



## MATHS

### BOOKS - RD SHARMA MATHS (HINGLISH)

#### TRIGONOMETRIC RATIOS OF COMPOUND ANGLES

##### Solved Examples And Exercises

1. If angle  $\theta$  is divided into two parts such that the tangents of one part is  $\lambda$  times the tangent of other, and  $\phi$  is their difference, then show that

$$\sin \theta = \frac{\lambda + 1}{\lambda - 1} \sin \phi .$$

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2. If  $\tan \alpha = \frac{1}{1 + 2^{-x}}$  and  $\tan \beta = \frac{1}{1 + 2^{x+1}}$ , then write the value of  $\alpha + \beta$  lying in the interval  $(0, \pi/2)$ .



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3. If  $\alpha$  and  $\beta$  are acute angles such that  $\tan \alpha = \frac{m}{m+1}$  and  $\tan \beta = \frac{1}{2m+1}$ , prove that  $\alpha + \beta = \frac{\pi}{4}$ .



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4. Find  $a$  and  $b$  such that the following inequality holds good for all  $\theta$ .

$$a \leq 3 \cos \theta + 5 \sin \left( \theta - \frac{\pi}{6} \right) \leq b$$



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5. Prove that  $(2\sqrt{3} + 3)\sin \theta + 2\sqrt{3}\cos \theta$  lies between  $-(2\sqrt{3} + \sqrt{15})$  and  $(2\sqrt{3} + \sqrt{15})$ ,



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6. Prove that:  $\frac{\sin(x + \theta)}{\sin(x + \phi)} = \cos(\theta - \phi) + \cot(x + \phi)\sin(\theta - \phi)$ .

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7. It  $\cos(\alpha + \beta) = \frac{4}{5}$ ,  $\sin(\alpha - \beta) = \frac{5}{13}$  and  $\alpha, \beta$  lie between 0 and  $\frac{\pi}{4}$ ,  
prove that  $\tan 2\alpha = \frac{56}{33}$

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8. If  $\tan A - \tan B = x$  and  $\cot B - \cot A = y$ , prove that  
 $\cot(A - B) = \frac{1}{x} + \frac{1}{y}$

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9. If  $\cos(\alpha - \beta) + \cos(\beta - \gamma) + \cos(\gamma - \alpha) = -\frac{3}{2}$ , prove that  
 $\cos \alpha + \cos \beta + \cos \gamma = \sin \alpha + \sin \beta + \sin \gamma = 0$

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10. If  $\sin B = 3 \sin(2A + B)$ , prove that  $2 \tan A + \tan(A + B) = 0$ .

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11. If  $2 \tan \beta + \cot \beta = \tan \alpha$ , prove that  $\cot \beta = 2 \tan(\alpha - \beta)$ .

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12. If the system of linear equations  $x = cy + bx$ ,  $y = ax + cz$ ,  
 $z = bx + ay$  has a non trivial solution show that  
 $a^2 + b^2 + c^2 + 2abc = 1$

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13. Prove that:  $\tan 3A \tan 2A \tan A = \tan 3A - \tan 2A - \tan A$   
 $\cot A \cot 2A - \cot 2A \cot 3A - \cot 3A \cot A = 1$



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14. Prove that:  $\sin^2\left(\frac{\pi}{8} + \frac{A}{2}\right) - \sin^2\left(\frac{\pi}{8} - \frac{A}{2}\right) = \frac{1}{\sqrt{2}}\sin A$

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15. Prove that:

$$\sin^2 A = \cos^2(A - B) + \cos^2 B - 2 \cos(A - B)\cos A \cos B.$$

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16. If  $3\tan A \tan B = 1$ , prove that  $2 \cos(A + B) = \cos(A - B)$ .

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17. Find :  $\tan 75^\circ + \cot 75^\circ =$

A. 1

B. 2

C. 3

D. 4

**Answer: D**



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**18.** If  $\alpha$  and  $\beta$  are the solutions of  $a \cos \theta + b \sin \theta = c$ , then show that

$$\cos(\alpha + \beta) = \frac{a^2 - b^2}{a^2 + b^2} \quad \text{(ii) } \cos(\alpha - \beta) = \frac{2c^2 - (a^2 + b^2)}{a^2 + b^2}$$



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**19.** If  $\alpha$  and  $\beta$  are the solutions of the equation  $a \tan \theta + b \sec \theta = c$ , then

$$\text{show that } \tan(\alpha + \beta) = \frac{2ac}{a^2 - c^2}$$



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20. If  $\frac{\sin(x+y)}{\sin(x-y)} = \frac{a+b}{a-b}$ , show that  $\frac{\tan x}{\tan y} = \frac{a}{b}$ .



