



MATHS

BOOKS - RD SHARMA MATHS (HINGLISH)

DEFINITE INTEGRALS

Solved Examples And Exercises

1. Evaluate : $\int_0^{\frac{\pi}{6}} \cos x \cos 2x dx$



[Watch Video Solution](#)

2. Evaluate : $\int_0^{\frac{\pi}{2}} \cos^3 x dx$



[Watch Video Solution](#)

3. Evaluate : $\int_0^{\frac{\pi}{4}} \sec x dx$

 [Watch Video Solution](#)

4. $\int_{\pi/4}^{\pi/2} \cot x dx = ?$

 [Watch Video Solution](#)

5. Evaluate : $\int_0^{\frac{\pi}{2}} (\sin x + \cos x) dx$

 [Watch Video Solution](#)

6. Evaluate : $\int_{-2}^3 \frac{1}{x+7} dx$

 [Watch Video Solution](#)

7. Evaluate : $\int_0^{\pi} \frac{1}{1 + \sin x} dx$

 [Watch Video Solution](#)

8. Evaluate : $\int_1^4 \frac{x^2 + x}{\sqrt{2x + 1}} dx$

 [Watch Video Solution](#)

9. Evaluate : $\int_0^1 x(1 - x)^5 dx$

 [Watch Video Solution](#)

10. Evaluate : $\int_1^2 \left(\frac{x - 1}{x^2} \right) e^x dx$

 [Watch Video Solution](#)

11. Evaluate : $\int_0^1 \sqrt{x(1-x)} dx$

 [Watch Video Solution](#)

12. Evaluate : $\int_0^1 \frac{1}{\sqrt{3+2x-x^2}} dx$

 [Watch Video Solution](#)

13. Evaluate : $\int_0^{\frac{\pi}{4}} (\tan x + \cot x)^{-2} dx$

 [Watch Video Solution](#)

14. Evaluate : $\int_0^1 \left(xe^x + \frac{\sin(\pi x)}{4} \right) dx$

 [Watch Video Solution](#)

15. Evaluate : $\int_0^1 \frac{1}{1 + 2x + 2x^2 + 2x^3 + x^4} dx$

 [Watch Video Solution](#)

16. Evaluate : $\int_0^1 x \log(1 + 2x) dx$

 [Watch Video Solution](#)

17. Evaluate : $\int_2^3 \frac{x}{x^2 + 1} dx$

 [Watch Video Solution](#)

18. Evaluate : $\int_0^\infty e^{-x} dx$

 [Watch Video Solution](#)

19. Evaluate : $\int_0^{\frac{\pi}{2}} x^2 \sin x dx$

 [Watch Video Solution](#)

20. Evaluate : $\int_4^9 \frac{1}{\sqrt{x}} dx$

 [Watch Video Solution](#)

21. Evaluate : $\int_0^{\frac{\pi}{2}} \sqrt{1 + \sin x} dx$

 [Watch Video Solution](#)

22. Evaluate : $\int_0^{\frac{1}{2}} \frac{1}{\sqrt{1-x^2}} dx$

 [Watch Video Solution](#)

23. Evaluate : $\int_0^1 \frac{1}{1+x^2} dx$

 [Watch Video Solution](#)

24. Evaluate : $\int_0^\pi \frac{x}{(a^2 \cos^2 x + b^2 \sin^2 x)^2} dx$

 [Watch Video Solution](#)

25. Evaluate : $\int_0^\infty \frac{1}{a^2 + b^2 x^2} dx$

 [Watch Video Solution](#)

26. Evaluate : $\int_{\frac{\pi}{3}}^{\frac{\pi}{4}} (\tan x + \cot x)^2 dx$

 [Watch Video Solution](#)

27. Evaluate : $\int_1^e \frac{\log x}{x} dx$

 [Watch Video Solution](#)

28. Evaluate : $\int_0^{2\pi} e^x \cos\left(\frac{\pi}{4} + \frac{x}{2}\right) dx$

 [Watch Video Solution](#)

29. Evaluate : $\int_1^2 \frac{x+3}{x(x+2)} dx$

 [Watch Video Solution](#)

30. Evaluate : $\int_e^{e^2} \left\{ \frac{1}{\log x} - \frac{1}{(\log x)^2} \right\} dx$

 [Watch Video Solution](#)

31. If $\int_0^k \frac{1}{2+8x^2} dx = \frac{\pi}{16}$, find the value of $2k$

 [Watch Video Solution](#)

32. Evaluate: $\int_{-\pi}^{\pi} \left((2x) \frac{1 + \sin x}{1 + \cos^2 x} \right) dx$

 [Watch Video Solution](#)

33. Evaluate: $\int_{-1}^1 \frac{x^3 + |x| + 1}{x^2 + 2|x| + 1} dx$

 [Watch Video Solution](#)

34. $\int_0^1 \log\left(\frac{1}{x} - 1\right) dx$ is equal to

 [Watch Video Solution](#)

35. Evaluate: $\int_0^{\frac{\pi}{2}} \frac{\sin^2 x}{1 + \sin x \cos x} dx$

 [Watch Video Solution](#)

36. Prove that: $\int_0^{\pi/2} \frac{\sin x}{\sin x - \cos x} dx = \frac{\pi}{4}$

 [Watch Video Solution](#)

37. Prove that: $\int_0^{2a} f(x) dx = \int_0^{2a} f(2a - x) dx$.

 [Watch Video Solution](#)

38. Evaluate: $\int_{-\pi/4}^{\pi/4} x^3 \sin^4 x dx$ (ii) $\int_a^a \sqrt{\frac{a-x}{a+x}} dx$

 [Watch Video Solution](#)

39. Evaluate: $\int_{\pi/4}^{\pi/4} \frac{x + \pi/4}{2 - \cos 2x} dx$

 [Watch Video Solution](#)

40. Evaluate: $\int_0^{\pi/2} \frac{\cos x}{1 + \cos x + \sin x} dx$

 [Watch Video Solution](#)

41. Prove that: $\int_0^{\pi} \frac{x}{1 + \cos \alpha \sin x} dx = \frac{\pi \alpha}{\sin \alpha}$

 [Watch Video Solution](#)

42. Evaluate the following integrals: (1-35) $\int_{-a}^a \log \left(\frac{a - \sin \theta}{a + \sin \theta} \right) d\theta, a > 0$

 [Watch Video Solution](#)

43. Evaluate the following integrals: $\int_{-1}^1 |x \cos \pi x| dx$

 [Watch Video Solution](#)

44. Evaluate the following integrals: (1-35) $\int_0^\pi \left(\frac{x}{1 + \sin^2 x} + \cos^7 x \right) dx$

 [Watch Video Solution](#)

45. Evaluate : $\int_0^\pi \frac{x}{1 + \sin \alpha \sin x} dx$

 [Watch Video Solution](#)

46. Evaluate the following integrals: (1-35) $\int_0^{\pi/2} \frac{a \sin x + b \cos x}{\sin x + \cos x} dx$

 [Watch Video Solution](#)

47. Evaluate the following integral as limit of sums: $\int_0^2 (x + 4) dx$

 [Watch Video Solution](#)

48. Evaluate $\int_1^4 (x^2 - x) dx$ as a limit of sums.

 [Watch Video Solution](#)

49. Evaluate: $\int_a^b \sin x dx$ using limit of sum

 [Watch Video Solution](#)

50. Mark the correct alternative in each of the following:

$\int_0^1 \sqrt{x(1-x)} dx$ equals $\pi/2$ (b) $\pi/4$ (c) $\pi/6$ (d) $\pi/8$

 [Watch Video Solution](#)

51. Evaluate : $\int_0^{\pi} \frac{1}{1 + \sin x} dx$

 [Watch Video Solution](#)

52. If $\int_0^a \sqrt{x} dx = 2a \int_0^{\pi/2} \sin^3 x dx$ find the value of integral $\int_a^{a+1} x dx$.

 [Watch Video Solution](#)

53. Evaluate: (i) $\int_0^4 \frac{1}{\sqrt{x^2 + 2x + 3}} dx$

 [Watch Video Solution](#)

54. If $\int_0^1 (3x^2 + 2x + k) dx = 0$, find the value of k .

 [Watch Video Solution](#)

55. If $\int_1^a (3x^2 + 2x + 1) dx = 11$ then the value of a is



[Watch Video Solution](#)

56. If $\int_a^b x^3 dx = 0$, and If $\int_a^b x^2 dx = \frac{2}{3}$, find a and b.



[Watch Video Solution](#)

57. Evaluate: $\int_0^{\pi/2} \sqrt{1 - \cos 2x} dx$.



[Watch Video Solution](#)

58. Evaluate: $\int_0^{\pi/2} \sin^4 x dx$



[Watch Video Solution](#)

59. Evaluate: $\int_0^{\pi/4} \sqrt{1 + \sin 2x} dx$ (ii) $\int_0^{\pi/4} \sqrt{1 - \sin 2x} dx$



[Watch Video Solution](#)

60. Evaluate: $\int_{\pi/4}^{\pi/2} \sqrt{1 - \sin 2x} dx$

 [Watch Video Solution](#)

61. Evaluate the following integrals: (1-35) $\int_{-2}^2 \frac{3x^3 + 2|x| + 1}{x^2 + |x| + 1} dx$

 [Watch Video Solution](#)

62. Evaluate the following integrals: (1-35) $\int_0^{\pi} x \sin x \cos^2 x dx$

 [Watch Video Solution](#)

63. Show that: $\int_0^{\pi/2} f(\sin 2x) \sin x dx = \sqrt{2} \int_0^{\pi/4} f(\cos 2x) \cos x dx$.

 [Watch Video Solution](#)

64. For $x > 0$, let $f(x) = \int_1^x \frac{(\log)_e t}{1+t} dt$. Find the function $f(x) + f\left(\frac{1}{x}\right)$ and show that $f(e) + f\left(\frac{1}{e}\right) = \frac{1}{2}$.

