

MATHS

BOOKS - RD SHARMA MATHS (HINGLISH)

LINEAR INEQUATIONS

Solved Examples And Exercises

1. Show that the solution set of the following linear inequations is an unbounded set:

$$x + y \ge 9, 3x + y \ge 12, x \ge 0, y \ge 0.$$



2. Solve the following inequations grapihically:

- $(i)|x| \leq 3$
- (ii) $|y-x| \leq 3$
 - **Watch Video Solution**

3. Exhibit graphically the solution set of the linear inequations

 $x + y \le 5, 4x + y \ge 4, x + 5y \ge 5, x \le 4, y \le 3$



$$R \cdot x + 5 > 2(x+1), 2-x < 3(x+2),$$



Watch Video Solution

5. Solve the following linear inequations: $\frac{x-3}{x-5}>0$

$$\text{(ii) } \frac{x-2}{x+5} > 2$$



Watch Video Solution

6. Solve: $5 \leq \frac{2-3x}{4} \leq 9$

A. [-6,11]

D. None of these

Answer: D



Watch Video Solution

7. Solve the following system of linear inequations

$$2(2x+3)-10<6(x-2)$$

$$\frac{2x-3}{4} + 6 \le 2 + \frac{4x}{3}$$



$$\frac{5x}{2}+\frac{3x}{4}\geq\frac{39}{4}$$



Watch Video Solution

9. Solve the following system of linear inequations:

$$3x - 6 > 0$$
, $4x - 10 < 6$



Watch Video Solution

10. Solve the following linear inequations in R-

$$\frac{7x-5}{8x+3}<4$$



$$\frac{5x+8}{4-x}<2$$



Watch Video Solution

12. A company manufactures cassettes and its cost and revenue functions for a week are $C=300+\frac{3}{2}x$ and R=2x respectively, where x is the number of cassettes produced and sold in a week. How many cassettes must be sold for the company to realize a profit?

13. A solution is to be kept between 68oF and 77oF .

What is the range in temperature in degree Celsius (C) if the Celsius / Fahrenheit (F) conversion formula is given by $F=rac{9}{5}C+32$?



Watch Video Solution

14. Show that the following system of linear equations has no solution:

$$x + 2y \le 3, 3x + 4y \ge 12, x \ge 0, y \ge 1.$$



$$R\cdot 0<rac{-x}{2}<3$$



Watch Video Solution

16. Solve each of the following system of equations in

R

$$\frac{2x-3}{4}-2 \geq \frac{4x}{3}-6, 2(2x+3) < 6(-2)+10$$



17. Write the solution set of inequation $\left|x+\frac{1}{x}\right|>2$.



$$R\cdotrac{|x-1|-1}{|x-2|-2}\leq 0.$$



19. write the solution set of inequation: $\left| \frac{1}{x-2} \right|$ < 4, x
eq 4.



