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## MATHS

# NCERT - NCERT MATHEMATICS(HINGLISH) 

## STATISTICS

## Miscellaneous Exercise

1. Given that $\bar{x}$ is the mean and $\sigma^{2}$ is the variance of n observations $x_{1} x_{2}$,
$\ldots, x_{n}$. Prove that the mean and variance of the observations $a x_{1}, a x_{2}$, $a x_{3}, \ldots \ldots \ldots, a x_{n}$ are $a \bar{x}$ and $a^{2} \sigma^{2}$,

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2. The mean and standard deviation of 20 observations are found to be 10 and 2 , respectively. One rechecking, it was found that an observation 8
was incorrect. Calculate the correct mean and standard deviation in each of the following cases. ( $i$ ) If wrong item is omitted (ii) If it is replaced by 12 .

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3. The mean and standard deviation of marks obtained by 50 students of a class in three subject, Mathematics, Physics and Chemistry are given below:

| Subject | Mathematics | Physics | Chemistry |
| :---: | :---: | :---: | :---: |
| Mean | 42 | 32 | 40.9 |
| Standard deviation | 12 | 15 | 20 |

Which of the three subjects shows the highest variability in marks and which shows the lowest?
4. The mean and standard deviation of a group of 100 observations were found to be 20 and 3, respectively. Later on it was found that three observations were incorrect, which are recorded as 21,21 and 18 . Find the mean and standard deviation if the incorrect observations are omitted.

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5. The mean and variance of 7 observations are 8 and 16 , respectively. If five of the observations are $2,4,10,12,14$. Find the remaining two observations.

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6. The mean and variance of eight observations are 9 and 9.25 , respectively. If six of the observations are $6,7,10,12,12$ and 13 , find the remaining two observations.
7. The mean and standard deviation of six observations are 8 and 4, respectively. If each observation is multiplied by 3 , find the new mean and new standard deviation of the resulting observations.

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## Solved Examples

1. Calculate mean, Variance and Standard Deviation for the following distribution.

| Classes | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 3 | 7 | 12 | 15 | 8 | 3 | 2 |

2. Two plants $A$ and $B$ of a factory show following results about the number of workers and the wages paid to them.
A
B
No. of workers
5000
6000

Average monthly wages
Variance of distribution
Rs 2500
81
Rs 2500
of wages

In which plant, A or B is there greater variability in individual wages?

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3. Calculate the mean, variance and standard deviation for the following distribution:

| Class interval | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 3 | 7 | 12 | 15 | 8 | 3 | 2 |

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4. Find the standard deviation for the following data :
5. The variance of 20 observations is 5 . If each observation is multiplied by 2 , find the new variance of the resulting observations.
A. 20
B. 30
C. 40
D. 50

## Answer: A

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6. The mean of 5 observations is 4.4 and their variance is 8.24 . If three of the observations are 1,2 and 6, find the other two observations.
7. Coefficient of variation of two distributions are 60 and 70 , and their standard deviations are 21 and 16, respectively. What are their arithmetic means.

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8. The following values are calculated in respect of heights and weights of the students of a section of Class XI

Height Weight

| Mean | 162.6 cm | 52.36 kg |
| :--- | :---: | :--- |
| Variance | $127.69 \mathrm{~cm}^{2}$ | $23.1361 \mathrm{~kg}^{2}$ |

Variance

Can we say that the weights show greater variation than the

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9. If each of the observation $x_{1}, x_{2}, \ldots \ldots \ldots, x_{n}$ is increased by a where a is
a negative or positive number, show that the variance remains unchanged.
10. The mean and standard deviation of 100 observations were calculated as 40 and 5.1 , respectively by a student who took by mistake 50 instead of 40 for one observation. What are the correct mean and standard deviation?

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11. Find the variance and standard deviation for the following data:

| $x_{i}$ | 4 | 8 | 11 | 17 | 20 | 24 | 32 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $f_{i}$ | 3 | 5 | 9 | 5 | 4 | 3 | 1 |

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12. Find the Variance of the following data:
$6,8,10,12,14,16,18,20,22,24$
13. Find the mean deviation about the median for the following data:

| $x_{i}$ | 3 | 6 | 9 | 12 | 13 | 15 | 21 | 22 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f_{i}$ | 3 | 4 | 5 | 2 | 4 | 5 | 4 | 3 |

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14. Find mean deviation about the mean for the following data : $x_{i} 2568$ $1012 f_{i} 2810785$

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15. Calculate the mean deviation about median for the following data :

| Class | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 6 | 7 | 15 | 16 | 4 | 2 |

16. Find the mean deviation about the mean for the following data.

| Marks obtained | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of students | 2 | 3 | 8 | 14 | 8 | 3 | 2 |

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17. Find the mean deviation about the mean for the following data:
$6,7,10,12,13,4,8,12$

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18. Find the mean deviation about the median for the following data: $3,9,5,3,12,10,18,4,7,19,21$.