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21. If  $\tan(\pi/4 + \theta) + \tan(\pi/4 - \theta) = a$ , then

$\tan^2(\pi/4 + \theta) + \tan^2(\pi/4 - \theta) =$  (a)  $a^2 + 1$  (b)  $a^2 + 2$  (c)  $a^2 - 2$  (d)

none of these



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22. If  $\tan x + \tan\left(x + \frac{\pi}{3}\right) + \tan\left(x + \frac{2\pi}{3}\right) = 3$ , then prove that

$$\frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x} = 1.$$



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23. If  $\theta$  lies in the first quadrant and  $\cos \theta = \frac{8}{17}$ , then prove that

$$\cos\left(\frac{\pi}{6} + \theta\right) + \cos\left(\frac{\pi}{4} - \theta\right) + \cos\left(\frac{2\pi}{3} - \theta\right) = \left(\frac{\sqrt{3}-1}{2} + \frac{1}{\sqrt{2}}\right) \frac{23}{17}$$



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24. If  $\tan(A - B) = 1$ ,  $\sec(A + B) = \frac{2}{\sqrt{3}}$ , then the smallest positive value of  $B$  is.  $\frac{25\pi}{24}$  (b)  $\frac{19\pi}{24}$  (c)  $\frac{13\pi}{24}$  (d)  $\frac{11\pi}{24}$

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25. If  $\tan\beta = \frac{n \sin \alpha \cos \alpha}{1 - n \sin^2 \alpha}$ , show that  $\tan(\alpha - \beta) = (1 - n)\tan\alpha$ .

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26. If  $A + B = \frac{\pi}{4}$ , prove that:  $(1 + \tan A)(1 + \tan B) = 2$   
 $(\cot A - 1)(\cot B - 1) = 2$

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27. Prove that:  $\cot \theta \cot 2\theta + \cot 2\theta \cot 3\theta + 2 = \cot \theta(\cot \theta - \cot 3\theta)$

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28. If  $\tan(\alpha + \theta) = n \tan(\alpha - \theta)$  , show that  
 $(n + 1)\sin 2\theta = (n - 1)\sin 2\alpha$ .

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29. Prove that:  $\frac{\sin(B - C)}{\cos B \cos C} + \frac{\sin(C - A)}{\cos C \cos A} + \frac{\sin(A - B)}{\cos A \cos B} = 0$

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30. If  $\tan(\pi \cos \theta) = \cot(\pi \sin \theta)$  then  $\sin\left(\theta + \frac{\pi}{4}\right)$  equals

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31. Find the values of the following: (i)  $\sin 75^\circ$  (ii)  $\cos 75^\circ$  (iii)  $\sin 15^\circ$  (iv)  
 $\cos 15^\circ$

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32. If  $\cot \alpha = \frac{1}{2}$ ,  $\sec \beta = -\frac{5}{3}$ , where  $\pi < \alpha < \frac{3\pi}{2}$  and  $\frac{\pi}{2} < \beta < \pi$ . find the value of  $\alpha + \beta$  terminates

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33. If  $\sin A = \frac{3}{5}$ ,  $0 < A < \frac{\pi}{2}$  and  $\cos B = \frac{-12}{13}$ ,  $0 < B < \frac{3\pi}{2}$ , find the following  $\sin(A - B)$  (ii)  $\cos(A + B)$  (iii)  $\tan(A - B)$

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34. Prove that:  $\frac{\sin x}{\cos 3x} + \frac{\sin 3x}{\cos 9x} + \frac{\sin 9x}{\cos 27x} = \left(\frac{1}{2}\right)(\tan 27x - \tan x)$

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35. Prove that:  $\frac{1}{\cos(x - a)\cos(x - b)} = \frac{\tan(x - b) - \tan(x - a)}{\sin(a - b)}$

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36. If  $\sin(\pi \cos \theta) = \cos(\pi \sin \theta)$ , then  $\sin 2\theta =$

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37. If  $a \tan \alpha + b \tan \beta = (a + b) \tan\left(\frac{\alpha + \beta}{2}\right)$ , where  $\alpha \neq \beta$ , prove that  $a \cos \beta = b \cos \alpha$ .

