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## MATHS

## BOOKS - RD SHARMA MATHS (HINGLISH)

## FUNCTION

## Solved Examples And Exercises

1. Find gofandfog wehn $f: R \vec{R}$ and $g: R \vec{R}$ are defined by $f(x)=2 x+3 \quad$ and $g(x)=x^{2}+5 \quad f(x)=2 x+x^{2} \quad$ and $\quad g(x)=x^{3}$ $f(x)=x^{2}+8$ and $g(x)=3 x^{3}+1 f(x)=8 x^{3}$ and $g(x)=x^{1 / 3}$

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2. Let $f=\{(1,-1),(4,-2),(9,-3),(16,4)\} \quad$ and $g=\{(-1,-2),(02,-4),(-3,-6),(4,8)\}$. Show that gof is
defined while $f o g$ is not defined. Also, find gof.

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3. Show that if $f_{1} a n d f_{1}$ are one-one maps from $R \rightarrow R$, then the product $f_{1} x f_{2}: R \vec{R}$ defined by $\left(f_{1} x f_{2}\right)(x)=f_{1}(x) f_{2}(x)$ need not be one-one.

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4. Give examples of two surjective function $f_{1} a n d f_{2}$ from $Z \rightarrow Z$ such that $f_{1}+f_{2}$ is not surjective.

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5. Given examples of two one-one functions $f_{1}$ and $f_{2}$ from $R$ to $R$ such that $f_{1}+f_{2}: R \vec{R}$, defined by $\left(f_{1}+f_{2}\right)(x)=f_{1}(x)+f_{2}(x)$ is not oneone.
6. If $f: A \rightarrow B$ and $g: B \rightarrow C$ are onto functions show that gof is an onto function.

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7. Show that the logarithmic function $f: R 0+\vec{R}$ given by $f(x)=(\log )_{a} x, a>0$ is bijection.

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8. If $f: A \vec{B}$ andg: $B \vec{C}$ are one-one functions, show that gof is one-one function.

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9. If $f: R \vec{R}$ be the function defined by $f(x)=4 x^{3}+7$, show that $f$ is a bijection.

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10. Let $A=\{1,2,3\}$. Write all one-one from $A$ to itself.

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11. Show that $f: R \vec{R}$, given by $f(x)=x-[x]$, is neither one-one nor onto.

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12. Suppose $f_{1}$ and $f_{2}$ are non=zero one-one functions from $R \rightarrow R$ is $\frac{f_{1}}{f_{2}}$ necessarily one-one? Justify your answer. Here, $\frac{f_{1}}{f_{2}}: R \vec{R}$ is given by $\left(\frac{f_{1}}{f_{2}}\right)(x)=\frac{f_{1}(x)}{f_{2}(x)}$ for all $x R$.
13. Let $f=\{(3,1),(9,3),(12,4)\}$ and $=\{(1,3),(3,3),(4,9)$, $(5,9)\}$. Show that gof and fog are both defined. Also, find fog and gof.

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14. Find $f \circ g(2)$ and $g \circ f(1)$ when: $f: R \rightarrow R ; f(x)=x^{2}+8$ and $g: R \rightarrow R ; g(x)=3 x^{3}+1$.

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15. Let $f: R \vec{R}$ and $g: R \vec{R}$ be defined by $f(x)=x^{2}$ and $g(x)=x+1$. Show that fog $\neq$ gof.

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16. Let $R^{+}$be the set of all non-negative real numbers. if $f: R^{+} \rightarrow R^{+}$ and $g: R^{+} \rightarrow R^{+}$are defined as $f(x)=x^{2}$ and $g(x)=+\sqrt{x}$. Find $f o g$ and $g o f$. Are they equal functions.

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17. Verify assoiativity for the following three mappings : $f: N \vec{Z}_{0}$ (the set of non zero integers), $g: Z_{0} \vec{Z}$ and $h: Q \vec{R}$ given by $f(x)=2 x, g(x)=\frac{1}{x}$ and $h(x)=e^{x}$.

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18. Let $f: R \rightarrow R$ and $g: R \rightarrow R$ be defined by $f(x)=x+1$ and $g(x)=x-1$. Show that $f o g=g o f=I_{R}$.

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19. Show that the exponential function $f: R \vec{R}$, given by $f(x)=e^{x}$, is one-one but not onto. What happens if the co-domain is replaced by $R_{0}^{+}$ (set of all positive real numbers).

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20. Let $A=\{-1,0,1)$ and $f=\left\{\left(x, x^{2}\right): x A\right\}$. Show that $f: A \vec{A}$ is neither one-one nor onto.

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21. If $f: A \vec{B}$ is an injection such that range of $f=\{a\}$. Determine the number of elements in $A$.

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22. Which of the following functions from $A \rightarrow B$ are one-one and onto?
$f_{1}=\{(1,3),(2,5),(3,7)\} ; A=\{1,2,3\}, B=\{3,5,7\}$
$f_{2}=\{(2, a),(3, b),(4, c)\} ; A=\{2,3,4\}, B=\{a, b, c\}$
$f_{3}=\{(a, x),(b, x),(c, z),(d, z)\} ; A=\{a, b, c, d\}, B=\{x, y, z\}$

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23. Prove that the function $F: N \vec{N}$, defined by $f(x)=x^{2}+x+1$ is one-one but not onto.

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24. Let A be any non-empty set. Then, prove that the identity function on set A is a bijection.

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25. Let $A=R-[2] \operatorname{and} B=R-[1]$. If $f: A \vec{B}$ is a mapping defined by $f(x)=\frac{x-1}{x-2}$, show that $f$ is bijective.

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26. Show that if $f_{1}$ and $f_{1}$ are one-one maps from $R \rightarrow R$, then the product $f_{1} x f_{2}: R \vec{R}$ defined by $\left(f_{1} x f_{2}\right)(x)=f_{1}(x) f_{2}(x)$ need not be one-one.

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27. Given examples of two one-one functions $f_{1}$ and $f_{2}$ from $R$ to $R$ such that $f_{1}+f_{2}: R \vec{R}$, defined by $\left(f_{1}+f_{2}\right)(x)=f_{1}(x)+f_{2}(x)$ is not oneone.

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28. If $f, g: R \vec{R}$ are defined respectively by $f(x)=x^{2}+3 x+1, g(x)=2 x-3$, find fog (ii) gof (iii) fof (iv) gog.

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29. If the function $f: R \vec{R}$ be given by $f(x)=x^{2}+2 a n d g: R \vec{R}$ be given by $g(x)=\frac{x}{x-1}$. Find fogandgof.

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30. If the function fandg are given by
$f=\{(1,2),(3,5),(4,1)\} \operatorname{and} g=((2,3),(5,1),(1,3)\}$, find range of fandg. Also, write down fogandgof as sets of ordered pairs.

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31. Suppose $f_{1}$ and $f_{2}$ are non=zero one-one functions from $R \rightarrow R$ is $\frac{f_{1}}{f_{2}}$ necessarily one-one? Justify your answer. Here, $\frac{f_{1}}{f_{2}}: R \vec{R}$ is given by $\left(\frac{f_{1}}{f_{2}}\right)(x)=\frac{f_{1}(x)}{f_{2}(x)}$ for all $x R$.

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32. Find whether the following functions are one-one or not: $f: R \vec{g}$ ivenby $f(x)=x^{3}+2 f$ or all $x \in R$.
$f: Z \vec{Z}$ givenby $f(x)=x^{2}+1 f$ or allx $\in Z$.

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33. If the function $f$ and $g$ are given by
$f=\{(1,2),(3,5),(4,1)\}$ and $g=\{(2,3),(5,1),(1,3)\}$, find range of f and g. Also write down fog and gofas set of ordered pairs.

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34. Discuss the surjectivity of the following functions: $f: R \rightarrow$ given by $f(x)=x^{3}+2$ for all $x \in R$.

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35. Show that the function $f: Z \vec{Z}$ defined by $f(x)=x^{2}+x$ for all $x \in Z$, is a many one function.

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36. Let $A$ be the set of all 50 students of class XII in a central school. Let $f: A \vec{N}$ be a function defined by $f(x)=$ Rol $\ln$ umberofstudentx Show that $f$ is one-one but not onto

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37. Show that the function $f: R \vec{R}$ defined by $f(x)=3 x^{3}+5$ for all $x \in R$ is a bijection.
38. Show that the function $f: R \vec{R}$ given by $f(x)=\cos x f$ or allx $\in R$, is neither one-one nor onto

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39. Show that the function $f: R^{\rightarrow}$ given by $f(x)=x a+b$, where $a, b \in R, a \neq 0$ is a bijection.

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40. If $f(x)=\frac{x}{\sqrt{1+x^{2}}}$ then $\operatorname{fofof}(x)$

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41. If $f(x)=\frac{3 x-2}{2 x-3}$, prove that $\left.f(f(x))\right)=x$ for all $x \in R-\left\{\frac{3}{2}\right\}$.
42. Show that $f: R \vec{R}$, given by $f(x)=x-[x]$, is neither one-one nor onto.

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43. Let $f: R \vec{R}$ be a function given by $f(x)=a x+b$ for all $x \in R$. Find the constants a and b such that fof $=I_{R}$.

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44. If $f(x)=e^{x}$ and $g(x)=(\log )_{e} x(x>0)$, find fogandgof. Is $f o g=g \circ f ?$

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45. 

$f: R \rightarrow R$ and $g: R \rightarrow R d e f \in \operatorname{edbyf}(x)=x 2$ and $g(x)=(x+1)$.
Show that gof $=f o g$.

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46. Let $f$ and $g$ be real functions defined by $f(x)=\frac{x}{x+1} \operatorname{andg}(x)=\frac{x}{1-3}$.
Then $(f o g)^{-1}(x)=(1) x(2) 2 x(3) 3 x(4) 4 x$

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47. If $f(x)=\sqrt{x}(x>0)$ and $g(x)=x^{2}-1$ are two real functions, find $f o g$ and $g o f$ is $f o g=g o f ?$

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48. Let $f: N-[1] \vec{N}$ be defined by, $f(x)=$ the highest prime factor of $n$. Show that $f$ is neither one-one nor onto. Find the range of $f$.

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49. If $f: R^{\rightarrow}$ is defined by $f(x)=3 x-5$ Prove that $f$ is a bijection. Also, find the inverse of $f$.

