



MATHS

BOOKS - RD SHARMA MATHS (HINGLISH)

DERIVATIVES

Solved Examples And Exercises

1. Differentiate the following with respect to x: (i)

 $x^3 e^x \sin x$ (ii) $x \sin x \log x$ (iii) $x^n (\log)_a x e^x$

2. Differentiate the following functions with $x+e^x$

respect to
$$x : \frac{1}{1 + \log x}$$

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3. If
$$f(x) = lpha x^n, ext{ prove that } lpha = rac{f'(1)}{n}$$
 .

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4. Differentiate the following functions with respect to $x : (ax + b)^n (cx + d)^n$

5. If
$$f(x)andg(x)$$
 are two differentiable
functions, show that $f(x)g(x)$ is also
differentiable such that
 $\frac{d}{dx}[f(x)g(x)] = f(x)\frac{d}{dx}\{g(x)\} + g(x)\frac{d}{dx}\{f(x)\}$
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6. The differentiation of $(\log)_a x$ (a >0) with respect to x i.e. $\frac{d}{dx}((\log)_a x) = \frac{1}{x(\log)_e a}$

7. If
$$y = \sqrt{\frac{x}{a}} + \sqrt{\frac{a}{x}}$$
 , prove that $2xy\frac{dy}{dx} = \left(\frac{x}{a} - \frac{a}{x}\right)$



8. If for
$$f(x) = \lambda x^2 + \mu x + 12$$
 and $f'(4) = 15$
and $f'(2) = 11$, then find λ and μ

9. Differentiate
$$x^2 \cos x$$



11. If
$$y = \sqrt{rac{1-\cos 2x}{1+\cos 2x}}, x \in \left(0,rac{\pi}{2}
ight) \cup \left(rac{\pi}{2},\pi
ight),$$
 then find $rac{dy}{dx}$.

12. The differentiation of
$$\log_e x$$
, $is\frac{1}{x}$. i.e.
 $\frac{d}{dx}\left((\log_e x) = \frac{1}{x}\right)$
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13. Differentiate the following functions with
respect to x from first principles: $\sqrt{ax + b}$
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14. Differentiate x^n by first princeple

15. Differentiate the following functions with respect to x from first principles: $tan \sqrt{x}$



16. The differentiation of tanx with respect to x is

$$\sec^2 x$$
 · i.e. $rac{d}{dx}(an x) = \sec^2 x$



17. The differentiation of $\cot x$ with respect to x is

$$-\cos ec^2 x$$
 i.e. $rac{d}{dx}(\cot x)=\ -\cos ec^2 x$

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18. (x) The differentiation of secx with respect to x

is $\sec x \tan x$

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19. The differentiation of $\cos ecx$ with respect to x

$$\frac{d}{dx}(\cos ec) = -\cos ecx \cot x$$

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20. The differentiation of e^{-x} with respect to x is
$$-e^{-x} \cdot \text{i.e.} \frac{d}{dx}(e^{-x}) = -e^{-x}$$

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21. Differentiate the following functions with respect to $x : e^{3 \log x}$

22. Let f(x) be a differentiable and let c a be a constant. Then cf(x) is also differentiable such that $\frac{d}{dx}\{cf(x)\} = c\frac{d}{dx}(f(x))$.

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23. Differentiate the following functions with

respect to
$$x \colon \left(\sqrt{x} + rac{1}{\sqrt{x}}
ight)^2$$

A.
$$1 - \left(\frac{1}{x}\right)^2$$

B. $1 + \left(\frac{1}{x}\right)^2$
C. $x - \left(\frac{1}{x}\right)^2$

D. None of these

Answer: A



25. Differentiate the following functions with respect to $x : \frac{10^x}{\sin x}$



26.
$$f(x) = x^2 e^x \log x$$

differentiate f(x) with respect to x at x = 1

A. 0

B. 1

C. e

D. none of these

Answer: C



27. Differentiate the following functions with

respect to $x \ rac{\sec x + \tan x}{\sec x - \tan x}$

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28. If
$$y = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^n}{n!}$$
, show that $\frac{dy}{dx} - y + \frac{x^n}{n!} = 0$.

