



MATHS

BOOKS - ARIHANT MATHS (HINGLISH)

PROPERTIES AND SOLUTION OF TRIANGLES

Examples

1. Find the angles of the triangle whose sides are $3 + \sqrt{3}$, $2\sqrt{3}$ and $\sqrt{6}$.

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2. The sides of a triangle are 8 cm, 10 cm and 12 cm. Prove that the greatest angle is double of the smallest angle.

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3. With usual notations, if in a ΔABC , $\frac{b+c}{11} = \frac{c+a}{12} = \frac{a+b}{13}$, then prove that $\frac{\cos A}{7} = \frac{\cos B}{19} = \frac{\cos C}{25}$.

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4. The sides of a triangle are three consecutive natural numbers and its largest angle is twice the smallest one. Determine the sides of the triangle.

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5. In the triangle ABC , lines OA , OB and OC are drawn so that angles OAB , OBC and OCA are each equal to ω , prove that $\cot \omega = \cot A + \cot B + \cot C$

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6. Solve

$b \cos^2 \frac{C}{2} + c \cos^2 \frac{B}{2}$ in terms of k , where k is perimeter of the $\triangle ABC$.

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7. In a $\triangle ABC$, $c \cos^2 \frac{A}{2} + a \cos^2 \frac{C}{2} = \frac{3b}{2}$, then a, b, c are in

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8. In a $\triangle ABC$, $a = 2b$ and $|A - B| = \frac{\pi}{3}$. Determine the $\angle C$.

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9. In a $\triangle ABC$, the tangent of half the difference of two angle is one-third the tangent of half the sum of the angle. Determine the ratio of the sides opposite to the angles.

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10. If the angles of a triangle are 30° and 45° , and the included side is $(\sqrt{3} + 1)$ cm, then prove that the area of the triangle is $\frac{1}{2}(\sqrt{3} + 1)$.

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11. Consider the following statements concerning a ΔABC

(i) The sides a, b, c and area of triangle are rational.

(ii) $a, \tan \frac{B}{2}, \tan \frac{C}{2}$

(iii) $a, \sin A \sin B, \sin C$ are rational .

Prove that $(i) \Rightarrow (ii) \Rightarrow (iii) \Rightarrow (i)$

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12. Show that $\frac{b - c}{r_1} + \frac{c - a}{r_2} + \frac{a - b}{r_3} = 0$.

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13. If in a triangle $r_1 = r_2 + r_3 + r$, prove that the triangle is right angled.

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14. In any ΔABC , prove the following : $r_1 = r \cot\left(\frac{B}{2}\right) \cot\left(\frac{C}{2}\right)$

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15. In a right angles triangle, prove that $r + 2R = s$.

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16. The exradii r_1, r_2 and r_3 of ABC are in H.P. Show that its sides a, b and c are in AP .

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17. If A, B, C are the angles of a triangle then prove that

$$\cos A + \cos B - \cos C = -1 + 4 \cos\left(\frac{A}{2}\right) \cos\left(\frac{B}{2}\right) \sin\left(\frac{C}{2}\right)$$

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18. Find the ratio of the circum-radius and the inradius of $\triangle ABC$, whose sides are in the ratio 4:5:6.

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19. Find the ratio of $IA:IB:IC$, where I is the incentre of $\triangle ABC$.

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20. If the sides of a triangle are in GP and the largest angle is twice the smallest angle, then find the relation for r .

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21. The equation $ax^2 + bx + c = 0$, where a, b, c are the side of a $\triangle ABC$, and the equation $x^2 + \sqrt{2}x + 1 = 0$ have a common root. Find measure for $\angle C$.



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22. In triangle ABC , if $\cot A, \cot B, \cot C$ are in AP ; then a^2, b^2, c^2 are in _____ progression.



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23. Find the Side of pedal triangle and Circum-Radius of pedal Triangle ?



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24. Find the area, circum-radius and in-radius of the pedal triangle.



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25. In a triangle ABC I_1, I_2, I_3 are excentre of triangle then show that

$$II_1 \cdot II_2 \cdot II_3 = 16R^2r.$$

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26. Prove that

$$\frac{l_1 \cdot l_2 l_3}{\sin A} = \frac{l_2 \cdot l_3 l_1}{\sin B}$$

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27. If g, h, k denotes the side of a pedal triangle, then prove that

$$\frac{g}{a^2} + \frac{h}{b^2} + \frac{k}{c^2} = \frac{a^2 + b^2 + c^2}{2abc}$$

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28. If x, y, z are respectively perpendiculars from the circumcentre on the sides of the ΔABC , the value of $\frac{a}{x} + \frac{b}{y} + \frac{c}{z} - \frac{abc}{4xyz} =$

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29. If O, H and G represents circum centre, orthocentre and centroid respectively, then show

$HG : GO = 2 : 1$. We have,

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30. In ΔABC it is given distance between the circumcentre (O) and orthocentre (H) is $R\sqrt{1 - 8 \cos A \cos B \cos C}$. If Q is the midpoint of OH , then AQ is

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31. Find the distance between the circumcentre and the incentre of the ΔABC .

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32. Let $A_0A_1A_2A_3A_4A_5$ be a regular hexagon inscribed in a circle of unit radius. Then the product of the lengths the line segments A_0A_1 , A_0A_2 and A_0A_4 is

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33. If the area of circle is A_1 and area of regular pentagon inscribed in the circle is A_2 , then find the ratio of area of two.

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34. The area of a cyclic quadrilateral ABCD is $\frac{3\sqrt{3}}{4}$. The radius of the circle circumscribing cyclic quadrilateral is 1. If $AB = 1$ and $BD = \sqrt{3}$, then $BC \cdot CD$ is equal to

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35. A regular pentagon and a regular decagon have the same perimeter, prove that their areas are as $2 : \sqrt{5}$.

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36. If the sides of a cyclic quadrilateral are 3, 3, 4, 4 show that a circle can be inscribed in it.

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37. The two adjacent sides of a cyclic quadrilateral are 2 and 5 and the angle between them is 60° . If the area of the quadrilateral is $4\sqrt{3}$, find the remaining two sides.



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38. If a, b, c, d are the sides of a quadrilateral, then find the minimum value of $\frac{a^2 + b^2 + c^2}{d^2}$



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39. In any triangle ABC, the sides are 6 cm, 10 cm and 14 cm. Then the triangle is obtuse angled with the obtuse angle equal to

A. 120°

B. 135°

C. 110°

D. 150°

Answer: A

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40. If a, b and A are given in a triangle and c_1, c_2 are possible values of the third side, then prove that $c_1^2 + c_2^2 - 2c_1c_2 \cos 2A = 4a^2 \cos^2 A$

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41. In a $\triangle ABC$, the median to the side BC is of length $\frac{1}{\sqrt{11 - 6\sqrt{3}}}$ and it divides the $\angle A$ into angles 30° and 45° . Find the length of the side BC .

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42. Two flagstaffs stand on a horizontal plane. A and B are two points on the line joining their feet and between them. The angle of elevation of the tops of the flagstaffs as seen from A are 30° and 60° and as seen from B are 60° and 45° . If AB is 30 m, the distance between the flagstaffs in metre is

A. $30 + 15\sqrt{3}$

B. $45 + 15\sqrt{3}$

C. $60 - 15\sqrt{3}$

D. $60 + 15\sqrt{3}$

Answer: A:C



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43. In a cubical hall $ABCDPQRS$ with each side $10m$, G is the centre of the walls $BCRQ$ and T is the midpoint of the side AB , the angle of elevation of G at the Point T is

A. $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$

B. $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$

C. $\tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$

D. $\cot^{-1}\left(\frac{1}{\sqrt{3}}\right)$

Answer: A:C

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44. Each side of an equilateral triangle subtends an angle of 60° at the top of a tower h m high located at the centre of the triangle. If a is the length of each side of the triangle, then

A. $3a^2 = 2h^2$

B. $2a^2 = 2h^2$

C. $a^2 = 3h^2$

D. $3a^2 = h^2$

Answer: A::B::C



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45. A vertical tower PQ subtends the same angle 30° at each of two places A and B, 60 m apart on the ground, AB subtends an angle 120° at the foot of the tower. If h is the height of the tower, then $9h^2 + h + 1$ is equal to

A. 3121

B. 2136

C. 3600

D. None of these

Answer: A::C



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46. if $\tan^2 \frac{\pi - A}{4} + \tan^2 \frac{\pi - B}{4} + \tan^2 \frac{\pi - C}{4} = 1$, then ΔABC is

- A. equilateral
- B. isosceles
- C. scalene
- D. None of these

Answer: A::B::C



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47. In ΔABC , $a^2 + c^2 = 2002b^2$ then $\frac{\cot A + \cot C}{\cot B}$ is equal to

- A. $\frac{1}{2001}$
- B. $\frac{2}{2001}$
- C. $\frac{3}{2001}$
- D. $\frac{4}{2001}$

Answer: B



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48. A triangle has vertices A, B and C, and the respective opposite sides have lengths a, b and c. This triangle is inscribed in a circle of radius R. If $b = c = 1$ and the altitude from A to side BC has length $\sqrt{\frac{2}{3}}$, then R equals:

A. $\frac{1}{\sqrt{3}}$

B. $\frac{2}{\sqrt{3}}$

C. $\frac{\sqrt{3}}{2}$

D. $\frac{\sqrt{3}}{2\sqrt{2}}$

Answer: B::C



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49. In $\triangle ABC$, if $AC = 8$, $BC = 7$ and D lies between A and B such that $AD = 2$, $BD = 4$, then the length CD equals

A. $\sqrt{46}$

B. $\sqrt{48}$

C. $\sqrt{51}$

D. $\sqrt{75}$

Answer: A



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50. In a triangle ABC , if

$$(a + b + c)(a + b - c)(b + c - a)(c + a - b) = \frac{8a^2b^2c^2}{a^2 + b^2 + c^2}$$
 then the

triangle is

A. isosceles

B. right angled

C. equilateral

D. obtuse angled

Answer: A::B::C::D



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51. Consider a $\triangle ABC$ and let a , b and c denote the lengths of the sides opposite to vertices A , B and C , respectively.

if $a = 1$, $b = 3$ and $C = 60^\circ$, then $\sin^2 B$ is equal to

A. $\frac{27}{28}$

B. $\frac{3}{28}$

C. $\frac{81}{28}$

D. $\frac{1}{3}$

Answer: B



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52. In $\triangle ABC$, if $\cos A + \sin A - \frac{2}{\cos B + \sin B} = 0$, then $\frac{a+b}{c}$ is equal to

A. $\sqrt{2}$

B. 1

C. $\frac{1}{\sqrt{2}}$

D. $2\sqrt{2}$

Answer: A::B::C



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53. In a triangle ABC , if $\angle A = 30^\circ$, $b = 10$ and $a = x$, then the values of x for which there are 2 possible triangles is given by (All symbols used have usual meaning in a triangle.)

A. $5 < x < 10$

B. $x < \frac{5}{2}$

C. $\frac{5}{3} < x < 10$

D. $\frac{5}{2} < x < 10$

Answer: A::B



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54. In a $\triangle ABC$, $AB = AC$, P and Q are points on AC and AB respectively such that $CB = BP = PQ = QA$. if $\angle AQP = \theta$, then $\tan^2 \theta$ is a root of the equation

A. $y^3 + 21y^2 - 35y - 12 = 0$

B. $y^3 - 21y^2 + 35y - 12 = 0$

C. $y^3 - 21y^2 + 35y - 7 = 0$

D. $12y^3 - 35y^2 + 35y - 12 = 0$

Answer: A::B::C



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55. The angle of elevation of the top of a tower a point A due south of it is 30° and from a point B due west of it is 45° . If the height of the tower is 100 meters, then find the distance AB.

- A. 150 m
- B. 200 m
- C. 173.2 m
- D. 141.4 m

Answer: A:B



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56. An aeroplane flying horizontally, 1km above the ground, is observed at an elevation of 60° , after 10 seconds, its elevation is observed to be 30° . Find the speed of the aeroplane in km/hr.

A. 240

B. $240\sqrt{3}$

C. $60\sqrt{3}$

D. None of these

Answer: A::B::C::D



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57. In $\triangle ABC$, the ratio $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ is not always equal to

(All symbols used have usual meaning in a triangle.)

A. $2R$, where R is the circumradius

B. $\frac{abc}{2\Delta}$, where Δ is the area of the triangle

C. $\frac{2}{3}(a^2 + b^2 + c^2)^{\frac{1}{2}}$

D. $\frac{(abc)^{\frac{2}{3}}}{(h_1 h_2 h_3)^{\frac{1}{3}}}$

Answer: A::B::C::D



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58. Let ABCD be a cyclic quadrilateral such that $AB = 2$, $BC = 3$, $\angle B = 120^\circ$ and area of quadrilateral $= 4\sqrt{3}$. Which of the following is/are correct ?

- A. The value of $(AC)^2$ is equal to 19
- B. The sum of all positive value of product AC. BD I is equal to 35
- C. The sum of all possible value of $(fAD)^2$ is equal to 29
- D. The value of $(CD)^2$ can be 4

Answer: B



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59. In a triangle ABC, which of the following quantities denote the area of the triangles $\frac{a^2 - b^2}{2} \frac{\sin A \sin B}{\sin(A - B)}$

$$A. \frac{a^2 - b^2}{2} \left(\frac{\sin A \sin B}{\sin(A - B)} \right)$$

$$B. \frac{r_1 r_2 r_3}{\sqrt{\sum r_1 r_2}}$$

$$C. \frac{a^2 + b^2 + c^2}{\cot A + \cot B + \cot C}$$

$$D. r^2 \cot \frac{A}{2} \cdot \cot \frac{B}{2} \cdot \cot \frac{C}{2}$$

Answer: A::B::C::D

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60. Consider the system of equations

$$\sin x \cos 2y = (a^2 - 1)^2 + 1, \cos x \sin 2y = a + 1$$

The number of values of $y \in [0, 2\pi]$, when the system has solution for permissible values of a , are

$$A. \left(\frac{-\pi}{2}, \frac{-\pi}{2} \right)$$

$$B. \left(\frac{\pi}{2}, \frac{3\pi}{2} \right)$$

$$C. \left(\frac{3\pi}{2}, \frac{-\pi}{2} \right)$$

$$D. \left(\frac{-\pi}{2}, \frac{3\pi}{2} \right)$$

Answer: A::B::C::D



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61. In a triangle ABC, let $2a^2 + 4b^2 + c^2 = 2a(2b + c)$, then which of the following holds good?

A. $\cos B = \frac{-7}{8}$

B. $\sin(A - C) = 0$

C. $\frac{r}{r_1} = \frac{1}{5}$

D. $\sin A : \sin B : \sin C = 1 : 2 : 1$

Answer: A::B::C



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62. In AABC, angle A, B and C are in the ratio 1:2:3, then which of the following is (are) correct? (All symbol used have usual meaning in a

triangle.) (A) Circumradius of $\triangle ABC = c$ (B) $a : b : c = 1 : \sqrt{3} : 2$ (C) Perimeter of $\triangle ABC = 3 + \sqrt{3}$ (D) Area of triangle $ABC = \frac{\sqrt{3}}{8}c^2$

A. Circum-radius of $\triangle ABC = c$

B. $a : b : c = 1 : \sqrt{3} : 2$

C. Perimeter of $\triangle ABC = 3 + \sqrt{3}$

D. Area of $\triangle ABC = \frac{\sqrt{3}}{8}c^2$

Answer: A::B::C



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63. If the length of tangents from A, B, C to the incircle of $\triangle ABC$ are 4, 6, 8 then which of the following is(are) correct? (All symbols used have usual meaning in a triangle.)