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50. If $f:\left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \rightarrow R$ and $g:[-1,1] \rightarrow R$ be defined as $f(x)=\tan x$ and $g(x)=\sqrt{1-x^{2}}$ respectively. Describe fog and gof

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## 51.

$f(x)=\sin ^{2} x+\sin ^{2}\left(x+\frac{\pi}{3}\right)+\cos x \cos \left(x+\frac{\pi}{3}\right)$ andg $\left(\frac{5}{4}\right)=1$,
then $(g o f)(x)$ is $\qquad$

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52. Let $f, g: R \vec{R}$ be a two function defined as $f(x)=|x|+x$ and $g(x)=|x|-x$ for all $x \in R$. Then, find $f o g$ and gof

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53. Let $A=\{a, b, c, d\}$ and $f: A \rightarrow A$ be given by $f=\{(a, b),(b, d),(c, a),(d, c)\}$, write $f^{-1}$

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54. Let $f=\{(3,1),(9,3),(12,4)\}$ and $g=\{(1,3),(3,3),(4,9),(5,9)\}$. Show that gofandfog are both defined. Also, find fogandgof.
55. If $F:[1, \infty) \overrightarrow{2, \infty}$ is given by $f(x)=x+\frac{1}{x}$, then $f^{-1}(x)$ equals. $\frac{x+\sqrt{x^{2}-4}}{2}$ (b) $\frac{x}{1+x^{2}}$ (c) $\frac{x-\sqrt{x^{2}-4}}{2}$ (d) $1+\sqrt{x^{2}-4}$

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56. Let $f: R \rightarrow R$ and $g: R \rightarrow R$ be two functions such that $f \circ g(x)=\sin x^{2} \operatorname{andgof}(x)=\sin ^{2} x$ Then, find $f(x) \operatorname{andg}(x)$.

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57. Let $R$ be the set of real number. If $f: R \vec{R} ; f(x)=x^{2}$ and $g: R \vec{R} ; g(x)=2 x+1$. Then, find fogandgof. Also, show that $f o g \neq g o f$.

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58. If $f(x)=-4-(x-7)^{3}$, write $f^{-1}(x)$.

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59. If $f:\{5,6\} \overrightarrow{2,3}$ andg: $\{2,3\} \overrightarrow{5,6}$ are given by $f=\{(5,2),(6,3)\}$ and $g=\{(2,5),(3,6)\}$, find $f o g$.

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60. If a function $g=\{(1,1),(2,3),(3,5),(4,7)\}$ is described by $g(x)=\alpha x+\beta$, find the values of $\alpha a n d \beta$.

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61. Show that $f: R-[0] \vec{R} 0[0]$ given by $f(x)=\frac{3}{x}$ is invertible and it is inverse of itself.
62. Let $A=\{1,2, \ldots, n\}$ and $B=\{a, b\}$. Then number of surjections from $A$ into $B$ is nP2 (b) $2^{n}-2$ (c) $2^{n}-1$ (d) nC2

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63. If $f: \overrightarrow{R-1,1}$ is defined by $f(x)=-\frac{x|x|}{1+x^{2}}$, then $f^{-1}(x)$ equals
$\sqrt{\frac{|x|}{1-|x|}}$ (b) $-\operatorname{sgn}(x) \sqrt{\frac{|x|}{1-|x|}}-\sqrt{\frac{x}{1-x}}$ (d) none of these

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64. Let $f: Z \vec{Z}$ be defined by $f(n)=3 n$ for all $n \in Z$ and $g: Z \overrightarrow{ }$ be defined by
$f(n)=\left\{\frac{n}{3}, \quad\right.$ if nisaultipleof30, if nis $\neg$ ltipleof $3 f$ or alln $\in Z$. Show that $g o f=I_{Z}$ and $f o g \neq I_{Z}$
65. Let $A=\{x \in R: 0 \leq x \leq 1\}$. If $f: A \vec{A}$ is defined by $f(x)=\{x, \quad$ if $x Q 1-x, \quad$ if $x Q$ then prove that $f o f(x)=x$ for all $x \in A$.

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66. Let $A=[-1,1]$. Then, discuss whether the following functions from A to itself are one-one onto or bijective: $f(x)=\frac{x}{2}$ (ii) $g(x)=|x|$ (iii) $h(x)=x^{2}$

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67. Let $R$ be a relation on the set $A$ of ordered pairs of positive integers defined by $(x, \quad y) \quad R \quad(u, \quad v)$ if and only if $x v=y u$. Show that $R$ is an equivalence relation.

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68. Let A be a finite set. If $f: A \vec{A}$ is an onto function, show that $f$ is oneone also.

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69. Show that the function $f: R-\{3\} \rightarrow R-\{1\}$ given by $f(x)=\frac{x-2}{x-3}$ is bijection.

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70. Show that the function $f: R^{\rightarrow}$ given by $f(x)=x^{3}+x$ is a bijection.

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71. Let $f: N \cup\{0\} \vec{N} \cup\{0\}$ be defined by $f\{n+1$, if $n$ is even $n-1$, if $n$ is odd Show that $f$ is a bijection.
72. Let $f: N-[1] \vec{N}$ be defined by, $f(n)=$ the highest prime factor of $n$. Show that $f$ is neither one-one nor onto. Find the range of $f$.

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73. Let $A=\{1,2\}$. Find all one-to-one function from A to A .

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74. Let $f: R^{\rightarrow}$ and $g$ : RvecRbedef $\in e d+\operatorname{1andg}(x)=x-1$. Show that $f o g=g o f=I_{R}$.

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75. Verify assoiativity for the following three mappings : $f: N \vec{Z}_{0}$ (the set of non zero integers), $g: Z_{0} \vec{Z}$ and $h: Q \vec{R}$ given by
$f(x)=2 x, g(x)=\frac{1}{x}$ and $h(x)=e^{x}$.

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76. If the set $A$ contains 5 elements and the set B contains 6 elements, then the number of one-one and onto mappings from $A$ to $B$ is (a)720 (b) 120 (c) 0 (d) none of these

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77. If the set $A$ contains 7 elements and the set $B$ contains 10 elements, then the number of one-one functions from $A$ to $B$ is

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78. $f: R \rightarrow R$ is defined by $f(x)=\frac{e^{x \wedge} 2-e^{-x \wedge} 2}{e^{x^{\wedge}} 2+e^{-x^{\wedge}} 2}$ is (a) one-one but not onto (b) many-one but onto (c) one-one and onto (d) neither one-one nor onto

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79. The inverse of the function $f: R x \in R: x<1$ given by $f(x)=\frac{e^{x}-e^{-x}}{e^{x}+e^{-x}}$, is $\frac{1}{2} \frac{\log (1+x)}{1-x}$ (b) $\frac{1}{2} \frac{\log (2+x)}{2-x} \frac{1}{2} \frac{\log (1-x)}{1+x}$ (d) None of these

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80. Let $A=\{1,2,3\}$. Write all one-one from $A$ to itself.

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81. If $f: R \vec{R}$ be the function defined by $f(x)=4 x^{3}+7$, show that $f$ is a bijection.

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82. If the function $f:[1, \infty) \rightarrow[1, \infty)$ is defined by $f(x)=2^{x(x-1)}$,
then $f^{-1}(x)$ is (A) $\left(\frac{1}{2}\right)^{x(x-1)}$
(B) $\frac{1}{2} \sqrt{1+4 \log _{2} x}$ $\frac{1}{2}\left(1-\sqrt{1+4 \log _{2} x}\right)$ (D) not defined

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83. The value of parameter $\alpha$, for which the function $f(x)=1+\alpha x, \alpha \neq 0$ is the inverse of itself

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84. Let $R^{+}$be the set of all non-negative real numbers. if $f: R^{+} \rightarrow R^{+}$ and $g: R^{+} \rightarrow R^{+}$are defined as $f(x)=x^{2}$ and $g(x)=+\sqrt{x}$. Find $f o g$ and $g o f$. Are they equal functions.

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85. Show that the function $f: R \rightarrow R$ is given by $f(x)=1+x^{2}$ is not invertible.

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86. If $f: R-1,1$ defined by $f(x)=\frac{10^{x}-10^{-x}}{10^{x}+10^{-x}}$ is invertible, find $f^{-1}$

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87. Let $f:[-1, \infty] \overrightarrow{-1,}$ is given by $f(x)=(x+1)^{2}-1, x \geq-1$. Show that $f$ is invertible. Also, find the set $S=\left\{x: f(x)=f^{-1}(x)\right\}$.

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88. Let $f: N \vec{S}$ be a function defined as $f(x)=4 x^{2}+12 x+15$. Show that $f: N \vec{S}$, where $S$ is the range of $f$, is invertible. Also find the inverse of $f$
89. Let $A=R-\{3\}$ and $B=R-[1]$. Consider the function $f: A \vec{B}$ defined by $f(x)=\left(\frac{x-2}{x-3}\right)$. Show that $f$ is one-one and onto and hence find $f^{-1}$

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90. Let $f, g: \vec{R}$ be defined by $f(x)=2 x+1$ and $g(x)=x^{2}-2$ for all $x \in R$, respectively. Then, find gof

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91. Let $A$ and $B$ be any two sets such that $n(B)=P, n(A)=q$ then the total number of functions $\mathrm{f}: A \rightarrow B$ is equal to

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92. If $f: A \rightarrow A, g: A \rightarrow A$ are two bijections, then prove that $f o g$ is an injection (ii) $f o g$ is a surjection.

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93. Let $f: Z \rightarrow Z$ be defined by $f(x)=x+2$. Find $g: Z \rightarrow Z$ such that $g \circ f=I_{Z}$.

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94. Which one the following relations on $A=\{1,2,3\}$ is function? $f=\{(1,3),(2,3),(3,2), g=\{(1,2),(1,23),(3,1)\}$

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95. Write the domain of the real function $f$ defined by $f(x)=\sqrt{25-x^{2}}$
96. Let $A\} x:-1 \leq x \leq 1\}$ and $f: A \rightarrow$ such that $f(x)=x|x|$, then $f$ is a bijection (b) injective but not surjective Surjective but not injective (d) neither injective nor surjective

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97. If the function $f:(1, \infty) \rightarrow(1, \infty)$ is defined by
$f(x)=2^{x(x-1)}$, thenf $f^{-1}(x)$ is
(a) $\left(\frac{1}{2}\right)^{x(x-1)}$
(b) $\frac{1}{2}\left(1+\sqrt{1+4(\log )_{2} x}\right)$
(c) $\frac{1}{2}\left(1-\sqrt{1+(\log ){ }_{2} x}\right.$
(d) not defined

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98. If $f(x)=\frac{x-1}{x+1}, x \neq-1$, then show that $f(f(x))=-\frac{1}{x}$ provided that $x \neq 0,1$.

