}_x(\log)_{10x}\right)^5$  is 1000, then find  $x$ .

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2. Find the value of

$$\frac{18^3 + 7^3 + 3 \cdot 18 \cdot 7 \cdot 25}{(3^6 + 6 \cdot 243 \cdot 4 + 15 \cdot 81 \cdot 4 + 20 \cdot 27 \cdot 8 + 15 \cdot 9 \cdot 16 \cdot 3 \cdot 32 + 64)}$$

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3. Determine the term independent of  $a$  in the expansion of

$$\left(\frac{a+1}{a^{\frac{2}{3}} - a^{\frac{1}{3}} + 1} - \frac{a-1}{a - a^{\frac{1}{2}}}\right)^{10}.$$

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4. If in the expansion of  $(1+x)^n$ ,  $a, b, c$  are three consecutive coefficients, then  $n =$   $\frac{ac+ab+bc}{b^2+ac}$  b.  $\frac{2ac+ab+bc}{b^2-ac}$  c.  $\frac{ab+ac}{b^2-ac}$  d. none of these

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5. Find  $n$  in the binomial  $\left[ \sqrt[3]{2} + \frac{1}{\sqrt[3]{3}} \right]^n$ , if the ratio of 7th term from beginning to 7th term from the end is  $1/6$ .

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6. if  $S_n = C_0C_1 + C_1C_2 + \dots + C_{n-1}C_n$  and  $\frac{S_{n+1}}{S_n} = \frac{15}{4}$  then  $n$  is

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7.  $\frac{C_1}{C_0} + 2\frac{C_2}{C_1} + 3\frac{C_3}{C_2} + \dots + n\frac{C_n}{C_{n-1}} = \frac{n(n+1)}{2}$

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8. Find the term in  $\left(\frac{a}{\sqrt{b}}3 + \sqrt{\frac{b}{a3}}\right)^{21}$  which has the same power of  $a$  and  $b$ .



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9. The coefficient of  $x^r$  [ $0 \leq r \leq (n-1)$ ] in the expansion of  $(x+3)^{n-1} + (x+3)^{n-2}(x+2) + (x+3)^{n-3}(x+2)^2 + \dots + (x+2)^{n-1}$  is  $\binom{n}{r}3^r - 2^n$  b.  $\binom{n}{r}(3^{n-r} - 2^{n-r})$  c.  $\binom{n}{r}(3^r + 2^{n-r})$  d. none of these



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10. Prove that if  $p$  is a prime number greater than 2, then the difference  $\left[(2 + \sqrt{5})^p\right] - 2^{p+1}$  is divisible by  $p$ , where  $[.]$  denotes greatest integer.



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11. Integer just greater than  $(\sqrt{3} + 1)^{2n}$  is necessarily divisible by (A)  $n + 2$  (B)  $2^{n+3}$  (C)  $2^n$  (D)  $2^{n+1}$

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12. Solve the equation

$${}^{11}C_1x^{10} - {}^{11}C_3x^8 + {}^{11}C_5x^6 - {}^{11}C_7x^4 + {}^{11}C_9x^2 - {}^{11}C_{11} = 0$$

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13. If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , find the value of

$$\sum_{0 \leq i < j \leq n} (i + j)(C_i + C_iC_j).$$

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14. Evaluate  $\sum_{0 \leq i \ln e j \leq 10} {}^{21}C_i \cdot {}^{21}C_j$ .

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15. Find the coefficient of  $x^4$  in the expansion of  $(1 + x + x^2 + x^3)^{11}$ .



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16. Find the coefficients of  $x^4$  in the expansions of

$$(2 - x + 3x^2)^6.$$



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17. If for  $z$  as real or complex,

$$(1 + z^2 + z^4)^8 = C_0 + C_1z^2 + C_2z^4 + \dots + C_{16}z^{32} \text{ then}$$

$$C_0 - C_1 + C_2 - C_3 + \dots + C_{16} = 1$$

$$C_0 + C_3 + C_6 + C_9 + C_{12} + C_{15} = 3^7$$

$$C_2 + C_5 + C_8 + C_{11} + C_{14} = 3^6$$

$$C_1 + C_4 + C_7 + C_{10} + C_{13} + C_{16} = 3^7$$



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18. If for  $z$  as real or complex .

$$(1 + z^2 + z^4)^8 = C_0 C_1 z^2 C_2 z^4 + \dots + C_{16} z^{32},$$

prove that

$$C_0 + C_3 + C_6 + C_9 + C_{12} + C_{15}$$

$$+ (C_2 + C_5 + C_8 + C_{11} + C_{14})$$

$$+ (C_1 + C_4 + C_7 + C_{10} + C_{16})\omega^2 = 0,$$

where  $\omega$  is a cube root of unity .



