

### **MATHS**

# **BOOKS - NAVBODH MATHS (HINGLISH)**

### **PYTHAGORAS THEOREM**

#### 3 11 Mark Each

**1.** Out of the following which is a Pythagoream triplet?

A. (5, 12, 14)

- B. (3, 4, 2)
- C. (8, 15, 17)
- D. (5, 5, 2)



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**2.** In a right angled triangle,if the sum of the squares of the sides making a right angle is 169, then what is the length of the hypotenuse?

A. 15

- B. 13
- **C**. 5
- D. 12



- **3.** If a,b,c are sides of a triangle and  $a^2+b^2=c^2$ , then name the type of the triangle.
  - A. Obtuse angled triangle
  - B. Acute angled triangle

- C. Right angled triangle
- D. Equilateral triangle



- **4.** Find the perimeter of a square, if its diagonal is  $10\sqrt{2}cm$ .
  - A. 10cm
  - B.  $40\sqrt{2}cm$
  - $\mathsf{C.}\ 20cm$

D.40cm

#### **Answer:**



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**5.** In  $\Delta PQR$ , seg PM is median. PM=9,  $PQ^2+PR^2=290$  then find length of seg QR.

A. 6

B. 10

C. 16

**D.** 8



**6.** The height and base of a right angled triangle are 24cm and 18cm, find the length of its hypotenuse.

A. 24cm

B.30cm

 $\mathsf{C.}\ 15cm$ 

D. 18cm



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7. In  $\Delta ABC$ ,  $AB=6\sqrt{3}cm$ , AC=12cm,

BC = 6cm. Find the measure of  $\angle A$ .

A.  $30^{\circ}$ 

B.  $60^{\circ}$ 

C.  $90^{\circ}$ 

D.  $45^{\circ}$ 

**Answer:** 

**8.** In  $\Delta ABC$ ,  $\angle B=90^{\circ}$ . D is the midpoint of hypotenuse AC. If BD=4.5cm, then find the length of hypotenuse AC.

A. 9*cm* 

 $\mathsf{B.}\ 4.5cm$ 

 $\mathsf{C.}\,5cm$ 

D. 9.5*cm* 

### Answer:

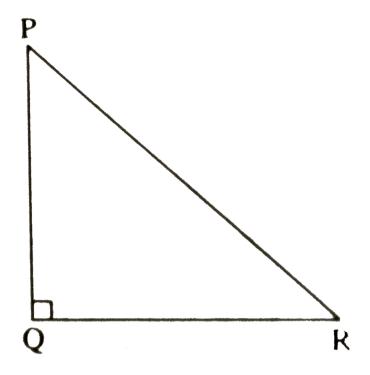


### 3 2 1 Mark Each

**1.** Observe the triplet (4, 5, 8). State whether it is a Pythagorean triplet or not.



**2.** In  $\Delta PQR$ ,  $\angle PQR=90^{\circ}$  . State the Pythagorean relation in the triangle.

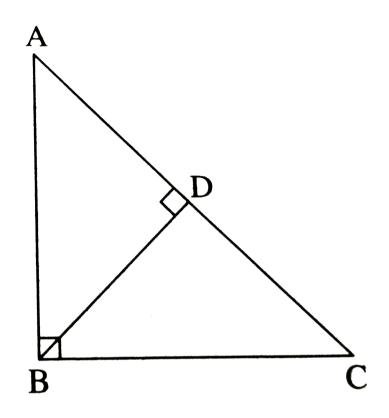




**3.** In  $\Delta ABC$ , if  $AB^2=AC^2+CB^2$ . State with reason whether  $\Delta ABC$  is a right angled triangle or not.

**4.** In the figure,  $\angle ABC=90^\circ$  and seg  $Bd\perp$  side AC, A-D-C then by property of geometric mean.  $BD^2=\square\times\square$  . Fill in the boxes with the

correct answer.

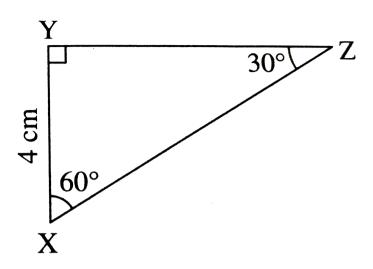




5. In  $\Delta XYZ$ ,  $\angle XYZ=90^{\circ}$ ,  $\angle YZX=30^{\circ}$ ,

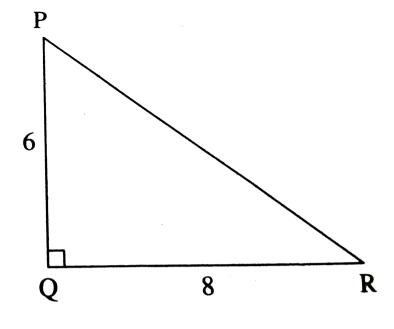
 $ngle YXZ=60^{\circ}$  , XY=4cm then write the value of

XZ.





**6.** In  $\Delta PQR$ ,  $\angle PQR=90^{\circ}$  , PQ=6 and QR=8 then the length of seg PR is...... .





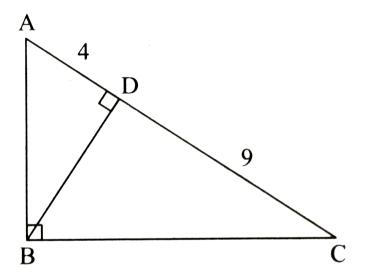
## 3 3 2 Mark Each

**1.** Is (3, 5, 4) a Pythagoren triplet ? Give reason.



**2.** In right angled  $\Delta ABC$ ,  $BD\perp AC$ . If AD=4,

DC = 9, then find BD.

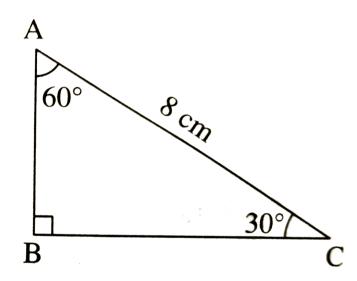




**3.** In the figure, AC=8cm,  $\angle ABC=90^{\circ}$ .

$$\angle BAC=60^{\circ}$$
 ,  $\ \ \angle ACB=30^{\circ}$  . Complete the

following activity to find AB and BC.



