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## MATHS

## BOOKS - RD SHARMA MATHS

## (HINGLISH)

## LINEAR PROGRAMMING

## Solved Examples And Exercises

1. A gardener has supply of fertilizer A which
consists of $10 \%$ nitrogen and $6 \%$ phosphoric
acid and fertilizer $B$ which consists of $5 \%$ nitrogen and 100/6 phosphoric acid. After testing the soil conditions, he finds that he needs at least 14 kg of nitrogen and 14 kg of phosphoric acid for his crop. If fertilizer A costs 10.60 per kg and fertilizer B costs 8 AO per kg, what is the minimum 'cost at which the farmer can meet the nutrient requirement by using a combination of both types of fertilizers? Rs. 1488 b. Rs. 1576 c. Rs. 1648
2. A fruit grower can use two types of fertilizer
in his garden, brand P and brand Q . The amounts (in kg ) of nitrogen, phosphoric acid, potash, and chlorine m a bag of each brand are given $m$ the table. Tests indicate that the
garden needs at least 240 kg of phosphoric acid, at least 270 kg of potash and at most 310
kg of chlorine. If the grower wants to minimise
the amount of nitrogen added to the garden, how many bags of each brand should be used?

What is the minimum amount of nitrogen
added in the garden?
3. Solve the following linear programming problem graphically: Maximise
$Z=4 x+y \ldots(1)$ subject to the constraints: $x+y \leq 50 \ldots$ (2) $3 x+y \leq 90 \ldots$
(3) $x \geq 0, y \geq 0 \ldots$ (4)

## D Watch Video Solution

4. (Transportation problem) There are two
factories located one at place $P$ and the other
at place Q. From these locations, a certain commodity is to be delivered to each of the three depots situated at A, B and C. The weekly requirements of the depo

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5. A manufacturer of a line of patent medicines
is preparing a production plane on medicines
$A$ and $B$. There are sufficient ingredients
available to make 20,000 bottles of $A$ and 40 ,

000 bottles of $B$ but there are only 45,000
bottles into which either of the medicines can be put. Further more, it takes 3 hours to prepare enough material to fill 100 bottles of

A, it takes on hours to prepare enough material to fill 1000 bottles of $B$ and there are 66 hours available for this operation. Te profit is Rs. 8 per bottle for $A$ and Rs. 7 per bottle for
B. Formulate this problem as a linear programming problem.

## - Watch Video Solution

6. A manufacturer makes two types of toys $A$
and B. Three machines are needed for this
purpose and the tune (in minutes) required
for each toy on the machines is given below:

Each machine is available for a maximum of 6
hours per day. If the profit on each toy of type

A is Rs 7.50 and that on each toy of type $B$ is Rs
5. show that 15 toys of type $A$ and 30 of the $B$
should be manufactured $m$ a day to get maximum profit.
7. An automobile manufacturer makes
automobiles and trucks in a factory that is divided into two shops. Shop A, which performs the basic assembly operation must work 5 man-days on each truck but only 2 mandays on each automobile. Shop B, which performs finishing operations, must work 3 man-days for each automobile or truck that it produces. Because of men and machine limitations, shop A has 180 man-days per week available while shop B has 135 man-days per week. If the manufacturer makes a profit of Rs.

30000 on each truck and Rs. 2000 on each automobile, how many of each should he produce to maximize his profit?, Formulate this as a LPP.

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8. To maintain his health a person must fulfil certain minimum daily requiremens for several kinds of nutrients. Assuming that there are only thee kinds of nutrients-calcium, protein and calories and the person's diet consists of
only two food items, I and II, whose price and nutrient contents are shown in the table below: , Food I (per Ib), Food II (per Ib), Minimum daily requirement for the nutrient

Calcium Protein Calories, 105 2, 54 6, 202013

Price (Rs.), 60, 100, What combination of two food items will satisfy the daily requirement and entail the least cost? Formulate this as a LPP.