A. Area of $\triangle ABC$ is $12\sqrt{6}$

B. r_1, r_2, r_3 are in HP

C. a, b, c are in AP

$$D. r = \frac{4\sqrt{6}}{3}$$

Answer: B



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64. In triangle ABC, let $b = 10$, $c = 10\sqrt{2}$ and $R = 5\sqrt{2}$ then which of the following are correct

A. Area of triangle ABC is 50.

B. Distance between orthocentre and circumcentre is $5\sqrt{2}$.

C. Sum of circum-radius and in-radius of ΔABC is equal to 10.

D. Length of internal angle bisector of $\angle ABC$ of ΔABC is $\frac{5}{2\sqrt{2}}$.

Answer: A::B::C



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65. Let 'l' is the length of median from the vertex A to the side BC of a ΔABC . Then

A. $4l^2 = 2b^2 + 2c^2 - a^2$

B. $4l^2 = b^2 + c^2 + 2bc \cos A$

C. $4l^2 = a^2 + 4bc \cos A$

D. $4l^2 = (2s - a)^2 - 4bc \sin^2 \frac{A}{2}$

Answer: A::B::C::D



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66. If a right angled ΔABC of maximum area is inscribed within a circle of radius R, then (Δ represents area of ΔABC and r, r_1, r_2, r_3 represent in-radius and ex-radii, and s is the semi-perimeter of ΔABC , then

A. $\Delta = R^2$

$$\text{B. } \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3} = \frac{\sqrt{2} + 1}{R}$$

$$\text{C. } r = (\sqrt{2} - 1)R$$

$$\text{D. } s = (1 + \sqrt{2})R$$

Answer: A,B,C,D



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67. Statement I In a $\triangle ABC$, if $a < b < c$ and r is inradius and $r_1, r_2 + r_2r_3$ are the exradii opposite to angle A,B,C respectively, then $r < r_1 < r_2 < r_3$.

Statement II For, $\triangle ABC$ $r_1r_2 + r_2r_3 + r_3r_1 = \frac{r_1r_2r_3}{r}$

A. Statement I is True, Statement II is True, Statement II is a correct explanation for Statement I.

B. Statement I is True, Statement II is True, Statement II is NOT a correct explanation for Statement I.

C. Statement I is True, Statement II is False.

D. Statement I is False, Statement II is True.

Answer: A::B::C::D



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68. Statement I If the sides of a triangle are 13, 14 15 then the radius of in circle =4

Statement II In ΔABC , $\Delta = \sqrt{s(s-a)(s-b)(s-c)}$ where $s = \frac{a+b+c}{2}$ and $r = \frac{\Delta}{s}$

A. Statement I is True, Statement II is True, Statement II is a correct explanation for Statement I.

B. Statement I is True, Statement II is True, Statement II is NOT a correct explanation for Statement I.

C. Statement I is True, Statement II is False.

D. Statement I is False, Statement II is True.

Answer: A::B::D



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69. Statement I In $a\Delta ABC$, $\sum \frac{\cos^2 \frac{A}{2}}{a}$ has the value equal to $\frac{s^2}{abc}$.

Statement II in $a\Delta ABC$, $\cos \frac{A}{2} = \sqrt{\frac{(s-b)(s-c)}{bc}}$

$\cos \frac{\beta}{2} = \sqrt{\frac{(s-a)(s-c)}{ac}}$, $\cos \frac{c}{2} = \sqrt{\frac{(s-a)(s-b)}{ab}}$

- A. Statement I is True, Statement II is True, Statement II is a correct explanation for Statement I.
- B. Statement I is True, Statement II is True, Statement II is NOT a correct explanation for Statement I.
- C. Statement I is True, Statement II is False.
- D. Statement I is False, Statement II is True.

Answer: C



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70. If $a=4$ then area of the ΔABC is equal to

A. $\frac{3\sqrt{2}}{2}$

B. 3

C. $4\sqrt{3}$

D. $3\sqrt{2}$

Answer: A::B::C::D



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71. The radius of the circle circumscribing the triangle ABC, is equal to

A. $\frac{\sqrt{10}}{2}$

B. $\sqrt{5}$

C. $\sqrt{10}$

D. $\frac{\sqrt{5}}{2}$

Answer: A::B::C::D



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72. Let Δ denote the area of the ΔABC and Δ_p be the area of its pedal triangle. If $\Delta = k\Delta_p$, then k is equal to



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73. x is equal to

A. $\frac{\pi}{9}$

B. $\frac{2\pi}{9}$

C. $\frac{\pi}{3}$

D. None of these

Answer: B



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74. $\triangle ABC$ is

- A. Equilateral
- B. Isosceles
- C. Scalene
- D. Right angled

Answer: D



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75. Which of the following is true ?

- A. $Bc > AC$

B. $AC = AB$

C. $AC > AB$

D. $BC = AC$

Answer: A::C::D

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76. If l, m, n denote the side of a pedal triangle, then $\frac{l}{a^2} + \frac{m}{b^2} + \frac{n}{c^2}$ is equal to

A. $\frac{a^2 + b^2 + c^2}{a^3 + b^3 + c^3}$

B. $\frac{a^2 + b^2 + c^2}{2abc}$

C. $\frac{a^3 + b^3 + c^3}{abc(a + b + c)}$

D. $\frac{1}{a} + \frac{1}{b} + \frac{1}{c}$

Answer: B

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77. If R be circum-radius of Δ , then circum-radius of a pedal Δ is

A. R

B. $\frac{2R}{3}$

C. $\frac{R}{3}$

D. $\frac{R}{2}$

Answer: D



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78. The in-radius of pedal Δ of a ΔABC is

A. $\frac{R}{2}$

B. $R \sin A \sin B \sin C$

C. $2R \cos A \cos B \cos C$

D. $4R \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$

Answer: A::B::C::D



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79. In a triangle ABC, if $r_1 + r_3 + r = r_2$, then find the value of $(\sec^2 A + \csc^2 B - \cot^2 C)$,



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80. In ΔABC , let $b = 6$, $c = 10$ and $r_1 = r_2 + r_3 + r$ then find area of ΔABC .



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81. Consider on obtuse angle triangles with side 8 cm, 15 cm and \times cm (largest side being 15 cm). If \times is an integer, then find the number of possible triangels.



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82. Let ABC be a right angled triangle at C . If the inscribed circle touches the side AB at D and $(AD)(BD) = 11$, then find the area of triangle ABC .

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83. Consider a $\triangle ABC$ and let a, b , and c denote the lengths of the sides opposite to vertices A, B and C , respectively. Suppose $a = 2, b = 3, c = 4$ and H be the orthocentre. Find $15(HA)^2$.

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84. In a triangle ABC , the internal angle bisector of $\angle ABC$ meets AC at K . If $BC = 2, CK = 1$ and $BK = \frac{3\sqrt{2}}{2}$, then find the length of side AB .

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85. Triangle ABC has $AC = 13$, $AB = 15$ and $BC = 14$. Let ' O ' be the circumcentre of the ΔABC . If the length of perpendicular from the point ' O ' on BC can be expressed as a rational $\frac{m}{n}$ in the lowest form then find $(m + n)$.

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86. Two sides of a triangle are given by the roots of the equation $x^2 - 2\sqrt{3}x + 2 = 0$. The angle between the sides is $\frac{\pi}{3}$. Find the perimeter of Δ .

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87. If in ΔABC , $\angle A = 90^\circ$ and $c, \sin B \cos B$ are rational numbers, then show a and b are rational.

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88. If the sides of a ΔABC are in AP and a is the smallest side, then $\cos A$ equals

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89. If A , B and C are angles of a triangle such that $\angle A$ is obtuse, then show $\tan B \tan C < 1$.

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90. If A is the area and $2s$ is the sum of the sides of a triangle, then

$$A \leq \frac{s^2}{4} \quad (\text{b}) \quad A \leq \frac{s^2}{3\sqrt{3}} \quad 2R \sin A \sin B \sin C \quad (\text{d}) \quad \text{none of these}$$

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91. In a triangle, if $r_1 > r_2 > r_3$, then show $a > b > c$.

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92. D is midpoint of BC in $\triangle ABC$ such that AD and AC are perpendicular,

Show that $\cos A \cos C = \frac{2(c^2 - a^2)}{3ac}$



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93. Prove that in

$\triangle ABC$, $a^3 \cos(B - C) + b^3 \cos(C - A) + c^3 \cos(A - B) = 3abc$



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94. If in a triangle of base 'a', the ratio of the other two sides is r ($r < 1$). Show that the altitude of the triangle is less than or equal to $\frac{ar}{1 - r^2}$



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95. Three circles touch each other externally. The tangents at their point of contact meet at a point whose distance from a point of contact is 4.

Then, the ratio of their product of radii to the sum of the radii is

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96. The internal bisectors of the angles of a ΔABC meet the sides BC, CA, AB in D, E and F, respectively. Show that the area of the ΔDEF is equal to,

$$\frac{2\Delta abc}{(b+c)(c+a)(a+b)}$$

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97. Prove m:n theorem in a ΔABC , a point D is taken on side BC such that BD:DC is m:n. Then prove that (1) $(m+n)\cot\theta = m\cot\alpha - n\cot\beta$
(2) $(m+n)\cot\theta = n\cot B - m\cot C$

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98. The base of a triangle is divided into three equal parts. If t_1, t_2, t_3 be the tangent of the angles subtended by these parts at the opposite vertex, prove that :

$$\left(\frac{1}{t_1} + \frac{1}{t_2}\right)\left(\frac{1}{t_1} + \frac{1}{t_3}\right) = 4\left(1 + \frac{1}{t_1^2}\right)$$

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99. Prove that the triangle ABC is equilateral if $\cot A + \cot B + \cot C = \sqrt{3}$

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100. In any triangle. if $\frac{a^2 - b^2}{a^2 + b^2} = \frac{\sin(A - B)}{\sin(A + B)}$, then prove that the triangle is either right angled or isosceles.

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101. The sides of a triangle are in AP. If the angles A and C are the greatest and smallest angle respectively, then $4(1 - \cos A)(1 - \cos C)$ is equal to

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102. Perpendiculars are drawn from the angles A, B and C of an acute-angled triangle on the opposite sides, and produced to meet the circumscribing circle. If these produced parts are α, β, γ , respectively,

then show that, then show that

$$\frac{a}{\alpha} + \frac{b}{\beta} + \frac{c}{\gamma} = 2(\tan A + \tan B + \tan C).$$

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103. If $a = \cos \theta + i \sin \theta$, $b = \cos \phi + i \sin \phi$, $c = \cos \psi + i \sin \psi$ and

$$\frac{a}{b} + \frac{b}{c} + \frac{c}{a} = 2 \text{ then } \sin(\theta - \phi) + \sin(\phi - \psi) + \sin(\psi - \theta) \text{ equals}$$

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104. The product of the sines of the angles of a triangle is p and the product of their cosines is q . Show that the tangents of the angles are the roots of the equation $qx^3 - px^2 + (1 + q)x - p = 0$.

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105. Given the base of a triangle, the opposite angle A , and the product k^2 of other two sides, show that it is not possible for a to be less than $2k \sin \frac{A}{2}$

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106. If in a triangle ABC , $\angle C = 60^\circ$, then prove that
$$\frac{1}{a+c} + \frac{1}{b+c} = \frac{3}{a+b+c}$$

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107. Let $1 < m < 3$. In a triangle ABC , if $2b = (m + 1)a$ &

$$\cos A = \frac{1}{2} \sqrt{\frac{(m-1)(m+3)}{m}}$$

prove that there are two values for the third side, one of which is m times the other.



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108. In any $\triangle ABC$, if D be any point on the base BC such that

$$\frac{BD}{DC} = \frac{m}{n} \text{ and } \angle ABD = \alpha, \angle DAC = \beta, \angle CDA = \theta \text{ and } AD = x$$

then prove that

$$(m+n)^2 \cdot x = (m+n)(mb^2 + nc^2) - mna^2$$



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109. $ABCD$ is a trapezium such that $AB \parallel CD$ and CB is perpendicular to them. If $\angle ADB = \theta$, $BC = p$, and $CD = q$, show that

$$AB = \frac{(p^2 + q^2) \sin \theta}{p \cos \theta + q \sin \theta}$$



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110. In a triangle ABC, prove that

$$\frac{\cot\left(\frac{A}{2}\right) + \cot\left(\frac{B}{2}\right) + \cot\left(\frac{C}{2}\right)}{\cot A + \cot B + \cot C} = \frac{(a + b + c)^2}{a^2 + b^2 + c^2}$$

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111. If the sides of a triangle are in A.P., and its greatest angle exceeds the least angle by α , show that the sides are in the ratio $1 + x : 1 : 1 - x$,

where $x = \sqrt{\frac{1 - \cos \alpha}{7 - \cos \alpha}}$

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112. In a ABC , if $\frac{\tan A}{2}, \frac{\tan B}{2}, \frac{\tan C}{2}$ are in A.P.; then show that $\cos A, \cos B, \cos C$ are in A.P.

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113. If a, b, c are in HP, then prove that $\sin^2 \frac{A}{2}, \sin^2 \frac{B}{2}, \sin^2 \frac{C}{2}$ are also in HP.

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114. If r_1, r_2, r_3 are the ex-radii of ΔABC , then prove that

$$\frac{bc}{r_1} + \frac{ca}{r_2} + \frac{ab}{r_3} = 2R \left[\left(\frac{a}{b} + \frac{b}{a} \right) + \left(\frac{b}{c} + \frac{c}{b} \right) + \left(\frac{c}{a} + \frac{a}{c} \right) - 3 \right]$$

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115. If r and R are radii of the incircle and circum-circle of ΔABC , then prove that :

$$\begin{aligned} & 8rR \{ \cos^2 A/2 + \cos^2 B/2 + \cos^2 C/2 \} \\ & = 2bc + 2ca + 2ab - a^2 - b^2 - c^2. \end{aligned}$$

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116. Prove that

$$r_1^2 + r_2^2 + r_3^2 + r^2 = 16R^2 - a^2 - b^2 - c^2.$$

where r = in radius, R = circumradius, r_1, r_2, r_3 are ex-radii.



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117. Tangent are parallel to the three sides are drawn to the in-circle. If x, y, z are the lengths of the parts of the tangents within triangle, then

prove that
$$\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1.$$



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118. If in a triangle ABC , $\cos A + 2\cos B + \cos C = 2$ prove that the sides of the triangle are in AP



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119. In a cyclic quadrilateral ABCD, prove that $\tan^2 \frac{B}{2} = \frac{(s-a)(s-b)}{(s-c)(s-d)}$, $a, b, c,$ and d being the lengths of sides ABC, CD and DA respectively and s is semi-perimeter of quadrilateral.

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120. If x, y, z are respectively perpendiculars from the circumcentre on the sides of the ΔABC , the value of $\frac{a}{x} + \frac{b}{y} + \frac{c}{z} - \frac{abc}{4xyz} =$

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121. In the ΔABC , a similar $\Delta A'B'C'$ is inscribed so that $B'C' = \lambda BC$. If $B'C'$ is inclined at an angle θ with Bc then prove that $\lambda \cos \theta = \frac{1}{2}$.

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122. The circle inscribed in the triangle ABC touches the side BC , CA and AB in the point A_1B_1 and C_1 respectively. Similarly the circle inscribed in the $\Delta A_1B_1C_1$ touches the sides in A_2, B_2, C_2 respectively and so on. If $A_nB_nC_n$ be the n th Δ so formed, prove that its angles are $\left(C - \frac{\pi}{3}\right)$. Hence prove that the triangle so formed is ultimately equilateral.