 [Watch Video Solution](#)

65. Evaluate the following integrals: (1-35) $\int_0^{\pi/2} \frac{\sin^n x}{\sin^n x + \cos^n x} dx$

 [Watch Video Solution](#)

66. Prove that: $\int_0^{2\pi} \frac{x \sin^{2n} x}{\sin^{2n} x + \cos^{2n} x} dx = \pi^2$

 [Watch Video Solution](#)

67. Prove that: $\int_0^{\pi/2} \log|\tan x + \cot x| dx = \pi(\log)_e 2$

 [Watch Video Solution](#)

68. Evaluate: $\int_{-2}^2 |x \cos \pi x| dx$

 [Watch Video Solution](#)

69. Evaluate: $\int_{\pi/4}^{\pi/4} \log(\sin x + \cos x) dx$

 [Watch Video Solution](#)

70. Evaluate: $\int_0^{\pi} x \log \sin x dx$

 [Watch Video Solution](#)

71. If $\int_0^{\pi} \frac{1}{a + b \cos x} dx = \frac{\pi}{\sqrt{a^2 - b^2}}$, then $\int_0^{\pi} \frac{1}{(a + b \cos x)^2} dx$ is

 [Watch Video Solution](#)

72. $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx = \frac{\pi}{2}$ (b) $\frac{\pi}{2} - 1$ (c) $\frac{\pi}{2} + 1$ (d) $\pi + 1$



Watch Video Solution

73. $\int_0^{\pi/2} \frac{\cos x}{(2 + \sin x)(1 + \sin x)} dx$ equals (a) $\log\left(\frac{2}{3}\right)$ (b) $\log\left(\frac{3}{2}\right)$ (c) $\log\left(\frac{3}{4}\right)$ (d) $\log\left(\frac{4}{3}\right)$



Watch Video Solution

74. $\int_0^{\pi} \frac{x \tan x}{\sec x + \cos x} dx$ is $\frac{\pi^2}{4}$ (b) $\frac{\pi^2}{2}$ (c) $\frac{3\pi^2}{2}$ (d) $\frac{\pi^2}{3}$



Watch Video Solution

75. $\int_0^2 \frac{1}{1 + \tan x} dx$ is equal to $\frac{\pi^{\square}}{4}$ (b) $\frac{\pi^{\square}}{3}$ (c) $\frac{\pi^{\square}}{2}$ (d) π



Watch Video Solution

76. $\int_{-\pi/2}^{\pi/2} \sin|x| dx$ is equal to 1 (b) 2 (c) -1 (d) -2



 Watch Video Solution

77. The value of the integral $\int_0^{\infty} \frac{x}{(1+x)(1+x^2)} dx$ is $\frac{\pi}{2}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{6}$
(d) $\frac{\pi}{3}$

 Watch Video Solution

78. $\int_0^3 \frac{3x+1}{x^2+9} dx = \frac{\pi}{12} + \log(2\sqrt{2})$ (b) $\frac{\pi}{2} + \log(2\sqrt{2})$ (c)
 $\frac{\pi}{6} + \log(2\sqrt{2})$ (d) $\frac{\pi}{3} + \log(2\sqrt{2})$

 Watch Video Solution

79. $I_{10} = \int_0^{\frac{\pi}{2}} x^{10} \sin x dx$ then $I_{10} + 90I_8$ is (A) $10\left(\frac{\pi}{2}\right)^6$ (B) $10\left(\frac{\pi}{2}\right)^9$ (C)
 $10\left(\frac{\pi}{2}\right)^8$ (D) $10\left(\frac{\pi}{2}\right)^7$

 Watch Video Solution

80. Evaluate: $\int_0^{\pi/2} \frac{\cos x}{1 + \cos x + \sin x} dx$

 [Watch Video Solution](#)

81. Evaluate: $\int_0^{\pi/2} \frac{1}{3 + 2 \cos x} dx$

 [Watch Video Solution](#)

82. Evaluate: $\int_{\pi/4}^{\pi/2} \cos 2x \log \sin x dx$

 [Watch Video Solution](#)

83. integrate $\int_0^{2\pi} e^x \cdot \sin\left(\frac{\pi}{4} + \frac{x}{2}\right) dx$

 [Watch Video Solution](#)

84. Evaluate: $\int_0^1 \frac{2x}{5x^2 + 1} dx$

 [Watch Video Solution](#)

85. Evaluate: (i) $\int_0^{\pi/6} (2 + 3x^2) dx$

 [Watch Video Solution](#)

86. Evaluate: (i) $\int_0^4 \frac{1}{x + \sqrt{x}} dx$ (ii) $\int_0^1 \frac{2x}{5x^2 + 1} dx$

 [Watch Video Solution](#)

87. Evaluate the following definite integrals (1-58):

$$\int_1^2 \frac{1}{\sqrt{(x-1)(2-x)}} dx$$

 [Watch Video Solution](#)

88. If $f(x)$ is of the form $f(x) = a + bx + cx^2$, show that

$$\int_0^1 f(x) dx = \frac{1}{6} \left\{ f(0) + 4f\left(\frac{1}{2}\right) + f(1) \right\}$$

 [Watch Video Solution](#)

89. Evaluate: $\int_0^{\infty} \frac{1}{(x^2 + a^2)(x^2 + b^2)} dx$.

 [Watch Video Solution](#)

90. Evaluate the following integrals: $\int_0^{\pi/6} \cos^{-3} 2\theta \sin 2\theta d\theta$

 [Watch Video Solution](#)

91. Evaluate the following integrals: $\int_0^{(\pi)^{2/3}} \sqrt{x} \cos^2 x^{3/2} dx$

 [Watch Video Solution](#)

92. Evaluate the following integrals: $\int_0^1 \frac{24x^3}{(1+x^2)^4} dx$

 [Watch Video Solution](#)

93. Evaluate the following integrals: $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx$

 [Watch Video Solution](#)

94. If $I_n = \int_0^{\pi/4} \tan^n x dx$, prove that $I_n + I_{n-2} = \frac{1}{n-1}$.

 [Watch Video Solution](#)

95. If $I_n = \int_0^{\pi/4} \tan^n x dx$, show that $\frac{1}{I_2 + I_4}, \frac{1}{I_3 + I_5}, \frac{1}{I_4 + I_6}, \frac{1}{I_5 + I_7}$, form an A.P. Find the common difference of this progression.

 [Watch Video Solution](#)

96. Evaluate: $\int_0^{\pi/2} \frac{1}{(a^2 \cos^2 x + b^2 \sin^2 x)^2} dx$

 [Watch Video Solution](#)

97. Evaluate: $\int_0^1 x (\tan^{-1} x)^2 dx$

 [Watch Video Solution](#)

98. Evaluate: $\int_0^a \frac{1}{(x^2 + a^2)} dx$ (ii) $\int_0^\infty \frac{x^2}{(a^2 + x^2)^{5/2}} dx$

 [Watch Video Solution](#)

99. Evaluate: $\int_0^1 x \sqrt{\frac{1-x^2}{1+x^2}} dx$

 [Watch Video Solution](#)

100. Evaluate the following integrals: $\int_0^a (\sin)^{-1} \sqrt{\frac{x}{a+x}} dx$

 [Watch Video Solution](#)

101. Evaluate the following integrals: $\int_1^2 \frac{1}{x(1+\log x)^2} dx$

 [Watch Video Solution](#)

102. Evaluate the following integrals: $\int_0^{\pi/4} \frac{\sin^2 x \cos^2 x}{(\sin^3 x + \cos^3 x)^2} dx$

 [Watch Video Solution](#)

103. Evaluate the following integrals: $\int_0^{\pi/2} \frac{\tan x}{1+m^2 \tan^2 x} dx$

 [Watch Video Solution](#)

104. Evaluate: $\int_0^1 |5x - 3| dx$

 [Watch Video Solution](#)

105. Evaluate:

(i) $\int_{-1}^1 f(x) dx$, where, $f(x) = \{1 - 2x, x \leq 0; 1 + 2x, x \geq 0\}$,

(ii) $\int_{-1}^4 f(x) dx$, where, $f(x) = \{2x + 8, -1 \leq x \leq 2; 6x, 2 \leq x \leq 4\}$

 [Watch Video Solution](#)

106. $\int_{\frac{1}{e}}^e |\log x| dx =$

 [Watch Video Solution](#)

107. If $a > 0$, find $\int_0^{3a} |x^2 - a^2| dx$.

 [Watch Video Solution](#)

108. If $[\cdot]$ denotes the greatest integer function, then find the value of

$$\int_1^2 [3x] dx$$

 [Watch Video Solution](#)

109. Evaluate: $\int_0^3 [x] dx$

 [Watch Video Solution](#)

110. $\int_0^1 \frac{d}{dx} \left\{ \sin^{-1} \left(\frac{2x}{1+x^2} \right) \right\} dx$ is equal to 0 (b) π (c) $\pi/2$ (d) $\pi/4$

 [Watch Video Solution](#)

111. Evaluate the following integrals: $\int_{-a}^a \frac{x e^{x^2}}{1+x^2} dx$

 [Watch Video Solution](#)

112. Evaluate the following integrals: $\int_0^{\pi/4} |\cos 2x| dx$

 [Watch Video Solution](#)

113. Evaluate the following integrals:

$$\int_{-5}^0 f(x) dx, \text{ where } f(x) = |x| + |x + 2| + |x + 5|$$

 [Watch Video Solution](#)

114. Evaluate the following definite integrals (1-58):

$$\int_1^2 \frac{1}{\sqrt{(x-1)(2-x)}} dx$$

 [Watch Video Solution](#)

115. Evaluate the following integrals: $\int_0^{\pi} \cos x |\cos x| dx$

 [Watch Video Solution](#)

116. Let $f(x) = x - [x]$, for every real number x , where $[x]$ is the greatest integer less than or equal to x . Then, evaluate $\int_{-1}^1 f(x) dx$.