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19. Let  $f(x) = a_0 + a_1x + a_2x^2 + \dots + a_{2n}x^{2n}$  and

$$g(x) = b_0 + b_1x + b_2x^2 + \dots + b_{n-1}x^{x-1} + x^n + x^{n+1} + \dots + x^{2n}.$$

If  $f(x) = g(x + 1)$ , find  $a_n$  in terms of  $n$ .



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20. If  $a_0, a_1, a_2, \dots$  be the coefficients in the expansion of  $(1 + x + x^2)^n$  in ascending powers of  $x$ . prove that :  $(i) a_0 a_1 - a_1 a_2 + a_2 a_3 - \dots = 0$

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21. If  $a_0, a_1, a_2, \dots$  are the coefficients in the expansion of  $(1 + x + x^2)^n$  in ascending powers of  $x$ , prove that

$$a_0 a_2 - a_1 a_3 + a_2 a_4 - \dots + a_{2n-2} a_{2n} = a_{n+1}.$$

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22. If  $a_0, a_1, a(2), \dots$  are the coefficients in the expansion of  $(1 + x + x^2)^n$  in ascending powers of  $x$ , prove that

if  $E_1 = a_0 + a_3 + a_6 + \dots$ ,  $E_2 = a_1 + a_4 + a_7 + \dots$  and

$E_3 = a_2 + a_5 + a_8 + \dots$  then  $E_1 = E_2 = E_3 = 3^{n-1}$

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1. The value of

$${}^{300}C_{3010} - {}^{301}C_{3011} + {}^{302}C_{3012} + \dots + {}^{3020}C_{3030} =$$

${}^{60}C_{20}$  b.  ${}^{30}C_{10}$  c.  ${}^{60}C_{30}$  d.  ${}^{40}C_{30}$

A.  ${}^{60}C_{20}$

B.  ${}^{30}C_{10}$

C.  ${}^{60}C_{30}$

D.  ${}^{40}C_{30}$

Answer: B

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2. If the coefficient of  $p$ th,  $(p + 1)$ th and  $(p + 2)$ th terms in the expansion of  $(1 + x)^n$  are in A.P

A.  $n^2 - 2np + 4p^2 = 0$

B.  $n^2 - n(4p + 1) + 4p^2 - 2 = 0$

C.  $n^2 - n(4p + 1) + 4p^2 = 0$

D. None of the above

**Answer: B**



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3. If the coefficient of  $x^7$  in  $\left(ax^2 + \frac{1}{bx}\right)^{11}$  is equal to the coefficient of  $x^7$  in  $\left(ax - \frac{1}{bx^2}\right)^{11}$  then

A. 1

B.  $1/2$

C. 2

D. 3

**Answer: A**



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4. For natural numbers  $m, n$ , if  $(1 - y)^m(1 + y)^n = 1 + a_1y + a_2y^2 + \dots$ , and  $a_1 = a_2 = 10$ , then

`m n c. m+n=80d. m-n=20`

A. (20,45)

B. (35,20)

C. (45,35)

D. (35,45)

**Answer: D**



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5. In the binomial expansion of  $(a - b)^n$ ,  $n \geq 5$ , the sum of the  $5^{th}$  and  $6^{th}$  terms is zero. Then,  $a/b$  equals

A.  $\frac{5}{n - 4}$

B.  $\frac{6}{n-5}$

C.  $\frac{n-5}{6}$

D.  $\frac{n-4}{5}$

**Answer: D**



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6. The sum of the series

$${}^{20}C_0 - {}^{20}C_1 + {}^{20}C_2 - {}^{20}C_3 + \dots - \dots + {}^{20}C_{10} \quad \text{is:} \quad (1)$$

$$- {}^{20}C_{10} \quad (2) \quad \frac{1}{2} {}^{20}C_{10} \quad (3) \quad 0 \quad (4) \quad {}^{20}C_{10}$$

A.  $- {}^{20}C_{10}$

B.  $\frac{1}{2} {}^{20}C_{10}$

C. 0

D.  ${}^{20}C_{10}$

**Answer: B**



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7. Statement-1:  $\sum_{r=0}^n (r+1)^n C_r = (n+2)2^{n-1}$

Statement -2:  $\sum_{r=0}^n (r+1)^n C_r x^r = (1+x)^n + nx(1+x)^{n-1}$

A. Statement-1 is true ,Statement-2 is true, Statement-2 is a correct

explanation for Statement-1

B. Statement-1 is true ,Statement-2 is true, Statement-2 is not a correct

explanation for Statement-1

C. Statement-1 is true ,Statement-2 is false

D. Statement-1 is true ,Statement-2 is true

**Answer: A**



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8. The remainder left out when  $8^{2n}(62)^{2n+1}$  is divided by 9 is (1) 0 (2) 2 (3) 7 (4) 8

A. 8

B. 0

C. 2

D. 7

**Answer: C**



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9. For  $r = 0, 1, \dots, 10$ , let  $A_r, B_r,$  and  $C_r$  denote, respectively, the coefficient of  $x^r$  in the expansions of  $(1+x)^{10}, (1+x)^{20}$  and  $(1+x)^{30}$