20. Solve each of the following system of equations in

$$|R \cdot |x-1| + |x-2| + |x-3| \ge 6$$

$$R \cdot |x+1| + |x| > 6$$



22. Solve each of the following system of equations in

$$R \cdot rac{1}{|x|-3} \leq rac{1}{2}$$



24. Solve:
$$\frac{|x-1|-1}{x+2} < 1$$
.



Watch Video Solution

 $< 4, x \neq 4.$

25. write the solution set of inequation: $\left| \frac{1}{x-2} \right|$

26. Solve: $\frac{|x+3|+x}{x+2} > 1$

27. Solve:
$$\dfrac{|x|-1}{|x|-2}\geq 0, x\in R, x
eq \pm 2.$$



28. Solve:
$$\dfrac{-1}{|x|-2} \geq 1, where x \in R, x
eq \pm 2.$$



$$R \cdot 1 < |x - 2| < 3$$



$$R \cdot 1 \leq |x-2| \leq 3$$



Watch Video Solution

31. Solve each of the following system of equations in

$$R\cdotrac{4}{x+1}\leq 3\leqrac{6}{x+1}, x>0$$



Watch Video Solution

32. Solve: $|x + 2| \le 5$



33. Solve the following linear inequations: $\dfrac{x-3}{x-5}>0$

$$: \frac{x-5}{x-5} > 0$$

(ii) $rac{x-2}{x+5}>2$



Watch Video Solution

34. Solve the following linear inequations in R.

$$\frac{2(x+3)}{4}-3<\frac{x-4}{3}-2$$



$$rac{x-3}{x-5}>0$$
 (ii) $rac{x-2}{x+5}>2$



Watch Video Solution

36. Solve the following linear inequations in R.

$$\frac{2(x+3)}{4} - 3 < \frac{x-4}{3} - 2$$



Watch Video Solution

37. Solve 5x-3<3x+1 when (i) x is an integer, (ii)

x is a real number.



38. Solve the following equations:

$$2(2x+3)-10 \le 6(x-2)$$



39. Solve the inequalities for real x :

$$\frac{x}{4} < \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$$



40. In the first four papers each of 100 marks, Rishi got 95, 72, 73, 83 marks. If he wants an average of greater than or equal to 75 marks and less than 80 marks, find the range of marks he should score in the fifth paper.



Watch Video Solution

41. Solve the following linear inequations in R-

$$\frac{5x}{2} + \frac{3x}{4} \ge \frac{39}{4}$$



$$\frac{2(x+3)}{4} - 3 < \frac{x-4}{3} - 2$$



Watch Video Solution

43. Solve each of the following system of equations in

R.