 [Watch Video Solution](#)

117. Evaluate: $\int_0^{\sqrt{3}} \frac{1}{1+x^2} \sin^{-1}\left(\frac{2x}{1+x^2}\right) dx$

 [Watch Video Solution](#)

118. Evaluate the following integrals: $\int_0^9 f(x) dx$, where $f(x) =$

$$\{\sin x, 0 \leq x \leq \pi/2$$

$$1, \frac{\pi}{2} \leq x \leq 3$$

$$e^{x-3}, 3 \leq x \leq 9$$

 [Watch Video Solution](#)

119. Evaluate the following integrals: $\int_0^2 |x^2 - 3x + 2| dx$



Watch Video Solution

120. Evaluate the following integrals: $\int_0^1 \left(\frac{1-x}{1+x} \right) dx$



Watch Video Solution

121. Prove that: $\int_a^b \frac{f(x)}{f(x) + f(a+b-x)} dx = \frac{b-a}{2}$



Watch Video Solution

122. Evaluate of each of the following integrals (1-15):

$$\int_0^5 \frac{\sqrt[3]{x+4}}{\sqrt[3]{x+4} + \sqrt[3]{9-x}} dx$$



Watch Video Solution

123. Evaluate each of the following integrals (1-15):

$$\int_{-\pi/4}^{\pi/4} \frac{x^{11} - 3x^9 + 5x^7 - x^5 + 1}{\cos^2 x} dx$$



Watch Video Solution

124. Evaluate each of the following integrals (1-15):

$$\int_{-a}^a \frac{1}{1 + a^x} dx, a > 0$$



Watch Video Solution

125. Evaluate $\int_{\pi/6}^{\pi/3} \frac{\sqrt{(\sin x)} dx}{\sqrt{(\sin x)} + \sqrt{(\cos x)}}$



Watch Video Solution

126. Evaluate each of the following integrals (1-15):

$$\int_0^{2\pi} \log(\sec x + \tan x) dx$$





Watch Video Solution

127. Evaluate: $\int_{-\pi/4}^{\pi/4} \frac{\sec^2 x}{e^{2x} - 1} dx$



Watch Video Solution

128. Evaluate: $\int_{-\pi/4}^{\pi/4} \frac{\tan^2 x}{1 + e^x} dx$



Watch Video Solution

129. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{x \sin x}{e^x + 1} dx$



Watch Video Solution

130. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \frac{a + b}{2} \int_a^b f(x) dx.$$



Watch Video Solution

131. Evaluate each of the following integrals (1-15):

$$\int_0^7 \left(\frac{x^{\frac{1}{3}}}{x^{\frac{1}{3}} + (7-x)^{\frac{1}{3}}} \right) dx$$

 [Watch Video Solution](#)

132. Evaluate: $\int_1^2 x^2 dx$

 [Watch Video Solution](#)

133. Evaluate: $\int_4^1 \frac{1}{x} dx$

 [Watch Video Solution](#)

134. Evaluate: $\int_0^1 \frac{1}{\sqrt{1+x} + \sqrt{x}} dx$

 [Watch Video Solution](#)

135. Evaluate: $\int_0^1 \frac{1}{2x-3} dx$

 [Watch Video Solution](#)

136. Evaluate: $\int_0^{\pi/4} \tan^2 x dx$

 [Watch Video Solution](#)

137. Evaluate $\int_0^{\pi/2} \sin^2 x dx$

 [Watch Video Solution](#)

138. Evaluate: $\int_0^{\pi/4} \sin 3x \sin 2x dx$

 [Watch Video Solution](#)

139. Evaluate: $\int_{1/4}^{1/2} \frac{1}{\sqrt{x-x^2}} dx$

 [Watch Video Solution](#)

140. Evaluate: $\int_2^4 \frac{x}{x^2+1} dx$

 [Watch Video Solution](#)

141. Evaluate: $\int_0^1 \frac{2x}{5x^2+1} dx$

 [Watch Video Solution](#)

142. Evaluate: $\int_0^2 \frac{5x+1}{x^2+4} dx$

 [Watch Video Solution](#)

143. Evaluate: $\int_0^1 x e^x dx$



Watch Video Solution

144. Evaluate: $\int_1^2 \frac{\log x}{x^2} dx$



Watch Video Solution

145. Evaluate: $\int_0^{\pi/2} x \sin x dx$



Watch Video Solution

146. Evaluate: $\int_1^2 \frac{\log x}{x^2} dx$



Watch Video Solution

147. Evaluate: $\int_0^{\pi/2} x \sin x dx$



Watch Video Solution

148. Evaluate the definite integrals $\int_0^1 \left(xe^x + \frac{\sin(\pi x)}{4} \right) dx$

 [Watch Video Solution](#)

149. $\int_1^2 \frac{5x^2}{x^2 + 4x + 3} dx$

 [Watch Video Solution](#)

150. Evaluate: $\int_1^3 \frac{1}{x^2(x+1)} dx$

 [Watch Video Solution](#)

151. Evaluate: $\int_1^3 \frac{1}{x^2(x+1)} dx$

 [Watch Video Solution](#)

152. Evaluate : $\int_4^9 \frac{1}{\sqrt{x}} dx$

 [Watch Video Solution](#)

153. Evaluate the following definite integral: $\int_2^3 \frac{1}{x+7} dx$

 [Watch Video Solution](#)

154. Evaluate the following definite integral: $\int_0^{1/2} \frac{1}{\sqrt{1-x^2}} dx$

 [Watch Video Solution](#)

155. Evaluate the following definite integral: $\int_0^1 \frac{1}{1+x^2} dx$

 [Watch Video Solution](#)

156. Evaluate the following definite integral: $\int_2^3 \frac{x}{x^2 + 1} dx$

 [Watch Video Solution](#)

157. Evaluate : $\int_0^{\infty} \frac{1}{a^2 + b^2 x^2} dx$

 [Watch Video Solution](#)

158. Evaluate the following definite integral: $\int_{-1}^1 \frac{1}{1 + x^2} dx$

 [Watch Video Solution](#)

159. Evaluate the following definite integrals: $\int_0^{\infty} e^{-x} dx$

 [Watch Video Solution](#)

160. Evaluate the following definite integral: $\int_0^1 \frac{x}{x+1} dx$

 [Watch Video Solution](#)

161. Evaluate the following definite integral: $\int_0^{\pi/2} (\sin x + \cos x) dx$

 [Watch Video Solution](#)

162. Evaluate the following definite integral: $\int_{\pi/4}^{\pi/2} \cot x dx$

 [Watch Video Solution](#)

163. Evaluate the following definite integral: $\int_0^{\pi/4} \sec x dx$

 [Watch Video Solution](#)

164. Evaluate the following definite integral: $\int_{\pi/6}^{\pi/4} \cos ec x dx$

 [Watch Video Solution](#)

165. Evaluate : $\int_0^{\pi} \frac{1}{1 + \sin x} dx$

 [Watch Video Solution](#)

166. Evaluate the definite integrals $\int_0^{\frac{\pi}{2}} \cos^2 x dx$

 [Watch Video Solution](#)

167. Evaluate the following definite integral: $\int_0^{\pi/6} \cos x \cos 2x dx$

 [Watch Video Solution](#)

168. Evaluate : $\int_{\frac{\pi}{3}}^{\frac{\pi}{4}} (\tan x + \cot x)^2 dx$

 [Watch Video Solution](#)

169. Evaluate the following definite integral $\int_0^{\frac{\pi}{2}} \cos^4 x dx$

 [Watch Video Solution](#)

170. Evaluate the following definite integral:

$$\int_0^{\pi/2} (a^2 \cos^2 x + b^2 \sin^2 x) dx$$

 [Watch Video Solution](#)

171. Evaluate the following definite integral: $\int_0^{\pi/2} \sqrt{1 + \cos x} dx$

 [Watch Video Solution](#)

172. Evaluate the following definite integral: $\int_0^1 \frac{1-x}{1+x} dx$

 [Watch Video Solution](#)

173. Evaluate the following definite integral: $\int_{-\pi/4}^{\pi/4} \frac{1}{1+s \in x} dx$

 [Watch Video Solution](#)

174. Evaluate the following definite integral: $\int_0^{\pi/2} \cos^3 x dx$

 [Watch Video Solution](#)

175. Evaluate the following definite integral $\int_0^{\pi/2} \cos^4 x dx$

 [Watch Video Solution](#)

176. Evaluate the following definite integral: $\int_0^{\pi/2} x^2 \sin x dx$



[Watch Video Solution](#)

177. Evaluate the following definite integral: $\int_0^{\pi/2} \cos x \, dx$



[Watch Video Solution](#)

178. Evaluate the following definite integral: $\int_0^{\pi/2} x^2 \sin x \, dx$



[Watch Video Solution](#)

179. Evaluate the following definite integral: $\int_0^{\pi/2} \cos^2 x \, dx$



[Watch Video Solution](#)

180. Evaluate the following definite integral: $\int_1^3 (\log x) \, dx$



[Watch Video Solution](#)

181. Evaluate the following definite integral: $\int \frac{e^{\log \sqrt{x}}}{x} dx$

 [Watch Video Solution](#)

182. Evaluate the following definite integral: $\int_1^2 \frac{x + 3}{x(x + 2)} dx$

 [Watch Video Solution](#)

183. Evaluate the following definite integral: $\int_0^2 \frac{1}{4 + x - x^2} dx$

 [Watch Video Solution](#)

184. Evaluate the following definite integral: $\int_0^1 \sqrt{x} dx$

 [Watch Video Solution](#)

185. Evaluate the following definite integral: $\int_0^4 \frac{1}{\sqrt{4x - x^2}} dx$

 [Watch Video Solution](#)

186. Evaluate the following definite integral: $\int_1^4 \frac{x^2 + x}{\sqrt{2x + 1}} dx$

 [Watch Video Solution](#)

187. Evaluate the following definite integral: $\int_1^2 \left(\frac{x - 1}{x^2} \right) e^x dx$

 [Watch Video Solution](#)

188. Evaluate the following definite integral: $\int_0^1 \left(xe^x + \frac{\cos(\pi x)}{4} \right) dx$

 [Watch Video Solution](#)

189. Evaluate the following definite integral: $\int_0^{2\pi} e^{x/2} \sin\left(\frac{x}{2} + \frac{\pi}{4}\right) dx$

 [Watch Video Solution](#)

190. Evaluate the definite integrals $\int_0^1 \frac{dx}{\sqrt{1+x} - \sqrt{x}}$

 [Watch Video Solution](#)

191. Evaluate the following definite integral: $\int_1^2 e^{2x} \left(\frac{1}{x} - \frac{1}{2x^2}\right) dx$

 [Watch Video Solution](#)

192. Evaluate the following definite integral: $\int_0^{\pi/2} x^2 \sin x dx$

 [Watch Video Solution](#)

193. Evaluate the following definite integral: $\int_0^{\pi/2} \cos^2 x \, dx$

 [Watch Video Solution](#)

194. Evaluate the following definite integral: $\int_1^2 \log x \, dx$

 [Watch Video Solution](#)

195. Evaluate the following definite integral: $\int_1^e \frac{e^x}{x} (1 + x \log x) dx$

 [Watch Video Solution](#)

196. Evaluate : $\int_e^{e^2} \left\{ \frac{1}{\log x} - \frac{1}{(\log x)^2} \right\} dx$

 [Watch Video Solution](#)

197. Evaluate the definite integrals $\int_0^1 \frac{2x + 3}{5x^2 + 1} dx$

 [Watch Video Solution](#)

198. Evaluate the following definite integral: $\int_0^1 \frac{1}{2x^2 + x + 1} dx$

 [Watch Video Solution](#)

199. Evaluate the following definite integral: $\int_0^2 \frac{1}{\sqrt{3 + 2x - x^2}} dx$

 [Watch Video Solution](#)

200. Evaluate the following definite integral: $\int_{-1}^1 \frac{1}{x^2 + 2x + 5} dx$

 [Watch Video Solution](#)

201. Evaluate : $\int_0^1 x(1-x)^5 dx$

 [Watch Video Solution](#)

202. Evaluate the following definite integral: $\int_0^1 \left(xe^{2x} + \frac{\sin(\pi x)}{2} \right) dx$

 [Watch Video Solution](#)

