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## MATHS

## NCERT - NCERT

## MATHEMATICS(HINGLISH)

## CONIC SECTIONS

Exercise 113

1. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the
eccentricity and the length of the latus rectum of the ellipse. $16 x^{2}+y^{2}=16$

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2. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum
of the ellipse. $4 x^{2}+9 y^{2}=36$

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3. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum
of the ellipse. $\frac{x^{2}}{36}+\frac{y^{2}}{16}=1$

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4. Find the coordinates of the foci, the
vertices, the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $\frac{x^{2}}{4}+\frac{y^{2}}{25}=1$

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5. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum
of the ellipse. $\frac{x^{2}}{16}+\frac{y^{2}}{9}=1$

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6. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the
eccentricity and the length of the latus rectum
of the ellipse. $\frac{x^{2}}{25}+\frac{y^{2}}{100}=1$

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7. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum
of the ellipse. $\frac{x^{2}}{49}+\frac{y^{2}}{36}=1$

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8. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum
of the ellipse. $\frac{x^{2}}{100}+\frac{y^{2}}{400}=1$

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9. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $36 x^{2}+4 y^{2}=144$
10. Find the equation for the ellipse that satisfies the given conditions:Centre at ( 0,0 ), major axis on the $y$-axis and passes through the points $(3,2)$ and $(1,6)$.

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11. Find the equation for the ellipse that satisfies the given conditions:b=3,c $=4$, centre at the origin; foci on a $x$ axis.

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12. Find the equation for the ellipse that satisfies the given conditions:Ends of major axis $( \pm 3,0)$, ends of minor axis $(0, \pm 2)$

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13. Find the equation for the ellipse that satisfies the given conditions:Vertices
$( \pm 6,0)$, foci $( \pm 4,0)$

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14. Find the equation for the ellipse that satisfies the given conditions:Vertices
$(0, \pm 13)$, foci $(0, \pm 5)$

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15. Find the equation for the ellipse that satisfies the given conditions:Vertices
$( \pm 5,0)$, foci $( \pm 4,0)$
16. Find the equation for the ellipse that satisfies the given conditions:Foci
$( \pm 3,0), a=4$

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17. Find the equation for the ellipse that satisfies the given conditions:Length of minor axis 16 , foci $(0, \pm 6)$.
18. Find the equation for the ellipse that satisfies the given conditions:Length of major axis 26 , foci $( \pm 5,0)$

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19. Find the equation for the ellipse that satisfies the given conditions:Ends of major axis $(0, \pm \sqrt{5})$, ends of minor axis $( \pm 1,0)$
20. Find the equation for the ellipse that satisfies the given conditions:Major axis on the $x$-axis and passes through the points $(4,3)$ and (6, 2).

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## Solved Examples

1. Find the equation of the hyperbola where foci are $(0, \pm 12)$ and the length of the latus
rectum is 36 .

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2. The focus of a parabolic mirror is at a distance of 5 cm from its vertex. If the mirror is

45 cm deep, find the distance $A B$


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3. Find the coordinates of the foci and the vertices, the eccentricity, the length of the latus rectum of the hyperbolas:
(i) $\frac{x^{2}}{9}-\frac{y^{2}}{16}=1$ (ii) $y^{2}-16 x^{2}=16$

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4. Find the equation of the hyperbola with foci
$(0, \pm 3)$ and vertices $\left(0, \pm \frac{\sqrt{11}}{2}\right)$
5. Find the equation of the ellipse, whose length of the major axis is 20 and foci are $(0, \pm 5)$.

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6. Find the equation of the ellipse, with major axis along the $x$-axis and passing through the points $(4,3)$ and $(-1,4)$.

## 7. Find the coordinates of the foci, the vertices,

 the lengths of major and minor axes and the eccentricity of the ellipse $9 x^{2}+4 y^{2}=36$.
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8. Find the equation of the ellipse whose vertices are $( \pm 13,0)$ and foci are $( \pm 5,0)$.