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99. Let $f$ be a real function defined by $f(x)=\sqrt{x-1}$. Find $(f o f o f)(x)$. Also, show that $f o f \neq f^{2}$.

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100. Let $f: R \rightarrow R$ be the function defined by $f(x)=4 x-3$ for all $x \in R$. Then write $f^{-1}$.

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101. Find whether $f: R \rightarrow R$ given by $f(x)=x^{3}+2$ for all $x \in R$.

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102. Find whether $f: Z \rightarrow Z$ given by $f(x)=x^{2}+1$ for all $x \in Z$

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103. Show that the function $f: Z \rightarrow Z$ defined by $f(x)=x^{2}$ for all $x \in Z$, is a function but not bijective function.

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104. Discuss the surjectivity of $f: R \rightarrow R$ given by $f(x)=x^{3}+2$ for all $x \in R$

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105. Discuss the surjectivity of $f: R \rightarrow R$ given by $f(x)=x^{2}+2$ for all $x \in R$
106. Discuss the surjectivity of $f: Z \rightarrow Z$ given by $f(x)=3 x+2$ for all $x \in Z$.

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107. Show that the function $f: N \rightarrow N$ given by $f(1)=f(2)=1$ and $f(x)=x-1$ for every $x \geq 2$, is onto but not one-one.

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108. Show that the Signum function $f: R \rightarrow R$, given by $\left.f(x)=\left\{\begin{array}{cc}1 & x>0 \\ 0 & x=0 \\ -1 & x<0\end{array}\right)\right\}$ is neither one-one nor onto

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109. Prove that the function $f: Q \rightarrow Q$ given by $f(x)=2 x-3$ for all $x \in Q$ is a bijection.

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110. Show that the function $f: R \rightarrow R$ defined by $f(x)=3 x^{3}+5$ for all $x \in R$ is a bijection.

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111. Let $A=\{x \in R:-1 \leq x \leq 1\}=B$. Then, the mapping $f: A \rightarrow B$ given by $f(x)=x|x|$ is (a) injective but not surjective (b) surjective but not injective (c) bijective (d) none of these

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112. Let $A$ be the set of all 50 students of class $X I I$ in a central school.

Let $f: A \rightarrow N$ be a function defined by $f(x)=$ Roll number of student $x$ Show that $f$ is one-one but not onto.

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113. Show that the function $f: N \rightarrow N$, given by $f(x)=2 x$, is one-one but not onto.

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114. Prove that $f: R \rightarrow R$, given by $f(x)=2 x$, is one-one and onto.

## - Watch Video Solution

115. Show that the function $f: R \rightarrow R$, defined as $f(x)=x^{2}$, is neither one-one nor onto.
116. Show that $f: R \rightarrow R$, defined as $f(x)=x^{3}$, is a bijection.

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117. Show that the function $f: R_{0} \rightarrow R_{0}$, defined as $f(x)=\frac{1}{x}$, is oneone onto, where $R_{0}$ is the set of all non-zero real numbers. Is the result true, if the domain $R_{0}$ is replaced by $N$ with co-domain being same as $R_{0}$ ?

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118. Prove that the greatest integer function $f: R \rightarrow R$, given by $f(x)=[x]$, is neither one-one nor onto, where [ x$]$ denotes the greatest integer less than or equal to $x$.
119. Show that the modulus function $f: R \rightarrow R$, given by $f(x)=|x|$ is neither one-one nor onto.

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120. Let $C$ be the set of complex numbers. Prove that the mapping $F: C \rightarrow R$ given by $f(z)=|z|, \forall z \in C$, is neither one-one nor onto.

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121. Show that the function $f: R^{\rightarrow}$ given by $f(x)=x a+b$, where $a, b \in R, a \neq 0$ is a bijection.

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122. Show that the function $f: R \rightarrow R$ given by $f(x)=\cos x$ for all $x \in R$, is neither one-one nor onto.
123. Let $A=R-\{2\}$ and $B=R-\{1\}$. If $f: A \rightarrow B$ is a mapping defined by $f(x)=\frac{x-1}{x-2}$, show that $f$ is bijective.

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124. Let $A$ and $B$ be two sets. Show that $f: A \times B \rightarrow B \times A$ defined by $f(a, b)=(b, a)$ is a bijection.

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125. Let A be any non-empty set. Then, prove that the identity function on set A is a bijection.

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126. Let $f: N-\{1\} \rightarrow N$ be defined by, $f(n)=$ the highest prime factor of $n$. Show that $f$ is neither one-one nor onto. Find the range of $f$.

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127. Let $A=\{1,2\}$. Find all one-to-one function from A to A .

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128. Consider the identity function $I_{N}: N \rightarrow N$ defined as, $I_{N}(x)=x$ for all $x \in N$. Show that although $I_{N}$ is onto but $I_{N}+I_{N}: N \rightarrow N$ defined as $\left(I_{N}+I_{N}\right)(x)=I_{N}(x)+I_{N}(x)=x+x=2 x$ is not onto.

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129. Consider a function $f:\left[0, \frac{\pi}{2}\right] \rightarrow R \quad$ given by $f(x)=\sin x$ and $g:\left[0, \frac{\pi}{2}\right] \rightarrow R$ given by $g(x)=\cos x$. Show that f
and g are one-one, but $f+g$ is not one-one.

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130. Let $f: X \rightarrow Y$ be a function. Define a relation $R$ in $X$ given by $R=\{(a, b): f(a)=f(b)\}$. Examine whether $R$ is an equivalence relation or not.

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131. Show that the function $f: R \rightarrow R$ given by $f(x)=x^{3}+x$ is a bijection.

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$$
\begin{aligned}
& \text { 132. Show that } f: n \rightarrow N \quad \text { defined by } \\
& f(n)=\left\{\left(\left(\frac{n+1}{2},(\text { if nisodd })\right),\left(\frac{n}{2},(\text { if niseven })\right)\right.\right. \text { is many - }
\end{aligned}
$$

133. Show that the function $f: N \rightarrow N$ given by, $f(n)=n-(-1)^{n}$ for all $n \in N$ is a bijection.

## - Watch Video Solution

134. Let $f: N \cup\{0\} \rightarrow N \cup\{0\}$ be defined by $f(n)=\{n+1, \quad$ if $n$ is even $\cap-1, \quad$ if $n$ is odd Show that $f$ is a bijection.

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135. Let $A$ be a finite set. If $f: A \rightarrow A$ is a one-one function, show that $f$ is onto also.

## - Watch Video Solution

136. Let $A$ be a finite set. If $f: A \rightarrow A$ is an onto function, show that $f$ is one-one also.

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137. Give an example of a function which is one-one but not onto. which is not one-one but onto.(iii) which is neither one-one nor onto.

## - Watch Video Solution

138. Which of the following functions from $A$ to $B$ are one-one and onto?
$f_{1}=\{(1,3),(2,5),(3,7)\} ; A=\{1,2,3\}, B=\{3,5,7\}$
$f_{2}=\{(2, a),(3, b),(4, c)\} ; A=\{2,3,4\}, B=\{a, b, c\}$
$f_{3}=\{(a, x),(b, x),(c, z),(d, z)\} ; A=\{a, b, c, d\}, B=\{x, y$, $z\}$
139. Prove that the function $f: N \rightarrow N$, defined by $f(x)=x^{2}+x+1$ is one-one but not onto.

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140. Let $A=\{-1,0,1\}$ and $f=\left\{\left(x, x^{2}\right): x \in A\right\}$. Show that $f: A \rightarrow A$ is neither one-one nor onto.

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141. Classify $f: N \rightarrow N$ given by $f(x)=x^{2}$ as injection, surjection or bijection.

## - Watch Video Solution

142. Classify $f: Z \rightarrow Z$ given by $f(x)=x^{2}$ as injection, surjection or bijection.
143. Classify $f: N \rightarrow N$ given by $f(x)=x^{3}$ as injection, surjection or bijection.

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144. Classify $f: Z \rightarrow Z$ given by $f(x)=x^{3}$ as injection, surjection or bijection.

## - Watch Video Solution

145. Classify $f: R \rightarrow R$, defined by $f(x)=|x|$ as injection, surjection or bijection.

## - Watch Video Solution

146. Classify $f: Z \rightarrow Z$, defined by $f(x)=x^{2}+x$ as injection, surjection or bijection.

## Watch Video Solution

147. Classify $f: Z \rightarrow Z$, defined by $f(x)=x-5$ as injection, surjection or bijection.

## - Watch Video Solution

148. Classify $f: R \rightarrow R$, defined by $f(x)=\sin x$ as injection, surjection or bijection.

## - Watch Video Solution

149. Classify $f: R \rightarrow R$, defined by $f(x)=x^{3}+1$ as injection, surjection or bijection.
150. Classify $f: R \rightarrow R$, defined by $f(x)=x^{3}-x$ as injection, surjection or bijection.

## - Watch Video Solution

151. Classify $f: R \rightarrow R$, defined by $f(x)=\sin ^{2} x+\cos ^{2} x$ as injection, surjection or bijection.

## - Watch Video Solution

152. Classify $f: Q-\{3\} \rightarrow Q$, defined by $f(x)=\frac{2 x+3}{x-3}$ as injection, surjection or bijection.

## - Watch Video Solution

153. Classify $f: Q \rightarrow Q$, defined by $f(x)=x^{3}+1$ as injection, surjection or bijection.

## - Watch Video Solution

154. Classify $f: R \rightarrow R$, defined by $f(x)=5 x^{3}+4$ as injection, surjection or bijection.

## - Watch Video Solution

155. Classify $f: R \rightarrow R$, defined by $f(x)=3-4 x$ as injection, surjection or bijection.

## - Watch Video Solution

156. Classify $f: R \rightarrow R$, defined by $f(x)=1+x^{2}$ as injection, surjection or bijection.
157. Classify $f: R \rightarrow R$, defined by $f(x)=\frac{x}{x^{2}+1}$ as injection, surjection or bijection.

