# ©゙’doubtnut 

India's Number 1 Education App

## PHYSICS

## NCERT - NCERT PHYSICS(HINGLISH)

## MOTION IN A PLANE

## Solved Example

1. Rain is falling vertically with a speed fo
$35 m s^{-1}$. Winds starts blowing after sometime
with the speeds of $12 m s^{-1}$ in east to west
direction. At what angles with the vertical should a boy waiting at a bus stop hold his umbrella to protect himself from rain?

## D Watch Video Solution

2. Find the magnitude and direction of the resultant of two vectors $A$ and $B$ in the terms of their magnitudes and angle $\theta$ between
them.


## - Watch Video Solution

3. A motor boat is racing towards North at $25 \mathrm{~km} / \mathrm{h}$ and the water current in that region is $10 \mathrm{~km} / \mathrm{h}$ in the direction of $60^{00}$ East of South. Find the resultant velocity of the boat.

## - Watch Video Solution

4. The position of a particle is given by
$r=3 t \hat{i}+2 t^{2} \hat{j}+8 \hat{k}$
where, $t$ is in seconds and the coefficients have the proper units for $r$ to be in metres.
(i) Find $v(t)$ and $a(t)$ of the particles.
(ii) Find the magnitude and direction of $v(t)$ and $\mathrm{a}(\mathrm{t})$ at $1=1 s$.
A. $(2.0 \hat{i}+4.0 t \hat{j}), a=4.0 m s^{-2} 5.0 m s^{-1}$ , $53^{\circ}$ with x -axis ${ }^{`}$
B. $(3.0 \hat{i}+4.0 t \hat{j}), a=4.0 m s^{-2} 5.0 m s^{-1}$
, $53^{\circ}$ with x -axis` C. \((3.0 \hat{i}+4.0 t \hat{j}), a=2 m s^{-2} 5.0 m s^{-1}\), \(53^{\circ}\) with x -axis`
D. $(3.0 \hat{i}+4.0 t \hat{j}), a=4.0 m s^{-2} 5.0 m s^{-1}$
, $45^{\circ}$ with $x$-axis ${ }^{`}$

## Answer: B

## D Watch Video Solution

5. A paarticle starts from origin at $t=0$ with a velocity $5.0 \hat{i} m / s$ and moves in $x-y$ plane under action of a force which produces a constant acceleration of $(3.0 \hat{i}+2.0 j) m / s^{2}$.
(a) What is the y-cordinate of the particle at the instant its $x$-coordinate is ' 84 m ? (b) What is the speed of the particle at this time?

## - Watch Video Solution

6. Rain is falling vertically with a speed of $10 \sqrt{3} m s^{-1}$. A woman rides a bicycle with a speed of $10 \mathrm{~ms}^{-1}$ in east to west direction.

What is the derection in which she shold hold
her umbrella to protect from rain ?

## D Watch Video Solution

7. Galileo, in his book Two new sciences, stated
that "for elevations which exceed or fall short
of $45^{\circ}$ by equal amounts, the ranges are equal. Prove this statement.

## D Watch Video Solution

8. A hiker stands on the edge of a cliff $490 m$ above the ground and throwns a stone horiozontally with an initial speed of $15 \mathrm{~ms}^{-1}$ neglecting air resistance.The time taken by the stone to reach the ground in seconds is $\left(g=9.8 m s^{2}\right)$
9. A cricket ball is thrown at a speed of $28 \mathrm{~ms}^{-1}$ in a direction $30^{\circ}$ above the horizontal. Calculate (a)the maximum height (b) the time taken by ball to return ti the same level, and (c )the distance from the thrower to the point wher the ball restance from the throwrt to the point where the ball returns to the same level.

A. $10.0 m 2.8 s 29 m$

$$
\text { B. } 10.0 m 2.8 s 69 m
$$

## C. 10.0 m 3.8 s 69 m

D. $20.0 m 2.8 s 69 m$

Answer: B

## D Watch Video Solution

10. An insect trapped in a circular groove of
radius 12 cm moves along the groove steadily
and completes 7 revolutions in 100 s. (i) What
is the angular speed and the linear speed of
the motion ? (ii) Is the acceleration vector a constant vector? What is its magnitude?

## D Watch Video Solution

## Exercise

1. State, for each of the following physical quantities, if it is a scalar or a vector. Volume, mass speed acceleration, density, number of moles, velocity, angular frequency, displacement, angular velocity.

## - Watch Video Solution

2. Pick out the two scalar quantities in the following list: force, angular momentum, work, current, linear momentum, electric field, average force, angular momentum, work, current , linear momentum, electric field, average velocity, magnetic moment, relative velocity.
3. Pick out the only vector quantity in the following list:

Temperature, pressure, impulse, time, power , total path length, energy, gravitational temperature, pressure, impulse, time, power, total path length, energy, gravitational potential, coefficient of friction, charge.