29. If
$$y = 1 + rac{x}{1!} + rac{x^2}{2!} + rac{x^3}{3!} + ,$$
 show that $rac{dy}{dx} = y - rac{x^n}{n!}$

30. Differentiate the following functions with respect to x $x^4(5\sin x - 3\cos x)$



31. Differentiate the following functions with respect to x $(x \sin x + \cos x)(e^x + x^x + \log x)$

32. Differentiate the following functions with respect to $x: \frac{e^x + \sin x}{1 + \log x}$

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33. Differentiate the following functions with respect to $x: \frac{e^x - \tan x}{\cot x - x^n}$ **Vatch Video Solution**

34. The differentiation of $\cos x$ with respect to x is

-sinx i.e. $\frac{d}{dx}(\cos x) = -\sin x$

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35. The differentiation of $\sin x$ with respect to x is

$$\cos x \cdot$$
 i.e. $rac{d}{dx}(\sin x) = \cos x$





38. The differentiation of $a^x(a>0, a
eq 1)$ with





39. Differentiate $e^{\sqrt{\tan x}}$ from the first principle.



40. If $f(x)=x^n$ where $x\in R$, then differentiation of x^n with respect to $x\ is x^{n-1}$.



43. If
$$f(x)andg(x)$$
 are differentiate functions,
then show that $f(x) \pm g(x)$ are also
differentiable such that
 $\frac{d}{dx} \{f(x) \pm g(x)\} = \frac{d}{dx} \{f(x)\} \pm \frac{d}{dx} \{g(x)\}$
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44. If f(x)andg(f) are two differentiable functions and $g(x) \neq 0$, then show that $\frac{f(x)}{g(x)}$ is

differentiable

$$rac{d}{dx}igg\{rac{f(x)}{g(x)}igg\}=rac{g(x)rac{d}{dx}\{f(x)\}-f(x)rac{d}{dx}\{g(x)\}}{\left[g(x)
ight]^2}$$

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also

45. If u, v and w are functions of x, then show that

$$rac{d}{dx}(u\dot{v}\dot{w})=rac{du}{dx}\dot{v}\dot{w}+urac{dv}{dx}\dot{w}+u\dot{v}rac{dw}{dx}$$
 in two

ways - first by repeated application of product rule, second by logarithmic differentiation.



46. Differentiation of a constant function is zero

i.e.,
$$rac{d}{dx}(c)=0.$$

47. If f(x) = mx + c and f(0) = f'(0) = 1. What is f(2)?

A. 2

B. 1

C. 0

D. none of these

Answer: B



48. Find
$$\frac{dy}{dx}, when y = 3 \tan x + 5(\log)_a x + \sqrt{x} - 3e^x + \frac{1}{x}$$

49. Differentiate the following functions with respect to x from first principles: $\cot \sqrt{x}$

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50. Differentiate the following functions with respect to x from first principles: $\sqrt{\sin x}$



53. Differentiate the following functions with respect to x from first principles: $\frac{1}{x}$



54. Differentiate the following functions with respect to x from first principles: $\frac{x-1}{x+1}$

A.
$$\displaystyle rac{x-1}{x+1}$$

B. $\displaystyle rac{x-1}{\left(x+1
ight)^2}$
C. $\displaystyle rac{2}{\left(x+1
ight)^2}$

D. None of these

Answer: C





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56. Find the derivative of $s \ i \ n \ x \setminus a \ t \setminus x = 0.$

57. Let f be a real valued function defined by $f(x) = x^2 + 1$. Find f'(2).

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58. Find the derivative of $f(x) = 2x^2 + 3x - 5$ at

x = -1. Also, prove that

f'(0) + 3f'(-1) = 0.

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59. Find the derivative of $f(x) = 3x \setminus a t \setminus x = 2$.







63. Find the derivative of
$$f(x) = x \setminus at \setminus x = 1$$

64. Find the derivative of the function at the indicated point: $\sin x$ at $x = \frac{\pi}{2}$

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65. Find the derivative of the following function at

the indicated point: $x \setminus at \setminus x = 1$

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66. Find the derivative of the following function at the indicated point: $2\cos x \setminus at \setminus x = \setminus \frac{\pi}{2}$



68. The distance f(t) in metres ived by a particle travelling in a straight line in t seconds is given by $f(t) = t^2 + 3t + 4$. Find the speed of the particle at the end of 2 seconds.