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158. If $f: A \rightarrow B$ is an injection such that range of $f=\{a\}$. Determine the number of elements in $A$.

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159. Show that the function $f: R-\{3\} \rightarrow R-\{1\}$ given by $f(x)=\frac{x-2}{x-3}$ is a bijection.

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160. Let $A=[-1,1]$. Then, discuss whether the following functions from $A$ to itself are one-one, onto or bijective: $f(x)=\frac{x}{2}$ (ii) $g(x)=|x|$ (iii) $h(x)=x^{2}$

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161. Are the following set of ordered pairs functions? If so, examine whether the mapping is injective or surjective: $\{(x, y): x$ is a person, $y$ is the mother of $x\}$ (ii) $\{(a, b): a$ is a person, $b$ is an ancestor of $a\}$

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162. Let $A=\{1,2,3\}$. Write all one-one from $A$ to itself.

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163. If $f: R \rightarrow R$ be the function defined by $f(x)=4 x^{3}+7$, show that $f$ is a bijection.

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164. Show that the exponential function $f: R \rightarrow R$, given by $f(x)=e^{x}$, is one-one but not onto. What happens if the co-domain is replaced by $R^{+}$(set of all positive real numbers).

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165. Show that the logarithmic function $f: R 0 \pm>R$ given by $f(x)=(\log )_{a} x, a>0$ is a bijection.

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166. Show that a one-one function $f:\{1,2,3\} \rightarrow\{1,2,3\}$ must be onto.
167. If $A=\{1,2,3\}$, show that an onto function $f: A \rightarrow A$ must be one-one

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168. Find the number of all onto functions from the set $A=\{1,2,3,, n\}$ to itself.

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169. Give examples of two one-one functions $f_{1}$ and $f_{2}$ from $R$ to $R$ such that $f_{1}+f_{2}: R \rightarrow R$, defined by $\left(f_{1}+f_{2}\right)(x)=f_{1}(x)+f_{2}(x)$ is not one-one.

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170. Give examples of two surjective function $f_{1}$ and $f_{2}$ from $Z$ to $Z$ such that $f_{1}+f_{2}$ is not surjective.

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171. Show that if $f_{1}$ and $f_{2}$ are one-one maps from $R$ to $R$, then the product $f_{1} \times f_{2}: R \rightarrow R$ defined by $\left(f_{1} \times f_{2}\right)(x)=f_{1}(x) f_{2}(x)$ need not be one-one.

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172. Suppose $f_{1}$ and $f_{2}$ are non-zero one-one functions from $R$ to $R$. Is $\frac{f_{1}}{f_{2}}$ necessarily one-one? Justify your answer. Here, $\frac{f_{1}}{f_{2}}: R \rightarrow R$ is given by $\left(\frac{f_{1}}{f_{2}}\right)(x)=\frac{f_{1}(x)}{f_{2}(x)}$ for all $x \in R$.

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173. Given $A=\{2,3,4\}, B=\{2,5,6,7\}$. Construct an example of an injective map from $A$ to $B$.

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174. Given $A=\{2,3,4\}, B=\{2,5,6,7\}$. Construct an example of a mapping from $A$ to $B$ which is not injective

## - Watch Video Solution

175. Given $A=\{2,3,4\}, B=\{2,5,6,7\}$. Construct an example of a mapping from $A$ to $B$.

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176. Show that $f: R \rightarrow R$, given by $f(x)=x-[x]$, is neither one-one nor onto.
177. Let $f: N \rightarrow N$ be defined by:
$f(n)=\{n+1, \quad$ if $n$ is oddn-1, $\quad$ if $n$ is even Show that $f$ is a bijection.

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178. Let $R$ be the set of real numbers. If $f: R \rightarrow R: f(x)=x^{2}$ and $g: R \rightarrow R ; g(x)=2 x+1$. Then, find $f o g$ and $g o f$. Also, show that $f o g \neq g \circ$.

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179. Let $: R \rightarrow R ; f(x)=\sin x$ and $g: R \rightarrow R ; g(x)=x^{2}$ find $f o g$ and gof.

## - Watch Video Solution

180. Let $f:\{2,3,4,5\} 3,4,5,9$ andg: $\{3,4,5,9\} 7,11,15$ be functions defined
$f(2)=3, f(3)=4, f(4)=f(5)=5, g(3)=g(4)=7, \operatorname{andg}(5)=g(9)=$

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181. Let $f:\{1,3,4\} \rightarrow\{1,2,5\}$ and $g:\{1,2,5\} \rightarrow\{1,3\}$ be given by $f=\{(1,2),(3,5),(4,1)\}$ and $g=\{(1,3),(2,3),(5,1)\}$. Write down gof.

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182. Find gof and fog, if $f: R \rightarrow R$ and $g: R \rightarrow R$ are given by $f(x)=|x|$ and $g(x)=|5 x-2|$.

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183. If the functions $f$ and $g$ are given by $f=\{(1,2),(3,5),(4,1)\}$ and $g=\{(2,3),(5,1),(1,3)\}$, find range of $f$ and $g$. Also, write down fog and gof as sets of ordered pairs.

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184. If the function $f: R \rightarrow R$ be given by $f(x)=x^{2}+2$ and $g: R \rightarrow R$ be given by $g(x)=\frac{x}{x-1}$. Find $f o g$ and $g o f$.

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185. If $f: R-\left\{\frac{7}{5}\right\} \rightarrow R-\left\{\frac{3}{5}\right\}$ be defined as $f(x)=\frac{3 x+4}{5 x-7}$ and $g: R-\left\{\frac{3}{5}\right\} \rightarrow R-\left\{\frac{7}{5}\right\}$ be defined as $g(x)=\frac{7 x+4}{5 x-3}$. Show that gof $=I_{A}$ and $f o g=I_{B}$, where $B=R-\left\{\frac{3}{5}\right\}$ and $A=R-\left\{\frac{7}{5}\right\}$.

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186. If $f: R \rightarrow R$ is defined by $f(x)=x^{2}-3 x+2$, find $f(f(x))$.

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187. If $f, g: R \vec{R}$ are defined respectively by $f(x)=x^{2}+3 x+1, g(x)=2 x-3$, find fog (ii) gof (iii) fof (iv) gog.

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188. Let $f: Z \rightarrow Z$ be defined by $f(x)=x+2$. Find $g: Z \rightarrow Z$ such that $g \circ f=I_{Z}$.

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189. If $f: Z \rightarrow Z$ be defined by $f(x)=2 x$ for all $x \in Z$. Find $g: Z \rightarrow Z$ such that $g o f=I_{Z}$.

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190. Let $f, g$ and $h$ be functions from $R$ to $R$. Show that $(f+g) o h=f o h+g o h$

## - Watch Video Solution

191. Let $f, g$ and $h$ be functions from $R$ to $R$. Show that $(f g) o h=(f o h)(g o h)$

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192. Let $f: R \rightarrow R$ be the signum function defined as $f(x)=\{1, x>0, \quad 0, x=0, \quad-1, x<0$ and $g: R \rightarrow R$ be the greatest integer function given by $g(x)=[x]$. Then, prove that $f o g$ and gof coincide in (0, 1].

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193. Let $A=\{x \in R: 0 \leq x \leq 1\}$. If $f: A \vec{A}$ is defined by $f(x)=\{x, \quad$ if $x Q 1-x, \quad$ if $x Q$ then prove that $f o f(x)=x$ for all $x \in A$.

## - Watch Video Solution

194. Let $f: R \vec{R}$ and $g: \vec{R}$ be two functions such that $f o g(x)=\sin x^{2} \operatorname{andgof}(x)=\sin ^{2} x$. Then, find $f(x) \operatorname{andg}(x)$.

## - Watch Video Solution

195. If $f: R \rightarrow R$
be given
by
$f(x)=\sin ^{2} x+\sin ^{2}(x+\pi / 3)+\cos x \cos (x+\pi / 3)$ for all $x \in R$, and $g: R \rightarrow R$ be such that $g(5 / 4)=1$, then prove that $g o f: R \rightarrow R$ is a constant function.

- Watch Video Solution

196. Let $f: Z \vec{Z}$ be defined by $f(n)=3 n$ for all $n \in Z$ and $g: Z \overrightarrow{ }$ be defined
$f(n)=\left\{\frac{n}{3}, \quad\right.$ if nisaultipleof30, if nis $\neg$ ltipleof $3 f$ or al $\ln \in Z$. Show that $g \circ f=I_{Z}$ and $f o g \neq I_{Z}$

## - Watch Video Solution

197. Let $f: R \vec{R}$ be a function given by $f(x)=a x+b$ for all $x \in R$. Find the constants aandb such that fof $=I_{R}$.

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198. Let $f: A \rightarrow A$ be a function such that $f o f=f$. Show that $f$ is onto if and only if $f$ is one-one. Describe $f$ in this case.

## - Watch Video Solution

199. Let $f, g: R \vec{R}$ be two functions defined as $f(x)=|x|+x$ and $g(x)=|x|-x$, for all $x R$. Then find fog and gof.

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200. Find gof and gof when $f: R \rightarrow R$ and $g: R \rightarrow R$ is defined by $f(x)=2 x+3$ and $g(x)=x^{2}+5$

## - Watch Video Solution

201. Find gof and gof when $f: R \rightarrow R$ and $g: R \rightarrow R$ is defined by $f(x)=2 x+x^{2}$ and $g(x)=x^{3}$

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202. Find $f o g(2)$ and $g o f(1)$ when: $f: R \rightarrow R ; f(x)=x^{2}+8$ and $g: R \rightarrow R ; g(x)=3 x^{3}+1$.
203. Find gof and fog when $f: R \rightarrow R$ and $g: R \rightarrow R$ is defined by $f(x)=x$ and $g(x)=|x|$

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204. Find gof and fog when $f: R \rightarrow R$ and $g: R \rightarrow R$ is defined by
$f(x)=x^{2}+2 x-3$ and $g(x)=3 x-4$

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205. Find gof and gof when $f: R \rightarrow R$ and $g: R \rightarrow R$ is defined by $f(x)=8 x^{3}$ and $g(x)=x^{1 / 3}$

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206. Let $f=\{(3,1),(9,3),(12,4)\}$ and $=\{(1,3),(3,3),(4,9)$, $(5,9)\}$. Show that gof and fog are both defined. Also, find fog and gof.