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9. A beam is supported at its ends by supports
which are 12 metres apart. Since the load is
connected at its centre, there is a deflection $f$

3 cm at the centre and the deflected beam is
in the shape of a parabola. How far from the centre is the deflection 1 cm ?

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10. $A$ rod $A B$ of length 15 cm rests in between
two coordinate axes in such a way that the
end point $A$ lies on $x$-axis and end point $B$ lies on $y$-axis. A point $P(x, y)$ is taken on the rod in such a way that $A P=6 \mathrm{~cm}$. Show that the locus of $P$ is an ellipse.

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11. Find an equation of the circle with centre at $(0,0)$ and radius $r$.

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12. Find the centre and the radius of the circle $x^{2}+y^{2}+8 x+10 y-8=0$.

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13. Find the equation of the circle with centre
$(-3,2)$ and radius 4.

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14. Find the coordinates of the focus, axis, the equation of the directrix and latus rectum of the parabola $y^{2}=8 x$.

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15. Find the equation of the circle which passes through the points $(2,-2)$, and $(3,4)$ and whose centre lies on the line $x+y=2$.

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16. Find the equation of the parabola with vertex at $(0,0)$ and focus at $(0,2)$.

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17. Find the equation of the parabola with
focus $(2,0)$ and directrix $x=-2$.

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18. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the latus rectum of
the ellipse $\frac{x^{2}}{25}+\frac{y^{2}}{9}=1$

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19. Find the equation of the parabola with
vertex at origin, symmetric with respect to $y$ axis and passing through $(2,-2)$

## Exercise 114

1. Find the equations of the hyperbola satisfying the given conditions :Vertices
$( \pm 7,0), e=\frac{4}{3}$

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2. Find the equations of the hyperbola satisfying the given conditions :Foci
$(0, \pm \sqrt{10})$, passing through $(2,3)$

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3. Find the equations of the hyperbola satisfying the given conditions :Foci $( \pm 3 \sqrt{5}, 0)$, the latus rectum is of length 8 .

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4. Find the equations of the hyperbola satisfying the given conditions :Foci $( \pm 4,0)$, the latus rectum is of length 12
5. Find the equations of the hyperbola satisfying the given conditions
:Foci $( \pm 5,0)$, the transverse axis is of length 8.

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6. Find the coordinates of the foci and the
vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $\frac{x^{2}}{16}-\frac{y^{2}}{9}=1$
7. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $9 y^{2}-4 x^{2}=36$

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8. Find the coordinates of the foci and the vertices, the eccentricity and the length of the
latus rectum of the hyperbolas. $\frac{y^{2}}{9}-\frac{x^{2}}{27}=1$

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9. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas.
$5 y^{2}-9 x^{2}=36$

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10. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas.
$16 x^{2}-9 y^{2}=576$

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11. Find the equations of the hyperbola satisfying the given conditions :Vertices
$( \pm 2,0)$, foci $( \pm 3,0)$
12. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas.
$49 y^{2}-16 x^{2}=784$

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13. Find the equations of the hyperbola satisfying the given conditions :Vertices
$(0, \pm 3)$, foci $(0, \pm 5)$
14. Find the equations of the hyperbola satisfying the given conditions :Vertices
$(0, \pm 5)$, foci $(0, \pm 8)$

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Exercise 112

1. Find the equation of the parabola that satisfies the given conditions:Vertex ( 0,0 );
focus $(-2,0)$

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2. Find the equation of the parabola that satisfies the given conditions:Vertex $(0,0)$ passing through $(2,3)$ arid axis is along $x$-axis.

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3. Find the equation of the parabola that satisfies the given conditions:Vertex $(0,0)$,
passing through $(5,2)$ and symmetric with respect to $y$-axis.