69. Find the slope of the tangent to the curve $y = x^2$ at $\left(-\frac{1}{2}, \frac{1}{4}\right)$.

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70. Find the derivatives of the following function

from first principle: $x^3 - 27$



71. Find the derivatives of the following function

from first principle: (x-1)(x-2)





73. Differentiate the following function with respect to x from first principle: $\sqrt{2x+3}$



76. Differentiate the following function with respect to x from first principle: $\frac{2x+3}{3x+2}$

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77. Differentiate the following function with respect to x from first principle: $x^{-3/2}$

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78. Differentiate each of the following from first principle: $\frac{2}{x}$



80. Differentiate each of the following from first

principle:
$$rac{x+2}{3x+5}$$
principle: $x^2 + x + 3$

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82. Differentiate each of the following from first principle: $(x^2 + 1)(x - 5)$

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83. Differentiate each of the following from first

principle: e^{-x}



principle: $\sin(x+1)$

principle: $x \cos x$



88. Differentiate each of the following from first

principle:
$$\displaystyle rac{x^2-1}{x}$$



principle: $(x+2)^3$

principle: $\sqrt{2x^2+1}$

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92. Differentiate each of the following from first principle: e^{3x}

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93. Differentiate each of the following from first

principle: -x



principle: $\sin(2x-3)$

96. Differentiate each of the following from first principle: $\frac{1}{x^3}$ **Vatch Video Solution**

97. Differentiate each of the following from first

principle: $\frac{x+1}{x+2}$

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98. Differentiate each of the following from first

principle:
$$\frac{1}{\sqrt{3-x}}$$



principle:
$$\displaystyle rac{2x+3}{x-2}$$

principle: e^{ax+b}

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102. Differentiate each of the following from first

principle: $(-x)^{-1}$

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103. Differentiate each of the following from first

principle: $x \sin x$



principle: $x^2 \sin x$

principle: $x^2 e^x$



107. Differentiate each of the following from first

principle: $e^{\sqrt{ax+b}}$

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108. Differentiate each of the following from first principle: $\tan^2 x$



principle: $\frac{\sin x}{x}$

principle: $\sqrt{\sin(3x+1)}$

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112. Differentiate each of the following from first principle: e^{x^2+1}

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113. Differentiate each of the following from first

principle: $a^{\sqrt{x}}$



114. Differentiate each of the following from first principle: an(2x+1)

A. 2 sec(2x+1)

- $\mathsf{B.sec}^2(2x+1)$
- $\mathsf{C.}\, 2 \sec^2(2x+1)$

D.
$$2\cos^2(2x+1)$$

Answer: null

principle: $\cos \sqrt{x}$

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116. Differentiate the following from first principle:

 $\tan 2x$



principle: $tan \sqrt{x}$





principle: $\frac{\cos x}{x}$

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119. Differentiate each of the following from first

principle: $\sin x + \cos x$



121. Differentiate the following from first principle:

 3^{x^2}

principle: $\sqrt{\tan x}$



123. Differentiate each of the following from first

principle: tan2x

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124. Differentiate the following with respect of x:

$$ig(x^2-3x+2ig)(x+1)$$



126. Differentiate the following with respect of $x: \frac{\sin(x+a)}{\cos x}$

x: $x^4 - 2\sin x + 3\cos x$



128. Differentiate the following with respect of

$$x: 3^x + x^3 + 3^3$$

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129. Differentiate the following with respect of

$$x\!:\!rac{x^3}{3}-2\sqrt{x}+rac{5}{x^2}$$



$$x : (2x^2 + 1)(3x + 2)$$

 $x : (\log)_3 x + 3(\log)_e x + 2\tan x$

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133. Differentiate the following with respect of

$$x : \left(x + \frac{1}{x}\right) \left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)$$

134. Differentiate the following with respect of
$$x: \frac{(x^3+1)(x-2)}{x^2}$$
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135. Differentiate the following with respect of $x: a_0x^n + a_1x^{n-1} + a_2x^{n-2} + a_{n-1}x + a_n$. Watch Video Solution