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207. Let $f=\{(1,-1),(4,-2),(9,-3),(16,4)\} \quad$ and $g=\{(-1,-2),(02,-4),(-3,-6),(4,8)\}$. Show that gof is defined while $f o g$ is not defined. Also, find $g o f$.

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208. Let $A=\{a, b, c\}, B=\{u v, w\}$ and let $f$ and $g$ be two functions from $A$ to $B$ and from $B$ to $A$ respectively defined as: $f=\{(a, v)$, $(b, u),(c, w)\}, g=\{(u, b),(v, a),(w, c)\}$. Show that $f$ and $g$ both are bijections and find fog and gof.

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209. Find $f o g(2)$ and $g o f(1)$ when: $f: R \rightarrow R ; f(x)=x^{2}+8$ and $g: R \rightarrow R ; g(x)=3 x^{3}+1$.

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210. Let $R^{+}$be the set of all non-negative real numbers. If $f: R^{+} \rightarrow R^{+}$ and $g: R^{+} \rightarrow R^{+}$are defined as $f(x)=x^{2}$ and $g(x)=+\sqrt{x}$. Find $f o g$ and $g o f$. Are they equal functions.

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211. Let $f: R \rightarrow R$ and $g: R \rightarrow R$ be defined by $f(x)=x^{2}$ and $g(x)=x+1$. Show that $f o g \neq g o f$.

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212. Let $f: R \vec{R}$ and $g: R \vec{R}$ be defined by $f(x)=x+1$ and $g(x)=x-1$. Show that $f o g=g o f=I_{R}$.

## ( Watch Video Solution

213. Verify associativity for the following three mappings : $f: N \vec{Z}_{0}$ (the set of non zero integers), $g: Z_{0} \vec{Z}$ and $h: Q \vec{R}$ given by $f(x)=2 x, g(x)=\frac{1}{x}$ and $h(x)=e^{x}$.

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214. Consider $f: N \rightarrow N, g: N \rightarrow N$ and $h: N \rightarrow R$ defined as $f(x)=2 x$, $g(y)=3 y+4$ and $h(z)=s \in z, \forall \mathrm{x}, \mathrm{y}$ and z in N . Show that ho(gof $)=$ (hog) of.

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215. Given examples of two functions $f: \quad N \rightarrow N$ and: $\quad N \rightarrow N$ such that of is onto but $f$ is not onto. (Hint: Consider $f(x)=x \operatorname{andg}(x)=|x|)$.
216. Give examples of two functions $f: N \rightarrow Z$ andg: $Z \rightarrow Z$ such that o f is injective but is not injective. (Hint: Consider $f(x)=x \operatorname{andg}(x)=|x|)$

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217. If $f: A \vec{B}$ and $g: B \vec{C}$ are one-one functions, show that gof is one-one function.

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218. If $f: R \rightarrow R$ and $g: R \rightarrow R$ be functions defined by $f(x)=x^{2}+1$ and $g(x)=\sin x$, then find $f o g$ and $g o f$.

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219. If $f:[0, \infty) \vec{R}$ andg: $\vec{R}$ be defined as $f(x)=\sqrt{x}$ and $g(x)=-x^{2}-1$, then find gofandfog.

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220. If $f(x)=e^{x}$ and $g(x)=(\log )_{e} x(x>0)$, find fogandgof. Is $f o g=g \circ f ?$

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221. If $f(x)=\sqrt{x}(x>0)$ and $g(x)=x^{2}-1$ are two real functions, find $f o g$ and $g o f$ is $f o g=g o f ?$

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222. If $f(x)=\frac{1}{x}$ and $g(x)=0$ are two real functions, show that $f o g$ is not defined.
223. Let $f(x)=[x]$ and $g(x)=|x|$. Find ( $g \circ f)\left(\frac{5}{3}\right) f \circ g\left(\frac{5}{3}\right)$

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224. Let $f(x)=[x]$ and $g(x)=|x|$. Find $(g \circ f)\left(\frac{5}{3}\right)-f o g\left(\frac{5}{3}\right)$

## - Watch Video Solution

225. Let $f(x)=[x]$ and $g(x)=|x|$. Find $(f+2 g)(-1)$

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226. Let fandg be real functions defined by $f(x)=\frac{x}{x+1} \operatorname{andg}(x)=\frac{1}{x+3}$. Describe the functions gofandfog (if they exist).
227. If $f(x)=\frac{3 x-2}{2 x-3}$, prove that $\left.f(f(x))\right)=x$ for all $x \in R-\left\{\frac{3}{2}\right\}$.

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228. If $f(x)=\frac{1}{2 x+1}, x \neq-\frac{1}{2}$, then show that $f(f(x))=\frac{2 x+1}{2 x+3}$, provided that $x \neq-\frac{3}{2}$.

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229. If $f(x)=\frac{x}{\sqrt{1+x^{2}}}$ then fofof $(x)$

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230. Let $f$ be a real function defined by $f(x)=\sqrt{x-1}$. Find $(f o f o f)(x)$. Also, show that $f o f \neq f^{2}$.
231. If $f(x)=\frac{x-1}{x+1}, x \neq-1$, then show that $f(f(x))=-\frac{1}{x}$ provided that $x \neq 0,1$.

## - Watch Video Solution

232. Find $f o g$ and $g \circ f$, if $f(x)=e^{x}, g(x)=(\log )_{e} x$

## - Watch Video Solution

233. Find $f \circ g$ and $g \circ f$, if $f(x)=x^{2}, g(x)=\cos x$

## - Watch Video Solution

234. Find $f o g$ and $g o f$, if $f(x)=|x|, g(x)=\sin x$

## - Watch Video Solution

235. Find $f o g$ and $g \circ f$, if $f(x)=x+1, g(x)=e^{x}$

## - Watch Video Solution

236. Find $f \circ g$ and $g \circ f$, if $f(x)=\sin ^{-1} x, g(x)=x^{2}$

## - Watch Video Solution

237. Find $f o g$ and $g o f$, if $f(x)=x+1, g(x)=\sin x$

## - Watch Video Solution

238. Find $f o g$ and $g \circ f$, if $f(x)=x+1, g(x)=2 x+3$

## - Watch Video Solution

239. Find $f o g$ and $g \circ f$, if $f(x)=c, c \in R, g(x)=\sin x^{2}$

## - Watch Video Solution

240. Find $f o g$ and $g \circ f$, if $f(x)=x^{2}+2, g(x)=1-\frac{1}{1-x}$

## - Watch Video Solution

241. Let $f(x)=x^{2}+x+1$ and $g(x)=\sin x$. Show that $f o g \neq g o f$.

## - Watch Video Solution

242. Let $f: R \rightarrow R: f(x)=|x|$, Prove that $f o f=f$

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243. If $f(x)=2 x+5$ and $g(x)=x^{2}+1$ be two real functions, then describe $f^{2}$. Also, show that $f o f \neq f^{2}$.

## - Watch Video Solution

244. If $f(x)=2 x+5$ and $g(x)=x^{2}+1$ be two real functions, then describe $f^{2}$. Also, show that fof $\neq f^{2}$.

## - Watch Video Solution

245. If $f(x)=2 x+5$ and $g(x)=x^{2}+1$ be two real functions, then describe $f^{2}$. Also, show that fof $\neq f^{2}$.

## - Watch Video Solution

246. If $f(x)=2 x+5$ and $g(x)=x^{2}+1$ be two real functions, then describe $f^{2}$. Also, show that $f o f \neq f^{2}$.
247. If $f(x)=\sin x$ and $g(x)=2 x$ be two real functions, then describe $g o f$ and $f o g$. Are these equal functions?

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248. Let $f, g, h$ be real functions given by $f(x)=\sin x, g(x)=2 x$ and $h(x)=\cos x$. Prove that $f o g=g o(f h)$.

## - Watch Video Solution

249. Let $f$ be any real function and let $g$ be a function given by $g(x)=2 x$
. Prove that $g o f=f+f$.

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250. If $f(x)=\sqrt{1-x}$ and $g(x)=(\log )_{e} x$ are two real functions, then describe functions $f o g$ and $g o f$.

## - Watch Video Solution

251. If $f:(-\pi / 2, \pi / 2) \rightarrow R$ and $g:[-1,1] \rightarrow R$ be defined as $f(x)=\tan x$ and $g(x)=\sqrt{1-x^{2}}$ respectively. Describe fog and gof.

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252. If $f(x)=\sqrt{x+3}$ and $g(x)=x^{2}+1$ be two real functions, then find $f o g$ and $g o f$.

## - Watch Video Solution

253. Let $f$ be a real function given by $f(x)=\sqrt{x-2}$. Find $f o f$. Also, show that fof $\neq f^{2}$
254. If $f,: R \vec{R}$ be two functions defined as $f(x)=|x|+x$ and $g(x)=|x|-x, \forall x R$, Then find fog and gof. Hence find $f o g(-3), f o g(5)$ and $g o f(-2)$.

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255. If $f: Q \rightarrow Q$ is given by $f(x)=x^{2}$, then find $f^{-1}(9)$

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256. If $f: Q \rightarrow Q$ is given by $f(x)=x^{2}$, then find $f^{-1}(-25)$

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257. If $f: Q \rightarrow Q$ is given by $f(x)=x^{2}$, then find $f^{-1}(9)$
258. If the function $f: R \rightarrow R$ be defined by $f(x)=x^{2}+5 x+9$, find $f^{-1}(8)$ and $f^{-1}(9)$.

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259. If the function $f: C \rightarrow C$ be defined by $f(x)=x^{2}-1$, find $f^{-1}(9)$ and $f^{-1}(8)$.

## - Watch Video Solution

260. Let $f: R \rightarrow R$ be defined as $f(x)=x^{2}+1$. Find: $f^{-1}(10)$

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261. If $A=\{0,1,2,3\},, B=\{1,3,5,7,9\}$ and $f: A \rightarrow B$ is given by $f(x)=2 x+1$, then write $f$ and $f^{-1}$ as a set of ordered pairs.

