



## PHYSICS

### NCERT - NCERT PHYSICS(ENGLISH)

#### DUAL NATURE OF RADIATION AND MATTER

##### Solved Examples

1. Monochromatic light of frequency  $6.0 \times 10^{14} \text{ Hz}$  is produced by a laser. The power emitted is  $2 \times 10^{-3} \text{ W}$ . The number of photons emitted, on the average, by the sources per second is

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2. The work function of cesium is 2.14 eV. Find (a) the threshold frequency for cesium, and (b) the wavelength of the incident light if the

photo current is brought to zero by a stopping potential 0.60 V. Given

$$h = 6.63 \times 10^{-34} Js.$$



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3. The wavelength of light in the visible region is about 390nm for violet color, about 550nm (average wavelength) for yellow green colour and about 760nm for red color. What are the energies of photon in eV at the (i) violet end (ii) average wavelength yellow-green color and (iii) red end of the visible spectrum?

(Take  $h = 6.63 \times 10^{-34} Js$  and  $1eV = 1.6 \times 10^{-19} Js$ )



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4. What is the de-Broglie wavelength associated with (a) an electron moving with speed of  $5.4 \times 10^6 ms^{-1}$ , and (b) a ball of mass 150g traveling at  $30.0 ms^{-1}$ ?  $h = 6.63 \times 10^{-34} Js$ , mass of electron  $= 9.11 \times 10^{-31} kg$ .



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5. An electron, an  $\alpha$ -particle and a proton have the same kinetic energy. Which of these particles has the largest de-Broglie wavelength?



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6. A particle is moving three times as fast as an electron. The ratio of the de- Broglie wavelength of the particle to that of the electron is  $1.813 \times 10^{-4}$ . Calculate the particle's mass and identify the particle.  
Mass of electron =  $9.11 \times 10^{-31} \text{ kg}$ .



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7. What is the de-Broglie wavelength associated with an electron moving with an electron, accelerated through a potential difference of 100 volt?



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## Exercise

1. Find the (a) maximum frequency and (b) minimum wave-length of X-rays produced by 30 kV electrons. Given,  $h = 6.63 \times 10^{-34} Js$ .



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2. The work function of caesium is 2.14 eV. When light of frequency  $6 \times 10^{14} Hz$  is incident on the metal surface, photoemission of electrons occurs. What is the (a) maximum kinetic energy of the emitted electrons. (b) stopping potential and (c) maximum speed of the emitted photoelectrons. given ,  
 $h = 6.63 \times 10^{-34} Js$ ,  $1eV = 1.6 \times 10^{-19} J$ ,  $c = 3 \times 10^8 m/s$ .



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3. The photoelectric cut off voltage in a certain experiment is 1.5V. What is the maximum kinetic energy of photoelectrons emitted?  
 $e = 1.6 \times 10^{-19}C$ .



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4. Monochromatic light of wavelength  $632.8nm$  is produced by a helium-neon laser. The power emitted is  $9.42mW$ . (a) Find the energy and momentum of each photon in the light beam. (b) How many photons per second, on the average, arrive at a target irradiated by this beam? (Assume the beam to have uniform cross-section which is less than the target area). (c) How fast does a hydrogen atom have to travel in order to have the same momentum as that of the photon.  
 $h = 6.663 \times 10^{-34}Js$ ,  $1a. m. u. = 1.66 \times 10^{-27}kg$ .



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5. The energy flux of the sunlight reaching the surface of the earth is  $1.388 \times 10^3 \text{ W m}^{-2}$ . How many photons (nearly) per square meter are incident on the earth per second? Assume that the photons in the sunlight have an average wavelength of 550 nm.



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6. In an experiment on photoelectric effect, the slope of the cut off voltage versus frequency of incident light is found to be  $4.12 \times 10^{-15} \text{ V s}$ . Given  $e = 1.6 \times 10^{-19} \text{ C}$ , estimate the value of Planck's constant.



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7. A 100W sodium lamp radiates energy uniformly in all directions. The lamp is located at the center of a large sphere that absorbs all the sodium light which is incident on it. The wavelength of the sodium

light is 589nm. (a) What is energy associated per photon with the sodium light? (b) At what rate are photons delivered to the sphere?