In  $\Delta ABC$ ,

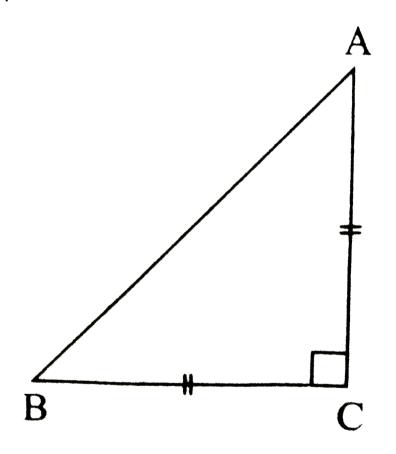
By  $30^{\circ}-60^{\circ}-90^{\circ}$  triangle theorem,

$$\therefore AB = rac{1}{2} imes AC$$
 and  $BC = -AC$ 

$$\therefore AB = rac{1}{2} imes 8$$
 and  $BC = - imes 8$ 

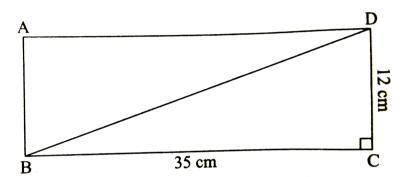
$$\therefore AB = \Box cm \text{ and } BC = \Box cm$$

**4.** In  $\Delta ABC$ , AC=BC and  $\angle ACB=90^\circ$  then prove  $AB^2=2AC^2$ 



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**5.** Find the diagonal of a rectangle whose length is 35cm and breadth is 12cm.





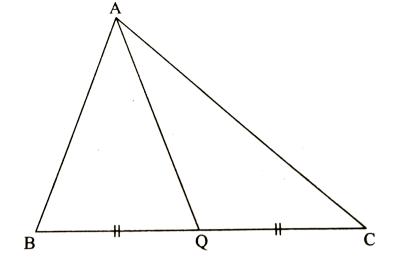
**6.** In order to prove, "In a right angled triangle, the perpendicular segment to the hypotenuse from the opposite vertex, is the geometric mean of the

segments into which the hypotenuse is divided."

- (i) Draw a neat labelled figure.
- (ii) Write 'Given' and 'To prove' from the figure drawn by you.



**7.** Complete the following activity to find the length of median AQ on side BC, if  $AB^2 + AC^2 = 122$  and BQ = 5.



In  $\Delta ABC$ ,

 $\ \, \operatorname{seg}\,AQ \text{ is the median,}$ 

$$AB^2 + \square = 2AQ^2 + 2BQ^2$$
......(Apollonius

theorem)

$$\therefore 122 = 2AQ^2 + 2(5)^2$$

$$\therefore 2AQ^2 = 122 - \square$$

On simplifying,  $\therefore AQ^2 = \Box$ 

$$\therefore AQ = \square$$
 ......(Taking square roots on both the sides)

**8.** With the help of the information given in the figure, fill in the boxes to find AB and BC.

$$AB = BC$$
.....(Given)

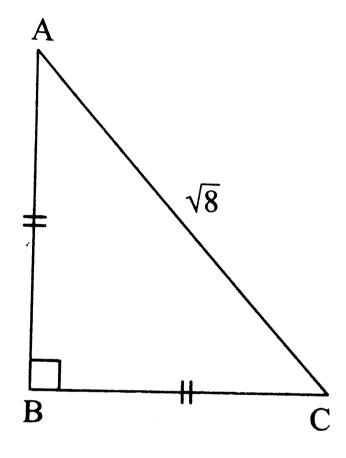
$$\therefore \angle BAC = \angle BCA = \Box$$

$$\therefore AB = BC = \square \times AC$$

$$= \square \times \sqrt{8}$$

$$= \; \Box \; imes 2\sqrt{2}$$



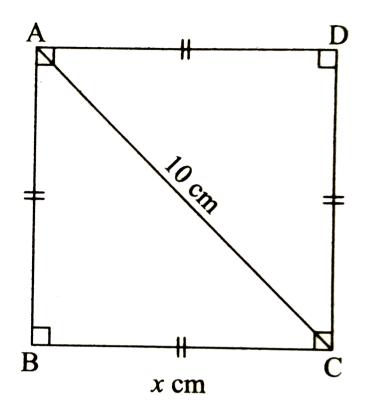




**1.**  $\square$  ABCD is a parallelogram. The diagonals AC and BD intersect at point M. The length of seg AC, AB and AD is 24, 22 and 34 respectively. Find the length of seg BD.

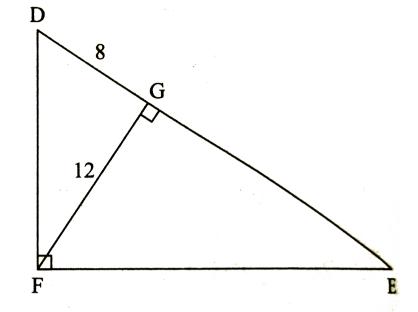


**2.** Find the side and perimeter of a square whose diagonal is 10cm.



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**3.** In the figure,  $\angle DFE=90^\circ$  , seg  $FG\perp$  side DE , DG=8, FG=12 then complete the following activity to find the length of seg DE.



In  $\Delta DFE$ ,  $\angle DFE=90^{\circ}$  ,

$$\mathsf{seg}\: FG \perp \mathsf{hypotenuse}\: DE$$

: by theorem of geometric mean,

$$FG^2 = \square imes EG$$

$$\therefore 12^2 = \square \times EG$$

$$EG = rac{12 imes 12}{\Box}$$

$$\therefore EG = \square$$

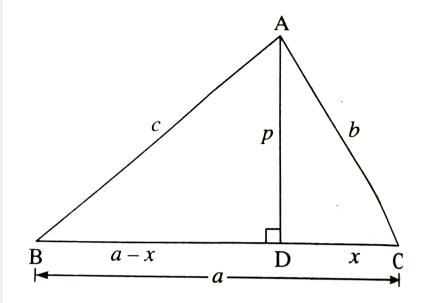
$$DE = DG + GE = 8 + \square = \square$$

**4.** In the figure, M is the midpoint of QR.

$$\angle PRQ = 90^{\circ}$$
 . Prove that  $PQ^2 = 4PM^2 - 3PR^2$ 



**5.** In  $\triangle ABC$ ,  $\angle C$  is an acute angle, seg  $AD\perp$  seg BC. Prove  $AB^2=BC^2+AC^2-2BC\times DC$  by completing the following activity.



Let AB=c, AC=b, AD=p, BC=a, DC=x

$$\therefore BD = a - x$$

In  $\Delta ADB$ , by Pythagoras theorem,

$$c^2=(a-x)^2+$$
  $\square$ 

$$c^2 = a^2 - 2ax + x^2 + \square$$
 .....(1)

In  $\Delta ADC$ , by Pythagoras theorem,

$$b^2=p^2+\ \Box$$

$$p^2 = b^2 - \square$$
 ......(2)

Substituting value of  $p^2$  from (2) in (1)

$$c^2 = a^2 - 2ax + x^2 + \ \square$$
  $c^2 = a^2 + b^2 - \ \square$ 

$$\therefore AB^2 = BC^2 + AC^2 - 2BC \times DC.$$

**6.** In  $\Delta PQR$ , seg PM is median. PM=9,

 $PQ^2 + PR^2 = 290$  then find length of seg QR.