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38. Prove that: 
$$\frac{1}{\sin(x - a)\sin(x - b)} = \frac{\cot(x - a) - \cot(x - b)}{\sin(a - b)}$$

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39. If  $\tan \theta = \frac{1}{2}$  and  $\tan \varphi = \frac{1}{3}$ , then the value of  $\theta + \varphi$  is  $\frac{\pi}{6}$  (b)  $\pi$  (c) 0  
(d)  $\frac{\pi}{4}$

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40. If  $\tan \theta = \frac{\sin \alpha - \cos \alpha}{\sin \alpha + \cos \alpha}$  then show that  $\sin \alpha + \cos \alpha = \sqrt{2} \cos \theta$ .

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41. Prove that:  $\frac{1}{\sin(x-a)\cos(x-b)} = \frac{\cot(x-a) + \tan(x-b)}{\cos(a-b)}$

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42. Find the maximum and minimum values of the following expressions.

(i)  $3 \cos \theta + 5 \sin\left(\theta - \frac{\pi}{6}\right)$  (ii)  $4 \sin \theta - 3 \cos \theta + 7$

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43. If  $\sin A = \frac{3}{5}$  and  $\cos B = \frac{9}{41}$ ,  $0 < A < \frac{\pi}{2}$  and  $0 < B < \frac{\pi}{2}$  then

find the values of

(i)  $\sin(A+B)$  (ii)  $\sin(A-B)$  (iii)  $\cos(A+B)$  (iv)  $\cos(A-B)$



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44. If  $\cos A = \frac{4}{5}$ ,  $\cos B = \frac{12}{13}$  and  $\frac{3\pi}{2} < A, B < 2\pi$  then find the value of  $\cos(A + B)$



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45. Find the values of the following:  $\tan 15^\circ$  ii.  $\tan 75^\circ$



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46. Find the values of the following:  $\frac{\tan(13\pi)}{12}$



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47. Evaluate the following:  $\frac{\sin(7\pi)}{12} \frac{\cos \pi}{4} - \frac{\cos(7\pi)}{12} \frac{\sin \pi}{4}$



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48. Evaluate the following:  $\frac{\cos(2\pi)}{3} \frac{\cos \pi}{4} - \frac{\sin(2\pi)}{3} \frac{\sin \pi}{4}$

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49. Prove that:

$$\cos\left(\frac{\pi}{4} - A\right)\cos\left(\frac{\pi}{4} - B\right) - \sin\left(\frac{\pi}{4} - A\right)\sin\left(\frac{\pi}{4} - B\right) = \sin(A + B)$$

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50. Prove that:

$$\sin(n + 1)A \sin(n + 2)A + \cos(n + 1)A \cos(n + 2)A = \cos A$$

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51. Prove that:  $\cos\left(\frac{\pi}{4} + x\right) + \cos\left(\frac{\pi}{4} - x\right) = \sqrt{2} \cos x$

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52. Prove that:  $\cos\left(\frac{3\pi}{4} + x\right) - \cos\left(\frac{3\pi}{4} - x\right) = \sqrt{2} \sin x$

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53. Prove that:  $\frac{\sin(x + y)}{\sin(x - y)} = \frac{\tan x + \tan y}{\tan x - \tan y}$

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54. Prove that  $\frac{\tan\left(\frac{\pi}{4} + x\right)}{\tan\left(\frac{\pi}{4} - x\right)} = \left(\frac{1 + \tan x}{1 - \tan x}\right)^2$

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55. if  $\tan \alpha = \frac{1}{\sqrt{x(x^2 + x + 1)}}$ ,  $\tan \beta = \frac{\sqrt{x}}{\sqrt{x^2 + x + 1}}$  and  $\tan \gamma = \sqrt{x^{-3} + x^{-2} + x^{-1}}$  then  $\alpha + \beta =$

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56. Prove that :  $\frac{\tan(A + B)}{\cot(A - B)} = \frac{\sin^2 A - \sin^2 B}{\cos^2 A - \sin^2 B}$

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57. Prove that :  $\sin^2 6x - \sin^2 4x = s \in 2x \ s \in 10x$

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58. Prove that:  $\cos^2 2x - \cos^2 6x = s \in 4x \ s \in 8x$

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59. Prove that:  $\frac{\cos^2 33^\circ - \cos^2 57^\circ}{\sin(21)^\circ - \cos(21)} = -\frac{1}{\sqrt{2}}$

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60.

