



## MATHS

### BOOKS - NAVBODH MATHS (HINGLISH)

#### CIRCLE

#### 4.1 (1 mark each)

1. .... circle (s) can pass through a given point.

A. One

B. Two

C. Three

D. Infinite.

**Answer: D**



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2. Two circles of radii 5.5 cm and 3.3cm respectively touch each other. What is the distance between their centre ?

A. 4.4 cm

B. 8.8 cm

C. 2.2 cm

D. 8.8 or 2.2 cm

**Answer: D**





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3. What is the measure of a semicircle ?

A.  $90^\circ$

B.  $180^\circ$

C.  $360^\circ$

D.  $270^\circ$

**Answer: B**



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4. If the measure of an arc of a circle is  $60^\circ$  , then what is the measure of its corresponding arc ?

A.  $60^\circ$

B.  $120^\circ$

C.  $30^\circ$

D.  $300^\circ$

**Answer: D**



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5. Length of a tangent segment drawn from a point which is at a distance 12.5 cm from the centre of a circle

is 12cm , find the diameter of the circle.

A. 25 cm

B. 24 cm

C. 7 cm

D. 14 cm

**Answer: C**



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**6.** If two circles touch externally , how many common tangents can be drawn to them ?

A. One

B. Two

C. Three

D. Four

**Answer: C**



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7.  $\angle ACB$  is inscribed in arc  $ACB$  of a circle with centre  $O$ .  
If  $\angle ACB = 65^\circ$ , find  $m(\text{arc } ACB)$ .

A.  $65^\circ$

B.  $130^\circ$

C.  $295^\circ$

D.  $230^\circ$

**Answer: D**



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**8.** Chords AB and CD of a circle intersect inside the circle at point E. If  $AE = 5.6$  ,  $EB = 10$  cm ,  $CE = 8$  ,find ED.

A. 7

B. 8

C. 11.2

D. 9

**Answer: A**



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9. In a cyclic  $\square$  ABCD, twice the measure of  $\angle A$  is thrice the measure of  $\angle C$ . Find the measure of  $\angle C$ .

A.  $36^\circ$

B.  $72^\circ$

C.  $90^\circ$

D.  $108^\circ$

**Answer: B**



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10. Points A,B,C are on a circle, such that  $m(\text{arc } AB) = m(\text{arc } BC) = 120^\circ$ . No point, except point B, is common to the arcs. What type is the  $\triangle ABC$ ?

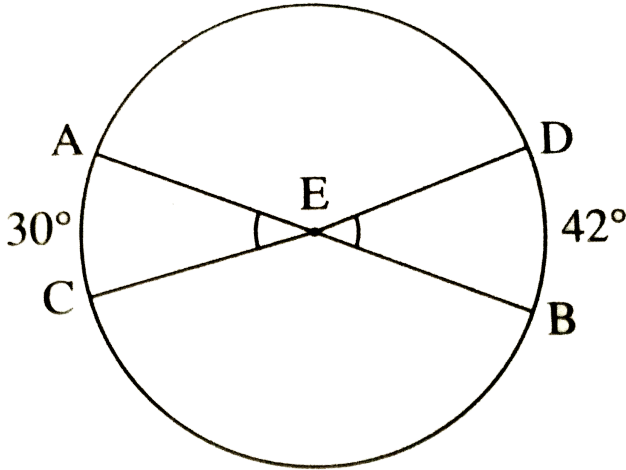
- A. Equilateral triangle
- B. Scalene triangle
- C. Right angled triangle
- D. Isosceles triangle

**Answer: A**



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11. From the information given in the figure, find the measure of  $\angle AED$ .



A.  $42^\circ$

B.  $30^\circ$

C.  $36^\circ$

D.  $72^\circ$



Answer: C

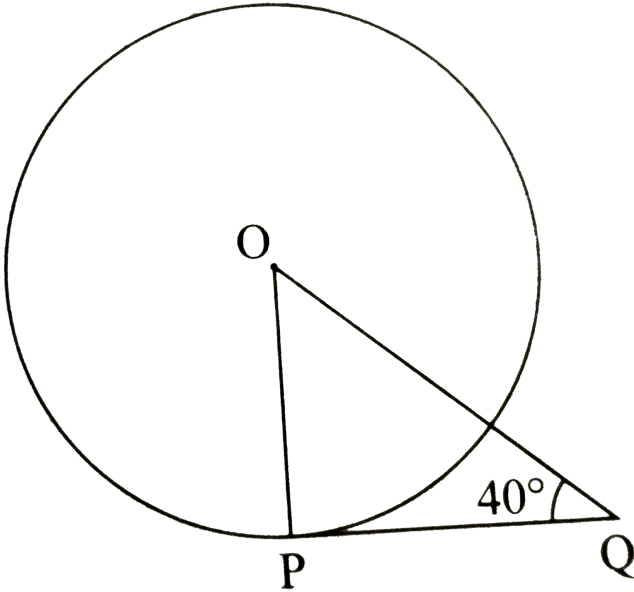


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#### 4.2 (1 mark each)

1. In the figure, seg PQ is tangent OP is the radius,  $\angle OQP = 40^\circ$ , then the measure of  $\angle OPQ$  is ..... and the measure of  $\angle POQ$  is

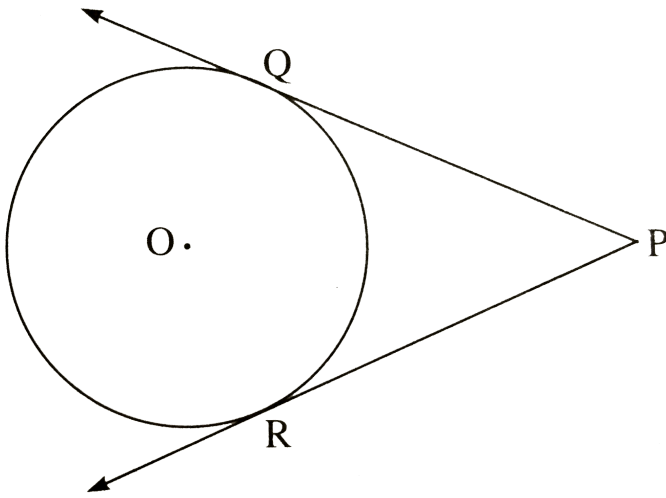
.....



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2. In the figure ,  $PQ$  and  $PR$  are tangents drawn from and external point  $P$  to the circle with centre  $O$ .  $Q$  and  $R$  are the points of contact. If  $PQ = 5$  cm then what is the

length of segment PR ? Why ?



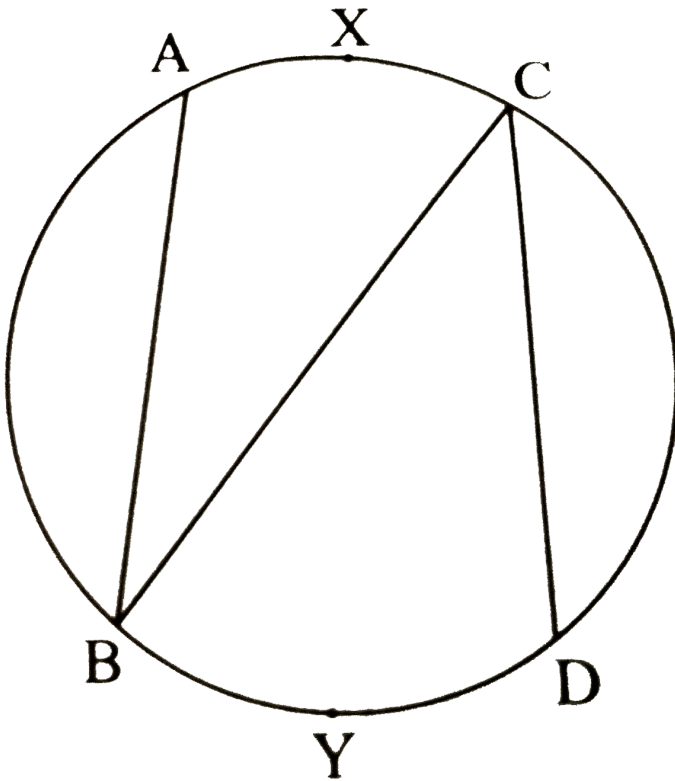
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3. Two circles with radii 3 cm and 2.5 cm touch each other externally then find the distance between their centre.

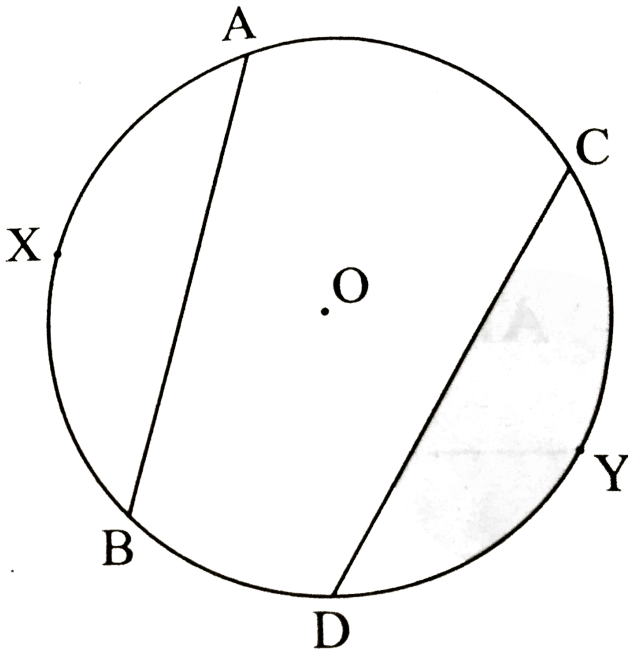


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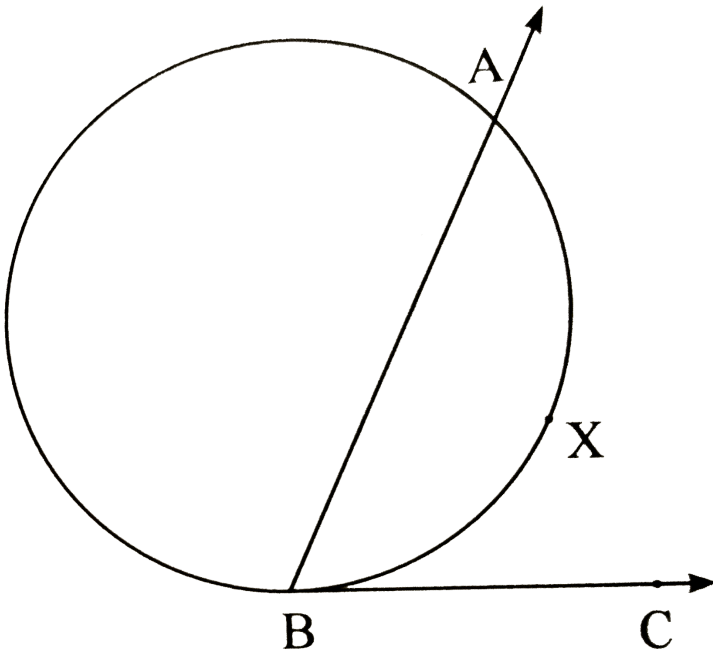
4. In the figures,  $\angle ABC$  is inscribed in arc  $AXC$  and intercepts arc  $AXC$  and  $\angle BCD$  is inscribed in arc  $BCD$  and intercepts arc  $BYD$ . If  $\angle ABC = 30^\circ$  and  $m(\text{arc } BYD) = 80^\circ$  then the  $m(\text{arc } AXC) = \dots\dots\dots$  and measure of  $\angle BCD = \dots\dots\dots$



5. Chords  $AB$  and  $CD$  of a circle with centre  $O$  are congruent. If  $m(\text{arc } AXB) = 120^\circ$  then what is the  $m(\text{arc } CYD)$ .

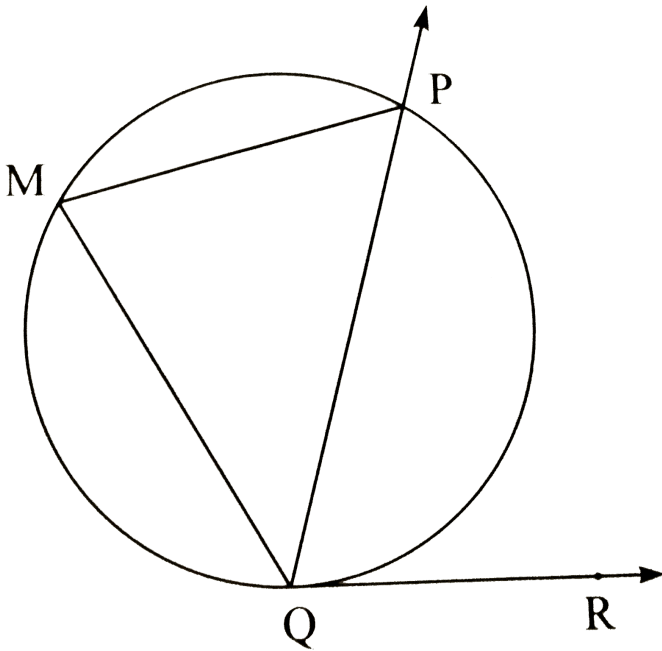


6. In the figure, ray BC is tangent at point B and ray BA is secant.  $\angle ABC$  intercepts arc AXB if  $m(\text{arc AXB}) = 130^\circ$  then find the measure of  $\angle ABC$ .



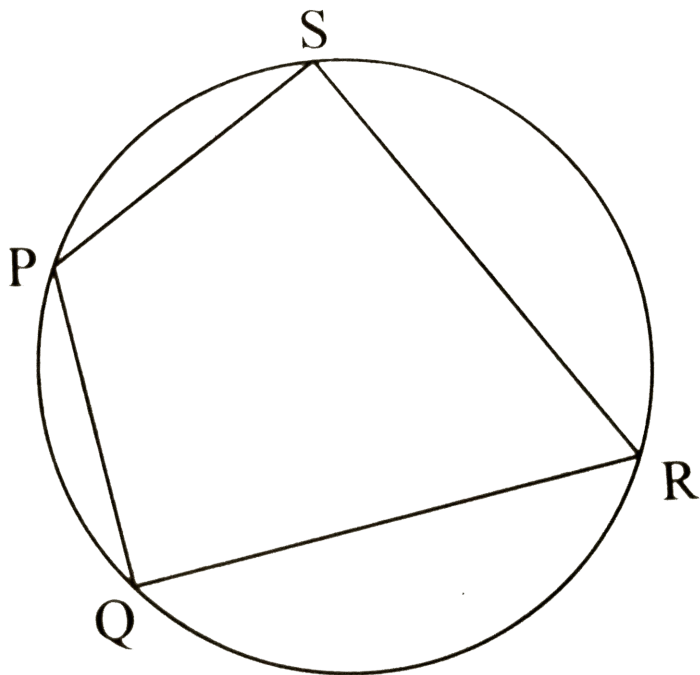
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7. In the figure, ray QR is tangent and ray QP is secant.  $\angle PMQ$  is inscribed in arc PMQ.  $\angle PQR$  and  $\angle PMQ$  intercept arc PQ. If  $\angle PQR = 75^\circ$  then what is the measure of  $\angle PMQ$ ? Why?



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8.  $\square$  PQRS is cyclic . If  $\angle QPS = 115^\circ$  then what is the measure of  $\angle QRS$  ? Why ?

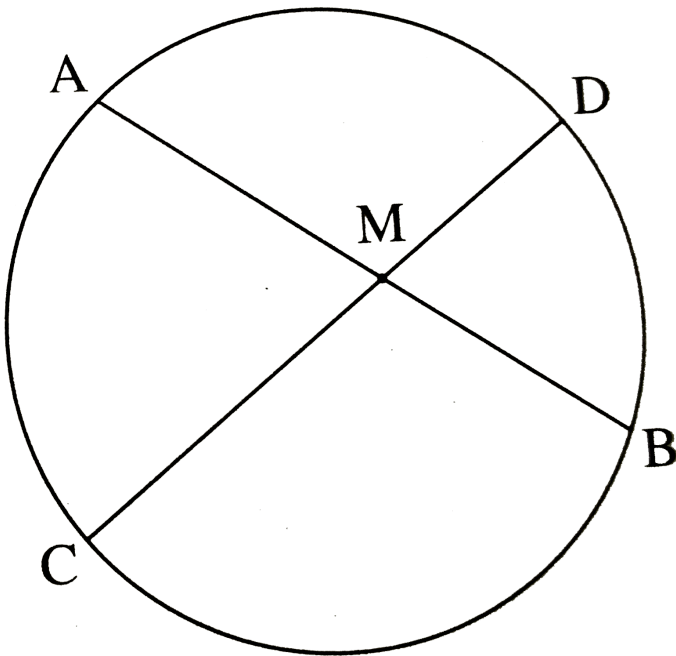


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9. Chords AB and CD intersect at point M inside the circle then theorem of internal division of chords.

$$AM \times BM = \square \times \square$$



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### 4.3 (1 mark each)

1. If two circles have radii 10 cm and 15cm and they touch each other. Find the distance between their centres.



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2. In the figure, tangents at B and C of the circle with centre O intersect at point A. If  $\angle BAC = 90^\circ$  then

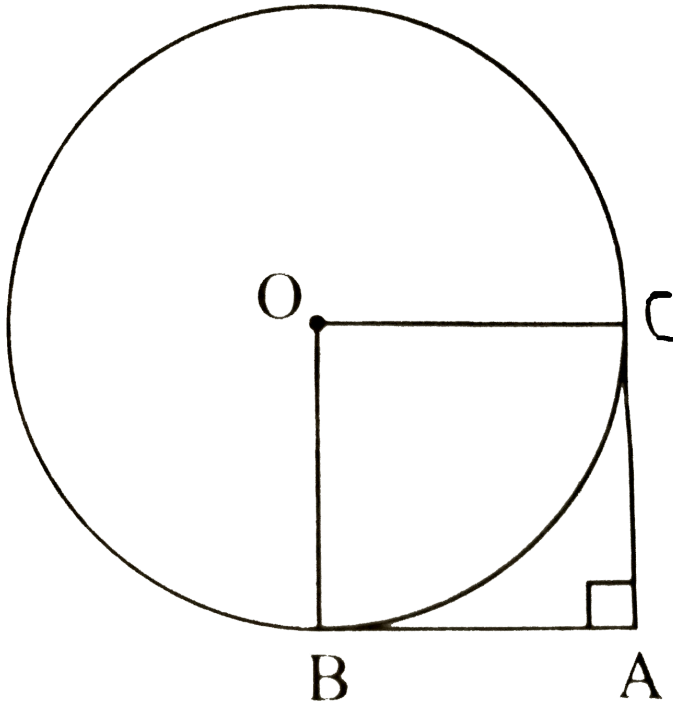
prove

$\square$  BACO

is

a

square



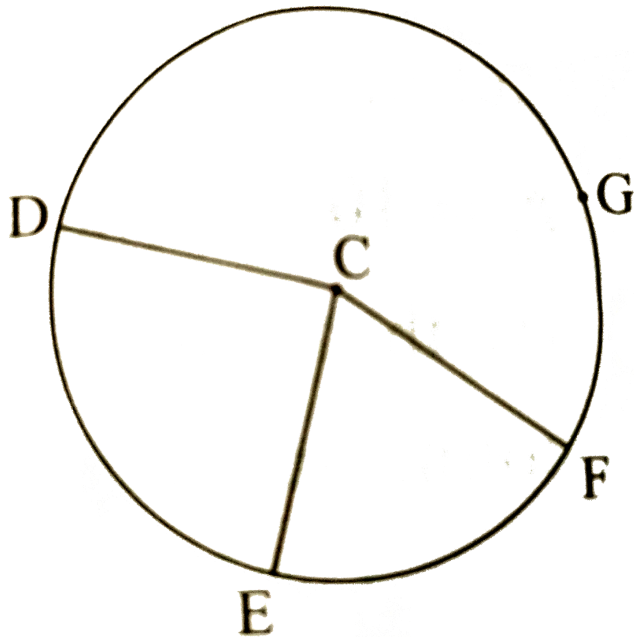
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3. In the figure , points G,D,E,F are concyclic points of a circle with centre C.

$$\angle ECF = 70^\circ$$

$$m(\text{arc DGF}) = 200^\circ,$$

find  $m(\text{arc DE})$  and  $m(\text{arc DEF})$ .

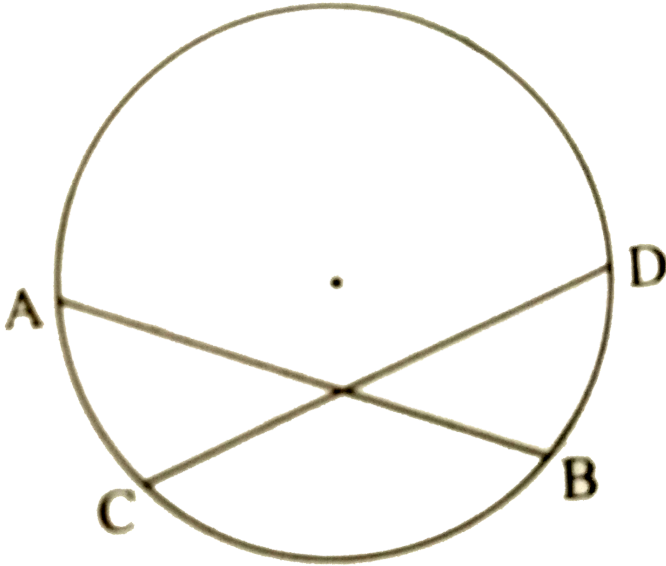


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4. In the figure, chord  $AB \cong$  chord  $CD$

Prove that ,

arc  $AC \cong$  arc  $BD$



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5. Prove that, angles inscribed in the same arc are congruent

$\angle PQR$  and  $\angle PSR$  are inscribed in the same arc.

Arc  $PXR$  is intercepted by the angles.

To prove :  $\angle PQR \cong \angle PSR$



Proof :

$$m\angle PQR = \frac{1}{2}m(\text{arc}PXR) \dots \square$$

$$m\angle \square = \frac{1}{2}m(\text{arc}PXR) \dots(2) \square$$

$$\therefore m\angle \square = m\angle PSR \dots[\text{From (1) and (2) }]$$

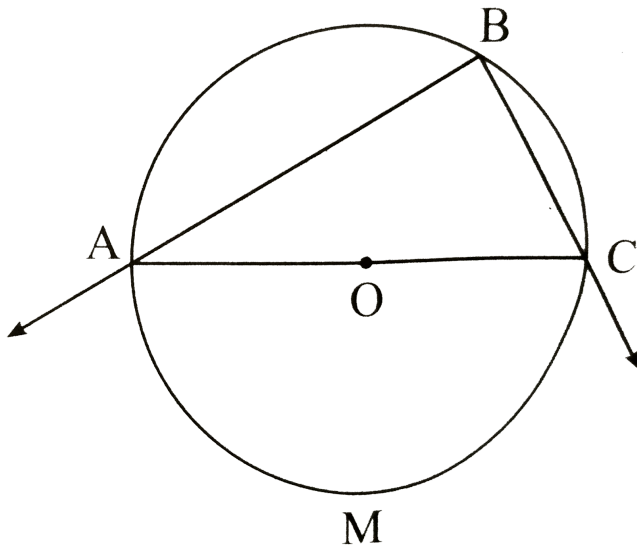
$\therefore \angle PQR \cong \angle PSR$  ...(Angles equal in measure are congruent )



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6. Observe the following figure and complete the following activity :

$\angle ABC$  is  $90^\circ$



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7. In order to prove 'Opposite angles of a cyclic quadrilateral are supplementary.'

(1) Draw a neat labelled figure.

(2) Write 'Given ' and 'To prove' from the figure drawn by you.



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8. Chord AB and CD intersect each other at point E in the interior of the circle. In order to prove

$$\angle CEB = \frac{1}{2} [m(\text{arc}AD) + m(\text{arc}CB)]$$



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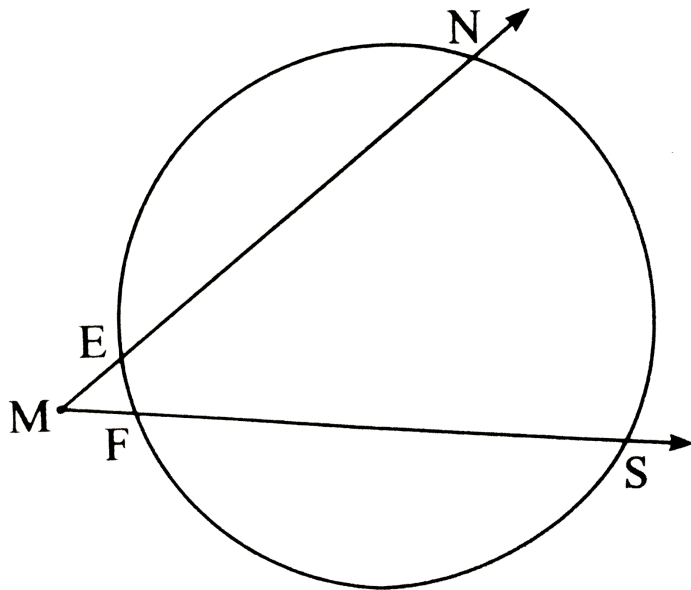
9. In the figure,

$$m(\text{arc}NS) = 125^\circ$$



$$m(\text{arc } EF) = 37^\circ$$

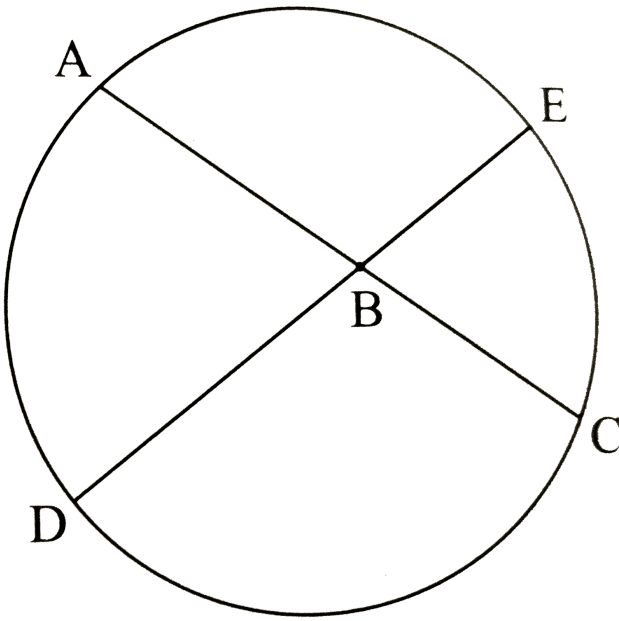
find the measure  $\angle NMS$ ,



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10. In the figure, chords AC and DE intersect at B. If

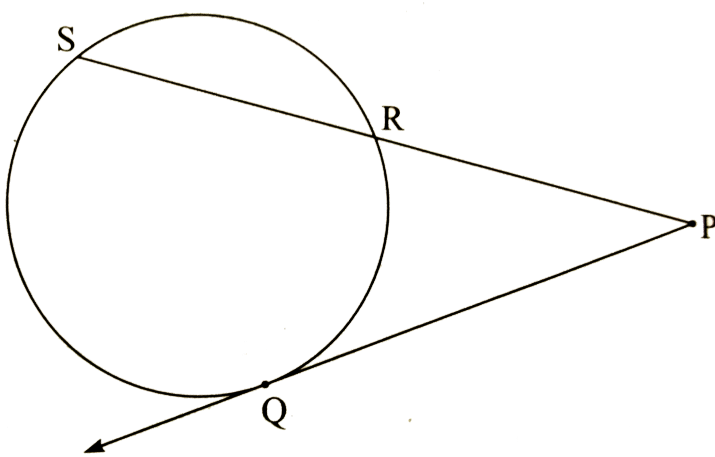
$$\angle ABE = 108^\circ, m(\text{arc } AE) = 95^\circ, \text{ find } m(\text{arc } DC).$$



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11. In the figure, ray PQ touches the circle at point Q. If

$PQ = 12$ ,  $PR = 8$ , then find PS.



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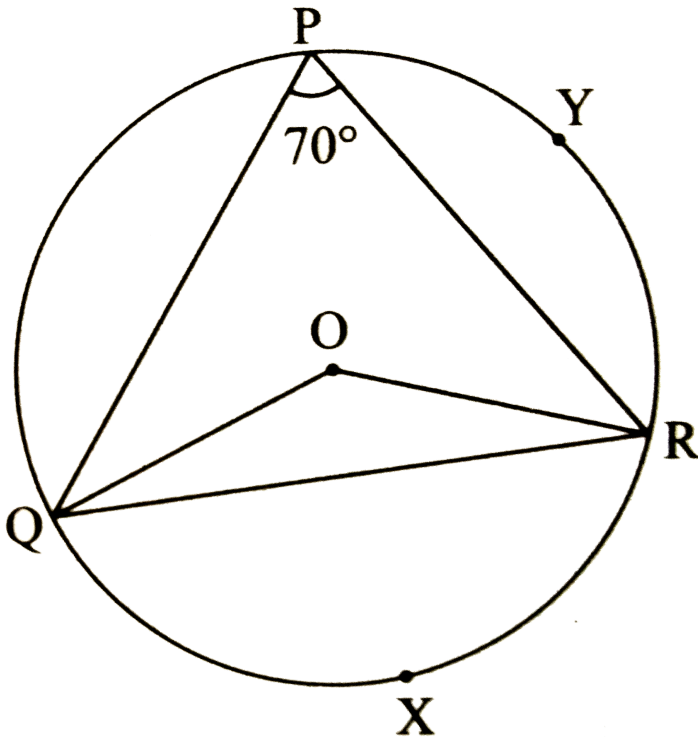
#### 4.4 (1 mark each)

1. In the figure, O is the centre of circle  $\angle QPR = 70^\circ$  and  $m(\text{arc PYR}) = 160^\circ$ , then find the value of each of the following :

(a)  $m(\text{arc QXR})$

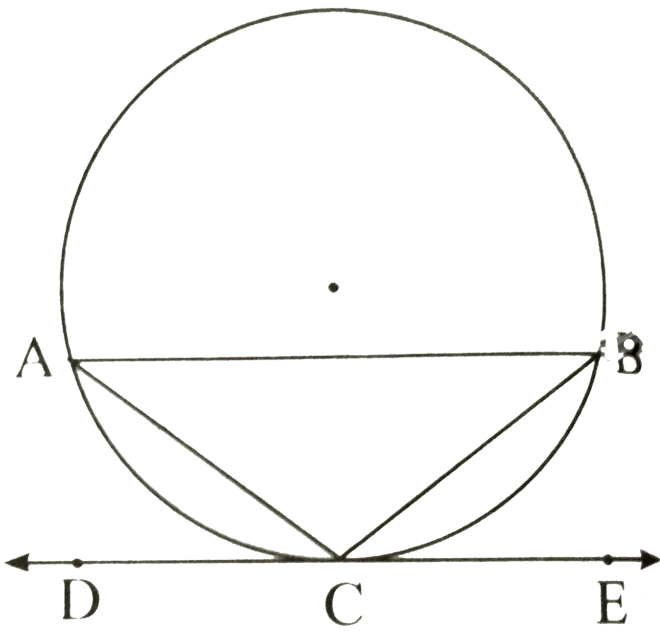
(b)  $\angle QOR$

(c)  $\angle PQR$



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2. In the figure, chord  $AB \parallel$  tangent  $DE$ . Tangent  $DE$  touches the circle at point  $C$  then prove  $AC = BC$ .



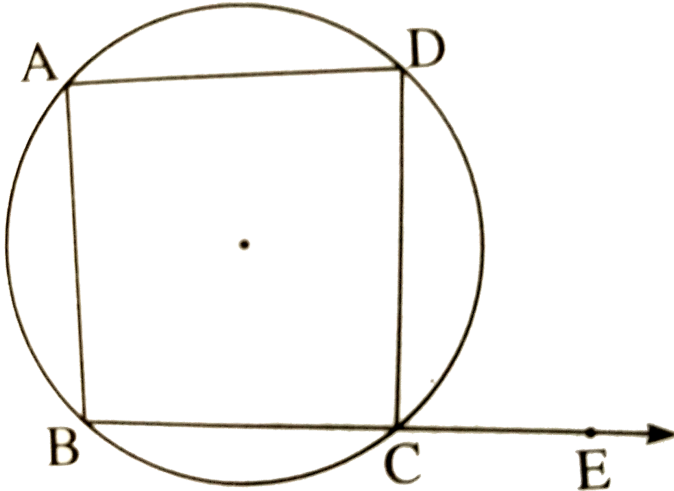
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3. Given :

□  $ABCD$  is cyclic.  $\angle DCE$  is an exterior angle of □  $ABCD$ .

To Prove :  $\angle DCE = \angle BAD$

Complete the proof by filling the boxes.



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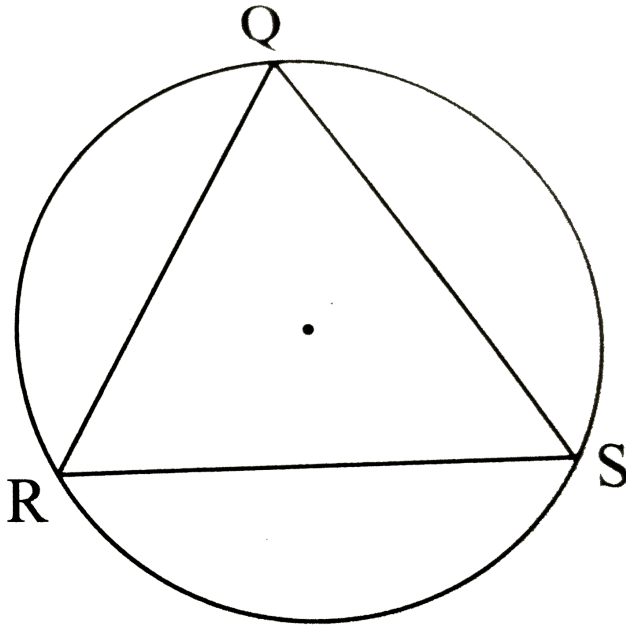
4. In the figure,  $\triangle QRS$  is an equilateral triangle.

Prove that

(1)  $\text{arc } RS \cong \text{arc } QS \cong \text{arc } QR$

(2)  $m(\text{arc } QRS) = 240^\circ$ .

Proof :

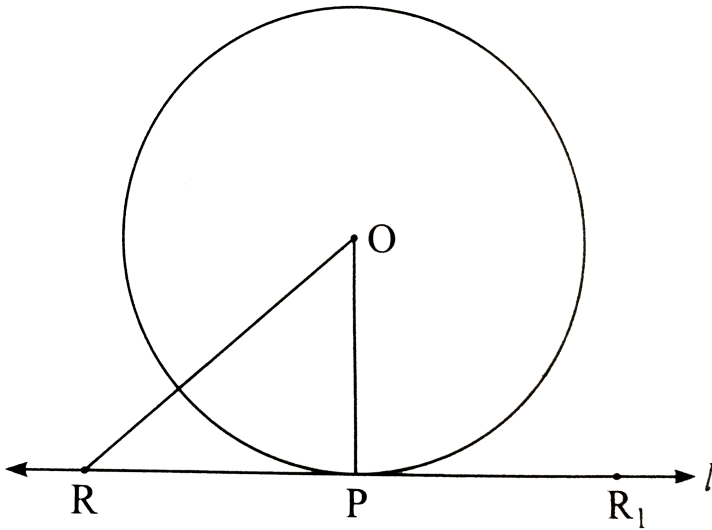


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5. Line  $l$  touches a circle with centre  $O$  at point  $P$ . If radius of the circle is 9 cm, answer the following :

(1) What is  $d(O,P)$  = ? Why ?

(2) If  $d(O,Q) = 8$  cm , where does the point Q lie ?



(3) If  $d(O,R) = 15$  cm , how many locations of point R are there on line l ? At what distance will each of them be from point P?