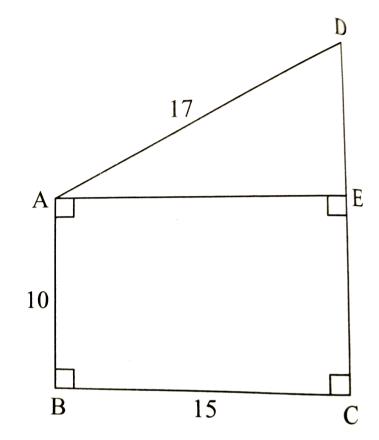


7. The perpendicular sides of a right angled triangle are 3x and 4x. The length of its hypotenuse is 30. Find the lengths of the perpendicular sides of the right angled triangle.



**8.** In the figure, AD=17, AB=10, BC=15.  $\angle ABC=\angle BCD=90^{\circ}$  seg  $AE\perp$  side CD

then find the length of  $(i)AE\,(ii)DE\,(iii)DC$ .





**9.** In  $\Delta RST$ ,  $\angle S=90^{\circ}$ .  $\angle T=30^{\circ}$ , RT=12cm, then find RS and ST.



## 3 5 4 Mark Each

1. Walls of two buildings on either side of a street are parallel to each othe. A ladder 5.8m long is placed on the street such that its top just reaches the window of a building at the height of 4m. On turning the ladder over to the other side of the street, its top touches the window of the other

building at a height 4.2m. Find the width of the street.



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2. In the adjoing figure, seg PS is the median of  $\Delta PQR$ and  $PT\perp QR$ .

i. 
$$PR^2 = PS^2 + QR imes ST + \left(rac{QR}{2}
ight)^2$$



**3.** Prove that the sum of the squares of the diagonals of parallelogram is equal to the sum of the squares of its sides.



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**4.**  $\Delta ABC$  is an equilateral triangle. Point D is on side BC such that  $BD=rac{1}{5}BC$  then prove  $25AD^2 = 21AB^2.$ 



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**Assignment 31** 

**1.** In  $\Delta LMN$ , if LM=10cm and  $\angle LNM=90^{\circ}$  ,

$$\angle LMN=30^{\circ}$$
 , then  $NM=?$ 

- A.  $5\sqrt{2}$
- $B.\,5cm$
- C.  $10\sqrt{3}cm$
- D.  $5\sqrt{3}cm$

#### Answer:



**2.** Two poles of height 100m and 111m stand vertically upright on the surface of the levelled ground. If the distance between their bases is 60m, what is the distance between their tops?

- A. 61m
- B.60m
- C. 100m
- D. 111m

#### **Answer:**



**3.** What is the length of a digonal of a square of side 10cm?

A. 
$$10\sqrt{3}cm$$

$$\mathrm{B.}\ 10\sqrt{2}cm$$

$$\mathsf{C.}\ 10cm$$

D. 
$$5\sqrt{2}cm$$

#### **Answer:**



- **4.** If two sides of the right angled triangle are  $\boldsymbol{3}$  and
- 4, then what is the length of the third side?
  - A. 5
  - B.  $\sqrt{7}$
  - C. 5 or  $\sqrt{7}$
  - D. none of these

### **Answer:**



- 5. Kartik and Pravin start cycling from some point  $\boldsymbol{A}$
- . Kartik travels due east and Pravin travels due north. After 1 hour, Pravin covers  $12 \mathrm{km}$  and Kartik travels  $5 \mathrm{km}$ . How far are they from each other?
  - A. 12km
  - B.5km
  - $\mathsf{C.}\ 13km$
  - D.17km

### **Answer:**



**6.** If in  $\Delta ABC$ , seg AM is the median,

$$AB^2 + AC^2 = 410$$
 and  $BC = 12$  then  $AM = ?$ 

- A. 12
- B.13
- $\mathsf{C.}\,\sqrt{17}$
- D.  $\sqrt{13}$

### Answer:



**7.** The length of the hypotenuse PR of an isosceles right angled triangle PQR, where PQ is 4cm, is

- A. 4cm
- $\mathrm{B.}~4\sqrt{3}cm$
- $\mathrm{C.}\,4\sqrt{2}cm$
- D. 16cm

#### **Answer:**



**8.**  $\Delta PQR$  is an equilateral triangle having length of side as 8cm. Find the height of  $\Delta PQR$ .

A. 
$$2\sqrt{3}cm$$

B. 
$$4\sqrt{8}cm$$

$$\mathsf{C.}\,3\sqrt{2}cm$$

D. 
$$4\sqrt{3}cm$$

#### **Answer:**



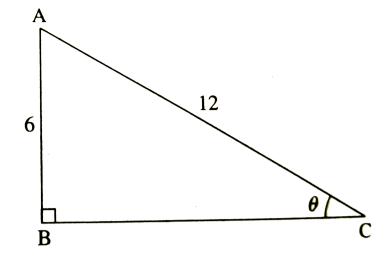
**1.** Observe the triplet (11, 12, 17). State whether it is a Pythagorean triplet or not.



**2.** In  $\Delta PQR$ ,  $PQ^2=PR^2+QR^2$  then state which angle will be the right angle.



**3.** In the figure , AB=6 and AC=12, then what is the value of heta ? Why

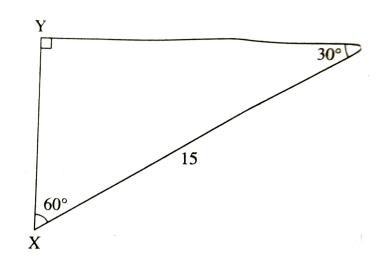




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**4.** In  $\Delta XYZ$ , XZ=15,  $\angle YZX=30^{\circ}$ ,

 $\angle YXZ=60^\circ$  then XY= ......and YZ= ......

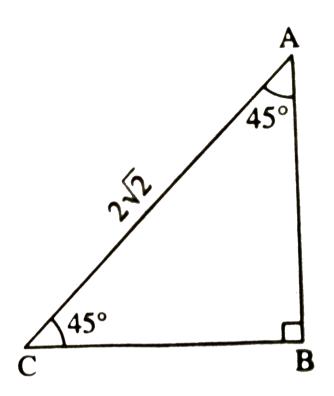




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5. In  $\triangle ABC$ ,  $\angle BAC = \angle BCA = 45^{\circ}$ ,

 $\angle ABC = 90^\circ$  then the value of AB.