203. Evaluate the following definite integral: $\int_{\pi/2}^{\pi} e^x \left(\frac{1 - \sin x}{1 - \cos x} \right) dx$

 [Watch Video Solution](#)

204. Evaluate : $\int_0^{2\pi} e^x \cos\left(\frac{\pi}{4} + \frac{x}{2}\right) dx$

 [Watch Video Solution](#)

205. Evaluate the following definite integral: $\int_1^2 \frac{x}{(x+1)(x+2)} dx$

 [Watch Video Solution](#)

206. Evaluate the following definite integral: $\int_0^\pi \left(\frac{\sin^2 x}{2} - \frac{\cos^2 x}{2} \right) dx$

 [Watch Video Solution](#)

207. If $\int_0^k \frac{1}{2+8x^2} dx = \frac{\pi}{16}$, find the value of k .

 [Watch Video Solution](#)

208. If $\int_0^a 3x^2 dx = 8$, find the value of a .

 [Watch Video Solution](#)

209. Evaluate the following integral : $\int_{\pi}^{3\pi/2} \sqrt{1 - \cos 2x} \, dx$

 [Watch Video Solution](#)

210. Evaluate the following integral : $\int_0^{2\pi} \sqrt{1 + \sin\left(\frac{x}{2}\right)} \, dx$

 [Watch Video Solution](#)

211. Evaluate : $\int_0^{\frac{\pi}{4}} (\tan x + \cot x)^{-2} \, dx$

 [Watch Video Solution](#)

212. Evaluate the following integral : $\int_{\pi/6}^{\pi/3} (\tan x + \cot x)^2 \, dx$

 [Watch Video Solution](#)

213. Evaluate : $\int_0^1 \frac{1}{1 + 2x + 2x^2 + 2x^3 + x^4} dx$

 [Watch Video Solution](#)

214. Evaluate : $\int_0^1 x \log(1 + 2x) dx$

 [Watch Video Solution](#)

215. Evaluate: $\int_0^{\pi/2} \frac{1}{(a^2 \cos^2 x + b^2 \sin^2 x)^2} dx$

 [Watch Video Solution](#)

216. Evaluate: $\int_0^1 \sin^{-1} x dx$

 [Watch Video Solution](#)

217. Evaluate: $\int_0^{\pi/2} \sqrt{\cos \theta} \sin^3 \theta d\theta$

 [Watch Video Solution](#)

218. Evaluate: $\int_0^{\pi/2} \frac{1}{\cos^3 x \sqrt{2 \sin 2x}} dx$

 [Watch Video Solution](#)

219. Evaluate: $\int_0^{\pi/2} \frac{\cos \theta}{(1 + \sin \theta)(2 + \sin \theta)} d\theta$

 [Watch Video Solution](#)

220. Evaluate the following integral: $\int_0^{1/2} \frac{1}{(1 + x^2)\sqrt{1 - x^2}} dx$

 [Watch Video Solution](#)

221. Evaluate: $\int_0^a \frac{x^4}{\sqrt{a^2 - x^2}} dx$

 [Watch Video Solution](#)

222. Evaluate: $\int_0^1 \frac{x \tan^{-1} x}{(1 + x^2)^{3/2}} dx$

 [Watch Video Solution](#)

223. Evaluate: $\int \frac{\sin^{-1} x}{(1 - x^2)^{\frac{3}{2}}} dx$

 [Watch Video Solution](#)

224. Evaluate: $\int_0^1 \sin^{-1} \left(\frac{2x}{1 + x^2} \right) dx$

 [Watch Video Solution](#)

225. Evaluate: $\int_0^{\pi/4} \tan^3 x \, dx$

 [Watch Video Solution](#)

226. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{2 \cos x + 4 \sin x} dx$

 [Watch Video Solution](#)

227. Evaluate: $\int_0^{\pi} \frac{x}{1 + \cos^2 x} dx$

 [Watch Video Solution](#)

228. Evaluate: $\int_0^{\pi/2} \frac{1}{4 \sin^2 x + 5 \cos^2 x} dx$

 [Watch Video Solution](#)

229. Evaluate: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$

 [Watch Video Solution](#)

230. Evaluate: $\int_0^{\pi/2} \frac{\sin 2x}{\cos^4 x + \sin^4 x} dx$

 [Watch Video Solution](#)

231. Evaluate: $\int_0^{\pi/2} \frac{\cos^2 x}{\cos^2 x + 4 \sin^2 x} dx$

 [Watch Video Solution](#)

232. Evaluate the following integral: $\int_2^4 \frac{x}{x^2 + 1} dx$

 [Watch Video Solution](#)

233. Evaluate the following integral: $\int_1^2 \frac{1}{x(1 + \log x)^2} dx$

 [Watch Video Solution](#)

234. Evaluate the following integral: $\int_1^2 \frac{3x}{9x^2 - 1} dx$

 [Watch Video Solution](#)

235. Evaluate the following integral: $\int_0^a \frac{x}{\sqrt{a^2 + x^2}} dx$

 [Watch Video Solution](#)

236. Evaluate the following integral: $\int_0^1 x e^{x^2} dx$

 [Watch Video Solution](#)

237. Evaluate the following integral: $\int_0^1 \frac{2x}{1+x^4} dx$

 [Watch Video Solution](#)

238. Evaluate the following integral: $\int_1^2 \frac{1}{x(1+\log x)^2} dx$

 [Watch Video Solution](#)

239. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{5 \cos x + 3 \sin x} dx$

 [Watch Video Solution](#)

240. Evaluate the following integral: $\int_0^1 \frac{e^x}{1+e^{2x}} dx$

 [Watch Video Solution](#)

241. Evaluate the following integral: $\int_1^3 \frac{\cos(\log x)}{x} dx$

 [Watch Video Solution](#)

242. Evaluate the following integral: $\int_0^a \sqrt{a^2 - x^2} dx$

 [Watch Video Solution](#)

243. Evaluate the following integral: $\int_0^{\pi/2} \sqrt{\sin \varphi} \cos^5 \varphi d\varphi$

 [Watch Video Solution](#)

244. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin \theta}{\sqrt{1 + \cos \theta}} d\theta$

 [Watch Video Solution](#)

245. Evaluate the following integral: $\int_0^1 \frac{\sqrt{\tan^{-1} x}}{1+x^2} dx$

 [Watch Video Solution](#)

246. Evaluate the following integral: $\int_0^1 \tan^{-1} \left(\frac{2x}{1-x^2} \right) dx$

 [Watch Video Solution](#)

247. Evaluate the following integral: $\int_0^{\pi/2} \frac{dx}{a \cos x + b \sin x} x$

 [Watch Video Solution](#)

248. Evaluate the following integral: $\int_0^{\pi} \frac{\sin x}{\sin x + \cos x} dx$

 [Watch Video Solution](#)

249. Evaluate the following integral: $\int_0^1 \tan^{-1} x \, dx$

 [Watch Video Solution](#)

250. Evaluate the following integral: $\int_0^{\pi/4} (\sqrt{\tan x} + \sqrt{\cot x}) \, dx$

 [Watch Video Solution](#)

251. Evaluate the following integral: $\int_0^{\pi} \frac{1}{5 + 3 \cos x} \, dx$

 [Watch Video Solution](#)

252. Evaluate the following integral: $\int_0^{\pi/2} \frac{x + \sin x}{1 + \cos x} \, dx$

 [Watch Video Solution](#)

253. Evaluate the following integral: $\int_0^{\pi/4} \frac{\sin x + \cos x}{3 + \sin 2x} dx$

 [Watch Video Solution](#)

254. Evaluate the following integral: $\int_0^1 \frac{1 + x^2}{x^4 + x^2 + 1} dx$

 [Watch Video Solution](#)

255. Evaluate the following integral: $\int_4^{12} x(x - 4)^{1/3} dx$

 [Watch Video Solution](#)

256. Evaluate the following integral: $\int_{-1}^1 5x^4 \sqrt{x^5 + 1} dx$

 [Watch Video Solution](#)

257. Evaluate the following integral: $\int_0^{\pi/4} \sin^3 2t \cos 2t dt$

 [Watch Video Solution](#)

258. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos x}{1 + \sin^2 x} dx$

 [Watch Video Solution](#)

259. Evaluate the following integral: $\int_0^{\pi/3} \frac{\cos x}{3 + 4 \sin x} dx$

 [Watch Video Solution](#)

260. Evaluate the following integral: $\int_0^2 x \sqrt{x+2} dx$

 [Watch Video Solution](#)

261. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin x \cos x}{1 + \sin^4 x} dx$

 [Watch Video Solution](#)

262. Evaluate the following integral: $\int_0^{\pi} \frac{1}{5 + 4 \sin x} dx$

 [Watch Video Solution](#)

263. Evaluate the following integral: $\int_0^{\pi} \frac{1}{3 + 2 \sin x + \cos x} dx$

 [Watch Video Solution](#)

264. Evaluate the following integral: $\int_0^{1/2} \frac{x \sin^{-1} x}{\sqrt{1 - x^2}} dx$

 [Watch Video Solution](#)

265. Evaluate the following integral: $\int_0^{\pi/4} \frac{\tan^3 x}{1 + \cos 2x} dx$

 [Watch Video Solution](#)

266. Evaluate the following integral: $\int_0^{\pi} \frac{x}{a^2 \cos^2 x + b^2 \sin^2 x} dx$

 [Watch Video Solution](#)

267. Evaluate the following integral: $\int_0^1 \frac{\tan^{-1} x}{1 + x^2} dx$

 [Watch Video Solution](#)

268. Evaluate the following integral: $\int_0^1 x \tan^{-1} x dx$

 [Watch Video Solution](#)

269. Evaluate the following integral: $\int_0^{\pi/2} x^2 \sin x \, dx$

 [Watch Video Solution](#)

270. Evaluate the following integral: $\int_0^1 \frac{1-x^2}{(1+x^2)^2} dx$

 [Watch Video Solution](#)

271. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos^2 x}{1+3\sin^2 x} dx$

 [Watch Video Solution](#)

272. Evaluate the following integral: $\int_0^{\pi} 5(5-4\cos\theta)^{1/4} \sin\theta d\theta$

 [Watch Video Solution](#)

273. Evaluate the following integral: $\int_4^9 \frac{\sqrt{x}}{\left(30 - x^{\frac{3}{2}}\right)^2} dx$

 [Watch Video Solution](#)

274. Evaluate the following integral: $\int_0^\pi \sin^3 x (1 + 2 \cos x)(1 + \cos x)^2 dx$

 [Watch Video Solution](#)