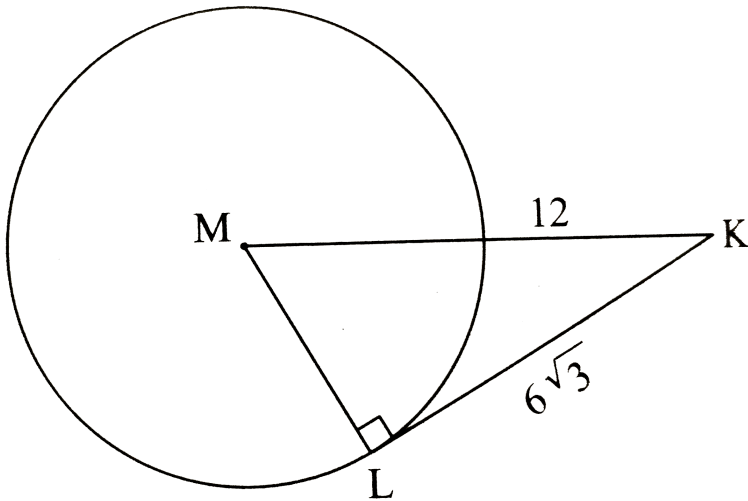
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6. In the figure, M is the centre of the circle and seg KL is a tangent segment. If  $MK = 12$ ,  $KL = 6\sqrt{3}$  then find,



(1) Radius of the circle,

(2) Measures of  $\angle K$  and  $\angle M$ .



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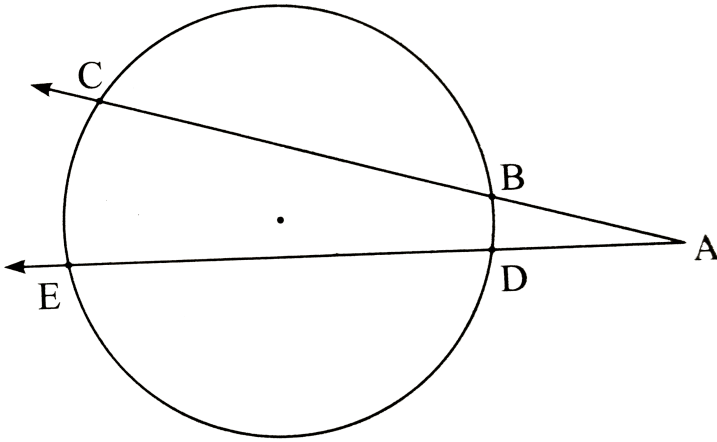
7. In the figure,

(1)  $m(\text{arc } CE) = 54^\circ$ ,  $m(\text{arc } BD) = 23^\circ$ , find measure of

$\angle CAE$ .

(2) If  $AB = 4.2$ ,  $BC = 5.4$ ,  $AE = 12.0$ , find  $AD$ .

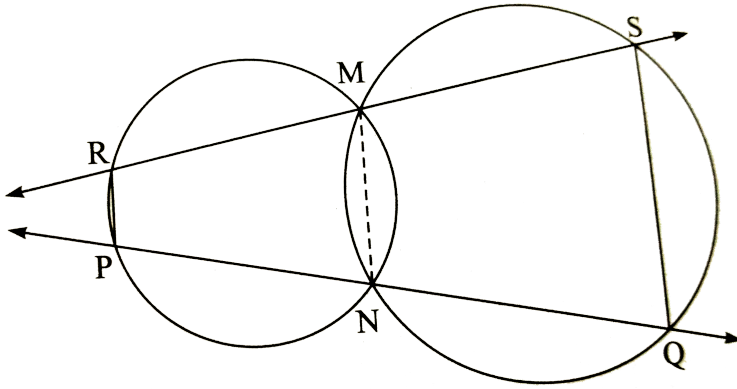
(3) If  $AB = 3.6$ ,  $AC = 9.0$ ,  $AD = 5.4$ , find  $AE$ .



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**8.** In the figure, two circles intersect at points M and N. Secants drawn through M and N intersect the circles at points R,S and P,Q respectively. Prove that :  $\text{seg } SQ \parallel$

seg RP.



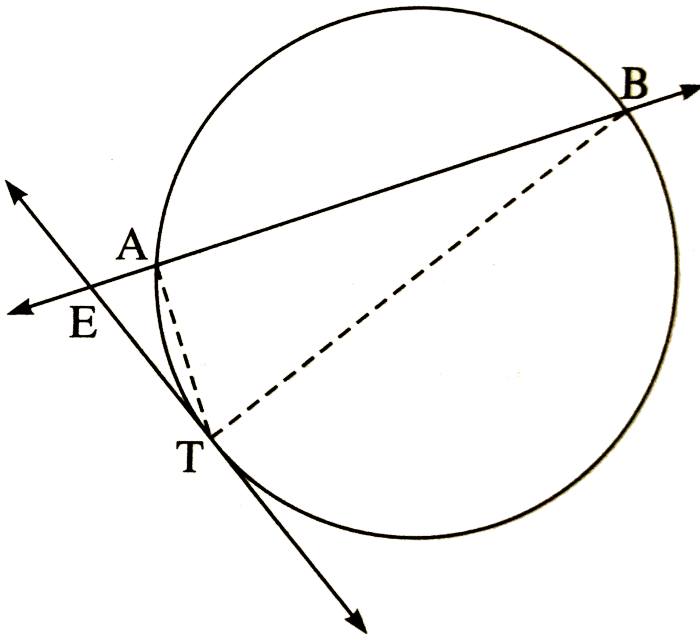
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**9.** Given : Line ET is tangent to the circle at point E. Line EAB is secant intersecting at point A and B.

To Prove :  $ET^2 = EA \times EB$

Construction : Draw seg BT and Seg AT

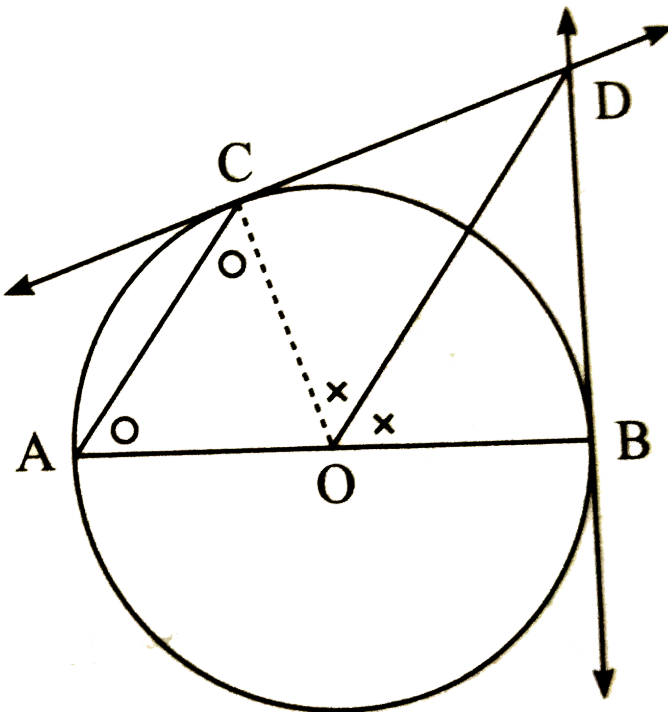
Complete the proof by filling the boxes.



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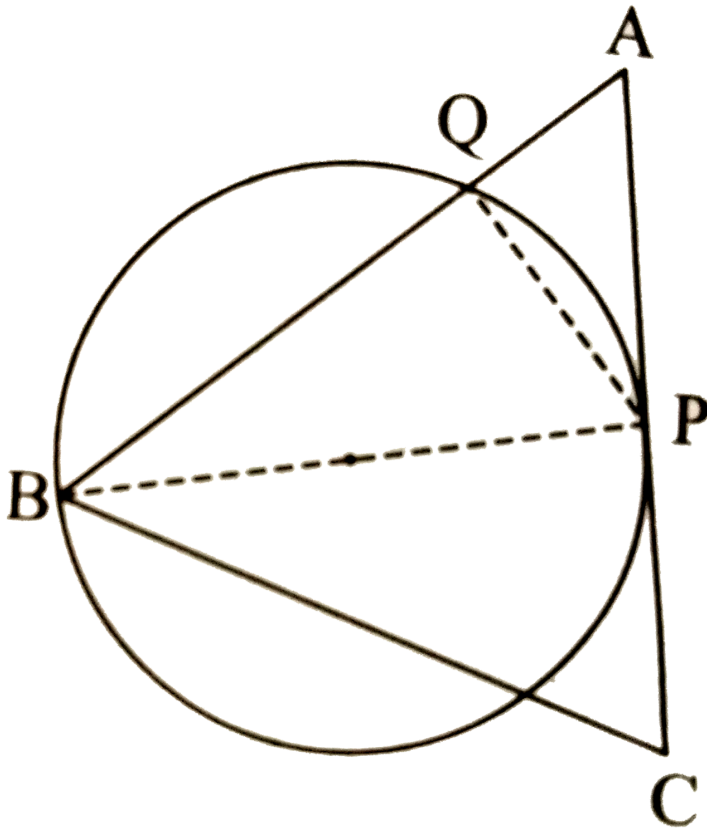
4.5 (1 mark each)

1. In the figure,  $O$  is the centre of the circle. Seg  $AB$  is the diameter at the point  $C$  on the circle the tangent  $CD$  is drawn. Line  $BD$  is a tangent to the circle at point  $B$ . Show that seg  $OD \parallel$  chord  $AC$ .



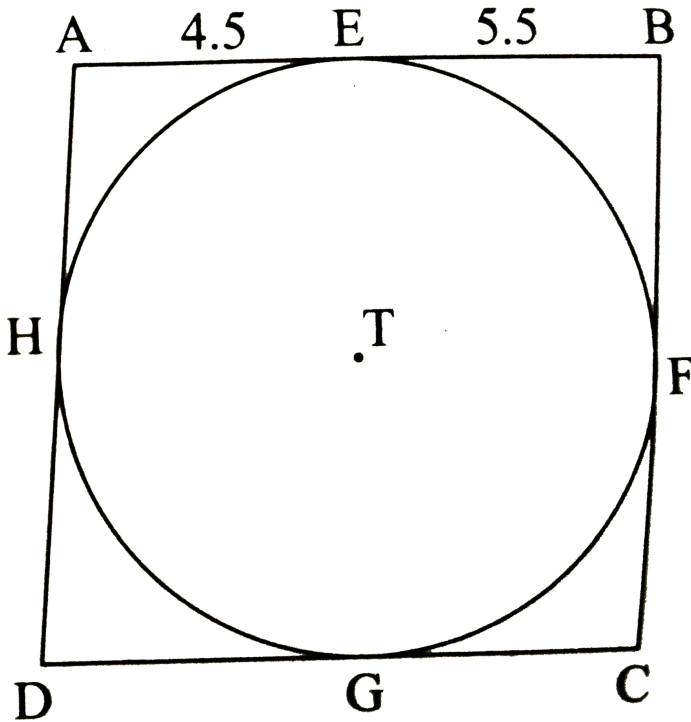
2. In  $\triangle ABC$ ,  $AB = AC$ . A circle passing through B touches side AC at its midpoint P and intersects side AB at Q then prove  $BQ = 3AQ$

Construction : Draw seg BP and seg PQ



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3. In the figure,  $\square ABCD$  is a parallelogram. It circumscribes the circle with centre T. Point E,F,G,H are touching points. If  $AE = 4.5$  , $EB = 5.5$  , find AD.

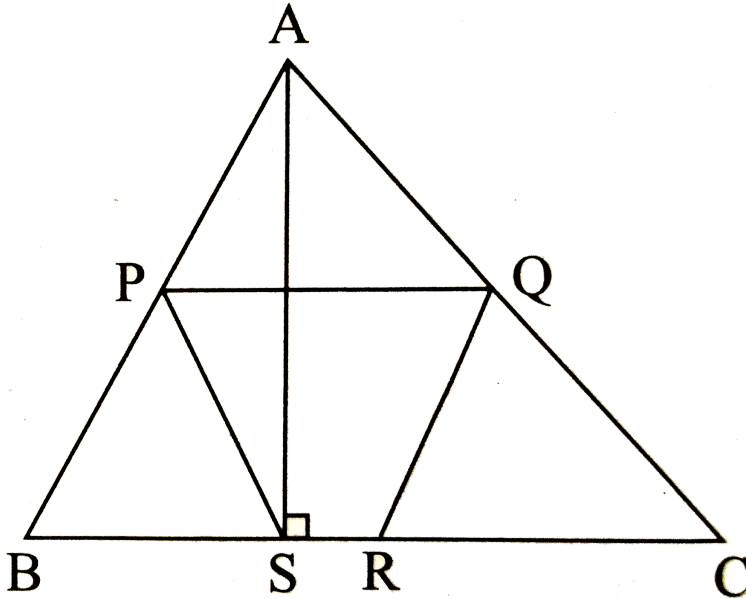


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4. In  $\triangle ABC$ , P,Q and R are midpoints of sides AB,AC and BC respectively. Seg  $AS \perp BC$  and  $PQ \parallel BC$ .

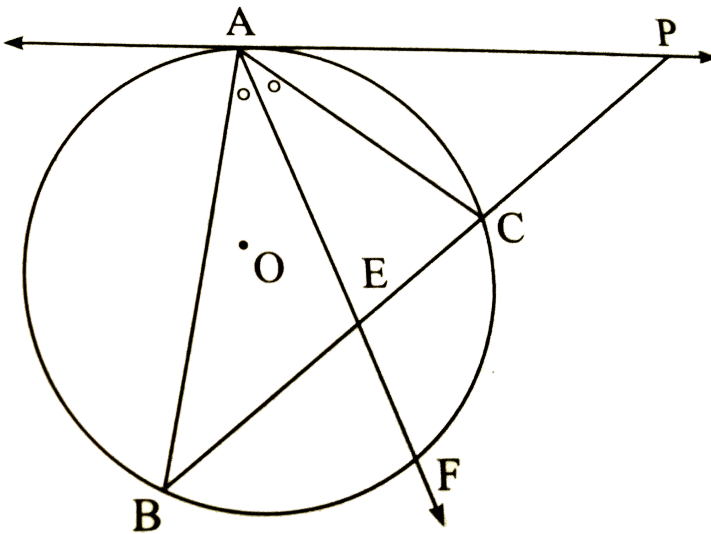
Prove that  $\square PQRS$  is a cyclic quadrilateral.



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5.  $\triangle ABC$  is inscribed in a circle with centre  $O$  and line  $AP$  is a tangent at the point  $A$ . Ray  $AF$  is the bisector of  $\angle BAC$

Prove that  $\text{seg } AP \cong \text{seg } PE$ .

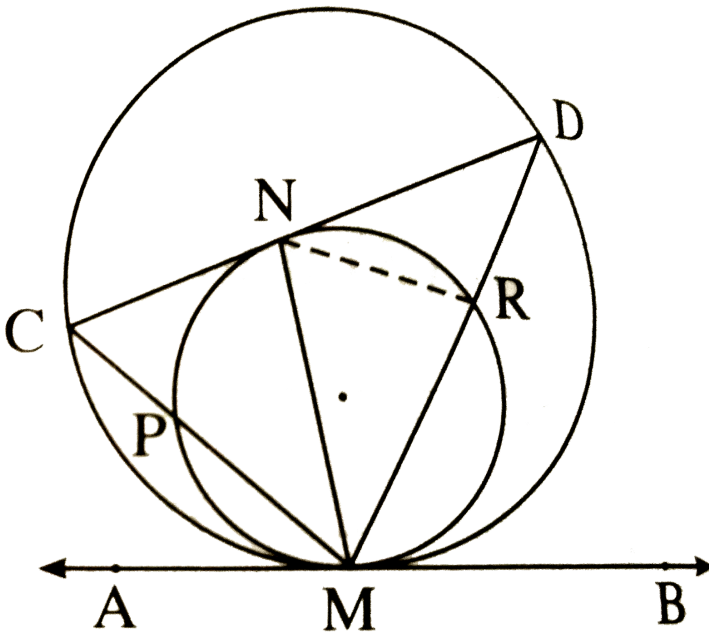


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6. Let  $M$  be a point of contact of two internally touching circles. Let line  $AMB$  be their common tangent. The chord  $CD$  of the bigger circle touches the smaller circle at the point  $N$ . Chord  $CM$  and chord  $DM$  of the bigger circle intersect the smaller circle at the points  $P$  and  $R$  respectively.

Prove that  $\angle CMN \cong \angle DMN$ .

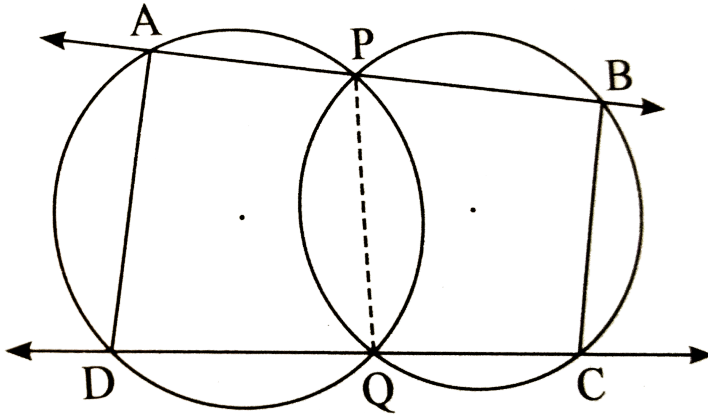
Construction : Draw seg NR.



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7. Two circles intersect each other at point P and Q. Secants drawn through p and Q intersect the circles at points A,B and D,C

Prove that :  $\angle ADC + \angle BCD = 180^\circ$



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## ASSIGNMENT 4.1

1. The angle made by the tangent and the radius made at the point of contact is

A.  $0^\circ$

B.  $45^\circ$

C.  $90^\circ$

D.  $75^\circ$

**Answer: C**



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2. A tangent AB, at a point A of a circle of radius 5 cm, meets a line through the centre O at point B such that  $OB = 12$  cm. Length AB is

A. 5 cm

B. 12 cm

C. 13 cm

D.  $\sqrt{19}$  cm

**Answer: D**



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3. If tangents PA and PB from a point P to a circle with centre O are inclined to each other at an angle of  $70^\circ$ , then  $\angle POA$  is equal to

A.  $70^\circ$

B.  $55^\circ$

C.  $100^\circ$

D.  $40^\circ$

**Answer: B**



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4. If TP and TQ are two tangents to a circle with centre O, so that  $\angle POQ = 120^\circ$ , then  $\angle PTQ$  is equal to

A.  $120^\circ$

B.  $30^\circ$

C.  $60^\circ$

D.  $90^\circ$

**Answer: C**





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5. AP is tangent to the circle with centre O at point A.  $OP = 10$  cm and  $\angle OPA = 30^\circ$ . The radius of the circle is

A. 10 cm

B.  $5\sqrt{3}$  cm

C. 5 cm

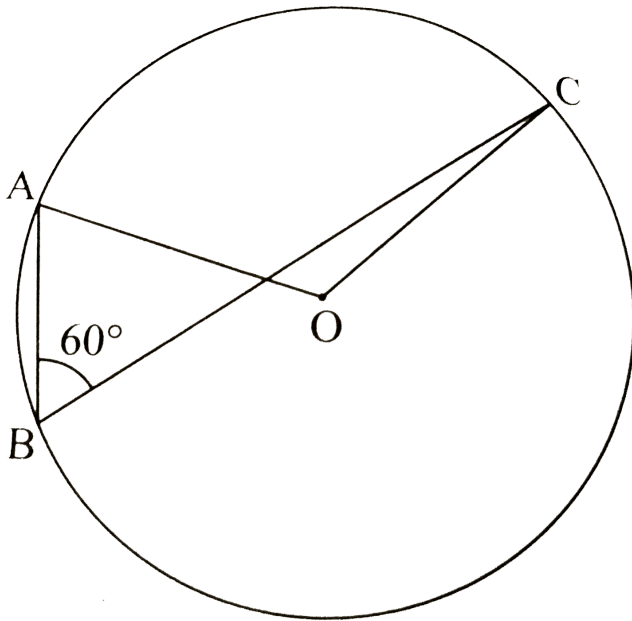
D.  $10\sqrt{3}$  cm

**Answer: C**



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6. In the figure, if  $\angle ABC = 60^\circ$ , then  $\angle AOC =$



A.  $120^\circ$

B.  $60^\circ$

C.  $30^\circ$

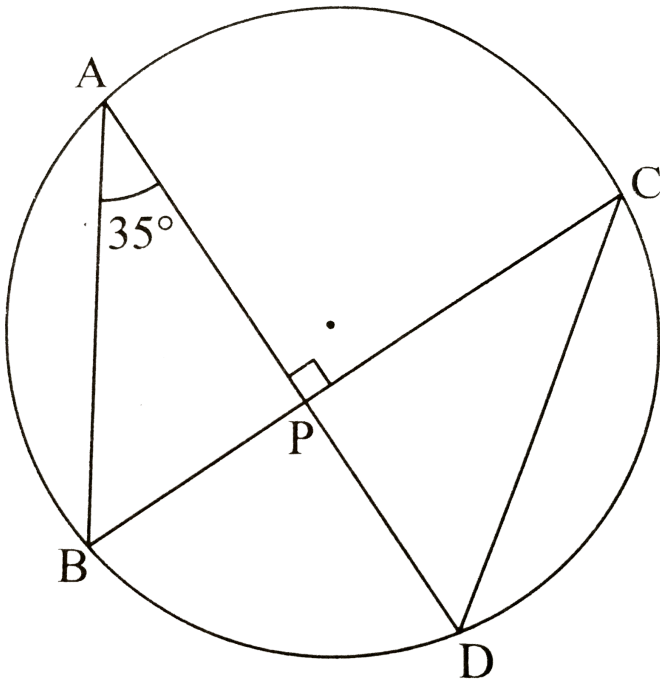
D.  $90^\circ$

Answer: A



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7. In the figure, chords AD and BC intersect each other at right angles at a point P. If  $\angle DAB = 35^\circ$ , then  $\angle ADC =$



A.  $35^\circ$

B.  $55^\circ$

C.  $65^\circ$

D.  $45^\circ$

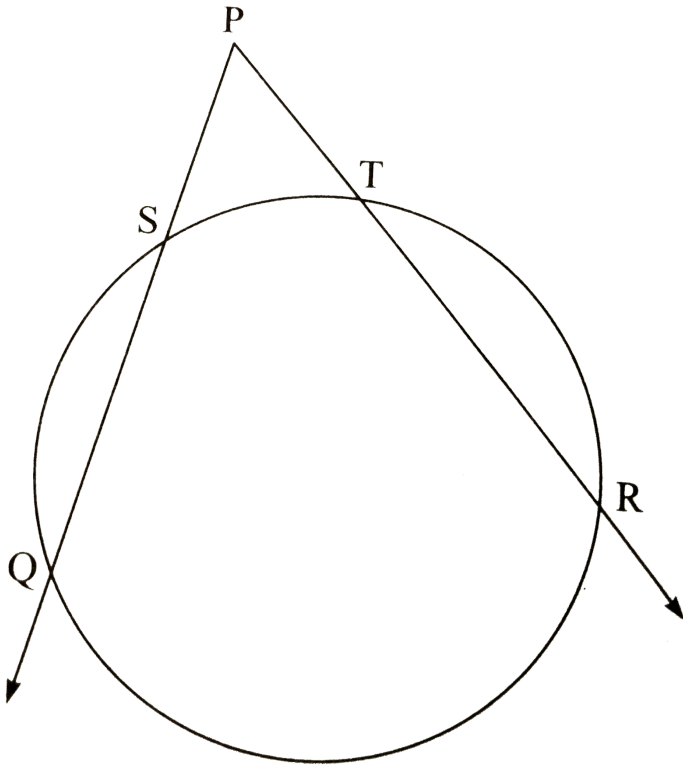
**Answer: B**



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**8.** In the figure ,  $\angle QPR$  has its vertex outside the circle such that  $m(\text{arc } QR) = 200^\circ$  and  $m(\text{arc } ST) = 90^\circ$ ,

then  $\angle QPR = ?$



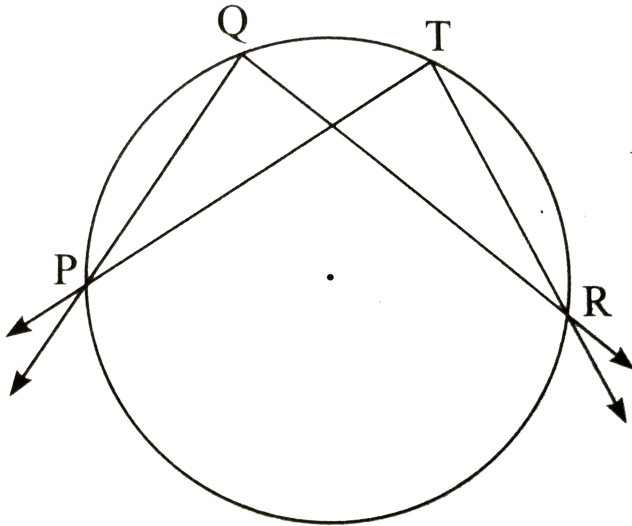
- A.  $45^\circ$
- B.  $100^\circ$
- C.  $110^\circ$
- D.  $55^\circ$

Answer: D



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9. In the figure,  $\angle PQR = 85^\circ$  then find the measure of  $\angle PTR$ .



A.  $75^\circ$

B.  $180^\circ$

C.  $90^\circ$

D.  $85^\circ$

**Answer: D**



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**10.** In the figure ,  $\angle ABC = 80^\circ$  then find the measure of  $m(\text{arc}APC)$  .

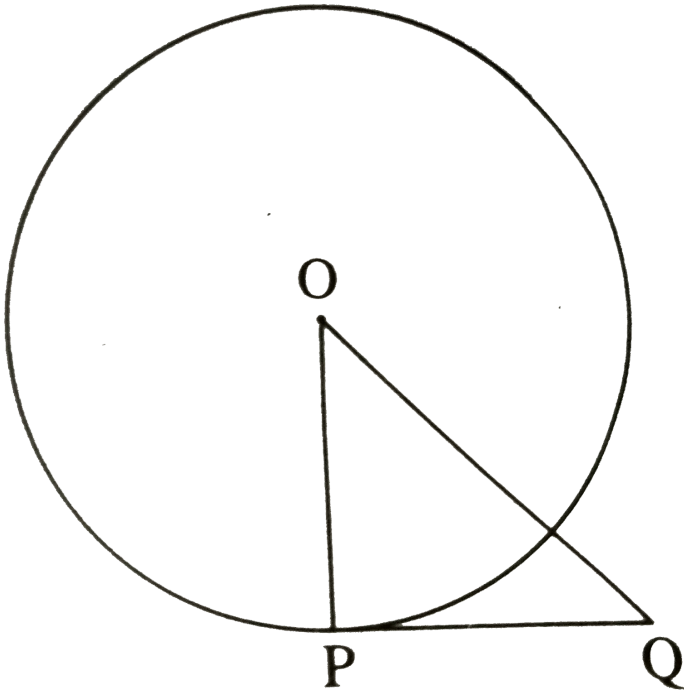


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**ASSIGNMENT 4.2**

1. In the figure,  $O$  is the centre of the circle  $PQ$  is the tangent at point  $P$  then what is the measure of  $\angle OPQ$  ?

Why ?



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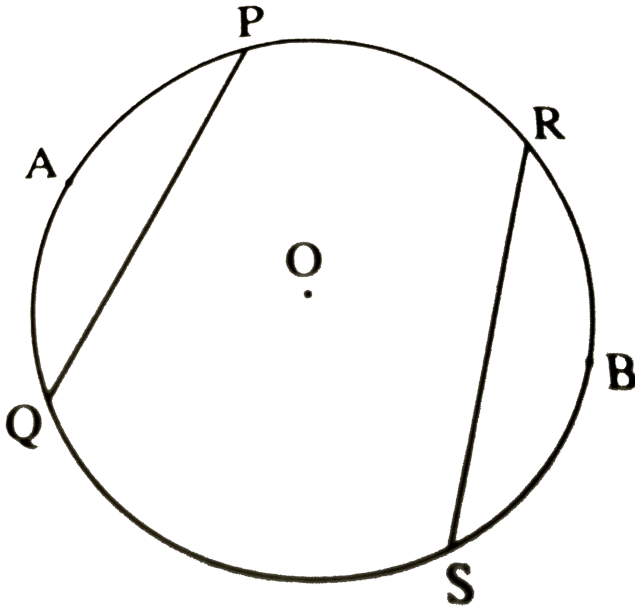
2. Two circles with radii 5cm and 1.5 cm touch each other internally then find the distance between their centres.



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3. In the figure,  $m(\text{arc PAQ}) = m(\text{arc RBS}) = 130^\circ$   
chord PQ has length 10cm then what is the length of

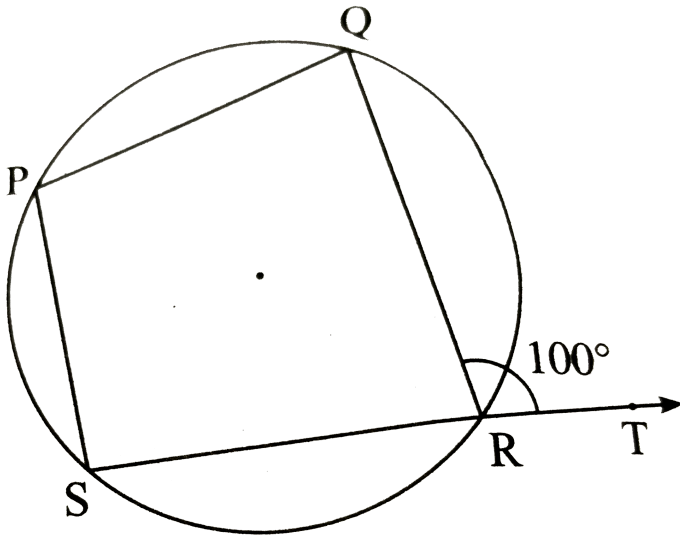
chord RS ? Why ?



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4.  PQRS is cyclic .T is a point of ray SR such that S-R-T and  $\angle QRT 100^\circ$  then what is the measure of  $\angle SPQ$  ?

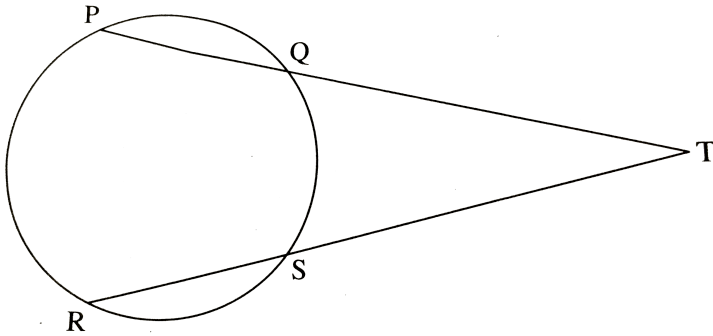
Why ?



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5. In the figure , chords PQ and RS intersect at point T outside the circle then by theorem of external division of chords,

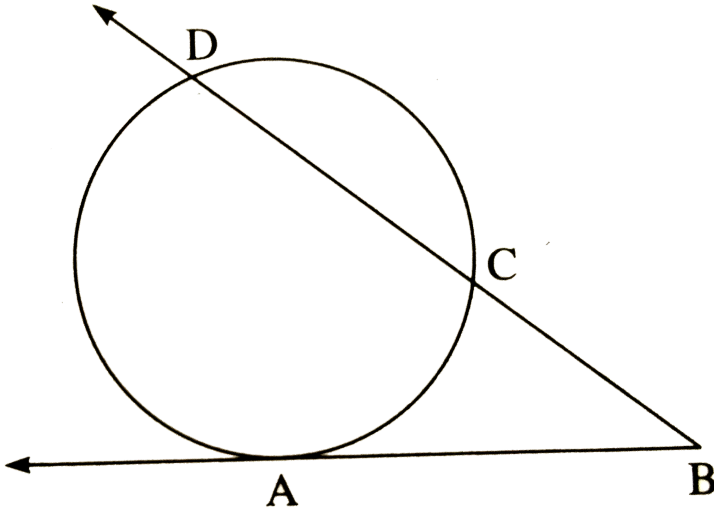
$$PT \times \square = ST \times \square$$



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6. Ray BA is tangent at point A . Ray BD is secant intersecting the circle at points C and D then

$$BA^2 = \square \times \square$$



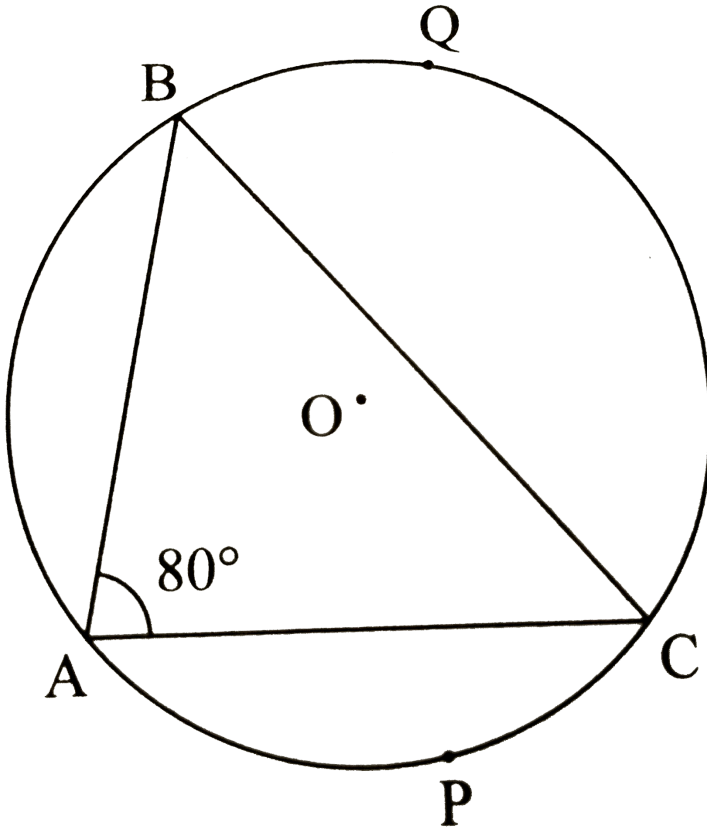
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### ASSIGNMENT 4.3

1. In the figure, O is the centre of the circle ,  
 $\angle BAC = 80^\circ$ ,  $m(\text{arc APC}) = 60^\circ$  then find the

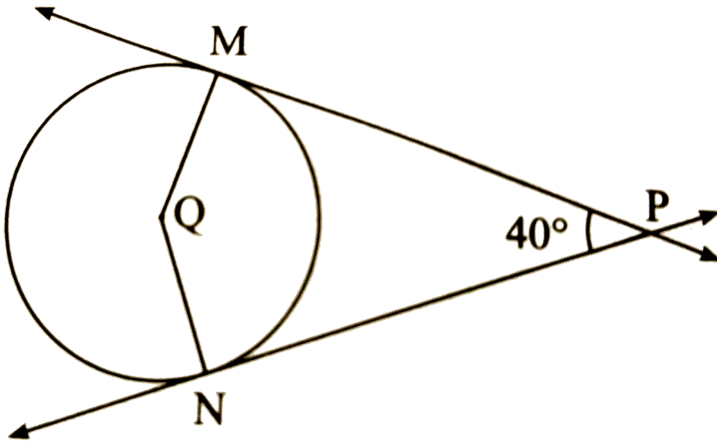
measure of

(i)  $\angle ABC$  (ii) arc BQC



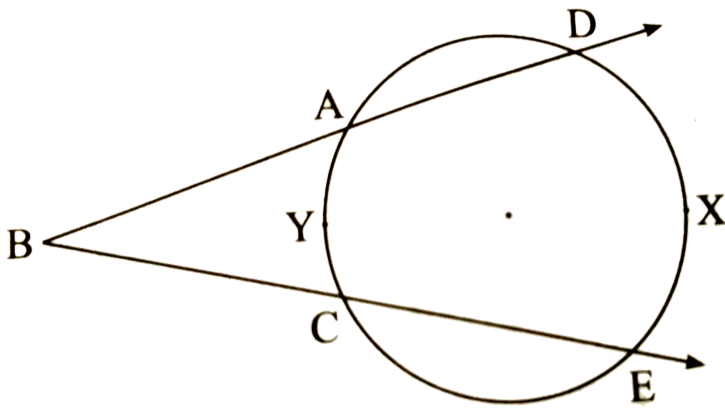
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2. In the figure,  $Q$  is the centre of the circle and  $PM$  and  $PN$  are tangent segments to the circle. If  $\angle MPN = 40^\circ$ , find  $\angle MQN$



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3. In the figure, if  $m(\text{arc } DXE) = 100^\circ$  and  $m(\text{arc } AYC) = 40^\circ$ , find  $\angle DBE$ .