## D Watch Video Solution

9. A firm manufactures two types of products,
$A$ and $B$, and sells them at a profil of 3 per unit
to type B product and 5 perunit of type A
product. Both product is processed on two
machines M1and M2 One unit of type $A$
requires one minute of processing time on M1
and two minutes of processing time on M 2 i
whereas one unit of type $B$ requires one minute of processing time on M1 and one minute on $M$ Machines sells them at a profit of

5 per unit of type $A$ and $M$, and $M$, are respectively available for at most 5 hours and

6 hours in a day. Find out how many units of each type of product the firn should produce a day in order to maximize the profit. Solve the problem graphically [CHSE 2000]

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10. A company sells two different products A and B . The two products are produced in a common production process and are sold in two different markets. The production process has a total capacity of 45000 man-hours. It
takes 5 hours to produce a unit of $A$ and 3
hours to produce a unit of $B$. The market has
been surveyed and company officials feel that the maximum number of units of $A$ that can be sold is 7000 ad that of $B$ is 10,000 . If the profit is Rs. 60 per unit for the product $A$ and Rs. 40 per unit for the product $B$, how many units of each product should be sold to maximize profit? Formulate the problem as LPP.
11. The objective of $A$ diet problem is to ascertain the quantities of certain foods that
should be eaten to meet certain nutritional requirement at minimum cost. The consideration is limited to milk, beaf and eggs,
and to vitamins $A, B, C$. The number of milligrams of each of these vitamins contained within A unit of each food is given below:

Vitamin, Litre of milk, Kg of beaf, Dozen of eggs, Minimum daily requirements A B C, 1100

10, 110 100, 1010 10, 1 mg 50 mg 10 mg Cost,

Rs. 1.00 , Rs. 1.10 , Rs. 0.50 , What is the linear programming formulation for this problem?

## D Watch Video Solution

12. (Transportation problem) There are two factories located one at place $P$ and the other at place Q. From these locations, a certain commodity is to be delivered to each of the three depots situated at A, B and C. The weekly requirements of the depo
13. A factory produces two product $P_{1} a n d P_{2}$.

Each of the product $P_{1}$ requires 2 hrs for moulding, 3 hrs for grinding and 4 hrs for polishing, and each of the product $P_{2}$ requires

4 hrs for moulding, 2 hrs for grinding and 2 hrs for polishing. The factory has moulding machine available for 20 hrs , grinding machine
for 24 hrs polishing machine available for 13 hrs. The profit is Rs. 5 per unit of $P_{1}$ and Rs 3 per unit of $P_{2}$ and the factory can sell all that it
produces. Formulate the problem as a linear programming problem to maximize the profit.

## D Watch Video Solution

14. A merchant plans to sell two types of personal computers - a desktop model and a portable model that will cost Rs 25000 and Rs

40000 respectively. He estimates that the total monthly demand of computers will not exceed

250 units. Determine the number of units of each type of computers which the merchant
should stock to get maximum profit if he does
not want to invest more than Rs 70 lakhs and
if his profit on the desktop model is Rs 4500 and on portable model is Rs 5000.

## D Watch Video Solution

15. A toy company manufactures two types of doll; a basic version doll; a basic version doll A and a deluxe version doll B. Each doll of type B takes twice as long to produce as one of type.

A and the company would have time to ,make
a maximum of 2,000 per day if it produces only the basic version. The supply of plastic is sufficient to produce 1500 dolls per day (both
$A$ and $B$ combined). The deluxe version requires a fancy dress of which there are only 600 per day available. If the company makes profit Rs. 3 and Rs. 5 per doll respectively o doll A and doll B; how many of each should be produced per day in order to maximize profit?
16. A manufacturer of a line of patent medicines is preparing a production plane on medicines $A$ and $B$. There are sufficient ingredients available to make 20,000 bottles of $A$ and 40,000 bottles of $B$ but there are only 45,000 bottles into which either of the medicines can be put. Further more, it takes 3
hours to prepare enough material to fill 100 bottles of $A$, it takes on hours to prepare enough material to fill 1000 bottles of $B$ and there are 66 hours available for this operation.

Te profit is Rs. 8 per bottle for A and Rs. 7 per
bottle for $B$. Formulate this problem as $a$ linear programming problem.

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17. A furniture form manufactures chairs and tables, each requiring the use of three machines A, B and C. Production of one chair requires 2 hours on machine $A$, 1 hour on machine $B$, and 1 hour on machine $C$. Each table requires 1 hour each on machines $A$ and $B$ and 3 hours on machine C. Profit realized by
selling one chair is Rs. 30 while for a table the
figure is Rs. 60. The total time available per week on machine $A$ is 70 hours, on machine $B$ is 40 hours, and on machine $C$ is 90 hours. How many chairs and table should be made per week so as to maximize profit? Develop a mathematical formulation.

