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India's Number 1 Education App

## MATHS

## NCERT - NCERT MATHEMATICS(HINGLISH)

## RELATIONS AND FUNCTIONS

Exercise 22

1. $A=\{1,2,3,5\}$ and $B=\{4,6,9\}$. Define a relation R from A to B by $\mathrm{R}=\{(\mathrm{x}, \mathrm{y})$ : the difference between $x$ and $y$ is odd:
$x \in A, y \in B\}$. Write R in roster form.
A.

$$
R=\{(1,4),(3,4),(5,4),(1,6),(5,6),(2,9)\}
$$

B.

$$
R=\{(1,4),(3,4),(5,4),(1,6),(3,6),(5,6)\}
$$

C.

$$
R=\{(1,4),(3,4),(1,6),(3,6),(5,6),(2,9)\}
$$

D.

$$
R=\{(1,4),(3,4),(5,4),(1,6),(3,6),(5,6),(2,9)\}
$$

## Answer: D

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2. Define a relation $R$ on the set $N$ of natural numbers by $R=\{(x, y): y=x+5, x$ is a natural number less than $4 ; x, y \in N\}$. Depict this relationship using roster form. Write down the domain and the range...
3. Let $A=\{1,2,3, \ldots, 14\}$. Define a relation $R$ from $A$ to $A$ by $R=\{(x, y): 3 x-y=0, \quad$ where $x, y \in A\}$. Write down its domain, co-domain and range.

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4. Determine the domain and range of the relation $R$ defined by
$R=\{(x, x+5): x \in\{0,1,2,3,4,5\}\}$.

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5. Let $A=\{1,2,3,4,6\}$. Let R be the relation on A defined by $\{(a \dot{b}): a, b \in A, b$ is exactly divisible by a\}.(i) Write R in roster form(ii) Find the domain of $R$ (iii) Find the range of $R$.
6. Let $R$ be the relation on $Z$ defined by $R=\{(a, b): a, b \in Z, a-b$ is an integer $\}$. Find the domain and range of $R$.

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7. Let $A=\{x, y, z\}$ and $B=\{1,2\}$. Find the number of relations from $A$ to $B$.

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8. Write the Relation $R=\left\{\left(x, x^{3}\right): x\right.$ is a prime number less than 10$\}$ in roster form.
9. The area bounded by the curves $y=\sqrt{x} ; 2 y+3=x$ and $x-$ axis in the 4 th quadrant is
A. if p " $\frac{p}{r}$ and $\cos \mathrm{R} . \frac{p}{q}$ "
B. null
C. null
D. null

## Answer: null

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## Exercise 21

1. The Cartesian product $A \times A$ has 9 elements among which are found $(-1,0)$ and $(0,1)$. Find the set $A$ and the remaining elements of $A \times A$.

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2. If the set A has 3 elements and the set $B=\{3,4,5\}$, then find the number of elements in $(A \times B)$.

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3. If $G=\{7,8\}$ and $H=\{5,4,2\}$, find $G \times H$ and $H \times G$.

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4. If $\left(\frac{x}{3}+1, y-\frac{2}{3}\right)=\left(\frac{5}{3}, \frac{1}{3}\right)$, find the values of x and y .

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5. If $A \times B=\{(a, x),(a, y),(b, x),(b, y)\}$. Find A and B.

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$$
\begin{aligned}
& \text { 6. Let } A=\{1,2\} \dot{B}=\{1,2,3,4\}, C=\{5,6\} \text { and } \\
& D=\{5,6,7,8\} . \\
& A \times(B \cap C)=(A \times B) \cap(A \times C) . \text { (ii) } A \times C \text { is a subset of } \\
& B \times D .
\end{aligned}
$$

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7. State whether each of the following statements are true or false. If the statement is false, rewrite the given statement correctly.(i)

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8. If $A=\{1,1\}$, find $A \times A \times A$.

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9. Let $A=\{1,2\}$ and $B=\{3,4\}$. Write $A \times B$. How many subsets will $A \times B$ have? List them.
10. Let A and B be two sets such that $n(A)=3$ and $n(B)=2$. If $(x, 1),(y, 2),(z, 1)$ are in $\mathrm{A} \times \mathrm{B}$. find A and B . where $\mathrm{x}, \mathrm{y}$ and z are distinct elements.

