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## MATHS

## BOOKS - RD SHARMA MATHS (HINGLISH)

## LINEAR INEQUATIONS

Solved Examples And Exercises

1. Show that the solution set of the following linear

$$
\begin{aligned}
& \text { inequations is an unbounded set: } \\
& x+\mathrm{y} \geq 9,3 x+y \geq 12, x \geq 0, y \geq 0
\end{aligned}
$$

2. Solve the following inequations grapihically:
$(i)|x| \leq 3$
(ii) $|y-x| \leq 3$

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3. Exhibit graphically the solution set of the linear inequations
$x+\mathrm{y} \leq 5,4 x+y \geq 4, x+5 y \geq 5, x \leq 4, y \leq 3$
4. Solve each of the following system of equations in

$$
R \cdot x+5>2(x+1), 2-x<3(x+2)
$$

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5. Solve the following linear inequations: $\frac{x-3}{x-5}>0$
(ii) $\frac{x-2}{x+5}>2$

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6. Solve: $5 \leq \frac{2-3 x}{4} \leq 9$
A. $[-6,11]$
B. $[-11,-6]$
C. $[6,11]$
D. None of these

## Answer: D

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7. Solve the following system of linear inequations
$2(2 x+3)-10<6(x-2)$
$\frac{2 x-3}{4}+6 \leq 2+\frac{4 x}{3}$
8. Solve the following linear inequations in $R$. $\frac{5 x}{2}+\frac{3 x}{4} \geq \frac{39}{4}$

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9. Solve the following system of linear inequations:
$3 x-6 \geq 0,4 x-10 \leq 6$

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10. Solve the following linear inequations in $R$.
$\frac{7 x-5}{8 x+3}<4$
11. Solve the following linear inequations in $R$. $\frac{5 x+8}{4-x}<2$

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12. A company manufactures cassettes and its cost and revenue functions for a week are $C=300+\frac{3}{2} x$ and $R=2 x$ respectively, where $x$ is the number of
cassettes produced and sold in a week. How many
cassettes must be sold for the company to realize a profit?
13. A solution is to be kept between $68 o F$ and $77 o F$.

What is the range in temperature in degree Celsius
(C) if the Celsius / Fahrenheit (F) conversion formula is given by $F=\frac{9}{5} C+32$ ?

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14. Show that the following system of linear equations has no solution:
$x+2 \mathrm{y} \leq 3,3 x+4 y \geq 12, x \geq 0, y \geq 1$.

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15. Solve each of the following system of equations in
R. $0<\frac{-x}{2}<3$

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16. Solve each of the following system of equations in
R.
$\frac{2 x-3}{4}-2 \geq \frac{4 x}{3}-6,2(2 x+3)<6(-2)+10$

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17. Write the solution set of inequation $\left|x+\frac{1}{x}\right|>2$.
18. Solve each of the following system of equations in R. $\frac{|x-1|-1}{|x-2|-2} \leq 0$.

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19. write the solution set of inequation: $\left|\frac{1}{x-2}\right|$ $<4, x \neq 4$.

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20. Solve each of the following system of equations in
$R \cdot|x-1|+|x-2|+|x-3| \geq 6$

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21. Solve each of the following system of equations in
R. $|x+1|+|x|>6$

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22. Solve each of the following system of equations in
R. $\frac{1}{|x|-3} \leq \frac{1}{2}$

D Watch Video Solution
23. Solve: $|x-1|+|x-2| \geq 4$
24. Solve: $\frac{|x-1|-1}{x+2}<1$.

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25. write the solution set of inequation: $\left|\frac{1}{x-2}\right|$
$<4, x \neq 4$.

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26. Solve: $\frac{|x+3|+x}{x+2}>1$
27. Solve: $\frac{|x|-1}{|x|-2} \geq 0, x \in R, x \neq \pm 2$.

- Watch Video Solution

28. Solve: $\frac{-1}{|x|-2} \geq 1$, wherex $\in R, x \neq \pm 2$.

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29. Solve each of the following system of equations in
$R \cdot 1 \leq|x-2| \leq 3$
30. Solve each of the following system of equations in $R .1 \leq|x-2| \leq 3$

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31. Solve each of the following system of equations in
R. $\frac{4}{x+1} \leq 3 \leq \frac{6}{x+1}, x>0$
(D) Watch Video Solution
32. Solve: $|x+2| \leq 5$
33. Solve the following linear inequations: $\frac{x-3}{x-5}>0$
(ii) $\frac{x-2}{x+5}>2$