## D Watch Video Solution

18. A company makes two kinds of leather belts, $A$ and $B$. Belt $A$ is high quality belt, and $B$
is of lower quality. The respective profits are

Rs. 40 and Rs. 30 per belt. Each belt of type $A$
requires twice as much time as a belt of type $B$, and if all belts were of type $B$, the company
could make 1000 belts per day. The supply of
leather is sufficient for only 800 belts per day
(both $A$ and $B$ combined). Belt $A$ requires $a$ fancy buckle, and only 400 buckles per day are available. There are only 700 buckles available
for belt B. What should be the daily production of each type $f$ belt? Formulate the problem as a LPP.
19. A resourceful home decorator manufactures two types of lamps say A and B.

Both lamps go through two technician, first a
cutter, second a finisher. Lamp A requires 2 hours of th cutter's time and 1 hour of the finisher's time. Lamp B requires 1 hour of cutter's and 2 hours of finisher's time. The cutter has 104 hours and finisher has 76 hours of time available each month. Profit o one
lamp $A$ is Rs. 6.00 and on one lamp $B$ is Rs.11.00. Assuming that he can sell all that he
produces, how many of each type of lamps should he manufacture to obtain the best return.

## D Watch Video Solution

20. A diet is to contain at least 4000 units of carbohydrates, 500 units of fat and 300 units of protein. Two foods $F_{1}$ and $F_{2}$ are available.

Food $F_{1}$ costs 2 Rs. per unit and food $F_{2}$ costs

4 Rs. per unit. A unit of food $F_{1}$ contains 10 units of carbohydrates, 20 units of fat and 15
units of protein. A unit of food $F_{2}$ contains 25
units of carbohydrates, 10 units of fat and 20
units of protein. Find the minimum cost for a diet that consists of a mixture of these two foods and also meets the minimum requirements.

## D Watch Video Solution

21. A dietician wishes to mix two types of food
in such a way that the vitamin contents of the mixture contain at least 8 units of Vitamin A
and 10 units of vitamin C, Food I contains 2
units per $k g$ of vitamin A and 1 unit per $k g$ of
vitamin C while food II contains 1 unit per $k g$
of vitamin A and 2 units per $k g$ of vitamin C. It
costs $R s 50.00$ per $k g$ to purchase food I and

Rs. 70.00 per $k g$ to produce food II.

Formulate the above linear programming problem to minimize the minimize the cost of such a mixture.

## D Watch Video Solution

22. A farmer mixes two brands $P$ and $Q$ of cattle feed. Brand $P$, costing $R s 250$ per $b a g$, contains 3 units of nutritional element $A, 2.5$ units of element $B$ and 2 units of element $C$.

Brand $Q$ costing $R s 200$ per bag contains 1.5
units of nutritional element $A, 11.25$ units of element $B$, and 3 units of element $C$. The minimum requirements of nutrients $A, B$ and
$C$ are 18 units, 45 units and 24 units respectively. Determine the number of bags of each brand which should be mixed in order to produce a mixture having a minimum cost per
bag? What is the minimum cost of the mixture per bag?

## D Watch Video Solution

23. Kellogg is a new cereal formed of a mixture of bran and rice, that contains at least 88 grams of protein and at least 36 milligrams of iron. Knowing that bran contains 80 grams of protein and 40 milligrams of iron per kilogram and that rice contains 100 grams of protein and 30 milligrams of iron per kilogram, find
the minimum cost of producing this new cereal f bran costs5 per kilogram and rice costs 4 per kilogram

## D Watch Video Solution

24. Solve the following liner programming problems by graphical method: Maximize
$Z=-x_{1}+2 x_{2}$, if possible, Subject to the
constraints $x_{1}-x_{2} \leq-1 \quad-x_{1}+x_{2} \leq 0$
$x_{1}, x_{2} \geq 0$

D Watch Video Solution
25. There are two types of fertilisers ' $A$ ' and ' $B$ '.
' $A$ ' consists of $12 \%$ nitrogen and $5 \%$ phosphoric acid whereas ' $B$ ' consists of $4 \%$ nitrogen and 5\% phosphoric acid. After testing the soil conditions, farmer finds that he needs at least 12 kg of nitrogen and 12 kg of phosphoric acid for his crops. If ' $A$ ' costs Rs.