Prove

that:

$$\cos 2\alpha \cos 2\beta + \sin^2(\alpha - \beta) - \sin^2(\alpha + \beta) = \cos 2(\alpha + \beta).$$

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61. Prove that:  $\tan 70^\circ = \tan 20^\circ + 2\tan 50^\circ$ .

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62. If  $s \in \alpha + s \in \beta = a$  and  $\cos \alpha + \cos \beta = b$ , show that :

$$\cos(\alpha + \beta) = \frac{b^2 - a^2}{b^2 + a^2}$$

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63. If  $s \in \alpha + s \in \beta = a$  and  $\cos \alpha + \cos \beta = b$ , show that :

$$\cos(\alpha + \beta) = \frac{b^2 - a^2}{a^2 + b^2}$$

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64. If  $\sin A = \frac{4}{5}$  and  $\cos B = \frac{5}{13}$ , where  $0$



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65. If  $\sin A = \frac{4}{5}$  and  $\cos B = \frac{5}{13}$ , where  $0$



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66. If  $\sin A = \frac{4}{5}$  and  $\cos B = \frac{5}{13}$ , where  $0$



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67. If  $\sin A = \frac{4}{5}$  and  $\cos B = \frac{5}{13}$ , where  $0$



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68. If  $\sin A = \frac{12}{13}$  and  $\sin B = \frac{4}{5}$  where  $\frac{\pi}{2} < A < \pi$  and  $0 < B < \frac{\pi}{2}$  then find the following (i)  $\sin(A + B)$  (ii)  $\cos(A + B)$

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69. Prove that  $\frac{\sin x}{\cos(3x)} + \frac{\sin(3x)}{\cos(9x)} + \frac{\sin(9x)}{\cos(27x)} = \frac{1}{2}(\tan 27x - \tan x)$

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70. If  $\sin A = \frac{3}{5}$ ,  $\cos B = -\frac{12}{13}$ , where  $A$  and  $B$  both lie in second quadrant, find the value of  $\sin(A + B)$ .

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71. If  $\cos A = \frac{4}{5}$  and  $\cos B = \frac{12}{13}$  where  $\frac{3\pi}{2} < B < A < 2\pi$  then find  $\cos(A + B)$

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72. If  $\cos A = \frac{4}{5}$  and  $\cos B = \frac{12}{13}$  where  $\frac{3\pi}{2} < B < A < 2\pi$  then find  $\cos(A + B)$

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73. If  $\tan A = \frac{3}{4}, \cos B = \frac{9}{41}$ , where  $\pi < A < \frac{3\pi}{2}$  and  $\frac{3\pi}{2} < B < 2\pi$  find  $\tan(A - B)$

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74. If  $\sin A = \frac{1}{2}, \cos B = \frac{12}{13}$ , where  $\frac{\pi}{2} < A < \pi$  and  $\frac{3\pi}{2} < B < 2\pi$ , find  $\tan(a - b)$ .

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75. If  $\sin A = \frac{1}{2}, \cos B = \frac{\sqrt{3}}{2}$ , where  $\frac{\pi}{2} < A < \pi$  and  $\frac{\pi}{2} < B < \pi$  find  $\tan(A - B)$

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76. If  $\sin A = \frac{1}{2}$ ,  $\cos B = \frac{\sqrt{3}}{2}$ , where  $\frac{\pi}{2} < A < \pi$  and  $0 < B < \frac{\pi}{2}$

find the following:  $\tan(A - B)$ .

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77. Evaluate the following:  $\sin 78^\circ \cos 18^\circ - \cos 78^\circ \sin 18^\circ$

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78. Evaluate the following:  $\sin 36^\circ \cos 9^\circ + \cos 36^\circ \sin 9^\circ$

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79. Evaluate the following:  $\cos 47^\circ \cos 13^\circ - \sin 47^\circ \sin 13^\circ$

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80. Evaluate the following:  $\cos 80^\circ \cos 20^\circ + \sin 80^\circ \sin 20^\circ$