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4. Find the coordinates of the focus, axis of
the parabola, the equation of the directrix and the length of the latus rectum. $y^{2}=-8 x$

## D Watch Video Solution

5. Find the coordinates of the focus, axis of the parabola, the equation of the directrix and the
length of the latus rectum. $x^{2}=6 y$

## D Watch Video Solution

6. Find the coordinates of the focus, axis of the
parabola, the equation of the directrix and the
length of the latus rectum. $x^{2}=-16 y$
7. Find the equation of the parabola that satisfies the given conditions:

Focus $(6,0)$; directrix $x=6$

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8. Find the coordinates of the focus, axis of the
parabola, the equation of the directrix and the
length of the latus rectum. $x^{2}=-9 y$
9. Find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum. $y^{2}=10 x$

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10. Find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum. $x^{2}=-16 y$

## D Watch Video Solution

11. Find the equation of the parabola that satisfies the given conditions:Vertex ( 0,0 );
focus $(3,0)$

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12. Find the equation of the parabola that satisfies the given conditions:Focus $(0,-3)$; directrix $y=3$
13. If a parabolic reflector is 20 cm in diameter and 5 cm deep, find the focus.

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2. An arch is in the form of a parabola with its
axis vertical. The arch is 10 m high and 5 m
wide at the base. How wide is it 2 m from the vertex of the parabola?
3. The cable of a uniformly loaded suspension bridge hangs in the form of a parabola. The roadway which is horizontal and 100 m long is supported by vertical wires attached to the cable, the longest wire being 30 m and the shortest being 6 m . Find the length of a supporting wire attached to the roadway 18 m from the middle.

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4. An arch is in the form of a semi-ellipse. It is

8 m wide and 2 m high at the centre. Find the
height of the arch at a point 1.5 m from one end.

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5. A rod of length 12 cm moves with its ends always touching the coordinate axes.

Determine the equation of the locus of a point $P$ on the rod, which is 3 cm from the end in contact with the x -axis.

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6. Find the area of the triangle formed by the
lines joining the vertex of the parabola $x^{2}=12 y$ to the ends of its latus rectum.

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7. A man running a racecourse notes that the sum of the distances from the two flag posts from him is always 10 m and the distance
between the flag posts is 8 m . Find the equation of the posts traced by the man.

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8. An equilateral triangle is inscribed in the parabola $y^{2}=4 a x$ where one vertex is at the vertex of the parabola. Find the length of the side of the triangle.
9. Find the equations of the hyperbola satisfying the given conditions :Foci $(0, \pm 13)$
, the conjugate axis is of length 24.

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Exercise 111

1. Find the equation of the circle with centre :
$(-2,3)$ and radius 4

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2. Find the equation of the circle with centre :
$\left(\frac{1}{2}, \frac{1}{4}\right)$ and radius $\frac{1}{12}$

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3. Find the equation of the circle with centre:
$(0,2)$ and radius 2

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4. Find the centre and radius of the circles
$(x+5)^{2}+(y-3)^{2}=36$

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5. Find the centre and radius of the circles
$x^{2}+y^{2}-4 x-8 y-45=0$

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6. Find the equation of the circle with centre :
$(1,1)$ and radius $\sqrt{2}$

- Watch Video Solution

7. Find the equation of the circle with centre :
$(-a,-b)$ and radius $\sqrt{a^{2}-b^{2}}$.

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8. Find the centre and radius of the circles
$x^{2}+y^{2}-8 x+10 y-12=0$

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9. Find the centre and radius of the circles
$2 x^{2}+2 y^{2}-x=0$

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10. Does the point $(-2.5,3.5)$ lie inside, outside or on the circle $x^{2}+y^{2}=25 ?$

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11. Find the equation of a circle with centre (2,
$2)$ and passes through the point $(4,5)$.

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12. Find the equation of the circle passing through the points $(2,3)$ and $(-1,1)$ and whose centre is on the line $x-3 y-11=0$.

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13. Find the equation of the circle passing
through the points $(4,1)$ and $(6,5)$ and whose centre is on the line $4 x+y=16$.
14. Find the equation of the circle passing through $(0,0)$ and making intercepts $a$ and $b$ on the coordinate axes.

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15. Find the equation of the circle with radius 5
whose centre lies on $x$-axis and passes
through the point $(2,3)$.

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