10 per kg and ' $B$ ' cost Rs. 8 per kg , then graphically determine how much of each type of fertilizer should be used so that nutrient requirement are met at a minimum cost.
A. $A=30 \mathrm{~kg} B=210 \mathrm{~kg}$

$$
\text { B. } A=40 \mathrm{~kg} B=200 \mathrm{~kg}
$$

C. $A=50 \mathrm{~kg} B=220 \mathrm{~kg}$
D. $A=60 \mathrm{~kg} B=240 \mathrm{~kg}$

Answer: A

## D Watch Video Solution

26. A dietician wishes to mix together two kinds of food $X$ and $Y$ m such a way that the mixture contains at least 10 units of vitamin $A$,

12 units of vitamin B and 8 units of vitamin C.

The vitamin contents of one kg food is given below: One kg of food X costs Rs 16 and one kg of food $Y$ costs Rs 20. Find the least cost of the mixture which will produce the required diet?

## D Watch Video Solution

27. (Manufacturing problem) A manufacturing
company makes two models $A$ and $B$ of $a$ product. Each piece of Model A requires 9
labour hours for fabricating and 1 labour hour
for finishing. Each piece of Model B requires 12
labour hours for fabricating and 3 labour hours for finishing. For fabricating and finishing, the maximum labour hours available are 180 and 30 respectively. The company makes a profit of Rs 8000 on each piece of model A and Rs 12000 on each piece of Model
B. How many-pieces of Model A and Model B
should be manufactured per week to realise a maximum profit? What is the maximum profit per week?
28. Solve the following linear programming problem graphically: Maximize $Z=50 x+15 y$ Subject to $5 x+y \leq 100 x+y \leq 60 x, y \geq 0$

## D Watch Video Solution

29. Determine graphically the minimum value
of the
objective
function
$Z=50 x+20 y \ldots$ (1) subject to
the constraints: $\quad 3 x-y \geq-5$
$3 x+y \geq 3$. . .(3) $2 x-3 j \leq 12$. . .(4) $x \geq 0, y \geq 0 \ldots$ (5)

## D Watch Video Solution

30. Solve the Following Linear Programming Problem graphically : Minimise
$Z=3 x+4 y$ Subject to $x+2 y \leq 8,3 x+2 y \leq 12, x \geq 0, y \geq 0$.

## - Watch Video Solution

31. A linear programming problem is as
follows: Minimize $30 x+50 y$ subject to the constraints, $3 x+5 y \geq 152 x+3 y \leq 18 x \geq 0, y \geq 0$

In the feasible region, the minimum value of $Z$ occurs at
A. a Unique Point
B. no point
C. infinite many point
D. two point only

## - Watch Video Solution

32. In a linear programming problem, the constraints on the decision variables x and y are $x-3 y \geq 0, y \geq 0,0 \leq x \leq 3$. The feasible region
A. is not in the first quadrant
B. is bounded in the first quadrant
C. is unbounded in the first quadrant
D. does not exist

## Answer: B

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33. Solve the Following Linear Programming
Problem graphically : Maximise
$Z=5 x+3 y$ subject to
$3 x+5 y \leq 15,5 x+2 y \leq 10, x \geq 0, y \geq 0$.

## - Watch Video Solution

34. A dealer wishes to purchase a number of
fans and sewing machines. He has only Rs.

5,760 to invest and has a space for at most 20
items. A fan costs him Rs. 360 and a sewing machine Rs. 240. His expectation is that he can
sell a fan at a profit of Rs. 22 and a sewing machine at a profit of Rs. 18. Assuming that he can sell all the items that he can buy, how should he invest his money in order to maximize the profit? Formulate this as a linear programming problem and solve it graphically.
35. A small manufacturer has employed 5
skilled men and 10 semi - skilled men and
makes an article in two qualities-deluxe model
and an ordinary model. The making of a deluxe
model requires 2 hrs work by a skilled man and

2 hrs work by a semi skilled man. The ordinary
model requires 1 hr by a skilled man and 3 hrs
by a semi skilled man. By union rules, no man
may work more than 8 hrs per day. The manufacture's clear profit on deluxe model is

Rs. 15 and an ordinary model is Rs. 10. How
many of each type should be made in order to maximize his total daily profit.