$$1 \le |x - 2| \le 3$$



Watch Video Solution

44. Solve each of the following system of equations in

$$R$$
· $1 \leq |x-2| \leq 3$

A.
$$(-\infty,4)$$

B.
$$(-\infty,2]$$

D. None of these

Answer: B



$$-3x + 12 < 0$$



47. Solve the following linear inequation:

$$4x - 12 \ge 0$$



48. Solve the following linear inequation:

$$7x + 9 > 30$$



49. Solve the following inequation: $\dfrac{1}{x-2} < 0$



Watch Video Solution

50. Solve the following inequation: $\dfrac{x+1}{x+2} \geq 1$



Watch Video Solution

51. Solve the following linear inequation in

 $R\colon\ 12x<50,\ when\ x\in R$



 $R\colon\ 12x<50,\ when\ x\in N$



53. Solve the following linear inequation in

 $R\colon -4x > 30, \ when \ x \in R$



54. Solve the following linear inequation in

 $R\colon -4x > 30, \ when \ x \in Z$



 $R\colon -4x > 30, \ when \ x \in N$



Watch Video Solution

56. Solve the following linear inequation in

 $R \colon 4x - 2 < 8, \ when \ x \in R$

A. [4,∞)

B. (5/2,∞)

C. $(-\infty, 5/2)$

D. None of these

Answer: C



Watch Video Solution

57. Solve the following linear inequation in

 $R \colon 4x - 2 < 8, \ when \ x \in Z$



Watch Video Solution

58. Solve the following linear inequation in

 $R: 4x - 2 < 8, when x \in N$



$$R: 3x - 7 > x + 1$$



Watch Video Solution

60. Solve the following linear inequation in

$$R\!:\!2(3-x)\geq rac{x}{5}+4$$



61. Solve the following linear inequation in

$$R \colon \frac{x}{5} < \frac{3x-2}{4} - \frac{5x-3}{5}$$



$$R\colon \frac{x-1}{3} \geq \frac{x-5}{5} - 2$$

- A. [20,∞)
- B. (20,∞)
- C. [-20,∞)
- D. None of these

Answer: C



$$R\colon \frac{4+2x}{3} \geq \frac{x}{2}-3$$



64. Solve the following linear inequation in $R : \frac{6x-5}{4x+1} < 0$



65. Solve the following linear inequation in $R \colon \frac{1}{x-1} \le 2$



66. Solve the following linear inequation in $R: \frac{x}{x-5} > \frac{1}{2}$



Watch Video Solution

67. Solve the following linear inequation in

$$R: x + 5 > 4x - 10$$



68. Solve the following linear inequation in $R\colon \frac{3x-2}{5}\,\leq\,\frac{4x-3}{2}$

69. Solve the following linear inequation in
$$R\colon \frac{2x+3}{5} - 2 < \frac{3(x-2)}{5}$$



$$R: \frac{2x-3}{3x-7} > 0$$



71. Solve the following linear inequation in $R\colon \frac{x-1}{x+3} > 2$



Watch Video Solution

72. Solve the following linear inequation in

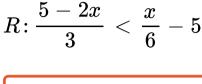
$$R: 3x + 9 > -x + 19$$



73. Solve the following linear inequation in

$$R: -(x-3)+4 < 5-2x$$







75. Solve the following linear inequation in $R\colon x-2 \leq \frac{5x+8}{3}$



76. Solve the following linear inequation in $R \colon \frac{3}{x-2} < 1$

77. Solve the following linear inequation in $R \colon \frac{5x-6}{x+6} < 1$



78. Solve $-11 \le 4x - 3 \le 13$



 $R: x + 3 > 0, \ 2x < 14$

79. Solve each of the following system of equation in

$$R:3x-6>0,\ 2x-5>0$$



81. Solve each of the following system of equation in

$$R: 3x - 1 \ge 5, \ x + 2 > -1$$



$$R: 2(x-6) < 3x-7, \ 11-2x < 6-x$$



Watch Video Solution

83. Solve each of the following system of equation in

$$R: \frac{2x+1}{7x-1} > 5, \frac{x+7}{x-8} > 2$$



84. Solve each of the following system of equation in

$$R: 10 \leq -5(x-2) < 20$$

$$R: 2x - 7 > 5 - x, \ 11 - 5x \le 1$$



Watch Video Solution

86. Solve each of the following system of equation in

$$R: 2x + 6 \ge 0, \ 4x - 7 < 0$$



Watch Video Solution

87. Solve each of the following system of equation in

R: 2x-3 < 7, (2x)>-4

R: 5x-1 < 24 and 5x+1 > -24



89. Solve each of the following system of equation in

 $R: 11 - 5x > 4, \ 4x + 13 \le -11$



90. Solve each of the following system of equation in

$$R:5x-7>3(x+3),\ 1-rac{3x}{2}\geq x-4$$



Watch Video Solution

91. Solve each of the following system of equation in

$$R \colon \frac{7x-1}{2} < -3, \frac{3x+8}{5} + 11 < 0$$



92. Solve each of the following system of equation in

$$R \colon -5 < 2x - 3 < 5$$



93.
$$|3x-2| \leq \frac{1}{2}$$



Watch Video Solution

94. Solve each of the following system of equation in

$$R: \left| x + \frac{1}{3} \right| > \frac{8}{3}$$



95. Solve each of the following system of equation in

$$R: \left| \frac{3x-4}{2} \right| \leq \frac{5}{12}$$



....

96. Solve each of the following system of equation in

$$R\colon \frac{1}{|x|-3}<\frac{1}{2}$$



Watch Video Solution

97. Solve each of the following system of equation in

$$R: \left| \frac{2x-1}{x-1} \right| > 2$$



98. Solve each of the following system of equation in

$$R: |4-x|+1 < 3$$



Watch Video Solution

99. Solve each of the following system of equation in

$$R: \frac{|x-2|}{x-2} > 0$$



100. Solve each of the following system of equation in

$$R \colon \frac{|x+2|}{r} < 2$$



Match Video Colution

watch video Solution

101. Find all pairs of consecutive odd positive integers, both of which are smaller than 18, such that their sum is more than 20.



Watch Video Solution

102. Find all pairs of consecutive even positive integers, both of which are larger than 8, such that their sum is less than 25.



103. The cost and revenue functions of a product are given by $C(x)=2x+400\ and\ R(x)=6x+20$ respectively, where x is the number of items produced by the manufacturer. How many items the manufacturer must sell to realize some profit?



Watch Video Solution

104. IQ of a person is given by formula: IQ $=\frac{MA}{CA}\times 100\,,\; where\; MA \text{ is mental age and CA is}$ chronological age. If $80\leq IQ\leq 140$ for a group of 12 year children, find the range of their mental age.



105. Find all pairs of consecutive add positive integers both of which are smaller than 10 such that their sum is more than 11,



Watch Video Solution

106. Find all pairs of consecutive odd natural number, both of which are larger than 10, such that their sum is less than 40.