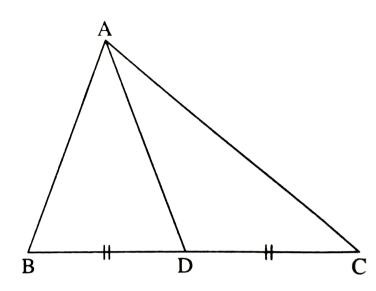




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**6.** In  $\triangle ABC$ , D is the midpoint of side BC. Fill in the boxes with correct answer

 $AB^2 + AC^2 = \Box + \Box.$ 

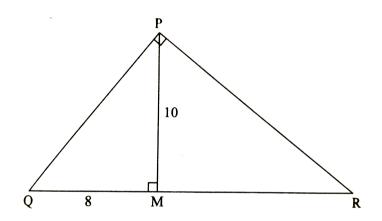




Assignment 3 3

- **1.** Is (5, 12, 13) a Pythagorean triplet ? Give reason.
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**2.** In the figure,  $\angle QPR=90^{\circ}$  , seg  $PM\perp$  seg QR and Q-M-R , PM=10 . QM=8 , find QR .





**3.** In  $\Delta ABC$ ,  $\angle ABC=90^{\circ}$ , AB=12, BC=16 and seg BP is the median drawn to side AC. Find

the length of seg BP.

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**4.** Do sides 7cm, 24cm, 25cm form a right angled triangle? Give reason.



**5.** Find the length of a diagonal of a rectangle having sides 11cm and 60cm.



**6.** Find the length of the hypotenuse of a right angeled triangle, if the remaining sides are 9cm and 12cm.

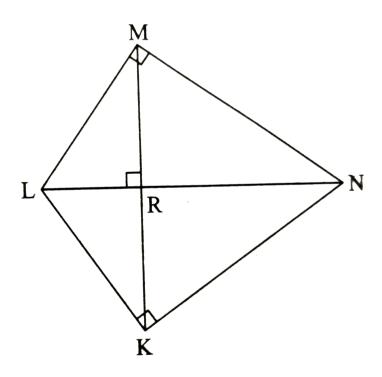


**7.** Find the side of a square whose diagonal is  $16\sqrt{2}cm$ .



**8.** In the figure,  $\angle LMN = \angle LKN = 90^{\circ}$  seg  $MK \perp \,\,$  seg LN.

Complete the following activity to prove R is the midpoint of  ${\rm seg}\ MK$ .



Proof: In  $\Delta LMN$ ,  $\angle LMN = 90^{\circ}$  seg  $MR \perp$  hypotenuse LN

... by property of geometric mean,

 $MR^2 = \square \times RN$ 

In  $\Delta LKN$ ,  $\angle LKN=90^\circ$ 

 $\log KR \perp \ \ \mathsf{hypotenuse} \ LN$ 

... by property of geometric mean,

 $KR^2 = LR \times \square$ 

From (1) and (2), we get

 $MR^2 = \square : MR = \square.$ 

 $\therefore R$  is the midpoint of seg MK.



**9.** In order to prove, 'In a right angled triangle, the square of the hypotenuse is equal to the sum of

the squares of remaining two sides

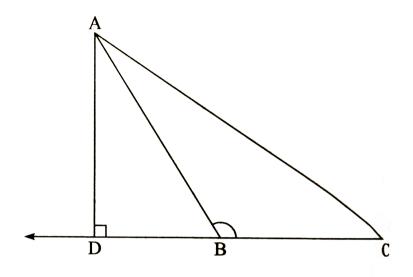
- (i) Draw a near labelled figure.
- (ii) Write 'Given' and 'To Prove' from the figure drawn by you.



## Assignment 3 4

1. In obtuse angled  $\Delta ABC$ ,  $\angle B>90^{\circ}$ . If seg  $Ad\perp$  ray CB and D-B-C, then prove that

 $AC^2 = AB^2 + BC^2 + 2BC \cdot DB.$ 





**2.** Find the length of the side and perimeter of an equilateral triangle whose height is  $4\sqrt{3}cm$ .



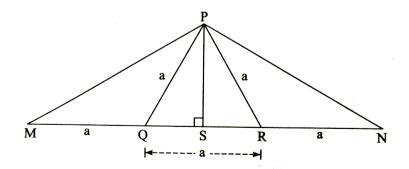
**3.** Find the diagonal of a rectangle whose length is 16cm and area 192sqcm.



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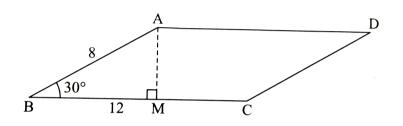
**4.** From the information given in the figure, prove that

$$PM = PN = \sqrt{3} \times a.$$



**5.** In the figure,  $\Box ABCD$  is a parallelogram.

$$AB=8$$
,  $BC=12$  and  $\angle B=30^{\circ}.$  Find  $Area(ABCD).$ 

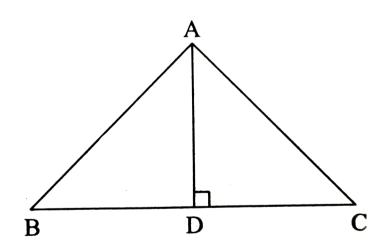




**6.** D is the midpoint of side BC of  $\Delta ABC$ . If AB=4, AC=6 and BC=8, then find l(AD) and hence perimeter of  $\Delta ABD$ .

**7.** In the figure, seg  $AD \perp$  side BC and B-D-C, then prove

$$AB^2 - BD^2 = AC^2 - CD^2.$$



**8.** In the figure, smaller diagonal AC of a kite

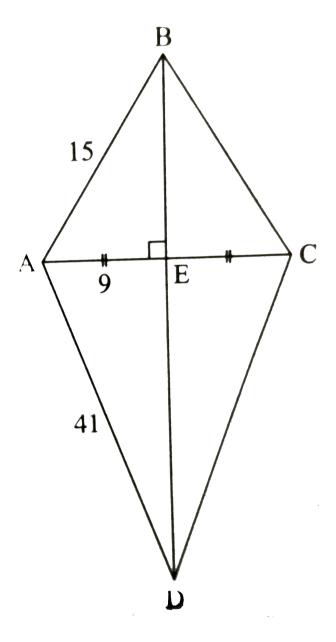
ABCD is 18cm long. AB=15cm and

AD=41cm. Find the length of

(i)BE

(ii)ED

(iii)BD





**9.** In an equilateral riangle ABC, AD is the altitude drawn from A on the side BC. Prove that  $3AB^2=4AD^2$ 

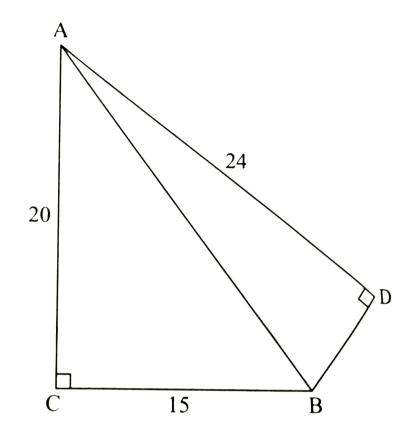


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10. In the figure,

AC = 20, CB = 15, AD = 24.

Find AB and BD.





**11.** Ramesh goes 24km to south, then turns and goes to west for 10km

 $\left(i\right)$  From the given information, drw a proportionate figure.