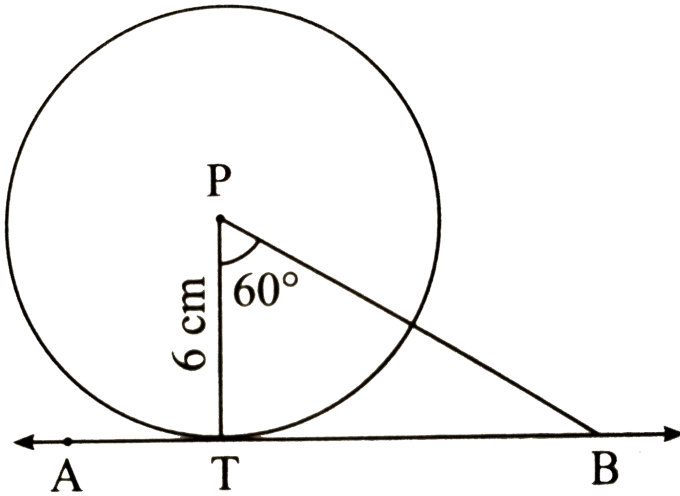


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4. In the figure, point P is the centre of the circle and line AB is the tangent to the circle at the point T. The radius



of the circle is 6 cm . Find PB, if  $\angle TPB = 60^\circ$

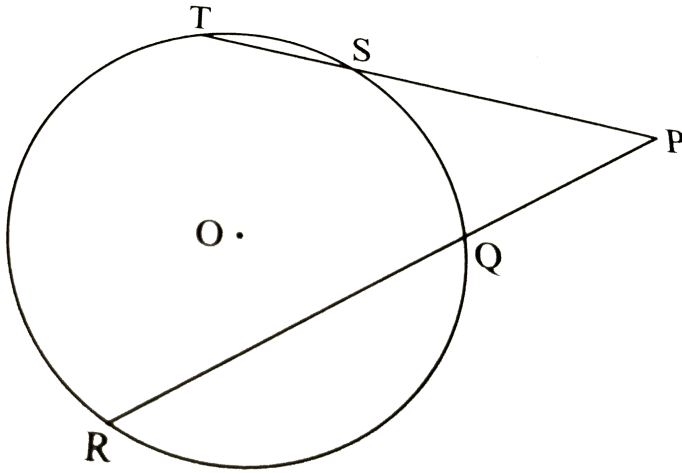


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5.  $\square MRPN$  is cyclic ,  
 $\angle R = (5x - 13)^\circ$ ,  $\angle N = (4x + 4)^\circ$ . Find measures of  
 $\angle R$  and  $\angle N$ .

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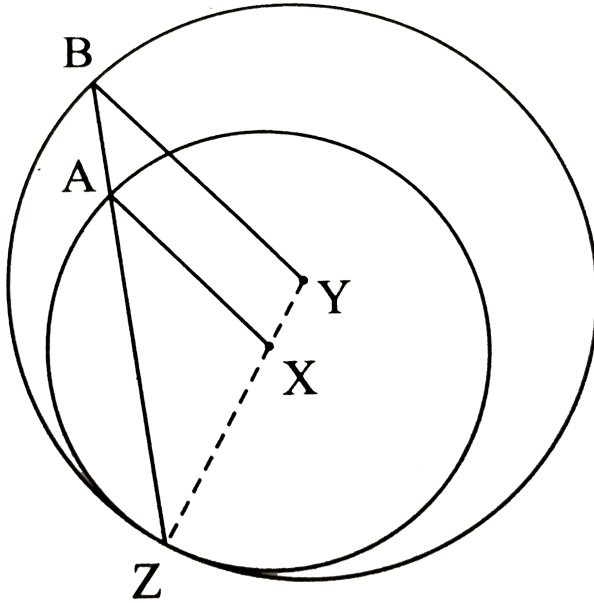
6. In the figure, if  $PQ = 6$ ,  $QR = 10$ ,  $PS = 4$ , find  $TS$



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7. In the figure, circles with centres  $X$  and  $Y$  touch internally at point  $Z$ . Seg  $BZ$  is a chord of bigger circle and it intersects smaller circle at point  $A$ . Prove that, seg

$AX \parallel \text{seg } BY$



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8. In the figure, chord  $EF \parallel$  chord  $GH$ .

Prove that ,

chord  $EG \cong$  chord  $FH$  .

Fill in the blanks and write the proof .

Proof : Draw seg GF.

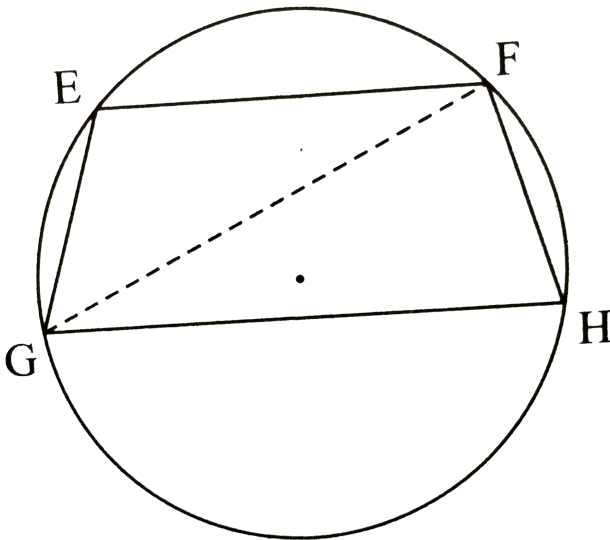
$$\angle EFG = \angle FGH \dots( \square ) \dots(1)$$

$$\angle EFG = \square \dots(\text{Inscribed angle theorem} ) \dots(2)$$

$$\angle FGH = \square \dots(\text{Inscribed angle theorem} ) \dots(3) , \text{brgt } \therefore$$

$$m(\text{ arc EG} ) = \square \dots[\text{From (1), (2) and (3) }]$$

$\therefore$  Chord EG  $\cong$  Chord FGH  $\dots(\text{Corresponding chords of congruent arcs} )$



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9. In the figure,  $m(\text{arc } LN) = 110^\circ$ ,  $m(\text{arc } PQ) = 50^\circ$

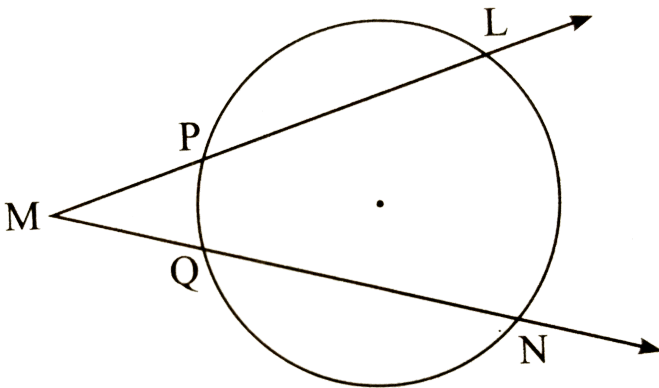
then complete the following activity to find  $\angle LMN$

$$\angle LMN = \frac{1}{2} [m(\text{arc } LN) - \square]$$

$$\therefore \angle LMN = \frac{1}{2} [\square - 50^\circ]$$

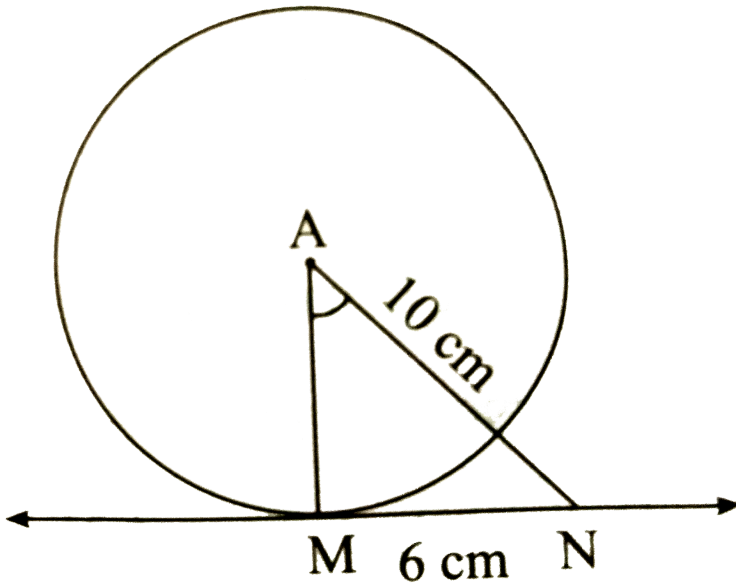
$$\therefore \angle LMN = \frac{1}{2} \times \square$$

$$\therefore \angle LMN = \square$$



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10. In the figure, A is the centre of the circle.  $AN = 10\text{ cm}$ .  
Line MN touches the circles in point M. If  $MN = 6\text{ cm}$  then  
find the radius of the circle.



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11. Two circles intersect each other in points A and B. Seg AB is the chord of both the circles . Point C is in the exterior point of both the circles on the line AB. From the point C tangents are drawn to the circles touching at M and N as shown. Completely the following to prove  $CM = CN$ .

Proof :

$$CM^2 = CA \times \square \dots(\square) \dots(1)$$

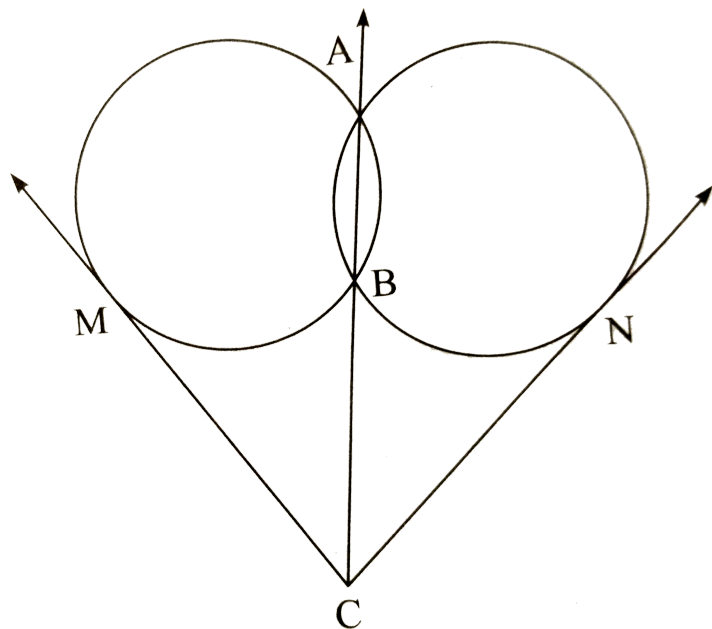
$$CN^2 = \square \times CB \dots(\text{Tangent secant segment property})$$

....(2)

$\therefore$  From (1) and (2),

$$CM^2 = \square$$

$$\therefore CM = CN$$



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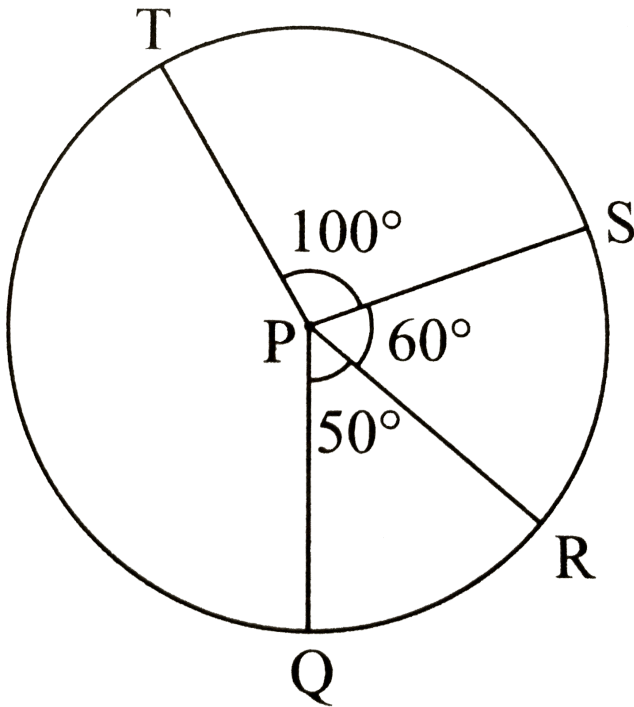
**ASSIGNMENT 4.4**



1. In the figure, P is the centre of the circle. If

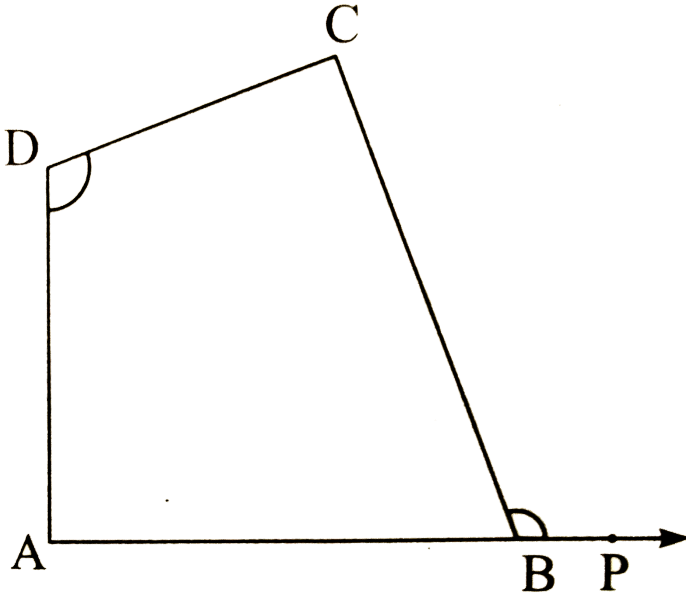
$\angle QPR = 50^\circ$ ,  $\angle RPS = 60^\circ$ ,  $\angle SPT = 100^\circ$  then find

(1)  $m(\text{arc QRS})$  (ii)  $m(\text{arc QST})$  (iii)  $m(\text{arc RTS})$



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2. In the figure, if  $\angle ADC = \angle CBP$  then prove that  $\square ABCD$  is cyclic.



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3. square ABCD is a cyclic quadrilateral in which  $AB = AD$  .

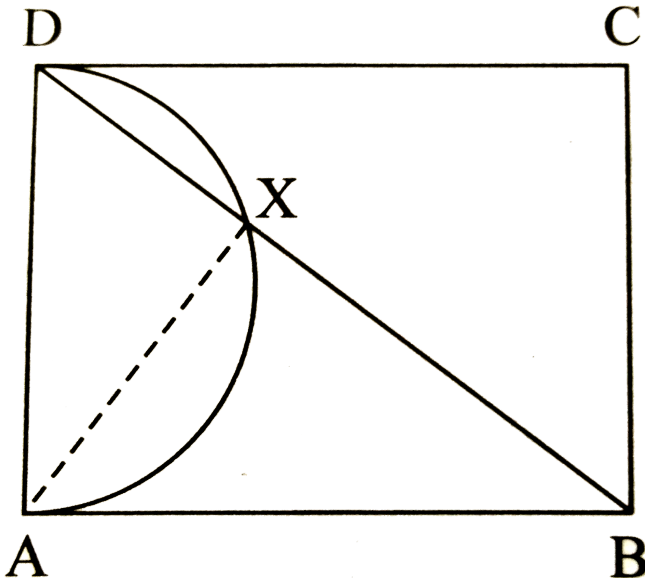
$\angle BCD = 70^\circ$  . Find (i)  $m$  (arc BCD) (ii)  $m$  (arc BAD) (iii)

$\angle ADB$



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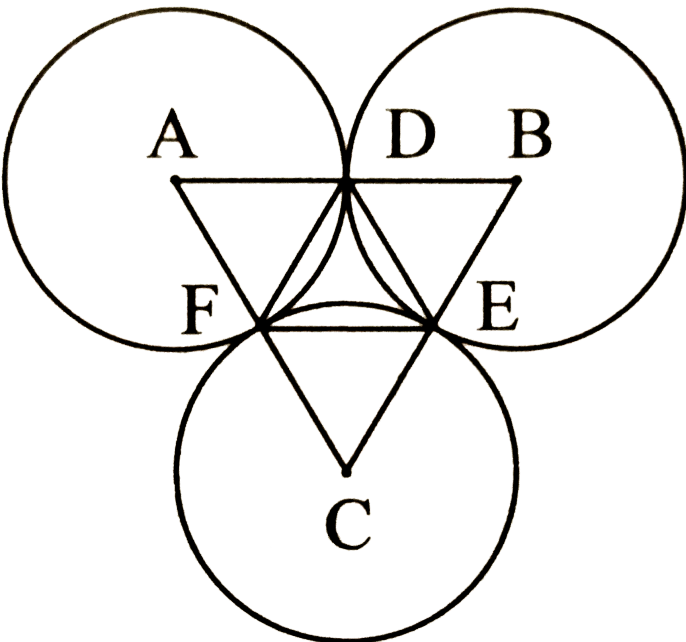
4.  $\square ABCD$  is a rectangle. Taking  $AD$  as a diameter a semicircle  $AXD$  is drawn which intersects diagonal  $BD$  at  $X$ . If  $AB = 12$  cm ,  $AD = 9$  cm , find the values of (i)  $BD$  (ii)  $BX$ .



5. Circles with centres A,B,C and radius 5 cm each, touch each other externally in the points D,E, and F as shown in the figure.

(i) What is the perimeter of  $\triangle ABC$ ?

(ii) What is the length of side of side DE and  $\triangle DEF$ ?





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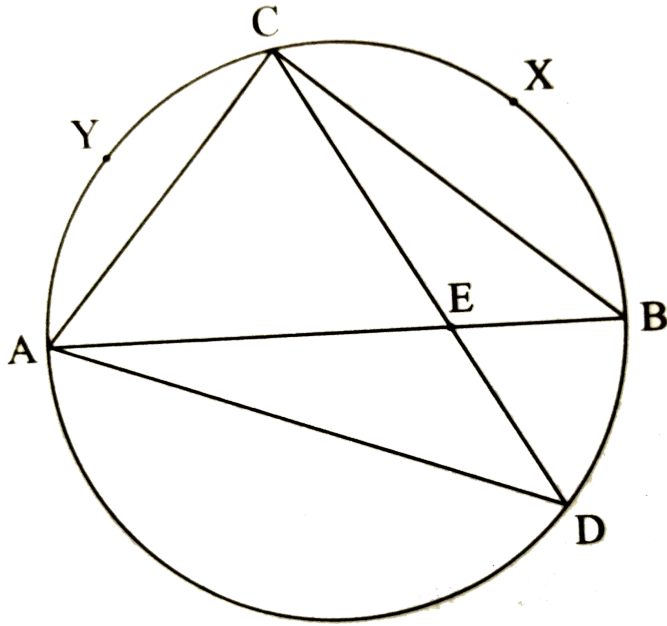
6. In the figure, diameter  $AB$  and chord  $CD$  intersect in point  $E$ .

If  $m(\text{arc } CXB) = 100^\circ$ . Find

(i)  $\angle ADC$

(ii)  $\angle CDB$

(iii)  $\angle ACB$



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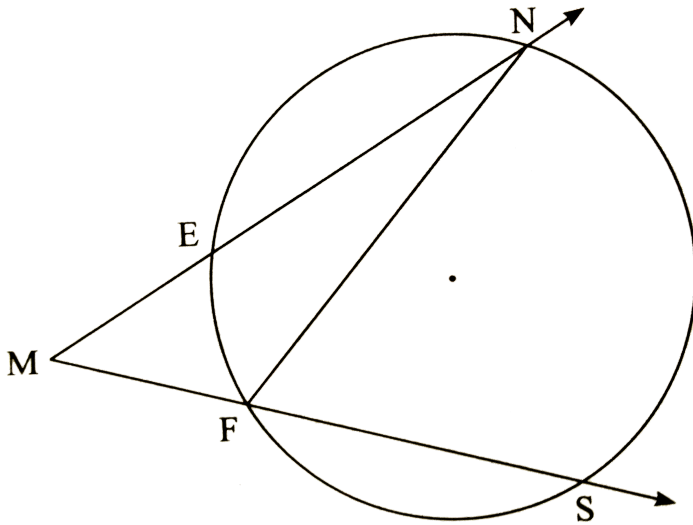
7. In the figure,  $m(\text{arc } NS) = 130^\circ$

$m(\text{arc } EF) = 60^\circ$ . Find

(i)  $\angle NMS$

(ii)  $\angle ENF$

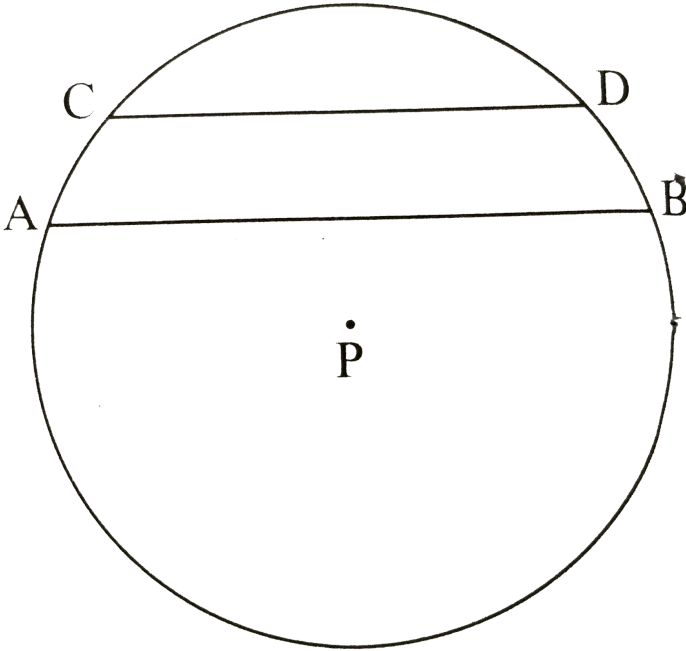
(iii)  $\angle NFS$



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8. In the figure, two chords AB and CD are parallel to each other. P is the centre of the circle.

Show that  $\angle CPA \cong \angle DPB$ .

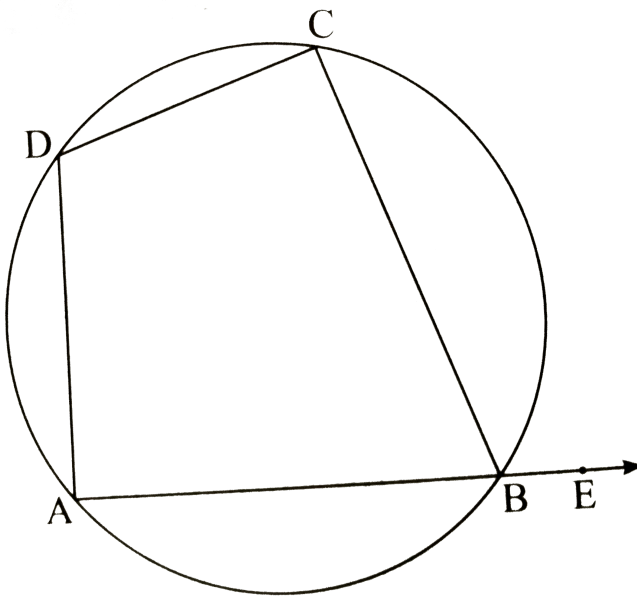


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9.  $\square ABCD$  is a cyclic quadrilateral,  $m(\text{arc } ABC) = 220^\circ$

then find  $\angle ABC$ ,  $\angle CDA$  and  $\angle CBE$

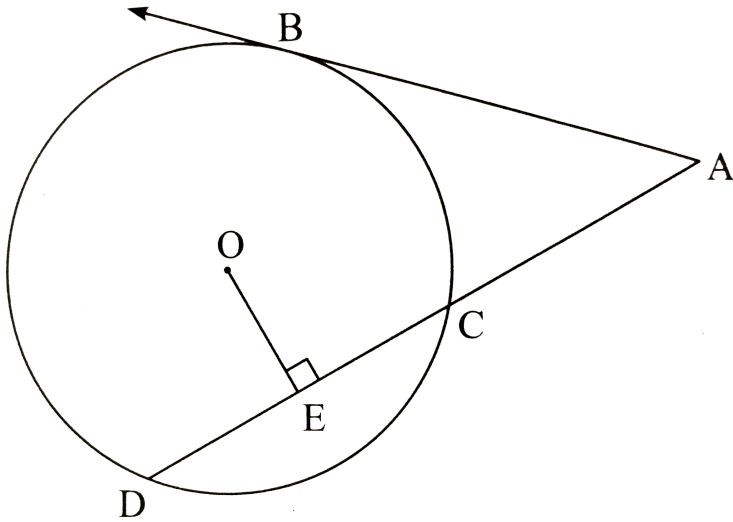




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10. In the figure,  $O$  is the centre of the circle and  $B$  is a point of contact. Seg  $OE \perp$  seg  $AD$ ,  $AB = 12$ ,  $AC = 8$ , find

(i) AD (ii) DC (iii) DE.



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**11.** In the figure,  $O$  is the radius of the circle. From point  $R$ , seg  $RM$  and seg  $RN$  are tangent segments touching the circle at  $M$  and  $N$ . If  $OR = 10\text{cm}$  and radius of the circle =  $5\text{ cm}$ , then (i) What is the length of each tangent

segment ? (iii) What is the measure of  $\angle MRO$  ? (iii)

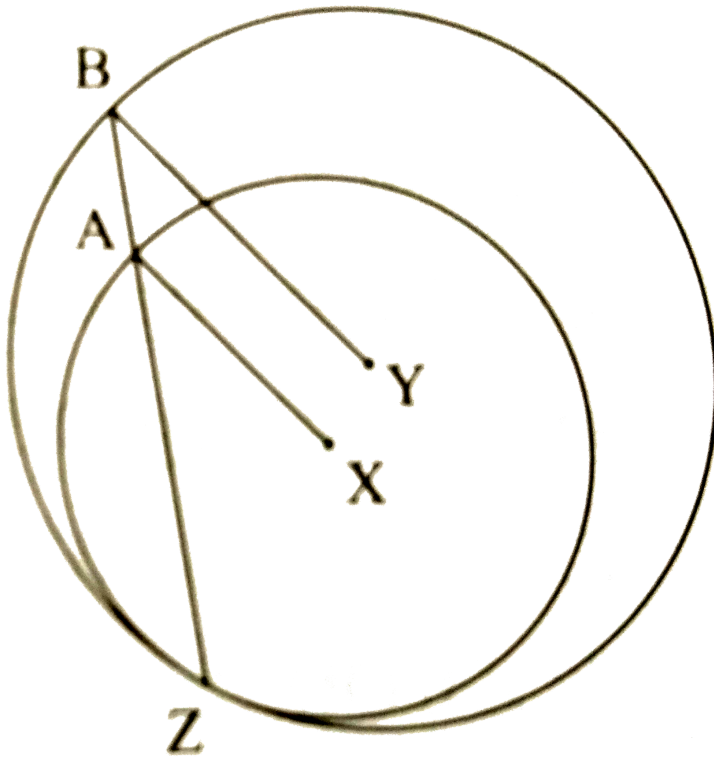
What is the measure of  $\angle MRN$  ?



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**12.** In the figure , circles with centres X and Y touch internally at point Z. Seg BZ is the chord of bigger circle and it intersects smaller k circle at point A.

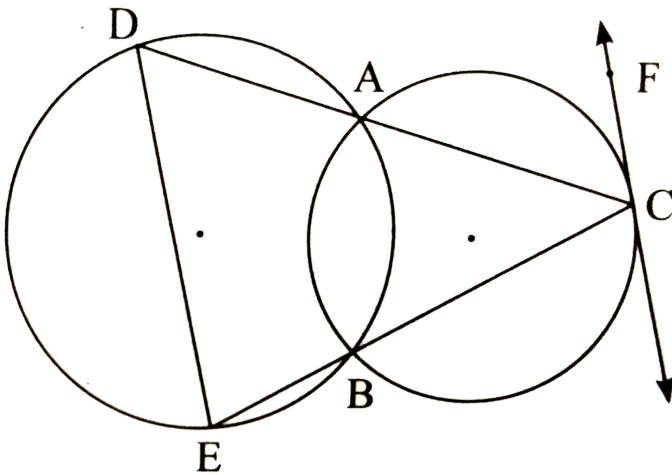
Prove that  $\text{seg } AX \parallel \text{seg } BY$ .



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ASSIGNMENT 4.5

1. In the figure, two circles intersect each other at points A and B. C is a point on the smaller circle. Secant CA and secant CB of the smaller circle intersect the bigger circle at points D and E respectively then prove :  $\text{seg DE} \parallel \text{line CF}$



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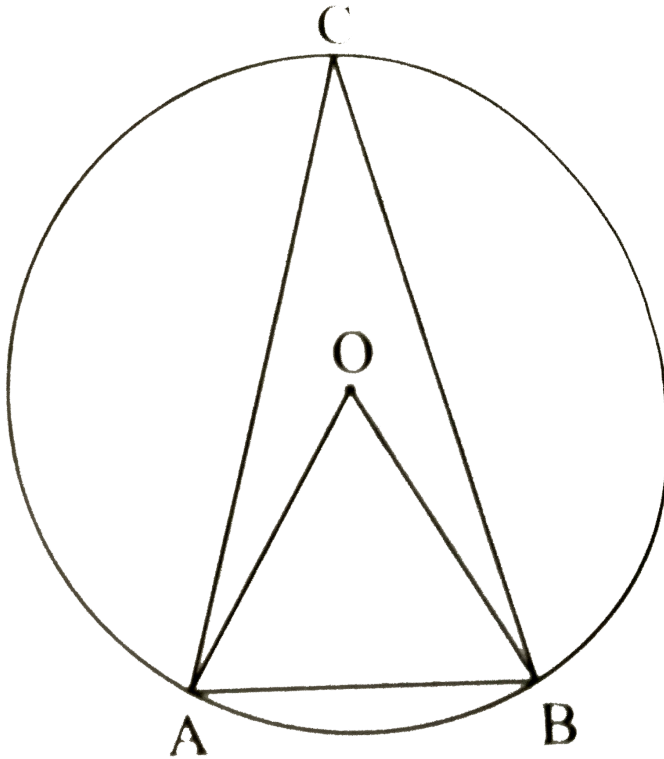
2. In the figure , in a circle with centre O, length of chord AB is equal to the radius of the circle. Find the measure of each of the following :

(1)  $\angle AOB$

(2)  $\angle ACB$

(3) arc AB

(4) arc ACB

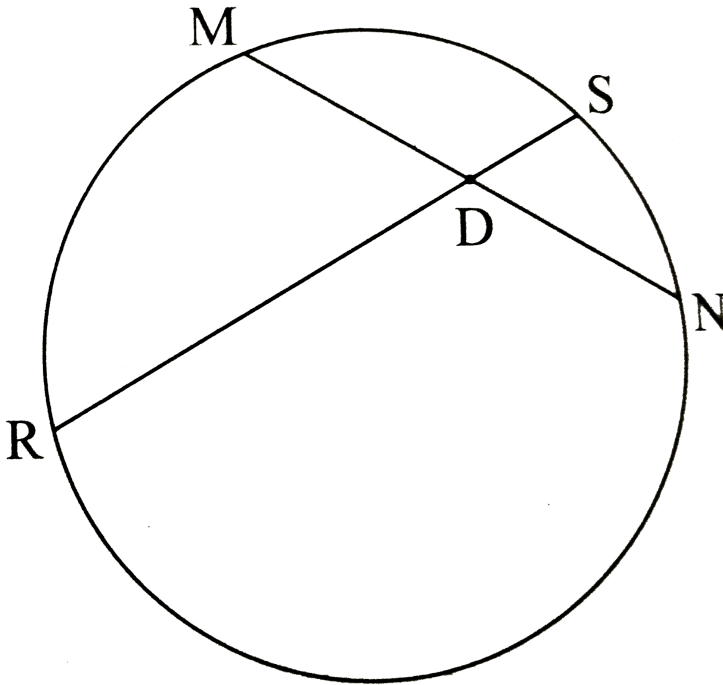


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3. In the figure, chord MN and chord RS intersect at point D.

(1) If  $RD = 15$ ,  $DS = 4$ ,  $MD = 8$ , find  $DN$ .

92) If  $RS = 18$ ,  $MD = 9$ ,  $DN = 8$ , find  $DS$ .



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4. In the figure, circle with centre  $M$  touches the circle with centre  $N$  at point  $T$ . Radius  $RM$  touches the smaller



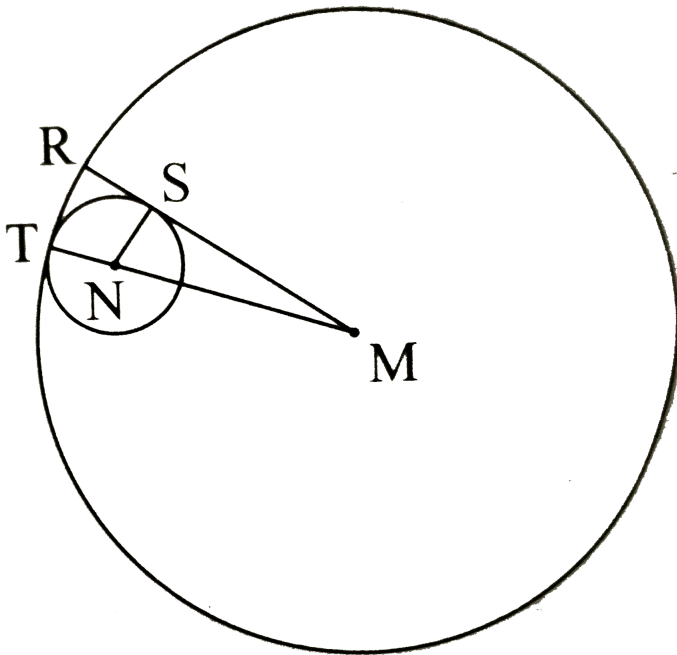
circle at S. Radii of circles are 9 cm and 2.5 cm. Find the answers to the following questions hence find the ratio

MS: SR

(1) Find the length of segment MT

(2) Find the length of seg MN

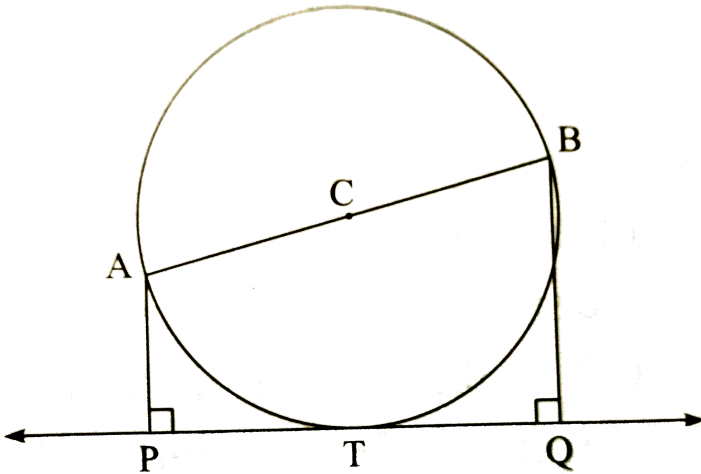
(3) Find the measure of  $\angle NSM$ .