- Watch Video Solution

34. Solve the following linear inequations in $R$.
$\frac{2(x+3)}{4}-3<\frac{x-4}{3}-2$

D Watch Video Solution
35. Solve the following linear inequations:
$\frac{x-3}{x-5}>0$ (ii) $\frac{x-2}{x+5}>2$

- Watch Video Solution

36. Solve the following linear inequations in $R$.
$\frac{2(x+3)}{4}-3<\frac{x-4}{3}-2$

D Watch Video Solution
37. Solve $5 x-3<3 x+1$ when (i) x is an integer, (ii)
x is a real number.
38. Solve the following equations:
$2(2 x+3)-10 \leq 6(x-2)$

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39. Solve the inequalities for real x :
$\frac{x}{4}<\frac{(5 x-2)}{3}-\frac{(7 x-3)}{5}$

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40. In the first four papers each of 100 marks, Rishi got $95,72,73,83$ marks. If he wants an average of greater than or equal to 75 marks and less than 80 marks, find the range of marks he should score in the fifth paper.

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41. Solve the following linear inequations in $R$.
$\frac{5 x}{2}+\frac{3 x}{4} \geq \frac{39}{4}$

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42. Solve the following linear inequations in $R$.
$\frac{2(x+3)}{4}-3<\frac{x-4}{3}-2$

## D Watch Video Solution

43. Solve each of the following system of equations in
$R$.

$$
1 \leq|x-2| \leq 3
$$

## D Watch Video Solution

44. Solve each of the following system of equations in
$R \cdot 1 \leq|x-2| \leq 3$
45. Solve the following linear inequation: $2 x-4=0$
A. $(-\infty, 4)$
B. $(-\infty, 2]$
C. $[2, \infty)$
D. None of these

Answer: B

# 46. Solve the following linear inequation: <br> $-3 x+12<0$ 

(D) Watch Video Solution
47. Solve the following linear inequation:
$4 x-12 \geq 0$
(D) Watch Video Solution
48. Solve the following linear inequation:
$7 x+9>30$
49. Solve the following inequation: $\frac{1}{x-2}<0$

## - Watch Video Solution

50. Solve the following inequation: $\frac{x+1}{x+2} \geq 1$

## D Watch Video Solution

51. Solve the following linear inequation in
$R: 12 x<50$, when $x \in R$
52. Solve the following linear inequation in
$R: 12 x<50$, when $x \in N$

## (D) Watch Video Solution

53. Solve the following linear inequation in
$R:-4 x>30$, when $x \in R$

## - Watch Video Solution

54. Solve the following linear inequation in

$$
R:-4 x>30, \text { when } x \in Z
$$

55. Solve the following linear inequation in
$R:-4 x>30$, when $x \in N$
(D) Watch Video Solution
56. Solve the following linear inequation in
$R: 4 x-2<8$, when $x \in R$
A. $[4, \infty)$
B. $(5 / 2, \infty)$
C. ( $-\infty, 5 / 2$ )
D. None of these

## Answer: C

## D Watch Video Solution

57. Solve the following linear inequation in
$R: 4 x-2<8$, when $x \in Z$

## D Watch Video Solution

58. Solve the following linear inequation in
$R: 4 x-2<8$, when $x \in N$

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59. Solve the following linear inequation in $R: 3 x-7>x+1$

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60. Solve the following linear inequation in
$R: 2(3-x) \geq \frac{x}{5}+4$

## - Watch Video Solution

61. Solve the following linear inequation in
$R: \frac{x}{5}<\frac{3 x-2}{4}-\frac{5 x-3}{5}$
62. Solve the following linear inequation in

$$
R: \frac{x-1}{3} \geq \frac{x-5}{5}-2
$$

A. $[20, \infty)$
B. $(20, \infty)$
C. $[-20, \infty)$
D. None of these

Answer: C

- Watch Video Solution

63. Solve the following linear inequation in
$R: \frac{4+2 x}{3} \geq \frac{x}{2}-3$

- Watch Video Solution

64. Solve the following linear inequation in
$R: \frac{6 x-5}{4 x+1}<0$

- Watch Video Solution

65. Solve the following linear inequation in
$R: \frac{1}{x-1} \leq 2$
66. Solve the following linear inequation in
$R: \frac{x}{x-5}>\frac{1}{2}$

D Watch Video Solution
67. Solve the following linear inequation in
$R: x+5>4 x-10$

D Watch Video Solution
68. Solve the following linear inequation in
$R: \frac{3 x-2}{5} \leq \frac{4 x-3}{2}$
69. Solve the following linear inequation in
$R: \frac{2 x+3}{5}-2<\frac{3(x-2)}{5}$