275. Evaluate the following integral: $\int_0^{\pi/2} 2s \in x \cos x \tan^{-1}(\sin x) dx$

 [Watch Video Solution](#)

276. Evaluate the following integral: $\int_0^{\pi/2} s \in 2x \tan^{-1}(\sin x) dx$

 [Watch Video Solution](#)

277. $\int_0^a x \sqrt{\frac{a^2 - x^2}{a^2 + x^2}} dx$

 [Watch Video Solution](#)

278. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin x \cos x}{\cos^2 x + 3 \cos x + 2} dx$

 [Watch Video Solution](#)

279. Evaluate the following integral: $\int_0^{1/2} \frac{1}{(1 + x^2)\sqrt{1 - x^2}} dx$

 [Watch Video Solution](#)

280. Evaluate the following integral: $\int_0^1 (\cos^{-1} x)^2 dx$

 [Watch Video Solution](#)

281. Evaluate the following integral: $\int_{\pi/3}^{\pi/2} \frac{\sqrt{1 + \cos x}}{(1 - \cos x)^{3/2}} dx$

 [Watch Video Solution](#)

282. Evaluate the following integral: $\int_{-a}^a \sqrt{\frac{a+x}{a-x}} dx$

 [Watch Video Solution](#)

283. Evaluate the following integral: $\int_{1/3}^1 \frac{(x - x^3)^{1/3}}{x^4} dx$

 [Watch Video Solution](#)

284. Evaluate the following integral:

$$\int_0^{\pi/2} \sqrt{\cos x - \cos^3 x} (\sec^2 x - 1) \cos^2 x dx$$

 [Watch Video Solution](#)

285. Evaluate the following integral:

$$\int_0^9 f(x)dx, \text{ where } f(x) \begin{cases} \sin x, & 0 \leq x \leq \pi/2 \\ 1, & \frac{\pi}{2} \leq x \leq 3 \\ 3e^{x-3}, & 3 \leq x \leq 9 \end{cases}$$

 [Watch Video Solution](#)

286. Evaluate the following integral:

$$\int_2^4 f(x)dx, \text{ where } f(x) = \begin{cases} 7x + 3, & \text{if } 1 \leq x \leq 3 \\ 38x, & \text{if } 3 \leq x \leq 4 \end{cases}$$

 [Watch Video Solution](#)

287. Evaluate the following integral: $\int_{-4}^4 |x + 2|dx$

 [Watch Video Solution](#)

288. Evaluate the following integral: $\int_{-1}^1 |x + 1|dx$

 [Watch Video Solution](#)

289. Evaluate the following integral: $\int_{-6}^6 |x + 2| dx$

 [Watch Video Solution](#)

290. Evaluate the following integral: $\int_1^2 |x - 3| dx$

 [Watch Video Solution](#)

291. Evaluate the following integral: $\int_1^{2\pi} |s - x| dx$

 [Watch Video Solution](#)

292. Evaluate the following integral: $\int_2^8 |x - 5| dx$

 [Watch Video Solution](#)

293. Evaluate the following integral: $\int_0^4 |x - 1| dx$

 [Watch Video Solution](#)

294. Evaluate the following integral: $\int_0^4 (|x| + |x - 2| + |x - 4|) dx$

 [Watch Video Solution](#)

295. Evaluate the following integral: $\int_{-2}^2 x e^{|x|} dx$

 [Watch Video Solution](#)

296. Evaluate the following integral: $\int_{-\pi/2}^{\pi} \sin^{-1}(\sin x) dx$

 [Watch Video Solution](#)

297. Evaluate the following integral: $\int_{-3}^3 |x + 1| dx$

 [Watch Video Solution](#)

298. Evaluate the following integral: $\int_{-1}^2 |2x + 3| dx$

 [Watch Video Solution](#)

299. Evaluate the following integral: $\int_0^3 |3x - 1| dx$

 [Watch Video Solution](#)

300. Evaluate the following integral: $\int_{-2}^2 |x + 1| dx$

 [Watch Video Solution](#)

301. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} |s \in x| dx$

 [Watch Video Solution](#)

302. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} |\sin x + \cos x| dx$

 [Watch Video Solution](#)

303. Evaluate the following integral: $\int_1^4 \{|x - 1| + |x - 2| + |x - 4|\} dx$

 [Watch Video Solution](#)

304. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} (2 \sin|x| + \cos x) dx$

 [Watch Video Solution](#)

305. Evaluate of each of the following integral: $\int_0^{2\pi} \frac{dx}{e^{\sin x} + 1} dx$

 [Watch Video Solution](#)

306. Evaluate of each of the following integral: $\int_{-\pi/4}^{\pi/4} \frac{\tan^2 x}{1 + e^x} dx$

 [Watch Video Solution](#)

307. Evaluate of each of the following integral: $\int_{-\pi/3}^{\pi/3} \frac{1}{1 + e^x} dx$

 [Watch Video Solution](#)

308. Evaluate of each of the following integral:

$$\int_0^{\pi/2} (2 \log \cos x - \log s \in 2x) dx$$

 [Watch Video Solution](#)

309. Evaluate of each of the following integral: $\int_{\pi/6}^{\pi/3} \frac{1}{1 + \sqrt{\tan x}} dx$

 [Watch Video Solution](#)

310. Evaluate of each of the following integral: $\int_{-\pi/2}^{\pi/2} \frac{\cos^2 x}{1 + e^x} dx$

 [Watch Video Solution](#)

311. Evaluate of each of the following integral:

$$\int_a^b \frac{x^{1/n}}{x^{1/n} + (a + b - x)^{\frac{1}{n}}} dx, \quad n \in \mathbb{N}, \quad n \geq 2$$

 [Watch Video Solution](#)

312. Evaluate of each of the following integral: $\int_0^a \frac{\sqrt{x}}{\sqrt{x} + \sqrt{a-x}} dx$

 [Watch Video Solution](#)

313. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \frac{a + b}{2} \int_a^b f(x) dx$$

 [Watch Video Solution](#)

314. Evaluate: $\int_0^{\pi/2} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$

 [Watch Video Solution](#)

315. Evaluate: $\int_0^{\pi/2} \log \tan x dx$

 [Watch Video Solution](#)

316. Evaluate: $\int_0^{\pi/4} \log(1 + \tan x) dx$

 [Watch Video Solution](#)

317. Evaluate: $\int_0^{\pi/2} \frac{s \in x - \cos x}{1 + s \in x \cos x} dx$

 [Watch Video Solution](#)

318. Evaluate: $\int_0^{\pi/2} (2 \log \sin x - \log \sin 2x) dx$

 [Watch Video Solution](#)

319. Evaluate: $\int_0^{\pi} \frac{e^{\cos x}}{e^{\cos x} + e^{-\cos x}} dx$

 [Watch Video Solution](#)

320. Evaluate: $\int_0^1 x(1-x)^n dx$

 [Watch Video Solution](#)

321. Evaluate: $\int_0^1 \cot^{-1}(1 - x + x^2) dx$

 [Watch Video Solution](#)

322. If f and g are continuous on $[0, a]$ and satisfy $f(x) = f(a - x)$ and $g(x) + g(a - x) = 2$. show that

$$\int_0^a f(x)g(x)dx = \int_0^a f(x)dx$$

 [Watch Video Solution](#)

323. Evaluate: $\int_0^{2\pi} \frac{1}{1 + e^{\sin x}} dx$

 [Watch Video Solution](#)

324. Evaluate: $\int_0^{\pi} \frac{1}{1 + e^{\cos x}} dx$

 [Watch Video Solution](#)

325. Evaluate: $\int_0^{\pi} \frac{x}{a^2 \cos^2 x + b^2 \sin^2 x} dx$

 [Watch Video Solution](#)

326. Evaluate: $\int_0^{\pi} \frac{x \sin x}{1 + \cos^2 x} dx$

 [Watch Video Solution](#)

327. Evaluate: $\int_0^{\pi} \frac{x}{1 + \sin x} dx$

 [Watch Video Solution](#)

328. Evaluate: $\int_0^{\pi} \frac{x \tan x}{\sec x + \tan x} dx$

 [Watch Video Solution](#)

329. Evaluate: $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$



Watch Video Solution

330. Evaluate: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$



Watch Video Solution

331. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{1}{1 + e^{s \in x}} dx$



Watch Video Solution

332. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{1}{1 + e^{\sin x}} dx$



Watch Video Solution

333. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{\cos x}{1 + e^x} dx$



Watch Video Solution

334. Evaluate: $\int_{-\pi/2}^{\pi/2} \sin^7 x dx$

 [Watch Video Solution](#)

335. Evaluate: $\int_{-\pi/2}^{\pi/2} \sin^2 x dx$

 [Watch Video Solution](#)

336. Evaluate: $\int_{-\pi/2}^{\pi/2} |\sin x| dx$

 [Watch Video Solution](#)

337. Evaluate: $\int_{-\pi}^{\pi} (\cos ax + \sin bx)^2 dx$

 [Watch Video Solution](#)

338. Evaluate: $\int_{-1}^{3/2} |x \sin \pi x| dx$

 [Watch Video Solution](#)

339. Evaluate: $\int_0^{2\pi} \cos^5 x dx$

 [Watch Video Solution](#)

340. Prove that: $\int_0^{\pi/2} \log \sin x dx = \int_0^{\pi/2} \log \cos x dx = -\frac{\pi}{2} \log 2$

 [Watch Video Solution](#)

341. Evaluate: $\int_0^{\pi} \log(1 + \cos x) dx$

 [Watch Video Solution](#)

342. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan x}$



Watch Video Solution

343. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sqrt{\cot x}}{\sqrt{\cot x} + \sqrt{\tan x}} dx$



Watch Video Solution

344. Evaluate the following integral: $\int_0^a \frac{1}{x + \sqrt{a^2 - x^2}} dx$



Watch Video Solution

345. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \cot x} dx$



Watch Video Solution

346. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin^{3/2} x}{\sin^{3/2} x + \cos^{3/2} x} dx$



Watch Video Solution

347. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan x} dx$

 [Watch Video Solution](#)

348. Evaluate the following integral: $\int_0^{\infty} \frac{\log x}{1 + x^2} dx$

 [Watch Video Solution](#)

349. Evaluate the following integral: $\int_0^1 \frac{\log(1 + x)}{1 + x^2} dx$

 [Watch Video Solution](#)

350. Evaluate the following integral: $\int_0^{\pi} \frac{x \tan x}{\sec x \cos ec x} dx$

 [Watch Video Solution](#)

351. Evaluate the following integral: $\int_0^{\pi} x \sin^3 x \, dx$

 [Watch Video Solution](#)

352. Evaluate the following integral: $\int_0^{\pi} \frac{x \sin x}{1 + \sin x} dx$

 [Watch Video Solution](#)