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Solved Examples

1. 2 Let N be the set of natural numbers. Define a real valued function $f: N->N$ by $f(x)=2 x+1$. Using this definition, complete the table given below.

| $x$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | $f(1)=\ldots$ | $f(2)=\ldots$ | $f(3)=\ldots$ | $f(4)=\ldots$ | $f(5)=\ldots$ | $f(6)=\ldots$ | $f(7)=\ldots$ |

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2. Examine each of the following relations given below and state in each case, giving reasons whether it is a function or not?
(i) $\mathrm{R}=\{(2,1),(3,1),(4,2)\}$,
(ii) $\mathrm{R}=\{(2,2),(2,4),(3,3),(4,4)\}$
(iii) $R=\{(1,2),(2,3),(3,4),(4,5),(5,6),(6,7)\}$

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3. Define the function $\mathrm{f}: \mathrm{R} \rightarrow \mathrm{R}$ by $\mathrm{y}=\mathrm{f}(\mathrm{x})=x^{2}, x \in R$. Complete the Table given below by using this definition. What is the domain and range of this function?

| $x$ | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y=f(x)=x^{2}$ |  |  |  |  |  |  |  |  |  |

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4. Let $N$ be the set of natural numbers and the relation $R$ be defined on N such that $R=\{(x, y): y=2 x, x, y \in N\}$. What is the domain, codomain and range of R ? Is this relation a function?

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5. Let $f(x)=\sqrt{x}$ and $g(x)=x$ be two functions defined over the set of nonnegative real numbers. Find $(f+g)(x),(f g)(x)$, $(f g)(x)$ and $\left(\frac{f}{g}\right)(x)$.

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6. Let $f(x)=x^{2}$ and $g(x)=2 x+1$ be two real functions. find $(f+g)(x),(f-g)(x),(f g)(x),\left(\frac{f}{g}\right)(x)$.
7. Define the real valued function $f: R\{0\} \rightarrow R$ defined by $f(x)=\frac{1}{x}, x \in R\{0\}$. Complete the Table given below using this definition. What is the domain and range of this function? $y=\frac{1}{x}$

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8. Draw the graph of the function $f: R \rightarrow R$ defined by $f(x)=x^{3}, x \in R$.

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9. Let $R$ be $a$ relation from $Q$ to $Q$ defined by $R=\{(a, b): a, b \in Q$ and $a, b \in Z\}$. Showt $\{\mathrm{a}, \mathrm{a})$ in R for all a in Q $\quad,\{a, b\} \in R \Rightarrow$ that
$\{b, a\} \in R,\{a, b\} \in R$ and $\{b, c\} \in R \Rightarrow t \widehat{a, c} \in R^{`}$
10. Let $R$ be the set of real numbers. Define the real function $f: R \rightarrow R b y f(x)=x+10$ and sketch the graph of this function.

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11. If $(x+1, y-2)=(3,-1)$, find the values of $x$ and $y$.
A. 2,1
B. $2,-1$
C. $-2,1$
D. None

## Answer: A

12. Let $A=\{1,2,3\}, \quad B=\{3,4\}$ and $C=\{4,5,6\}$. Find(i)
$A \times(B \cap C) \quad$ (ii) $\quad(A \times B) \cap(A \times C)$ (iii) $\quad A \times(B \cup C)$
$(A \times B) \cup(A \times C)$

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13. If $P=\{a, b, c\}$ and $A \times B=\{(p, q),(p, r),(m, q),(m, r)\}$ $Q=\{r\}$, form the sets $P \times Q a n d Q \times P$.Are these two products equal?

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14. If $R$ is the set of all real numbers, what do the cartesian products $R \times R$ and $R \times R \times R$ represent?
15. If $P=\{1,2\}$ form the set $P \times P \times P$.

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16. The function f is defined by $f(x)=\left\{\begin{array}{cr}1-x x<0 \\ 1 & x=0 \\ x+1 & x>0\end{array}\right\}$. Draw the graph of $f(x)$.

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17. Find the domain of the function $f(x)=\frac{x^{2}-3 x+5}{x^{2}-5 x+4}$.

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18. Let $f=\{(1,2),(2,3),(0,-1),(-1,-3)\}$ be a linear function from Z into Z . Find $f(x)$.

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19. If $A \times B=\{(p, q),(p, r),(m, q),(m, r)\}$, find A and B .