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8. The threshold frequency of a certain metal is  $3.3 \times 10^{14} Hz$ . If light of frequency  $8.2 \times 10^{14} Hz$  is incident on the metal, predict the cut off voltage for photoelectric emission. Given Planck's constant,  $h = 6.62 \times 10^{-34} Js$ .



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9. The work function for a certain metal is 4.2eV. Will this metal give photoelectric emission for incident radiation of wavelength 330 nm? Use,  $h = 6.6 \times 10^{-34} Js$ .



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10. Light of frequency  $7.21 \times 10^{14} \text{ Hz}$  is incident on a metal surface. Electrons with a maximum speed of  $6.0 \times 10^5 \text{ ms}^{-1}$  are ejected from the surface. What is the threshold frequency for photoemission of electrons?  $h = 6.63 \times 10^{-34} \text{ Js}$ ,  $m_e = 9.1 \times 10^{-31} \text{ kg}$ .



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11. Light of wavelength 488 nm is produced by an atom laser which is used in the photoelectric effect. When light from this spectral line is incident on the cathode, the stopping potential of photoelectrons is 0.38 eV. Find the work function of the material from which the cathode is made. given,  $h = 6.63 \times 10^{-34} \text{ Js}$ ,  $1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$ .



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12. Calculate the (a) momentum and (b) de-Broglie wavelength of the electrons accelerated through a potential difference of 56V. Given,



$$h = 6.63 \times 10^{-34} Js, m_e = 9.1 \times 10^{-31} kg, e = 1.6 \times 10^{-19} C.$$



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**13.** What is the (a) momentum (b) speed and (c) de-Broglie wavelength of an electron with kinetic energy of 120 eV. Given  $h = 6.6 \times 10^{-34} Js, m_e = 9 \times 10^{-31} kg, 1eV = 1.6 \times 10^{-19} J$ .



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**14.** The wavelength of light from the spectral emission line of sodium is 589nm. Find the kinetic energy at which (a) an electron and (b) a neutron would have the same deBroglie wavelength. Given that mass of neutron  $= 1.66 \times 10^{-27} kg$



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15. What is the de-Broglie wavelength of (a) a bullet of mass  $0.040\text{kg}$  traveling at the speed of  $1.0\text{km s}^{-1}$ . (b) a ball of mass  $0.060\text{kg}$  moving at a speed of  $1.0\text{m s}^{-1}$  and (c) a dust particle of mass  $1.0 \times 10^{-9}\text{kg}$  drifting with a speed of  $2.2\text{m s}^{-1}$ ?  $h = 6.63 \times 10^{-34}\text{Js}$ .



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16. An electron and a photon each has a wavelength of  $1.0\text{nm}$ . Find (a) their momenta, (b) the energy of the photon, and (c) the kinetic energy electron.

Take  $h = 6.63 \times 10^{-34}\text{Js}$ .



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17. A. For what kinetic energy of neutron will the associated de Broglie wavelength be  $1.40 \times 10^{-10}\text{m}$ ?

B. Also, find the de Broglie wavelength of a neutron, in thermal

equilibrium with matter, having an average kinetic energy of  $\left(\frac{3}{2}\right) kT$  at  $300K$ . Given the mass of neutron  $= 1.66 \times 10^{-27} kg$  and  $k = 1.38 \times 10^{-23} Jkg^{-1}$ .



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**18.** Show that the wavelength of electromagnetic radiation is equal to the de-Broglie wavelength of its quantum (photon).



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**19.** What is the de-Broglie wavelength of nitrogen molecule in air at  $300K$  ? Assume that the molecule is moving with the root mean square speed of molecules at this temperature. (Atomic mass of nitrogen  $= 14.0076U$ ) Planck's constant  $= 6.63 \times 10^{-34} Js$  , Boltzmann constant  $= 1.38 \times 10^{-23} JK^{-1}$



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**20.** (a) Estimate the speed with which electrons emitted from a heated cathode of an evacuated tube impinge on the anode maintained at a potential difference of 500 V with respect to the cathode. Ignore the small initial speeds of the electrons. The specific charge of the electron, i.e., its  $e/m$  is given to  $1.76 \times 10^{11} \text{ C kg}^{-1}$ .