(ii) If starting point and end point are joined, then which type triangle do we get?

 $\left(iii\right)$  At last how far is he from the starting point?



**12.**  $\Delta PQR$  is an equilateral triangle. Seg  $PS \perp$  side QR such that Q-S-R. Prove  $PS^2=3QS^2$  by completing the following activity.

In  $\Delta PQS$ ,

$$\angle PSQ = \square$$
 .....(Given)

$$\angle Q = \; \square$$
 .....(Angle of an equilateral triangle)

$$\therefore$$
  $\angle QPS=30^{\circ}$  .....(Remaining angle of

$$\Delta PQS$$
)

$$\therefore \Delta PQS$$
 is a  $\square$  triangle

$$PS = \ \Box \ PQ$$
.....(Side opposite to  $60^\circ$ )....(1)

and 
$$QS = \ \Box \ PQ$$
.....(Side opposite to  $30^\circ$ )

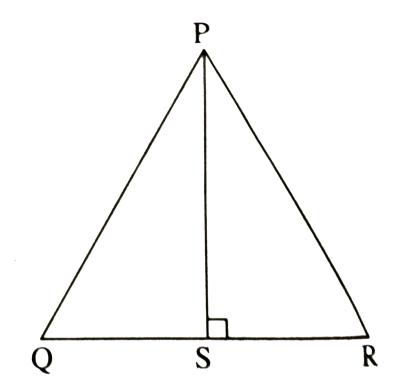
$$PQ = 2QS....(2)$$

Substituting value of PQ from (2) in (1)

$$PS = rac{\sqrt{3}}{2} imes 2QS$$

$$\therefore PS = \Box QS$$

 $\therefore PS^2 = 3QS^2$ .....(Square both the sides)





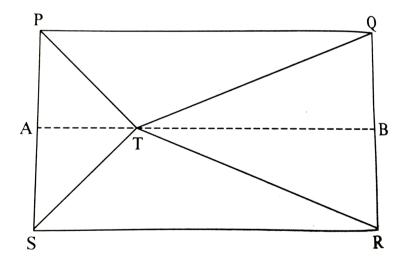
**1.** In the figure , point T is in the interior of rectangle PQRS.

Prove that,

and A-T-B.)

$$TS^2 + TQ^2 = TP^2 + TR^2$$

(As shown in the figure, draw seg  $AB \mid \mid$  side SR



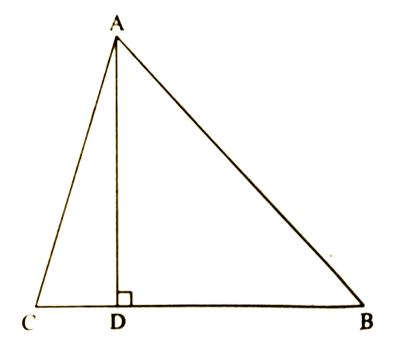


**2.** In  $\triangle ABC$ ,

 $\operatorname{seg} AD \perp \operatorname{seg} BC$ ,

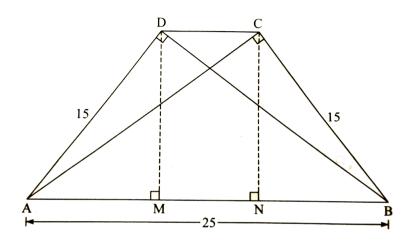
$$DB = 3CD$$
.

Prove that  $2AB^2=2AC^2+BC^2$ .





**3.** In a trapezium ABCD, seg  $AB \mid \mid$  seg DC, seg  $BD \perp$  seg AD, seg  $AC \perp$  seg BC, if AD = 15, BC = 15 and AB = 25. Find  $A(\Box ABCD)$ .





**4.** Show that if the diagonals of a quadrilateral cut each other in a right angle, then the sum of the squares of opposite sides are equal.



**5.** Starting from Madhav's house, John first goes 12m north, then 73m west, then 67m south and finally 25m east and reaches Mohamad's house. The what is the direct distance between Madhav's and Mohamad's houses?



Examples For Practice 1 Mark Multiple Choice Questions

1. Out of the given triplets, which is not a

Pythagorean triplet?

A. (104,96,40)

B.(52, 20, 48)

 $\mathsf{C.}\,(32,15,30)$ 

D. (61,60,11)

**Answer: D** 



**2.** In 
$$\Delta LMN$$
, if  $LM=10cm$  and  $\angle LNM=90^{\circ}$  ,

$$\angle LMN=30^{\circ}$$
 , then  $NM=?$ 

- A.  $5\sqrt{2}$  cm
- B. 5 cm
- C.  $10\sqrt{3}$  cm
- D.  $5\sqrt{3}$ cm

## **Answer: D**



**3.** Two poles of height 100m and 111m stand vertically upright on the surface of the levelled ground. If the distance between their bases is 60m, what is the distance between their tops?

A. 61 m

B. 60 m

C. 100 m

D. 111 m

## **Answer: A**



**4.**  $\Delta PQR$  is an equilateral triangle. Seg  $PS\perp$  side QR such that Q-S-R. Prove  $PS^2=3QS^2$  by completing the following activity.

In  $\Delta PQS$ ,

$$\angle PSQ = \square$$
 .....(Given)

$$\angle Q = \ \square$$
 .....(Angle of an equilateral triangle)

$$\therefore$$
  $\angle QPS=30^{\circ}$  .....(Remaining angle of

$$\Delta PQS$$
)

$$\therefore \Delta PQS$$
 is a  $\square$  triangle

$$PS = \ \Box \ PQ$$
.....(Side opposite to  $60^\circ$ ).....(1)

and 
$$QS = \ \Box \ PQ$$
.....(Side opposite to  $30^\circ$ )

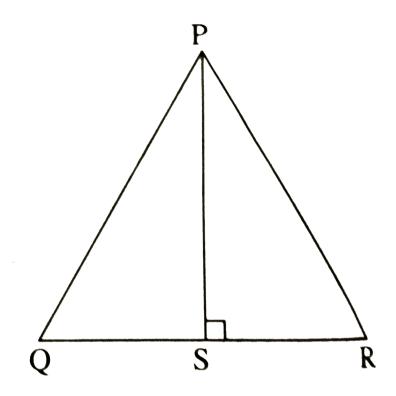
$$PQ=2QS$$
 ....(2)

Substituting value of PQ from (2) in (1)

$$PS=rac{\sqrt{3}}{2} imes 2QS$$

$$\therefore PS = \Box QS$$

$$\therefore PS^2 = 3QS^2$$
.....(Square both the sides)



A.  $4QS^2$ 

 ${\sf B.}\,3QS^2$ 

C. 
$$rac{3}{2}QS^2$$

### **Answer: B**



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5. Find the diagonal of a square whose side is 10 cm.