## (D) Watch Video Solution

262. Let $S=\{1,2,3\}$. Determine whether the functions $f: S \rightarrow S$ defined as below have inverses. Find $f^{-1}$, if it exists.(a) $f=\{(1,1),(2,2),(3,3)\}$ (b) $f=\{(1,2),(2,1),(3,1)\}$

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263. Consider $f:\{1,2,3\} \rightarrow\{a, b, c\}$ given by $f(1)=a, f(2)=b$ and $f(3)=c$. Find $f^{-1}$ and show that $\left(f^{-1}\right)^{-1}=f$.

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264. If $f: R^{\rightarrow}$ is defined by $f(x)=2 x+7$. Prove that $f$ is a bijection. Also, find the inverse of $f$.

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265. If $f: R \rightarrow R$ is a bijection given by $f(x)=x^{3}+3$, find $f^{-1}(x)$.

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266. Let $f: R \rightarrow R$ be defined by $f(x)=3 x-7$. Show that $f$ is invertible and hence find $f^{-1}$.

## - Watch Video Solution

267. Show that $f: R-c R 0[0]$ given by $f(x)=$ is invertible and it is inverse of itself.

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268. Let $f: N \cup\{0\} \rightarrow N \cup\{0\}$ be defined by
$f(n)=\{n+1, \quad$ if $n$ is even, $n-1, \quad$ if $n$ is odd Show that $f$ is invertible and $f=f^{-1}$.
269. Prove that the function $f: R \rightarrow R$ defined as $f(x)=2 x+3$ is invertible. Also, find $f^{-1}$.

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270. Show that the function $f: R \rightarrow R$ is given by $f(x)=1+x^{2}$ is not invertible.

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271. Show that $f: R-\{-1\} \rightarrow R-\{1\}$ given by $f(x)=\frac{x}{x+1}$ is invertible. Also, find $f^{-1}$.

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272. Show that $f:[-1,1] \rightarrow R$, given by $f(x)=\frac{x}{(x+2)}$ is one- one . Find the inverse of the function $f:[-1,1]$

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273. Let $f: R^{\rightarrow}$ be defined as $f(x)=10 x+7$. Find the function $g: R \vec{R}$ such that $g o f=f o g=I_{R}$.

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274. If the function $f:[1, \infty) \rightarrow[1, \infty)$ is defined by $f(x)=2^{x(x-1)}$, then $f^{-1}(x)$ is (A) $\left(\frac{1}{2}\right)^{x(x-1)} \quad$ (B) $\frac{1}{2} \sqrt{1+4 \log _{2} x}$ $\frac{1}{2}\left(1-\sqrt{1+4 \log _{2} x}\right)$ (D) not defined
275. The value of parameter $\alpha$, for which the function $f(x)=1+\alpha x, \alpha \neq 0$ is the inverse of itself

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276. Let $f: N \vec{Y}$ be a function defined as $f(x)=4 x+3$, where $Y=\{y \in N: y=4 x+3$ for some $x \in N\}$. Show that f is invertible and its inverse is (1) $g(y)=\frac{3 y+4}{3}$ (2) $g(y)=4+\frac{y+3}{4}$ (3) $g(y)=\frac{y+3}{4}$
(4) $g(y)=\frac{y-3}{4}$

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277. Let $Y=\left\{n^{2}: n \in N\right\} \in N$. Consider $f: N \rightarrow Y$ as $f(n)=n^{2}$. Show that $f$ is invertible. Find the inverse of $f$.

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278. Let $f: N \rightarrow R$ be a function defined as $f(x)=4 x^{2}+12 x+15$. Show that $f: N \rightarrow S$, where, S is the range of f , is invertible. Find the inverse of $f$.

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279. State with reason whether following functions have inverse (i)
$f:\{1,2,3,4 t h f=\{(1,10),(2,10),(3,10),(4,10)\}$ (ii)
$g:\{5,6,7,8\}$ withg $=\{(5,4),(6,3),(7,4),(8,2)\}($ iii $) ` h:\{2,3,4,5\}->\{7,9$

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280. State with reason whether following functions have inverse (i) $f:\{1,2,3,4\} \rightarrow\{10\}$ with $f=\{(1,10),(2,10),(3,10),(4,10)\}$ (ii) $g:\{5,6,7,8\} \rightarrow\{1,2,3,4\}$ with $=\{(5,4),(6,3),(7,4),(8,2)\}$ (iii) $\mathrm{h}:$ $\{2,3,4,5\}->\{7,9$
281. Find $f^{-1}$ if it exists: $f: A \rightarrow B$ where $A=\{0,-1,-3,2\}$; $B=\{-9,-3,0,6\}$ and $f(x)=3 x$.

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282. Find $f^{-1}$ if it exists: $f: A \rightarrow B$ where $A=\{1,3,5,7,9\} ; B=$ $\{0,1,9,25,49,81\}$ and $f(x)=x^{2}$.

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283. Show that the function $f: Q \rightarrow Q$ defined by $f(x)=3 x+5$ is invertible. Also, find $f^{-1}$.

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284. Consider $f: R \rightarrow R$ given by $f(x)=4 x+3$. Show that f is invertible. Find the inverse of $f$.
285. Consider $f: R_{+} \overrightarrow{4, \infty}$ given by $f(x)=x^{2}+4$. Show that $f$ is invertible with the inverse $f^{-1}$ of $f$ given by $f^{-1}(y)=\sqrt{y-4}$, where $R_{+}$is the set of all non-negative real numbers.

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286. If $f(x)=\frac{4 x+3}{6 x-4}, x \neq \frac{2}{3}$, show that $f o f(x)=x$ for all $x \neq \frac{2}{3}$. What is the inverse of $f$ ?

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287. Consider $f: R_{ \pm}>[-5, \infty)$ given by $f(x)=9 x^{2}+6 x-5$. Show that f is invertible with $f^{-1}(y)=\left(\frac{(\sqrt{y+6})-1}{3}\right)$
288. If $f: R \rightarrow R$ be defined by $f(x)=x^{3}-3$, then prove that $f^{-1}$ exists and find a formula for $f^{-1}$. Hence, find $f^{-1}(24)$ and $f^{-1}(5)$.

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289. A function $f: R \rightarrow R$ is defined as $f(x)=x^{3}+4$. Is it a bijection or not? In case it is a bijection, find $f^{-1}(3)$.

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290. If $f: Q \rightarrow Q, g: Q \rightarrow Q$ are two functions defined by $f(x)=2 x$ and $g(x)=x+2$, show that $f$ and $g$ are bijective maps. Verify that $(g o f)^{-1}=f^{-1} o g^{-1}$.

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291. Let $A=R-\{3\}$ and $B=R-\{1\}$. Consider the function $f: A^{\rightarrow}$ defined by $f(x)=\frac{x-2}{x-3}$. Show that is one-one and onto and hence find $f^{-1}$

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292. Consider $f: R_{ \pm}>\left[-9, \infty\left[\right.\right.$ given by $f(x)=5 x^{2}+6 x-9$. Prove that $f$ is invertible with $f^{-1}(y)=\frac{\sqrt{54+5 y}-3}{5}$

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293. Let $f: N^{\rightarrow}$ be a function defined as $f(x)=9 x^{2}+6 x-5$. Show that $f: N \vec{S}$, where $S$ is the range of $f$, is invertible. Find the inverse of $f$ and hence $f^{-1}(43)$ and $f^{-1}(163)$.

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294. If $f: R-1,1$ defined by $f(x)=\frac{10^{x}-10^{-x}}{10^{x}+10^{-x}}$ is invertible, find $f^{-1}$

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295. If $f: R \rightarrow(0,2)$ defined by $f(x)=\frac{e^{x}-e^{-x}}{e^{x}+e^{-x}}+1$ is invertible, find $f^{-1}$.

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296. Let $f:[-1, \infty] \overrightarrow{-1}$, is given by $f(x)=(x+1)^{2}-1, x \geq-1$. Show that $f$ is invertible. Also, find the set $S=\left\{x: f(x)=f^{-1}(x)\right\}$.

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297. Let $A=\{x \in R \mid-1 \leq x \leq 1\}$ and let $f: A \rightarrow A, g: A \rightarrow A$ be two functions defined by $f(x)=x^{2}$ and $g(x)=\frac{\sin (\pi x)}{2}$. Show that $g^{-1}$ exists but $f^{-1}$ does not exist. Also, find $g^{-1}$.
298. Let $f$ be a function from $R$ to $R$ such that $f(x)=\cos (x+2)$. Is $f$ invertible? Justify your answer.

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299. If $A=\{1,2,3,4\}$ and $B=\{a, b, c, d\}$. Define any four bijectives from $A$ to $B$. Also, give their inverse functions.

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300. Let $A$ and $B$ be two sets each with a finite number of elements.

Assume that there is an injective mapping from A to Band that there is an injective mapping from B to A Prove that there is a bijective mapping from $A$ to $B$.
301. If $f: A \vec{A}, g: A^{\rightarrow}$ are two bijections, then prove that $f o g$ is an injection (ii) $f o g$ is a surjection.

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302. If $f: A \rightarrow A, g: A \rightarrow A$ are two bijections, then prove that $f o g$ is an injection.

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303. Let $A=\{1,2,3,4\}$ and $B=\{a, b\}$ be two sets. Write total number of onto functions from $A$ to $B$.

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304. Write total number of one-one functions from set $A=\{1,2,3,4\}$ to set $B=\{a, b, c\}$.
305. If $f: R \rightarrow R$ is defined by $f(x)=x^{2}$, write $f^{-1}(25)$.

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306. If $f: C \rightarrow C$ is defined by $f(x)=x^{2}$, write $f^{-1}(-4)$. Here, $C$ denotes the set of all complex numbers.

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307. If $f: R \rightarrow R$ is given by $f(x)=x^{3}$, write $f^{-1}(1)$.

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308. Let $C$ denote the set of all complex numbers. A function $f: C \rightarrow C$ is defined by $f(x)=x^{3}$. Write $f^{-1}(1)$.
309. Let $f$ be a function from $C$ (set of all complex numbers) to itself given by $f(x)=x^{3}$. Write $f^{-1}(1)$.

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310. Let $f: R \rightarrow R$ be defined by $f(x)=x^{4}$, write $f^{-1}(1)$.

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311. If $f: C \rightarrow C$ is defined by $f(x)=x^{4}$, write $f^{-1}(1)$.