353. Evaluate the following integral: $\int_0^{\pi/2} \frac{\tan^7 x}{\tan^7 x + \cot^7 x} dx$

 [Watch Video Solution](#)

354. Evaluate the following integral: $\int_0^{\pi/2} x \sin x \cos^2 x \, dx$

 [Watch Video Solution](#)

355. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^3 x \, dx$

 [Watch Video Solution](#)

356. Evaluate the following integral: $\int_{-1}^1 \log\left(\frac{2-x}{2+x}\right) dx$

 [Watch Video Solution](#)

357. Evaluate the following integral: $\int_0^{\pi} \log(1 - \cos x) dx$

 [Watch Video Solution](#)

358. Evaluate the following integral: $\int_{-\pi}^{\pi} \frac{2x(1 + \sin x)}{1 + \cos^2 x} dx$

 [Watch Video Solution](#)

359. Evaluate the following integral: $\int_0^2 x \sqrt{2-x} dx$

 [Watch Video Solution](#)

360. Evaluate the following integral: $\int_0^{\infty} \frac{x}{(1+x)(1+x^2)} dx$

 [Watch Video Solution](#)

361. Evaluate the following integral: $\int_0^{\pi} x \sin x \cos^4 x dx$

 [Watch Video Solution](#)

362. Evaluate the following integral: $\int_0^{\pi} x \log \sin x dx$

 [Watch Video Solution](#)

363. Evaluate the following integral: $\int_0^{\pi} x \log \sin x dx$



Watch Video Solution

364. Evaluate the following integral: $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \left(\frac{1}{1 + \cot^{\frac{3}{2}} x} \right) dx$,



Watch Video Solution

365. Evaluate the following integral: $\int_{\pi/6}^{\pi/3} \frac{1}{1 + \cot^{3/2} x} dx$



Watch Video Solution

366. Evaluate the following integral: $\int_2^8 \frac{\sqrt{10-x}}{\sqrt{x} + \sqrt{10-x}} dx$



Watch Video Solution

367. Evaluate the following integral: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$



Watch Video Solution

368. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^4 x \, dx$

 [Watch Video Solution](#)

369. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} \sin^2 x \, dx$

 [Watch Video Solution](#)

370. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \log\left(\frac{2 - \sin x}{2 + \sin x}\right) dx$

 [Watch Video Solution](#)

371. Evaluate the following integral:

$$\int_{-3\pi/2}^{-\pi/2} \left\{ \sin^2(3\pi + x) + (\pi + x)^3 \right\} dx$$

 [Watch Video Solution](#)

372. Evaluate the following integral: $\int_0^1 \log\left(\frac{1}{x} - 1\right) dx$

 [Watch Video Solution](#)

373. Evaluate the following integral: $\int_0^{2\pi} \sin^{100} x \cos^{101} x dx$

 [Watch Video Solution](#)

374. If f is an integrable function such that $f(2a - x) = f(x)$, then prove that $\int_0^{2a} f(x) dx = 2 \int_0^a f(x) dx$

 [Watch Video Solution](#)

375. If $f(2a - x) = -f(x)$, prove that $\int_0^{2a} f(x) dx = 0$

 [Watch Video Solution](#)

376. If f is an integrable function, show that

$$\int_{-a}^a f(x^2) dx = 2 \int_0^a f(x^2) dx$$

 [Watch Video Solution](#)

377. If f is an integrable function, show that $\int_{-a}^a x f(x^2) dx = 0$

 [Watch Video Solution](#)

378. If $f(x)$ is a continuous function defined on $[0, 2a]$. Then prove that

$$\int_0^{2a} f(x) dx = \int_0^a \{f(x) + (2a - x)\} dx$$

 [Watch Video Solution](#)

379. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \frac{a + b}{2} \int_a^b f(x) dx.$$

 [Watch Video Solution](#)

380. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \left(\frac{a + b}{2} \right) \int_a^b f(x) dx.$$



[Watch Video Solution](#)

381. Property 8: If $f(x)$ is a continuous function defined on $[-a; a]$ then

$$\int_{-a}^a f(x) dx = \int_0^a \{f(x) + f(-x)\} dx$$



[Watch Video Solution](#)

382. If $\int_0^\pi x f(\sin x) dx = A \int_0^{\frac{\pi}{2}} f(\sin x) dx$, then A is (A) $\frac{\pi}{2}$ (B) π (C) 0
(D) 2π



[Watch Video Solution](#)

383. Evaluate the following integrals as limit of sum: $\int_0^2 (x + 4) dx$



Watch Video Solution

384. Evaluate the following integrals as limit of sum: $\int_0^2 (2x + 1)dx$



Watch Video Solution

385. Evaluate the following integrals as limit of sum: $\int_0^3 (x + 4)dx$



Watch Video Solution

386. Evaluate the following integrals as limit of sum: $\int_1^3 (3x - 2)dx$



Watch Video Solution

387. Evaluate the following integrals as limit of sum: $\int_1^3 (3x - 2)dx$



Watch Video Solution

388. Evaluate the following definite integrals as limit of sums.

$$\int_0^5 (x + 1) dx$$

 [Watch Video Solution](#)

389. Evaluate the following integrals as limit of sum: $\int_3^5 (2 - x) dx$

 [Watch Video Solution](#)

390. Evaluate the definite integrals as limit of sums $\int_1^2 x^2 dx$

 [Watch Video Solution](#)

391. Evaluate the following integrals as limit of sum: $\int_1^2 (x^2 - 1) dx$

 [Watch Video Solution](#)

392. Evaluate the following integrals as limit of sum: $\int_0^2 (x + 3)dx$

 [Watch Video Solution](#)

393. Evaluate the following integrals as limit of sum: $\int_{-1}^1 (x + 3)dx$

 [Watch Video Solution](#)

394. Evaluate the following integrals as limit of sum: $\int_1^3 (2x + 3)dx$

 [Watch Video Solution](#)

395. Evaluate the following integrals as limit of sum: $\int_1^3 (2x + 3)dx$

 [Watch Video Solution](#)

396. Evaluate the following integrals as limit of sum: $\int_0^2 (x^2 + 1)dx$

 [Watch Video Solution](#)

397. Evaluate the following integrals as limit of sum: $\int_2^3 (2x^2 + 1) dx$

 [Watch Video Solution](#)

398. Evaluate the following integrals as limit of sum: $\int_0^2 (x^2 + 4) dx$

 [Watch Video Solution](#)

399. Evaluate the following integrals as limit of sum: $\int_1^4 (x^2 - x) dx$

 [Watch Video Solution](#)

400. Evaluate the following integrals as limit of sum: $\int_0^2 e^x dx$

 [Watch Video Solution](#)

401. Evaluate the following integrals using limit of sum.

$$\int_a^b \cos x dx$$

 [Watch Video Solution](#)

402. Evaluate the following integrals as limit of sum: $\int_0^{\pi/2} \cos x dx$

 [Watch Video Solution](#)

403. Evaluate the following integrals as limit of sum: $\int_0^2 (3x^2 - 2) dx$

 [Watch Video Solution](#)

404. Evaluate the following definite integrals as limit of sums.

$$\int_0^4 (x + e^{2x}) dx$$

 [Watch Video Solution](#)

405. Evaluate $\int_0^2 (x^2 + 2x + 1) dx$ as limit of a sum.

 [Watch Video Solution](#)

406. Evaluate the following definite integrals as limit of sums. $\int_a^b x dx$

 [Watch Video Solution](#)

407. Evaluate the following integrals as limit of sum: $\int_2^3 x^2 dx$

 [Watch Video Solution](#)

408. Evaluate the following definite integrals as limit of sums. $\int_2^3 x^2 dx$

 [Watch Video Solution](#)

409. Evaluate the following integrals as limit of sum: $\int_0^2 (x^2 - x) dx$

 [Watch Video Solution](#)

410. Evaluate the following integrals as limit of sum: $\int_1^3 (3x^2 + 1) dx$

 [Watch Video Solution](#)

411. Evaluate the following integrals as limit of sum: $\int_0^1 (3x^2 + 5x) dx$

 [Watch Video Solution](#)

412. Evaluate the following integrals as limit of sum: $\int_0^2 e^x dx$

 [Watch Video Solution](#)

413. Evaluate the following integrals as limit of sum: $\int_0^{\pi/2} \sin x \, dx$

 [Watch Video Solution](#)

414. Evaluate the following definite integrals as limit of sum:

$$\int_0^2 (x^2 + 2) \, dx$$

 [Watch Video Solution](#)

415. Evaluate the following integrals as limit of sum: $\int_1^4 (3x^2 + 2x) \, dx$

 [Watch Video Solution](#)

416. Evaluate the following integral: $\int_0^2 (x^2 + x) \, dx$

 [Watch Video Solution](#)

417. Evaluate the following integrals as limit of sum:

$$\int_0^3 (2x^2 + 3x + 5) dx$$

 [Watch Video Solution](#)

418. Evaluate the following definite integrals as limit of sums.

$$\int_0^5 (x + 1) dx$$

 [Watch Video Solution](#)

419. Evaluate the following definite integrals as limit of sums.

$$\int_0^4 (x^2 - x) dx$$

 [Watch Video Solution](#)

420. Evaluate: $\int_1^3 (2x^2 + 5x) dx$ as limit of a sum.

 [Watch Video Solution](#)

421. Evaluate each of the following integral: $\int_0^{\pi/2} \sin^2 x \, dx$

 [Watch Video Solution](#)

422. Examples: $\int_{-\pi/2}^{\pi/2} \sin^2 x \, dx$

 [Watch Video Solution](#)

423. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} \sin^3 x \, dx$

 [Watch Video Solution](#)

424. Evaluate each of the following integral: $\int_0^{\pi/4} \tan^2 x \, dx$

 [Watch Video Solution](#)

425. Evaluate each of the following integral: $\int_{-2}^1 \frac{|x|}{x} dx$

 [Watch Video Solution](#)

426. Evaluate each of the following integral: $\int_0^4 \frac{1}{\sqrt{16-x^2}} dx$

 [Watch Video Solution](#)

427. Evaluate: $\int_0^{\pi/2} \sqrt{1-\cos 2x} dx$.

 [Watch Video Solution](#)

428. Evaluate each of the following integral: $\int_0^{\pi/2} \log\left(\frac{3+5\cos x}{3+5\sin x}\right) dx$

 [Watch Video Solution](#)

429. Evaluate each of the following integral: $\int_0^{\pi} \cos^5 x \, dx$

 [Watch Video Solution](#)

430. Evaluate each of the following integral: $\int_{-1}^1 x|x| \, dx$

 [Watch Video Solution](#)