107. Find all pairs of consecutive even positive integers, both of which are larger than 5, such that their sum is less than 23.



Watch Video Solution

108. The marks scored by Rohit in two tests were 65 and 70. Find the minimum marks the should score in the third test to have an average of at least 65 marks.



109. A solution is to be kept between $30^{0}C\ and\ 35^{0}C$. What is the range of temperature in degree Fahrenheit?



Watch Video Solution

110. To receive grade A in a cource, one must obtain an average of 90 marks or more in five papers each of 100 marks. If Shikha scored 87, 95, 92 and 94 marks in first four papers find the minimum marks that she must score in the last paper to get grade A in the course.



111. The longest side of a triangle is three times the shortest side and the third side is 2 cm shorter than the longest side if the perimeter of the triangles at least 61 cm, find the minimum length of the shortest side.



Watch Video Solution

112. How may litres of water will have to be added to 1125 litres of the $45\,\%$ solution of acid so that the resulting mixture will contain more than $25\,\%$ but less than $30\,\%$ acid content?

113. A solution of 8% boric acid is to be diluted by adding a 2% boric acid solution to it. The resulting mixture is to be more than 4% but less than 6% boric acid. If there are 640 litres of the 8% solution, how many litres of 2% solution will have to be added?



114. The water acidity in a pool is considered normal when the average pH reading of three daily measurements is between 7.2 and 7.8. If the first two

pH reading are 7.48 and 7.85, find the range of pH value for the third reading that will result in the acidity level being normal.

115. Solve the following inequation graphically:



 $2x+3y\leq 6$

116. Solve the following inequation graphically:

$$2x - y \ge 1$$



• Watch video Solution

117. Solve the following inequation graphically: $x \geq 2$



Watch Video Solution

118. Solve the following inequation graphically:

$$y \leq -3$$



Watch Video Solution

119. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$x + 2y - y \le 0$$



Watch Video Solution

120. Represent to solution set of each of the following inequation graphically in two dimensional plane:



x - 2y < 0



Watch Video Solution

121. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$0 \le 2x - 5y + 10$$



Watch Video Calution

• watch video solution

122. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$-3x + 2y \ge -6$$



123. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$x + 2y \ge 6$$



124. Represent to solution set of each of the following inequation graphically in two dimensional plane: $-3x + 2y \le 6$



Watch Video Solution

125. Represent to solution set of each of the following inequation graphically in two dimensional plane: 3y>6-2x



Watch Video Solution

126. Represent to solution set of each of the following inequation graphically in two dimensional plane:



Watch Video Solution

127. Represent to solution set of each of the following inequation graphically in two dimensional plane:

$$x \leq 8 - 4y$$



Watch Video Solution

128. Represent to solution set of each of the following inequation graphically in two dimensional plane: y > 2x - 8



Watch video Solution

129. Draw the diagram f the solution set of the linear inequations $3x + 4y \ge 12, \ y \ge 1, \ x \ge 0.$



Watch Video Solution

130. Find the linear equations for which the shaded area in Fig: 15.39 is the solution set.



131. Find the linear inequations for which the shaded region in fig. 15.40 is the solution set.



Watch Video Solution

132. solve the following system of inequation by graphical method:

$$2x + 3y \le 6, 3x + 2y \le 6, x \ge 0, y \ge 0$$



Watch Video Solution

133. Solve the following system of linear inequation graphically:



134. Solve the following system of linear inequation graphically: $x+y\geq 1,\ 7x+9y\leq 63,\ x\leq 6,\ y\leq 5,\ x\geq 0,\ y\geq 0$



graphically:

135. Solve the following system of linear inequation

 $2x + 3y \le 35, y \ge 3, x \ge 2, x \ge 0, y \ge 0$

• watch video solution

136. Solve the following system of linear inequation graphically:

$$2x + 3y \le 6$$
, $x + 4y \le 4$, $x \ge 0$, $y \ge 0$



137. Show that the solution set of the following linear inequations is empty s-2ygeq0,\ 2x-ylt=-2,\ xgeq0,\ ygeq0`



138. Show that the solution set of the following linear inequations is empty set: lt=3,\ 3x+4ygeq12,\ ygeq1,\ xgeq0,\ ygeq0



Watch Video Solution

139. Find the linear inequations for which the shaded area in fig. 15.41 is the solution set. Draw the diagram of the solution set of the linear inequations.