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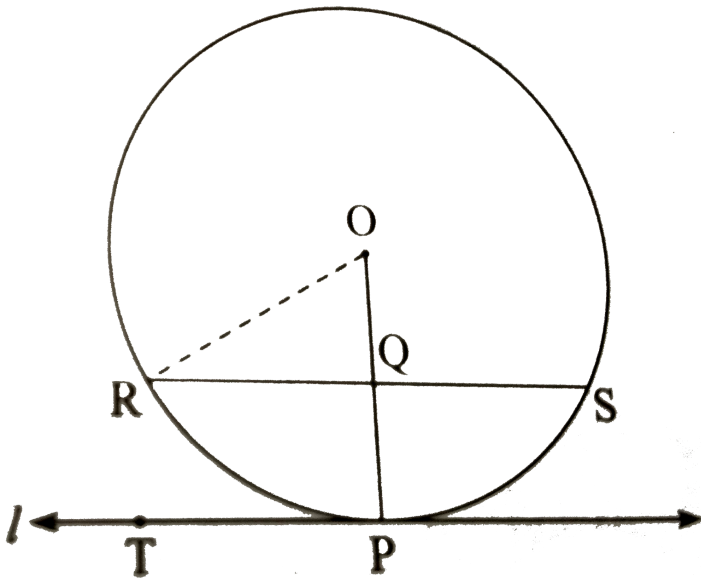
5. In the figure, seg  $AB$  is a diameter of a circle with centre  $C$ . Line  $PQ$  is a tangent, which touches the circle at point  $T$ . seg  $AP \perp$  line  $PQ$  and seg  $BQ \perp$  line  $PQ$ .

Prove that, seg  $CP \cong$  seg  $CQ$ .



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6. In the figure, line  $l$  touches the circle with centre  $O$  at point  $P$ .  $Q$  is the midpoint of radius  $OP$ .  $RS$  is a chord through  $Q$  such that chords  $RS \parallel$  line  $l$ . If  $RS = 12$ , find the radius of the circle.



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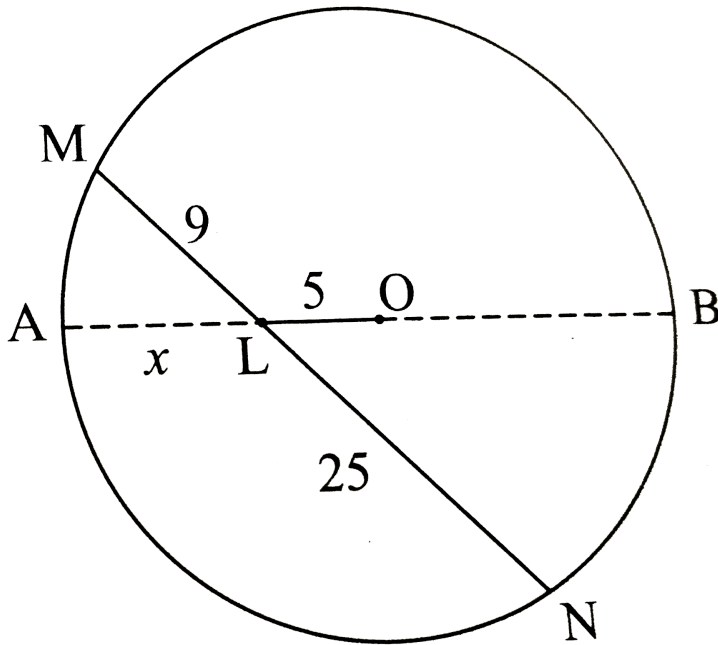
7. Prove that any three points on a circle cannot be collinear.



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8. In the figure, segment  $MN$  is a chord of a circle with centre  $O$ .  $MN = 15$ ,  $L$  is a point on chord  $MN$  such that  $ML = 9$

and  $d(O, L) = 5$ . Find the radius of the circle.



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**EXAMPLES FOR PRACTICE**

1. How many circles can be drawn to pass through three non-collinear points 1 (b) 2 (c) 0 (d) as many as possible

A. 1

B. 0

C. 2

D. 3

**Answer: A**



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2. A tangent AB, at a point A of a circle of radius 5 cm, meets a line through the centre O at point B such that

OB = 12 cm. Length AB is

A. 5 cm

B. 12 cm

C. 13 cm

D.  $\sqrt{119}$  cm

**Answer: D**



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3. If tangents PA and PB from a point P to a circle with centre O are inclined to each other at an angle of  $70^\circ$ , then  $\angle POA$  is equal to

A.  $70^\circ$

B.  $55^\circ$

C.  $100^\circ$

D.  $40^\circ$

**Answer: B**



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4. If TP and TQ are two tangents to a circle with centre O, so that  $\angle POQ = 120^\circ$ , then  $\angle PTQ$  is equal to

A.  $120^\circ$

B.  $30^\circ$



C.  $60^\circ$

D.  $90^\circ$

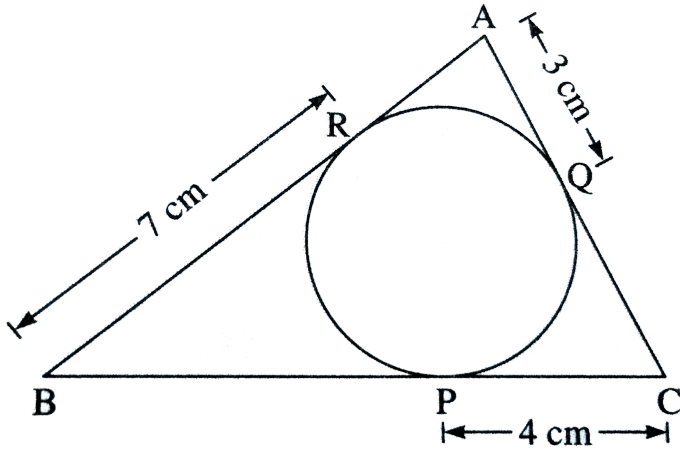
**Answer: C**



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5. In the figure, sides of  $\triangle ABC$  are tangents to the circle touching the circle at points P, Q and R as shown. If  $AQ=3$  cm,  $BR=7$  cm and  $PC=4$  cm, then perimeter of

$\triangle ABC$  is



A.  $14\text{ cm}$

B.  $28\text{ cm}$

C.  $20\text{ cm}$

D. cannot be determined

**Answer: B**



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6. AP is tangent to the circle with centre O at point A.  $OP = 10$  cm and  $\angle OPA = 30^\circ$ . The radius of the circle is

A. 10 cm

B.  $5\sqrt{3}$  cm

C. 5 cm

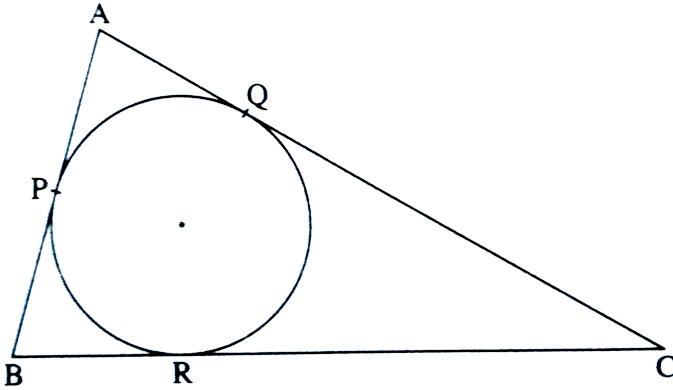
D.  $10\sqrt{3}$  cm

**Answer: C**



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7. In the given figure, if  $AP = PB$ , then



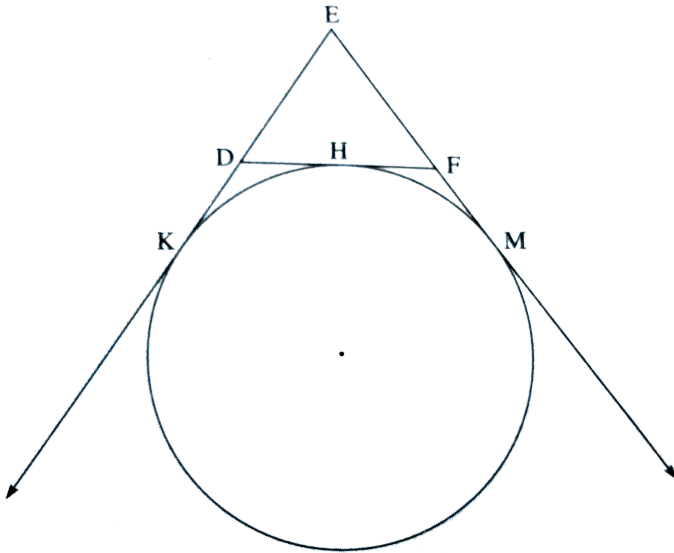
- A.  $AC = AB$
- B.  $AC = BC$
- C.  $AB = BC$
- D.  $AQ = QC$

**Answer: B**



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8. In the figure, a circle touches the side  $DF$  of  $\triangle EDF$  at  $H$  and touches line  $ED$  and  $EF$  at points  $K$  and  $M$  respectively. If  $EK = 9\text{cm}$ , then perimeter of  $\triangle EDF$  is



A. 18 cm

B. 9 cm

C. 13.5 cm

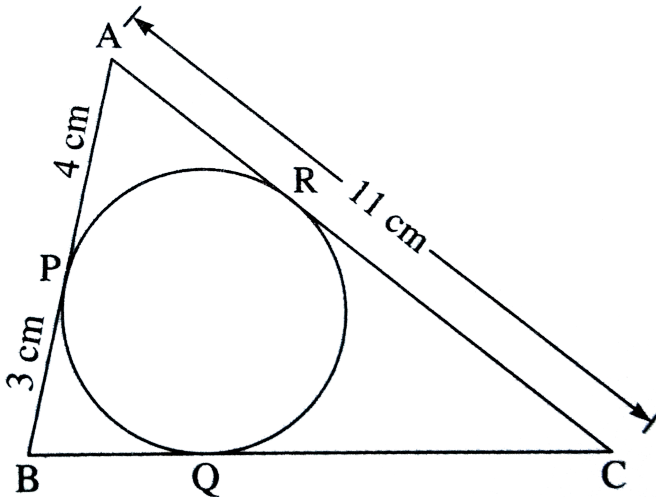
D. cannot be determined

Answer: A



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9. The side AB, BC and CA of triangle ABC touch a circle at P, Q and R respectively. If  $PA = 4$  cm,  $BP = 3$  cm and  $AC = 11$  cm, then length of BC is



A. 11 cm

B. 10 cm

C. 14 cm

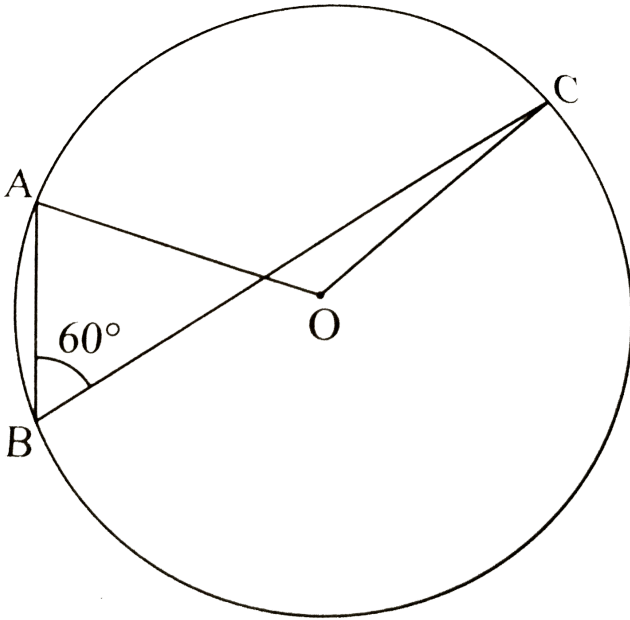
D. 15 cm

**Answer: B**



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10. In the figure, if  $\angle ABC = 60^\circ$ , then  $\angle AOC =$



A.  $120^\circ$

B.  $60^\circ$

C.  $30^\circ$

D.  $90^\circ$

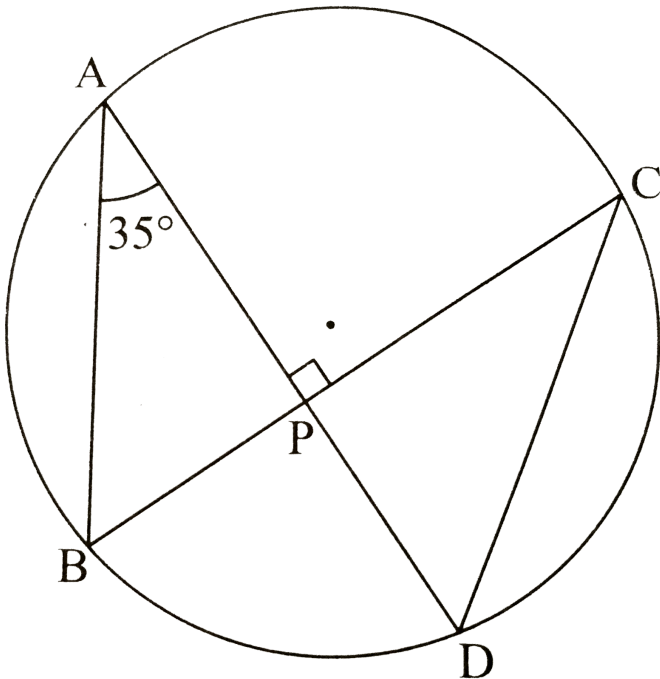


Answer: A



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11. In the figure, chords AD and BC intersect each other at right angles at a point P. If  $\angle DAB = 35^\circ$ , then  $\angle ADC =$



A.  $35^\circ$

B.  $55^\circ$

C.  $65^\circ$

D.  $45^\circ$

**Answer: B**



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12. PQRS is a cyclic quadrilateral such that PR is the diameter of the circle. If  $\angle QPR = 50^\circ$  and  $\angle SPR = 60^\circ$ , then  $\angle QRS = \dots\dots$

A.  $50^\circ$

B.  $60^\circ$

C.  $110^\circ$

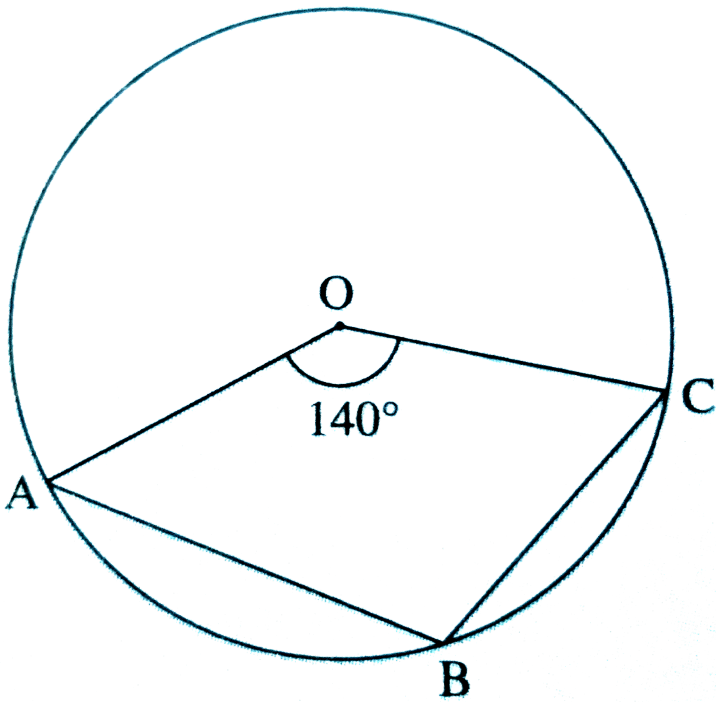
D.  $70^\circ$

**Answer: D**



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**13.** In the figure,  $O$  is the centre of the circle such that  $\angle AOC = 140^\circ$ , then  $\angle ABC = \dots\dots$



A.  $140^\circ$

B.  $110^\circ$

C.  $70^\circ$

D.  $90^\circ$

**Answer: B**



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14. If P,Q,R are three points which lie on the circle with centre O such that  $\angle POQ = 110^\circ$ ,  $\angle QOR = 130^\circ$ , then  $\angle PQR = \dots\dots\dots$

A.  $110^\circ$

B.  $130^\circ$

C.  $60^\circ$

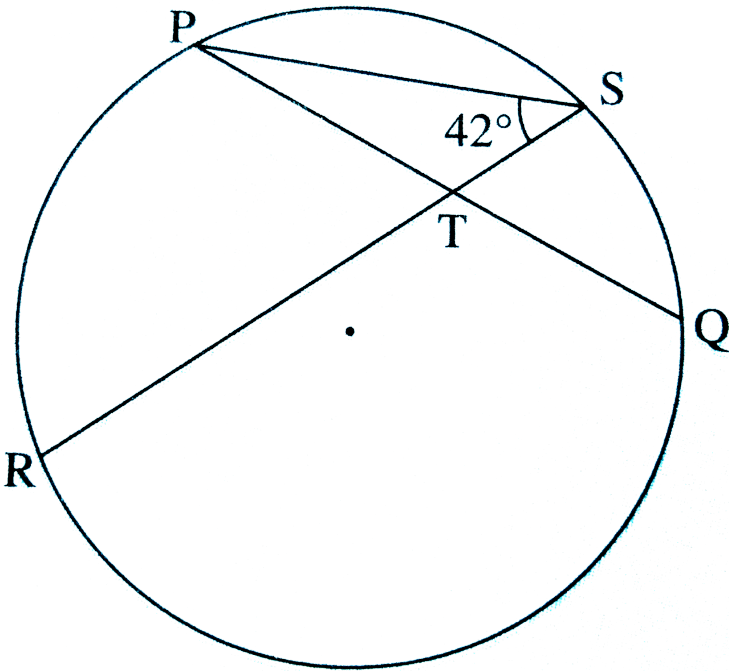
D.  $120^\circ$

**Answer: C**



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15. In the figure, chords PQ and RS intersect at T as shown. If  $\angle PSR = 42^\circ$  and  $m(\text{arc } SQ) = 42^\circ$ , then  $\angle STQ = \dots\dots\dots$



- A.  $63^\circ$
- B.  $42^\circ$
- C.  $90^\circ$

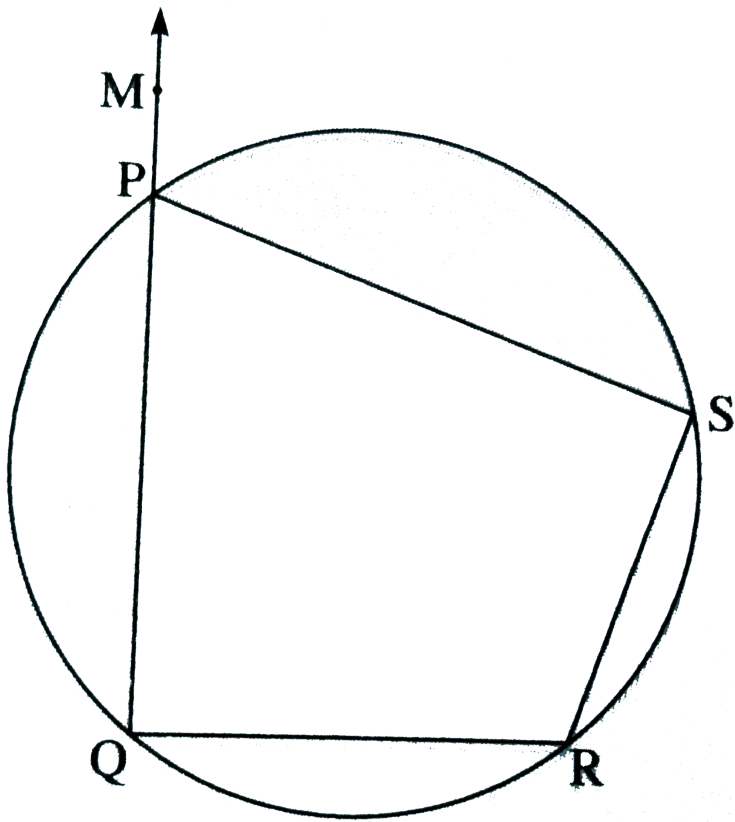
D. cannot be determined

**Answer: A**



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**16.** In the figure,  $\square PQRS$  is cyclic,  $\angle SPQ = 7x^\circ$  and  $\angle SRQ = 11x^\circ$ , then  $\angle MPS = \dots\dots\dots$



A.  $70^\circ$

B.  $110^\circ$

C.  $120^\circ$

D.  $60^\circ$



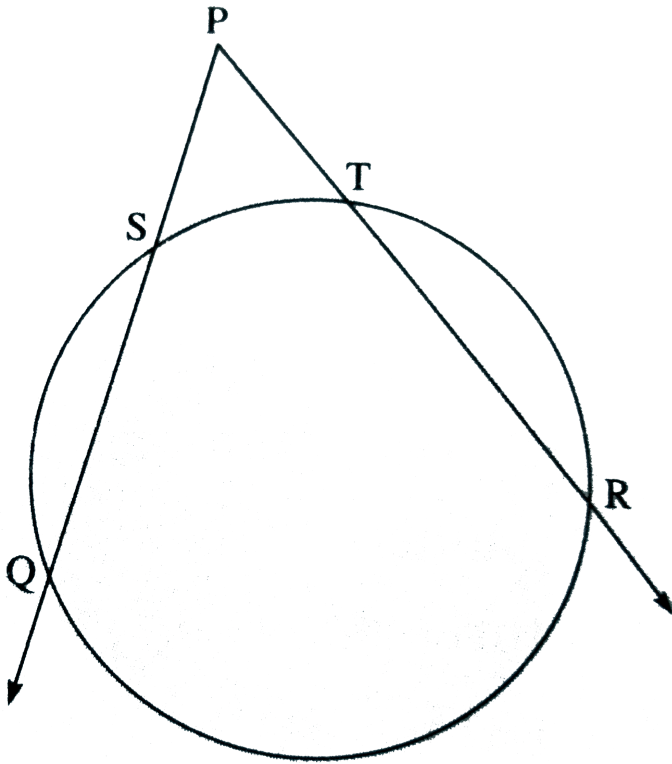
**Answer: B**



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17. In the figure,  $\angle QPR$  has its vertex outside the circle such that  $m(\text{arc } QR)=200^\circ$  and  $m(\text{arc } ST)=90^\circ$ , then

$\angle QPR = \dots\dots\dots$



- A.  $45^\circ$
- B.  $100^\circ$
- C.  $110^\circ$
- D.  $55^\circ$

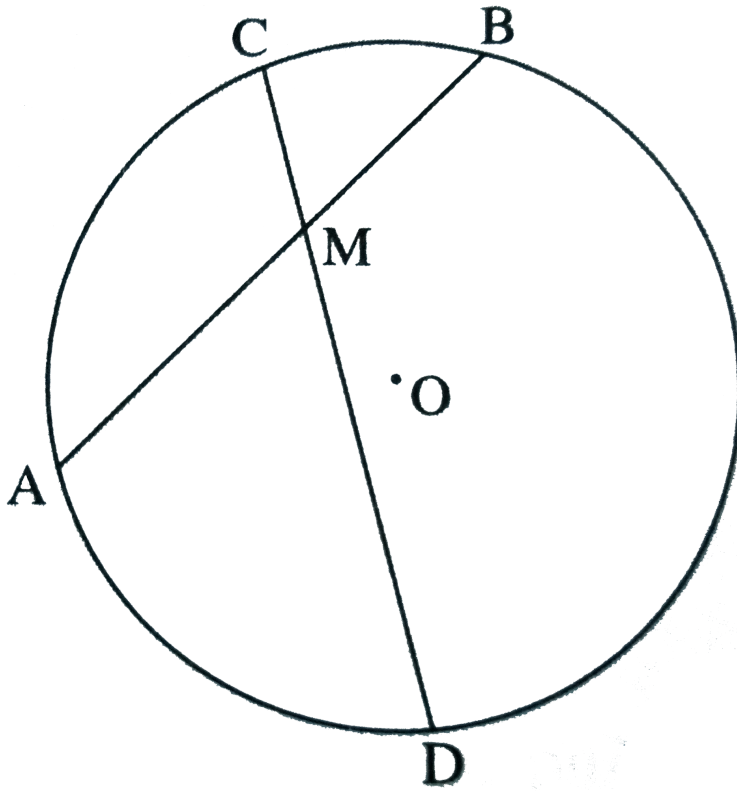
**Answer: D**



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**18.** In the figure, chord AB and chord CD intersect at point M inside the circle such that  $AM=4$ ,  $BM=3$ ,  $CM=2$ ,

then  $CD = \dots\dots\dots$



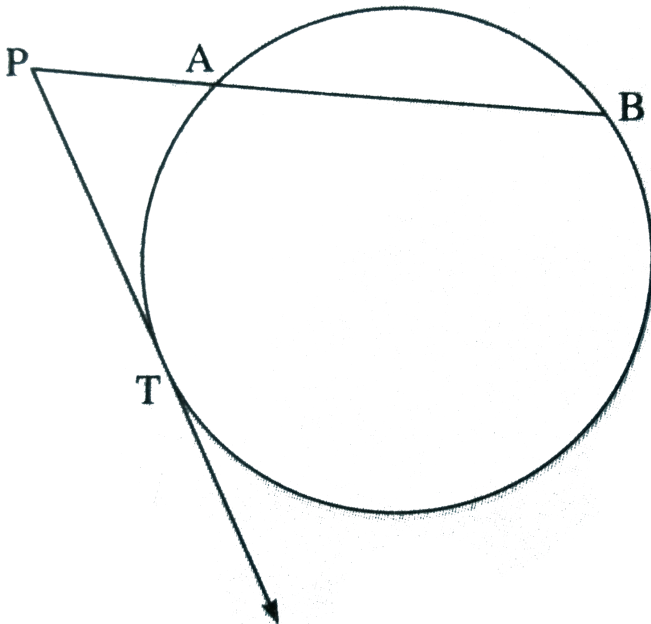
- A. 6
- B. 3
- C. 7
- D. 8

Answer: D



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19. In the figure, ray  $PT$  touches the circle at point  $T$  and line  $PAB$  is secant intersecting the circle at points  $A$  and  $B$ , then



A.  $PT = PA \times PB$

B.  $PT^2 = \sqrt{PA \times AB}$

C.  $PT^2 = PA \times PB$

D.  $PT^2 = PA^2 \times PB^2$

**Answer: C**



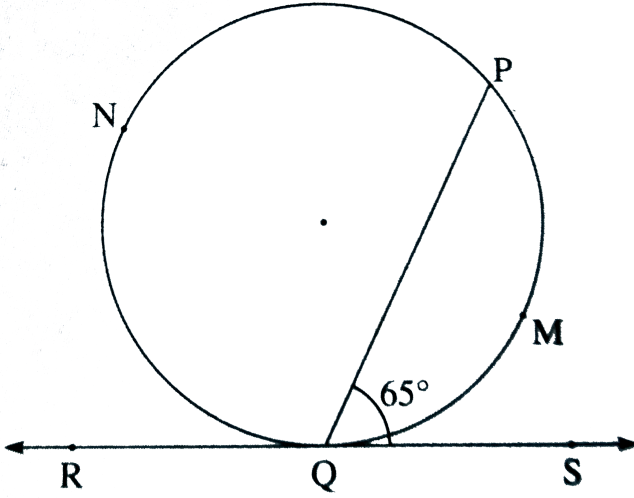
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**20.** Find the length of tangent segment drawn to a circle with radius 5 cm from a point 13 cm from the centre of the circle.



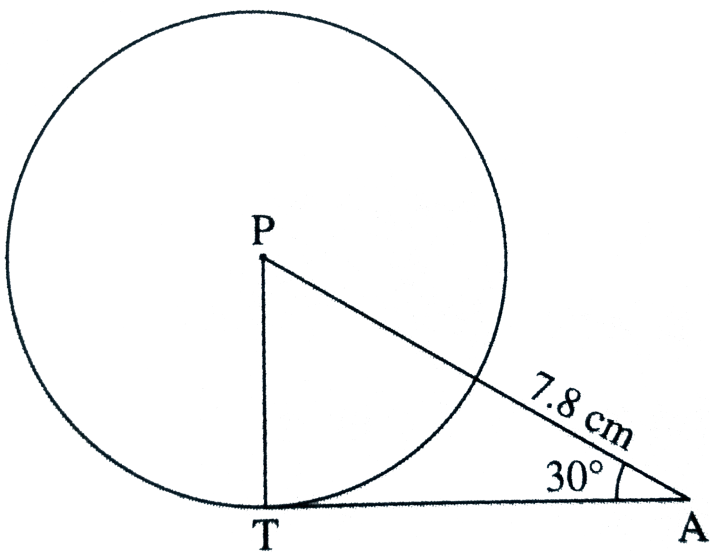
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21. In the figure, line RS is tangent at point Q. If  $\angle PQS = 65^\circ$  find  $m(\text{arc PMQ})$  and  $m(\text{arc PNQ})$ .



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22. In the figure, line TA is tangent at point T,  $\angle PAT = 30^\circ$  and  $PA=7.8$  cm then find PT and TA.



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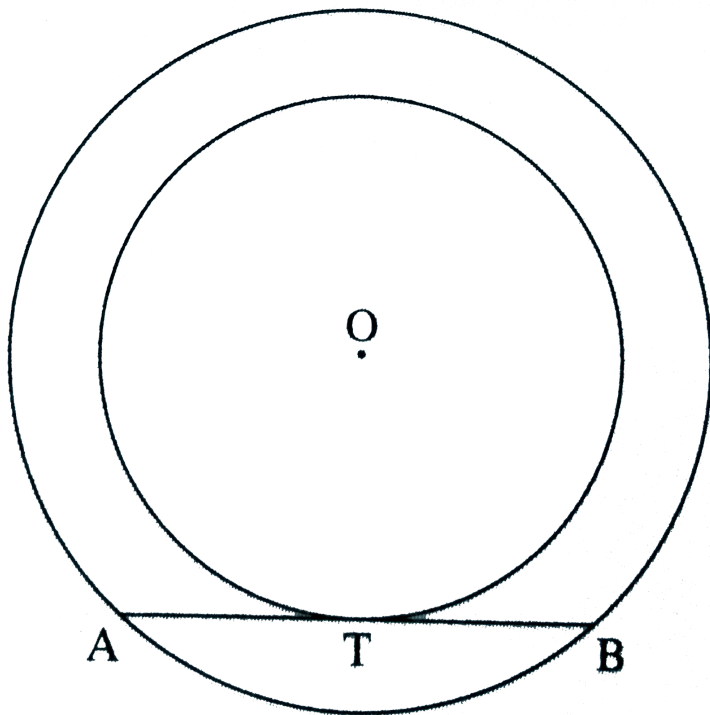
**23.** Two circles of radius 5 cm and 4 cm touch each other.

Find the distance between their centers.

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24. In the figure, two concentric circles are given and line  $AB$  is tangent to the smaller circle at  $T$ . Show that  $T$  is the midpoint of seg  $AB$ .

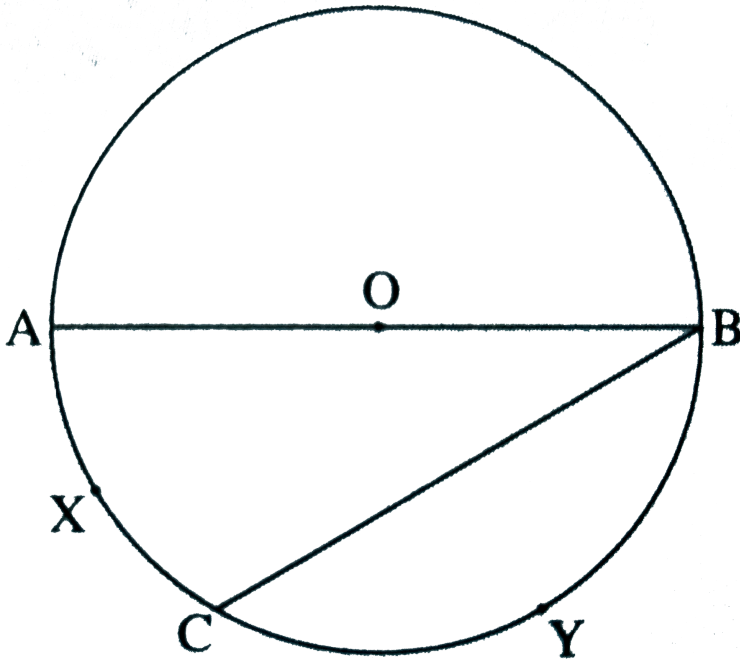


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25. In the figure, seg AB is the diameter of the circle,

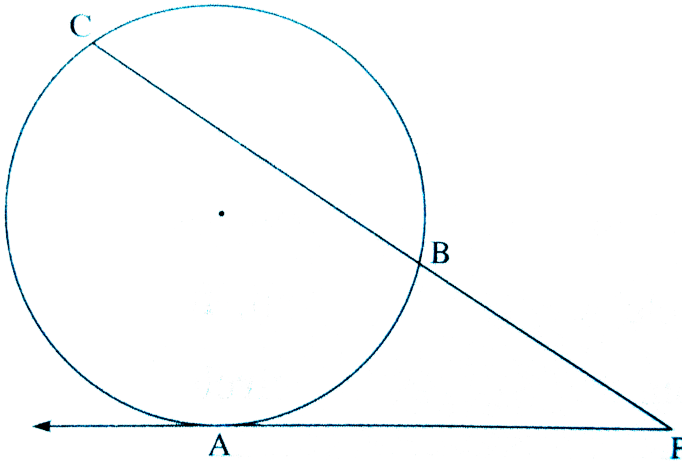
$\angle ABC = 30^\circ$ , Find (1)  $m(\text{arc } AXC)$

(2)  $m(\text{arc } BYC)$



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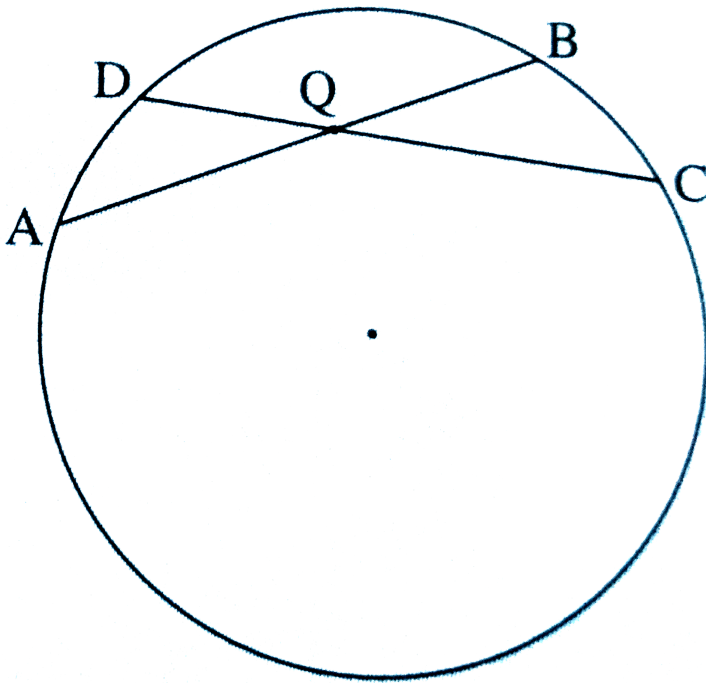
26. In the figure, a tangent segment PA touches the circle at point A and secant PBC intersects the circle at points B and C. If  $AP=15$  cm and  $BP=10$ , then find BC.