A.  $10\sqrt{3}$  cm

B.  $10\sqrt{2}cm$ 

 $\mathsf{C}.\,10cm$ 

D.  $5\sqrt{2}$  cm

**Answer: B** 



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**6.** In and segBD bot sideAC and AD=DC` then

A. 
$$BD^2=DC imes AC$$

$${\tt B.}\,BD^2=AD\times AC$$

$$\mathsf{C.}\,BD^2=DC\times AC$$

D. none of these

#### **Answer: A**



## **View Text Solution**

- 7. If two sides of the right angled triangle are <math>3 and
- 4, then what is the length of the third side?
  - A. 5
  - B.  $\sqrt{7}$
  - C. 5 or  $\sqrt{7}$
  - D. none of these

### **Answer: C**

**8.** Kartik and Pravin start cycling from some point A . Kartik travels due east and Pravin travels due north. After 1 hour, Pravin covers 12km and Kartik travels 5km. How far are they from each other?

A. 12 km

B. 5 km

C. 13 km

D. cannot be determined

Answer: C

**9.** If in  $\Delta ABC$ , seg AM is the median,

$$AB^2+AC^2=410$$
 and  $BC=12$  then  $AM=\,?$ 

A. 12

B. 13

 $C.\sqrt{12}$ 

D.  $\sqrt{13}$ 

**Answer: B** 



10. The length of the hypotenuse PR of an isosceles right angled triangle PQR, where PQ is 4cm, is

- A. 4 cm
- B.  $4\sqrt{3}$  cm
- C.  $4\sqrt{2}$  cm
- D. 16 cm

**Answer: C** 



**11.** Out of the following which is a Pythagorean triplet?

A. (5,12,14)

B. (3,4,2)

C. (8,15,17)

D. (5,5,2)

#### **Answer: C**



**1.** In right angled triangle, the lengtj of the perpendicular sides are 15 cm and 8 cm. Find the length of its hypotenuse.



2. If the sides of the triangle are 12, 35 and 37, determine whether the triangle is a right angled triangle. Justify.



3. 10 m लंबी एक सीढी एक दीवार पर टिकाने पर भूमि से 8 m की उँचाई पर स्थित एक खिड़की तक पहुँचती है । दीवार के आधार से सीढी के निचले सिरे की दूरी ज्ञात कीजिए ।



**4.** Determine whether (11,12,15) is a Pythagorean triplet ? Justify .



**5.** Find the side of a square whose diagonal is  $16\sqrt{2}cm$ .

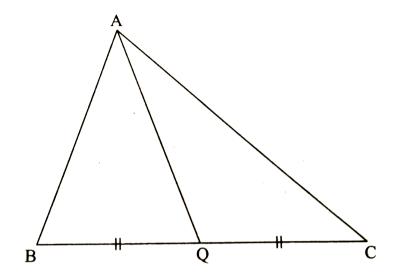


**6.** Find the perimeter of an isosceles right angled triangle with each of its congruent sides as 7 cm.



**7.** Complete the following activity to find the length of median AQ on side BC, if  $AB^2 + AC^2 = 122$ 

and BQ=5.



In  $\Delta ABC$ ,

 $\operatorname{seg} AQ$  is the median,

$$AB^2 + \square = 2AQ^2 + 2BQ^2$$
......(Apollonius

theorem)

$$\therefore 122 = 2AQ^2 + 2(5)^2$$

$$\therefore 2AQ^2 = 122 - \square$$

On simplifying,  $\therefore AQ^2 = \Box$ 

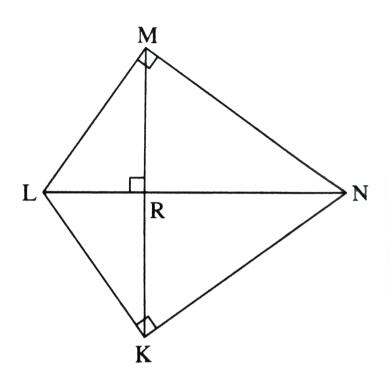
 $\therefore AQ = \square$  ......(Taking square roots on both the sides)



**8.** In the figure ,  $\angle LMN = \angle LKN = 90^{\circ}$  seg MK  $\perp$  seg LN .

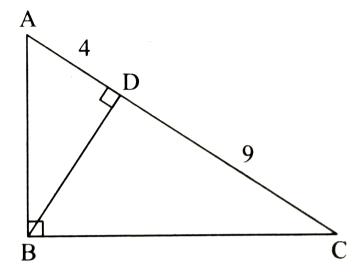
Complete the following activtiy

to prove R is the midpoint of seg MK.





**9.** In right angled  $\Delta ABC$ ,  $BD\perp AC$ . If AD=4, DC=9, then find BD.





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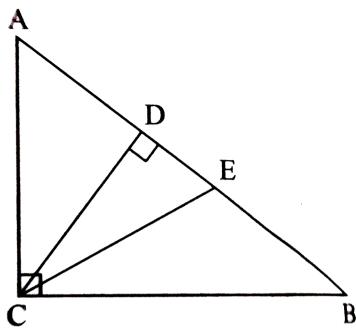
# **Examples For Practice 3 Mark Questions**

1. किसी समबाहु त्रिभुज में , सिद्ध कीजिए कि उसकी एक भुजा के वर्ग का तिगुना उसके एक शीर्षलंब के वर्ग के चार गुने के बराबर होता है । **2.** In  $\Delta PQR$ , seg PM is median. PM=9,  $PQ^2+PR^2=290$  then find length of seg QR.



**3.** In  $\Delta ABC$ ,  $\angle ACB=90^{\circ}$ ,  $~ {
m seg}~ CD \perp ~ {
m side}$  AB and seg CE is angle bisector of  $\angle ACB$ 

Prove :  $\frac{AD}{BD} = \frac{AE}{BE^2}$ 





**4.** In right angled  $\Delta BAC$ ,  $\angle BAC=90^\circ$  ,segments AD,BE and CF are medians.Prove that  $2ig(AD^2+BE^2+CF^2ig)=3BC^2$ 

**5.** Three times the sum of square of the sides of a triangle is equal to four times the sum of the square of the medians of the triangle.



**6.** Suppose m and n are any two numbers . If  $m^2-n^2$ , 2mn and  $m^2+n^2$  are the three sides of a triangle , then show that it is a right angled triangle and hence write any two pairs of Pythagorean triplet .

**7.** Show that if the diagonals of a quadrilateral cut each other in a right angle, then the sum of the squares of opposite sides are equal.



**8.** Starting from Madhav's house, John first goes 12m north, then 73m west, then 67m south and finally 25m east and reaches Mohamad's west , then 67m south and finally 25m east and reaches

Mohamad's house. The whast is the direct distance between Madhav's and Mohamad's houses?



## **Examples For Practice 2 Mark Questions**

1. Each side of a rhombus is 10 cm long and one of its diagonals measures 16 cm. Find the length of the other diagonal and hence find the area of the rhombus.