## - Watch Video Solution

4. State with reasons, whether the following algebraic operations with scalar and vector physical quantities are meaningful:
(i) Adding any two scalars (ii) Adding a scalar to a vector of the same dimensions
(iii) Multiplying any vector by any scalar (iv)

Multiplying any two scalars
(v) Adding any two vectors

## D Watch Video Solution

5. Read each statement below carefully and
state with reasons, with it is true or false :
(a) The magnitude of vector is always a scalar.
(b) Each component of a vector is always a scalar.
(c) The total path length is always equal to the magnitude of the displacement vector of a particle.
(d) The average speed of a particle (defined as total path length divided by the time taken to
cover the path) is greater or equal to the magnitude of average velocity of the particle
over the same interval of time.
(e) three vectors not lying in a plane can never add up to give a null vector.

## D Watch Video Solution

6. Establish the following inequalities geometrically or otherwise,
(a) $|\vec{A}+\vec{B}| \leq|\vec{A}|+|\vec{B}|$,
(b) $|\vec{A}+\vec{B}| \geq||\vec{A}|-|\vec{B}||$
(C) $|\vec{A}-\vec{B}| \leq|\vec{A}|+|\vec{B}|$
(d) $|\vec{A}-\vec{B}| \geq||\vec{A}|-|\vec{B}||$

When does the equality sign above apply ?

## D Watch Video Solution

7. Given $\vec{A}+\vec{B}+\vec{C}+\vec{D}=0$, which of the
following statements are correct ?
(a) $\vec{A}, \vec{B}, \vec{C}$ abd $\vec{D}$ each must be a null
vector.
(b) The magnitude of $(\vec{A}+\vec{C})$ equals the magnitude of $(\vec{B}+\vec{D})$.
(c) The magnitude of $\vec{A}$ can never be greater
than the sum of the magnitude of $\vec{B}, \vec{C}$ and $\vec{D}$.
(d) $\vec{B}+\vec{C}$ must lie in the plane of $\vec{A}+\vec{D}$. if
$\vec{A}$ and $\vec{D}$ are not collinear and in the line of $\vec{A}$ and $\vec{D}$, if they are collinear.

## D Watch Video Solution

8. Three girls skating on a circular ice ground of radius 200 m start from a point ( P ) on the edge of the ground and reach a point $Q$ diametrically opposite to (P) following
different paths as shown in Fig. What is the magnitude of the displacement vector for each ? which girl's displacement is equal to the actual length of path skate?

9. A cyclist starts from the center O of a circular park of radius 1 km , reaches the edge $P$ of the park, then cycles along the $P Q$ circumference and returns to the center along

OQ as shown in fig. If the round trip taken ten minute, the (a) net displacement, (b) average
velocity and (c) average speed of the cyclists
(in kilometer and kinetic per hour) is


- Watch Video Solution

10. On an open ground, a motorist follows a track that turns to his left by an angle of $60^{\circ}$
after every 500 m . Starting from a given turn,

The path followed by the motorist is a regular hexagon with side 500 m , as shown in the given figure specify the displacement of the motorist

at the third, sixth and eighth turn. Compare the magnitude of the displacement with the
total path length covered by the motorist in each case.

## D Watch Video Solution

11. A passenger arriving in a new town wishes
to go from the station to a hotel located

10 km away on a straight road from the
station. A dishonest cabman takes him along a circuitous path 23 km long and reaches the
hotel in 28 minutes. What is (a) the average
speed of the taxi, (b) the magnitude of average velocity ? Are the two equal ?

## D Watch Video Solution

12. Rain is falling vertically with a speed of $30 \mathrm{~ms}^{-1}$. A woman rides a bicycle with a speed of $10 \mathrm{~ms}^{-1}$ in the North to South direction. What is the direction in which she should hold her umbrella?
13. A man can swim with a speed of $4 k m h^{-1}$
in still water. He crosses a river 1 km wide that
flows steadly at $3 \mathrm{kmh}^{-1}$. If he makes his strokes normal to the river current, how far down the river does he go when he reaches the other bank?

## - Watch Video Solution

14. In a harbour, wind is blowing at the speed of $72 \mathrm{~km} / \mathrm{h}$ and the flag on the mast of a boat anchored in the harbour flutters along the N-E
direction. If the boat starts moving at a speed of $51 \mathrm{~km} / \mathrm{h}$ to the North, what is the direction of flag on the mast of the bat ?

## D Watch Video Solution

15. The ceiling of a long hall is 25 m high. What
is the maximum horizontal distance if a ball thrown with a speed of $40 \mathrm{~ms}^{-1}$ can go without hitting the ceiling of the hall ?

## D Watch Video Solution

16. A cricketer can throw a ball to a maximum
horizontal distance of 100 m . With the same speed how much high above the ground can the cricketer throw the same ball?
A. $150 m$
B. 250 m
C. 350 m
D. 50 m

Answer: D
17. A stone tied to end of a string 80 cm long is whirled in a horizontal plane with a constant speed. If the stone makes 14 revolutions in 25 seconds, what is the magnitude and direction of acceleration of the stone?

## - Watch Video Solution

18. An aircraft executes a horizontal loop of radius 1 km with a steady speed of $900 \mathrm{kmh}^{-1}$.

Compare its centripetal acceleration with the acceleration due to gravity.