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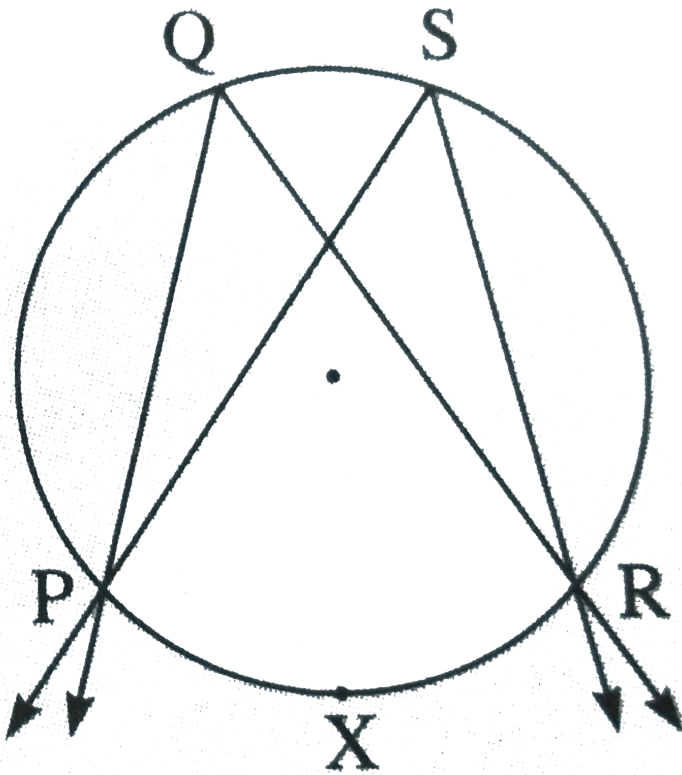
27. Chords AB and CD of a circle intersect in point Q in interior of a circle. If  $m(\text{arc AD})=25^\circ$  and  $m(\text{arc BC})=31^\circ$ ,

find  $\angle BQC$ .



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28. Prove that, angles inscribed in the same arc are congruent.



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**29.** Two circles intersect each other in points A and B. Seg AB is the chord of both the circles. Point C is in the exterior point of both the circles on the line AB. From

the point C tangents are drawn to the circles touching at M and N as shown. Completely the following to prove  $CM = CN$ .

Proof :

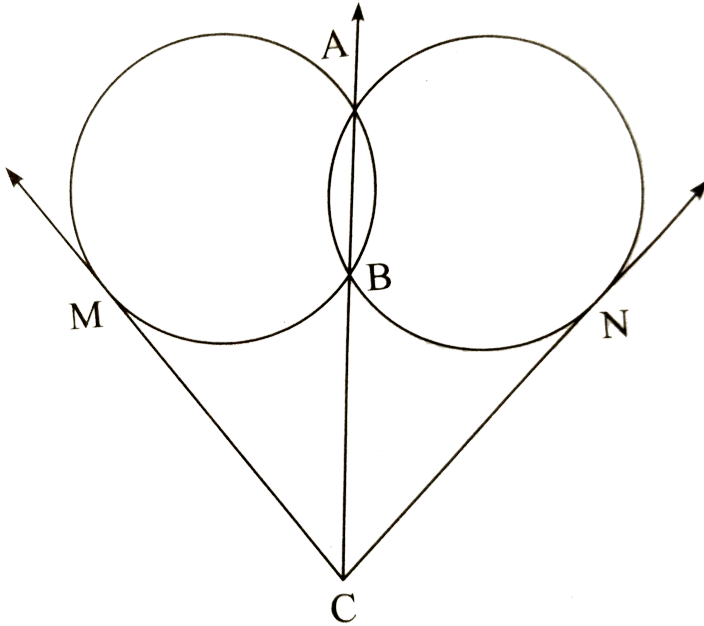
$$CM^2 = CA \times \square \dots(\square) \dots(1)$$

$$CN^2 = \square \times CB \dots(\text{Tangent secant segment property}) \dots(2)$$

$\therefore$  From (1) and (2),

$$CM^2 = \square$$

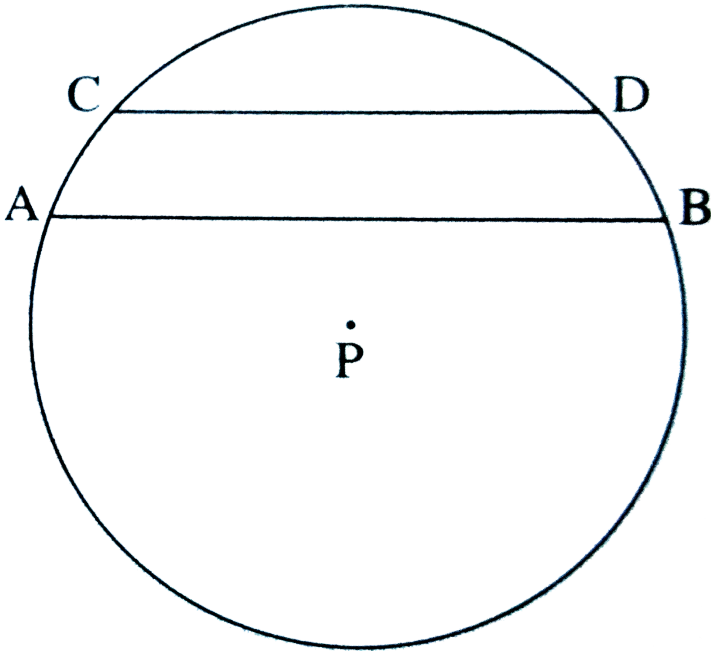
$$\therefore CM = CN$$



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**30.** In the figure, P is the centre of the circle. Two chords AB and CD are parallel to each other. Prove AB and CD are parallel to each other. Prove

$$\angle CPA = \angle DPB.$$

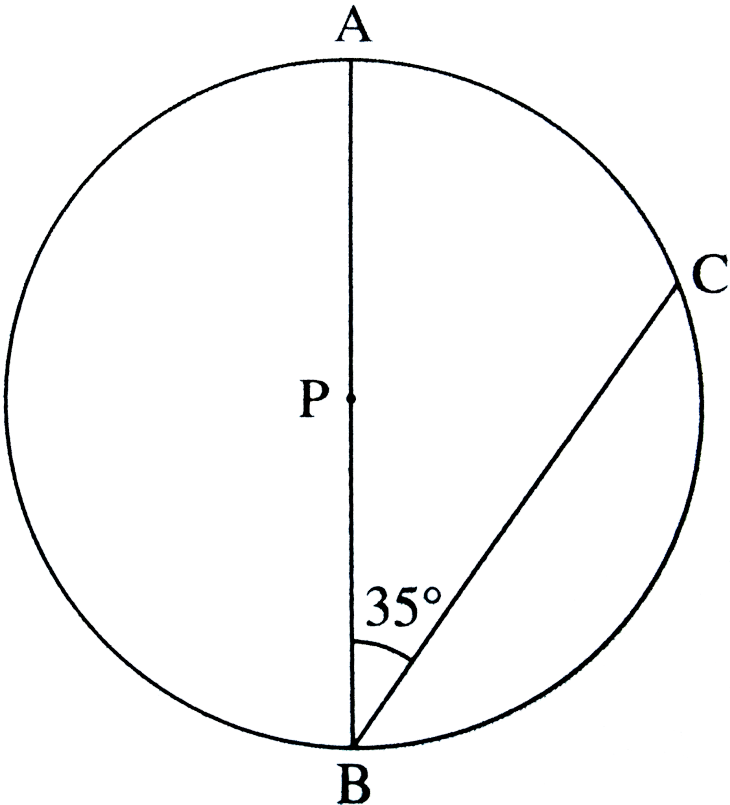


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**31.** Three circles touch each other pairwise externally. If the distance between their centres is 5 cm and 7 cm and 6 cm. Find their radii.



32. In the figure P is the centre and A and B are the endpoints of diameter of circle. C is a point of the circle such that  $\angle ABC = 35^\circ$ . Determine  $\angle BAC$ ,  $\angle PCB$  and  $\angle PCA$ .





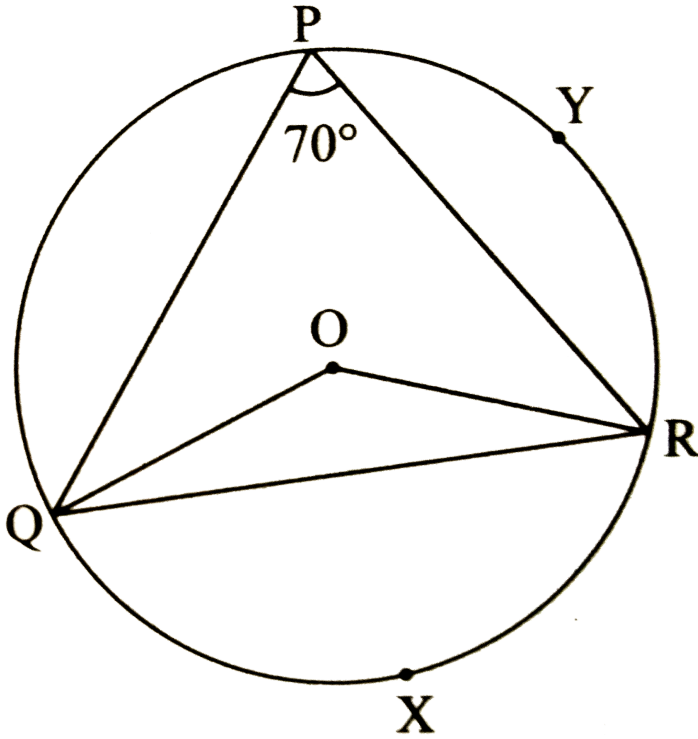
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**33.** In the figure,  $O$  is the centre of circle  $\angle QPR = 70^\circ$  and  $m(\text{arc } PYR) = 160^\circ$ , then find the value of each of the following :

(a)  $m(\text{arc } QXR)$

(b)  $\angle QOR$

(c)  $\angle PQR$



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34. As per the figure, two circles intersect each other at points  $P$  and  $Q$ . Point  $A$  is on  $PQ$  produced and  $AMD$  and

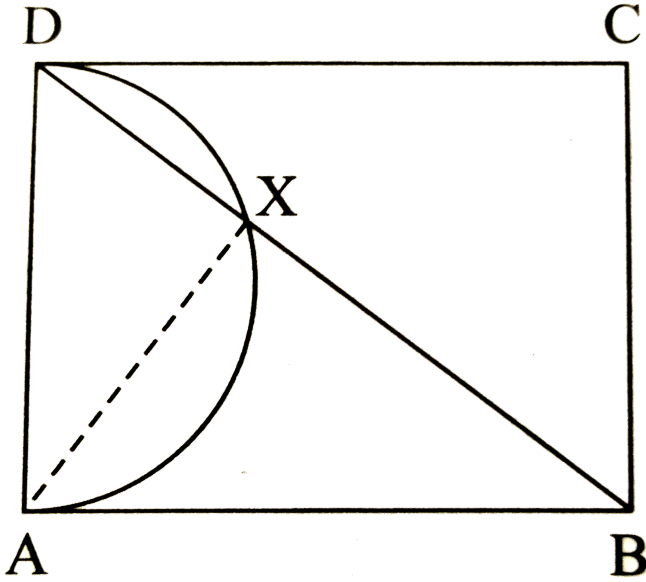
ASR are the secants to the circles. If  $AM = 3$ ,  $MD = 5$ ,  $AS = 4$ , The value of SR is :



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35.  $\square ABCD$  is a rectangle. Taking AD as a diameter a semicircle AXD is drawn which intersects diagonal BD at X. If  $AB = 12$  cm ,  $AD = 9$  cm , find the values of (i) BD (ii)

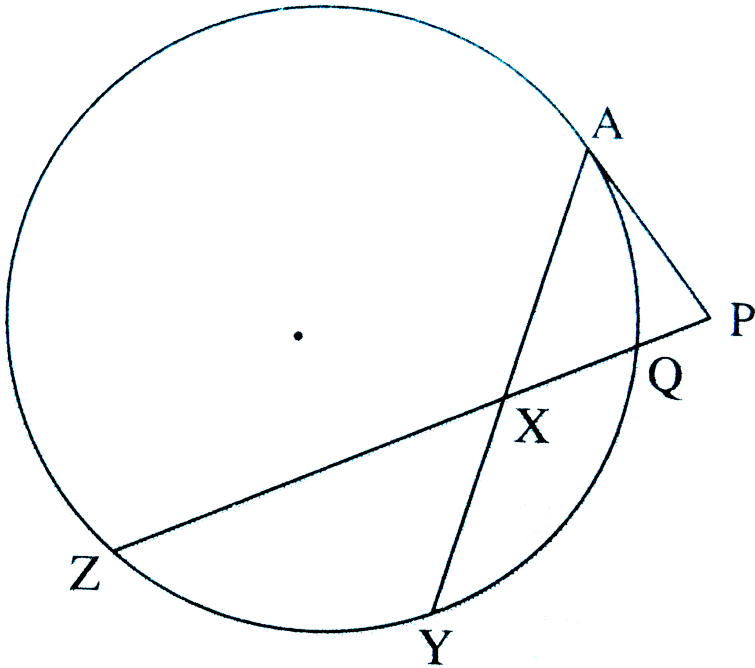
BX.



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**36.** As shown in the figure, AP is tangent to the circle at point A. Secant through P intersects chord AY in point X,

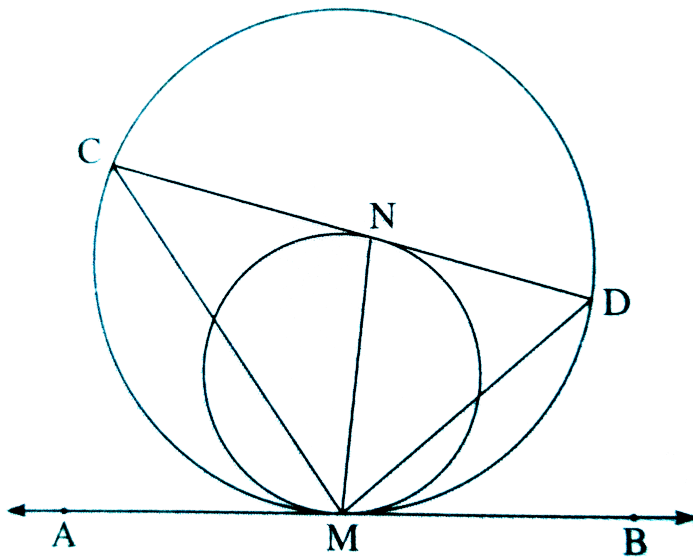
such that  $AP=PX=XY$ . If  $PQ = 1$ ,  $QZ = 8$ . Then find  $AX$



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37. In the figure,  $M$  is the point of contact of two internally touching circles. The chord  $CD$  of the bigger circle touches the smaller circle at point  $N$ . Line  $AMB$  is

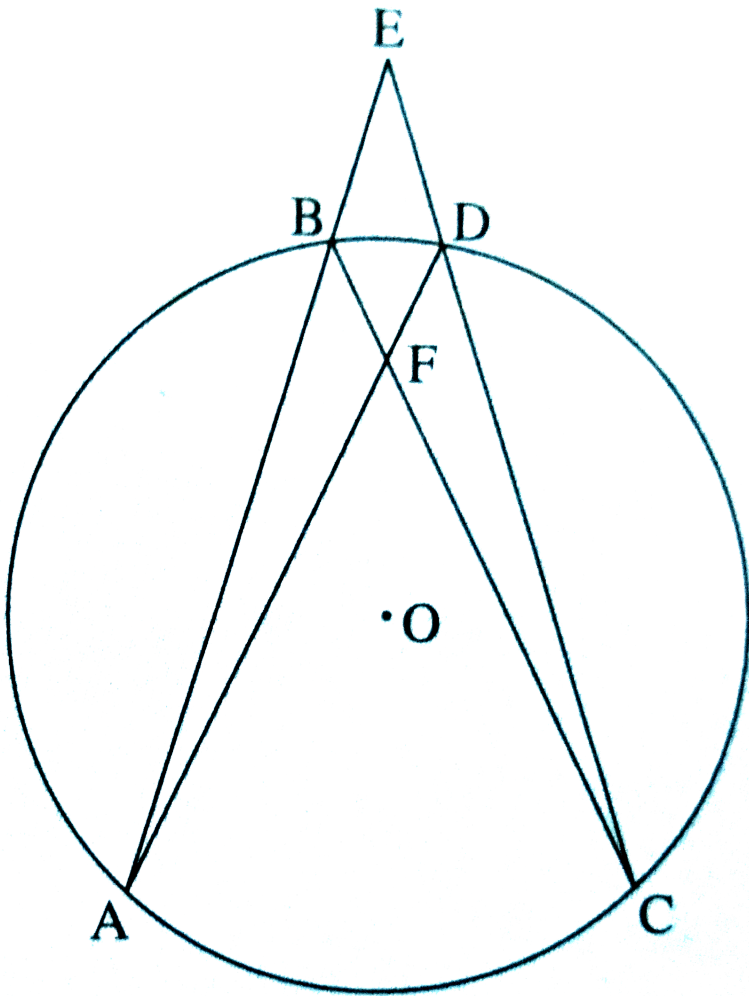
their common tangent. Prove  $MN$  bisects  $\angle CMD$



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**38.** In the figure,  $O$  is the centre of the circle. Prove

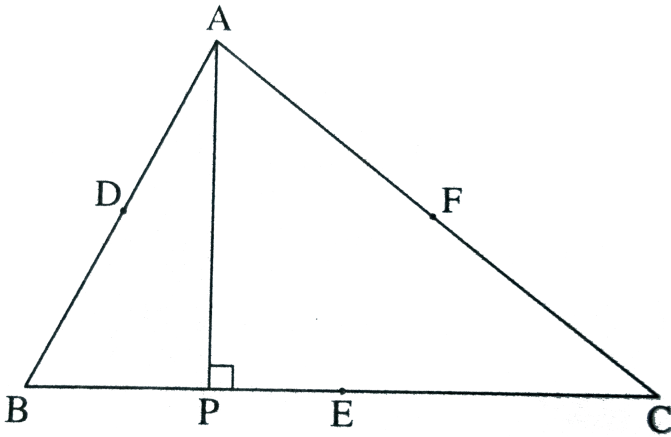
$$\angle AOC = \angle AFC + \angle AEC.$$



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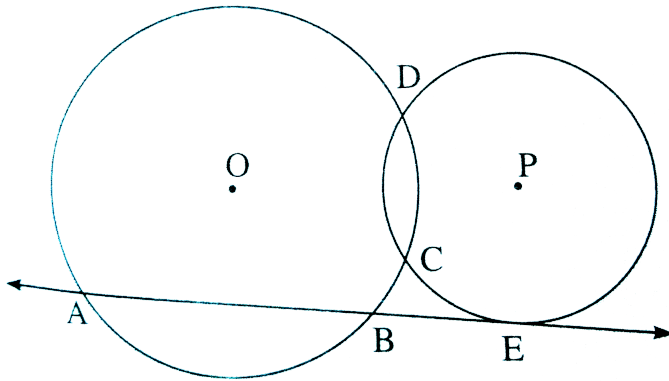
**39.** In the figure, D, E and F are midpoints of sides AB, BC and AC respectively. P is the foot of the perpendicular from A to side BC. Show that points D, E, F and P are concyclic.



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**40.** In the figure, two circles with centers O and P intersect each other at points D and C. Line AB intersects

the circle with centre O at points A and B and touches the circle with centre P at point E. Prove  $\angle ADE + \angle BCE = 180^\circ$ .



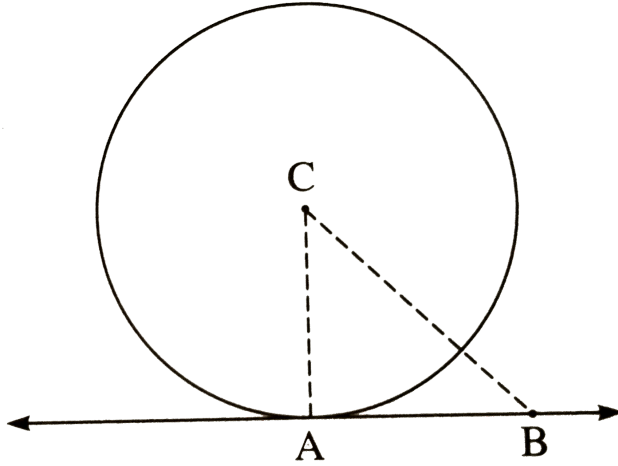
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### PRACTICE SET 3.1

1. In the figure, the radius of a circle with centre C is 6 cm, line AB is a tangent at A. Answer the following

questions.

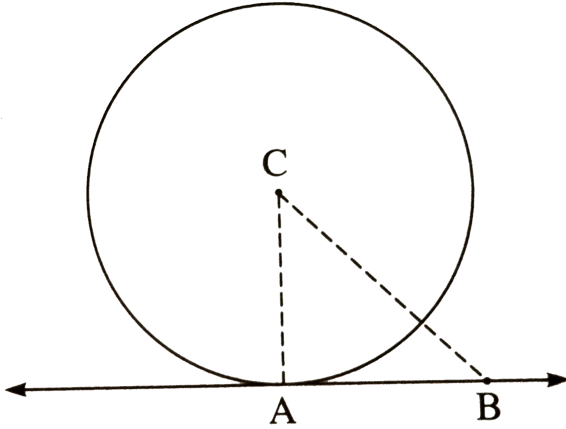
What is the measure of  $\angle CAB$ ? Why?.



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2. In the figure, the radius of a circle with centre C is 6 cm, line AB is a tangent at A. Answer the following questions.

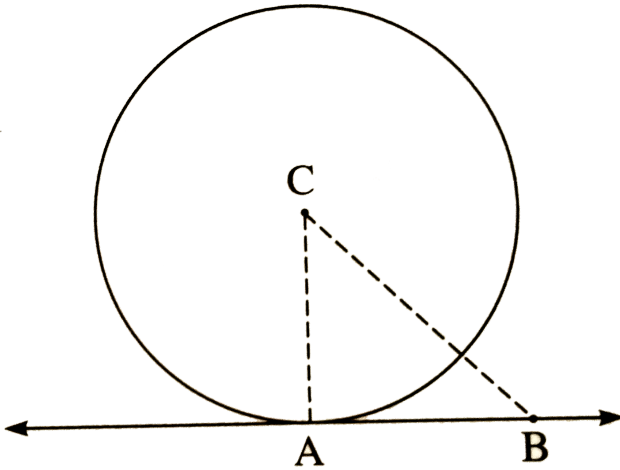
What is the distance of point C from line AB? Why?



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3. In the figure, the radius of a circle with centre C is 6 cm, line AB is a tangent at A. Answer the following questions.

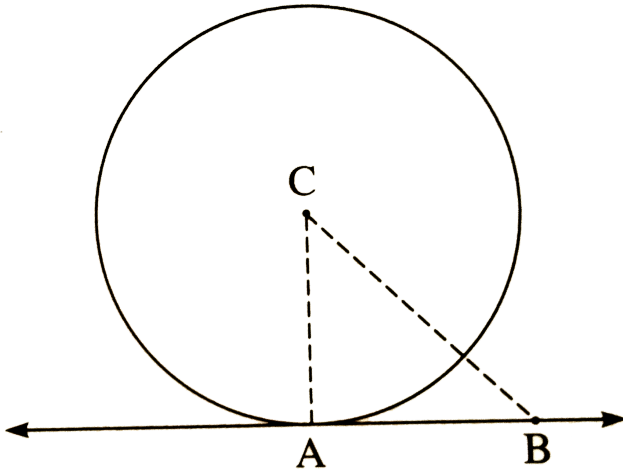
$d(A,B)=6\text{cm}$ , find  $d(B,C)$ .



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4. In the figure, the radius of a circle with centre C is 6 cm, line AB is a tangent at A and AB is 6 cm. Answer the following questions.

What is the measure of  $\angle ABC$ ? Why?.



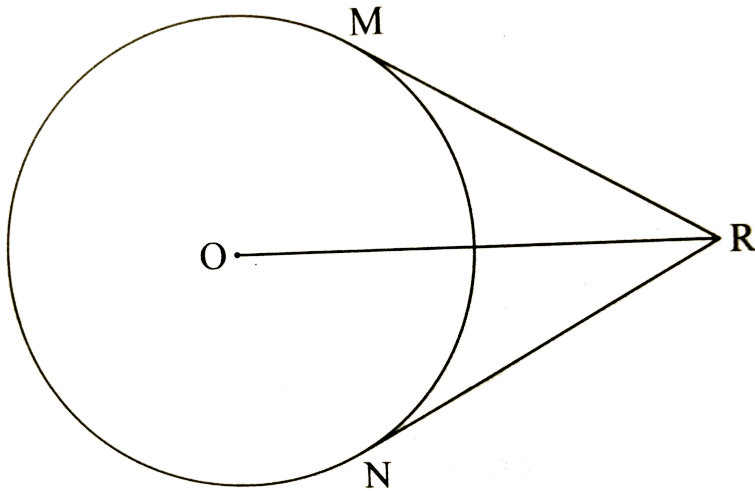
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5. In the figure, O is the same of the circle. From point R, seg RM and seg RN are tangent segments touching the circle at M and N. If  $OR = 10\text{cm}$  and radius of the circle = 5 cm, then

(i) What is the length of each tangnet segment ?

(iii) What is the measure of  $\angle MRO$  ?

(iii) What is the measure of  $\angle MRN$  ?



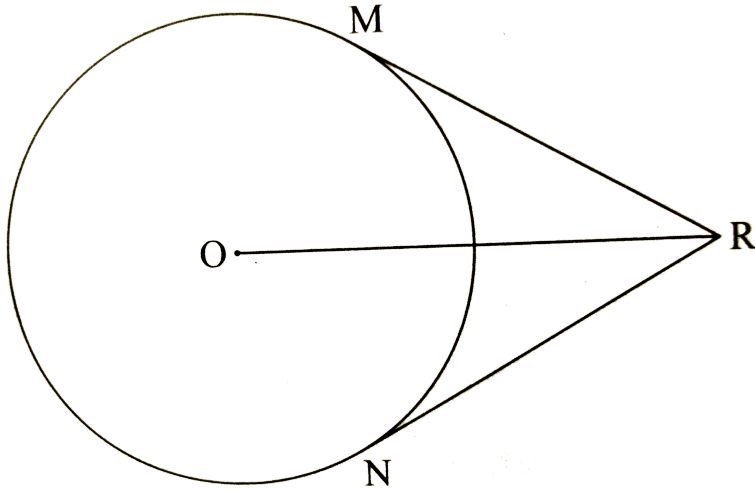
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**6.** In the figure,  $O$  is the center of the circle. From point  $R$ , seg  $RM$  and seg  $RN$  are tangent segments touching the circle at  $M$  and  $N$ . If  $OR = 10\text{cm}$  and radius of the circle =  $5\text{ cm}$ , then

(i) What is the length of each tangent segment ?

(iii) What is the measure of  $\angle MRO$  ?

(iii) What is the measure of  $\angle MRN$  ?

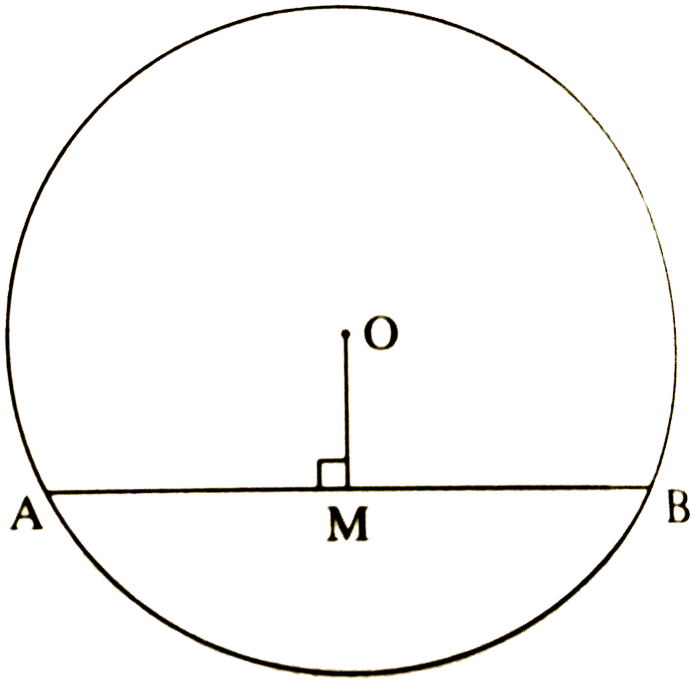


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7. In the figure , seg AB is the chord of the circle with centre O. if  $AM = 4$  cm then find MB and AB. State your



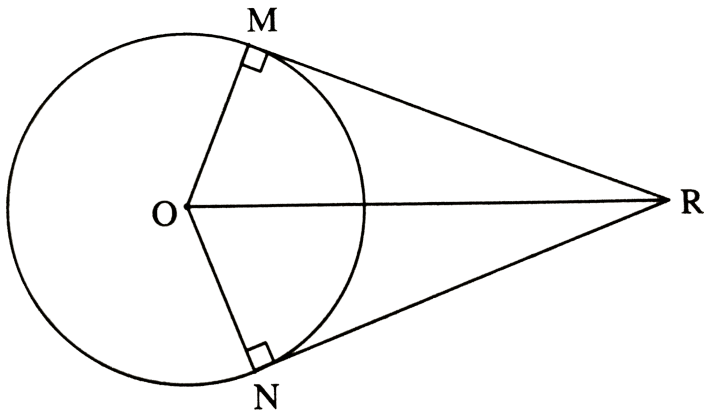
reason.



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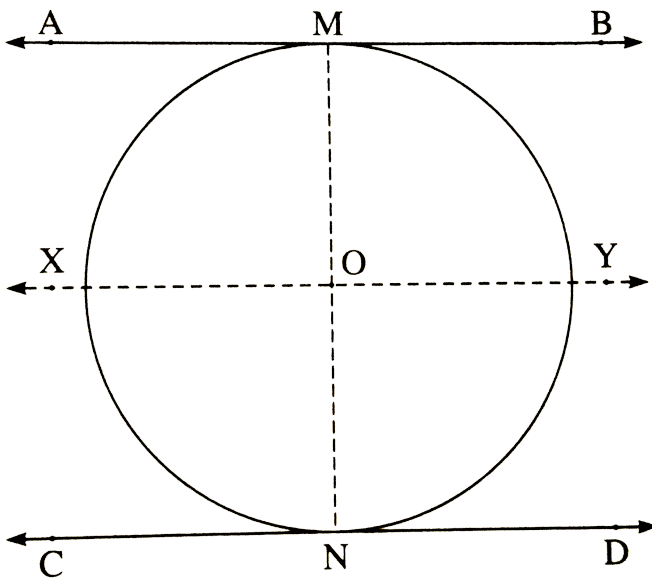
8. Seg RM and seg RN are tangent segments of a circle with centre O. Prove that seg OR bisects  $\angle MRN$  as well

as  $\angle MON$ .



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9. What is the distance between two parallel tangents of a circle having radius 4.5 cm ?. Justify your answer.



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## PRACTICE SET 3.2

1. Two circles having radii 3.5 cm and 4.8 cm touch each other internally. Find the distance between their centres.

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2. Two circles of radii 5.5 cm and 4.2 cm touch each other externally. Find the distance between their centres.



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3. If radii of two circles are 4 cm and 2.8 cm. Draw figure of these circles touching each other. Externally.



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4. If radii of two circles are 4 cm and 2.8 cm. Draw figure of these circles touching each other.

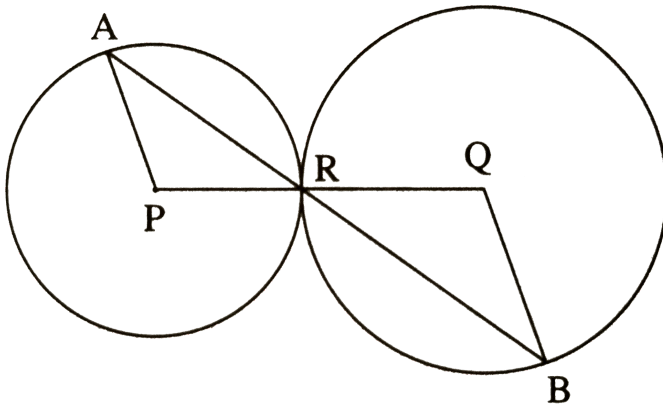
Internally.



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5. In the figure, the circles with centers  $P$  and  $Q$  touch each other at  $R$ . A line passing through  $R$  meets the circles at  $A$  and  $B$  respectively. Prove that

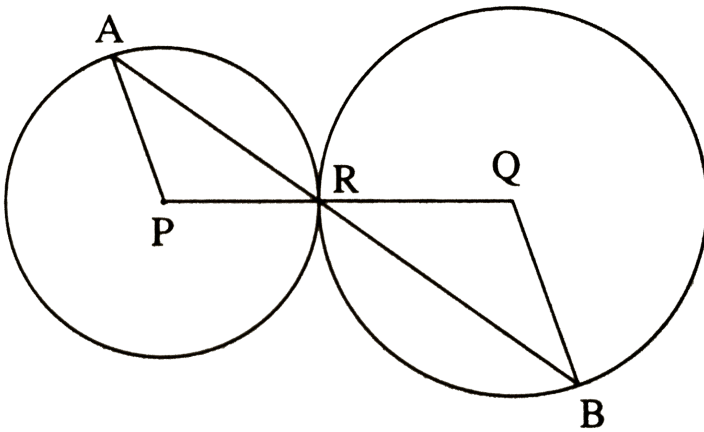
$\text{seg } AP \parallel \text{seg } BQ$



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6. In the figure, the circles with centers P and Q touch each other at R. A line passing through R meets the circles at A and B respectively. Prove that

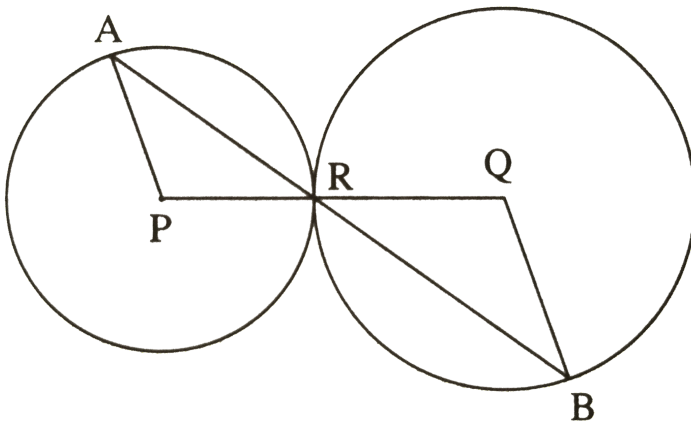
$$\triangle APR \sim \triangle RQB$$



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7. In the figure, the circles with centers P and Q touch each other at R. A line passing through R meets the circles at A and B respectively.

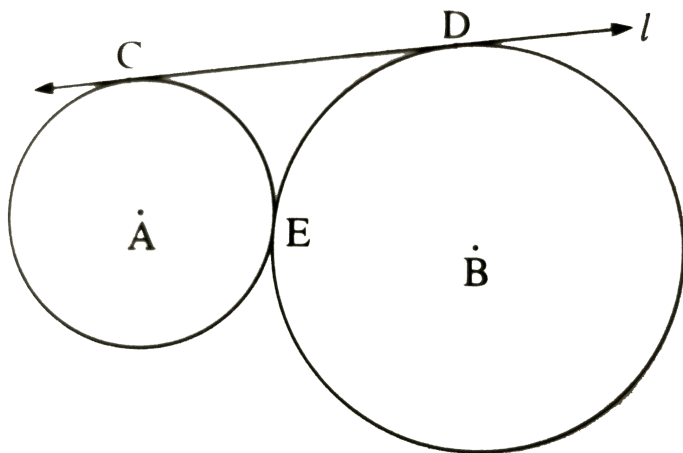
Find  $\angle RQB$  if  $\angle PAR = 35^\circ$



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8. In the figure, the circles with centers A and B touch each other at E. Line l is a common tangent which

touches the circles at C and D respectively. Find the length of seg CD, if the radii of the circle are 4 cm, 6 cm.