431. Evaluate the following definite integral: $\int_0^1 \frac{1}{1+x^2} \, dx$

 [Watch Video Solution](#)

432. Evaluate each of the following integral: $\int_2^3 \frac{1}{x} \, dx$

 [Watch Video Solution](#)

433. Evaluate each of the following integral: $\int_0^1 \frac{2x}{1+x^2} dx$

 [Watch Video Solution](#)

434. Evaluate each of the following integral: $\int_0^{\pi/4} \sin 2x \, dx$

 [Watch Video Solution](#)

435. Evaluate each of the following integral: $\int_0^{\pi/2} \cos^2 x \, dx$

 [Watch Video Solution](#)

436. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} \cos^2 x \, dx$

 [Watch Video Solution](#)

437. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} x \cos^2 x \, dx$

 [Watch Video Solution](#)

438. Evaluate the following definite integral: $\int_0^{\frac{1}{2}} \frac{1}{\sqrt{1+x^2}} \, dx$

 [Watch Video Solution](#)

439. Evaluate each of the following integral: $\int_0^{\infty} e^{-x} \, dx$

 [Watch Video Solution](#)

440. Evaluate each of the following integral: $\int_0^3 \frac{1}{x^2 + 9} \, dx$

 [Watch Video Solution](#)

441. Evaluate each of the following integral: $\int_0^{\pi/2} \log \tan x dx$

 [Watch Video Solution](#)

442. Evaluate the following integrals: (1-35) $\int_0^{\pi/2} \frac{\sin^n x}{\sin^n + \cos^n x} dx$

 [Watch Video Solution](#)

443. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} \log \left(\frac{a - \sin \theta}{a + \sin \theta} \right) d\theta$

 [Watch Video Solution](#)

444. Evaluate each of the following integral: $\int_a^b \frac{f(x)}{f(x) + f(a + b - x)} dx$

 [Watch Video Solution](#)

445. Evaluate each of the following integral: $\int_0^2 \sqrt{4 - x^2} dx$

 [Watch Video Solution](#)

446. Evaluate each of the following integral: $\int_0^1 x e^{x^2} dx$

 [Watch Video Solution](#)

447. Evaluate each of the following integral: $\int_e^{e^2} \frac{1}{x \log x} dx$

 [Watch Video Solution](#)

448. Evaluate each of the following integral: $\int_0^{\pi/2} e^x (\sin x - \cos x) dx$

 [Watch Video Solution](#)

449. Evaluate each of the following integral: $\int_2^4 \frac{x}{x^2 + 1} dx$

 [Watch Video Solution](#)

450. If $\int_0^1 (3x^2 + 2x + k) dx = 0$, find the value of k .

 [Watch Video Solution](#)

451. If $\int_0^a 3x^2 dx = 8$, write the value of ' a '.

 [Watch Video Solution](#)

452. If $f(x) = \int_0^x t \sin t dt$, then write the value of $f'(x)$

 [Watch Video Solution](#)

453. If $\int_0^a \frac{1}{4+x^2} dx = \frac{\pi}{8}$, find the value of a .

 [Watch Video Solution](#)

454. The value of $\int_{-2}^2 (ax^3 + bx + c) dx$ depends on (A) the value of b
(B) the value of c (C) the value of a (D) the value of a and b

 [Watch Video Solution](#)

455. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^2 [x] dx$

 [Watch Video Solution](#)

456. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^1 \{x\} dx$

 [Watch Video Solution](#)

457. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^2 x[x] dx$

 [Watch Video Solution](#)

458. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral:

$$\int_1^2 (\log)_e [x] dx$$

 [Watch Video Solution](#)

459. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^{15} [x] dx$

 [Watch Video Solution](#)

460. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^1 e^{[x]} dx$

 [Watch Video Solution](#)

461. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^1 2^{x - [x]} dx$

 [Watch Video Solution](#)

462. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^{\sqrt{2}} [x^2] dx$

 [Watch Video Solution](#)

463. The value of $\int_0^{\pi/2} \frac{\sqrt{\cos x}}{\sqrt{\cos x} + \sqrt{\sin x}} dx$ is $\pi/2$ b. $\pi/4$ c. 0 d. none of these



Watch Video Solution

464. $\int_0^{\frac{\pi}{2}} \frac{1}{1 + \sin x} dx$ equals 0 b. $1/2$ c. 2 d. $3/2$



Watch Video Solution

465. $\int_0^{\infty} \frac{1}{1 + e^x} dx$ equals a. $\log 2 - 1$ b. $\log 2$ c. $\log 4 - 1$ d. $\log 2$



Watch Video Solution

466. The value of $\int_0^{2\pi} \sqrt{1 + \sin\left(\frac{x}{2}\right)} dx$ is 0 b. 4 c. 2 d. 8



Watch Video Solution

467. $\int_0^{\pi^2/4} \frac{\sin \sqrt{x}}{\sqrt{x}} dx$ equals

a. $\pi^2/8$

b. $\pi/4$

c. 2

d. 1

 [Watch Video Solution](#)

468. $\int_0^{\pi/2} \frac{1}{2 + \cos x} dx$ equals $\frac{1}{3} \tan^{-1} \left(\frac{1}{\sqrt{3}} \right)$ b. $\frac{2}{\sqrt{3}} \tan^{-1} \left(\frac{1}{\sqrt{3}} \right)$ c. $\sqrt{3} \tan^{-1} (\sqrt{3})$ d. $2\sqrt{3} \tan^{-1} \sqrt{3}$

 [Watch Video Solution](#)

469. $\frac{36}{\pi} \int_{\pi/6}^{\pi/3} \frac{dx}{1 + \sqrt{\cot x}}$ equals to

 [Watch Video Solution](#)

470. Given that

$\int_0^{\infty} \frac{x^2}{(x^2 + a^2)(x^2 + b^2)(x^2 + c^2)} dx = \frac{\pi}{2(a + b)(b + c)(c + a)}$ the

value of $\int_0^{\infty} \frac{dx}{(x^2 + 4)(x^2 + 9)}$, is $\frac{\pi}{60}$ b. $\frac{\pi}{40}$ c. $\frac{\pi}{20}$ d. $\frac{\pi}{80}$



Watch Video Solution

471. $\int_1^e \log x \, dx = 1$ b. $e - 1$ c. $e + 1$ d. 0



Watch Video Solution

472. $\int_1^{\sqrt{3}} \frac{1}{1+x^2} dx$ is equal to $\frac{\pi}{12}$ b. $\frac{\pi}{4}$ c. $\frac{\pi}{6}$ d. $\frac{\pi}{3}$



Watch Video Solution

473. The value of $\int_0^{\pi/2} \cos x e^{\sin x} dx$ is 1 b. $e - 1$ c. 0 d. -1



Watch Video Solution

474. If $\int_0^a \frac{1}{1+4x^2} dx = \frac{\pi}{8}$, then a equals $\frac{\pi}{2}$ b. $\frac{\pi}{4}$ c. $\frac{1}{2}$ d. 1

 [Watch Video Solution](#)

475.

$$\int_0^1 f(x) dx = 1, \int_0^1 x f(x) dx = a, \int_0^1 x^2 f(x) dx = a^2, \text{ then } \int_0^1 (a - x)^2$$

equals a. $4a^2$ b. 0 c. $2a^2$ d. none of these

 [Watch Video Solution](#)

476. The value of $\int_{-\pi}^{\pi} \sin^3 x \cos^2 x dx$ is $\frac{\pi^4}{2}$ b. $\frac{\pi^4}{4}$ c. 0 d. none of these

 [Watch Video Solution](#)

477. $\int_{\pi/6}^{\pi/3} \frac{1}{\sin 2x} dx$ is equal to $(\log)_e 3$ b. $(\log)_e \sqrt{3}$ c. $\frac{1}{2} \log(-1)$ d.

$\log(-1)$

 [Watch Video Solution](#)

478. $\int_{-1}^1 |1 - x| dx$ is equal to -2 b. 2 c. 0 d. 4

 [Watch Video Solution](#)

479. $(\lim)_{n \rightarrow \infty} \left\{ \frac{1}{2n+1} + \frac{1}{2n+2} + \dots + \frac{1}{2n+n} \right\}$ $\ln\left(\frac{1}{3}\right)$ b.
 $\ln\left(\frac{2}{3}\right)$ c. $\ln\left(\frac{3}{2}\right)$ d. $\ln\left(\frac{4}{3}\right)$

 [Watch Video Solution](#)

480. The value of the integral $\int_{-2}^2 |1 - x^2| dx$ is 4 b. 2 c. -2 d. 0

 [Watch Video Solution](#)

481. $\int_0^{\pi/2} \frac{1}{1 + \cot^3 x} dx$ is equal to 0 b. 1 c. $\pi/2$ d. $\pi/4$

 [Watch Video Solution](#)

482. $\int_0^{\pi/2} \frac{\sin x}{\sin x + \cos x} dx$ equals to $\pi/2$ b. $\pi/4$ c. $\pi/3$ d. π

 [Watch Video Solution](#)

483. $\int_0^{\pi/2} x \sin x dx$ is equal to $\pi/2$ b. $\pi/4$ c. π d. 1

 [Watch Video Solution](#)

484. $\int_0^{\pi/2} \sin 2x \log \tan x dx$ is equal to $\pi/2$ b. π c. 0 d. 2π

 [Watch Video Solution](#)

485. The value of $\int_0^{\pi} \frac{1}{5 + 3 \cos x} dx$ is $\pi/2$ b. $\pi/4$ c. 0 d. $\pi/8$

 [Watch Video Solution](#)

486. $\int_0^{\infty} \log \left(x + \frac{1}{x} \right) \frac{dx}{1 + x^2}$



Watch Video Solution

487. $\int_0^{2a} f(x)dx$ is equal to $2\int_0^a f(x)dx$ b. 0 c. $\int_0^a f(x)dx + \int_0^a f(2a-x)dx$ d. $\int_0^a f(x)dx + \int_0^{2a} f(2a-x)dx$



Watch Video Solution

488. If $f(a+b-x) = f(x)$, then $\int_a^b xf(x)dx$ is equal to $\frac{a+b}{2} \int_a^b f(b-x)dx$ b. $\frac{a+b}{2} \int_a^b f(b+x)dx$ c. $\frac{b-1}{2} \int_a^b f(x)dx$ d. $\frac{a+b}{2} \int_a^b f(x)dx$



Watch Video Solution

489. The value of $\int_0^1 \tan^{-1}\left(\frac{2x-1}{1+x-x^2}\right)dx$, is 1 b. -1 c. 0 d. $\pi/4$



Watch Video Solution

490. Choose the correct answer The value of $\int_0^{\frac{\pi}{2}} \log\left(\frac{4 + 3 \sin x}{4 + 3 \cos x}\right) dx$