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1. Find the mean deviation about the mean for the data : $x_{i} 1030507090$ $f_{i} 42428168$

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2. Find the mean deviation about the median for the data : $x_{i}$ : 5791012
3. $f_{i}: 862226$

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3. Find the mean deviation about the median for the data : $36,72,46,42,60,45,53,46,51,49$

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4. Find the mean deviation about the mean for the data :
$x_{i}$
5
10
$15 \quad 20$
25
$f_{i}$
7
4
63
5

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5. Find the mean deviation about the mean for the data : $38,70,48,40,42,55,63,46,54,44$

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6. Find the mean deviation about the median for the data : $13,17,16,14,11,13,10,16,11,18,12,17$

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7. Find the mean deviation about the mean for the data : $4,7,8,9,10,12,13,17$

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8. Find the mean deviation about the median for the data : $x_{i} 15212730$
$35 f_{i} 35678$

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9. Find the mean deviation about the mean for the data : Income 100 100-200 200-300 300-400 400-500 500-600 600-700 700-800per dayNumber 4 8 9 10 7 5

4 3of persons

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10. Find the mean deviation about median for the following data

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Girls | 6 | 8 | 14 | 16 | 4 | 2 |

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11. Find the mean deviation about the mean for the data :
$\left\{\begin{array}{llllll}\text { Height } & 95-105 & 105-115 & 115-125 & 125-135 & 135 \\ \text { Number of Boys } & 9 & 13 & 26 & 30 & 12\end{array}\right.$

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12. Calculate the mean deviation about median age for the age distribution of 100 persons given below:Age $\begin{array}{lllll} & 16-20 & 21-25 & 26-30 & 31-\end{array}$ $\begin{array}{llllllll}35 & 36-40 & 41-45 & 46-50 & 51-55 N u m b e r & 5 & 6 & 12\end{array}$
$\begin{array}{lllll}14 & 26 & 12 & 16 & 9\end{array}$

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1. The following is ht record of goals scored by team $A$ in a football session

| No. of goals scored | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. of matches | 1 | 9 | 7 | 5 | 3 |

For the team $b$, mean number of goals scored per match was 2 with $a$ standard deviation 1.25 goals. Find which team may be considered more consistent?

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2. The sum and sum of squares corresponding to length $x$ (in cm ) and weight $y$ (in gm) of 50 plant products are given below $\sum_{i=1}^{50} x_{i}=212, \sum_{i=1}^{50} x_{i}^{2}=902.8, \sum_{i=1}^{50} y_{1}=261, \sum_{i=1}^{50} y_{i}^{2}=1457.6 \mathrm{Which}$ is more varying the length or weight?

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3. For the data given below state which group is more variable, A or B ?

| Marks | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Group A | 9 | 17 | 32 | 33 | 40 | 10 | 9 |
| Group B | 10 | 20 | 30 | 25 | 43 | 15 | 7 |

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4. From the prices of shares $X$ and $Y$ below, find out which is more stable in value

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5. An analysis of monthly wages paid to workers in two firms A and B, belonging to the same industry, gives the following result

|  | Firm A | Firm B |
| :---: | :---: | :---: |
| No.of wage earners | 586 | 648 |
| Mean of monthly wages | Rs 5253 | Rs 5253 |
| Variance of the distribution of wages | 100 | 121 |

(i) Which firm A or B pays larger amount as monthly wages?
(ii) Which firm, A or B , show greater variability in individual wages?

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## Exercise 152

1. Find the mean and variance for the following frequency distributions :

| Classes | $0-30$ | $30-60$ | $60-90$ | $90-120$ | $120-150$ | $150-180$ | $180-210$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequencies | 2 | 3 | 5 | 10 | 3 | 5 | 2 |

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2. Find the mean and standard deviation using short-cut method.

| $x_{i}$ | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $f_{i}$ | 2 | 1 | 12 | 29 | 25 | 12 | 10 | 4 | 5 |

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3. Find the mean and variance for each of the data :

| $x_{i}$ | 92 | 93 | 97 | 98 | 102 | 104 | 109 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $f_{i}$ | 3 | 2 | 3 | 2 | 6 | 3 | 3 |

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4. Find the mean and variance for each of the data :

| $x_{i}$ | 6 | 10 | 14 | 18 | 24 | 28 | 30 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $f_{i}$ | 2 | 4 | 7 | 12 | 8 | 4 | 3 |

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5. Find the mean and variance for each of the data :

First 10 multiples of 3 .

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6. Find the mean and variance for each of the data :

First n natural numbers

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7. Find the mean and variance for each of the data : $6,7,10,12,13,4,8,12$

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8. Find the mean, variance and standard deviation using short-cut method

| Height <br> in cms | $70-75$ | $75-80$ | $80-85$ | $85-90$ | $90-95$ | $95-100$ | $100-105$ | $105-110$ | $110-115$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> children | 3 | 4 | 7 | 7 | 15 | 9 | 6 | 6 | 3 |

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9. Find the mean and variance for the following frequency distributions :

| Classes | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequencies | 5 | 8 | 15 | 16 | 6 |

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10. The diameters of circle (in mm ) drawn in a design are given below:

| Diameters | $33-36$ | $37-40$ | $41-44$ | $45-48$ | $49-52$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| No. of circles | 15 | 17 | 21 | 22 | 25 |

Calculate the SD and mean

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