## D Watch Video Solution

36. A factory manufactures two types of screws, A and B. Each type of screw requires
the use of two machines, an automatic and a
hand operated. It takes 4 minutes on the automatic and 6 minutes on hand operated machines to manufacture a package of screws

A, while it takes 6 minutes on automatic and 3
minutes on the hand operated machines to
manufacture a package of screws B. Each machine is available for at the most 4 hours on any day. The manufacturer can sell a package of screws $A$ at a profit of 70 paise and screws $B$ at a profit of Rs 1. Assuming that he can sell all the screws he manufactures, how many packages of each type should the factory owner produce in a day in order to maximise his profit? Formulate the above LPP and solve it graphically and determine the maximum profit.
37. Reshma wishes to mix two types of food $P$ and $Q$ in such a way that the vitamin contents of the mixture contain at least 8 units of vitamin $A$ and 11 units of vitamin $B$. Food $P$ costs Rs $60 / \mathrm{kg}$ and Food Q costs Rs $80 / \mathrm{kg}$.

Food $P$ contains 3 units/kg of Vitamin $A$ and 5 units / kg of Vitamin B while food Q contains 4 units "kg of Vitamin A and 2 units $/ \mathrm{kg}$ of vitamin B. Determine the minimum cost of the mixture.
38. For an objective function $Z=a x+b y$, where $a$, b $>0$; the corner points of the feasible region determined by a set of constraints (linear inequalities) are ( 0,20 ), ( 10,10 ), ( 30,30 ) and ( 0 ,
40). The condition on $a$ and $b$ such that the maximum $Z$ occurs at both the points $(30,30)$ and $(0,40)$ is:

$$
\text { A. } b-3 a=0
$$

$$
\text { B. } a=3 b
$$

C. $a+2 b=0$
D. $2 a-b=0$

## Answer: A

## D Watch Video Solution

39. Solve each of the following linear programming problems by graphical method.

Maximize $Z=x+y$ Subject to $-2 x+y \leq 1$
$x \leq 2 x+y \leq 3 x, y \geq 0$
40. Solve each of the following linear programming problems by graphical method. Maximize $Z=3 x+3 y$ Subject to the constraints $x-y \leq 1 x+y \geq 3 x, y \geq 0$

## - Watch Video Solution

41. One kind of cake requires 200 g of flour and 25 g of fat, and another kind of cake requires 100 g of flour and 50 g of fat. Find the
maximum number of cakes which can be made
from 5 kg of flour and 1 kg of fat assuming that there is no shortage of the other ingredients used in making the cakes. Make an L.P.P. of the above and solve it graphically.

## D Watch Video Solution

42. If a young man rides his motorcycle at 25
$\mathrm{km} / \mathrm{hr}$, he has to spend 2 per kilometer on
petrol if per he rides it at a faster speed of 40
$\mathrm{km} / \mathrm{hr}$ the petrol cost increases to 5 per
kilometer.He has 100 to spend on petrol and wishes to find the maximum distance he can travel within one hours. Express this as a linear programming problem and then solve it.

## - Watch Video Solution

43. Two tailors $A$ and $B$ earns 15 and 20 per dayrespectively. A can stitch 6 shirts and 4 paints while Bcan stitch 10 shirts and 4 paints per day. To minimise the cost to stitch 60
shirts and 32 paints, how manydays should they work?

## D Watch Video Solution

44. A manufacturer makes two types of toys $A$
and B. Three machines are needed for this
purpose and the tune (in minutes) required
for each toy on the machines is given below:
Each machine is available for a maximum of 6
hours per day. If the profit
45. A factory uses three different resources for
the manufacture of two different productoof the resource $A, 12$ units of $B$ and 16 unit of
$C$ being available. One unit of there quires
2,2 and 4 units of the respective resources
and one unit of the second requires

4,2 and 0 units of respective resources. It is
known that the first product givesatof 2 monetary units per unit and the second 3.

Formulate the linear programming problem

How many units of each product should be
manufactured for maximizing the profit? solve it graphically.

## D Watch Video Solution

46. A cottage industry manufactures pedestal lamps and wooden shades, each requiring the use of grinding/cutting machine and a sprayer.

It takes 2 hours on the grinding/cutting machine and 3 hours on the sprayer to manufacture a pedestal lamp. It takes one
hour on the grinding/cutting machine and 2
hours on the sprayer to manufacture a shade.
On any day, the sprayer is available for at the most 20 hours and the grinding/cutting machine for at the most 12 hours. The profit from the sale of a lamp is Rs. 5 and that from a shade is Rs. 3. Assuming that the manufacturer can sell all the lamps and shades that he produces, how should he schedule his daily production in order to maximise his profit? Make an L.P.P. and solve it graphically.
47. A small firm manufactures items $A$ and $B$.