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123. In a ΔABC , prove that:

$$2r \leq \frac{a \cot A + b \cot B + c \cot C}{3} \leq R$$

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124. If A, B and C are angles of a triangle, then prove

$$\text{that } E = \frac{\cos\left(\frac{B-C}{2}\right)}{\cos\left(\frac{B+C}{2}\right)} + \frac{\cos\left(\frac{C-A}{2}\right)}{\cos\left(\frac{C+A}{2}\right)} + \frac{\cos\left(\frac{A-B}{2}\right)}{\cos\left(\frac{A+B}{2}\right)} \geq 6$$

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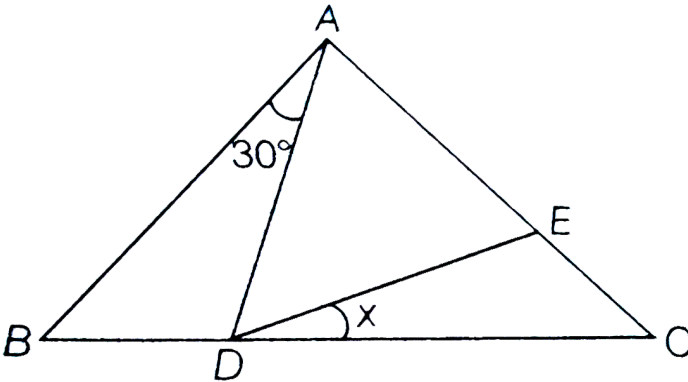
125. If Δ is the area of a triangle with side lengths a, b, c , then show that as $\Delta \leq \frac{1}{4}\sqrt{(a+b+c)abc}$ Also, show that the equality occurs in the above inequality if and only if $a = b = c$.



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Exercise For Session 1

1. In the given figure, if $AB = AC$, $\angle BAD = 30^\circ$ and $AE = AD$, then x is equal to



A. 15°

B. 10°

C. $12\frac{1}{2}$

D. $7\frac{1}{2}$

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2. In $\triangle ABC$, $a = 4$, $b = 12$ and $B = 60^\circ$, then the value of $\sin A$ is

A. $\frac{1}{2\sqrt{3}}$

B. $\frac{1}{3\sqrt{2}}$

C. $\frac{2}{\sqrt{3}}$

D. $\frac{\sqrt{3}}{2}$

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3. Let ABC be a triangle such that $\angle A = 45^\circ$, $\angle B = 75^\circ$, then $a + c\sqrt{2}$ is equal to

A. 0

B. b

C. $2b$

D. $-b$



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4. Angles A, B and C of a $\triangle ABC$ are in AP . If $\frac{b}{c} = \frac{\sqrt{3}}{\sqrt{2}}$, then $\angle A$ is equal to

A. $\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. $\frac{5\pi}{12}$

D. $\frac{\pi}{2}$



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5. If $\cot \frac{A}{2} = \frac{b+c}{a}$, then $\triangle ABC$ is

- A. Isosceles
- B. Equilateral
- C. Right angled
- D. None of these



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6. If in a $\triangle ABC$, $\frac{a^2 - b^2}{a^2 + b^2} = \frac{\sin(A - B)}{\sin(A + B)}$, then the triangle is

- A. Right angled or isosceles

B. Right angled and isosceles

C. Equilateral

D. None of these



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7. In any triangle ABC , prove that:

$$\frac{a^2 \sin(B - C)}{\sin B + s \in C} + \frac{b^2 \sin(C - A)}{\sin C + s \in A} + \frac{c^2 \sin(A - B)}{\sin A + s \in B} = 0$$

A. $a + b + c$

B. $a + b - c$

C. $a - b + c$

D. 0



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8. In any $\triangle ABC$, is $2 \cos B = \frac{a}{c}$, then the triangle is

- A. right angled
- B. equilateral
- C. isosceles
- D. None of these



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9. Prove that $\frac{(a + b + c)(b + c - a)(c + a - b)(a + b - c)}{4b^2c^2} = \sin^2 A$

- A. $\cos^2 A$
- B. $\sin^2 A$
- C. $\cos A \cos B \cos C$
- D. None of these



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10. If $a \cos A = b \cos B$, then the triangle is

- A. Isosceles
- B. Right angled
- C. Isosceles or right angled
- D. Right angled isosceles



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11. In a ΔABC , $(a + b + c)(b + c - a) = \lambda bc$ if

- A. $\lambda < 0$
- B. $\lambda > 0$
- C. $0 < \lambda < 4$
- D. $\lambda < 4$



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12. If: $a = 9$, $b = 8$ and $c = x$ satisfies $3 \cos C = 2$, then: $x =$

A. $x = 5$

B. $x = 6$

C. $x = 4$

D. $x = 7$



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13. In $\triangle ABC$, if $\sin^2 A + \sin^2 B = \sin^2 C$, then the triangle is

A. equilateral

B. isosceles

C. right angled

D. None of these

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14. The lengths of the sides of a triangle are $\alpha - \beta$, $\alpha + \beta$ and $\sqrt{3\alpha^2 + \beta^2}$, ($\alpha > \beta > 0$). Its largest angle is

A. $\frac{2\pi}{3}$

B. $\frac{\pi}{2}$

C. $\frac{3\pi}{4}$

D. $\frac{5\pi}{6}$

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15. In any triangle, $\frac{1 + \cos(A - B)\cos C}{1 + \cos(A - C)\cos B} =$

A. $\frac{a^2 + b^2}{a^2 + c^2}$

B. $\frac{b^2 + c^2}{b^2 - c^2}$

C. $\frac{c^2 - a^2}{a^2 + b^2}$

D. None of these



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16. The sides a, b, c of a triangle ABC are in arithmetic progression and ' a ' is the smallest side. What is $\cos A$ equal to ?

A. $\frac{3c - 4b}{2c}$

B. $\frac{3c - 4b}{2b}$

C. $\frac{4c - 3b}{2c}$

D. None of these



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17. In a $\triangle ABC$, $a^2 \cos 2B + b^2 \cos 2A + 2ab \cos(A - B) =$

A. a^2

B. c^2

C. b^2

D. $a^2 + b^2$



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18. In any $\triangle ABC$, $2[bc \cos A + ca \cos B + ab \cos C] =$

A. $a^2 + b^2 + c^2$

B. $a^2 + b^2 - c^2$

C. $a^2 - b^2 + c^2$

D. $a^2 - b^2 + c^2$

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19. In a $\triangle ABC$, $\tan \frac{1}{2}(A + B) \cdot \cot \frac{1}{2}(A - B)$ is equal to

A. $\frac{a - b}{a + b}$

B. $\frac{a + b}{c}$

C. $\frac{a + b}{a - b}$

D. $\frac{a - b}{2(a + b)}$

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20. If in a $\triangle ABC$, $b = \sqrt{3}$, $c = 1$ and $B - C = 90^\circ$, then $\angle A$ is

A. 30°

B. 45°

C. 75°

D. 15°



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Exercise For Session 2

1. If in a triangle ABC , $(s - a)(s - b) = s(s - c)$, then angle C is equal to

A. 90°

B. 45°

C. 30°

D. 60°



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2. In any $\triangle ABC$, if $\cot \frac{A}{2}$, $\cot \frac{B}{2}$, $\cot \frac{C}{2}$ are in AP, then a, b, c are in

A. AP

B. GP

C. HP

D. None of these



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3. In any $\triangle ABC$, $\frac{\tan \frac{A}{2} - \tan \frac{B}{2}}{\tan \frac{A}{2} + \tan \frac{B}{2}}$ is equal to

A. $\frac{a-b}{a+b}$

B. $\frac{a-b}{c}$

C. $\frac{a-b}{a+b+c}$

D. $\frac{c}{a+b}$

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4. In a triangle ABC, $bccos^2\frac{A}{2} + cacos^2\frac{B}{2} + abc\cos^2\frac{C}{2} =$

A. $(s-a)^2$

B. $(s-b)^2$

C. $(s-c)^2$

D. s^2

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5. In a $\triangle ABC$, if $\cos A + \cos C = 4\sin^2\left(\frac{B}{2}\right)$, then a,b,c are in

A. AP

B. GP

C. HP

D. None of these



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6. In a $\triangle ABC$, if $b^2 + c^2 = 3a^2$, then $\cot B + \cot C - \cot A$ is equal to

A. 1

B. $\sqrt{3}$

C. 2

D. None of these



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7. In any ΔABC ,
$$\left(\frac{b-c}{a}\right)\cos^2\left(\frac{A}{2}\right) + \left(\frac{c-a}{b}\right)\cos^2\left(\frac{B}{2}\right) + \left(\frac{a-b}{c}\right)\cos^2\left(\frac{C}{2}\right)$$

is equal

A. $\frac{b^2 - c^2}{a^2}$

B. $\frac{c^2 - a^2}{b^2}$

C. $\frac{a^2 - b^2}{c^2}$

D. 0



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8. If in a ΔABC , the tangent of half the difference of two angles is one-third the tangent of half the sum of the angles. Then, the ratio of the sides opposite to the angles is

A. 2 : 3

B. 1 : 3

C. 2:1

D. 3:4

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9. If in a triangle a $\frac{\cos^2 C}{2} + \frac{\cos^2 A}{2} = \frac{3b}{2}$, then find the relation between the sides of the triangle.

A. AP

B. GP

C. HP

D. AGP

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10. If $c^2 = a^2 + b^2$, then $4s(s - a)(s - b)(s - c)$ is equal to

A. s^4

B. b^2c^2

C. c^2a^2

D. a^2b^2



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11. The number of possible $\angle ABC$ in which $BC = \sqrt{11}cm$, $CA = \sqrt{13}cm$ and $A = 60^\circ$ is

A. 0

B. 1

C. 2

D. None of these



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12. If two sides a, b and the $\angle A$ be such that the sum of two values of the third side is

A. $b^2 - a^2$

B. $2b \cos A$

C. $2b \sin A$

D. $\frac{b - c}{b + c}$



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13. If in a ΔABC , $\sin A = \sin^2 B$ and $2 \cos^2 A = 3 \cos^2 B$, then the ΔABC is

A. right angled

B. obtuse angled

C. isosceles

D. equilateral



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14. If $a \cos A = b \cos B$, then the triangle is

A. equilateral

B. right angled

C. isosceles

D. isosceles or right angled



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15. Point D, E are taken on the side BC of an acute angled triangle ABC,, such that $BD = DE = EC$. If

$\angle BAD = x$, $\angle DAE = y$ and $\angle EAC = z$ then the value of $\frac{\sin(x + y)\sin(y + z)}{\sin x \sin z}$ is _____

- A. 1
- B. 2
- C. 4
- D. None of these



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16. If the base angles of triangle are $\frac{22}{12}$ and $112\frac{1}{2}$, then prove that the altitude of the triangle is equal to $\frac{1}{2}$ of its base.

- A. half the base
- B. the base

C. twice the base

D. four times the base

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17. In a $\triangle ABC$, $a = 1$ and the perimeter is six times the AM of the sines of the angles. The measure of $\angle A$ is

A. $\frac{\pi}{3}$

B. $\frac{\pi}{2}$

C. $\frac{\pi}{6}$

D. $\frac{\pi}{4}$

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18. In a $\triangle ABC$, if median AD is perpendicular to AB , the $\tan A + 2 \tan B$ is equal to

A. 1

B. 3

C. 0

D. $\frac{1}{2}$



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19. The product of the sines of the angles of a triangle is p and the product of their cosines is q . Then the tangents of the angles are the roots of the equation $qx^3 - px^2 + (1 + q)x - p = ?$.

A. $qx^2 - px^2 + (1 + q)x - p = 0$

B. $px^3 - qz^2 + (1 - p)x - q = 0$

C. $(1 + q)x^3 - px^2 + qx - p = 0$

D. None of these

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Exercise For Session 3

1. The side of a triangle are 22 cm, 28 cm, and 36 cm So, find the area of a the circumscribed circle.

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2. If the lengths of the side of a triangle are 3,4 and 5 units, then find the circum radius R.

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3. In an equilateral triangle of side $2\sqrt{3}$ cm. The find circum-radius.

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4. If $8R^2 = a^2 + b^2 + c^2$. then prove that the Δ is right angled.

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5. In a ΔABC , show that $2R^2 \sin A \sin B \sin C = \Delta$.

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6. In a ΔABC , show that $\frac{a \cos A + b \cos B + c \cos C}{a + b + c} = \frac{r}{R}$

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7. If the sides of a triangles are 3: 7: 8, then ratio R:r

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8. In an equilateral triangle show that the in-radius and the circum-radius are connected by $r = \frac{R}{2}$.

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9. In any $\triangle ABC$, find $\sin A + \sin B + \sin C$.

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10. In any $\triangle ABC$, show that $\cos A + \cos B + \cos C = \left(1 + \frac{r}{R}\right)$.

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11. Prove that $\frac{r_1 - r}{a} + \frac{r_2 - r}{b} = \frac{c}{r_3}$

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12. show that $r_2r_3 + r_3r_1 + r_1r_2 = s^2$

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13. Show that $(r_1 + r_2)(r_2 + r_3)(r_3 + r_1) = 4Rs^2$

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14. If $r_1 + r_2 + r = r_3$, then show that Δ is right angled.

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15. In an equilateral triangle, the in-radius, circum-radius and one of the ex-radii are in the ratio

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16. Show that $\left(\frac{1}{r_1} + \frac{1}{r_2}\right)\left(\frac{1}{r_2} + \frac{1}{r_1}\right)\left(\frac{1}{r_3} + \frac{1}{r_1}\right) = \frac{64R^3}{a^2b^2c^2}$

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17. The exradii r_1, r_2, r_3 of $\triangle ABC$ and in HP, show that a, b and c in AP

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18. In a $\triangle ABC$, show that $r_1 \cdot r_2 \cdot r_3 \cdot r = \Delta^2$.

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19. If the angle of a triangle are in the ratio $1:2:3$, then show that the sides opposite to the respective angle are in the ratio $1:\sqrt{3}:2$.

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20. Show that, $4Rr \cos \frac{A}{2} \cos \frac{B}{2} \cos \frac{C}{2} = \Delta$

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21. In ΔABC , if $(a - b)(s - c) = (b - c)(s - a)$ then r_1, r_2, r_3 are in

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22. In a triangle ABC, if $\frac{1}{r_1^2} + \frac{1}{r_2^2} + \frac{1}{r_3^2} + \frac{1}{r^2} =$

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23. $(r_1 - r)(r_2 - r)(r_3 - r) = 4Rr^2$

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24. Show that $\left(\frac{1}{r_1} + \frac{1}{r_2}\right)\left(\frac{1}{r_2} + \frac{1}{r_3}\right)\left(\frac{1}{r_3} + \frac{1}{r_1}\right) = \frac{64R^3}{a^2b^2c^2}$

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25. Prove that

$$(r + r_1)\tan\left(\frac{B - C}{2}\right) + (r + r_2)\tan\left(\frac{C - A}{2}\right) + (r + r_3)\tan\left(\frac{A - B}{2}\right)$$

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26. Show that $\frac{b - c}{r_1} + \frac{c - a}{r_2} + \frac{c - a}{r_3} = 0$.

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27. If the sides be a, b, c , then find $(r_1 - r)(r_2 + r_3)$.

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28. If a, b, c are in AP, then show that r_1, r_2, r_3 are in HP.

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29. In ΔABC with usual notation $\frac{r_1}{bc} + \frac{r_2}{ca} + \frac{r_3}{ab}$ is

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30. Show that $r_1 + r_2 = c \cot\left(\frac{C}{2}\right)$

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31. Show that $Rr(\sin A + \sin B + \sin C) = \Delta$

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32. Show that $16R^2 r r_1 r_2 r_3 = a^2 b^2 c^2$

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33. If $\frac{r}{r_1} = \frac{r_2}{r_3}$, then show that $c = 90^\circ$.

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Exercise For Session 4

1. If H is the orthocentre of the ΔABC , then find AH.

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2. Prove that $a \cos A + b \cos B + c \cos C = 4R \sin A \sin B \sin C$.

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3. If the altitudes of a triangle be 2,4,6, then find its in-radius.

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4. In a $\triangle ABC$, if $a = 3, b = 4, c = 5$, then find the distance between its incentre and circumcentre.

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5. If p_1, p_2, p_3 are respectively the perpendicular from the vertices of a triangle to the opposite sides, then find the value of $p_1 p_2 p_3$.

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6. Prove that the distance between the circumcenter and the incenter of triangle ABC is $\sqrt{R^2 - 2Rr}$

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7. In $\triangle ABC$ it is given distance between the circumcentre (O) and orthocentre (H) is $R\sqrt{1 - 8 \cos A \cos B \cos C}$. If Q is the midpoint of

OH, then AQ is

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8. If in a $\triangle ABC$, AD , BE and CF are the altitudes and R is the circumradius, then find the radius of the DEF.