## D Watch Video Solution

19. Read each statement below carefully and state, with reasons, if it is true or false :
(a) The net acceleration of a particle in circular motion is always along the radius of the circle towards the center.
(b) The velocity vector of a particle at a point is always along the tangent to the path of the
particle at that point.
(c) The acceleration vector of a particle in uniform circular motion averaged over one cycle is a null vector.

## D Watch Video Solution

20. The position of a particle is given by
$\vec{r}=3.0 t \hat{i}-2.0 t^{2} \hat{j}+4.0 \hat{k} m$, where ( t ) in seconds and the coefficients have the proper units for $\vec{r}$ to be in metres. (a) Find the $\vec{v}$ and $\vec{a}$ of the particle ? (b) What is the
magnitude and direction of velocity of the particle at $t=2 s ?$

## D Watch Video Solution

21. A particle starts from the origin at $t=0$ with a velocity of $10.0 \hat{j} m / s$ and moves in the
$x-y$ plane with a constant acceleration of $(8.0 \hat{i}+2.0 \hat{j}) m s^{-2}$. (a) At what time is the x-coordinate of the particle $16 m$ ? What is the $y$-coordinate of the particle at that time?

What is the speed of the particle at that time?

## Watch Video Solution

22. $\hat{i}$ and $\hat{j}$ are unit vectors along x -and y -axis respectively. What is the magnitude and the direction of the vectors $\hat{i}+\hat{j}$ and $\hat{i}-\hat{j}$ ?

What are the components of a vector $\vec{A}=2 \hat{i}+3 \hat{j}$ along the direction $\hat{i}+\hat{j}$ and $\hat{i}-\hat{j}$ ?

## - Watch Video Solution

23. For any arbitrary motion in space, which of the following relations are true?
(a) $v_{\text {average }}=(1 / 2)\left(v\left(t_{1}\right)+v\left(t_{2}\right)\right)$
(b) $v_{\text {average }}=\left[r\left(t_{2}\right)-r\left(t_{1}\right] /\left(t_{2}-t_{1}\right)\right.$
(c) $v(t)=v(0)+a t$
(d) $a_{\text {average }}=\left[v\left(t_{2}\right)-v\left(t_{1}\right)\right] /\left(t_{2}-t_{1}\right)$

The average stands for average of the quantity over time interval $t_{1}$ to $t_{2}$

## D Watch Video Solution

24. Read each statement below carefully and
state with reason and examples, if it is true or
false.

A scalar quantity is one that
(a) is conserved in a process
(b) can never take negative values
(c) must be dimensionless
(d) does not vary from one point to another in
space
(e) has the same value for observers with different orientations of axes.
25. An aircraft is flying at a height of 3400 m above the ground. If the angle subtended at a ground observation point by the aircraft positions 10 s apart is $30^{\circ}$, what is the speed of the aircraft ?

## - Watch Video Solution

26. A vector has magnitude and direction
vary with time? (iii) Will two equal vectors $\vec{a}$ and $\vec{b}$ different locations in space necessarily have identical physical effects ? Give examples in support of your answer.

## - Watch Video Solution

27. A vector has both magnitude and direction.

Does that mean anything that has magnitude and direction is necessarily a vector ? The rotation of a body can specified by the direction of the axis of rotation and the angle
of rotation about the axis. Does the make any rotation a vector?

D Watch Video Solution
28. Can you associate vectors with (a) the length of a wire bent into a loop (b) a plane area (c) a sphere ? Explain.

D Watch Video Solution
29. A bullet fired at an angle of $30^{\circ}$ with the horizontal hits the ground 3.0 km away. By adjusting its angle of projection, can one hope to hit a target 5.0 km away? Assume the muzzle speed to be fixed and neglect air resistance.

## - Watch Video Solution

30. A fighter plane flying horizontally at an altitude of 1.5 km with speed $720 \mathrm{kmh}^{-1}$
passes directly over head an anti-aircraft gun.

At what angle from the vertical should the gun
be fired from the shell with muzzle speed $600 \mathrm{~ms}^{-1}$ to hit plane.

At what minimum altitude should the pilot fly the plane to avoid being hit ? ( Take $\mathrm{g}=10$ $m s^{-2}$ ).

## D Watch Video Solution

31. A cyclist is riding with a speed of $27 \mathrm{kmh}^{-1}$.

As he approaches a circular turn on the road
of radius 80 m , he applies brakes and reduces
his speed at the constant rate $0.5 m s^{-1}$. What
is the magnitude and direction of the net acceleration of the cyclist on the circular turn
?

## D Watch Video Solution

32. Show that for a projectile the angle between the velocity and the $x$-axis as function of time is given
by $\theta_{t}=\tan ^{-1}\left(\frac{v_{0 y}-g t}{v_{o x}}\right)$
(b) Shows that the projection angle $\theta_{0}$ for a projectile launched from the origin is given by $\theta_{t}=\tan ^{-1}\left(\frac{4 h_{m}}{R}\right)$ where the symbols have their usual meanings.