136. Differentiate the following with respect of
$$x: \frac{(x+5)(2x^2-1)}{x}$$



$$egin{array}{lll} & \setminus & y = igg(rac{2-3\cos x}{\sin x}igg), egin{array}{ll} & f \in drac{dy}{dx}igg & atigwedge & x = rac{\pi}{4} \end{array}$$

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140. Differentiate the following with respect of $x: \frac{2x^2 + 3x + 4}{x}$



141. Differentiate the following with respect of $x: \frac{a\cos x + b\sin x + c}{\sin x}$

lf



$$x : rac{1}{\sin x} + 2^{x+3} + rac{4}{\log_x 3}$$

$$x : \log \left(rac{1}{\sqrt{x}}
ight) + 5 x^a - 3 a^x + \sqrt[3]{x^2} + 6 \sqrt[4]{x^{-3}}$$

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145. Differentiate the following with respect of $x \colon rac{\cos(x-2)}{\sin x}$



146. Find the rate of at which the function $f(x) = x^4 - 2x^3 + 3x^2 + x + 5$ changes with respect to x.

147. If
$$y = \frac{2x^9}{3} - \frac{5}{7}x^7 + 6x^3 - x$$
, find $\frac{dy}{dx}at \ x = 1.$







 $x : x \sin x$



 $x : e^x \sin x + x^n \cos x$



151. Differentiate the following with respect of $x: (x + \sec x)(x - \tan x)$

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152. Differentiate the following with respect of $x : (x^2 + 1) \cos x$



 $x\!:\!e^x(x+\log x)$

 $x : (x + \cos x)(x - \tan x)$



156. Differentiate the following with respect of $x: (ax^2 + \sin x)(p + q\cos x)$

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157. Using mathematical induction prove that : $rac{d}{dx}(x^n)=nx^{n-1}$ for all $n\in N.$



159. Differentiate the following function with

respect of $x : x^n \tan x$

160. Differentiate the following function with

respect of x: $\sin x \cos x$

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161. Differentiate the following function with respect of $x : x^5 e^x + x^6 \log x$

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162. Differentiate the following function with respect of $x: (1 + x^2) \cos x$



164. Differentiate the following function with respect of $x : x^5 (3 - 6x^{-9})$ Watch Video Solution

165. Differentiate the following function with respect of
$$x: \frac{ax+b}{cx+d}$$

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166. Differentiate the following function with respect of $x : x^3 e^x$

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167. Differentiate the following function with respect of $x : x^n \log_a x$




170. Differentiate the following function with respect of $x : \sin^2 x$ **Vatch Video Solution**

171. Differentiate the following function with respect of x: $x^3 e^x \cos x$

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172. Differentiate the following function with respect of $x \setminus x^{-4}(3-4x^{-5})$



174. Differentiate the following function with respect of $x: x^2 \sin x \log x$ Watch Video Solution 175. Differentiate the following function with

respect of x: $(1 - 2\tan x)(5 + 4\sin x)$



176. Differentiate the following function with respect of $x : (\log)_{x^2} x$





178. Differentiate the following function with respect of $x: (2x^2 - 3)\sin x$



179. Differentiate the following function with respect of $x : x^{-3}(5+3x)$ Watch Video Solution

180. Differentiate in two ways, using product rule and otherwise, the function $(1+2\tan x)(5+4\cos x)$.Verify that the answer

are the same.

181. Differentiate each of the following functions by the product rule and the other method and verify that answer from both the methods is the same.

(i)
$$\left(3x^2 + 2
ight)^2$$

(ii) $(x+2)(x+3)$

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182. Differentiate the following function by the product rule and the other method and verify

that answer from both the methods is the same :

 $(3\sec x-4\cos ecx)(-2\sin x+5\cos x)$



184. Differentiate the following function with respect of $x: \frac{\sin x + \cos x}{\sin x - \cos x}$



186. Differentiate the following function with respect of $x: \frac{\sec x - 1}{\sec x + 1}$

187. Differentiate the following function with respect of
$$x: \frac{x^2 + 1}{x + 1}$$

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189. Differentiate the following function with respect of $x: \frac{x \tan x}{secx + tanx}$