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Exercise For Session 5

1. Find the sum of the radii of the circles, which are respectively inscribed and circumscribed about the a regular polygon of n sides.

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2. Find the radius of the circumscribing circle of a regular polygon of n sides each of length is a.



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3. If A , A_1 , A_2 and A_3 are the areas of the inscribed and escribed circles

of a triangle, prove that $\frac{1}{\sqrt{A}} = \frac{1}{\sqrt{A_1}} + \frac{1}{\sqrt{A_2}} + \frac{1}{\sqrt{A_3}}$



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4. A polygon of nine sides, each side of length 2, is inscribed in a circle.

The radius of the circle is _____.



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5. The area of the circle and the area of a regular polygon of n sides and

of perimeter equal to that of the circle are in the ratio of $\tan\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$ (b)

$\cos\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$ $\frac{\sin \pi}{n} : \frac{\pi}{n}$ (d) $\cot\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$



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6. Let $A_1, A_2, A_3, \dots, A_n$ be the vertices of an n -sided regular polygon such that $\frac{1}{A_1A_2} = \frac{1}{A_1A_3} + \frac{1}{A_1A_4}$. Find the value of n . Prove or disprove the converse of this result.

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7. I_n is the area of n sided regular polygon inscribed in a circle unit radius and O_n be the area of the polygon circumscribing the given circle, prove

that
$$I_n = \frac{O_n}{2} \left(1 + \sqrt{1 - \left(\frac{2I_n}{n} \right)^2} \right)$$

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Exercise For Session 6

1. The area of a cyclic quadrilateral ABCD is $\frac{3\sqrt{3}}{4}$. The radius of the circle circumscribing cyclic quadrilateral is 1. If $AB = 1$ and $BD = \sqrt{3}$, then $BC \cdot CD$ is equal to

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2. If two adjacent sides of a cyclic quadrilateral are 2 and 5 and the angle between them is 60° . If the third side is 3, then the remaining fourth side is (a) 2 (b) 3 (c) 4 (d) 5

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3. The ratio of the area of a regular polygon of n sides inscribed in a circle to that of the polygon of same number of sides circumscribing the same is 3:4. Then the value of n is (a) 6 (b) 4 (c) 8 (d) 12

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4. A right angled trapezium is circumscribed about a circle. Find the radius of the circle. If the lengths of the bases (i.e. parallel sides) are equal to a and b .

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5. If A, B, C, D are the angles of quadrilateral, then find $\frac{\sum \tan A}{\sum \cot A}$.

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Exercise For Session 7

1. In triangle ABC , $a:b:c = (1+x):1:(1-x)$ where $x \in (0, 1)$ If $\angle A = \frac{\pi}{2} + \angle C$, then x equal to

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2. In a ΔABC , $2s =$ perimeter and $R =$ circumradius. Then, find $\frac{s}{R}$.

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3. If in a ΔABC , $\angle C = 90^\circ$, then the maximum value of $\sin A \sin B$ is



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4. If the area of a triangle is 81 square cm and its perimeter is 27 cm, then find its in-radius in centimetres.



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5. In a $\triangle ABC$, if $r_1 = 2r_2 = 3r_3$, then show that $\frac{a}{b} = \frac{5}{4}$.



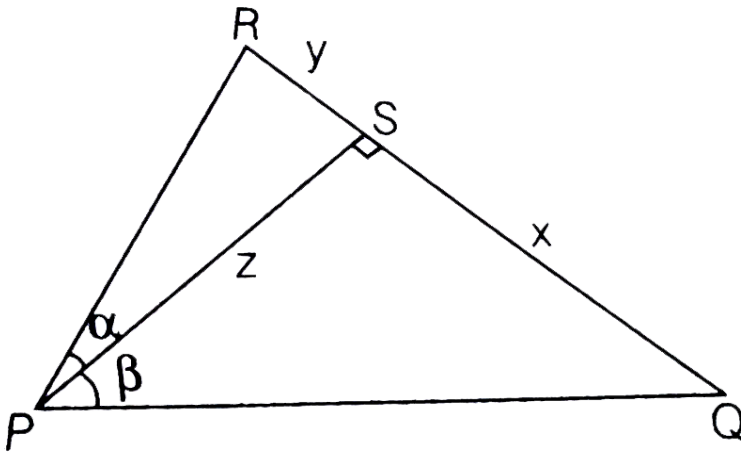
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6. The radius of the larger circle lying in the first quadrant and touching the line $4x + 3y - 12 = 0$ and the coordinate axes, is



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7. In a $\triangle PQR$ as show in figure given that $x:y:z::2:3:6$, then find value of $\angle QPR$.



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8. If the angle of a righta angled triangle are in A.P. then the ratio of the in -radius and the perimeter, is



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9. If in a triangle $\left(1 - \frac{r_1}{r_2}\right)\left(1 - \frac{r_1}{r_3}\right) = 2$ then the triangle is right angled (b) isosceles equilateral (d) none of these

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Exercise For Session 8

1. If a tower subtends angles θ , 2θ and 3θ at three points A, B, and C respectively, lying on the same side of a horizontal line through the foot of the tower, show that $\frac{AB}{BC} \frac{\cot \theta - \cot 2\theta}{\cot 2\theta - \cot 3\theta}$.

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2. A person stands at a point A due south of a tower of height h and observes that its elevation is 60° . He then walks westwards towards B, where the elevation is 45° . At a point C on AB produced, show that if he finds it to be 30° . OA , OB , OC are in GP.

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3. A train travelling on one of two intersecting railway lines, subtends at a certain station on the other line, an/ angle α when the front of the carriage reaches the junction and an angle β when the end of the carriage reaches it. Then, the two lines are inclined to each other at an angle θ , show that $2 \cot \theta = \cot \alpha - \cot \beta$

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4. The angle of elevation of the top of the tower observed from each of three points A,B , C on the ground, forming a triangle is the same angle α . If R is the circum-radius of the triangle ABC, then find the height of the tower

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5. The length of the shadow of a pole inclined at 10° to the vertical towards the sun is 2.05 meters, when the elevation of the sun is 38° . Then, the length of the pole.



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Exercise (Single Option Correct Type Questions)

1. In a $\triangle ABC$, if $a = 13$, $b = 14$ and $c = 15$, then $\angle A$ is equal to (All symbols used have their usual meaning in a triangle.)

A. $\sin^{-1} \frac{4}{5}$

B. $\sin^{-1} \frac{3}{5}$

C. $\sin^{-1} \frac{3}{4}$

D. $\sin^{-1} \frac{2}{3}$

Answer: A



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2. In a ΔABC , if $b = (\sqrt{3} - 1)a$ and $\angle C = 30^\circ$, then the value of $(A-B)$ is equal to (All symbols used have usual meaning in the triangle.)

A. 30°

B. 45°

C. 60°

D. 75°

Answer: C



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3. In a ΔABC , if $\angle C = 105^\circ$, $\angle B = 45^\circ$ and length of side $AC = 2$ units, then the length of the side AB is equal to

A. $\sqrt{2}$

B. $\sqrt{3}$

C. $\sqrt{2} + 1$

D. $\sqrt{3} + 1$

Answer: C



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4. If P is a point on the altitude AD of the $\triangle ABC$ such that $\angle CBP = \frac{B}{3}$, then AP is equal to

A. $2a \sin \frac{C}{3}$

B. $2b \sin \frac{A}{3}$

C. $2c \sin \frac{B}{3}$

D. $2c \sin \frac{C}{3}$

Answer: C



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5. In $\triangle ABC$, if $2b = a + c$ and $A - C = 90^\circ$, then $\sin B$ equal

All symbols used have usual meaning in $\triangle ABC$.]

A. $\frac{\sqrt{7}}{5}$

B. $\frac{\sqrt{5}}{8}$

C. $\frac{\sqrt{7}}{4}$

D. $\frac{\sqrt{5}}{3}$

Answer: C



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6. Let ABC be a right triangle with length of side $AB = 3$ and hypotenuse $AC = 5$. If D is a point on BC such that $\frac{BD}{DC} = \frac{AB}{AC}$, then AD is equal to

A. $\frac{4\sqrt{3}}{3}$

B. $\frac{3\sqrt{5}}{2}$

C. $\frac{4\sqrt{5}}{3}$

D. $\frac{5\sqrt{3}}{4}$

Answer: B



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7. Two medians drawn from the acute angles of a right angled triangle intersect at an angle $\frac{\pi}{6}$. If the length of the hypotenuse of the triangle is 3 units, then the area of the triangle (in sq units) is \sqrt{K} , then K is

A. 3

B. $\frac{3\sqrt{5}}{2}$

C. $\sqrt{3}$

D. None of these

Answer: C



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8. If in a right angle $\triangle ABC$, $4\sin A \cos B - 1 = 0$ and $\tan A$ is finite, then

- A. angles are in AP
- B. angles are in GP
- C. angles are in HP
- D. None of these

Answer: A



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9. Let $A = \begin{bmatrix} a & b & c \\ p & q & r \\ 1 & 1 & 1 \end{bmatrix}$ and $B = A^2$

If

$$(a - b)^2 + (p - q)^2 = 25, (b - c)^2 + (q - r)^2 = 36 \text{ and } (c - a)^2 + (r - p)^2 = 49$$

then $\det B$ is

A. 192

B. 864

C. 2456

D. $25 \times 36 \times 47$

Answer: B



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10. If in a $\triangle ABC$, the incircle passing through the point of intersection of perpendicular bisector of sides BC, AB, then $4 \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$ equal to

A. $\sqrt{2}$

B. $\sqrt{2} - 1$

C. $\sqrt{2} + 1$

D. $\frac{1}{2}$

Answer: B



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11. If two sides of a triangle are roots of the equation $x^2 - 7x + 8 = 0$ and the angle between these sides is 60° then the product of inradius and circumradius of the triangle is $\frac{8}{7}$ (b) $\frac{5}{3}$ (c) $\frac{5\sqrt{2}}{3}$ (d) 8

A. $\frac{8}{7}$

B. $\frac{5}{3}$

C. $\frac{5\sqrt{3}}{3}$

D. 8

Answer: B



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12. If median AD of a triangle ABC makes angle $\frac{\pi}{6}$ with side BC , then the value of $(\cot B - \cot C)^2$ is equal to

A. 6

B. 9

C. 12

D. 15

Answer: C



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13. If the perimeter of the triangle formed by feet of altitudes of the triangle ABC is equal to four times the circumradius of ΔABC , then identify the type of ΔABC

A. isosceles triangle

B. equilateral triangle

C. right angled triangle

D. None of these

Answer: D



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14. In a triangle with one angle $\frac{2\pi}{3}$, the lengths of the sides form an A.P.

If the length of the greatest side is 7 cm, the radius of the circumcircle of the triangle is

A. $\frac{7\sqrt{3}}{3} \text{ cm}$

B. $\frac{5\sqrt{3}}{3} \text{ cm}$

C. $\frac{2\sqrt{3}}{3} \text{ cm}$

D. $\sqrt{3} \text{ cm}$

Answer: A



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15. Sides of triangle ABC are in A.P. if $a < \min \{b, c\}$ then $\cos A$ is equal to

A. $\frac{3c - 4b}{2b}$

B. $\frac{3c - 4b}{2c}$

C. $\frac{4c - 3b}{2b}$

D. $\frac{4c - 3b}{2c}$

Answer: D



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16. The product of the sines of the angles of a triangle is p and the product of their cosines is q . Show that the tangents of the angles are the roots of the equation $qx^3 - px^2 + (1 + q)x - p = 0$.

A. $qx^2 - px^2 + (1 - x)x - p = 0$

B. $qx^3 - px^2 - (1 - q)x - p = 0$

C. $qx^3 - px^2 + (1 + q)x - p = 0$

D. None of these

Answer: A



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17. Let C be incircle of $\triangle ABC$. If the tangents of lengths t_1, t_2 and t_3 are drawn inside the given triangle parallel to sides a, b and c, respectively,

then $\frac{t_1}{a} + \frac{t_2}{b} + \frac{t_3}{c}$ is equal to

A. 0

B. 1

C. 2

D. 3

Answer: B

18. If the sine of the angles of ΔABC satisfy the equation

$$c^3x^3 - c^2(a + b + c)x^2 + lx + m = 0$$

(where a,b,c are the sides of ΔABC), then ΔABC is

A. always right angled for any l, m

B. right angled only when

$$l = c(ab + bc + ca) = c \sum ab, m = -abc$$

C. right angled only when $l = \frac{c \sum ab}{4}, m = -\frac{abc}{8}$

D. never right angled

Answer: B

19. The rational number which equals the number 2. 357 with recurring

decimal is $\frac{2355}{1001}$ b. $\frac{2379}{997}$ c. $\frac{2355}{999}$ d. none of these

A. $\frac{50}{9}$

B. $\frac{25}{9}$

C. $\frac{25}{3}$

D. $\frac{27}{7}$

Answer: C



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20. In a triangle ABC , $a \geq b \geq c$. If

$$\frac{a^3 + b^3 + c^3}{\sin^3 A + \sin^3 B + \sin^3 C} = 8,$$

then the maximum value of a

$$\sin^3 A + \sin^3 B + \sin^3 C$$

A. $\frac{1}{2}$

B. 2

C. 8

D. 64

Answer: B



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21. A triangle ABC exists such that

A. $(b + c + a)(b + c - a) = 5bc$

B. the sides are of lengths $\sqrt{19}$, $\sqrt{38}$, $\sqrt{116}$

C. $\cos\left(\frac{b^2 - c^2}{a^2}\right) + \left(\frac{c^2 - a^2}{b^2}\right) + \left(\frac{a^2 - b^2}{c^2}\right) = 0$

D. $\cos\left(\frac{B - C}{2}\right) = (\sin B + \sin C)\cos\left(\frac{B + C}{2}\right)$

Answer: D



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22. In a δABC , a, c, A are given and b_1, b_2 are two values of third side b such that $b_2 = 2b_1$. Then, the value of $\sin A$.

A. $\sqrt{\frac{9a^2 - c^2}{8a^2}}$

B. $\sqrt{\frac{9a^2 - c^2}{8c^2}}$

C. $\sqrt{\frac{9a^2 - c^2}{8b^2}}$

D. None of these

Answer: B



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23. In a triangle ABC, if

$$\cot A = (x^3 + x^2 + x)^{\frac{1}{2}}, \cot B = (x + x^{-1} + 1)^{\frac{1}{2}} \text{ and } \cot C = \frac{(x^{-3} + \dots)}{\dots}$$

then the triangle is

A. equilateral

B. isosceles

C. right angled

D. obtuse angled

Answer: C



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24. In a $\triangle ABC$, a, b, A are given and c_1, c_2 are two values of the third side c . The sum of the areas two triangles with sides a, b, c_1 and a, b, c_2 is

A. $\frac{1}{2}a^2 \sin 2A$

B. $\frac{1}{2}a^2 \sin 2A$

C. $b^2 \sin 2A$

D. None of these

Answer: A



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25. In $\triangle ABC$, if $a = 10$ and $b \cot B + c \cot C = 2(r + R)$ then the maximum area of $\triangle ABC$ will be

A. 50

B. $\sqrt{50}$

C. 25

D. 5

Answer: C



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26. Three circles touch one-another externally. The tangents at their point of contact meet at a point whose distance from a point contact is 4. Then, the ratio of the product of the radii of the sum of the radii of circles is

A. 16: 1

B. 1: 16

C. 8: 1

D. None of these

Answer: A



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27. Let a, b, c be the sides of a triangle. No two of them are equal and

$\lambda \in \mathbb{R}$ If the roots of the equation

$x^2 + 2(a + b + c)x + 3\lambda(ab + bc + ca) = 0$ are real distinct, then

A. $\lambda < \frac{4}{3}$

B. $\lambda > \frac{5}{3}$

C. $\lambda \in \left(\frac{1}{3}, \frac{5}{3}\right)$

D. $\lambda \in \left(\frac{4}{3}, \frac{5}{3}\right)$

Answer: A



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28. In triangle ABC, if P, Q, R divides sides BC, AC and AB, respectively, in the ratio k,1 (in order). If the ratio $\left(\frac{\text{area}\Delta PQR}{\text{area}\Delta ABC}\right)$ is $\frac{1}{3}$, then k is equal to

A. $\frac{1}{3}$

B. 2

C. 3

D. None of these

Answer: B



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29. Let $f(x + y) = f(x) \cdot f(y)$ for all x and y $f(1) = 2$ If in a triangle ABC, $a = f(3)$, $b = f(1) + f(3)$, $c = f(2) + f(3)$,

A. C

B. 2C

C. 3C

D. 4C

Answer: A



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30. Let a, b, c be given positive numbers, then values of x, y and $z \in \mathbb{R}^+$ which satisfies equations $x + y + z = a + b + c$ and $4xyz = -(a^2x + b^2y + c^2z) = abc$ are respectively.