Watch Video Solution

140. Find the linear inequations for which the solution set is the shaded region given in fig. 15.42.

141. Solve the following systems of inequation graphically: x+ygeq8, x+2ygeq8, x+ylt=6



142. Solve the following systems of inequation graphically: 2 x+12 ylt=840 ,\ 3x+6ylt=300 ,\ $8x+4ylt=480\ xgeq0$,\ ygeq0`



143. Solve the following systems of inequation graphically: +2ylt=40, 3x+ygeq30, 4x+3ygeq60,



xgeq0,\ygeq0`

144. Solve the following systems of inequation graphically:

+y > 10, 2x + 2y > 12, x + 4y > 12, x > 0, y > 0

145. Show that the solution set of the following system of linear inequalities in an unbounded regioygeq8,\ x+2ygeq10 ,\ xgeq0,\ ygeq0.`



Watch Video Solution

146. Write the following set of the inequation $\frac{x^2}{x-2} > 0.$



Watch Video Solution

147. Write the solution set of the inequation $x+rac{1}{x}\geq 2.$

148. Write the solution set of the equation |2-x|=x-2.



149. Writhe the set of values of x satisfying $|x-1| \leq 3$ and $|x-1| \leq 1$.

150. The number of integral solutions of $rac{x+2}{x^2+1} > rac{1}{2}$ is 4 2. 5 3. 3 4. 2 5. 6



Watch Video Solution

151. Write the solution set of the inequation |x-1| > |x-3|



Watch Video Solution

152. If < 7 then x < -7 b. x < 7 c. x > 7 d.

$$x > -7$$



153. If $-3x+17 < -13, \ then \ x \in (10,\infty)$ b. $x \in [10,\infty)$ c. $x \in (-\infty,\ 10]$ d. $x \in [-10,10)$



Watch Video Solution

154. Given that $x, y \ and \ b$ are real numbers and `x<>0 thenx/b y/bd. x/bgeqy/b`



Watch Video Solution

155. If x is a real number and |x| < 5, then $x \geq 5$ b.

156. If $x\ and\ a$ are real numbers such that a>0 and

$$|x|>a,$$
 then $x\in (-a,\infty)$ b. $x\in [-\infty,a)$ c.

$$x\in (\,-a,a)$$
 d. $x\in (\,-\infty,\,\,-a)\cup (a,\infty)$



157. If
$$|x-1| > 5$$
, then a. $x \in (-4,6)$ b.

$$x \in [-4,6]$$
 c. $x \in (-\infty,-4) \cup (6,\infty)$ d.

$$x \in (-\infty, -4) \cup [6, \infty)$$

158. If $|x+2| \le 9$ then $x \in (-7, 11)$ b.

$$x \in [\,-\,11,7]$$
 c. $x \in (\,-\infty,7) \cup (11,\infty)$ d.

$$x \in (-\infty, -7) \cup [11, \infty)$$



159. The inequality representing the following graph is |x| < 3 b. $|x| \le 3$ c. |x| > 3 d. $|x| \ge 3$



160. The linear inequality representing the solution set given in gig. 15.44 is a. |x| < 5 b. |x| > 5 c.

$$|x| \geq 5$$
 d. $|x| \leq 5$



161. The solution set of the inequation $|x+2| \leq 5$ is (-7,5) b. [-7,3] c. [-5,5] d. (-7,3)



162. If $|x+3|\geq 10,$ then $x\in (-13,\ 7]$ b. $x\in (-\infty,\ -13)\cup (7,\infty)$ c. $x\in (-13,7)$ d. $x\in (-\infty,\ -13]\cup [7,\infty)$

163. If $\dfrac{|x-2|}{x-2} \geq 0$, then $x \in [2,\infty)$ b. $x \in (2,\infty)$ c.

$$x\in (-\infty,2)$$
 d. $x\in (-\infty,2]$