(b) Use the same formula you employ in (a) to obtain electron speed for an anode potential of 10 MV. Do you see what is wrong? In what way is the formula to be modified?



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**21.** (a) A monoenergetic electron beam with electron speed of  $5.20 \times 10^6 \text{ m s}^{-1}$  is subjected to a magnetic field of  $1.30 \times 10^{-4} \text{ T}$ , normal to the beam velocity. What is the radius of the circle traced by the beam, given  $e/m$  for electron equal  $1.76 \times 10^{11} \text{ C. kg}^{-1}$ .

(b) Is the formula you employ in (a) valid for calculating radius of the path of 20 MeV electrons beam? If not, in what way is it modified!



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22. An electron gun with its anode at a potential of 100V fires out electrons in a spherical bulb containing hydrogen gas at low pressure ( $10^{-2}$  mm of Hg). A magnetic field of  $2.83 \times 10^{-4} T$  curves the path of the electrons in a circular orbit of radius 12.0 cm. (The path can be viewed because the gas ions in the path focus the beam by attracting electrons and emitting light by electron capture, this method is known as 'fine beam tube' method). Determine  $e/m$  from the data.

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23. (a) An X-ray tube produces a continuous spectrum of radiation with its short wavelength end at  $0.45 \text{ \AA}$ . What is the maximum energy of the photon in the radiation? (b) From your answer to (a), guess what order of accelerating voltage (for electrons) is required in such a tube?

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**24.** In an accelerator experiment on high energy collision of electrons with positrons, a certain events is interpreted as annihilation of an electron-positron pair of total energy 10.2 BeV into two  $\gamma$ -rays of equal energy. What is the wavelength associated with each  $\gamma$ -rays?  
( $1\text{BeV} = 10^9\text{eV}$ )



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**25.** Estimate the following the following two numbers should be interesting. The first number will tell you why radio engineers do not need to worry much about a photons. The second number tells you why our eye can never "count photon" even in barely detectable light.

(i) The number of photons emitted per second by a MW transmitter of 10kW power emitting radiowaves of length 500m.

(ii) The number of photons entering the pupil of our eye per second corresponding to the minimum intensity of white light that we humans can perceive ( $\sim 10^{-10}\text{Wm}^{-2}$ ). Take the area of the pupil to be about

$0.4\text{cm}^2$ , and the average frequency of white light to be about  $6 \times 10^4\text{Hz}$ . ( $h = 6.6 \times 10^{-34}\text{J}$ )



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**26.** Ultraviolet light of wavelength  $2271\text{\AA}$  from a  $100\text{W}$  mercury source irradiates a photocell made of molybdenum metal. If the stopping potential is  $1.3\text{V}$ , estimate the work function of the metal. How would the photocell respond to a high intensity ( $\sim 10^5\text{Wm}^{-2}$ ) red light of wave length  $6328\text{\AA}$  produced by a He-Ne laser?



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**27.** Monochromatic radiation of wave length  $640.2\text{ nm}$  ( $1\text{nm} = 10^{-9}\text{m}$ ) from a neon lamp irradiates a photosensitive material made of calcium or tungsten. The stopping voltage is measured to be  $0.54\text{V}$ . The source is replaced by an iron source and its

427.2 nm line irradiates the same photocell. Predict the new stopping voltage.



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**28.** A mercury lamp is a convenient source for studying frequency dependence of photoelectric emission, since it gives a number of spectral lines ranging from the UV to the end of the red visible spectrum. In our experiment with rubidium photocell, the following lines from a mercury source were used:

$$\lambda_1 = 3650 \text{Å}, \lambda_2 = 4047 \text{Å}, \lambda_3 = 4358 \text{Å}, \lambda_4 = 5461 \text{Å}, \lambda_5 = 6907 \text{Å}$$

The stopping voltages, respectively were measured to be:

$$V_{01} = 1.28 \text{V}, V_{02} = 0.95 \text{V}, V_{03} = 0.74 \text{V}, V_{04} = 0.16 \text{V}, V_{05} = 0 \text{V}.$$

(a) Determine the value of Planck's constant  $h$ .