A. $\frac{b+c}{2}, \frac{a+c}{2}, \frac{a+b}{2}$

B. $\frac{a}{2}, \frac{b}{2}, \frac{c}{2}$

C. $\frac{a+b}{2}, \frac{a+c}{2}, \frac{b+c}{2}$

D. None of these

Answer: A



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31. If ' t_1 ', ' t_2 ' and ' t_3 ' are the lengths of the tangents drawn from centre of x-circle to the circumcircle of the ΔABC , then $\frac{1}{t_1} + \frac{1}{t_2} + \frac{1}{t_3}$

is equal to

A. $\frac{abc}{a + b + c}$

B. $\frac{a + b + c}{abc}$

C. $\frac{a + b + c}{2abc}$

D. $\frac{2abc}{a + b + c}$

Answer: B



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32. In triangle ABC , $\angle A > \frac{\pi}{2}$. AA_1 and AA_2 are the median and altitude, respectively. If $\angle BAA_1 = \angle A_1AA_2 = \angle A_2AC$, then $\sin^3 \frac{A}{3} \cdot \cos \frac{A}{3}$ is equal to

A. $\frac{3a^3}{16b^2c}$

B. $\frac{3a^3}{64b^2c}$

C. $\frac{3a^2}{4b^2c}$

D. $\frac{3a^3}{12b^2c}$

Answer: D



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33. In an ambiguous case of solving a triangle when $a = \sqrt{5}$, $b = 2$, $\angle A = \frac{\pi}{6}$ and the two possible values of third side are c_1 and c_2 , then

A. $|c_1 - c_2| = 2\sqrt{6}$

B. $|c_1 - c_2| = 4\sqrt{6}$

C. $|c_1 - c_2| = 4$

D. $|c_1 - c_2| = 6$

Answer: C



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34. If R_1 is the circumradius of the pedal triangle of a given triangle ABC , and R_2 is the circumradius of the pedal triangle of the pedal triangle formed, and so on R_3, R_4 then the value of $\sum_{i=1}^{\infty} R_i$, where R (circumradius) of ABC is 5 is 8 (b) 10 (c) 12 (d) 15

A. 8

B. 10

C. 12

D. 15

Answer: B



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35. If in a triangle $\left(1 - \frac{r_1}{r_2}\right)\left(1 - \frac{r_1}{r_3}\right) = 2$ then the triangle is right angled (b) isosceles equilateral (d) none of these

- A. right angled
- B. isosceles
- C. equilateral
- D. None of these

Answer: A



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36. If the median AD of a triangle ABC makes an angle θ with side, AB, then $\sin(A - \theta)$ is equal to

- A. $\frac{b}{c} \sin \theta$
- B. $\frac{c}{b} \sin \theta$
- C. $\frac{c}{b} \cos \theta$

D. None of these

Answer: B

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37. In a ΔABC , angles A,B,C are in AP, then $\lim_{A \rightarrow C} \frac{\sqrt{3 - 4A \sin C}}{|A - C|}$ is

A. 1

B. 2

C. 3

D. 4

Answer: A

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38. In a triangle ABC , $(a + b + c)(b + c - a) = \lambda bc$ if

A. $\lambda < 0$

B. $\lambda > 6$

C. $0 < \lambda < 4$

D. $\lambda > 4$

Answer: C

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39. In the triangle ABC, if $(a^2 + b^2)\sin(A - B) = (a^2 - b^2)\sin(A + B)$, then the triangle is

A. either isosceles or right angled

B. only right angled

C. only isosceles triangle

D. None of the above

Answer: A

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40. In a ΔABC , sides a, b, c are in AP and $\frac{2}{1!9!} + \frac{2}{3!7!} + \frac{1}{5!5!} = \frac{8^a}{(2b)!}$, then the maximum value of $\tan A \tan B$ is equal to

A. $\frac{1}{2}$

B. $\frac{1}{3}$

C. $\frac{1}{4}$

D. $\frac{1}{5}$

Answer: B

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41. If a, b, c be the sides of a triangle ABC and if roots of equation $a(b - c)x^2 + b(c - a)x + c(a - b) = 90$ are equal then $\frac{\sin^2 A}{2}, \sin^2 B, \frac{\sin^2 C}{2}$ are in (A) A.P. (B) G.P. (C) H.P. (D) none of these

A. AP

B. GP

C. HP

D. AGP

Answer: C



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42. The ratio of the area of a regular polygon of n sides inscribed in a circle to that of the polygon of same number of sides circumscribing the same is 3:4. Then the value of n is 6 (b) 4 (c) 8 (d) 12

A. 6

B. 4

C. 8

D. 12

Answer: A



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43. In any triangle ABC $\sum \frac{\sin^2 A + \sin A + 1}{\sin A}$ is always greater than or equal

A. 9

B. 3

C. 27

D. None of these

Answer: C



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44. If the incircle of the triangle ABC, through it's circumcentre, then the $\cos A + \cos B + \cos C$ is

A. -2

B. $\sqrt{2}$

C. $-\sqrt{2}$

D. None of these

Answer: B



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45. The perimeter of a triangle ABC is six times the arithmetic mean of the sines of its angles. If the side a is 1 then find angle A .

A. 30°

B. 60°

C. 90°

D. 120°

Answer: A

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46. If there are only two linear functions f and g which map $[1, 2]$ on $[4, 6]$ and in a ΔABC , $c = f(1) + g(1)$ and a is the maximum value of r^2 , where r is the distance of a variable point on the curve $x^2 + y^2 - xy = 10$ from the origin, then $\sin A : \sin C$ is

A. 1 : 2

B. 2 : 1

C. 1 : 1

D. None of these

Answer: C

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47. A circle is inscribed in an equilateral triangle of side a . The area of any square inscribed in this circle is _____.

A. a^2

B. $\frac{a^2}{4}$

C. $\frac{a^2}{3}$

D. $\frac{a^2}{6}$

Answer: D



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48. In any triangle ABC, if $\sin A$, $\sin B$, $\sin C$ are in AP, then the maximum value of $\tan \frac{B}{2}$ is

A. $-\frac{1}{\sqrt{3}}$

B. $\frac{1}{\sqrt{3}}$

C. $\frac{1}{3}$

D. None of these

Answer: B

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49. In a $\triangle ABC$, $2 \cos A = \frac{\sin B}{\sin C}$ and $2^{\tan^2 B}$ is a solution of equation $x^2 - 9x + 8 = 0$, then $\triangle ABC$ is

- A. equilateral
- B. isosceles
- C. scalene
- D. right angled

Answer: A

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50. A triangle is inscribed in a circle. The vertices of the triangle divide the circle into three arcs of length 3, 4 and 5 units. Then area of the triangle is equal to:

A. $\frac{9\sqrt{3}(1 + \sqrt{3})}{\pi^2}$ unit

B. $\frac{3\sqrt{3}(\sqrt{3} - 1)}{\pi^2}$ sq unit

C. $\frac{9\sqrt{3}(1 + \sqrt{3})}{2\pi^2}$ sq unit

D. $\frac{9\sqrt{3}(\sqrt{3} - 1)}{2\pi^2}$ sq unit

Answer: A



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51. If a, b and c are the sides of a triangle such that $b \cdot c = \lambda^2$, then the relation is a, λ and A is

A. $c \geq 2\lambda \sin\left(\frac{C}{2}\right)$

B. $b \geq 2\lambda \sin\left(\frac{A}{2}\right)$

C. $a \geq 2\lambda \sin\left(\frac{A}{2}\right)$

D. None of these

Answer: C



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52. In a triangle ABC , AD is the altitude from A (Fig. 12.9). Given

$b > c$, $2C = 23^\circ$ and $AD = \frac{abc}{b^2 - c^2}$ then $\angle B$ is equal to

A. 110°

B. 113°

C. 120°

D. 130°

Answer: B



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53. In triangle ABC , $a = 5$, $b = 4$ and $\cos(A + B) = \frac{31}{32}$ In this triangle, $c =$

A. 3

B. 6

C. 7

D. 9

Answer: B



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54. In a ABC , if $AB = x$, $BC = x + 1$, $\angle C = \frac{\pi}{3}$, then the least integer value of x is 6 (b) 7 (c) 8 (d) none of these

A. 6

B. 7

C. 8

D. None of these

Answer: B

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55. In an equilateral triangle, three coins of radii 1 unit each are kept so that they touch each other and also the sides of the triangle. The area of the triangle ABC is

A. $(4 + 2\sqrt{3}) cm^2$

B. $\frac{1}{4}(12 + 7\sqrt{3}) cm^2$

C. $\frac{1}{4}(48 + 7\sqrt{3}) cm^2$

D. $(6 + 4\sqrt{3}) cm^2$

Answer: D

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56. The sides of a triangle are in AP. If the angles A and C are the greatest and smallest angle respectively, then $4(1 - \cos A)(1 - \cos C)$ is equal to

A. $\cos A - \cos C$

B. $\cos A \cos C$

C. $\cos A + \cos C$

D. $\cos C - \cos A$

Answer: C

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57. If in $\triangle ABC$, $c(a + b)\cos \frac{B}{2} = b(a + c)\cos \frac{C}{2}$, the triangle is

A. isosceles

B. equilateral

C. right angled but not isosceles

D. right angled and isosceles

Answer: A

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58. In a triangle ABC , the line joining the circumcentre and incentre is parallel to BC, then $\cos B + \cos C$ is equal to:

A. $\frac{3}{2}$

B. 1

C. $\frac{3}{4}$

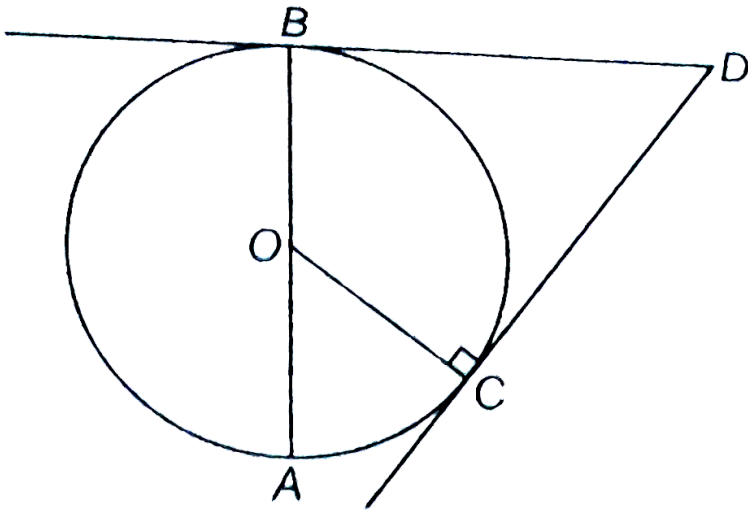
D. $\frac{1}{2}$

Answer: B



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59. In the given figure, AB is the diameter of the circle, centered at O. If $\angle COA = 60^\circ$, $AB = 2r$, $Ac = d$ and $CD = l$, then l is equal to



A. $d\sqrt{3}$

B. $\frac{d}{\sqrt{3}}$

C. $3d$

D. $\frac{\sqrt{3}d}{2}$

Answer: A



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60. If in a ΔABC , AD , BE and CF are the altitudes and R is the circumradius, then the radius of the circumcircle of ΔDEF is

A. $2R$

B. R

C. $\frac{R}{2}$

D. None of these

Answer: C



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61. In a right angled triangle ABC, the bisector of the right angle C divides AB into segment x and y and $\tan\left(\frac{A - B}{2}\right) = t$, then x:y is equal to

A. $(1 + t) = (1 - t)$

B. $(1 - t) : (t + 1)$

C. $1 : (1 + t)$

D. $(1 - t) : 1$

Answer: B



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62. A variable triangle ABC is circumscribed about a fixed circle of unit radius. Side BC always touches the circle at D and has fixed direction. If B and C vary in such a way that $(BD) \cdot (CD) = 2$, then locus of vertex A will be a straight line

A. parallel to side BC

B. right angle to side BC

C. making an angle $\frac{\pi}{6}$ with BC

D. making an angle $\sin^{-1}\left(\frac{2}{3}\right)$ with BC

Answer: A



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63. A tower of height b subtends an angle at a point O on the level of the foot of the tower and at a distance a from the foot of the tower. If a

pole mounted on the lower also subtends an equal angle at O , the height of the pole is

A. $b \left(\frac{a^2 - b^2}{a^2 + b^2} \right)$

B. $b \left(\frac{a^2 + b^2}{a^2 - b^2} \right)$

C. $a \left(\frac{a^2 - b^2}{a^2 + b^2} \right)$

D. $a \left(\frac{a^2 + b^2}{a^2 - b^2} \right)$

Answer: B



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64. A balloon is observed simultaneously from three points A , B and C on a straight road directly under it. The angular elevation at B is twice and at C is thrice that at A . If the distance between A and B is 200 metres and the distance between B and C is 100 metres, then find the height of balloon above the road.

A. 50 m

B. $50\sqrt{3}m$

C. $50\sqrt{2}m$

D. None of these

Answer: D



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65. A vertical pole (more than 100 m high) consists of two portions, the lower being one third of the whole. If the upper portion subtends an angle $\tan^{-1}\left(\frac{1}{2}\right)$ at a point in a horizontal plane through the foot of the pole and distance 40 ft from it, then the height of the pole is

A. 100 ft

B. 120 ft

C. 150 ft

D. None of these :

Answer: B



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Exercise (More Than One Correct Option Type Questions)

1. If the area of a triangle is given Δ and angle C is given and if the value of the side c opposite to angle C is minimum then

A. $a = \sqrt{\frac{2\Delta}{\sin C}}$

B. $b = \sqrt{\frac{2\Delta}{\sin C}}$

C. $a = \frac{4\Delta}{\sin C}$

D. $b = \frac{4\Delta}{\sin^2 C}$

Answer: A



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2. If Δ represents the area of acute angled triangle ABC, then

$$\sqrt{a^2b^2 - 4\Delta^2} + \sqrt{b^2c^2 - 4\Delta^2} + \sqrt{c^2a^2 - 4\Delta^2} = a^2 + b^2 + c^2 - \frac{a^2 + b^2 + c^2}{2}$$

$$ab \cos C + bc \cos A + ca \cos B - ab \sin C + bc \sin A + ca \sin B$$

A. $a^2 + b^2 + c^2$

B. $\frac{a^2 + b^2 + c^2}{2}$

C. $ab \cos C + bc \cos A + ca \cos B$

D. $ab \sin C + bc \sin A + ca \sin B$

Answer: C



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3. In ΔABC , the value of $c \cos(A - \theta) + a \cos(C + \theta) =$



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4. In $\triangle ABC$, If $ac = 3$, $bc = 4$ and $(A - B) = \frac{3}{4}$, then

A. measure of $\angle A$ is $\frac{\pi}{2}$

B. measure of $\angle B$ is $\frac{\pi}{2}$

C. $\cot \frac{C}{2} = \sqrt{7}$

D. circumradius of $\triangle ABC$ is $\frac{2}{7^{1/14}}$

Answer: B::C::D



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5. If in $\triangle ABC$, $a = 5$, $b = 4$ and $\cos(A - B) = \frac{31}{32}$, then

A. The perimeter of $\triangle ABC$ equals $\frac{15}{2}$

B. The radius of circle inscribed in $\triangle ABC$ equals $\frac{\sqrt{7}}{2}$

C. The measure of $\angle C$ equals $\cos^{-1} \frac{1}{8}$

D. The value of $R(b^2 \sin 2C + c^2 \sin 2B)$ equal 120

Answer: B::C::D



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6. In which of the following situations, it is possible to have $a\Delta ABC$?