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312. If $f: R \rightarrow R$ is defined by $f(x)=x^{2}$, write $f^{-1}(25)$.
313. If $f: C \rightarrow C$ is defined by $f(x)=(x-2)^{3}$, write $f^{-1}(-1)$.

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314. If $f: R \rightarrow R$ is defined by $f(x)=10 x-7$, then write $f^{-1}(x)$.

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315. Let $f:\left\{-\frac{\pi}{2}, \frac{\pi}{2}\right\} \rightarrow R$ be a function defined by $f(x)=\cos [x]$. Write range ( $f$ ) .

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316. If $f: R \rightarrow R$ defined by $f(x)=3 x-4$ is invertible then write $f^{-1}(x)$.
317. If $f: R \rightarrow R, g: R \rightarrow R$ are given by $f(x)=(x+1)^{2}$ and $g(x)=x^{2}+1$, then write the value of $f o g(-3)$.

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318. Let $A=\{x \in R:-4 \leq x \leq 4$ and $x \neq 0\}$ and $f: A \rightarrow R$ be defined by $f(x)=\frac{|x|}{x}$. Write the range of $f$.

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319. Let $f:\left[-\frac{\pi}{2}, \frac{\pi}{2}\right] \rightarrow A$ be defined by $f(x)=\sin x$. If $f$ is a bijection, write set $A$.

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320. Let $f: R \rightarrow R^{+}$be defined by $f(x)=a^{x}, a>0$ and $a \neq 1$. Write $f^{-1}(x)$.
321. Let $f: R-\{-1\} \rightarrow R-\{1\}$ be given by $f(x)=\frac{x}{x+1}$. Write $f^{-1}(x)$.

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322. Let $f: R-\left\{-\frac{3}{5}\right\} \rightarrow R$ be a function defined as $f(x)=\frac{2 x}{5 x+3}$. Write $f^{-1}$ : Range of $f \rightarrow R-\left\{-\frac{3}{5}\right\}$.

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323. Let $f: R \rightarrow R, g: R \rightarrow R$ be two functions defined by $f(x)=x^{2}+x+1$ and $g(x)=1-x^{2}$. Write $f o g(-2)$.

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324. Let $f: R \rightarrow R$ be defined as $f(x)=\frac{2 x-3}{4}$. Write fof $^{-1}(1)$.

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325. Let $f$ be an invertible real function. Write $\left(f^{-1} o f\right)(1)+\left(f^{-1} o f\right)(2)++\left(f^{-1} o f\right)(100)$.

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326. Let $A=\{1,2,3,4\}$ and $B=\{a, b\}$ be two sets. Write total number of onto functions from $A$ to $B$.

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327. Write the domain of the real function $f(x)=\sqrt{x-[x]}$.

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328. Write the domain and range of function $f(x)$ given by $f(x)=\sqrt{[x]-x}$.

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329. Write the domain of the real function $f(x)=\frac{1}{\sqrt{|x|-x}}$

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330. Write whether $f: R \rightarrow R$ given by $f(x)=x+\sqrt{x^{2}}$ is one-one, many-one, onto or into.

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331. If $\mathrm{f}(\mathrm{x})=x+7$ and $g(x)=x-7, x R$, find $(f o g)(7)$
A. 7
B. 0
C. 14
D. none of these

## Answer: A

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332. What is the range of the function $f(x)=\frac{|x-1|}{x-1}$

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333. If $f: R \div R$ be defined by $f(x)=\left(3-x^{3}\right)^{1 / 3}$, then find $f o f(x)$

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334. If $f: R \rightarrow R$ is defined by $f(x)=3 x+2$, find $f(f(x))$.
335. Let $A=\{1,2,3\}, B=\{4,5,6,7\} \quad$ and let $f=\{(1,4),(2,5),(3,6)\}$ be a function from $A$ to $B$. State whether $f$ is one-one or not.

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336. If $f:\{5,6\} \rightarrow\{2,3\}$ and $g:\{2,3\} \rightarrow\{5,6\}$ are given by $f=\{(5,2),(6,3)\}$ and $g=\{(2,5),(3,6)\}$, find fog.

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337. Let $f: R \rightarrow R$ be the function defined by $f(x)=4 x-3$ for all $x \in R$. Then write $f^{-1}$.

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338. Which one the following relations on $A=\{1,2,3\}$ is a function? $f=\{(1,3),(2,3),(3,2)\}, g=\{(1,2),(1,3),(3,1)\}$

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339. Write the domain of the real function $f$ defined by $f(x)=\sqrt{25-x^{2}}$.

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340. Let $A=\{a, b, c, d\} \operatorname{and} f: A \vec{A}$ be given by
$f=\{(a, b),(b, d),(c, a),(d, c)\}$, write $f^{-1}$.

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341. Let $f, g: R^{\rightarrow}$ be defined by $f(x)=2 x+\operatorname{1andg}(x)=x^{2}-2$ for all $x \in R$, respectively. Then, find gof.
342. If the mapping $f:\{1,3,4\} \rightarrow\{1,2,5\}$ and $g:\{1,2,5\} \rightarrow\{1,3\}$ , given by $f=\{(1,2),(3,5),(4,1)\}$ and $g=\{(2,3),(5,1),(1,3)\}$ , write fog.

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343. If a function $g=\{(1,1),(2,3),(3,5),(4,7)\}$ is described by $g(x)=\alpha x+\beta$, find the values of $\alpha a n d \beta$.

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344. If $f(x)=-4-(x-7)^{3}$, write $f^{-1}(x)$.

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345. $f: R \rightarrow R$ given by $f(x)=x+\sqrt{x^{2}}$ is (a) injective (b) surjective (c) bijective (d) none of these

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346. If $f: A \rightarrow B$ given by $3^{f(x)}+2^{-x}=4$ is a bijection, then $` \mathrm{~A}=\{\mathrm{x}$ in R :-1

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347. The function $f: R \rightarrow R$ defined by $f(x)=2^{x}+2^{|x|}$ is (a) one-one and onto (b) many-one and onto (c) one-one and into (d) many-one and into

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348. Let the function $f: R-\{-b\} \rightarrow R-\{1\}$ be defined by $f(x)=\frac{x+a}{x+b}, a \neq b$, then (a) $f$ is one-one but not onto (b) $f$ is onto but not one-one (c) $f$ is both one-one and onto (d) none of these

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349. The function $f: A \rightarrow B$ defined by $f(x)=-x^{2}+6 x-8$ is a bijection, if $A=(-\infty, 3]$ and $B=(-\infty, 1]$ (b) $A=[-3, \infty)$ and $B=(-\infty, 1]$ (c) $A=(-\infty, 3]$ and $B=[1, \infty)$ (d) $A=[3, \infty)$ and $B=[1, \infty)$

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350. Let $A=\{x \in R:-1 \leq x \leq 1\}=B$. Then, the mapping $f: A \rightarrow B$ given by $f(x)=x|x|$ is (a) injective but not surjective (b) surjective but not injective (c) bijective (d) none of these
351. Let $f: R \rightarrow R$ be given by $f(x)=[x]^{2}+[x+1]-3$, where $[x]$ denotes the greatest integer less than or equal to $x$. Then, $f(x)$ is (a) many-one and onto (b) many-one and into (c) one-one and into (d) oneone and onto

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352. Let $M$ be the set of all $2 \times 2$ matrices with entries from the set $R$ of real numbers. Then the function $f: M \rightarrow R$ defined by $f(A)=|A|$ for every $A \in M$, is (a) one-one and onto (b) neither one-one nor onto (c) one-one but not onto (d) onto but not one-one

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353. The function $f:[0, \infty) \rightarrow R$ given by $f(x)=\frac{x}{x+1}$ is (a) one-one and onto (b) one-one but not onto (c) onto but not one-one (d) neither one-one nor onto
354. The range of the function $f(x)={ }^{7-x} P_{x-3}$ is (a) $\{1,2,3,4,5\}$ (b) $\{1$, $2,3,4,5,6\}$ (c) $\{1,2,3,4\}$ (d) $\{1,2,3\}$

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355. A function $f$ from the set of natural numbers to integers is defined by $n$ when $n$ is odd $f(n) 3$, when $n$ is even Then $f$ is (b) one-one but not onto
a) neither one-one nor onto (c) onto but not one-one (d) one-one and onto both

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356. Let $f$ be an injective map. with domain ( $x, y, z$ and range ( $1,2,3$ ), such that exactly one following statements is correct and the remaining are false : $f(x)=1, f(y) \neq 1, f(z) \neq 2$ The value of $\left.f^{-1}\right)(1)$ is
357. Which of the following function from $Z$ to itself are bijections? $f(x)=x^{3}$ (b) $f(x)=x+2 f(x)=2 x+1$ (d) $f(x)=x^{2}+x$

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358. Let $A=[-1,1]$. Then, discuss whether the following functions from A to itself are one-one onto or bijective: $f(x)=\frac{x}{2}$ (ii) $g(x)=|x|$ (iii) $h(x)=x^{2}$

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359. Let $A\} x:-1 \leq x \leq 1\}$ andf: $A^{\rightarrow}$ such that $f(x)=x|x|$, then $f$ is a bijection (b) injective but not surjective Surjective but not injective (d) neither injective nor surjective

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360. If the function $f: R \vec{A}$ given by $f(x)=\frac{x^{2}}{x^{2}+1}$ is surjection, then find $A$.

