



## MATHS

### BOOKS - JEE MAINS PREVIOUS YEAR

### RELATIONS AND FUNCTIONS

#### Others

1. The largest interval lying in  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$  for which the function  $\left[f(x) = 4^{-x} \wedge 2 + \cos^{-1}\left(\frac{x}{2} - 1\right) + \log(\cos x)\right]$  is defined, is (1)  $[0, \pi]$  (2)  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$  (3)  $\left[-\frac{\pi}{4}, \frac{\pi}{2}\right)$  (4)  $\left[0, \frac{\pi}{2}\right)$

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2. If the function  $f: R \setminus \{0\} \rightarrow$  given by  $f(x) = \frac{1}{x} - \frac{2}{e^{2x} - 1}$  is continuous at  $x = 0$ , then find the value of  $f(0)$

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3. Let  $f: N \rightarrow Y$  be a function defined as  $f(x) = 4x + 3$ , where  $Y = \{y \in N: y = 4x + 3 \text{ for some } x \in N\}$ . Show that  $f$  is invertible and its inverse is

$$(1) g(y) = \frac{3y + 4}{3}$$

$$(2) g(y) = 4 + \frac{y + 3}{4}$$

$$(3) g(y) = \frac{y + 3}{4}$$

$$(4) g(y) = \frac{y - 3}{4}$$

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4. Let  $R$  be the real line. Consider the following subsets of the plane  $R \times R$ .  $S = \{(x, y): y = x + 1 \text{ and } 0 < x < 2\}$ ,  $T = \{(x, y): x - y \text{ is an integer}\}$ .

Which one of the following is true?

(1) neither  $S$  nor  $T$  is an equivalence relation on  $R$

(2) both  $S$  and  $T$  are equivalence relations on  $R$

(3) S is an equivalence relation on R but T is not

(4) T is an equivalence relation on R but S is not



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5. Consider the following relations:  $R = \{(x, y) \mid x, y \text{ are real numbers and } x = wy \text{ for some rational number } w\}$ ;

$$S = \left\{ \left( \frac{m}{n}, \frac{p}{q} \right) \mid m, n, p \text{ and } q \text{ are integers such that } n, q \neq 0 \text{ and } mq = np \right\}.$$

. Then

(1) neither R nor S is an equivalence relation

(2) S is an equivalence relation but R is not an equivalence relation

(3) R and S both are equivalence relations

(4) R is an equivalence relation but S is not an equivalence relation



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6. The domain of the function  $f(x) = \frac{1}{\sqrt{|x| - x}}$  is:

(A)  $(-\infty, \infty)$

(B)  $(0, \infty$

(C)  $(-\infty, 0)$

(D)  $(-\infty, \infty) - \{0\}$

A.  $(-\infty, \infty) - \{0\}$

B.  $(-\infty, \infty)$

C.  $(0, \infty)$

D.  $(-\infty, 0)$

**Answer: null**



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7. If  $g$  is the inverse of a function  $f$  and  $f'(x) = \frac{1}{1+x^5}$ , then  $g'(x)$  is equal to



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8. The sum of all real values of  $x$  satisfying the equation  $(x^2 - 5x + 5)^{x^2 + 4x - 60} = 1$  is: (1) 3 (2) -4 (3) 6 (4) 5



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9. The function  $f: \overrightarrow{R - \frac{1}{2}, \frac{1}{2}}$  defined as  $f(x) = \frac{x}{1 + x^2}$ , is : Surjective but not injective (2) Neither injective nor surjective Invertible (4) Injective but not surjective



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