(All symbols used have usual meaning in a triangle)

A. $(a + c - b)(a - c + b) = 4bc$

B. $b^2 \sin 2C + \cos^2 \sin 2B = ab$

C. $a = 3, b = 5, c = 7$ and $C = \frac{2\pi}{3}$

D. $\cos\left(\frac{A - C}{2}\right) = \cos\left(\frac{A + C}{2}\right)$

Answer: B::C



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7. In a triangle ABC, let $BC = 1, AC = 2$ and measure of angle C is 30° . Which of the following statement(s) is (are) correct? (A) $2 \sin A = \sin B$ (B) Length

of side AB equals $5 - 2\sqrt{3}$ (C) Measure of angle A is less than 30° (D)

Circumradius of triangle ABC is equal to length of side AB

A. $2 \sin A = \sin B$

B. Length of side AB equals $5 - 2\sqrt{3}$

C. measure of $\angle A$ is less than 30°

D. Circumradius of $\triangle ABC$ is equal to length of side AB

Answer: A::C::D



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8. 6. Let one angle of a triangle be 60° , the area of triangle is $\frac{10}{3}$ and perimeter is 20 cm. If $a > b > c$ where a, b and c denote lengths of sides opposite to vertices A, B and C respectively, then which of the following is (are) correct? (A) Inradius of triangle is 3 (C) (B) Length of longest side of triangle is 7 (D) Circum radius of triangle is 12 (D) Radius of largest escribed circle is 12

A. Inradius of triangle is $\sqrt{3}$

B. Length of longest side of triangle is 7

C. Circum-radius of triangles is $\frac{7}{\sqrt{3}}$

D. Radius of largest escribed circle is $\frac{1}{12}$

Answer: A:C



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9. In a triangle ABC, if $a = 4, b = 8, \angle C = 60^\circ$, then which of the following relations is (are) correct? [Note: All symbols used have usual meaning in triangle ABC.]

A. The area of $\triangle ABC$ is $8\sqrt{3}$

B. The value of $\sum \sin^2 A = 2$

C. Inradius of triangle ABC is $\frac{2\sqrt{3}}{3 + \sqrt{3}}$

D. The length of internal angle bisector of $\angle C$ is $\frac{4}{\sqrt{3}}$.

Answer: A::B



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10. Given an isosceles triangle with equal sides of length b , base angle $\alpha < \frac{\pi}{4}$ and R, r the radii and O, I the centres of the circumcircle and incircle, respectively. Then

A. $R = \frac{1}{2}b \cos \alpha$

B. $\Delta = 2b^2 \sin 2\alpha$

C. $r = \frac{b \sin 2\alpha}{2(1 + \cos \alpha)}$

D. $OI = \left| \frac{b \cos\left(\frac{3\alpha}{2}\right)}{2 \sin \alpha\left(\frac{\alpha}{2}\right)} \right|$

Answer: A::C::D



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11. There can exist a triangle ABC satisfying the conditions :

A. $\tan A + \tan B + \tan C = 0$

B. $\frac{\sin A}{2} = \frac{\sin B}{3} = \frac{\sin C}{7}$

C. $(a + b)^2 = c^2 + ab$ and $\sqrt{2}(\sin A + \cos A) = \sqrt{3}$

D.

$$\sin A + \sin B = \left(\frac{\sqrt{3} + 1}{2} \right) \cos A \cos B = \frac{\sqrt{3}}{4} = \frac{\sqrt{3}}{4} = \sin A \sin B$$

Answer: C::D



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12. Let a, b, c be the sides of triangle whose perimeter is P and area is A , then

A. $p^3 \leq 27(b + c - a)(c + a - b)(a + b - c)$

B. $p^2 \leq 3(a^2 + b^2 + c^2)$

C. $a^2 + b^2 + c^2 \geq 4\sqrt{3}A$

D. $p^4 \leq 25 < A$

Answer: B::C



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13. If in $\triangle ABC$, $A = 90^\circ$ and $c, \sin B$ and $\cos B$ are rational number, then

A. a is rational

B. a is irrational

C. b is rational

D. b is irrational

Answer: A::C



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14. In $\triangle ABC$, which of the following statements are true

A. maximum value of $\sin 2A + \sin 2B + \sin 2C$ is same as the maximum value of $\sin A + \sin B + \sin C$

B. $R \geq 2r$, where R is circumradius and r is inradius

C. $R^2 \geq \frac{abc}{(a + b + c)}$

D. $\triangle ABC$ is right angled if $r + 2R = s$, where s is semiperimeter

Answer: A::B::C::D



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15. Let ' l ' is the length of median from the vertex A to the side BC of a $\triangle ABC$. Then

A. $4l^2 = 2b^2 + 2c^2 - a^2$

B. $4l^2 = b^2 + c^2 + 2bc \cos A$

C. $4l^2 = b^2 + 4bc \cos A$

$$D. 4l^2 - (2s - a)^2 - 4bc \sin^2\left(\frac{A}{2}\right)$$

Answer: A::B::C::D



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16. If A , A_1 , A_2 and A_3 are the areas of the inscribed and escribed circles of a triangle, prove that $\frac{1}{\sqrt{A}} = \frac{1}{\sqrt{A_1}} + \frac{1}{\sqrt{A_2}} + \frac{1}{\sqrt{A_3}}$

A. $\sqrt{A_1} + \sqrt{A_2} + \sqrt{A_3} = \sqrt{\pi}(r_1 + r_2 + r_3)$

B. $\frac{1}{\sqrt{A_1}} + \frac{1}{\sqrt{A_2}} + \frac{1}{\sqrt{A_3}} = \frac{1}{\sqrt{A}}$

C. $\frac{1}{\sqrt{A_1}} + \frac{1}{\sqrt{A_2}} + \frac{1}{\sqrt{A_3}} = \frac{s^2}{\sqrt{\pi r_1 r_2 r_3}}$

D. $\sqrt{A_1} + \sqrt{A_2} + \sqrt{A_3} = \sqrt{\pi}(4R + r)$

Answer: A::B::C::D



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17. If a, b, A be given in a triangle and c_1 and c_2 be two possible value of the third side such that $c_1^2 + c_1c_2 + c_2^2 = a^2$, then A is equal to

A. 30°

B. 60°

C. 90°

D. 120°

Answer: B::C



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18. D, E and F are the middle points of the sides of the triangle ABC, then

A. centroid of the triangle DEF is the same as that of ABC

B. orthocentre of the triangle DEF is the circumcentre of ABC

C. orthocentre of the triangle DEF is the incentre of ABC

D. centroid of the triangle DEF is not the same as that of ABC

Answer: A::B



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19. The sides of ABC satisfy the equation $2a^2 + 4b^2 + c^2 = 4ab + 2a \cdot$

Then the triangle is isosceles the triangle is obtuse $B = \cos^{-1}\left(\frac{7}{8}\right)$

$$A = \cos^{-1}\left(\frac{1}{4}\right)$$

A. the triangle is isosceles

B. the triangle is obtuse

C. $B = \cos^{-1}\left(\frac{7}{8}\right)$

D. $A = \cos^{-1}\left(\frac{1}{4}\right)$

Answer: A::C::D



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20. If Δ represents the area of acute angled triangle ABC, then

$$\sqrt{a^2b^2 - 4\Delta^2} + \sqrt{b^2c^2 - 4\Delta^2} + \sqrt{c^2a^2 - 4\Delta^2} = a^2 + b^2 + c^2 - \frac{a^2 + b^2 + c^2}{2}$$

$$ab \cos C + bc \cos A + ca \cos B = ab \sin C + bc \sin A + ca \sin B$$

A. $(a^2 + b^2 + c^2)$

B. $\frac{a^2 + b^2 + c^2}{2}$

C. $ab \cos C + bc \cos A + ca \cos B$

D. $ab \sin C + bc \sin A + ca \sin B$

Answer: B::C



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21. In triangle, ABC if $2a^2b^2 + 2b^2c^2 = a^2 + b^4 + c^4$, then angle B is equal to 45° (b) 135° 120° (d) 60°

A. 45°

B. 135°

C. 120°

D. 60°

Answer: A::B



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22. If H is the orthocentre of the triangle ABC, R = circumradius and

$P = AH + BH + CH$, then

A. $p = 2(R + r)$

B. max, of P is 3R

C. min. of P is 3R

D. $P = 2(R - r)$

Answer: A::B



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23. If inside a big circle exactly $n(n \leq 3)$ small circles, each of radius r , can be drawn in such a way that each small circle touches the big circle and also touches both its adjacent small circles, then the radius of big circle is $r \left(1 + \cos ec \frac{\pi}{n}\right)$ (b) $\left(\frac{1 + \frac{\tan \pi}{n}}{\frac{\cos \pi}{\pi}}\right) r \left[1 + \cos ec \frac{2\pi}{n}\right]$ (d)

$$\frac{r \left[s \in \frac{\pi}{2n} + \frac{\cos(2\pi)}{n} \right]^2}{\frac{\sin \pi}{n}}$$

A. $r \left(1 + \cos ec \frac{\pi}{n}\right)$

B. $\left(\frac{1 + \tan \frac{\pi}{n}}{\cos \frac{\pi}{n}}\right)$

C. $r \left[1 + \cos ec \frac{2\pi}{n}\right]$

D. $\frac{r \left[\sin \frac{\pi}{2n} + \cos \frac{2\pi}{n} \right]^2}{\sin \frac{\pi}{n}}$

Answer: A:D



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24. If in triangle ABC, a, c and angle A are given and $c \sin A < a < c$, then

(b_1 and b_2 are values of b)

A. $b_1 + b_2 = 2c \cos A$

B. $b_1 + b_2 = c \cos A$

C. $b_1 b_2 = c^2 - a^2$

D. $b_1 b_2 = c^2 + a^2$

Answer: A:C

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Exercise (Statement I And II Type Questions)

1. In a triangle ABC , $a^3 + b^3 + c^3 = c^2(a + b + c)$ (All symbol used have usual meaning in a triangle.) Statement-1: The value of $\angle C = 60^\circ$.

Statement-2: $\triangle ABC$ must be equilateral.

A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I

- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: C

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2. In a triangle ABC, let $a = 6$, $b = 3$ and $\cos(A - B) = \frac{4}{5}$ [Note: All symbols used have usual meaning in a triangle.] Statement 1: $\angle B = \frac{\pi}{2}$
Statement 2: $\sin A = \frac{2}{\sqrt{5}}$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement I is correct but Statement I is incorrect

Answer: D



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3. Statement I If in a triangle ABC $\sin^2 A + \sin^2 B + \sin^2 C = 2$, then one of the angle must be 90° . Statement II In any triangles ABC $\cos 2A + \cos 2B + \cos 2C = -1 - 4 \cos A \cos B \cos C$

A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I

B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement I is correct but Statement I is incorrect

Answer: A



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4. Statement I if A, B, C, D are angles of a cyclic quadrilateral then

$$\sum \sin A = 0.$$

Statement II If A, B, C, D are angles of cyclic quadrilateral then,

$$\sum \cos A = 0.$$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement II is correct but Statement I is incorrect

Answer: D



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5. Statement I In any triangle ABC, the square of the length of the bisector AD is $bc \left(1 - \frac{a^2}{(b+c)^2} \right)$.

Statement II In any triangle ABC length of bisector AD is $\frac{2bc}{(b+c)} \cos \left(\frac{A}{2} \right)$.

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: A



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6. Statement I If I is incentre of $\triangle ABC$ and I_1 excentre opposite to A and P is intersection of II_1 and BC , then $IP \cdot I_1P = BP \cdot PC$

Statement II In a $\triangle ABC$, I is incentre and I_2 is excentre opposite to A , then BI, I_1, C must be square.

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: C



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7. All the notations used in statement I and statement II are usual.

Statement I In triangle ABC, if $\frac{\cos A}{a} = \frac{\cos B}{b} = \frac{\cos C}{c}$. then value of $\frac{r_1 + r_2 + r_3}{r}$ is equal to 9.

Statement II If ΔABC : $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = 2R$, where R is circumradius.

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: A



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8. Statement I In a triangle ABC if $\tan A : \tan B : \tan C = 1 : 2 : 3$, then $A = 45^\circ$

Statement II If $p, q, r = 1 : 2 : 3$, then $p = 1$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: C



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9. Statement I In any right angled triangle $\frac{a^2 + b^2 + c^2}{R^2}$ is always equal to 8.

Statement II $a^2 = b^2 + c^2$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: A



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10. Statement I perimeter of a regular pentagon inscribed in a circle with centre O and radius a cm equals $10a \sin 36^\circ$ cm.

Statement II Perimeter of a regular polygon inscribed in a circle with centre O and radius a cm equals $(3n - 5) \sin \left(\frac{360^\circ}{2n} \right) cm$, then it is n sided, where $n \geq 3$.

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: C



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11. Statement I In any triangle ABC

$$a \cos A + b \cos B + c \cos C \leq s.$$

Statement II In any triangle ABC

$$\sin\left(\frac{A}{2}\right)\sin\left(\frac{B}{2}\right)\sin\left(\frac{C}{2}\right) \leq \frac{1}{8}$$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I

- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: A

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12. Statement I In a ΔABC , if $\cos^2 \frac{A}{2} + \cos^2 \frac{B}{2} + \cos^2 \frac{C}{2} = y \left(x^2 + \frac{1}{x^2} \right)$ then the maximum value of y is $\frac{9}{8}$.

Statement II In a ΔABC , $\sin \frac{A}{2} \cdot \sin \frac{B}{2} \cdot \sin \frac{C}{2} \leq \frac{1}{8}$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement I is correct but Statement I is incorrect

Answer: A



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13. Statement I In any triangle

$$a \cos A + b \cos B + c \cos C \leq s$$

Statement II In any triangle $\sin\left(\frac{A}{2}\right)\sin\left(\frac{B}{2}\right)\sin\left(\frac{C}{2}\right) \leq \frac{1}{8}$

A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I

B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement I is correct but Statement I is incorrect

Answer: A



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14. Statement I In triangle ABC , $\frac{a^2 + b^2 + c^2}{\Delta} \geq 4\sqrt{3}$

Statement II If $a_i > 0, i = 1, 2, 3, \dots, n$ which are not

$$\frac{a_1^m + a_2^m + \dots + a_n^m}{n} > \left(\frac{a_1 + a_2 + \dots + a_n}{n} \right)^m, \text{ if } m < 0 \text{ or } m > 1$$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: A



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15. Statement I AA_1, BB_1, CC_1 are the medians of triangle ABC whose centroid is G . If the points A, C_1, G and B are concyclic, then c^2, a^2, b^2 are in AP.