(b) Estimate the threshold frequency and work function for the material.



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29. The work function for the following metals is given Na: 2.75 eV, K: 2.30 eV, Mo: 4.17 eV, Ni: 5.15 eV.

Which of these metals will not give photoelectric emission for a radiation of wavelength 3300 Å from a *He – Cd* laser placed 1m away from the photocell? What happens if the laser is brought nearer and placed 50 cm away?



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30. Light of intensity  $10^{-5} \text{ W m}^{-2}$  falls on a sodium photocell of surface area  $2 \text{ cm}^2$ . Assuming that the top 5 layers of sodium absorb the incident energy, estimate the time required for photoelectric emission in the wave picture of radiation. The work function of the metal is given to be about 2 eV. What is the implication of your answer?

effective atomic area  $= 10^{-20} \text{ m}^2$ .



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**31.** Crystal diffraction experiments can be performed using X-rays, or electrons accelerated through appropriate voltage. Which probe has greater energy? An X-ray photon or the electron? (For quantitative comparison, take the wavelength of the probe equal to  $1\text{\AA}$ , which is of the order of interatomic spacing in the lattice),  $m_e = 9.11 \times 10^{-31} \text{kg}$ .



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**32. (a)** Obtain the de-Broglie wavelength of a neutron of kinetic energy 150 eV. As you have seen in previous problem 31, an electron beam of this energy is suitable for crystal diffraction experiments. Would a neutron beam of the same energy be equally suitable? Explain. Given  $m_n = 1.675 \times 10^{-27} \text{kg}$ .

**(b)** Obtain the de-Broglie wavelength associated with thermal neutrons at room temperature ( $27^\circ \text{C}$ ). Hence explain why a fast neutrons beam needs to be thermalised with the environment before it can be used for neutron diffraction experiments.



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**33.** An electron microscope uses electrons accelerated by a voltage of  $50kV$ . Determine the De Broglie wavelength associated with the electrons. If other factors ( such as numerical aperture, etc.) are taken to be roughly the same, how does the resolving power of an electron microscope compare with that of an optical microscope which uses yellow light?



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**34.** The wavelength of a probe is roughly a measure of the size of structure that it can probe in some detail. The quarks structure of photons and neutrons appears at the minute length -scale of  $10^{-15}m$  or less. This structure was first probed in early 1970's using high energy electron beam produced by a linear accelerator at Stanford's USA. Guess what might have been the order of energy of these electron beams (Rest mass energy of electron= $0.511\text{ eV}$ ).



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35. Find the typical de-Broglie wavelength associated with a H-atom in helium gas at room temperature ( $27^{\circ}C$ ) and 1atm pressure, and compare it with the mean separation between two atom under these conditions.

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36. Compute the typical de-Broglie wavelength of an electrons in a metal at  $27^{\circ}C$  and compare it with the mean separation between two electrons in a metal which is given to be about  $2 \times 10^{-10}m$ .

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37. Answer the following questions:

(a) Quarks inside protons and neutrons are thought to carry fractional charges  $[(+2/3)e, (-1/3)e]$ . Why do they not show up in Millikan's oil-

drop experiment?

(b) What is so special about the combination  $e/m$ ? Why do we not simply talk of  $e$  and  $m$  separately?

(c) Why should gases be insulators at ordinary pressures and start conducting at very low pressures?

(d) Every metal has a definite work function. Why do all photoelectrons not come out with the same energy if incident radiation is monochromatic? Why is there an energy distribution of photoelectrons?

(e) The energy and momentum of an electron are related to the frequency and wavelength of the associated matter wave by the relations:

$$E = h \nu, p = \frac{h}{\lambda}$$

But while the value of  $\lambda$  is physically significant, the value of  $\nu$  (and therefore, the value of the phase speed  $\nu \lambda$ ) has no physical significance. Why?



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