The total number of items that it can manufacture in a day is at the most 24 Item A takes on hour to make while item B takes only half an hour. The maximum time available per day is 16 hours. If the profit on one unit of item $A$ be 300 and that on one unit of item $B$ be 160 , how many of each type of item should be produced to maximize the profit? Solve the problem graphically
48. A small firm manufactures items $A$ and $B$.

The total number of items that it can manufacture in a day is at the most 24 Item A takes on hour to make while item B takes only half an hour. The maximum time available per day is 16 hours. If the profit on one unit of item A be 300 and that on one unit of item B be 160 , how many of each type of item should be produced to maximize the profit? Solve the problem graphically
49. A small firm manufactures gold rings and chains. The total number of rings and chains manufactured per day is atmost 24 . It takes 1 hour to make a ring and 30 minutes to make a chain. The maximum number of hours available per day is 16 . If the profit on a ring is Rs. 300 and that on a chain is Rs 190, find the number of rings and chains that should be manufactured per day, so as to earn the maximum profit. Make it as an L.P.P. and solve it graphically.
50. Objective function of a LLP is
(A) a constraint
(B) a function to be optimized
(C) a relation between the variables
(D) none of these
A. a constraint
B. a function to be optimized
C. a relation between the variables
D. none of these

## Answer: B

## - Watch Video Solution

51. The maximum value of $Z=4 x+2 y$
subjected $\quad$ to the constraints
$2 x+3 y \leq 18, x+y \geq 10 ; x, y \geq 0$ is 36 b.

40 c .20 d . none of these

## - Watch Video Solution

52. The optimal value of the objective function
is attained at the points A)Given by intersection of inequations with the axes only B)Given by intersection of inequations with the axes only C)Given by corner points of the feasible region D)None of these

## - Watch Video Solution

## Others

1. Two tailors A and B earn Rs. 150 and Rs. 200
per day respectively. A can stitch 6 shirts and 4
pants per day while B can stitch 10 shirts and
4 pants per day. Form a linear programming problem to minimize the labour cost to produce at least 60 shirts an 32 pants.

## D View Text Solution

2. Vitamins $A$ and $B$ are found in two different
foods $F_{1} a n d F_{2}$. One unit of food $F_{1}$ and 2
units of vitamin $A$ and 3 units $f$ vitamin $B$. One unit of food $F_{2}$ contains 4 units of vitamin A and 2 units of vitamin B. One unit of food $F_{1} a n d F_{2}$ cost Rs. 50 and 25 respectively. The minimum daily requirements for a person of vitamin $A$ and $B$ is 40 and 50 units respectively.

Assuming that anything in excess of daily minimum requirement of vitamin $A$ and $B$ not
harmful, find out the optimum mixture of food
$F_{1} a n d F_{2}$ at the minimum cost which meets
the daily minimum requirement of vitamin $A$ and B. Formulate this as a LPP.
3. A company is making two products $A$ and $B$.

The cost of producing one unit of products a and $B$ are Rs. 60 and 80 respectively. As per the agreement, the company has to supply at least

200 units of product $B$ to its regular customers. One unit f product $A$ requires one machine hour whereas product $B$ has machine hours available abundantly within the company. Total machine hours available for product AS are 400 hours. One unit of each product $A$ and $B$ requires one labour hour
each and total of 500 labour hours are available. The company wants to minimize the cost of production by satisfying the given requirements. Formulate t problem as a LPP.

## D View Text Solution

4. A firm manufactures two products, each of which must be processed through two departments, 1 and 2 . The hourly requirements per unit for each product in each department, the weekly capacities in each department,
selling price per unit, labour cost per unit, and
raw mater cost per unit are summarized as
follows: , Product A, Product B, Weekly capacity

Department 1 Department 2 Selling price per unit Labour cost per unit Raw material cost per unit, 34 Rs. 25 Rs. 16 Rs. 4, 26 Rs. 30 Rs. 20

Rs. 4, 130260 The problem is to determine the number of units to produce each product so
as to maximize total contribution to profit.

Formulate this as a LPP.
5. An airline agrees to charter planes for a group. The group needs at least 160 first class seats and at least 300 tourist class seats. The airline must use at least two of its model 314
planes which have 20 first class and 30 tourist
class seats. The airline will also use some of its model 535 planes which have 20 first class seats and 60 tourist class seats. Each flight of
a cost Rs. 150,000. How many of each type $f$ plane should be used to minimize the flight cost? Formulate this as a LPP.