Statement II $BG \cdot CC_1 = BC_1 \cdot BA$

- A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement I is correct but Statement I is incorrect

Answer: B



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Exercise (Passage Based Questions)

1. R is circumradius of $\triangle ABC$, H is orthocentre, R_1, R_2, R_3 are circumradii of $\triangle AHB, \triangle BHC$. If AH produced meet the circumradii of ABC at M and intersect BC at L ,

$$\angle AHB = 180^\circ - C$$

$$\frac{c}{\sin(180^\circ - C)} = 2R_1$$

$$\frac{c}{\sin C} = 2R_1$$

$$R_1 = R$$

$R_1R_2 + R_2R_3 + R_1R_3$ is equal to

A. $2R^2$

B. $3R^2$

C. $5R^2$

D. R^2

Answer: B



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2. R is circumradius of $\triangle ABC$, H is orthocentre, R_1, R_2, R_3 are circumradii of $\triangle AHB, \triangle BHC$. If AH produced meet the circumradii of ABC at M and intersect BC at L ,

$$\angle AHB = 180^\circ - C$$

$$\frac{c}{\sin(180^\circ - C)} = 2R_1$$

$$\frac{c}{\sin C} = 2R_1$$

$$R_1 = R$$

Area of $\triangle AHB$

- A. $2R \cos A \cos B \cos C$
- B. $R^2 \cos A \cos B \cos C$
- C. $2R^2 \cos A \cos B \cos C$
- D. None of the above

Answer: C



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3. R is circumradius of $\triangle ABC$, H is orthocentre, R_1, R_2, R_3 are circumradii of $\triangle AHB, \triangle BHC$. If AH produced meet the circumradius of ABC at M and intersect BC at L ,

$$\angle AHB = 180^\circ - C$$

$$\frac{c}{\sin(180^\circ - C)} = 2R_1$$

$$\frac{c}{\sin C} = 2R_1$$

$$R_1 = R$$

Ratio of area of $\triangle AHB$ to $\triangle BML$, is

A. $\cos B : 2 \cos A$

B. $2 : 1$

C. $\cos A : \cos B \cos C$

D. None of these

Answer: C



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4. Let ABC to be an acute triangle with $BC = a$, $CA = b$ and $AB = c$, where $a \neq b \neq c$. From any point 'p' inside $\triangle ABC$, E, F denote foot of perpendiculars from 'p' onto the sides, BC, CA and AB , respectively. Now, answer the following questions.

All positions of point 'p' for which $\triangle BEF$ is isosceles lie on

- A. the incircle of $\triangle ABC$
- B. line of internal angle bisectors from A, B and C
- C. arcs of 3 circles
- D. None of the above

Answer: C



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5. Let ABC to be an acute triangle with $BC = a$, $CA = b$ and $AB = c$, where $a \neq b \neq c$. From any point 'p' inside $\triangle ABC$, E, F denote foot of perpendiculars from 'p' onto the sides, BC, CA and AB , respectively.

Now, answer the following equations.

Let $(A(7, 0), B(4, 4)$ and $C(0, 0)$ and $\triangle DEF$ is isosceles with $DE = DF$. Then, the curve on which 'P' may lie

A. $x = 4$ or $x + yy = 7$ or $4x = 3y$

B. $x = 4$ or $x^2 + y^2 = 4x + 4y$

C. $3(x^2 + y^2) + 196 = 49(x + y)$

D. None of the above

Answer: C



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6. Let ABC to be an acute triangle with $BC = a, CA = b$ and $AB = c$, where $a \neq b \neq c$. From any point 'p' inside $\triangle ABC$ $\leq tB, E, F$ denot foot of perpendiculars form 'p' noto the sides, BC, CA and AB, respectively.

Now, answer the following equations.

If $\triangle DEF$ is equilateral, then 'P'

- A. coincides with incentre of $\triangle ABC$
- B. coincides with orthocentre of $\triangle ABC$
- C. lies on pedal \triangle of $\triangle ABC$
- D. None of the above

Answer: D

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7. In an acute angled triangle ABC , let AD , BE and CF be the perpendicular opposite sides of the triangle. The ratio of the product of the side lengths of the triangles DEF and ABC , is equal to

A. $\frac{3(abc)^{\frac{1}{3}}}{4(a+b+c)}$

B. $\frac{1}{4}$

C. $\cos A \cos B \cos C$

D. $\sin\left(\frac{A}{2}\right)\sin\left(\frac{B}{2}\right)\sin\left(\frac{C}{2}\right)$

Answer: C



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8. In an acute angle $\triangle ABC$, let AD, BE and CF be the perpendicular from A, B and C upon the opposite sides of the triangle. (All symbols used have usual meaning in a triangle.)

The orthocentre of the $\triangle ABC$, is the

- A. centroid of the $\triangle DEF$
- B. circum-centre of the $\triangle DEF$
- C. incentre of the $\triangle DEF$
- D. orthocentre of the $\triangle DEF$

Answer: C



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9. In an acute angle $\triangle ABC$, let AD, BE and CF be the perpendicular from A, B and C upon the opposite sides of the triangle. (All symbols used have usual meaning in a triangle.)

The circum-radius of the $\triangle DEF$ can be equal to

A. $\frac{abc}{8\Delta}$

B. $\frac{a}{4\sin A}$

C. $\frac{R}{2}$

D. $\frac{r}{8} \cos ec \frac{A}{2} \cos ec \frac{B}{2} \cos ec \frac{C}{2}$

Answer: A::B::C::D



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10. Let a, b, c are the sides opposite to angles A, B, C respectively in a

$$\triangle ABC \tan \frac{A - B}{2} = \frac{a - b}{a + b} \cot \frac{C}{2} \text{ and } \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C},$$

If $a = 6, b = 3$ and $\cos(A - B) = \frac{4}{5}$

Angle C is equal to

A. $\frac{\pi}{4}$

B. $\frac{\pi}{2}$

C. $\frac{3\pi}{4}$

D. $\frac{2\pi}{3}$

Answer: B

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11. Let a, b, c are the sides opposite to angles A, B, C respectively in a

$$\Delta ABC \tan \frac{A - B}{2} = \frac{a - b}{a + b} \cot \frac{C}{2} \text{ and } \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C},$$

$$\text{If } a = 6, b = 3 \text{ and } \cos(A - B) = \frac{4}{5}$$

Area of the triangle is equal to

A. 8

B. 9

C. 10

D. 11

Answer: B



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12. Let a, b, c are the sides opposite to angles A, B, C respectively in a

$$\Delta ABC \tan \frac{A - B}{2} = \frac{a - b}{a + b} \cot \frac{C}{2} \text{ and } \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C},$$

$$\text{If } a = 6, b = 3 \text{ and } \cos(A - B) = \frac{4}{5}$$

Value of $\sin A$ is equal to

A. $\frac{1}{\sqrt{5}}$

B. $\frac{2}{\sqrt{5}}$

C. $\frac{1}{2\sqrt{5}}$

D. $\frac{1}{\sqrt{3}}$

Answer: B



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13. When any two sides and one of the opposite acute angle are given, under certain additional conditions two triangles are possible. The case when two triangles are possible is called the ambiguous case.

In fact when any two sides and the angle opposite to one of them are given either no triangle is possible or only one triangle is possible or two triangles are possible.

In the ambiguous case, let a, b and $\angle A$ are given and c_1, c_2 are two values of the third side c .

On the basis of above information, answer the following questions

Two different triangles are possible when

A. $b \sin A < a$

B. $b \sin A < a$ and $b > a$

C. $b \sin A < a$ and $b < a$

D. $b \sin A < a$ and $a = b$

Answer: B



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14. When any two sides and one of the opposite acute angle are given, under certain additional conditions two triangles are possible. The case when two triangles are possible is called the ambiguous case.

In fact when any two sides and the angle opposite to one of them are given either no triangle is possible or only one triangle is possible or two triangles are possible.

In the ambiguous case, let a, b and $\angle A$ are given and c_1, c_2 are two values of the third side c .

On the basis of above information, answer the following questions

The difference between two values of c is

A. $2\sqrt{(a^2 - b^2)}$

B. $\sqrt{(a^2 - b^2)}$

C. $2\sqrt{(a^2 - b^2 \sin^2 A)}$

D. $\sqrt{(a^2 - b^2 \sin^2 A)}$

Answer: B



15. When any two sides and one of the opposite acute angle are given, under certain additional conditions two triangles are possible. The case when two triangles are possible is called the ambiguous case.

In fact when any two sides and the angle opposite to one of them are given either no triangle is possible or only one triangle is possible or two triangles are possible.

In the ambiguous case, let a, b and $\angle A$ are given and c_1, c_2 are two values of the third side c .

On the basis of above information, answer the following questions

The value of $c_1^2 - 2c_1c_2 \cos 2A + c_2^2$ is

A. $4a \cos A$

B. $4a^2 \cos A$

C. $4a \cos^2 A$

D. $4a^2 \cos A$

Answer: D



16. When any two sides and one of the opposite acute angle are given, under certain additional conditions two triangles are possible. The case when two triangles are possible is called the ambiguous case.

In fact when any two sides and the angle opposite to one of them are given either no triangle is possible or only one triangle is possible or two triangles are possible.

In the ambiguous case, let a, b and $\angle A$ are given and c_1, c_2 are two values of the third side c .

On the basis of above information, answer the following questions

If $\angle A = 45^\circ$ and in ambiguous case (a, b, A are given) c_1, c_2 are two values of c and if θ be the angle between the two positions of the ambiguous side c then $\cos \theta$ is

A. $\frac{c_1 c_2}{c_1^2 + c_2^2}$

B. $\frac{2c_1 c_2}{c_1^2 + c_2^2}$

C. $\frac{\sqrt{c_1 c_2}}{(c_1 + c_2)}$

$$D. \frac{2\sqrt{c_1 c_2}}{(c_1 + c_2)}$$

Answer: B



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17. When any two sides and one of the opposite acute angle are given, under certain additional conditions two triangles are possible. The case when two triangles are possible is called the ambiguous case.

In fact when any two sides and the angle opposite to one of them are given either no triangle is possible or only one triangle is possible or two triangles are possible.

In the ambiguous case, let a, b and $\angle A$ are given and c_1, c_2 are two values of the third side c .

On the basis of above information, answer the following questions

If

$$2b = (m + 1)a \text{ and } \cos A = \frac{1}{2} \sqrt{\left(\frac{(m + 1)(m + 3)}{m}\right)}, \text{ where } 1 < m < 3, \text{ then}$$

is

A. m or $\frac{1}{m}$

B. $(m - 1)$ or $\frac{1}{(m + 3)}$

C. $(m + 1)$ or $\frac{1}{(m + 1)}$

D. $(m + 3)$ or $\frac{1}{(m + 3)}$

Answer: A



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18. Consider a triangle ABC, where c, y, z are the length of perpendicular drawn from the vertices of the triangle to the opposite sides a, b, c respectively. Let the letters R, r, S, Δ denote the circumradius, inradius semi-perimeter and area of the triangle respectively.

If $\frac{bx}{c} + \frac{cy}{a} + \frac{az}{b} = \frac{a^2 + b^2 + c^2}{k}$, then the value of k is

A. R

B. S

C. $2R$

D. $\frac{3}{2}R$

Answer: C



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19. Consider a triangle ABC, where x, y, z are the length of perpendicular drawn from the vertices of the triangle to the opposite sides a, b, c respectively. Let the letters R, r, S, Δ denote the circumradius, inradius, semi-perimeter and area of the triangle respectively.

If $\cot A + \cot B + \cot C = k \left(\frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} \right)$, then the value of k is

A. R^2

B. rR

C. Δ

D. $a^2 + b^2 + c^2$

Answer: C



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20. Consider a triangle ABC, where x, y, z are the length of perpendicular drawn from the vertices of the triangle to the opposite sides a, b, c respectively. Let the letters R, r, S, Δ denote the circumradius, inradius, semi-perimeter and area of the triangle respectively.

The value of $\frac{c \sin B + b \sin C}{x} + \frac{a \sin C + c \sin A}{y} + \frac{b \sin A + a \sin B}{z}$

is equal to

A. $\frac{R}{r}$

B. $\frac{S}{R}$

C. 2

D. 6

Answer: D



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21. AL, BM and CN are perpendicular from angular points of a triangle ABC on the opposite sides BC, CA and AB respectively. Δ is the area of triangle ABC, (r) and R are the inradius and circumradius.

If perimeters of ΔLMN and ΔABC are λ and μ , then the value of $\frac{\lambda}{\mu}$ is

A. $\frac{r}{R}$

B. $\frac{R}{r}$

C. $\frac{rR}{\Delta}$

D. $\frac{\Delta}{rR}$

Answer: B



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22. AL, BM and CN are perpendicular from angular points of a triangle ABC on the opposite sides BC, CA and AB respectively. Δ is the area of triangle ABC, (r) and R are the inradius and circumradius.

If areas of Δ 's AMN, BNL and CLM are Δ_1 , Δ_2 and Δ_3 respectively, then the value of $\Delta_1 + \Delta_2 + \Delta_3$ is

A. $\Delta(2 + 2 \cos A \cos B \cos C)$

B. $\Delta(2 + 2 \sin A \sin B \sin C)$

C. $\Delta(1 - 2 \cos A \cos B \cos C)$

D. $\Delta(1 - 2 \sin A \sin B \sin C)$

Answer: C

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23. AL, BM and CN are perpendicular from angular points of a triangle ABC on the opposite sides BC, CA and AB respectively. Δ is the area of triangle ABC, (r) and R are the inradius and circumradius.

If area of ΔLMN is Δ' , then the value of $\frac{\Delta'}{\Delta}$ is

A. $2 \sin A \sin B \sin C$

B. $2 \cos A \cos B \cos C$

C. $\sin A \sin B \sin C$

D. $\cos A \cos B \cos C$

Answer: D



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24. AL, BM and CN are perpendicular from angular points of a triangle ABC on the opposite sides BC, CA and AB respectively. Δ is the area of triangle ABC, (r) and R are the inradius and circumradius.

Radius of the circum circle of ΔLMN is

A. $2R$

B. R

C. $\frac{R}{2}$

D. $\frac{R}{4}$

Answer: B



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25. AL, BM and CN are perpendicular from angular points of a triangle ABC on the opposite sides BC, CA and AB respectively. Δ is the area of triangle ABC, (r) and R are the inradius and circumradius.

If radius of the incircle of ΔLMN is r' , then the value of $r' \sec A \sec B \sec C$ is

A. $4R$

B. $3R$

C. $2R$

D. R

Answer: A

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1. If in ΔABC , $\angle C = \frac{\pi}{8}$, $a = \sqrt{2}$ and $b = \sqrt{2 + \sqrt{2}}$ then find the measure of angle A (in degree).

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2. If in ABC , $A = \frac{\pi}{7}$, $B = \frac{2\pi}{7}$, $C = \frac{4\pi}{7}$ then $a^2 + b^2 + c^2$ must be R^2
 (b) $3R^2$ (c) $4R^2$ (d) $7R^2$

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3. If A, B, C the angles of an acute angled

$$\Delta ABC \text{ and } D = \begin{vmatrix} (\tan B + \tan C)^2 & \tan^2 A & \tan^2 A \\ \tan^2 B & (\tan A + \tan C)^2 & \tan^2 A \\ \tan^2 C & \tan^2 C & (\tan A + \tan B)^2 \end{vmatrix},$$

then the least integral values of $\frac{D}{1000}$ is

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4. In a $\triangle ABC$ and P and Q are the mid-point of AB and AC , respectively. If O is the circumcentre of the $\triangle ABC$, then the value of $\left(\frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle OPQ}\right) \cot B \cot C$ equal to

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5. With usual notation in $\triangle ABC$, the numerical value of

$$\left(\frac{a+b+c}{r_1+r_2+r_3}\right) \left(\frac{a}{r_1} + \frac{b}{r_2} + \frac{c}{r_3}\right) \text{ is}$$

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6. D is midpoint of BC in $\triangle ABC$ such that AD and AC are perpendicular,

$$\text{Show that } \cos A \cos C = \frac{2(c^2 - a^2)}{3ac}$$

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7. In a triangle ABC , medians AD and CE are drawn. If $AD = 5$, $\angle DAC = \frac{\pi}{8}$ and $\angle ACE = \frac{\pi}{4}$ then the area of the triangle ABC is equal to $\frac{5a}{b}$, then $a + b$ is equal to

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8. In ΔABC , $\frac{r}{r_1} = \frac{1}{2}$, then the value of $16 \left(\sum \tan \left(\frac{A}{2} \right) \right)$ must be.

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9. In a ΔABC , the maximum value of $120 \left(\frac{\sum a \cos^2 \left(\frac{A}{2} \right)}{a + b + c} \right)$ must be

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10. The sides of a triangle are three consecutive natural numbers and its largest angle is twice the smallest one. Determine the sides of the

triangle.