2. Adjacent sides of a parallelogram are 11 cm and 17 cm. If the length of one of its diagonal is 26 cm, find the length of the other.



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### **Practice Set 21**

**1.** Idenetify, with reason, which of the following are Pythagorean triplets:

(3,5,4)



**2.** Idenetify , with reason , which of the following are Pythagorean triplets :

(4, 9, 12)



**3.** Is (5, 12, 13) a Pythagorean triplet ? Give reason.



**4.** Idenetify, with reason, which of the following are Pythagorean triplets:

(24,70,74)



**5.** Idenetify , with reason , which of the following are Pythagorean triplets :

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**6.** Idenetify, with reason, which of the following are Pythagorean triplets:

(11,60,61)

(10,24,27)

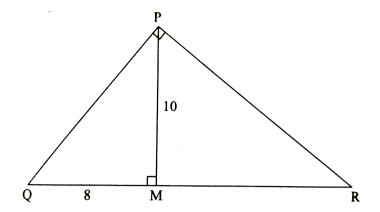
7. In the adjoining figure,

$$\angle MNP = 90^{\circ}\,, segNQ \perp segMP$$
,MQ=9,QP=4 find

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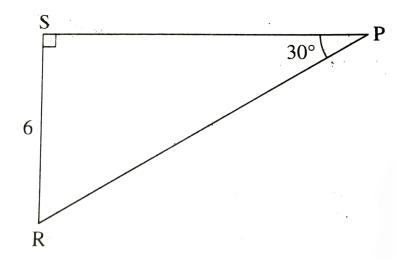
NQ.

**8.** In the figure,  $\angle QPR=90^{\circ}$  , seg  $PM\perp$  seg QR and Q-M-R , PM=10 . QM=8 , find QR .





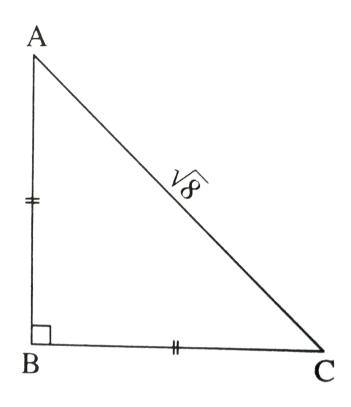
**9.** See flugre Find RP and PS using the ingormation given in  $\triangle$  PSR





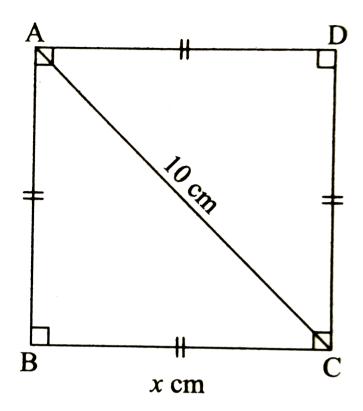
10. For finding AB and BC with the help of information given in figure, complete following

activity:





11. Find the side and perimeter of a square whose diagonal is 10cm.



0

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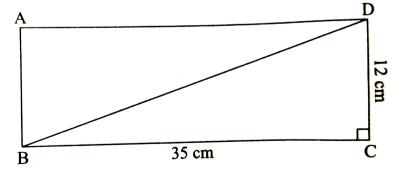
**12.** In the adjoining figure,  $\angle DFE = 90^{\circ}, FG \perp ED. \ If GD = 8, FG = 12,$  find

- (i) EG
- (ii) FD, and
- (iii) EF

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13. Find the diagonal of a rectangle whose length is

35cm and breadth is 12cm.



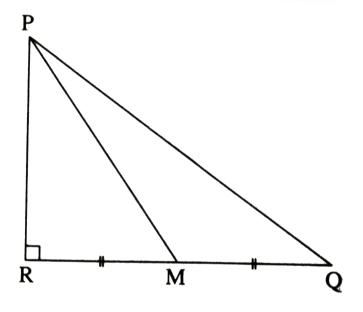


14. In the figure, M is the midpoint of QR.

$$\angle PRQ = 90^{\circ}$$
.

Prove that,

$$PQ^2 = 4PM^2 - 3PR^2.$$





**15.** Walls of two buildings on either side of a street are parallel to each othe. A ladder 5.8m long is placed on the street such that its top just reaches the window of a building at the height of 4m. On turning the ladder over to the other side of the street, its top touches the window of the other building at a height 4.2m. Find the width of the street.



**1.** In  $\Delta PQR$ , point S is the midpoint of side QR. If

PQ =11, PR =17 PS =13 , find QR.

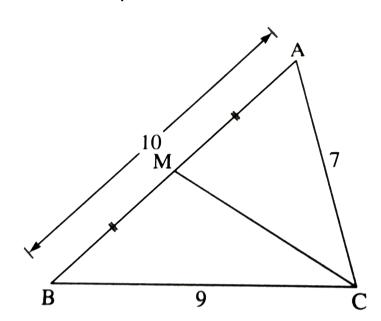


**2.** In 
$$\ \triangle \ ABC$$
 ,  $AB=10$ 

$$AC = 7, BC = 9$$

then find the length find the length of the median

drawn from point C to side AB.





 $\Delta PQR{
m seg}PS$ is median of $\Delta PQR$ . And $PT\perp QR$ ,

(i) 
$$PR^2=PS^2+QR imes ST+\left(rac{QR}{2}
ight)^2$$

**4.** In  $\Delta ABC$ , point M is the midpoint of BC,  $AB^2 + AC^2 = 290cm$ , AM=8cm,find BC.



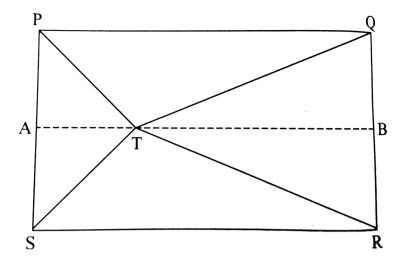
**5.** In the figure , point T is in the interior of rectangle PQRS.

Prove that,

$$TS^2 + TQ^2 = TP^2 + TR^2$$

(As shown in the figure, draw seg  $AB \mid \; \mid \;$  side SR

and A - T - B.)





### **Problem Set 2**

**1.** Out of the following which is the Pythagorean triplet?

- A. (1,5,10)
- B. (3,4,5)
- C.(2,2,2)
- D. (5,5,2)

#### **Answer: B**



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**2.** In a right angled triangle,if the sum of the squares of the sides making a right angle is 169, then what is the length of the hypotenuse?

- **A.** 15
- B. 13
- C. 5
- D. 12

#### **Answer: B**



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**3.** out of the dates given below which date constitutes a Pythagorean triplet?