## View Text Solution

6. Solve the following LPP by graphically method: Minimize $Z=20 x+10 y$ Subject to
$x+2 y \leq 403 x+y \geq 304 x+3 y \geq 60$ and,
$x, y \geq 0$

## D View Text Solution

7. Solve the following liner programming problems by graphical method: Maximize
$Z=5 x+3 y \quad$ Subject $\quad$ to $\quad 4 x+5 y \leq 15$
$5 x+2 y \leq 10 x, y \geq 0$

## - View Text Solution

8. A firm manufacturing two types of electric items, $A$ and $B$, can make a profit of Rs. 20 per unit of $A$ and Rs. 30 per unit of $B$. Each unit of

A requires 3 motors and 4 transformers and each unit of $B$ requires 2 motors and 4 transformers. The total supply of these per month is restricted to 210 mOtors and 300 transformers. Type B is an export model requiring a voltage stabilizer which has a supply restricted to 65 units per month.

Formulate the linear programming problem for maximum profit and solve it graphically.

## D View Text Solution

9. A furniture manufacturing company plans to
make two products: chairs and tables. From its
available resources which consists of 400 square feet of teak wood and 450 man hours.

It is known that to make a chair requires 5 square feet of wood and 10 man-hours and yields a profit of Rs. 45, while each table uses

20 square feet of wood and 25 man-hours and
yields a profit of Rs. 80. How many items of each product should be produced by the company so that the profit is maximum?

## D View Text Solution

10. A firm manufactures two products $A$ and $B$.

Each product is processed on two machines
$M_{1} a n d M_{2}$. Product A requires 4 minutes of processing time on $M_{1}$ and 8 min . on $M_{2}$; product B requires 4 minutes on $M_{1}$ and 4
min . on $M_{2}$. The machine $M_{1}$ is available for not more than 8 hrs 20 min . while machine $M_{2}$ is available for 10 hrs . during any working day. The products $A$ and $B$ are sold at a profit of Rs.

3 and Rs. 4 respectively. Formulate the problem as a linear programming problem and find how many products of each type should be produced by the firm each day in order to get maximum profit.
11. A manufacturer considers that men and women workers are equally efficient and so he pays them at the same rate. He has 30 and 17 units of workers (male and female) and capital respectively, which he uses to produce two
types of goods A and B. To produce one unit of

A, 2 workers and 3 units of capital are required while 3 workers and 1 unit of capital is required to produce one unit of $b$. If $A$ and $B$ are priced at Rs. 100 and Rs. 120 per unit respectively, how should he use his resources to maximize the total revenue? Form the
above as an LPP and solve graphically. Do you agree with this view of the manufacture that men and women workers are equally efficient and so should be paid at the same rate?

## D View Text Solution

12. A publisher sells a hard cover edition of a text book for Rs. 72.00 and a paperback edition of the same ext for Rs. 40.00 . Costs to
the publisher are Rs. 56.00 and Rs. 28.00 per book respectively in addition to weekly costs
of Rs. 9600.00. Both types require 5 minutes of
printing time, although hardcover requires 10 minutes binding time and the paperback requires only 2 minutes. Both the printing and binding operations have 4,800 minutes available each week. How many of each type o book should be produced in order to maximize profit?

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13. A house wife wishes to mix together two
kind of food, $X$ and $Y$, in such a way that the mixture contains at least 10 units of vitamin $A$,

12 units of vitamin $B$ and 8 units of vitamin $C$.

Vitamin A Vitamin B Vitamin C Food X: Food Y:

122231 One kg of food X cost Rs. 6 and one
kg of food Y costs Rs. 10. Find the least cost of the mixture which will produce the diet.

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14. A toy manufacturer produces two types of
dolls; a basic version dill A and a deluxe
version doll $B$. Each doll of type $B$ takes twice
as long to produce as one doll of type A. The
company have time to make a maximum of
2000 dolls of type A per day, the supply of
plastic is sufficient to produce 1500 dolls per day and each type requires equal amount of it.

The deluxe version i.e. type B requires a fancy dress of which there are only 600 per day available. If the company makes a profit of RLs.

3 and Rs. 5 per doll, respectively, on doll A and

B; how many of each should be produced per day in order to maximize profit? Solve it by graphical method.

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