192. Differentiate the following function with respect of $x: \frac{x}{1 + \tan x}$ Watch Video Solution



194. Differentiate the following function with respect of $x : \frac{x^n}{\sin x}$





respect of
$$x : \frac{e^x}{1+x^2}$$



199. Differentiate the following function with respect of 2-x+1/(x^2+x+1)`





202. Differentiate the following function with respect of
$$x: \frac{x^5 - \cos x}{\sin x}$$

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204. Differentiate the following function with respect of $x : \frac{x}{1 + \tan x}$



206. Differentiate the following function with respect of $x : \sec(\tan(\sqrt{x}))$

207. Differentiate the following function with

respect of
$$x \colon rac{1+3^x}{1-3^x}$$

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209. Differentiate the following function with respect of $x: \frac{px^2 + qx + r}{ax + b}$



211. Differentiate the function with respect of $x: \frac{1}{a x^2 + b x + c}$ **Vatch Video Solution**





216. Write the value of
$$\frac{d}{dx}(x |x|)$$
.

217. Write the value of
$$\displaystyle rac{d}{dx} \{(x+|x|)|x|\}$$
 .

218. If f(x) = |x| + |x - 1| , write the value of $\displaystyle rac{d}{dx}(f(x)).$

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219. Write the value of the derivative of $f(x) = |x-1| + |x-3| \ at \ x = 2.$

220. If
$$f(x)=rac{x^2}{|x|}$$
 , write $rac{d}{dx}(f(x))$





221. Write the value of
$$\frac{d}{dx}(\log |x|)$$
.

222. If
$$f(1)=1,$$
 $f'(1)=2,$ then write the value of $\lim_{x
ightarrow 1}rac{\sqrt{f(x)}-1}{\sqrt{x}-1}$

223. Write the derivative of f(x) = 3 |2 + x| at

x = -3.





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225. Let $f(x)=x-[x], x\in \mathbb{R},$ then $f'\left(rac{1}{2}
ight)$ is a. $rac{3}{2}$ b. 1 c. 0 d. -1



226. If
$$f(x)=rac{x-4}{2\sqrt{x}}$$
 , then $f'(1)$ is a. $rac{5}{4}$ b. $rac{4}{5}$ c. 1

d. 0

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227. If
$$y=1+rac{x}{1!}+rac{x^2}{2!}+rac{x^3}{3!}+...$$
 , then $rac{dy}{dx}= ext{ a. }y+1 ext{ b. }y-1 ext{ c. }y ext{ d. }y^2$

$$f(x) = 1 - x + x^2 - x^3 + ... - x^{99} + x^{100}$$
,

then f'(1) equals a. 150 b. -50 c. -150 d. 50

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229. If
$$y = \frac{1 + \frac{1}{x^2}}{1 - \frac{1}{x^2}}$$
, then $\frac{dy}{dx}$ = a. $-\frac{4x}{(x^2 - 1)^2}$ b. $-\frac{4x}{x^2 - 1}$ c. $\frac{1 - x^2}{4x}$ d. $\frac{4x}{x^2 - 1}$

230. If
$$y=\sqrt{x}+rac{1}{\sqrt{x}}$$
, then $rac{dy}{dx}$ at $x=1$ is a. 1 b. $rac{1}{2}$ c. $rac{1}{\sqrt{2}}$ d. 0

231. If $f(x) = x^{100} + x^{99} + ... + x + 1$, then

f'(1) is equal to a. 5050 b. 5049 c. 5051 d. 50051

232. If
$$f(x) = 1 + x + rac{x^2}{2} + ... + rac{x^{100}}{100},$$
 then $f'(1)$ is equal to a. $rac{1}{100}$ b. 100 c. 50 d. 0



234. If
$$y = \frac{\sin(x+9)}{\cos x}$$
, then $\frac{dy}{dx}$ at x = 0 is: a.

 $\cos 9$ b. $\sin 9$ c. 0 d. 1

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235. If
$$f(x) = rac{x^n-a^n}{x-a}$$
, then $f'(a)$ is a. 1 b. $rac{1}{2}$ c.

0 d. does not exist

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236. If
$$f(x) = x \sin x$$
, then $f'\left(rac{\pi}{2}
ight)$ is a. $rac{1}{2}$ b. 1 c.
 0 d. -1