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11. In $\triangle ABC$, $\angle C = 2\angle A$, and $AC = 2BC$, then the value of $\frac{a^2 + b^2 c^2}{R^2}$ (where R is circumradius of triangle) is _____

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12. If a, b and A are given in a triangle and c_1, c_2 are possible values of the third side, then prove that $c_1^2 + c_2^2 - 2c_1c_2 \cos 2A = 4a^2 \cos^2 A$

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13. In triangle ABC, $a = 5, b = 4, c = 3$. G is the centroid of triangle. If R_1 be the circumradius of triangle GAB then the value of $\frac{a}{65} R_1^2$ must be

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14. A triangle ABC is inscribed in a circle with centre at O , The lines AO , BO and CO meet the opposite sides at D , E , and F , respectively.

Prove that
$$\frac{1}{AD} + \frac{1}{BE} + \frac{1}{CF} = \frac{a \cos A + b \cos B + c \cos C}{bc}$$



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15. In $\triangle ABC$, $a \geq b \geq c$ and if $\frac{a^3 + b^2 + c^2}{\sin^3 A \sin^3 B + \sin^3 C} = 8$, that the maximum value of a is



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16. In a cyclic quadrilateral $PQRS$, $PQ=2$ units, $QR=5$ units, $RS=3$ units and $\angle PQR = 60^\circ$, then what is the measure of SP ?



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Exercise (Subjective Type Questions)

1. In a ΔABC , the angles A and B are two values of θ satisfying $\sqrt{3} \cos \theta + \sin \theta = k$, where $|K| < 2$, then show triangle is obtuse angled.

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2. In an obtuse angled triangle, the obtuse angle is $\frac{3\pi}{4}$ and the other two angles are equal to two values of θ satisfying $a \tan \theta + b \sec \theta = c$, where $|b| \leq \sqrt{a^2 + c^2}$, then $a^2 - c^2$ is equal to

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3. In a δABC , a, c, A are given and b_1, b_2 are two values of third side b such that $b_2 = 2b_1$. Then, the value of $\sin A$.

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4. If P is a point on the altitude AD of the $\triangle ABC$, such that $\angle CBP = \frac{B}{3}$, then find the value of AP.

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5. If R denotes circumradius, then in $\triangle ABC$, $\frac{b^2 - c^2}{2aR}$ is equal to

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6. In $\triangle ABC$, $A = \frac{2\pi}{3}$, $b - c = 3\sqrt{3}$ cm and $\text{are}(\triangle ABC) = \frac{9\sqrt{3}}{2} \text{cm}^2$.

Solve for side a.

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7. If $\Delta = a^2 - (b - c)^2$, Δ is the area of the $\triangle ABC$ then $\tan A = ?$

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8. In a $\triangle ABC$, $B = 90^\circ$, $AC = h$ and the length of perpendicular from B to AC is p such that $h = 4p$. If $AB < BC$, then measure $\angle C$.

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9. If in a $\triangle ABC$, $\sin^3 A + \sin^3 B + \sin^3 C$

$= 3 \sin A \cdot \sin B \cdot \sin C$, then find the value of determinant

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}.$$

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10. In a $\triangle ABC$, the side a , b , and c are such that they are roots of

$x^3 - 11x^2 + 38x - 40 = 0$. Then the value of

$$\frac{\cos A}{a} + \frac{\cos B}{b} + \frac{\cos C}{c}.$$

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11. If the sides a, b, c are in A.P., prove that

$$(\tan) \frac{A}{2} + (\tan) \frac{C}{2} = \frac{2}{3} (\cot) \frac{B}{2}.$$

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12. The side of a Δ are in AP. And its area is $\frac{3}{5} \times$ (area of an equilateral triangle of the same perimeter). Find the ratio of its sides.

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13. If AD, BE and CF are the medians of a ΔABC , then evaluate

$$(AD^2 + BE^2 + CF^2) : (BC^2 + CA^2 + AB^2).$$

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14. AD is a median of the ΔABC . If AE are medians of the ΔABD and ΔADC respectively, and

$AD = m_1, AE = m_2, AF = m_3$, then find the value of $\frac{a^2}{8}$.



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15. In ΔABC , If
 $x = \tan\left(\frac{B-C}{2}\right)\tan\left(\frac{A}{2}\right), y = \tan\left(\frac{C-A}{2}\right)\tan\left(\frac{B}{2}\right), z = \tan\left(\frac{A-B}{2}\right)\tan\left(\frac{C}{2}\right)$
, then $x + y + z$ (in terms of x, y, z only) is



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16. In the given figure ΔABC is equilateral on side AB produced. We choose a point P such that A lies between P and B . We now denote 'a' as the length of sides of ΔABC , r_1 as the radius of incircle ΔPAC and r_2 as the ex-radius of ΔPBC with respect to side BC . Then $r_1 + r_2$ is equal to



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17. The base of a triangle is divided into three equal parts. If $\theta_1, \theta_2, \theta_3$ be the angles subtended by these parts at the vertex, then prove that

$$(\cot \theta_1 + \cot \theta_2)(\cot \theta_2 + \cot \theta_3) = 4 \cos^2 \theta_2$$

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18. If the circumradius of a triangle is $\frac{54}{\sqrt{1463}}$ and the sides are in G.P with common ratio $\frac{3}{2}$. then find the sides of the triangle.

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19. If the angle at the vertex of an isosceles triangle having the maximum area for the given length of the median to one of its equal sides, is x then $5 \cos x$ is equal to

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20. In an acute angle triangle ABC, AD, BE and CF are the altitudes, then

$$\frac{EF}{a} + \frac{FD}{b} + \frac{DE}{c} \text{ is equal to -}$$

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21. Let P be the point inside that $\triangle ABC$. Such that

$\angle APB = \angle BPC = \angle CPA$. Prove that

$$PA + PB + PC = \sqrt{\frac{a^2 + b^2 + c^2}{2}} + 2\sqrt{3}\Delta, \text{ where } a, b, c \Delta \text{ are the}$$

sides and the area of $\triangle ABC$.

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Exercise (Questions Asked In Previous 13 Years Exam)

1. In a triangle XYZ, let x, y, z be the lengths of sides opposite to the

angles X, Y, Z, respectively, and $2s = x + y + z$. If $\frac{s-x}{4} = \frac{s-y}{3} = \frac{s-z}{2}$

of incircle of the triangle XYZ is $\frac{8\pi}{3}$

A. area of the ΔXYZ is $6\sqrt{6}$

B. the radius of circum-circle of the ΔXYZ is $\frac{35}{6}\sqrt{6}$

C. $\sin \frac{X}{2} \sin \frac{Y}{2} \sin \frac{Z}{2} = \frac{4}{35}$

D. $\sin^2 \left(\frac{X+Y}{2} \right) = \frac{3}{5}$

Answer: A::C::D



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2. In a triangle the sum of two sides is x and the product of the same is y .

If $x^2 - c^2 = y$ where c is the third side. Determine the ration of the in-radius and circum-radius

A. $\frac{3y}{2x(x+c)}$

B. $\frac{3y}{2c(x+c)}$

C. $\frac{3y}{4x(x+c)}$

D. $\frac{3y}{4c(x+c)}$

Answer: B



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3. Consider a triangle ABC and let a, b and c denote the lengths of the sides opposite to vertices A, B , and C , respectively. Suppose $a = 6, b = 10$, and the area of triangle is $15\sqrt{3}$. If $\angle ACB$ is obtuse and if r denotes the radius of the incircle of the triangle, then the value of r^2 is



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4. In a triangle PQR , P is the largest angle and $\cos P = \frac{1}{3}$. Further the incircle of the triangle touches the sides PQ, QR and RP at N, L and M respectively, such that the lengths of PN, QL and RM are consecutive even integers. Then possible length(s) of the side(s) of the triangle is (are)

A. 16

B. 18

C. 20

D. 22

Answer: A::B



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5. Let PQR be a triangle of area Δ with $a = 2$, $b = \frac{7}{2}$ and $c = \frac{5}{2}$, where a , b and c are the lengths of the sides of the triangle opposite to the angles at P , Q and R respectively. Then $\frac{2 \sin P - \sin 2P}{2 \sin P + \sin 2P}$ equals

A. $\frac{3}{4\Delta}$

B. $\frac{45}{4\Delta}$

C. $\left(\frac{3}{4\Delta}\right)^2$

D. $\left(\frac{45}{4\Delta}\right)^5$

Answer: B::C::D



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6. If the angle A, B and C of a triangle are in an arithmetic progression and if a, b and c denote the lengths of the sides opposite to A, B and C respectively, then the value of the expression $\frac{a}{c} \sin 2C + \frac{c}{a} \sin 2A$ is $\frac{1}{2}$

(b) $\frac{\sqrt{3}}{2}$ (c) 1 (d) $\sqrt{3}$

A. $\frac{1}{2}$

B. $\frac{\sqrt{3}}{2}$

C. 1

D. $\sqrt{3}$

Answer: D



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7. Let ABC be a triangle such that $\angle ACB = \frac{\pi}{6}$ and let a, b and c denote the lengths of the side opposite to A, B , and C respectively. The value(s)

of x for which $a = x^2 + x + 1$, $b = x^2 - 1$, and $c = 2x + 1$ is (are)

– $(2 + \sqrt{3})$ (b) $1 + \sqrt{3}$ (c) $2 + \sqrt{3}$ (d) $4\sqrt{3}$

A. $-(2 + \sqrt{3})$

B. $1 + \sqrt{3}$

C. $2 + \sqrt{3}$

D. $4\sqrt{3}$

Answer: B



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8. a triangle ABC with fixed base BC , the vertex A moves such that

$\cos B + \cos C = 4 \frac{\sin^2 A}{2}$. If a, b and c , denote the length of the sides of

the triangle opposite to the angles A, B , and C , respectively, then

$b + c = 4a$ (b) $b + c = 2a$ the locus of point A is an ellipse the locus of

point A is a pair of straight lines

A. $b + c = 4a$

B. $b + c = 2a$

C. locus of point A is an ellipes

D. locus of point A is a pair of straight line

Answer: B::C

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9. Let ABC and ABC' be two non-congruent triangles with sides $AB = 4$, $AC = AC' = 2\sqrt{2}$ and angle $B = 30^\circ$. The absolute value of the difference between the areas of these triangles is

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10. A straight line through the vertex P of a triangle PQR intersects the side QR at the point S and the circuecircle of the triangle PQR at the point T . If S is not the centre of the circumeircle, then

A. $\frac{1}{PS} + \frac{1}{ST} < \frac{2}{\sqrt{QS \times SR}}$

B. $\frac{1}{PS} + \frac{1}{ST} > \frac{2}{\sqrt{QS \times SR}}$

C. $\frac{1}{PS} + \frac{1}{ST} < \frac{4}{QR}$

D. $\frac{1}{PS} + \frac{1}{ST} > \frac{4}{QR}$

Answer: D

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11. Consider the circle $x^2 + y^2 = 9$ and the parabola $y^2 = 8x$. They intersect at P and Q in first and 4th quadrant, respectively. Tangents to the circle at P and Q intersect the x-axis at R and tangents at the parabola at P and Q intersect the x-axis at S.

A. 4

B. 3

C. $\frac{8}{3}$

D. 2

Answer: B



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12. Consider the circle $x^2 + y^2 = 9$ and the parabola $y^2 = 8x$. They intersect at P and Q in first and 4th quadrant, respectively. Tangents to the circle at P and Q intersect the x-axis at R and tangents at the parabola at P and Q intersect the x-axis at S.

A. 5

B. $3\sqrt{3}$

C. $3\sqrt{2}$

D. $2\sqrt{3}$

Answer: B



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13. Consider the circle $x^2 + y^2 = 9$ and the parabola $y^2 = 8x$. They intersect at P and Q in first and 4th quadrant, respectively. Tangents to the circle at P and Q intersect the x-axis at R and tangents at the parabola at P and Q intersect the x-axis at S.

A. $1 : \sqrt{2}$

B. $1 : 2$

C. $1 : 4$

D. $1 : 8$

Answer: C



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14. Internal bisector of $\angle A$ of triangle ABC meets side BC at D. A line drawn through D perpendicular to AD intersects the side AC at E and the side AB at F. If a, b, c represent sides of $\triangle ABC$, then

A. AE is HM of b and a

$$B. AD = \frac{2bc}{b+c} \cos \frac{A}{2}$$

$$C. EF = \frac{4bc}{b+c} \sin \frac{A}{2}$$

D. $\triangle AEF$ is isosceles

Answer: A::B::C::D



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15. Given an isosceles triangle, whose one angle is $2\frac{\pi}{3}$ and the radius of its incircle $=\sqrt{3}$ Then find the area of the triangle

A. $4\sqrt{3}$

B. $12 - 7\sqrt{3}$

C. $12 + 7\sqrt{3}$

D. None of the above

Answer: C

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16. In $\triangle ABC$, which one is true among the following ?

A. $(b + c)\cos \frac{A}{2} = a \sin\left(\frac{B + C}{2}\right)$

B. $(b + c)\cos\left(\frac{B + C}{2}\right) = a \sin \frac{A}{2}$

C. $(b - c)\cos\left(\frac{B - C}{2}\right) = a \cos\left(\frac{A}{2}\right)$

D. $(b - c)\cos \frac{A}{2} = a \sin\left(\frac{B - C}{2}\right)$

Answer: D

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17. Let a vertical tower Ab have its end A on the level ground. Let C be the mid point of AB and P be a point on the ground such that $AP = 2AB$. If $\angle BPC = \beta$, then $\tan \beta$ is equal to : $\frac{2}{9}$ (2) $\frac{4}{9}$ (3) $\frac{6}{7}$ (4) $\frac{1}{4}$

A. $\frac{6}{7}$

B. $\frac{1}{4}$

C. $\frac{2}{9}$

D. $\frac{4}{9}$

Answer: C

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18. ABCD is a trapezium such that AB and CD are parallel and $BC \perp CD$. If $\angle ADB = \theta$, $BC = p$ and $CD = q$, then AB is equal to

A. $\frac{(p^2 + q^2) \sin \theta}{p \cos \theta + q \sin \theta}$

B. $\frac{p^2 + q^2 \cos \theta}{p \cos \theta + q \sin \theta}$

C. $\frac{p^2 + q^2}{p^2 \cos \theta + q^2 \sin \theta}$

D. $\frac{(p^2 + q^2) \sin \theta}{(p \cos \theta + \sin \theta)^2}$

Answer: A

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19. For a regular polygon, let r and R be the radii of the inscribed and the circumscribed circles. A false statement among the following is

There is a regular polygon with $\frac{r}{R} = \frac{1}{\sqrt{2}}$ (17) There is a regular polygon with $\frac{r}{R} = \frac{2}{3}$ (30) There is a regular polygon with $\frac{r}{R} = \frac{\sqrt{3}}{2}$ (47) There is a regular polygon with $\frac{r}{R} = \frac{1}{2}$ (60)

A. there is a regular polygon with $\frac{r}{R} = \frac{1}{2}$

B. there is a regular polygon with $\frac{r}{R} = \frac{1}{\sqrt{2}}$

C. there is a regular polygon with $\frac{r}{R} = \frac{2}{3}$

D. there is a regular polygon with $\frac{r}{R} = \frac{\sqrt{3}}{2}$

Answer: A::B::D



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20. In triangle ABC , let $\angle c = \frac{\pi}{2}$. If r is the inradius and R is circumradius of the triangle, then $2(r + R)$ is equal to $a + b$ (b) $b + c$

$$c + a \quad (d) \quad a + b + c$$

A. $c + a$

B. $a + b + c$

C. $a + b$

D. $b + c$

Answer: A



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21. If in a $\triangle ABC$, the altitudes from the vertices A, B, C on opposite sides are in H.P, then $\sin A, \sin B, \sin C$ are in

A. HP

B. AGP

C. AP

D. GP

Answer: C



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