A. 15/18/16

- B. 16/08/16
- C.3/5/17
- D. 4/9/15

## **Answer: A**



- **4.** If a, b, c are sides of a triangle and  $a^2 + b^2 = c^2$ , then name the type of the triangle.
  - A. Obtuse angled triangle.
  - B. Acute angled triangle

- C. Right engled triangle
- D. Equilateral triangle

**Answer: C** 



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**5.** Find the perimeter of a square, if its diagonal is  $10\sqrt{2}cm$ .



**6.** Altitude on the hypotenuse of a right angled triangle triangle divides it in two parts of lengths 4 cm and 9 cm. Find the length of the altitude.

- A. 9 cm
- B. 4 cm
- C. 6 cm
- D.  $2\sqrt{6}$  cm

## **Answer: C**



**7.** The height and base of a right angled triangle are 24cm and 18cm, find the length of its hypotenuse.

A. 24 cm

B. 30 cm

C. 15 cm

D. 18 cm

**Answer: B** 



8. In

 $\Delta ABC, AB = 6\sqrt{3}cm, AC = 12cm \text{ and } BC = 6cm$ 

. Then  $\angle B$  is

A.  $30^{\circ}$ 

 $B.60^{\circ}$ 

C.  $90^{\circ}$ 

D.  $45^{\circ}$ 

**Answer: A** 



**9.** Find the length of the altitude of an equilateral triangle of side 2a cm.



**10.** Do sides 7 cm , 24 cm , 25 cm from a right angled triangle ? Give reason .



**11.** Find the length of a diagonal of a rectangle having sides 11cm and 60cm.



12. Find the length of the hypotenuse of a right angeled triangle, if the remaining sides are 9cm and 12cm.



**13.** A side of an isosceles right angled triangle is x.

Find its hypotenuse.



14.

In

 $\Delta PQR, PQ = \sqrt{8}, QR = \sqrt{5}, PR = \sqrt{3}. \ Is \Delta PQR$ 

a right angled triangle? If yes, which angle is of  $90^\circ$ ?

**15.** In  $\triangle RST$ ,  $\angle S = 90^{\circ}$ .  $\angle T = 30^{\circ}$ , RT = 12cm,



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then find RS and ST.



**16.** Find the diagonal of a rectangle whose length is 16cm and area 192sqcm.



**17.** Find the length of the side and perimeter of an equilateral triangle whose height is  $\sqrt{3}$  cm



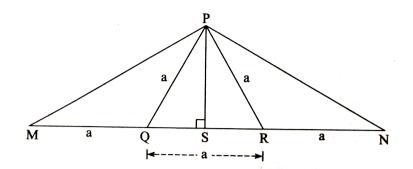
**18.** In  $\Delta ABC$ , seg AP is a median. If BC = 18,  $AB^2 + AC^2 = 260$  then find the length of AP.

**19.**  $\Delta ABC$  is an equilateral triangle. Point P is on base BC such that  $PC=\frac{1}{3}BC,$  if AB=6 cm find AP.



**20.** From the information given in the figure, prove that

 $PM = PN = \sqrt{3} \times a.$ 





**21.** Prove by vector method that the sum of the square of the diagonals of a parallelogram is equal to the sum of the squares of its sides.



**22.** Paranali and Prasad started walking to the East and to the Noorth respectively, from the same point and at the same speed. After 2 hours distance between then was  $15\sqrt{2}$ km. Find their speed per hour.



**23.** BL and CM are medians of a triangle ABC right angled at A. Prove that  $4(BL^2+CM^2)=5BC^2$ 



**24.** Sum of the squares of adjacent sides of a parallelogram is 130 cm length of one of its diagonals is 14 cm. Find the length of the other diagonal.



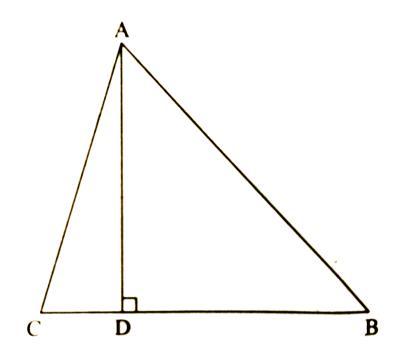
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**25.** In  $\triangle ABC$ ,

 $\mathsf{seg}\:AD\perp \mathsf{seg}\:BC$ ,

DB = 3CD.

Prove that  $2AB^2=2AC^2+BC^2$ .





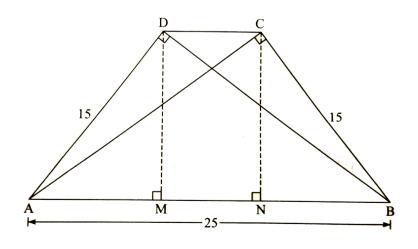
**26.** In an isosceles triangle, length of the congruent sides is 13 cm and its base is 10 cm. Find the

distance between the vertex opposite the base and the centroid.



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**27.** In a trapezium ABCD, seg  $AB \mid |$  seg DC, seg  $BD \perp$  seg AD, seg  $AC \perp$  seg BC, if AD = 15, BC = 15 and AB = 25. Find  $A(\Box ABCD)$ .





**28.** In the figure  $2.35,\,\Delta PQR$  is an equilatral triangle. Point S is on seg QR such that  $QS=rac{1}{3}QR.$  Prove that  $:9PS^2=7PQ^2$ 



29. Seg Pm is a median of `Delta PQR. If PQ = 40, PR = 42 and PM = 29, find QR.



**30.** Seg AM is a median of  $\Delta ABC$ . If AB =22, AC

=34, BC = 24, find AM.



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## **Challenging Questions**

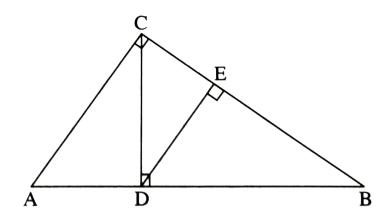
**1.** In  $\triangle$  ABC,

$$\angle ACB = 90^{\circ}$$
 ,

 $CD \perp AB$  and

 $DE \perp CB$ 

Prove that  $CD^2 imes AC = AD imes AB imes DE$  .





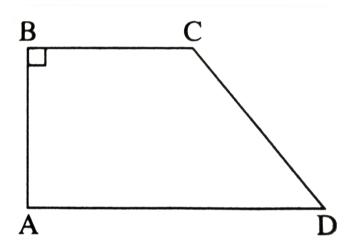
**2.** Using  $8^2-7^2=15$  , draw a square of area 15 sq cm



**3.** In the figure  $\angle B = 90^{\circ}$  ,

$$AD^2 = AB^2 + BC^2 + CD^2.$$

Prove  $\angle ACD = 90^{\circ}$  .



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**4.** P and Q are points on the sides CA and CB respectively of ABC , right angled at C . Prove that

 $AQ^2 + BP^2 = AB^2 + PQ^2.$ 



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**5.**  $\Delta ABC$  is an equilateral triangle. Point D is on side BC such that  $BD=rac{1}{5}BC$  then prove  $25AD^2 = 21AB^2.$ 