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### PRACTICE SET 3.3

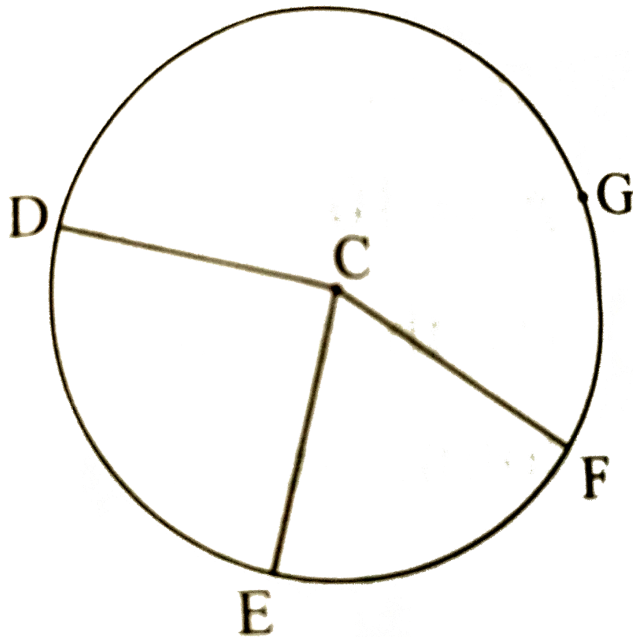
1. In the figure, points G, D, E, F are concyclic points of a circle with centre C.



$$\angle ECF = 70^\circ$$

$$m(\text{arc DGF}) = 200^\circ,$$

find  $m(\text{arc DE})$  and  $m(\text{arc DEF})$ .

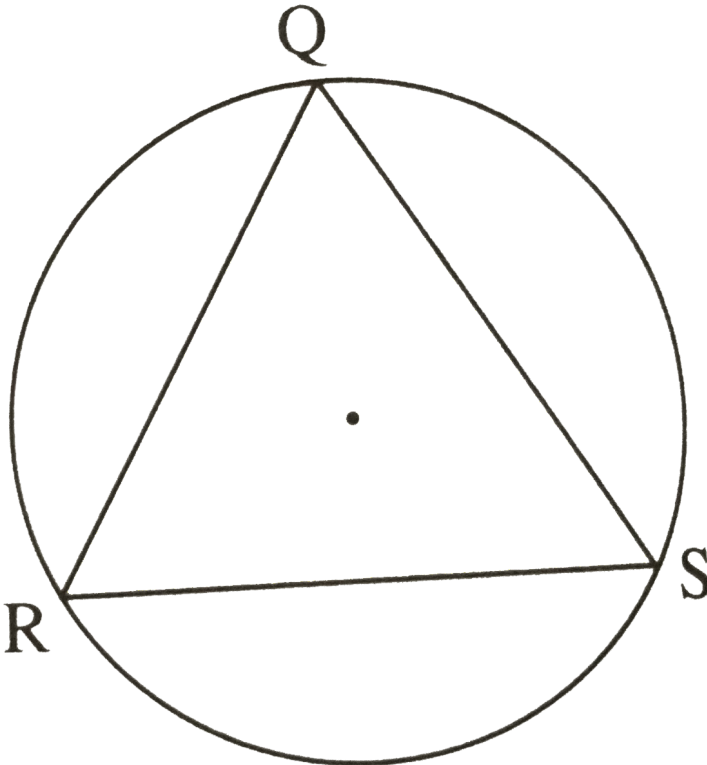


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2. In figure,  $\triangle QRS$  is an equilateral triangles. Prove that,

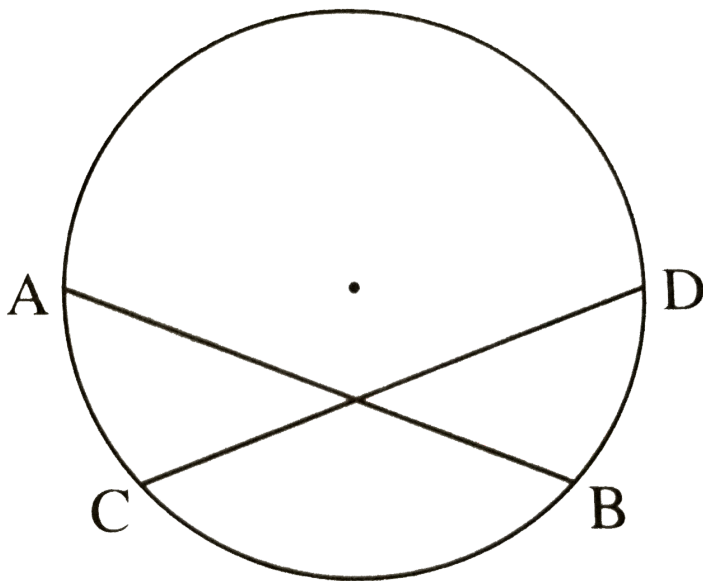
(1)  $\text{arc}RS \cong \text{arc}QS \cong \text{arc}QR$

(2)  $m(\text{arc}QRS) = 240^\circ$ .



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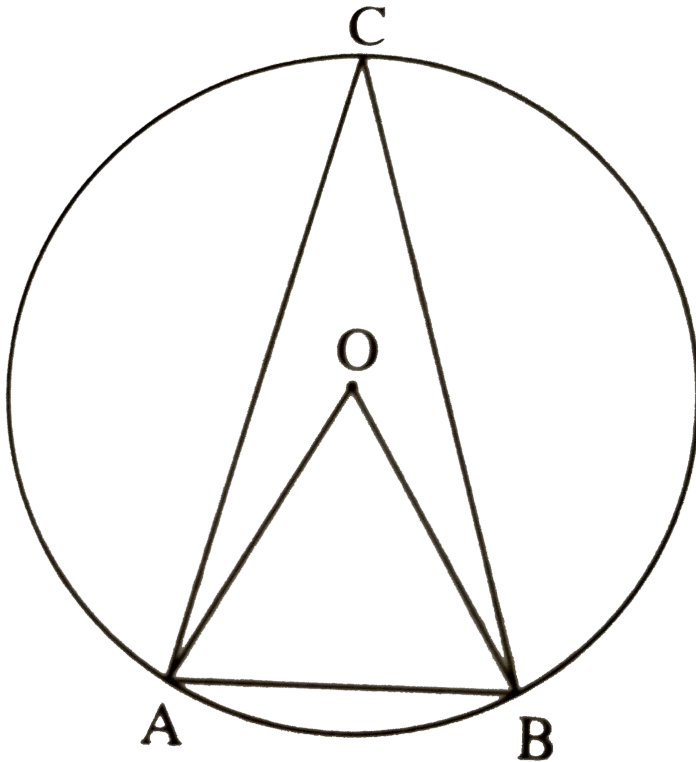
3. In figure, chord  $AB \cong$  chord  $CD$ , Prove that, arc  $AC \cong$  arc  $BD$ .



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1. In the figure, in a circle with centre O, length of chord AB is equal to the radius of the circle. Find measure of each of the following.

$\angle AOB$



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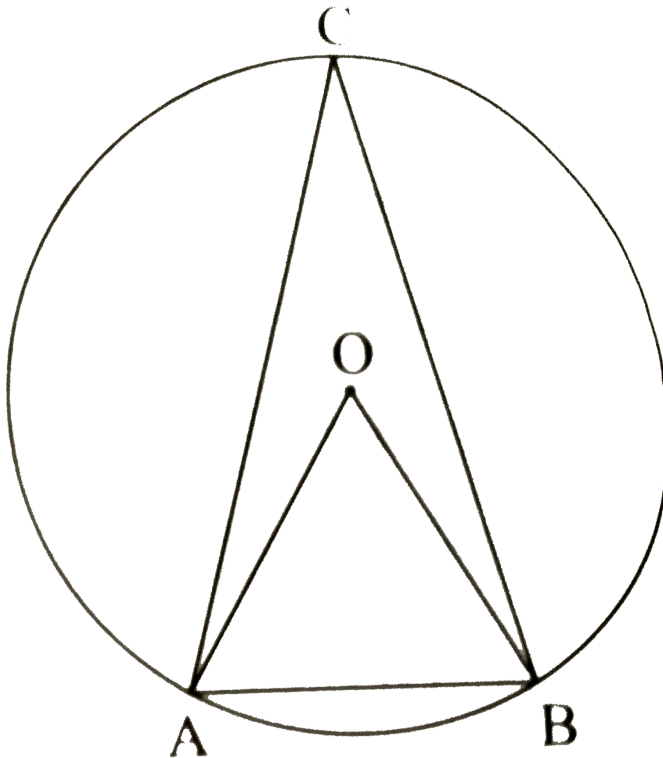
2. In the figure , in a circle with centre O, length of chord AB is equal to the radius of the circle. Find the measure of each of the following :

(1)  $\angle AOB$

(2)  $\angle ACB$

(3) arc AB

(4) arc ACB



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3. In the figure, in a circle with centre  $O$ , length of chord  $AB$  is equal to the radius of the circle. Find the measure

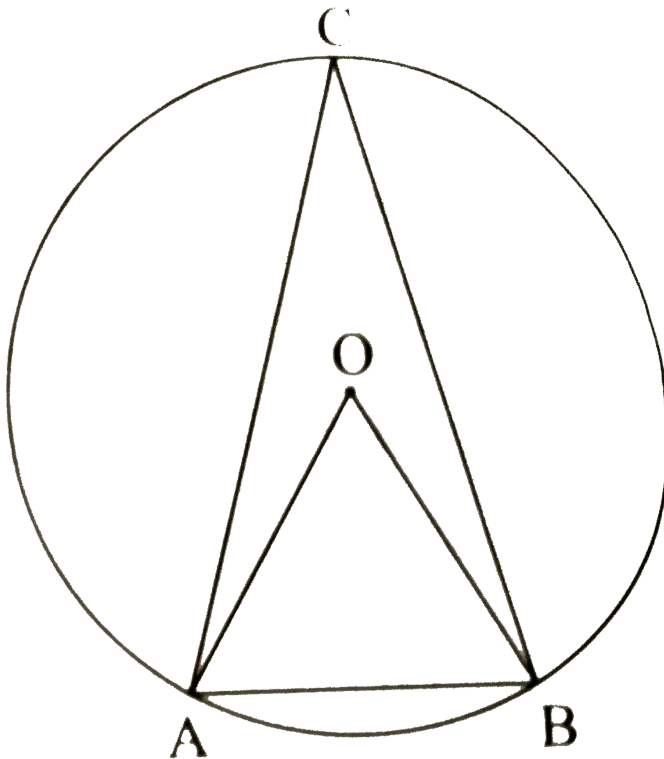
of each of the following :

(1)  $\angle AOB$

(2)  $\angle ACB$

(3) arc AB

(4) arc ACB



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4. In the figure , in a circle with centre  $O$ , length of chord  $AB$  is equal to the radius of the circle. Find the measure of each of the following :

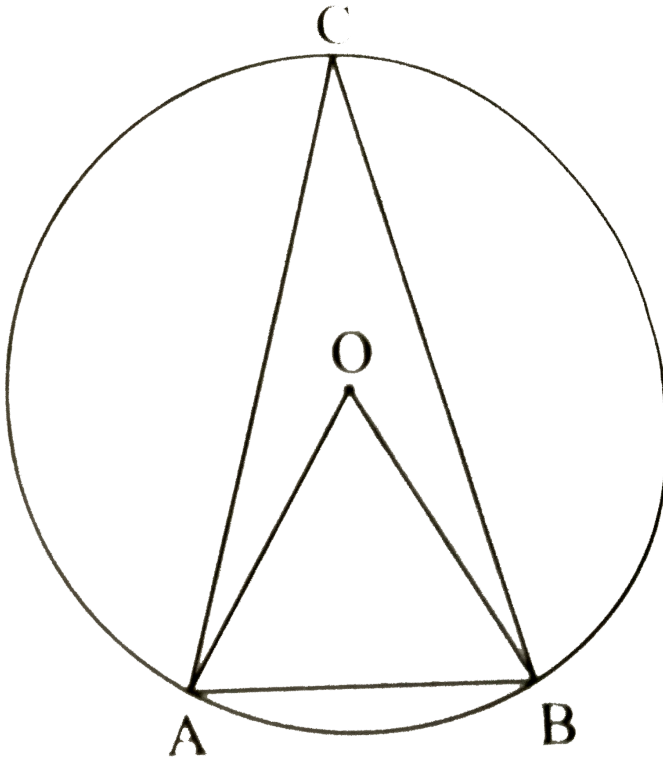
(1)  $\angle AOB$

(2)  $\angle ACB$

(3) arc  $AB$



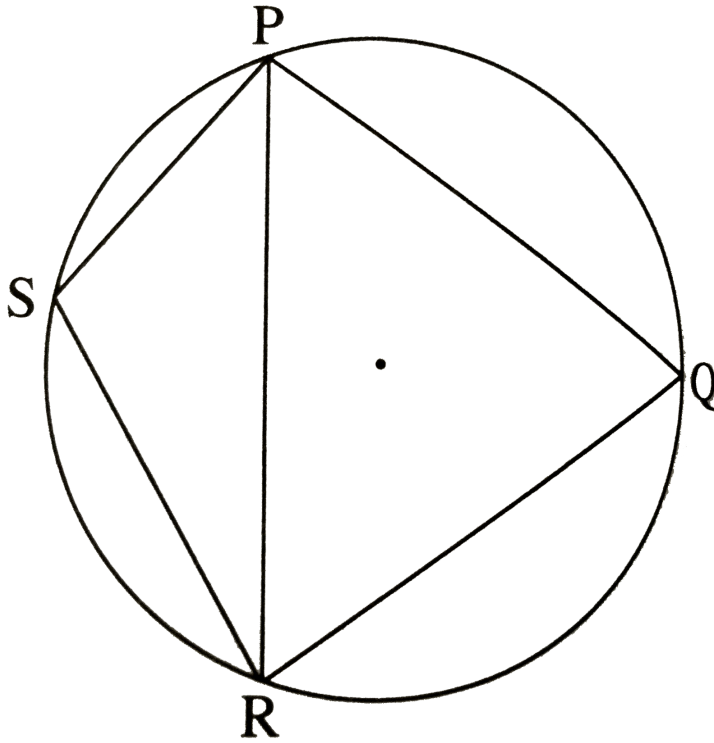
(4) arc ACB



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5. In the figure,  $\square PQRS$  is cyclic side  $PQ \cong RQ$ ,  
 $\angle PSR = 110^\circ$ , Find

$\angle PQR$

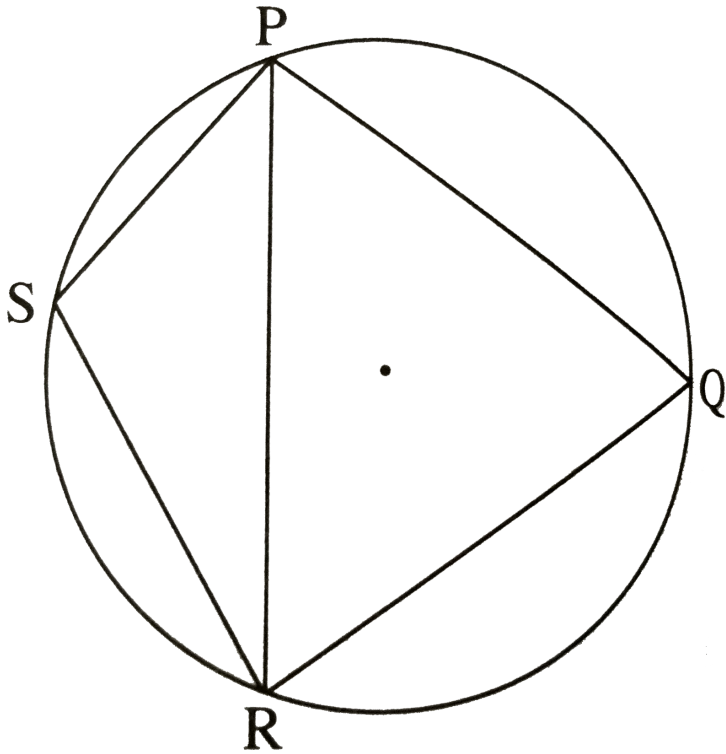


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6. In the figure,  $\square PQRS$  is cyclic side  $PQ \cong RQ$ ,

$\angle PSR = 110^\circ$ , Find

$m(\text{arc } PQR)$

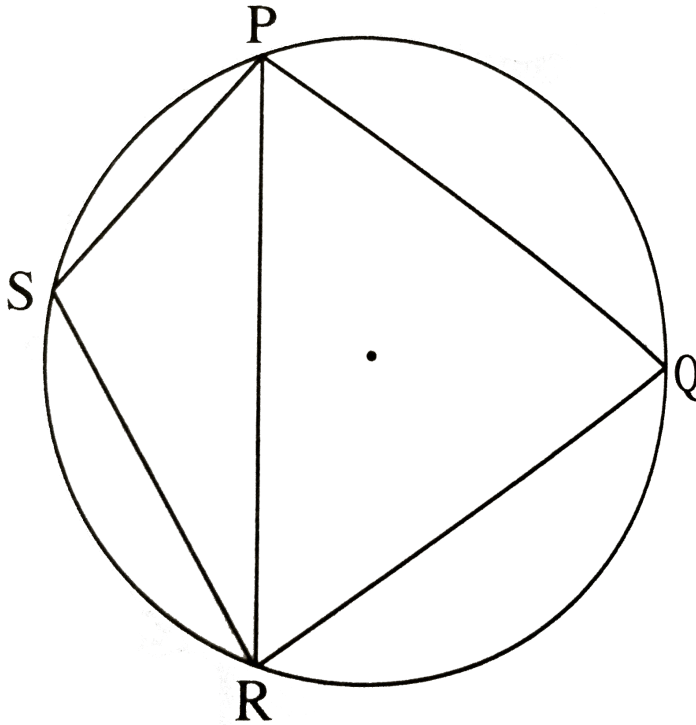


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7. In the figure,  $\square PQRS$  is cyclic side  $PQ \cong RQ$ ,

$\angle PSR = 110^\circ$ , Find

$m(\text{arc } QR)$

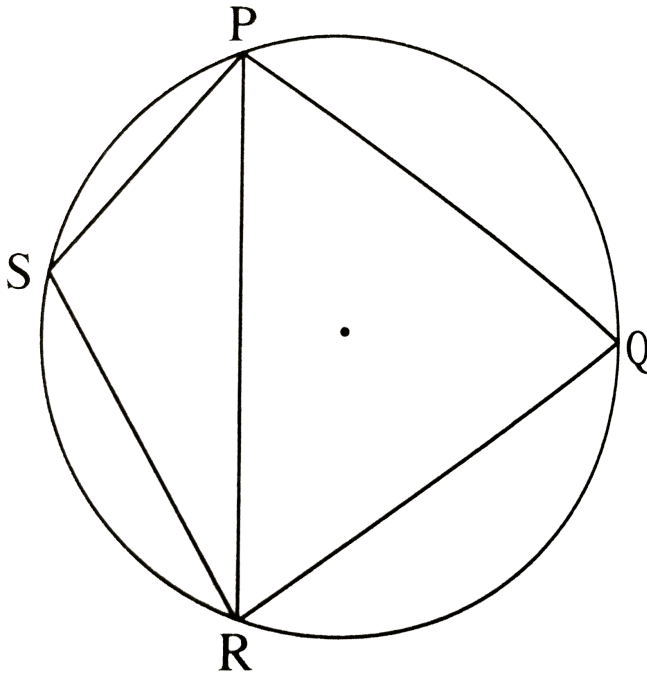


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8. In the figure,  $\square PQRS$  is cyclic side  $PQ \cong RQ$ ,

$\angle PSR = 110^\circ$ , Find

measure of  $\angle PRQ$

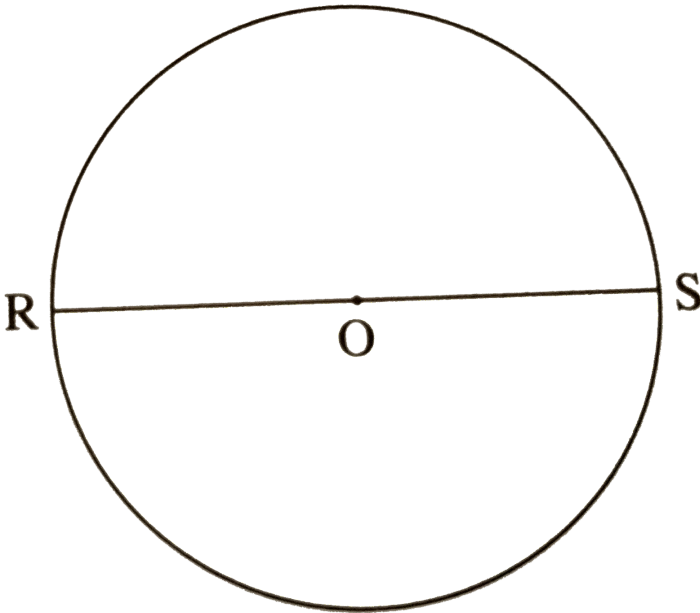


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9.  $\square MRPN$  is cyclic ,  
 $\angle R = (5x - 13)^\circ$ ,  $\angle N = (4x + 4)^\circ$ . Find measures of  
 $\angle R$  and  $\angle N$ .

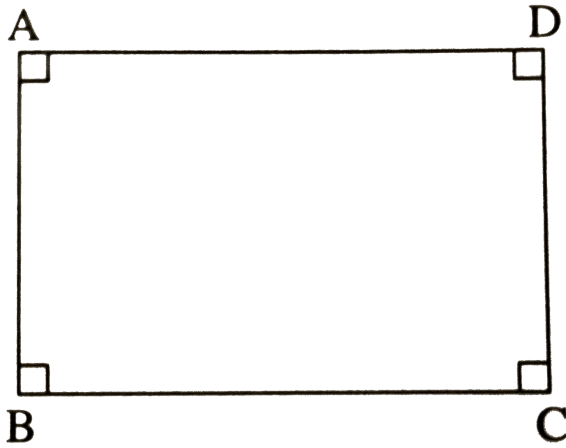
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10. In figure, seg  $RS$  is a diameter of the circle with centre  $O$ . Point  $T$  lies in the exterior of the circle. Prove that  $\angle RTS$  is an acute angle.



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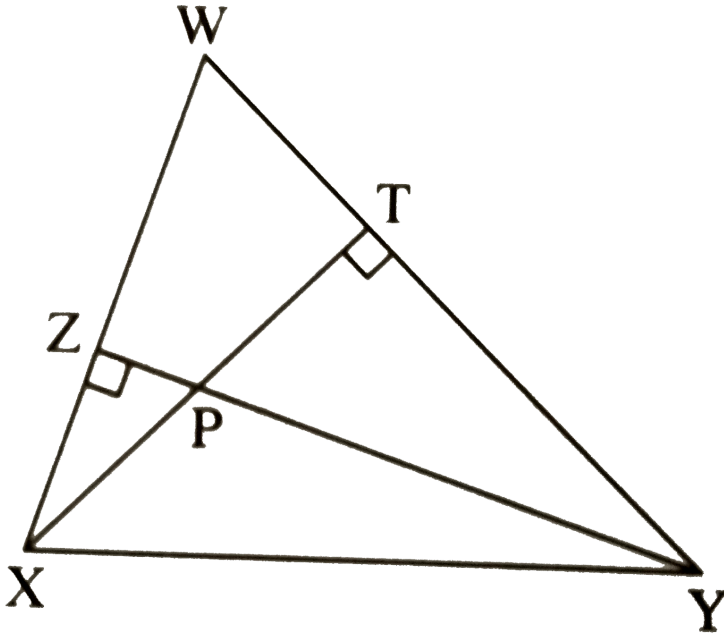
11. Prove that, any rectangle is a cyclic quadrilateral.



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12. In figure, altitudes YZ and XT of  $\triangle WXY$  intersect at P. Prove that

□  $WZPT$  is cyclic

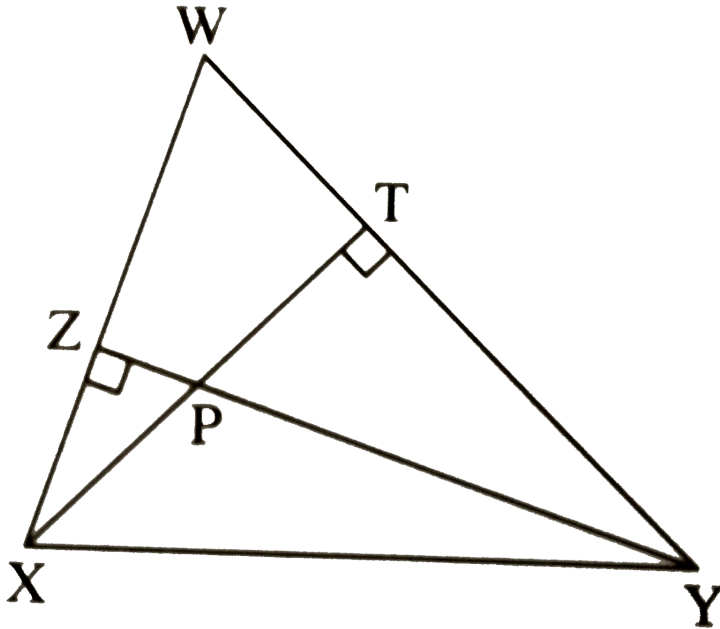


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13. In figure, altitudes  $YZ$  and  $XT$  of  $\triangle WXY$  intersect at  $P$ . Prove that



Points X,Z,T,Y are concyclic.



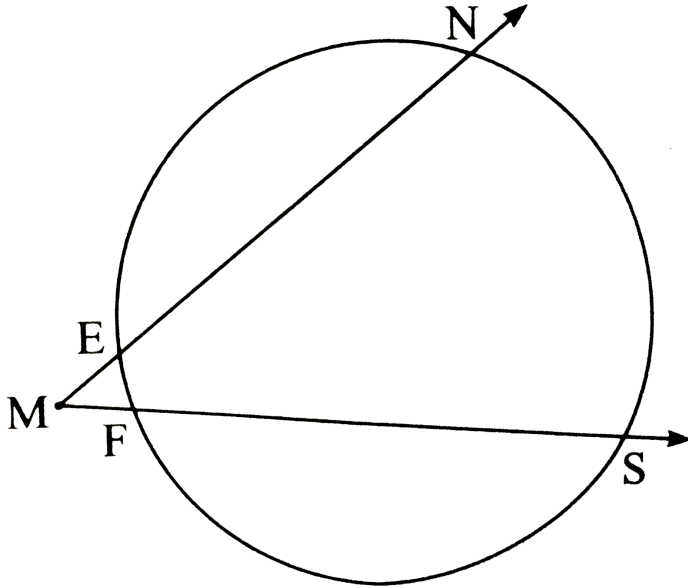
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14. In the figure,

$$m(\text{arc } NS) = 125^\circ$$

$$m(\text{arc } EF) = 37^\circ$$

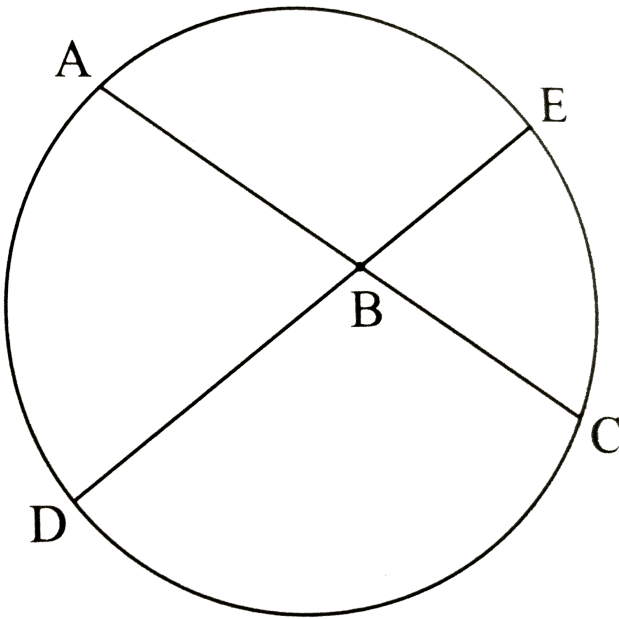
find the measure  $\angle NMS$ ,



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15. In the figure, chords AC and DE intersect at B. If

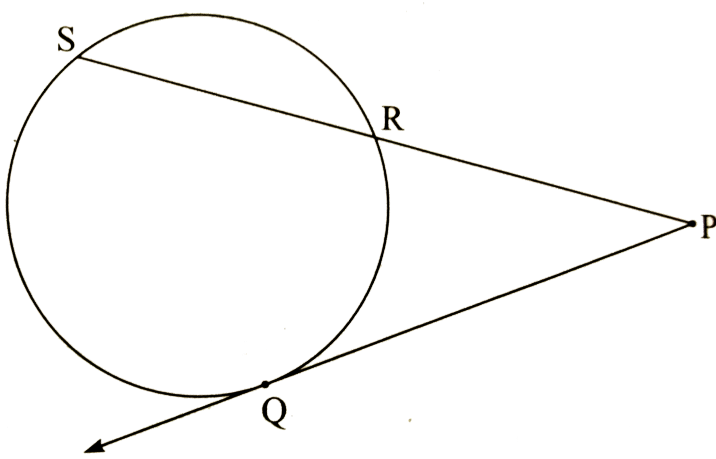
$\angle ABE = 108^\circ$ ,  $m(\text{arc } AE) = 95^\circ$ , find  $m(\text{arc } DC)$ .



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## PRACTICE SET 3.5

1. In the figure, ray PQ touches the circle at point Q. If  $PQ = 12$ ,  $PR = 8$ , then find PS.

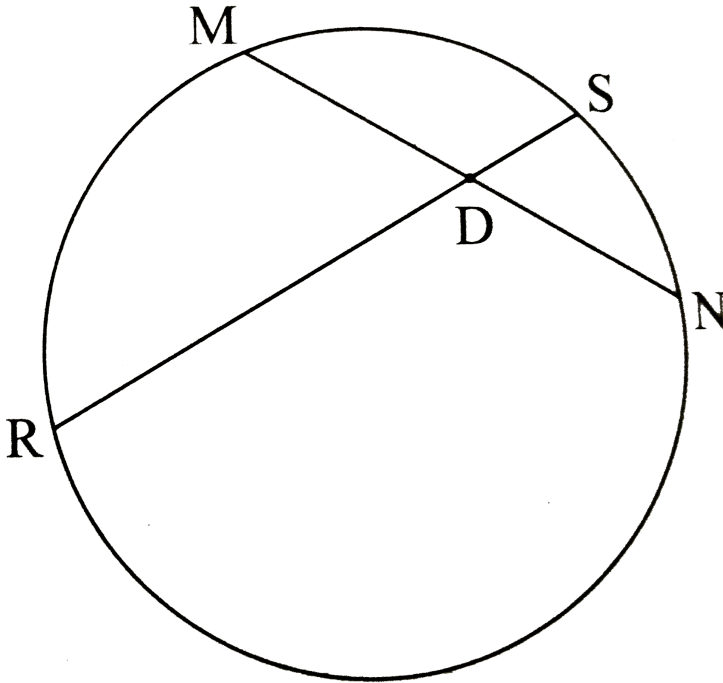


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2. In the figure, chord MN and chord RS intersect at point D.

(1) If  $RD = 15$ ,  $DS = 4$ ,  $MD = 8$ , find DN.

92) If  $RS = 18$ ,  $MD = 9$ ,  $DN = 8$ , find  $DS$ .

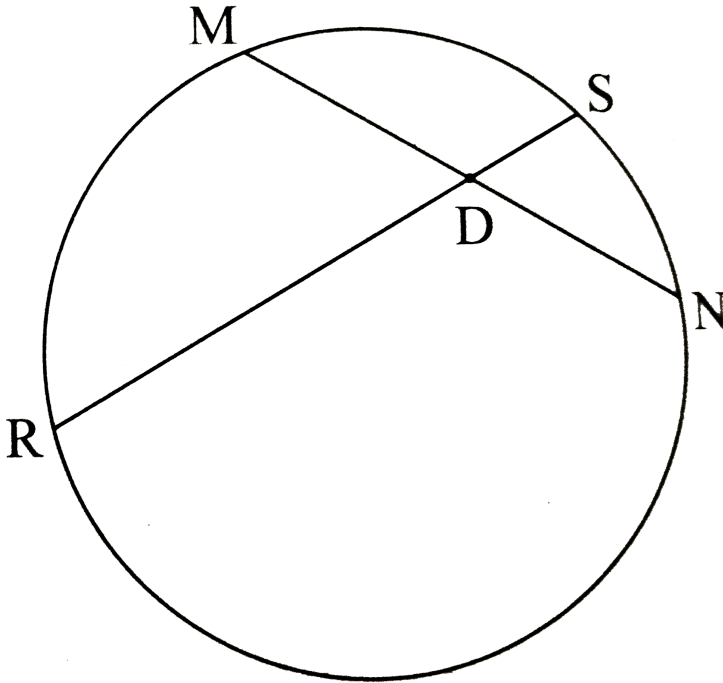


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**3.** In the figure, chord  $MN$  and chord  $RS$  intersect at point  $D$ .

(1) If  $RD = 15$ ,  $DS = 4$ ,  $MD = 8$ , find  $DN$ .

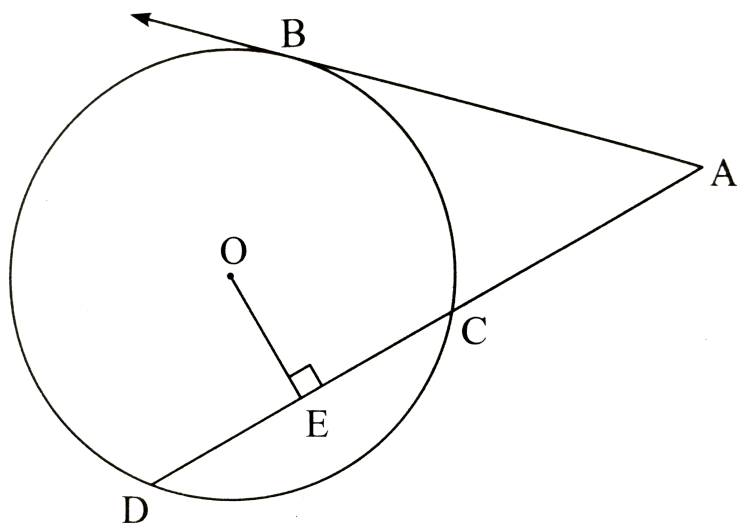
92) If  $RS = 18$ ,  $MD = 9$ ,  $DN = 8$ , find  $DS$ .



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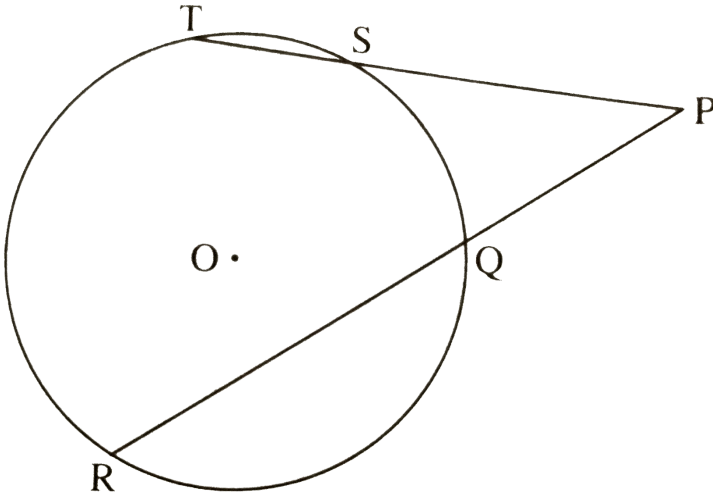
4. In the figure,  $O$  is the centre of the circle and  $B$  is a point of contact. Seg  $OE \perp$  seg  $AD$ ,  $AB = 12$ ,  $AC = 8$ , find

(i) AD (ii) DC (iii) DE.



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5. In figure, if  $PQ=6, QR=10, PS=8$ , find  $TS$ .