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81. If  $\cos A = -\frac{12}{13}$  and  $\cot B = \frac{24}{7}$  where  $A$  lies in second quadrant and  $B$  lies in third quadrant then find the values of  
(i)  $\sin(A + B)$  (ii)  $\cos(A + B)$  (iii)  $\tan(A + B)$

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82. Prove that:  $\cos 105^\circ + \cos 15^\circ = \sin 75^\circ - \sin 15^\circ$

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83. 
$$\frac{\tan A + \tan B}{\tan A - \tan B} = \frac{\sin(A + B)}{\sin(A - B)}$$

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84. Prove that:  $\frac{\cos 11^\circ + \sin 11^\circ}{\cos 11^\circ - \sin 11^\circ} = \tan 56^\circ$



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85. Prove that:  $\frac{\cos 8^\circ - \sin 8^\circ}{\cos 8^\circ + \sin 8^\circ} = \tan 37^\circ$



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86.  $\frac{\cos 9^\circ + \sin 9^\circ}{\cos 9^\circ - \sin 9^\circ} =$  (a)  $\tan 54^\circ$  (b)  $\tan 36^\circ$  (d) None of these (c)  $\tan 18^\circ$



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87. Prove that:  $\sin(60^\circ - \theta) - \cos(30^\circ + \theta) = 0$ .



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88.

Prove

that:

$$\sin\left(\frac{4\pi}{9} + 7\right)\cos\left(\frac{\pi}{9} + 7\right) - \cos\left(\frac{4\pi}{9} + 7\right)\sin\left(\frac{\pi}{9} + 7\right) = \frac{\sqrt{3}}{2}$$

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89.

Prove

that:

$$\sin\left(\frac{3\pi}{8} - 5\right)\cos\left(\frac{\pi}{8} + 5\right) + \cos\left(\frac{3\pi}{8} - 5\right)\sin\left(\frac{\pi}{8} + 7\right) = 1$$

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90. Prove that : 
$$\frac{\tan 69^\circ + \tan 66^\circ}{1 - \tan 69^\circ \tan 66^\circ} = -1$$

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91. If  $\tan A = \frac{5}{6}$  and  $\tan B = \frac{1}{11}$ , prove that  $A + B = \frac{\pi}{4}$

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92. If  $\tan A = \frac{m}{m-1}$  and  $\tan B = \frac{1}{2m-1}$ , then prove that  $A - B = \frac{\pi}{4}$

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93. Prove that:  $\cos^2 45^\circ - \sin^2 15^\circ = \frac{\sqrt{3}}{4}$

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94. Prove that:  $\sin^2(n+1)A - \sin^2 nA = \sin(2n+1)As \in A$

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95. Prove that:  $\frac{\sin(A+B) + \sin(A-B)}{\cos(A+B) + \cos(A-B)} = \tan A$

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96. Prove that: 
$$\frac{\sin(A - B)}{\cos A \cos B} + \frac{\sin(B - C)}{\cos B \cos C} + \frac{\sin(C - A)}{\cos C \cos A} = 0$$

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97. Prove that: 
$$\frac{\sin(A - B)}{s \in A s \in B} + \frac{\sin(B - C)}{s \in B s \in C} + \frac{\sin(C - A)}{s \in C s \in A} = 0$$

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98. Prove that:

$$\sin^2 B = \sin^2 A + \sin^2(A - B) - 2 \sin A \cos B \sin(A - B)$$

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99. Prove that:

$$\cos^2 A + \cos^2 B - 2 \cos A \cos B \cos(A + B) = \sin^2(A + B)$$

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100. Prove that: 
$$\frac{\tan(A + B)}{\cot(A - B)} = \frac{\tan^2 A - \tan^2 B}{1 - \tan^2 A \tan^2 B}$$

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101. If  $\tan A = x \tan B$  then prove that 
$$\frac{\sin(A - B)}{\sin(A + B)} = \frac{x - 1}{x + 1}$$

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102. If  $\tan(A + B) = x$  and  $\tan(A - B) = y$  then find the values of  $\tan 2A$  and  $\tan 2B$

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103. If  $\cos A + \sin B = m$  and  $\sin A + \cos B = n$ , prove that 
$$2 \sin(A + B) = m^2 + n^2 - 2.$$

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104. If  $\tan A + \tan B = a$  and  $\cot A + \cot B = b$ , prove that:

$$\cot(A + B) = \frac{1}{a} - \frac{1}{b}$$

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105. If  $\sin(\alpha + \beta) = 1$  and  $\sin(\alpha - \beta) = \frac{1}{2}$ , where  $0 \leq \alpha, \beta \leq \frac{\pi}{2}$ , then

find the values of  $\tan(\alpha + 2\beta)$  and  $\tan(2\alpha + \beta)$ .