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20. Let $A=\{1,2,3,4,5,6\}$. Define a relation R from A to A by $R=\{(x, y): y=x+1\}(\mathrm{i})$ Depict this relation using an arrow diagram.(ii) Write down the domain, co-domain and range of R.

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21. The Fig 2.6 shows a relation between the sets $P$ and $Q$. Write this relation
(i) in set-builder form,
(ii) in roster form. What is its domain and range?


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22. Let $A=\{1,2\}$ and $B=\{3,4\}$. Find the number of relations from $A$ to $B$.

## Miscellaneous Exercise

1. Find the domain of the function $f(x)=\frac{x^{2}+2 x+1}{x^{2}-8 x+12}$
A. R
B. $R-\{4\}$
C. $R-\{2,6\}$
D. $R-\{2\}$

## Answer: C

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2. The relation $f$ is defined by
$f(x)=\left\{x^{2}, 0 \leq x \leq 33 x, 3 \leq x \leq 10\right.$ The relation $g$ is defined
by $g(x)=\left\{x^{2}, 0 \leq x \leq 33 x, 2 \leq x \leq 10\right.$ Show that $f$ is a function and $g$ is not a function.

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3. If $f(x)=x^{2}$, find $\frac{f(1.1)-f(1)}{(1.1-1)}$

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4. Let $f=\{(1,1),(2,3),(0,1),(1,3)\}$ be a function from Z to Z defined by $f(x)=a x+b$, for some integers $\mathrm{a}, \mathrm{b}$. Determine $\mathrm{a}, \mathrm{b}$.

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5. Let $R$ be $a$ relation from $N$ to $N$ defined by $R=\left\{(a, b): a \dot{b} \in N\right.$ and $\left.a=b^{2}\right)$. Are the following true?(i)
$(a, a) \in R, f$ or alla $\in N($ ii $) \quad(a, b) \in R, \operatorname{implies}(b, a) \in R(\mathrm{iii})$ ` $(a$,

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6. Find the domain and the range of the real function $f$ defined by $f(x)=\sqrt{(x-1)}$.

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7. Find the domain and the range of the real function/defined by
$f(x)=|x-1|$

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8. Let $A=\{9,10,11,12,13\}$ and let $f: A \rightarrow N$ be defined by $\mathrm{f}(\mathrm{n})$
$=$ the highest prime factor of $n$. Find the range of $f$.

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9. Let f be the subset of $Z \times Z$ defined by $f=\{(a b, a+b): a, b \in Z\}$. Is f a function from Z to Z ? Justify your answer.

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10. Let $A=\{1,2,3,4\}, B=\{1,5,9,11,15,16\}$ and $f=\{(1,5),(2,9),(3,1),(4,5),(2,11)\}$. Are the following true?
(i) $f$ is a relation from $A$ to $B$ (ii) $f$ is a function from $A$ to B.Justify $y$
11. Let $f=\left\{\left(x, \frac{x^{2}}{1+x^{2}}\right): x \in R\right\}$ be a function from R into R . Determine the rage of $f$.

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12. Let $f, g: R \rightarrow R$ be defined, respectively by
$f(x)=x+1, g(x)=2 x-3$. Find $f+g, f g$ and $\frac{f}{g}$.

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## Exercise 23

1. Which of the following relations are functions?

$$
\begin{equation*}
\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\} \tag{ii}
\end{equation*}
$$

$\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$
A. i only
B. ii only
C. i and ii both
D. neither i nor ii

## Answer: A

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2. Find the domain and range of the following real functions:(i)

$$
f(x)=-|x| \text { (ii) } f(x)=\sqrt{9-x^{2}}
$$

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3. A function $f$ is defined by $f(x)=2 x-5$. Write down the values of(i) $f(0)$, (ii) $f(7)$, (iii) $f(3)$.

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4. The function $t$ which maps temperature in degree Celsius into temperature in degree Fahrenheit is defined by $t(C)=\frac{9 C}{5}+32$ .Find (i) $t(0)$ (ii) $t(28)$ (iii) $t(-10)$ (iv) The value of $C$, when $t(C)=212$.

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5. Find the range of each of the following functions.
(i) $f(x)=2-3 x, x \in \mathbb{R}, x>0$
(ii) $f(x)=x^{2}+2, \mathrm{x}$ is a real number.
(iii) $f(x)=x, x$ is a real number.

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