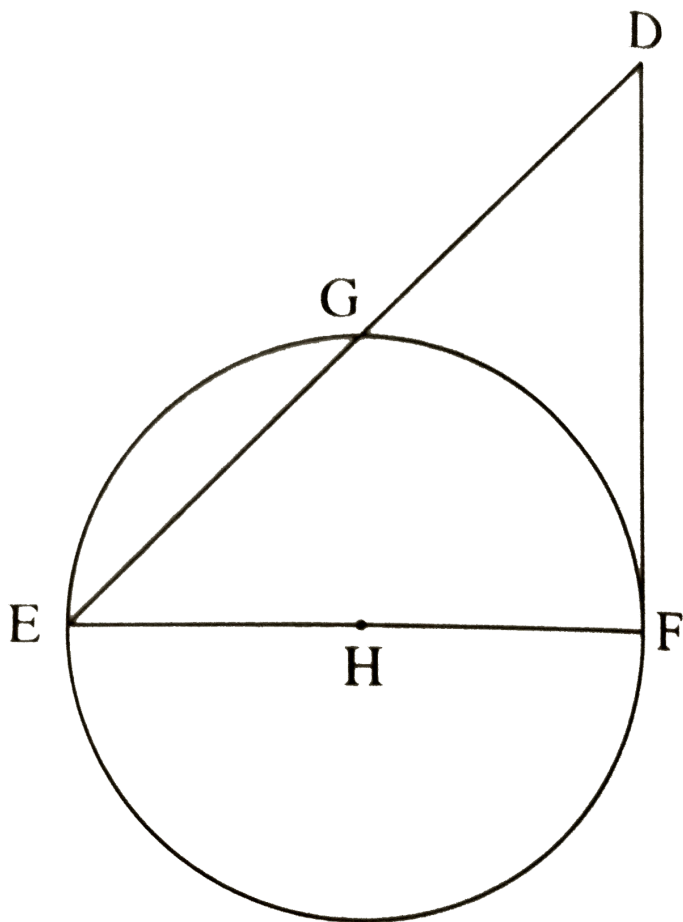


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6. In figure, *seg*  $EF$  is a diameter and *seg*  $DF$  is a tangent segment. The radius of the circle is  $r$ . Prove that,



$$DE \times GE = 4r^2.$$



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1. Two circles of radii 5.5 cm and 3.3 cm respectively touch each other. What is the distance between their centre ?

A. 4.4 cm

B. 8.8 cm

C. 2.2 cm

D. 8.8 or 2.2 cm

**Answer: D**



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2. Two circles intersect each other such that each circle passes through the centre of the other. If the distance between their centres is 12, what is the radius of each circle?

A. 6 cm

B. 12 cm

C. 24 cm

D. cannot say

**Answer: B**



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3. A circle touches all sides of a parallelogram. So the parallelogram must be a

A. rectangle

B. rhombus

C. square

D. trapezium

**Answer: B**



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4. Length of a tangent segment drawn from a point which is at a distance 12.5 cm from the centre of a circle

is 12cm , find the diameter of the circle.

A. 25 cm

B. 24 cm

C. 7 cm

D. 14 cm

**Answer: C**



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5. If two circles touch externally , how many common tangents can be drawn to them ?

A. One

B. Two

C. Three

D. Four

**Answer: C**



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6.  $\angle ACB$  is inscribed in arc  $ACB$  of a circle with centre  $O$ .  
If  $\angle ACB = 65^\circ$ , find  $m(\text{arc } ACB)$ .

A.  $65^\circ$

B.  $130^\circ$

C.  $295^\circ$

D.  $\angle 230^\circ$

**Answer: D**



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7. Chords  $AB$  and  $CD$  of a circle intersect inside the circle at point  $E$ . If  $AE = 5.6$ ,  $EB = 10$  cm,  $CE = 8$ , find  $ED$ .

A. 7

B. 8

C. 11.2

D. 9

**Answer: A**



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8. In a cyclic  $\square$  ABCD, twice the measure of  $\angle A$  is thrice the measure of  $\angle C$ . Find the measure of  $\angle C$ .

A.  $\angle 36^\circ$

B.  $\angle 72^\circ$

C.  $\angle 90^\circ$

D.  $\angle 108^\circ$

**Answer: B**



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9. Points A,B,C are on a circle, such that  $m(\text{arc } AB) = m(\text{arc } BC) = 120^\circ$ . No point, except point B, is common to the arcs. What type is the  $\triangle ABC$ ?

- A. Equilateral triangle
- B. Scalene triangle
- C. Right angled triangle
- D. Isoseles triangle

**Answer: A**



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10. Seg  $XZ$  is a diameter of a circle. Point  $Y$  lies in its interior. How many of the following statements are true?

(1) It is not possible that  $\angle XYZ$  is an acute angle.

(2)  $\angle XYZ$  can't be a right angle

(3)  $\angle XYZ$  is an obtuse angle.

(4) Can't make a definite statement for measure of  $\angle XYZ$

A. Only one

B. Only two

C. Only three

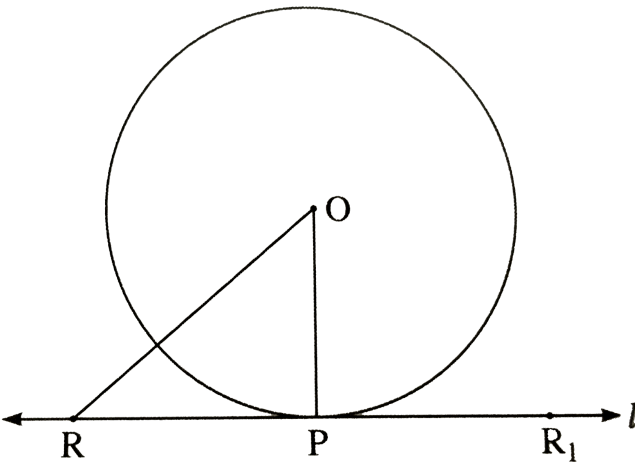
D. All

**Answer: C**

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11. Line  $l$  touches a circle with centre  $O$  at point  $P$ . If radius of the circle is 9 cm, answer the following:

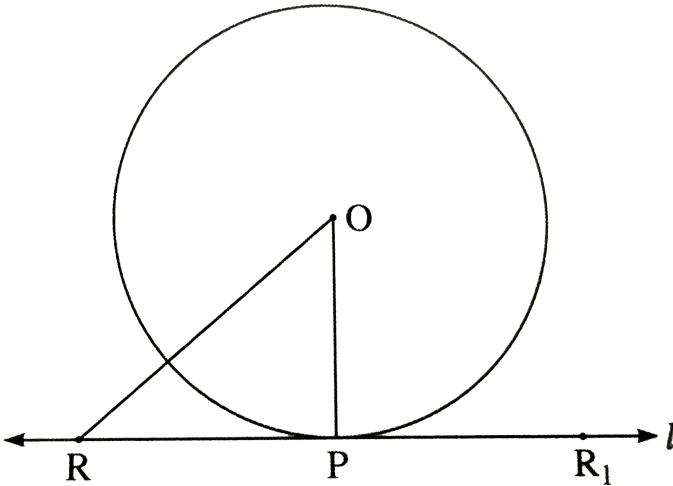
What is  $d(O,P)=?$  Why?



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12. Line  $l$  touches a circle with centre  $O$  at point  $P$ . If radius of the circle is 9 cm, answer the following:

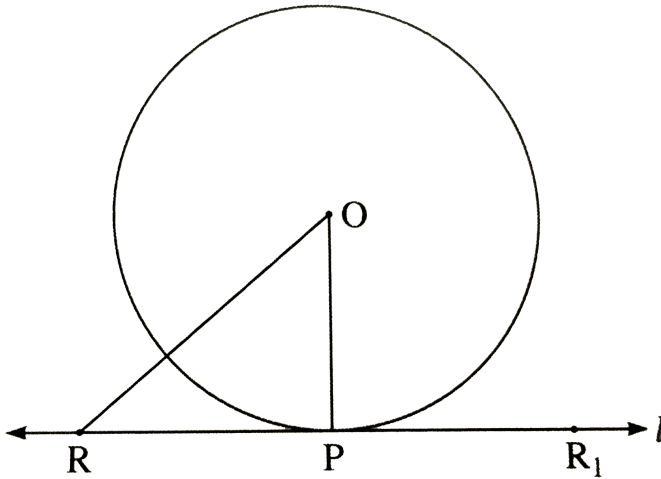
If  $d(O,Q)=8$  cm, where does the point  $Q$  lie?



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13. Line  $l$  touches a circle with centre  $O$  at point  $P$ . If radius of the circle is 9 cm, answer the following:

If  $d(O,R)=15$  cm, how many locations of point R are line on  $l$ ? At what distance will each of them be from point P?

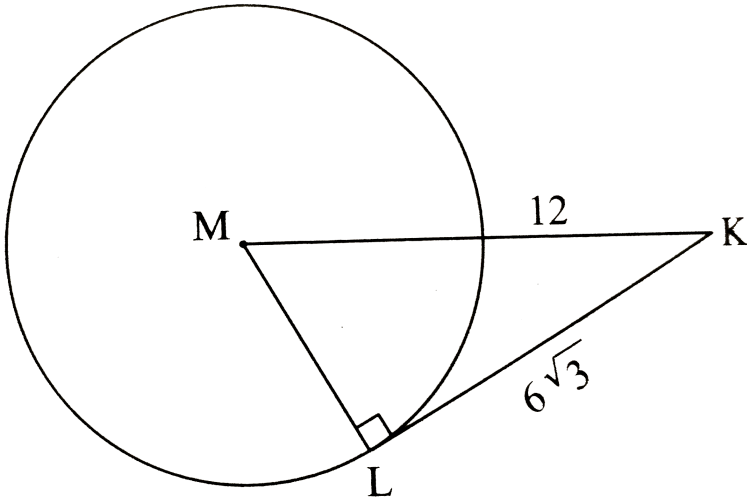


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**14.** In the figure, M is the centre of the circle and seg KL is a tangent segment. If  $MK = 12$ ,  $KL = 6\sqrt{3}$  then find,

(1) Radius of the circle,

(2) Measures of  $\angle K$  and  $\angle M$ .

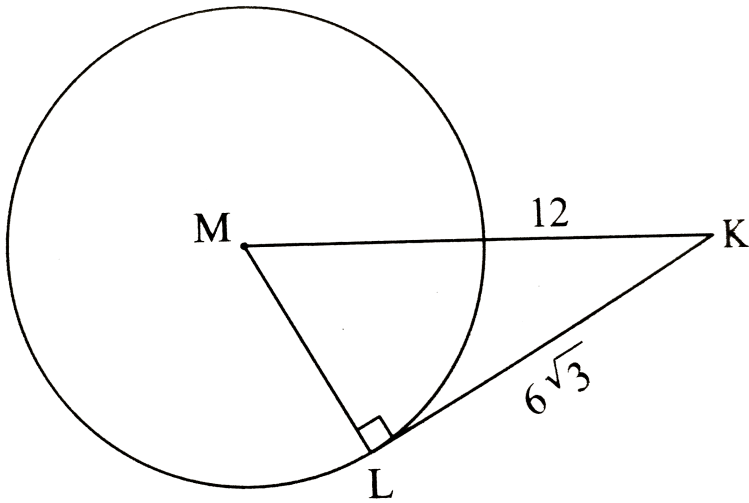


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**15.** In the figure, M is the centre of the circle and seg KL is a tangent segment. If  $MK = 12$ ,  $KL = 6\sqrt{3}$  then find,

(1) Radius of the circle,

(2) Measures of  $\angle K$  and  $\angle M$ .

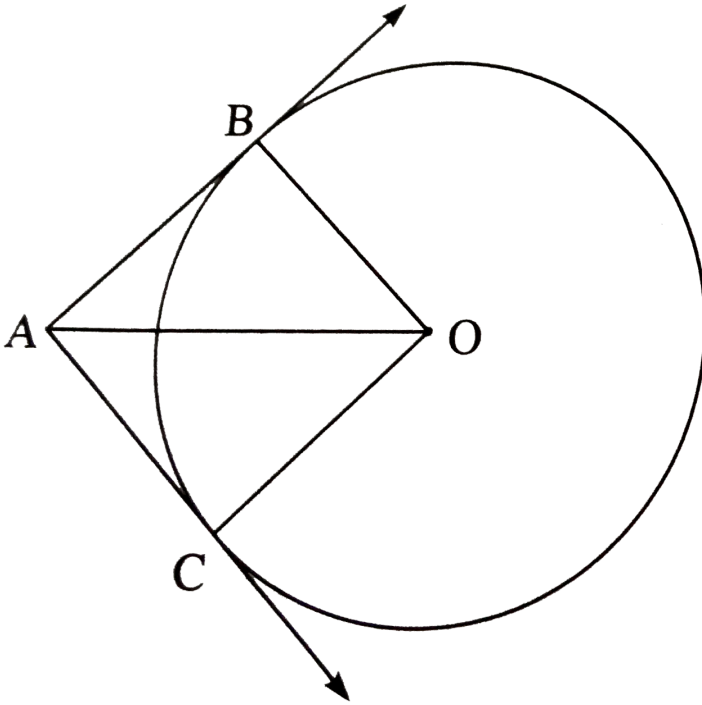


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**16.** In the figure, O is the centre of the circle of the circle.

Seg AB, seg AC are tangent segments. Radius of the

circle is  $r$  and  $l(AB)=r$ . Prove that,  $\square ABOC$  is a square.

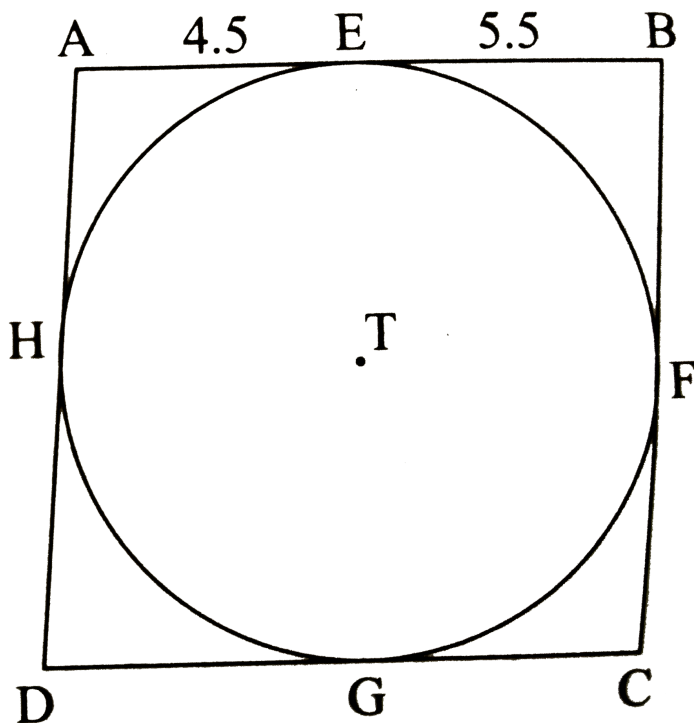


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17. In the figure,  $\square ABCD$  is a parallelogram. It circumscribes the circle with centre T. Point E, F, G, H are



touching points. If  $AE = 4.5$ ,  $EB = 5.5$ , find  $AD$ .



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**18.** In the figure, circle with centre  $M$  touches the circle with centre  $N$  at point  $T$ . Radius  $RM$  touches the smaller

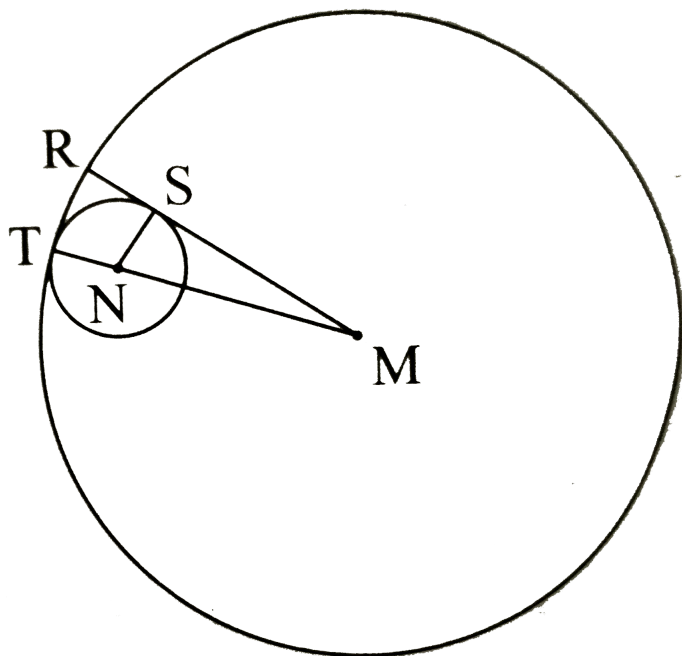
circle at S. Radii of circles are 9 cm and 2.5 cm. Find the answers to the following questions hence find the ratio

MS: SR

(1) Find the length of segment MT

(2) Find the length of seg MN

(3) Find the measure of  $\angle NSM$ .



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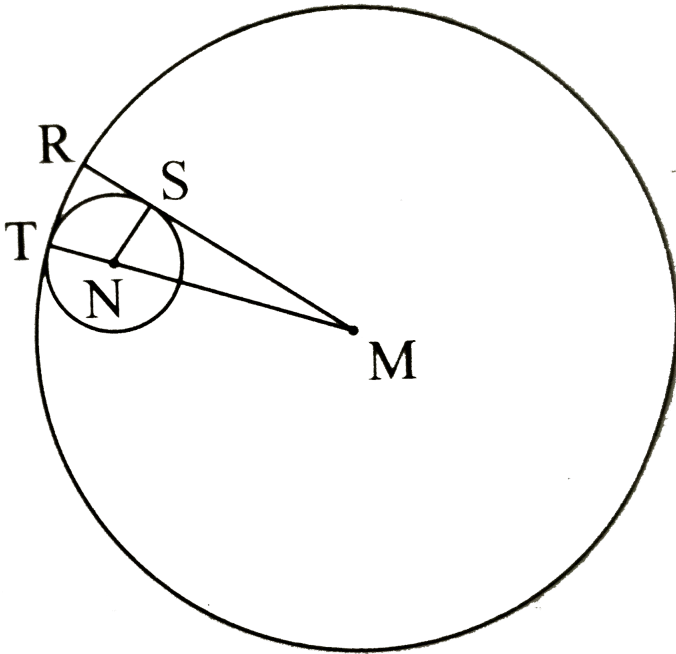
**19.** In the figure, circle with centre M touches the circle with centre N at point T. Radius RM touches the smaller circle at S. Radii of circles are 9 cm and 2.5 cm. Find the answers to the following questions hence find the ratio

MS: SR

(1) Find the length of segment MT

(2) Find the length of seg MN

(3) Find the measure of  $\angle NSM$ .



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**20.** In the figure, circle with centre M touches the circle with centre N at point T. Radius RM touches the smaller circle at S. Radii of circles are 9 cm and 2.5 cm. Find the

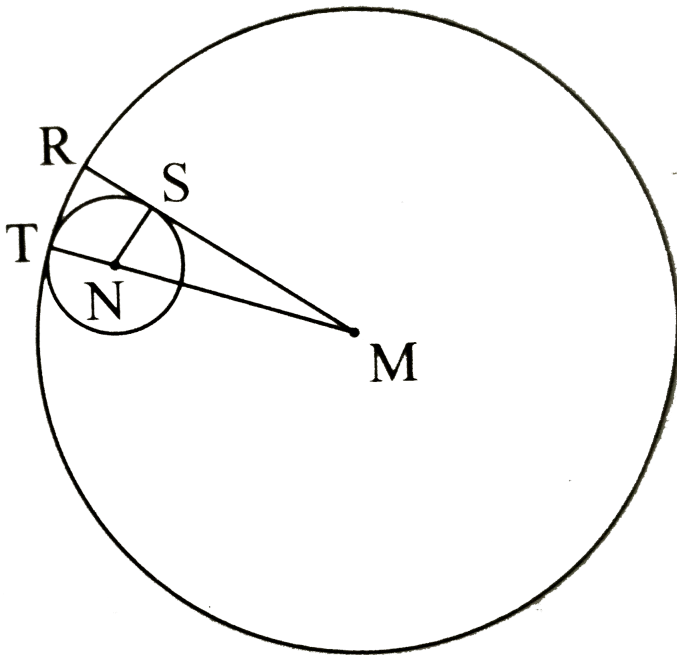
answers to the following questions hence find the ratio

MS: SR

(1) Find the length of segment MT

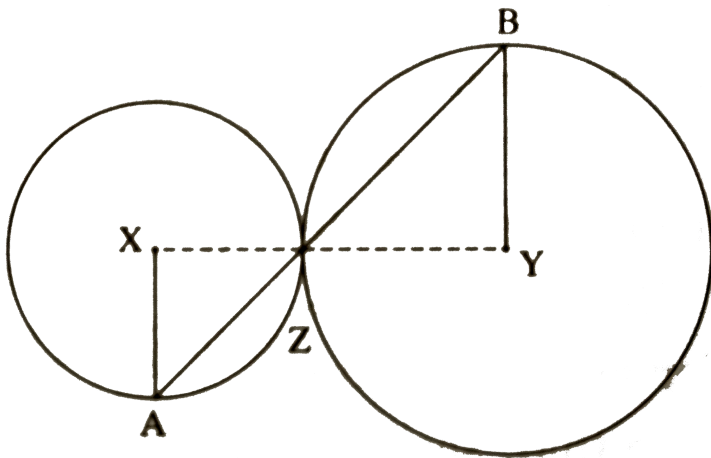
(2) Find the length of seg MN

(3) Find the measure of  $\angle NSM$ .



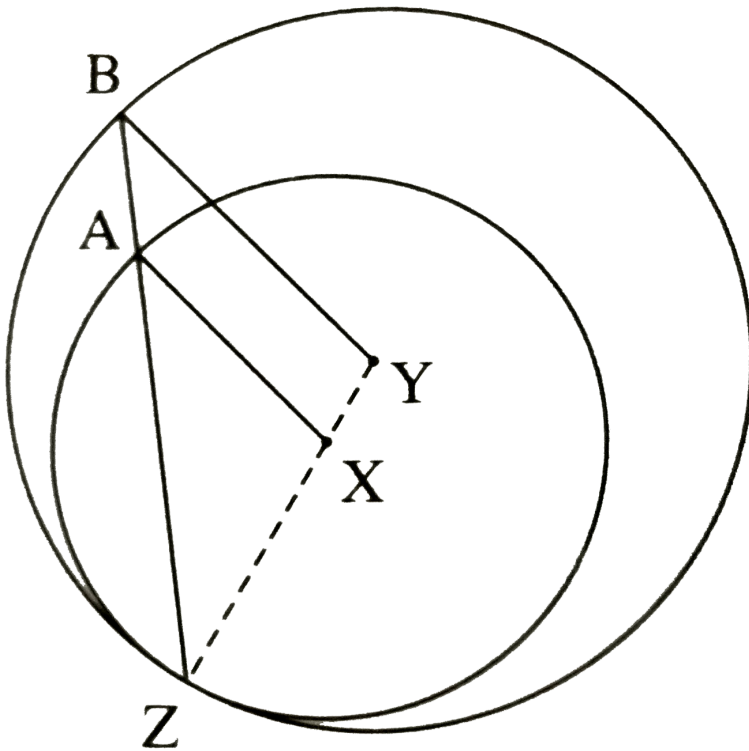
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21. In the figure, circles with centres X and Y touch each other at point Z. A secant passing through Z intersects the circles at points A and B respectively. Prove that, radius  $XA \parallel$  radius  $YB$ . Fill in the blanks and complete the proof:



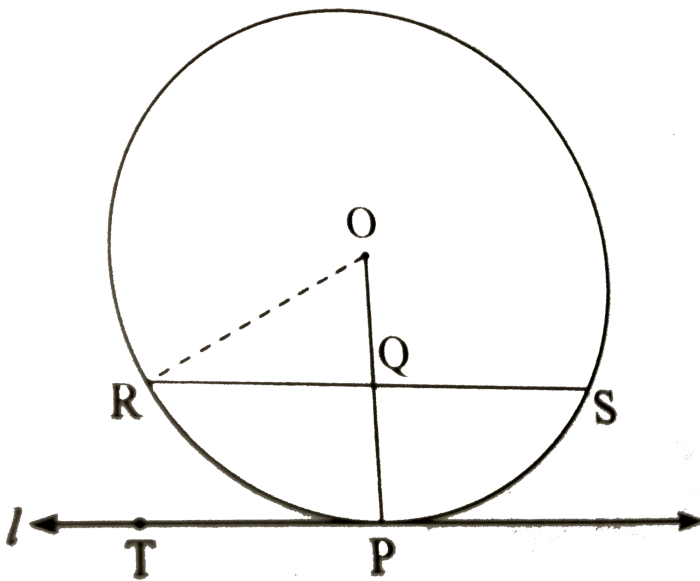
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22. In the figure, circles with centres  $X$  and  $Y$  touch internally at point  $Z$ . Seg  $BZ$  is a chord of bigger circle and it intersects smaller circle at point  $A$ . Prove that, seg  $AX \parallel$  seg  $BY$ .



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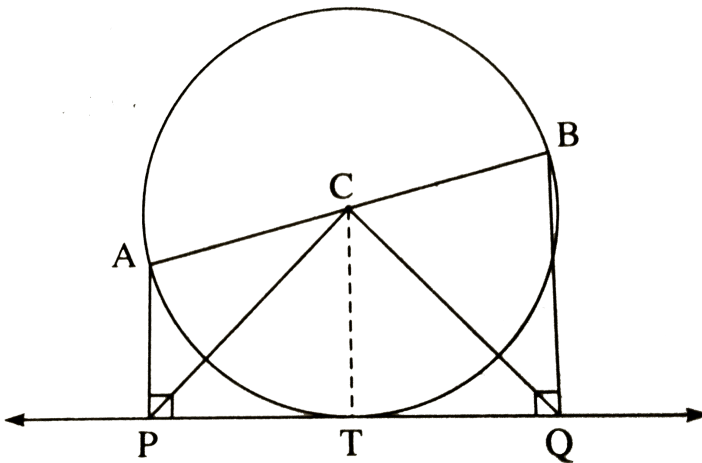
**23.** In the figure, line  $l$  touches the circle with centre  $O$  at point  $P$ .  $Q$  is the midpoint of radius  $OP$ .  $RS$  is a chord through  $Q$  such that chords  $RS \parallel$  line  $l$ . If  $RS = 12$ , find the radius of the circle.



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24. In the figure, seg AB is a diameter of a circle with centre C. Line PQ is a tangent, which touches the circle at point T. seg AP  $\perp$  line PQ and seg BQ  $\perp$  line PQ. Prove that, seg CP  $\cong$  seg CQ.



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25. Draw circles with centres A, B and C each of radius 3 cm, such that each circle touches the other two circles.



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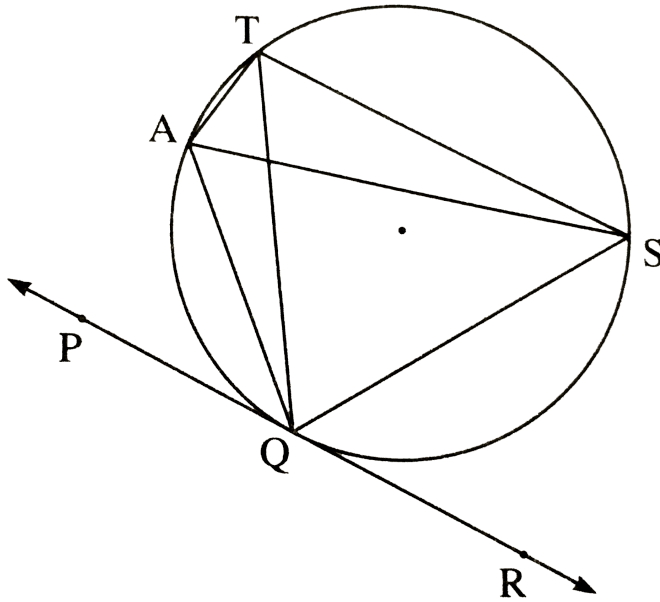
**26.** Prove the any three points on a circle cannot be collinear .



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**27.** In the figure, line PR touches the circle at point Q.  
Answer the following questions with the help of the figure:

What is the sum of  $\angle TAQ$  and  $\angle TSQ$ ?



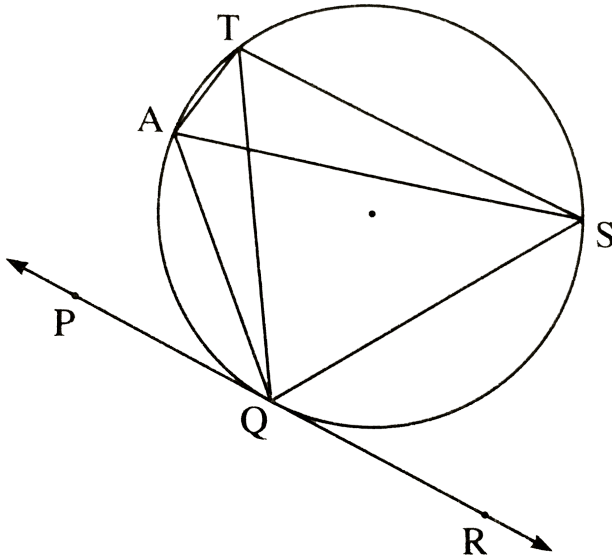
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**28.** In the figure, line  $PR$  touches the circle at point  $Q$ .

Answer the following questions with the help of the

figure:

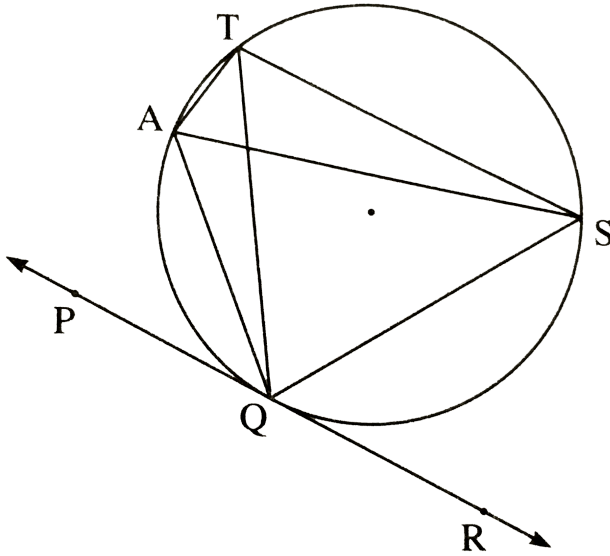
Find the angles which are congruent to  $\angle AQP$ .



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**29.** In the figure, line  $PR$  touches the circle at point  $Q$ . Answer the following questions with the help of the figure:

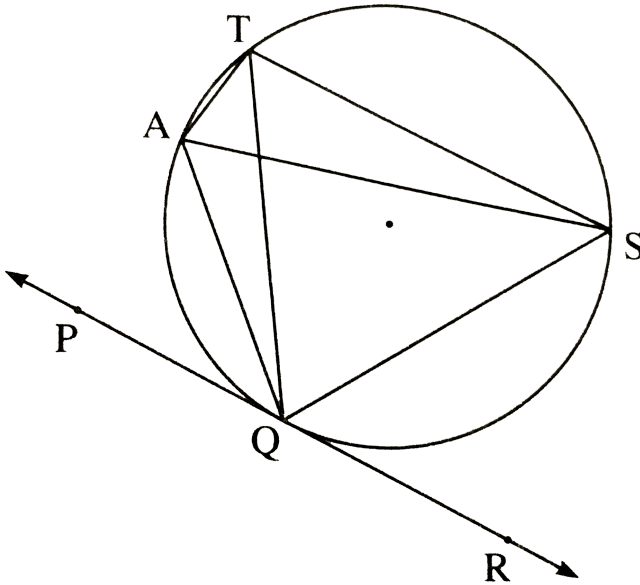
Which angles are congruent to  $\angle QTS$ ?



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**30.** In the figure, line  $PR$  touches the circle at point  $Q$ . Answer the following questions with the help of the figure:

$\angle TAS = 65^\circ$ , find the measure of  $\angle TQS$  and arc TS.



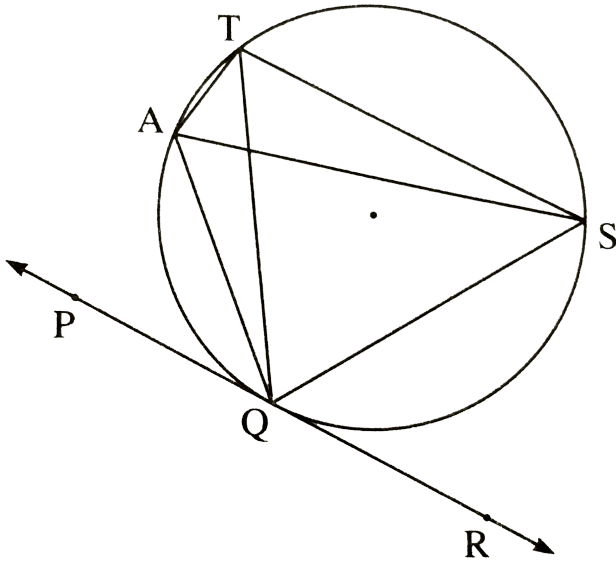
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31. In the figure, line PR touches the circle at point Q.

Answer the following questions with the help of the figure:

If  $\angle AQP = 42^\circ$  and  $\angle SQR = 58^\circ$  find measure of

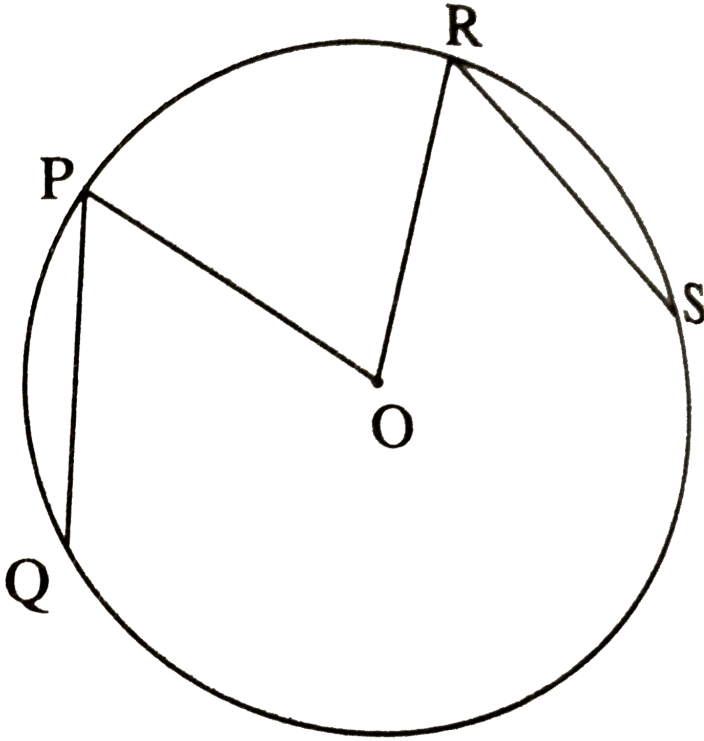
$\angle ATS$ .