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106. If  $\alpha, \beta$  are two different values of  $x$  lying between  $0$  and  $2\pi$  which satisfy the equation  $6 \cos x + 8 \sin x = 9$ , find the value of  $\sin(\alpha + \beta)$

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107. Prove that  $\frac{\tan^2(2\theta) - \tan^2 \theta}{1 - \tan^2(2\theta)\tan^2 \theta} = \tan(3\theta)\tan \theta$

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108. If  $\sin \alpha \sin \beta - \cos \alpha \cos \beta + 1 = 0$ , then prove that  $1 + \cot \alpha \tan \beta = 0$



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109. If  $\tan \alpha = x + 1$ ,  $\tan \beta = x - 1$ , show that  $2 \cot(\alpha - \beta) = x^2$ .



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110. Find the maximum and minimum values of  $7 \cos \theta + 24 \sin \theta$



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111. Prove that  $5 \cos \theta + 3 \cos\left(\theta + \frac{\pi}{3}\right) + 3$  lies between  $-4$  and  $10$ .



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112. Reduce  $\sqrt{3} \sin \theta - \cos \theta$  as a single term consisting sine only

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113. Express  $\sin \theta - \cos \theta$  as cosine of a single expression.

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114. Find the maximum and minimum values of each of the following trigonometrical expression:  $24s \int h\eta + 7 \cos \theta$

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115. Find the maximum and minimum values of each of the following trigonometrical expression:  $5 \cos \theta + 3 \sin \left( \frac{\pi}{6} - \theta \right) + 4$

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**116.** Find the maximum and minimum values of each of the following trigonometrical expression:  $12 \cos \theta + 5s \int h\eta + 4$

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**117.** Find the maximum and minimum values of each of the following trigonometrical expression:  $s \int h\eta - \cos \theta + 1$

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**118.** Reduce each of the following expressions to the sine or cosine of a single expression:  $\sqrt{3} \sin \theta - \cos \theta$

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**119.** Reduce each of the following expressions to the sine and cosine of a single expression:  $\sin \theta - \cos \theta$

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120. Reduce each of the following expressions to the sine and cosine of a single expression:  $24 \cos \theta + 7s \int h\eta$

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121. Show that  $\sin 100^\circ - \sin 10^\circ$  is positive

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122. If  $\alpha + \beta - \gamma = \pi$  and  $\sin^2 \alpha + \sin^2 \beta - \sin^2 \gamma = \lambda \sin \alpha \sin \beta \cos \gamma$ , then write the value of  $\lambda$

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123. If  $x \cos \theta = y \cos \left( \theta + \frac{2\pi}{3} \right) = z \cos \left( \theta + \frac{4\pi}{3} \right)$ , then write the value of  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$ .





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124. Write the maximum and minimum values of  $3 \cos x + 4 \sin x + 5$ .



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125. Write the maximum value of  $12s \int \sin \theta - 9 \sin^2 \theta$ .



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126. If  $12 \sin \theta - 9 \sin^2 \theta$  attains its maximum value at  $\theta = \alpha$ , then write the value of  $s \in \alpha$ .



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127. Write the interval in which the values of  $5 \cos \theta + 3 \cos \left( \theta + \frac{\pi}{3} \right) + 3$  lie.

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128. If  $\tan(A + B) = p$  and  $\tan(A - B) = q$  then write the value of  $\tan 2A$ .

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129. If  $\frac{\cos(x - y)}{\cos(x + y)} = \frac{m}{n}$ , then write the value of  $\tan x \tan y$ .

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130. If  $a = b \cos\left(\frac{2\pi}{3}\right) = c \cos\left(\frac{4\pi}{3}\right)$ , then write the value of  $ab + bc + ca$

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131. If  $A + B = C$ , then write the value of  $\tan A \tan B \tan C$ .



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132. If  $\sin \alpha - \sin \beta = a$  and  $\cos \alpha + \cos \beta = b$  then write the value of  $\cos(\alpha + \beta)$ .