D Watch Video Solution
70. Solve the following linear inequation in $R: \frac{2 x-3}{3 x-7}>0$
71. Solve the following linear inequation in $R: \frac{x-1}{x+3}>2$

## - Watch Video Solution

72. Solve the following linear inequation in $R: 3 x+9 \geq-x+19$

## - Watch Video Solution

73. Solve the following linear inequation in
$R:-(x-3)+4<5-2 x$
74. Solve the following linear inequation in $R: \frac{5-2 x}{3}<\frac{x}{6}-5$

D Watch Video Solution
75. Solve the following linear inequation in
$R: x-2 \leq \frac{5 x+8}{3}$
(D) Watch Video Solution
76. Solve the following linear inequation in
$R: \frac{3}{x-2}<1$
77. Solve the following linear inequation in $R: \frac{5 x-6}{x+6}<1$

D Watch Video Solution
78. Solve $-11 \leq 4 x-3 \leq 13$

- Watch Video Solution

79. Solve each of the following system of equation in
$R: x+3>0,2 x<14$
80. Solve each of the following system of equation in
$R: 3 x-6>0,2 x-5>0$

D Watch Video Solution
81. Solve each of the following system of equation in
$R: 3 x-1 \geq 5, x+2>-1$

- Watch Video Solution

82. Solve each of the following system of equation in
$R: 2(x-6)<3 x-7,11-2 x<6-x$

## - Watch Video Solution

83. Solve each of the following system of equation in
$R: \frac{2 x+1}{7 x-1}>5, \frac{x+7}{x-8}>2$

D Watch Video Solution
84. Solve each of the following system of equation in

$$
R: 10 \leq-5(x-2)<20
$$

85. Solve each of the following system of equation in
$R: 2 x-7>5-x, 11-5 x \leq 1$

D Watch Video Solution
86. Solve each of the following system of equation in
$R: 2 x+6 \geq 0,4 x-7<0$

D Watch Video Solution
87. Solve each of the following system of equation in
$R: 2 \mathrm{x}-3<7,(2 \mathrm{x})>-4{ }^{`}$
88. Solve each of the following system of equation in
$R: 5 \mathrm{x}-1<24$ and $5 \mathrm{x}+1>-24$ `

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89. Solve each of the following system of equation in
$R: 11-5 x \succ 4,4 x+13 \leq-11$

D Watch Video Solution
90. Solve each of the following system of equation in
$R: 5 x-7>3(x+3), 1-\frac{3 x}{2} \geq x-4$

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91. Solve each of the following system of equation in
$R: \frac{7 x-1}{2}<-3, \frac{3 x+8}{5}+11<0$

- Watch Video Solution

92. Solve each of the following system of equation in
$R:-5<2 x-3<5$
93. $|3 x-2| \leq \frac{1}{2}$

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94. Solve each of the following system of equation in
$R:\left|x+\frac{1}{3}\right|>\frac{8}{3}$

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95. Solve each of the following system of equation in
$R:\left|\frac{3 x-4}{2}\right| \leq \frac{5}{12}$
96. Solve each of the following system of equation in
$R: \frac{1}{|x|-3}<\frac{1}{2}$
D Watch Video Solution
97. Solve each of the following system of equation in
$R:\left|\frac{2 x-1}{x-1}\right|>2$
D Watch Video Solution
98. Solve each of the following system of equation in
$R:|4-x|+1<3$

- Watch Video Solution

99. Solve each of the following system of equation in
$R: \frac{|x-2|}{x-2}>0$

D Watch Video Solution
100. Solve each of the following system of equation in
$R: \frac{|x+2|}{x}<2$
101. Find all pairs of consecutive odd positive integers, both of which are smaller than 18 , such that their sum is more than 20.

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102. Find all pairs of consecutive even positive integers, both of which are larger than 8, such that their sum is less than 25.
103. The cost and revenue functions of a product are
given by $\quad C(x)=2 x+400$ and $R(x)=6 x+20$
respectively, where $x$ is the number of items produced by the manufacturer. How many items the manufacturer must sell to realize some profit?

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104. IQ of a person is given by formula: IQ $=\frac{M A}{C A} \times 100$, where $M A$ is mental age and CA is chronological age. If $80 \leq I Q \leq 140$ for a group of 12
year children, find the range of their mental age.
105. Find all pairs of consecutive add positive integers both of which are smaller than 10 such that their sum is more than 11 ,

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106. Find all pairs of consecutive odd natural number,
both of which are larger than 10 , such that their sum is less than 40.
107. Find all pairs of consecutive even positive integers, both of which are larger than 5, such that their sum is less than 23.