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32. In the figure,  $O$  is the centre of a circle, chord  $PQ \cong$  chord  $RS$ . If  $\angle POR = 70^\circ$  and  $m(\text{arc } RS) = 80^\circ$ , find

(arc PR)



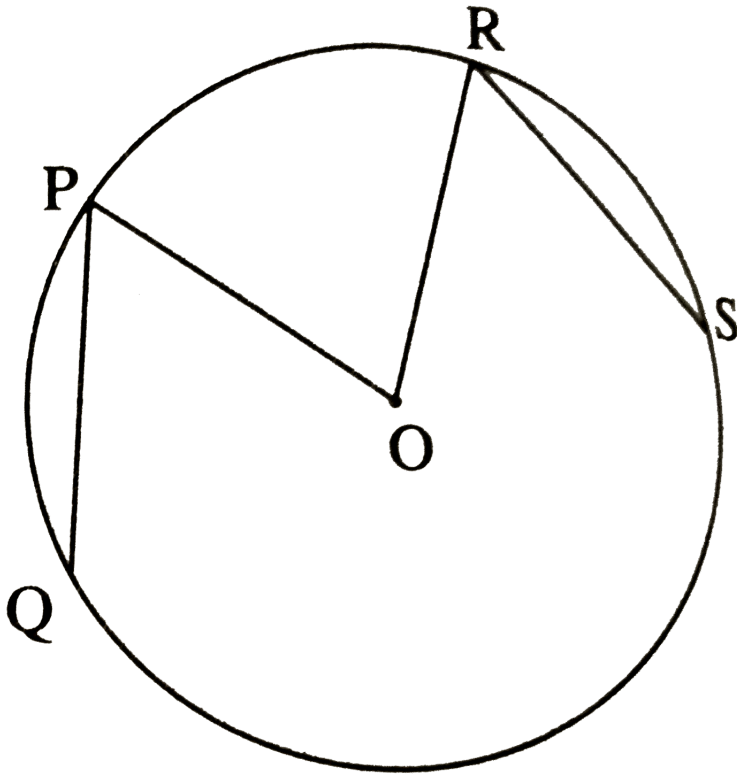
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**33.** In the figure, O is the centre of a circle, chord  $PQ \cong$  chord RS. If  $\angle POR = 70^\circ$  and  $m(\text{arc } RS) = 80^\circ$ ,



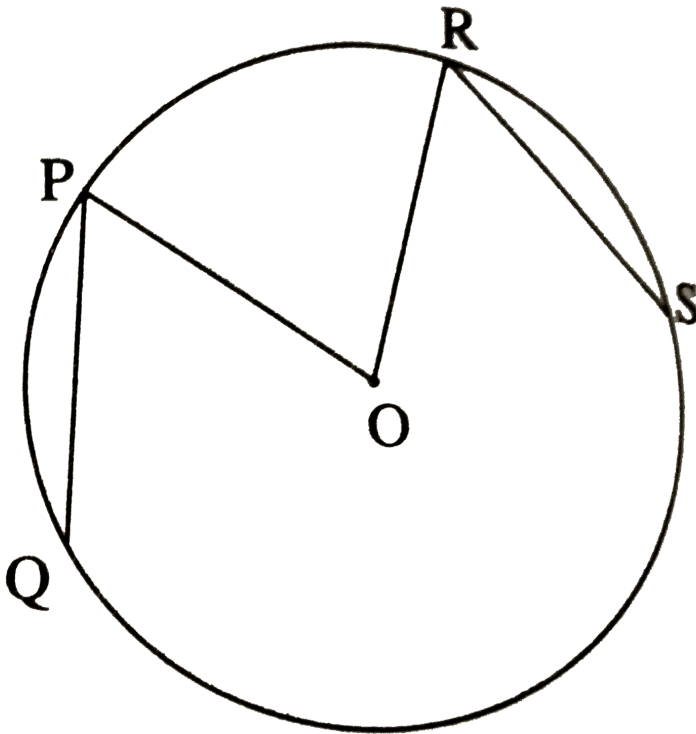
find

(arc QS)



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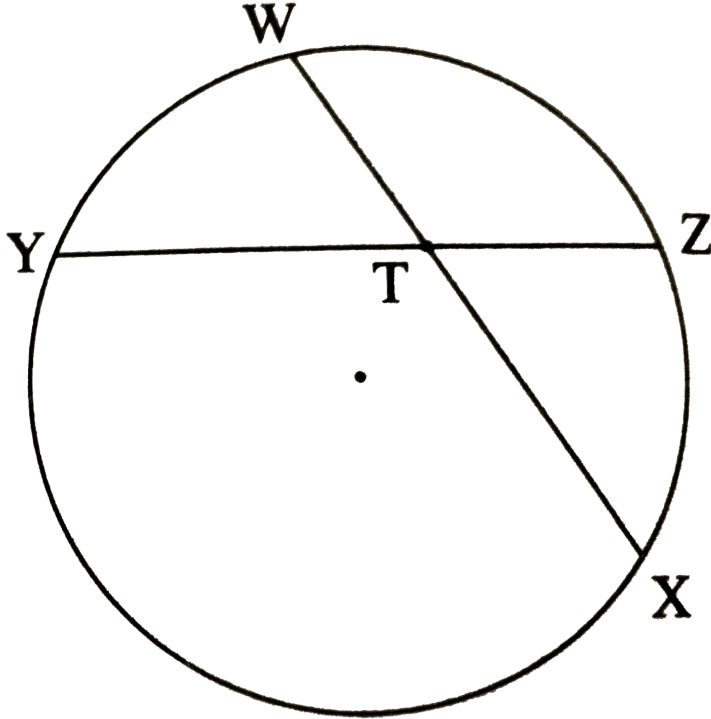
34. In the figure,  $O$  is the centre of a circle, chord  $PQ \cong$  chord  $RS$ . If  $\angle POR = 70^\circ$  and  $m(\text{arc } RS) = 80^\circ$ , find  
(arc  $QSR$ )



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35. In the figure,  $m(\text{arc } WY) = 44^\circ$ ,  $m(\text{arc } ZX) = 68^\circ$ , then

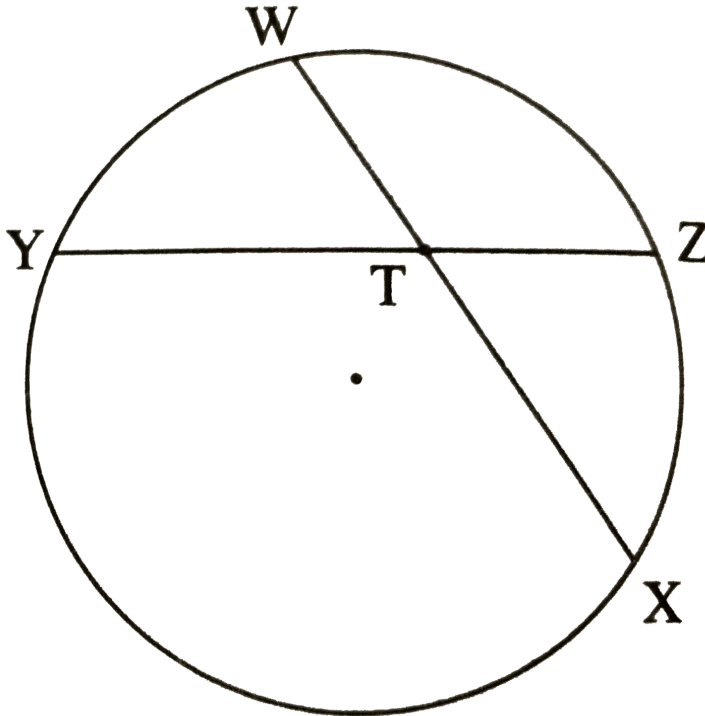
Find the measure of  $\angle ZTX$ .



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36. In the figure,  $m(\text{arc } WY) = 44^\circ$ ,  $m(\text{arc } ZX) = 68^\circ$ , then

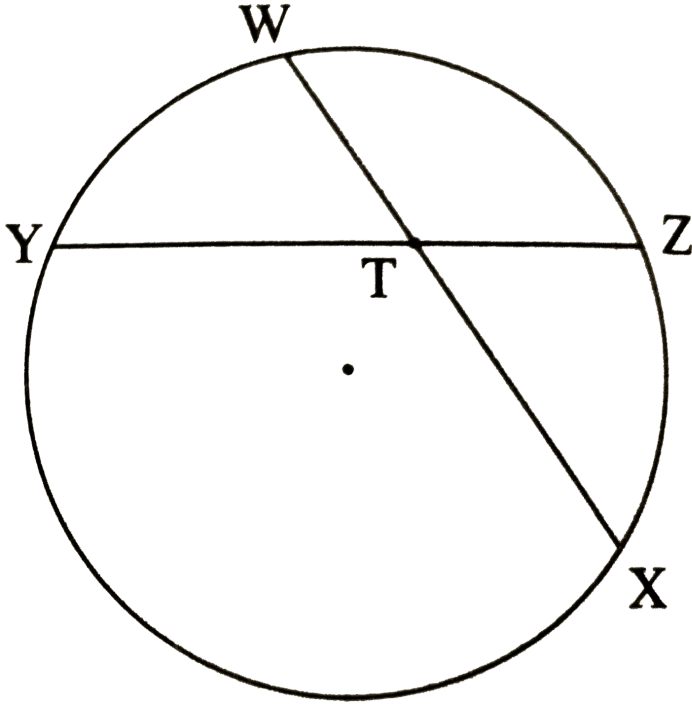
If  $WT = 4.8$ ,  $TX = 8.0$ ,  $YT = 6.4$ , find  $TZ$ .



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37. In the figure,  $m(\text{arc WY})=44^\circ$ ,  $m(\text{arc ZX})=68^\circ$ , then

If  $WX=25$ ,  $YT=8$ ,  $YZ=26$ , find  $WT$ .



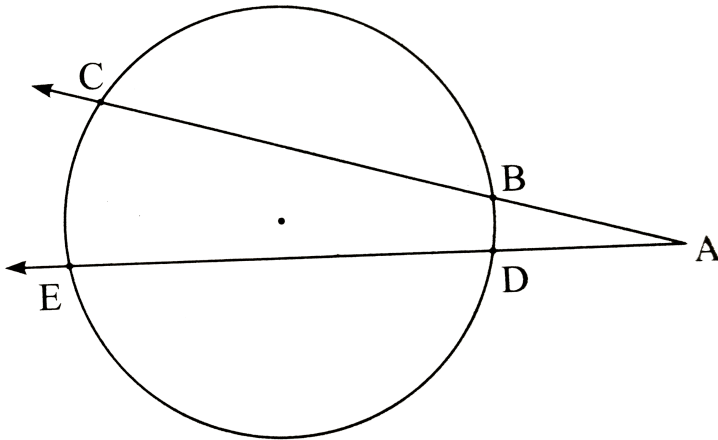
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38. In the figure,

(1)  $m(\text{arc } CE) = 54^\circ$ ,  $m(\text{arc } BD) = 23^\circ$ , find measure of  $\angle CAE$ .

(2) If  $AB = 4.2$ ,  $BC = 5.4$ ,  $AE = 12.0$ , find  $AD$ .

(3) If  $AB = 3.6$ ,  $AC = 9.0$ ,  $AD = 5.4$ , find  $AE$ .



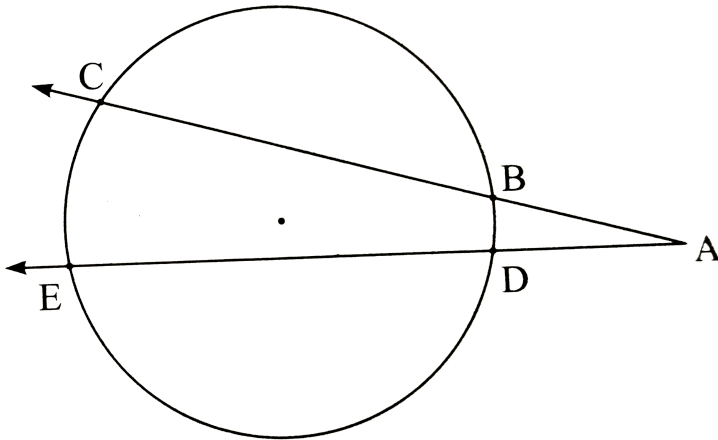
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39. In the figure,

(1)  $m(\text{arc CE}) = 54^\circ$ ,  $m(\text{arc BD}) = 23^\circ$ , find measure of  $\angle CAE$ .

(2) If  $AB = 4.2$ ,  $BC = 5.4$ ,  $AE = 12.0$ , find  $AD$ .

(3) If  $AB = 3.6$ ,  $AC = 9.0$ ,  $AD = 5.4$ , find  $AE$ .



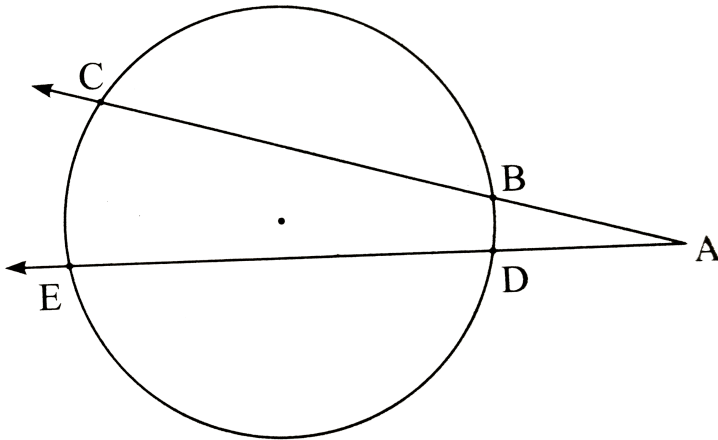
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40. In the figure,

(1)  $m(\text{arc CE}) = 54^\circ$ ,  $m(\text{arc BD}) = 23^\circ$ , find measure of  $\angle CAE$ .

(2) If  $AB = 4.2$ ,  $BC = 5.4$ ,  $AE = 12.0$ , find  $AD$ .

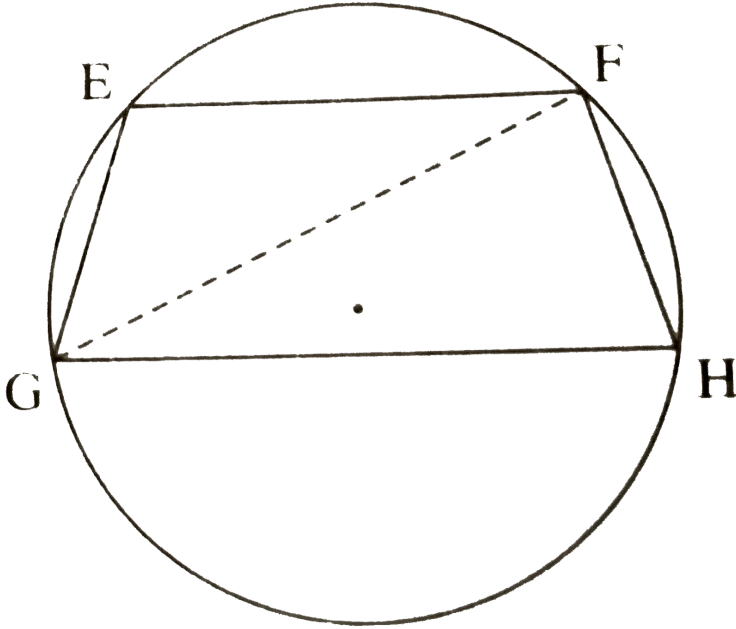
(3) If  $AB = 3.6$ ,  $AC = 9.0$ ,  $AD = 5.4$ , find  $AE$ .



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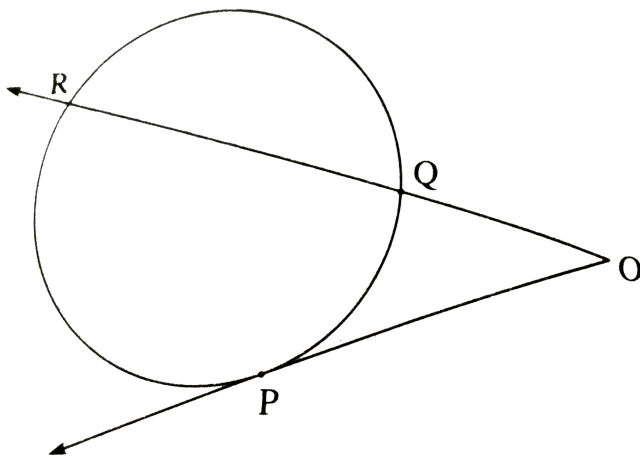
41. In the figure, chord  $EF \parallel$  chord  $GH$ . Prove that, chord  $EG \cong$  chord  $FH$ . Fill in the blanks and write the proof



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42. In the figure, P is the point of contact.

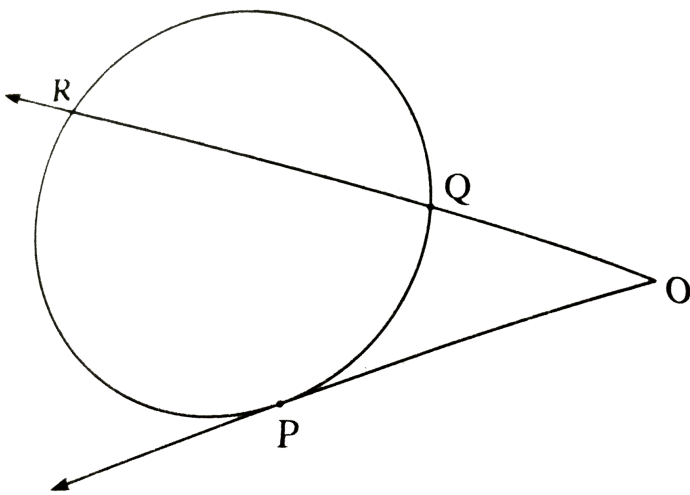
If  $m(\text{arc } PR) = 140^\circ$ ,  $\angle POR = 36^\circ$ , find  $m(\text{arc } PQ)$ .



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**43.** In the figure, P is the point of contact.

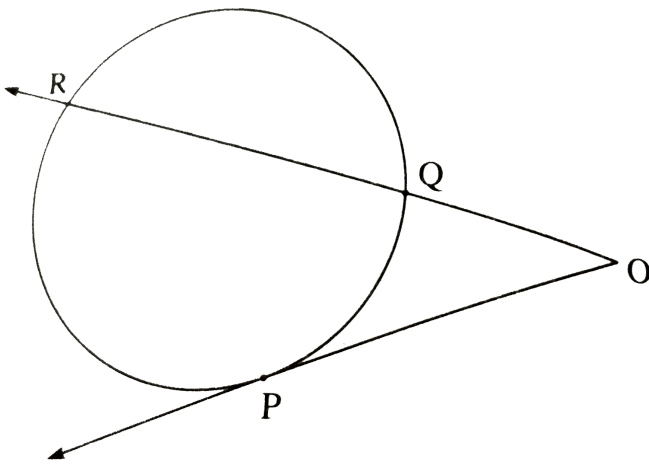
If  $OP=7.2, OQ=3.2$ , find OR and QR.



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44. In the figure, P is the point of contact.

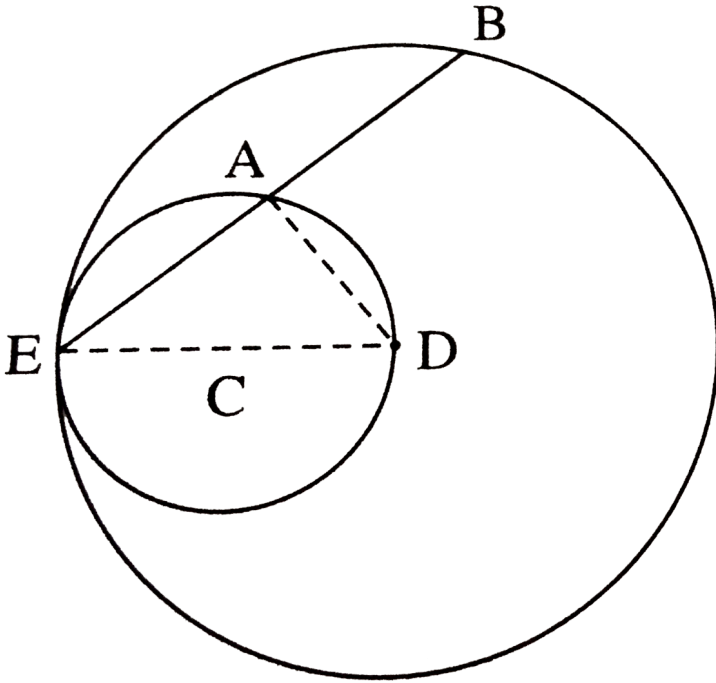
If  $OP=7.2$ ,  $OR=16.2$ , find QR.



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**45.** In figure, circles with centers  $C$  and  $D$  touch internally at point  $E$ .  $D$  lies on the inner circle. Chord  $EB$  of the outer circle intersects inner circle at point  $A$ . Prove that, seg  $EA$

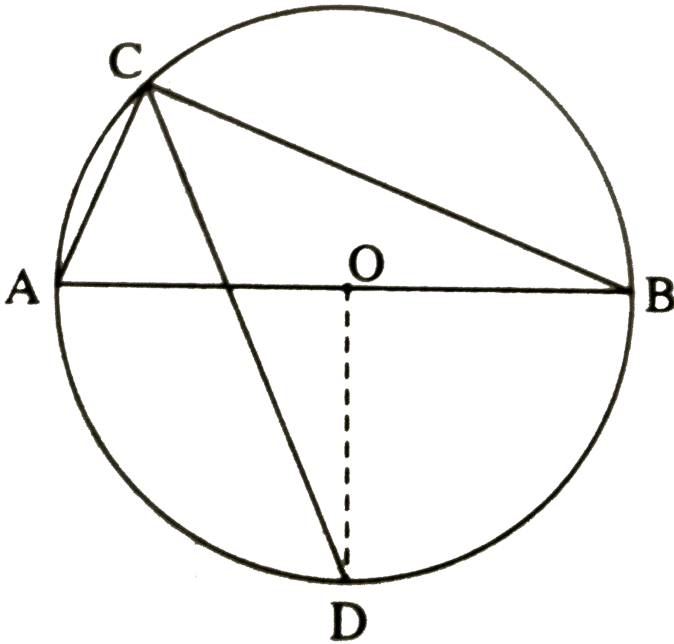
$\cong$  seg AB.



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**46.** In figure, seg AB is a diameter of a circle with centre O. The bisector of  $\angle ACB$  intersects the circle at point D. Prove that seg AD  $\cong$  seg BD. Complete the following

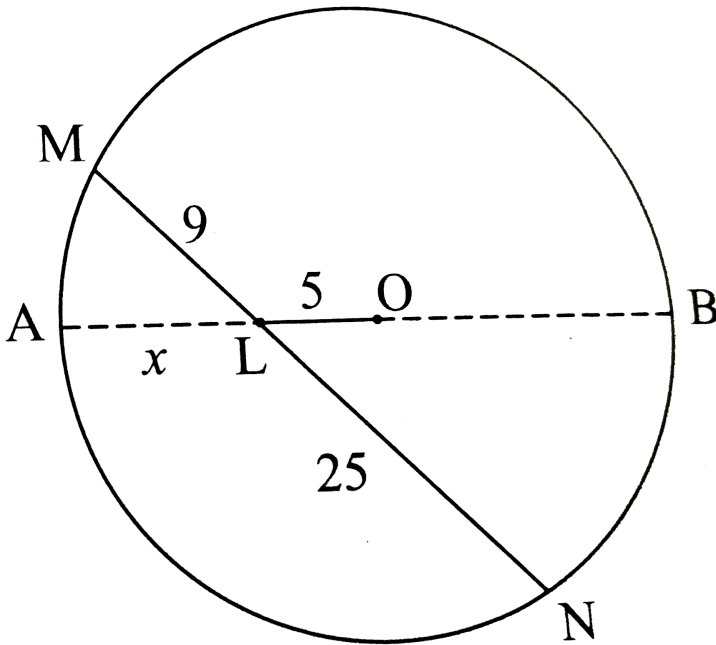
proof by filling in the blanks



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**47.** In the figure, seg  $MN$  is a chord of a circle with centre  $O$ .  $MN = 15$ ,  $L$  is a point on chord  $MN$  such that  $ML = 9$

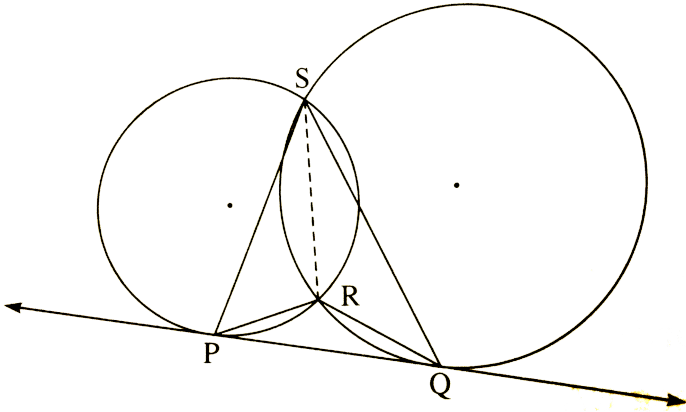
and  $d(O, L) = 5$ . Find the radius of the circle.



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**48.** In figure, two circles intersect each other at points  $S$  and  $R$ . Their common tangent  $PQ$  touches the circle at

points P,Q. Prove that,  $\angle PRQ + \angle PSQ = 180^\circ$ .

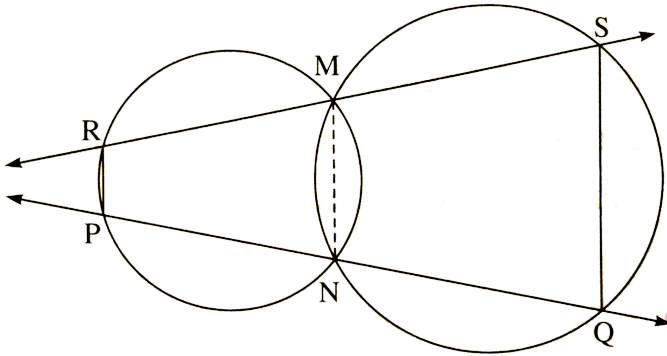


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**49.** In figure, two circles intersect at points M and N. Secants drawn through M and N intersect the circles at points R,S and P,Q respectively. Prove that :  $\text{seg } SQ \parallel \text{seg } PR$



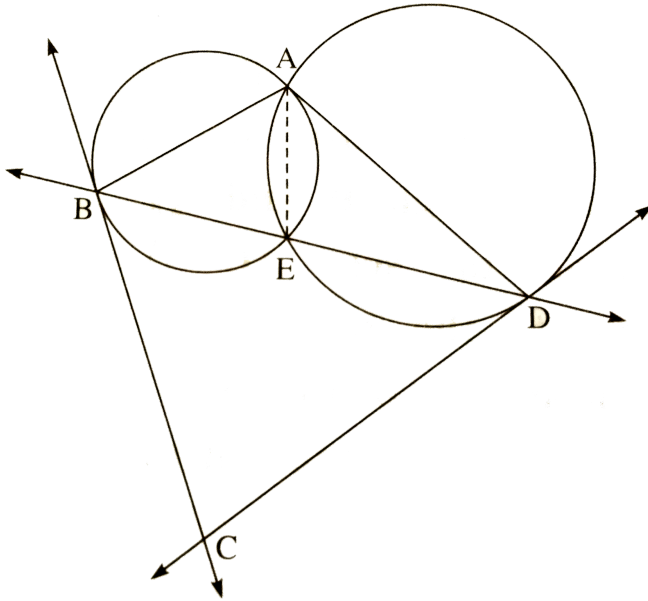
RP.



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**50.** In figure, two circles intersect each other at points A and E. Their common secant through E intersects the circles at points B and D. The tangents of the circles at points B and D intersect each other at point C. Prove

that  $\square ABCD$  is cyclic.

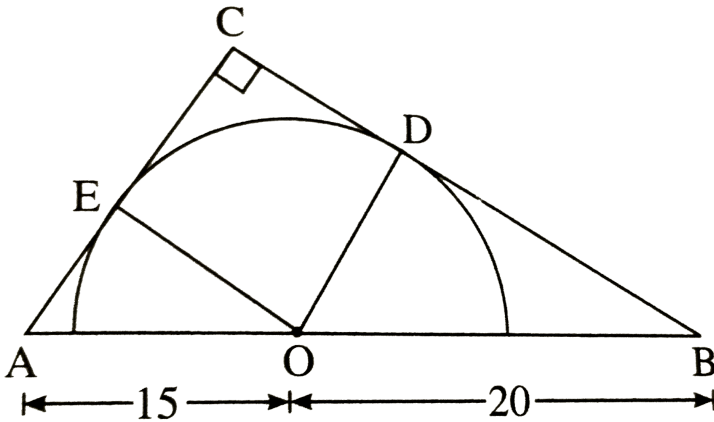


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## Challenging Questions

1. In the figure, a semicircle with its diameter on the hypotenuse of a right angled triangle, is shown touching

the remaining sides of the triangle. The two parts of the hypotenuse made by the centre of the semicircle have lengths 15 cm and 20 cm respectively. Find the radius of the semicircle.



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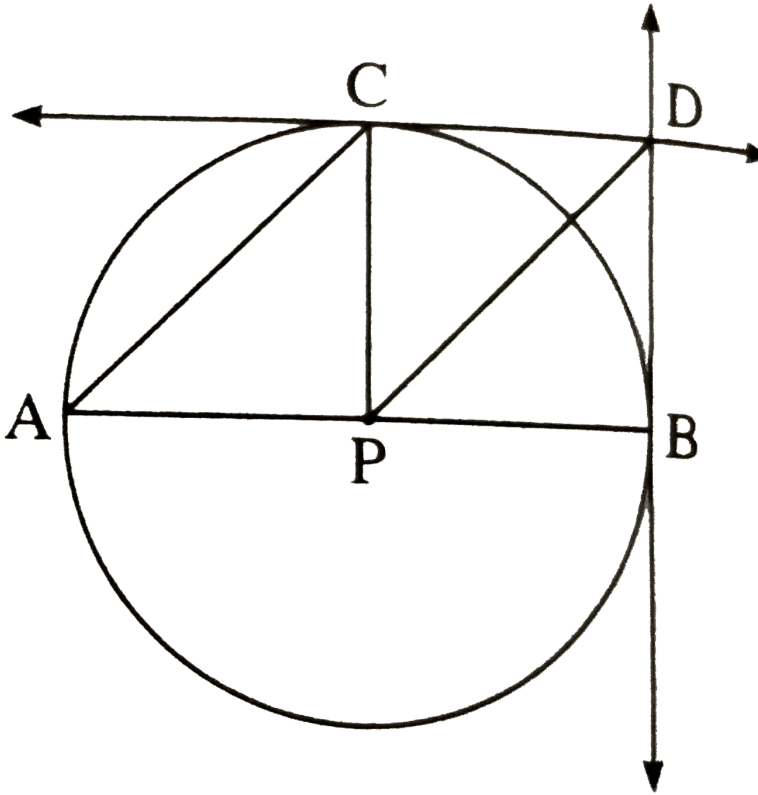
2. A square has two of its vertices on a circle and the other two on the tangent to the circle. If the diameter of the circle is 10. determine the side of the square.



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3. Seg AB is a diameter of a circle with centre P. Seg AC is a chord. A secant through P and parallel to seg AC intersects the tangent drawn at C in D. Prove that line

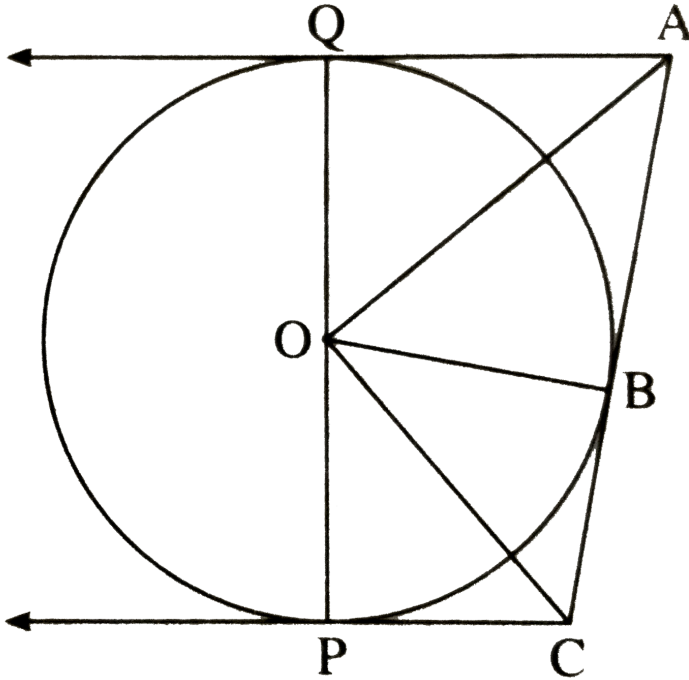
DB is a tangent to the circle.



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4. In the figure, points P, B and Q are points of contact of respective tangents. Line QA is parallel to line PC. If

$QA=7.2$  cm ,  $PC=5$  cm, find the radius of the circle.



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5. If the diagonals of a cyclic quadrilateral are perpendicular to each other, show that the line passing

through the point of intersection of diagonals and midpoint of a side is perpendicular to the opposite side.

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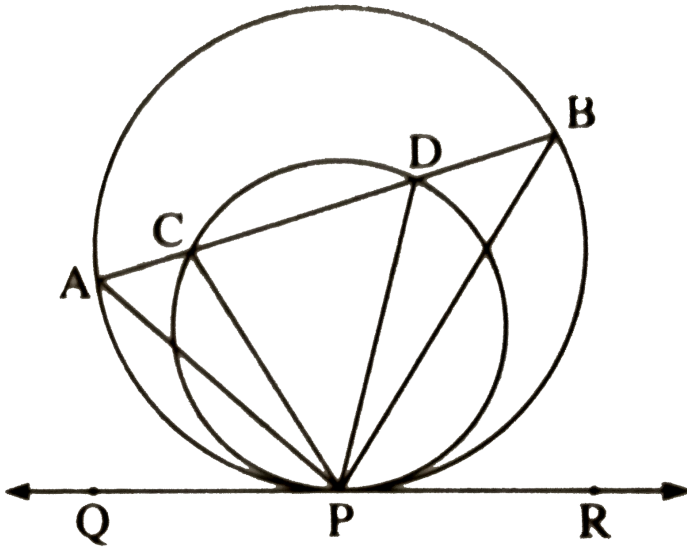
6. A cyclic trapezium is isosceles and its diagonals are equal.

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7. The diagonals of cyclic quadrilateral ABCD are congruent. Show that  $AD=BC$  and  $\text{seg } AB \parallel \text{seg } CD$ .

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8. In the figure, two circles touch internally at point P. chord AB of the larger circle intersects the smaller circle in C and D. Prove  $\angle CPA \cong \angle DPB$ .



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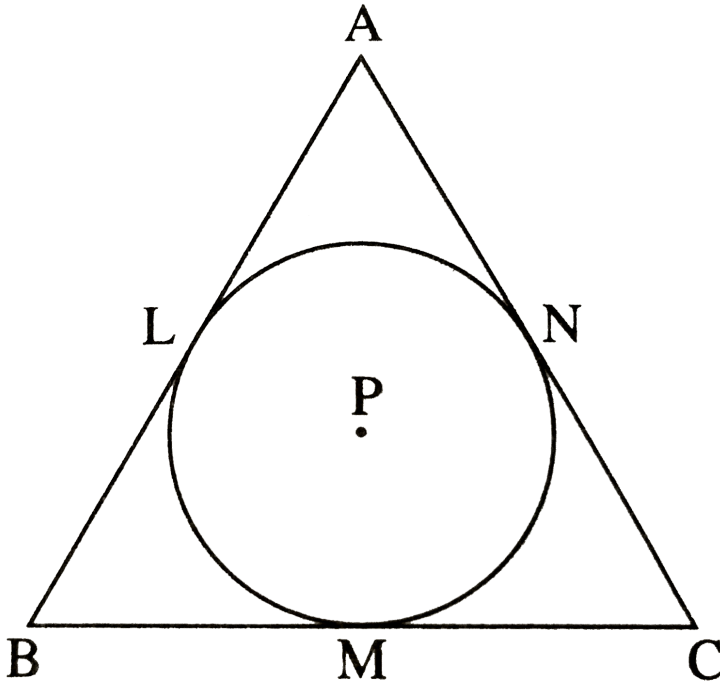
9. The quadrilateral formed by angle bisectors of a cyclic quadrilateral is also cyclic.



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10. A circle with centre  $P$  is inscribed in the  $\triangle ABC$ . Side  $AB$ , side  $BC$  and side  $AC$  touch the circle at points  $L, M$  and  $N$  respectively. Radius of the circle is  $r$ . Prove that:

$$A(\triangle ABC) = \frac{1}{2}(AB + BC + AC) \times r.$$



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