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361. If a function $f:[2, \infty) \rightarrow R \quad$ defined by $f(x)=(x-1)(x-2)(x-3)$ is (a) one-one but not onto (b) onto but not one-one (c) both one and onto (d) neither one-one nor onto

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362. The function $f:[-1 / 2,1 / 2] \rightarrow[-\pi / 2, \pi / 2]$ defined by $f(x)=\sin ^{-1}\left(3 x-4 x^{3}\right)$ is (a) bijection (b) injection but not a surjection (c) surjection but not an injection (d) neither an injection nor a surjection

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363. Let $f: R \rightarrow R$ be a function defined by $f(x)=\frac{e^{|x|}-e^{-x}}{e^{x}+e^{-x}}$ then -(1) $f$ is bijection (2) $f$ is an injection only (3) $f$ is a surjection (4) $f$ is neither injection nor a surjection

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364. Let $f: R-\{n\} \rightarrow R$ be a function defined by $f(x)=\frac{x-m}{x-n}$ such that $m \neq n 1$ ) f is one one into function2) f is one one onto function3) f is many one into funciton4) $f$ is many one onto funcionn then

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365. Let $f: R \rightarrow R$ be a function defined by $f(x)=\frac{x^{2}-8}{x^{2}+2}$. Then, $f$ is (a) one-one but not onto (b) one-one and onto (c) onto but not one-one (d) neither one-one nor onto
366. $f: R \rightarrow R$ is defined by $f(x)=\frac{e^{x \wedge} 2-e^{-x \wedge} 2}{e^{x \wedge} 2+e^{-x \wedge} 2}$ is (a) one-one but not onto (b) many-one but onto (c) one-one and onto (d) neither oneone nor onto

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367. The function $f: R \rightarrow R, f(x)=x^{2}$ is (a) injective but not surjective (b) surjective but not injective (c) injective as well as surjective (d) neither injective nor surjective

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368. A function $f$ from the set of natural numbers to integers defined by $f(n)=\left\{\frac{n-1}{2}\right.$, when nis odd $-\frac{n}{2}$, whennis even is (a) neither one-one nor onto (b) one-one but not onto (c) onto but not one-one (d) one-one and onto both
369. Which of the following functions from $A=\{x \in R:-1 \leq x \leq 1\}$ to itself are bijections? $f(x)=|x| \quad$ (b) $f(x)=\frac{\sin (\pi x)}{2}$
$f(x)=\frac{\sin (\pi x)}{4}$ ( d ) none of these

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370. 

Let
$f: Z \rightarrow Z$
be given
by
$f(x)= \begin{cases}\frac{x}{2}, & \text { if } \quad x \text { is even, } 0, \\ \text { if } & x \text { is odd. Then, } \mathrm{f} \text { is (a) onto but }\end{cases}$ not one-one (b) one-one but not onto (c) one-one and onto (d) neither one-one nor onto

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371. The function $f: R \rightarrow R$ defined by $f(x)=6^{x}+6^{|x|}$ is (a) one-one and onto (b) many one and onto (c) one-one and into (d) many one and into
372. Let $f(x)=x^{2}$ and $g(x)=2^{x}$. Then the solution set of the equation $f \circ g(x)=g \circ f(x)$ is $R(b)\{0\}$ (c) $\{0,2\}$ (d) none of these

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373. If $f(x)=3 x-5$, then $f^{-1}(x)$ is given by $\frac{1}{(3 x-5)}$ is given by $\frac{(x+5)}{3}$ does not exist because $f$ is not one-one does not exist because $f$ is not onto

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374. If $g(f(x))=|\sin x| \operatorname{and} f(g(x))=(\sin \sqrt{x})^{2} \quad$, then $f(x)=\sin ^{2} x, g(x)=\sqrt{x} \quad f(x)=\sin x, g(x)=|x|$ $f\left(x=x^{2}, g(x)=\sin \sqrt{x}\right.$ fand $g$ cannot be determined
375. The inverse of the function $f: R \overrightarrow{x \in R: x<1}$ given by $f(x)=\frac{e^{x}-e^{-x}}{e^{x}+e^{-x}}$, is $\frac{1}{2} \frac{\log (1+x)}{1-x}$ (b) $\frac{1}{2} \frac{\log (2+x)}{2-x} \frac{1}{2} \frac{\log (1-x)}{1+x}$
None of these

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376. If the function $f:(1,) \overrightarrow{1, \infty}$ is defined by
$f(x)=2^{x(x-1)}$, thenf $f^{-1}(x) \quad$ is $\quad\left(\frac{1}{2}\right)^{x(x-1)}$
$\frac{1}{2}\left(1+\sqrt{1+4(\log )_{2} x}\right) \frac{1}{2}\left(1-\sqrt{1+(\log )_{2} x}\right.$

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377. Let $f(x)=\frac{1}{1-x}$. Then, $\{f o(f o f)\}(x)=x$ for all $x \in R$ (b) $x$ for all $x \in R-\{1\}$ (c) $x$ for all $x \in R-\{0,1\}$ (d) none of these

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378. If the function $f: R \rightarrow R$ be such that $f(x)=x-[x]$, where $[x]$ denotes the greatest integer less than or equal to $x$, then $f^{-1}(x)$ is

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379. If $F:[1, \infty) \overrightarrow{2, \infty}$ is given by $f(x)=x+\frac{1}{x}$, thenf $f^{-1}(x)$ equals. $\frac{x+\sqrt{x^{2}-4}}{2}$ (b) $\frac{x}{1+x^{2}}$ (c) $\frac{x-\sqrt{x^{2}-4}}{2} 1+\sqrt{x^{2}-4}$

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380. Let $g(x)=1+x-[x] \operatorname{and} f(x)=\{-1, x<00, x=0 f, x>0$. Then for all $x, f(g(x))$ is equal to (where [.] represents the greatest integer function). $x$ (b) 1 (c) $f(x)$ (d) $g(x)$

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381. Let $f(x)=\frac{\alpha x}{(x+1)}, x \neq-1$. The for what value of $\alpha$ is $f(f(x))=x ? \sqrt{2}$ (b) $-\sqrt{2}$ (c) 1 (d) -1

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382. If $f:[2, \infty) \rightarrow(-\infty, 4]$, where $f(x)=x(4-x)$ then find $f^{-1}(x)$

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383. If $f: \overrightarrow{R-1,1}$ is defined by $f(x)=-\frac{x|x|}{1+x^{2}}$, then $f^{-1}(x)$ equals $\sqrt{\frac{|x|}{1-|x|}}$ (b) $-\operatorname{sgn}(x) \sqrt{\frac{|x|}{1-|x|}}-\sqrt{\frac{x}{1-x}}$ (d) none of these

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384. If $g(x)=x^{2}+x-2 \operatorname{and} \frac{1}{2} g \circ f(x)=2 x^{2}-5 x+2$, then which is not a possible $f(x) ? 2 x-3$ (b) $-2 x+2 x-3$ (d) None of these

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385. If $f(x)=\sin ^{2} x$ and the composite function $g(f(x))=|\sin x|$, then $g(x)$ is equal to $\sqrt{x-1}$ (b) $\sqrt{x}$ (c) $\sqrt{x+1}$ (d) $-\sqrt{x}$

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386. Let $f: R \rightarrow R$ be given by $f(x)=x^{2}-3$. Then, $f^{-1}$ is given by $\sqrt{x+3}$ (b) $\sqrt{x}+3$ (c) $x+\sqrt{3}$ (d) none of these

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387. Let $f(x)=x^{3}$ be a function with domain $\{0,1,2,3\}$. Then domain of $f^{-1}$ is (a) $\{3,2,1,0\}$ (b) $\{0,-1,-2,-3\}$ (c) $\{0,1,8,27\}$ (d) $\{0,-1,-8,-27\}$

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388. Let $f: R \rightarrow R$ be given by $f(x)=x^{2}-3$. Then, $f^{-1}$ is given by $\sqrt{x+3}$ (b) $\sqrt{x}+3$ (c) $x+\sqrt{3}$ (d) none of these

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389. Let $f: R \rightarrow R$ be given by $f(x)=\tan x$. Then, $f^{-1}(1)$ is $\frac{\pi}{4}$ $\left\{n \pi+\frac{\pi}{4}: n \in Z\right\}$ (c) does not exist (d) none of these

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390. Let $A=\{1,2, \ldots, n\}$ and $B=\{a, b\}$. Then number of subjections from $A$ into $B$ is nP2 (b) $2^{n}-2$ (c) $2^{n}-1$ (d) nC2

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391. If the set $A$ contains 5 elements and the set B contains 6 elements, then the number of one-one and onto mappings from $A$ to $B$ is 720 (b)

120 (c) 0 (d) none of these

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392. If the set $A$ contains 7 elements and the set $B$ contains 10 elements, then the number of one-one functions from $A$ to $B$ is $10 C 7$ (b) $10 C 7 \times 7$ ! (c) $7^{10}$ (d) $10^{7}$

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393. Let $f: R-\left\{\frac{3}{5}\right\} \rightarrow R$ be defined by $f(x)=\frac{3 x+2}{5 x-3}$. Then

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## Others

1. State with reasons whether $h:\{2,3,4,5\} \rightarrow\{7,9,11,13\}$ with $h=\{(2,7),(3,9),(4,11),(5,13)\}$
2. Consider $f:\{1,2,3\} \rightarrow\{a, b, c\}$ and $g:\{a, b, c\} \rightarrow$ \{apple, ball, cat $\}$ defined as $f(1)=a, f(2)=b, f(3)=c, g(a)=$ apple, $g(b)=$ ball and $g(c)=$ cat. Show that $f, g$ and gof are invertible. Find $f^{-1}, g^{-1}$ and $(g \circ f)^{-1}$ and show that $(g \circ f)^{-1}=f^{-1} o g^{-1}$.

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3. Let $A=\{1,2,3,4\} ; B=\{3,5,7,9\} ; C=\{7,23,47,79\}$ and $f: A \rightarrow B, g: B \rightarrow C$ be defined as $f(x)=2 x+1$ and $g(x)=x^{2}-2$. Express $(g o f)^{-1}$ and $f^{-1} o g^{-1}$ as the sets of ordered pairs and verify that $(g \circ f)^{-1}=f^{-1} o g^{-1}$.

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4. Let $A=\{x \in R:-1 \leq x \leq 1\}=B$ and $C=\{x \in R: x \geq 0\}$ and let

$$
S=\left\{(x, y) \in A \times B: x^{2}+y^{2}=1\right\}
$$

$S_{0}=\left\{(x, y) \in A \times C: x^{2}+y^{2}=1\right\}$. Then $S$ defines a function from $A$ to $B$ (b) $S_{0}$ defines a function from $A$ to $C$ (c) $S_{0}$ defines a function from $A$ to $B$ (d) $S$ defines a function from $A$ to $C$

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5. The distinct linear functions which map $[-1,1]$ onto $[0,2]$ are
$f(x)=x+1, g(x)=-x+1$
(b) $f(x)=x-1, g(x)=x+1$
$f(x)=-x-1, g(x)=x-1(\mathrm{~d})$ none of these

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6. Let $f: R \rightarrow R$ be defined as $f(x)=\left\{\begin{array}{lll}2 x & \text { if } x>3 \\ x^{2} & \text { if } x<1\end{array}\right.$
find value of $f(-1)+f(4)$

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