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133. The value of  $\sin^2 75^\circ - \sin^2 15^\circ$  is  $1/2$  b.  $\sqrt{3}/2$  c.  $1$  d.  $0$



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134. If  $A + B + C = 180^\circ$ , then  $\sec A(\cos B \cos C - \sin B \sin C)$  is equal to  $0$  b.  $-1$  c.  $1$  d. none of these



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135.  $\tan 20^\circ + \tan 40^\circ + \sqrt{3}\tan 20^\circ \tan 40^\circ =$   
a.  $\frac{\sqrt{3}}{4}$ , b.  $\frac{\sqrt{3}}{2}$ , c.  $\sqrt{3}$ , d. 1

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136. If  $\tan A = \frac{a}{a+1}$  and  $\tan B = \frac{1}{2a+1}$  then the value of  $A + B$  is 0  
b.  $\frac{\pi}{2}$  c.  $\frac{\pi}{3}$  d.  $\frac{\pi}{4}$

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137. If  $3 \cos \theta + 4 \sin \theta = 5$  then  $4 \sin \theta - 3 \cos \theta$  is equal to

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138.  $\tan 3A - \tan 2A - \tan A =$

a.  $\tan 3A \tan 2A \tan A$ , b.  $-\tan 3A \tan 2A \tan A$ , c.  $\tan A \tan 2A - \tan A \tan 3A$   
none of these

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139. If  $A + B + C = 180^\circ$ , then  $\frac{\tan A + \tan B + \tan C}{\tan A \tan B \tan C}$  is equal to  $\tan A \tan B \tan C$  b. 0 c. 1 d. none of these

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140. If  $\cos P = \frac{1}{7}$  and  $\cos Q = \frac{13}{14}$  where  $P$  and  $Q$  both are acute angles. Then, the value of  $P - Q$  is  $30^\circ$  b.  $60^\circ$  c.  $45^\circ$  d.  $75^\circ$

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141. If  $\cot(\alpha + \beta) = 0$  then  $\sin(\alpha + 2\beta)$  is equal to a.  $\sin \alpha$  b.  $\cos 2\beta$  c.  $\cos \alpha$  d.  $\sin 2\alpha$

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142.  $\frac{\cos 10^\circ + \sin 10^\circ}{\cos 10^\circ - \sin 10^\circ}$  is equal to  $\tan 55^\circ$  b.  $\cos 55^\circ$  c.  $-\tan 35^\circ$  d.  $-\cot 35^\circ$



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143. The value of  $\cos^2\left(\frac{\pi}{6} + \theta\right) - \sin^2\left(\frac{\pi}{6} - \theta\right)$  is  $\frac{1}{2}\cos 2\theta$  b. 0 c.  $-\frac{1}{2}\cos 2\theta$  d.  $-\cot 35^\circ$



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144. If  $\tan\theta_1 \tan\theta_2 = k$ , then  $\frac{\cos(\theta_1 - \theta_2)}{\cos(\theta_1 + \theta_2)} = \frac{1+k}{1-k}$  b.  $\frac{1-k}{1+k}$  c.  $\frac{k+1}{k-1}$  d.  $\frac{k-1}{k+1}$



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145. If  $A - B = \pi/4$ , then  $(1 + \tan A)(1 - \tan B)$  is equal to a. 2 b. 1 c. 0 d. 3



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146. The maximum value of  $\sin^2(120^\circ + \theta) + \sin^2(120^\circ - \theta)$  is  $1/2$  b.  $3/2$   
c.  $1/4$  d.  $3/4$



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147. If  $\cos(A - B) = \frac{3}{5}$  and  $\tan A \tan B = 2$ , then  $\cos A \cos B = \frac{1}{5}$  b.  
 $\cos A \cos B = -\frac{1}{5}$  c.  $\sin A \sin B = -\frac{1}{5}$  d.  $\sin A \sin B = \frac{1}{5}$



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148. If  $\tan 69^\circ + \tan 66^\circ - \tan 69^\circ \tan 66^\circ = 2k$ , then  $k =$  a.  $-1$  b.  $1/2$   
c.  $-1/2$  d.  $17$



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149. If  $\tan \alpha = \frac{x}{x+1}$  and  $\tan \beta = \frac{1}{2x+1}$ , then  $\alpha + \beta$  is equal to  $\frac{\pi}{2}$   
b.  $\frac{\pi}{3}$  c.  $\frac{\pi}{6}$  d.  $\frac{\pi}{4}$



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