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108. The marks scored by Rohit in two tests were 65
and 70 . Find the minimum marks the should score in
the third test to have an average of at least 65 marks.

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109. A solution is to be kept between $30^{\circ} \mathrm{C}$ and $35^{\circ} \mathrm{C}$. What is the range of temperature in degree Fahrenheit?

## D Watch Video Solution

110. To receive grade $A$ in a cource, one must obtain an average of 90 marks or more in five papers each of

100 marks. If Shikha scored 87, 95,92 and 94 marks in
first four papers find the minimum marks that she must score in the last paper to get grade A in the course.
111. The longest side of a triangle is three times the shortest side and the third side is 2 cm shorter than the longest side if the perimeter of the triangles at least 61 cm , find the minimum length of the shortest side.

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112. How may litres of water will have to be added to

1125 litres of the $45 \%$ solution of acid so that the resulting mixture will contain more than $25 \%$ but less than $30 \%$ acid content?
113. A solution of $8 \%$ boric acid is to be diluted by adding a $2 \%$ boric acid solution to it. The resulting mixture is to be more than $4 \%$ but less than $6 \%$ boric acid. If there are 640 litres of the $8 \%$ solution, how many litres of $2 \%$ solution will have to be added?

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114. The water acidity in a pool is considered normal when the average $p H$ reading of three daily measurements is between 7.2 and 7.8 . If the first two
pH reading are 7.48 and 7.85 , find the range of pH value for the third reading that will result in the acidity level being normal.

## D Watch Video Solution

115. Solve the following inequation graphically:
$2 x+3 y \leq 6$

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116. Solve the following inequation graphically:
$2 x-y \geq 1$
117. Solve the following inequation graphically: $x \geq 2$

## D Watch Video Solution

118. Solve the following inequation graphically:
$y \leq-3$

- Watch Video Solution

119. Represent to solution set of each of the following inequation graphically in two dimensional plane:
$x+2 y-y \leq 0$

## D Watch Video Solution

120. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$
x-2 y<0
$$

## - Watch Video Solution

121. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$
0 \leq 2 x-5 y+10
$$

122. Represent to solution set of each of the following inequation graphically in two dimensional plane: $-3 x+2 y \geq-6$

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123. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$
x+2 y \geq 6
$$

124. Represent to solution set of each of the following inequation graphically in two dimensional plane: $-3 x+2 y \leq 6$

## D Watch Video Solution

125. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$
3 y>6-2 x
$$

## - Watch Video Solution

126. Represent to solution set of each of the following inequation graphically in two dimensional plane:
$x+2 \geq 0$

## D Watch Video Solution

127. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$
x \leq 8-4 y
$$

## D Watch Video Solution

128. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$
y>2 x-8
$$

129. Draw the diagram $f$ the solution set of the linear inequations $3 x+4 y \geq 12, y \geq 1, x \geq 0$.

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130. Find the linear equations for which the shaded area in Fig: 15.39 is the solution set.
131. Find the linear inequations for which the shaded region in fig. 15.40 is the solution set.

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132. solve the following system of inequation by graphical method:
$2 x+3 y \leq 6,3 x+2 y \leq 6, x \geq 0, y \geq 0$

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133. Solve the following system of linear inequation graphically:
$x-y \leq 1, x+2 y \leq 8,2 x+y \geq 2, x \geq 0, y \geq 0$

## D Watch Video Solution

134. Solve the following system of linear inequation graphically:
$x+y \geq 1,7 x+9 y \leq 63, x \leq 6, y \leq 5, x \geq 0, y \geq 0$

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135. Solve the following system of linear inequation graphically:
$2 x+3 y \leq 35, y \geq 3, x \geq 2, x \geq 0, y \geq 0$
136. Solve the following system of linear inequation graphically:
$2 x+3 y \leq 6, x+4 y \leq 4, x \geq 0, y \geq 0$

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137. Show that the solution set of the following linear inequations is empty $s$-2ygeq $0, \backslash 2 x$-ylte- $2, \backslash$ xgeq0, $\backslash$ ygeq0` 138. Show that the solution set of the following linear inequations is empty set: \(\mathrm{It}=3, \backslash 3 \mathrm{x}+4 \mathrm{yg}\) eq 12 , \(\backslash\) ygeq \(1, \backslash\) xgeq0,\ ygeq0`

## D Watch Video Solution

139. Find the linear inequations for which the shaded area in fig. 15.41 is the solution set. Draw the diagram of the solution set of the linear inequations.