(A) 2 (B) $\frac{3}{4}$ (C) 0 (D) -2

 [Watch Video Solution](#)

491. The value of $\int_{\pi/2}^{\pi/2} (x^3 + x \cos x + \tan^5 x + 1) dx$, is 2 b. π c. 0 d. 1

 [Watch Video Solution](#)

492. Evaluate the following integral: $\int_0^4 x \sqrt{4-x} dx$

 [Watch Video Solution](#)

493. Evaluate the following integral: $\int_1^5 \frac{x}{\sqrt{2x-1}} dx$

 [Watch Video Solution](#)

494. Evaluate the following integral: $\int_0^1 \tan^{-1} x \, dx$

 [Watch Video Solution](#)

495. Evaluate the following integral: $\int_0^1 \tan^{-1} \left(\frac{2x}{1-x^2} \right) dx$

 [Watch Video Solution](#)

496. Evaluate the following integral: $\int_0^1 \frac{1-x}{1+x} dx$

 [Watch Video Solution](#)

497. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin^2 x}{(1 + \cos x)^2} dx$

 [Watch Video Solution](#)

498. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos x}{1 + \sin^2 x} dx$

 [Watch Video Solution](#)

499. Evaluate the following integrals: $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx$

 [Watch Video Solution](#)

500. Evaluate the following integral: $\int_0^{\pi/4} \cos^4 x \sin^3 x dx$

 [Watch Video Solution](#)

501. Evaluate the following integral: $\int_0^{\pi/2} x^2 \cos 2x dx$

 [Watch Video Solution](#)

502. Evaluate the following integral: $\int_2^4 \frac{x^2 + x}{\sqrt{2x + 1}} dx$

 [Watch Video Solution](#)

503. $\int_0^1 (\cos^{-1} x)^2 dx$

 [Watch Video Solution](#)

504. Evaluate the following integral: $\int_1^2 x \sqrt{3x - 2} dx$

 [Watch Video Solution](#)

505. Evaluate the following integral: $\int_0^1 \cos^{-1} x dx$

 [Watch Video Solution](#)

506. Evaluate the following integral: $\int_0^1 \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right) dx$

 [Watch Video Solution](#)

507. Evaluate the following integral: $\int_0^{1/\sqrt{3}} \tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right) dx$

 [Watch Video Solution](#)

508. If $\int_0^{\frac{\pi}{3}} \frac{\cos x}{3+4\sin x} dx = k \log\left(\frac{3+2\sqrt{3}}{3}\right)$, then k is equal to

 [Watch Video Solution](#)

509. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin x}{\sqrt{1+\cos x}} dx$

 [Watch Video Solution](#)

510. $\int_0^{\pi} \sin^3 x (1 + 2 \cos x)(1 + \cos x)^2 dx$

 [Watch Video Solution](#)

511. Evaluate the following integral: $\int_0^{\pi/4} \sin 2x \sin 3x dx$

 [Watch Video Solution](#)

512. Evaluate the following integral: $\int_1^2 \frac{1}{x^2} e^{-1/x} dx$

 [Watch Video Solution](#)

513. Evaluate the following integral: $\int_0^1 \log(1 + x) dx$

 [Watch Video Solution](#)

514. Evaluate: $\int_0^1 x (\tan^{-1} x)^2 dx$

 [Watch Video Solution](#)

515. Evaluate the following integral: $\int_1^2 \frac{x+3}{x(x+2)} dx$

 [Watch Video Solution](#)

516. Evaluate the following integral: $\int_0^{\pi/4} e^x \sin x dx$

 [Watch Video Solution](#)

517. Evaluate the following integral: $\int_0^1 |2x - 1| dx$

 [Watch Video Solution](#)

518. Evaluate the following integral: $\int_0^{\pi/2} |\sin x - \cos x| dx$

 [Watch Video Solution](#)

519. Evaluate the following integral: $\int_1^3 |x^2 - 4| dx$

 [Watch Video Solution](#)

520. Evaluate: $\int_{-\frac{1}{2}}^{\frac{1}{2}} \cos x \log\left(\frac{1-x}{1+x}\right) dx$

 [Watch Video Solution](#)

521. By using the properties of definite integrals, evaluate the integrals

$$\int_0^a \frac{\sqrt{x}}{\sqrt{x} + \sqrt{a-x}} dx$$

 [Watch Video Solution](#)

522. Evaluate $\int_0^{\pi} \frac{x \sin x}{1 + \cos^2 x} dx$

 [Watch Video Solution](#)

523. $\int_0^{\pi} \frac{x}{a^2 \cos^2 x + b^2 \sin^2 x} dx$

 [Watch Video Solution](#)

524. Evaluate the following integral: $\int_0^{15} [x^2] dx$

 [Watch Video Solution](#)

525. Evaluate : $\int_0^{\frac{\pi}{2}} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$

 [Watch Video Solution](#)

526. Evaluate: $\int_0^{\pi} \frac{x \tan x}{\sec x + \tan x} dx$



Watch Video Solution

527. Evaluate the following integral: $\int_0^{\pi} \cos 2x \log \sin x \, dx$



Watch Video Solution

528. Evaluate the following integral: $\int_{-\pi}^{\pi} x^{10} \sin^7 x \, dx$



Watch Video Solution

529. Evaluate the following integral: $\int_0^{\pi} \frac{dx}{6 - \cos x}$



Watch Video Solution

530. Evaluate the following integral: $\int_0^{\pi/4} \tan^4 x \, dx$



Watch Video Solution

531. Evaluate the following integral: $\int_1^3 |x^2 - 2x| dx$

 [Watch Video Solution](#)

532. Evaluate the following integral: $\int_0^1 |\sin 2\pi x| dx$

 [Watch Video Solution](#)

533. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^9 x dx$

 [Watch Video Solution](#)

534. Evaluate the following integral: $\int_0^{2\pi} \cos^7 x dx$

 [Watch Video Solution](#)

535. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan^3 x} dx$

 [Watch Video Solution](#)

536. Evaluate the following integral: $\int_0^{\pi} x \sin x \cos^4 x dx$

 [Watch Video Solution](#)

537. Evaluate the following integral: $\int^{\pi/4} |\tan x| dx$

 [Watch Video Solution](#)

538. Evaluate the following integral: $\int_0^{\pi} \frac{x}{1 + \cos \alpha s \in x} dx$

 [Watch Video Solution](#)

539. Evaluate the following integral: $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$

 [Watch Video Solution](#)

540. Evaluate the following integral: $\int_{-\pi}^{\pi} x^{10} \sin^7 x dx$

 [Watch Video Solution](#)

541. Evaluate the following integral: $\int_0^{\pi} \frac{dx}{6 - \cos x}$

 [Watch Video Solution](#)

542. Evaluate the following integral: $\int_0^{\pi/4} \tan^4 x dx$

 [Watch Video Solution](#)

543. Evaluate the following integral: $\int_1^3 |x^2 - 2x| dx$

 [Watch Video Solution](#)

544. Evaluate the following integral: $\int_0^\pi |\sin^2 x| dx$

 [Watch Video Solution](#)

545. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^9 x dx$

 [Watch Video Solution](#)

546. Evaluate the following integrals: $\int_0^\pi \left(\frac{x}{1 + \sin^2 x} + \cos^7 x \right) dx$

 [Watch Video Solution](#)

547. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan^3 x} dx$

 [Watch Video Solution](#)

548. Evaluate the following integral: $\int_0^{\pi} x \sin x \cos^4 x dx$

 [Watch Video Solution](#)

549. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} |\sin x| dx$

 [Watch Video Solution](#)

550. Evaluate the following integral: $\int_0^{\pi} \frac{x}{1 + \cos \alpha \sin x} dx$

 [Watch Video Solution](#)

551. Evaluate the following integral: $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$

 [Watch Video Solution](#)

552. Evaluate $\int_0^{\pi} \frac{x}{a^2 - \cos^2 x} dx$

 [Watch Video Solution](#)

553. The value of $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x} + \sqrt{x}} dx$ is --

 [Watch Video Solution](#)

554. Evaluate the following integral: $\int_0^{\pi/2} x \sin x + \cos^2 x$

 [Watch Video Solution](#)

555. $\int_0^1 \cot^{-1}(1 - x + x^2) dx$

 [Watch Video Solution](#)

556. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{2 \cos x + 4 \sin x} dx$

 [Watch Video Solution](#)

557. Evaluate the following integral: $\int_{\pi/6}^{\pi/2} \frac{\operatorname{cosec} x \cot x}{1 + \operatorname{cosec}^2 x} dx$

 [Watch Video Solution](#)

558. Evaluate the following integral: $\int_0^{\pi/2} \frac{dx}{4 \cos x + 2 \sin x}$

 [Watch Video Solution](#)

559. Evaluate the following definite integrals as limit of sum: $\int_0^4 x \, dx$

 [Watch Video Solution](#)

560. Evaluate the following definite integrals as limit of sum:

$$\int_1^4 (x^2 + x) \, dx$$

 [Watch Video Solution](#)

561. Evaluate the following definite integrals as limit of sums. $\int_{-1}^1 e^x \, dx$

 [Watch Video Solution](#)

562. Evaluate the following definite integrals as limit of sum:

$$\int_1^3 (x^2 + 3x) \, dx$$

 [Watch Video Solution](#)

563. Evaluate the following definite integrals as limit of sum:

$$\int_0^2 (2x^2 + 3) dx$$

 [Watch Video Solution](#)

564. Evaluate the following definite integrals as limit of sum: $\int_{-1}^1 (e^{2x} dx)$

 [Watch Video Solution](#)

565. Evaluate: $\int_1^3 (2x^2 + 5x) dx$ as limit of a sum

 [Watch Video Solution](#)

566. Evaluate the following definite integrals as limit of sum:

$$\int_0^2 (x^2 + 2) dx$$

 [Watch Video Solution](#)

567. Evaluate the following definite integrals as limit of sum:

$$\int_0^3 (x^2 + 1) dx$$

 [Watch Video Solution](#)

Others

1. The derivative of $f(x) = \int_{x^2}^{x^3} \frac{1}{(\log)_e t} dt$, ($x > 0$), is $\frac{1}{3 \ln x}$ (b) $\frac{1}{3 \ln x} - \frac{1}{2 \ln x}$ (c) $(\ln x)^{-1} x(x-1)$ (d) $\frac{3x^2}{\ln x}$

 [View Text Solution](#)

2. Evaluate the following integral: $\int_{-\pi/4}^{\pi/2} \sin|\sin x| dx$

 [View Text Solution](#)