.Then  $\sum_{r=1}^{10} A_r(B_{10}B_r - C_{10}A_r)$  is equal to

A.  $B_{10} - C_{10}$

B.  $A_{10}(B_{10} - C_{10}A_{10})$

C. 0

D.  $C_{10} - B_{10}$

**Answer: D**



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10. So, statement-1 is also true. Statement-2 is a correct explanation for statement-1.

$$S_1 = \sum_{j=1}^{10} j(j-1)^{10} C_j, S_2 = \sum_{j=1}^{10} j \cdot {}^{10}C_j \text{ and } S_2 = \sum_{j=1}^{10} j \cdot {}^{10}C_j.$$

Statement-1  $S_3 = 50 \times 2^9$ .

Statement-2  $S_1 = 90 \times 2^8$  and  $S_2 = 10 \times 2^8$

A. Statement-1 is true, Statement-2 is true, Statement-2 is a correct explanation for Statement-1

B. Statement-1 is true, Statement-2 is true, Statement-2 is not a correct explanation for Statement-1

C. Statement-1 is true, Statement-2 is false

D. Statement-1 is true ,Statement-2 is ture

**Answer: B**



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11. The coefficient of  $x^7$  in the expansion of  $(1 - x - x^2 + x^3)^6$  is :

A.  $-132$

B.  $-144$

C.  $132$

D.  $144$

**Answer: B**



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12. If  $n$  is a positive integer, then  $(\sqrt{3} + 1)^{2n} - (\sqrt{3} - 1)^{2n}$  is (1) an irrational number (2) an odd positive integer (3) an even positive integer (4) a rational number other than positive integers

- A. an odd positive integer
- B. an even positive integer
- C. a rational number other than positive integer
- D. an irrational number

**Answer: D**



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13. In the expansion of  $\left( \frac{x + 1}{x^{\frac{2}{3}} - x^{\frac{1}{3}} + 1} - \frac{x - 1}{x - x^{\frac{1}{2}}} \right)^{10}$  the term which does not contain  $x$

A. 120

B. 210

C. 310

D. 4

**Answer: B**



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14. The coefficients of three consecutive terms of  $(1 + x)^{n+5}$  are in the ratio 5:10:14. Then  $n =$  \_\_\_\_\_.



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15. If the coefficients of  $x^3$  and  $x^4$  in the expansion of  $(1 + ax + bx^2)(1 - 2x)^{18}$ , in powers of  $x$  both zero, then  $(a,b)$  is equal to

A.  $\left(14, \frac{272}{3}\right)$

B.  $\left(16, \frac{272}{3}\right)$

C.  $\left(14, \frac{251}{3}\right)$

D.  $\left(16, \frac{251}{3}\right)$

**Answer: B**



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16. Coefficient of  $x^{11}$  in the expansion of  $(1 + x^2)(1 + x^3)^7(1 + x^4)^{12}$  is

1051 b. 1106 c. 1113 d. 1120

A. 1051

B. 1106

C. 1113

D. 1120

**Answer: C**



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17. The sum of coefficients in integral powers of  $x$  in the binomial expansion  $(1 - 2\sqrt{x})^{50}$  is

A.  $\frac{1}{2}(2^{50} + 1)$

B.  $\frac{1}{2}(2^{50} - 1)$

C.  $\frac{1}{2}(3^{50})$

D.  $\frac{1}{2}(3^{50} - 1)$

**Answer: B**



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18. The coefficient of  $x^9$  in the expansion of  $(1 + x)(16x^2)(1 + x^3)(1 + x^{100})$  is



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19. If the number of terms in the expansion of  $\left(1 - \frac{2}{x} + \frac{4}{x^2}\right)^n$ ,  $x \neq 0$ , is 28, then the sum of the coefficients of all the terms in this expansion, is : (1) 64 (2) 2187 (3) 243 (4) 729

- A. 243
- B. 729
- C. 64
- D. 2187

**Answer: B**

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20. Let  $m$  be the smallest positive integer such that the coefficient of  $x^2$  in the expansion of  $(1+x)^2 + (1+x)^3 + (1+x)^4 + \dots + (1+x)^{49} + (1+mx)^{50}$  is  $(3n+1) \cdot {}^{51}C_3$  for some positive integer  $n$ . Then the value of  $n$  is

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21. The value of  $({}^{21}C_1 - {}^{10}C_1) + ({}^{21}C_2 - {}^{10}C_2) + ({}^{21}C_3 - {}^{10}C_3) + ({}^{21}C_4 - {}^{10}C_4)$  is

A.  $2^{20} - 2^{10}$

B.  $2^{21} - 2^{11}$

C.  $2^{21} - 2^{10}$

D.  $2^{20} - 2^9$

**Answer: A**



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