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140. Find the linear inequations for which the solution set is the shaded region given in fig. 15.42.

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141. Solve the following systems of inequation graphically: $x+y g e q 8, \backslash x+2 y g e q 8, \backslash x+y l t=6^{`}$

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142. Solve the following systems of inequation graphically: $2 \mathrm{x}+12$ ylt=840 ,\ $3 x+6 y \mid t=300, \backslash$ $8 x+4 y \mid t=480 \backslash x g e q 0, \backslash$ ygeq0`
143. Solve the following systems of inequation graphically: +2ylt=40, , $3 x+y g e q 30, \backslash 4 x+3 y g e q 60, \$ xgeqO, ${ }^{\text {ygeq0` }}$

## (D) Watch Video Solution

144. Solve the following systems of inequation graphically:

$$
+y \geq 10,2 x+2 y \geq 12, x+4 y \geq 12, x \geq 0, y \geq 0
$$

145. Show that the solution set of the following system of linear inequalities in an unbounded regioygeq $8, \backslash x+2 y g e q 10, \backslash x g e q 0, \backslash$ ygeq0.

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146. Write the following set of the inequation $\frac{x^{2}}{x-2}>0$.

- Watch Video Solution

147. Write the solution set of the inequation
$x+\frac{1}{x} \geq 2$.
148. Write the solution set of the equation $|2-x|=x-2$.

## D Watch Video Solution

149. Writhe the set of values of $x$ satisfying $|x-1| \leq 3$ and $|x-1| \leq 1$.
150. The number of integral solutions of $\frac{x+2}{x^{2}+1}>\frac{1}{2}$ is 42.53 .34 .25 .6

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151. Write the solution set of the inequation $|x-1| \geq|x-3|$.

## - Watch Video Solution

152. If $<7$ then $x<-7$ b. $x \leq 7$ c. $x \succ 7$ d.
$x \geq-7$
153. If $-3 x+17<-13$, then $x \in(10, \infty)$ b.
$x \in[10, \infty)$ c. $x \in(-\infty, 10]$ d. $x \in[-10,10)$

## D Watch Video Solution

154. Given that $x, y$ and $b$ are real numbers and ${ }^{`} x<>0$ thenx/by/bd. $\mathrm{x} / \mathrm{bgeq} \mathrm{y} / \mathrm{b}$ `

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155. If $x$ is a real number and $|x|<5$, then $x \geq 5 \mathrm{~b}$.

## - Watch Video Solution

156. If $x$ and $a$ are real numbers such that $a>0$ and $|x|>a$, then $x \in(-a, \infty)$ b. $x \in[-\infty, a)$ c. $x \in(-a, a)$ d. $x \in(-\infty,-a) \cup(a, \infty)$

## - Watch Video Solution

157. If $|x-1|>5$, then a. $x \in(-4,6)$ b.
$x \in[-4,6] \quad$ c. $\quad x \in(-\infty,-4) \cup(6, \infty) \quad$ d.
$x \in(-\infty,-4) \cup[6, \infty)$
158. If $|x+2| \leq 9 \quad$ then $\quad x \in(-7,11) \quad$ b.
$x \in[-11,7] \quad$ c. $\quad x \in(-\infty, 7) \cup(11, \infty) \quad$ d.
$x \in(-\infty,-7) \cup[11, \infty)$

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159. The inequality representing the following graph is $|x|<3 \mathrm{~b} .|x| \leq 3 \mathrm{c} .|x|>3 \mathrm{~d} .|x| \geq 3$

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160. The linear inequality representing the solution set given in gig. 15.44 is a. $|x|<5$ b. $|x|>5$ c.
$|x| \geq 5 \mathrm{~d} .|x| \leq 5$

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161. The solution set of the inequation $|x+2| \leq 5$ is
$(-7,5)$ b. $[-7,3]$ c. $[-5,5]$ d. $(-7,3)$

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162. If $|x+3| \geq 10$, then $x \in(-13,7] \quad \mathrm{b}$.

$$
\begin{aligned}
& x \in(-\infty,-13) \cup(7, \infty) \quad \text { c. } \quad x \in(-13,7) \quad \text { d. } \\
& x \in(-\infty,-13] \cup[7, \infty)
\end{aligned}
$$

163. If $\frac{|x-2|}{x-2} \geq 0$, then $x \in[2, \infty)$ b. $x \in(2, \infty)$ c. $x \in(-\infty, 2)$ d. $x \in(-\infty, 2]$

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