# びdoubtnut 

## MATHS

## BOOKS - RD SHARMA MATHS (HINGLISH)

## RELATIONS

## Solved Examples And Exercises

1. An integer $m$ is said to be related to another integer $n$ if $m$ is a multiple of $n$. Check if the relation is symmetric, reflexive and transitive.

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2. If $R$ and $S$ are relations on a set $A$, then prove the following : $R$ and $S$ are symmetric $R \cap S$ and $R \cup S$ are symmetric $R$ is reflexive and $S$ is any relation $R \cup S$ is reflexive.
3. If $R$ and $S$ are transitive relations on a set $A$, then prove that $R \cup S$ may not be a transitive relation on $A$.

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4. Let $L$ be the set of all lines in $X Y=$ plane and $R$ be the relation in $L$ defined as $R=\left\{\left(L_{1}, L_{2}\right): L_{1}\right.$ is parallel to $\left.L_{2}\right\}$. Show that $R$ is an equivalence relation. Find the set of all lines related to the line $y=2 x+4$.

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5. Show that the relation $\geq$ on the set $R$ of all real numbers is reflexive and transitive but nut symmetric.
6. Let $S$ be a relation on the set $R$ of all real numbers defined by $S=\left\{(a, b) R x R: a^{2}+b^{2}=1\right\}$. Prove that $S$ is not an equivalence relation on $R$.

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7. Given to relation $R=\{(1,2),(2,3)\}$ on the set $A=\{1,2,3\}$, add a minimum number of ordered pairs so that the enlarged relation is symmetric, transitive and reflexive.

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8. Let $O$ be the origin. We define a relation between two points $P$ and $Q$ in a plane if $O P=O Q$. Show that the relation, so defined is an equivalence relation.

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9. The following relations are defined on the set of real number: $a R b$ if $a-b>0 a R b$ if $1+a b>0 a R b$ if $|a| \leq b$ Find whether these relations are reflexive, symmetric or transitive.

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Find whether or not each of the relations $R_{1}, R_{2}, R_{3}$ on $A$ is (i) reflexive
(ii) symmetric (iii) transitive.

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11. Let $R$ be a relation defined on the set of natural numbers $N$ as $R=\{(x, y): x, y \in N, 2 x+y=41\}$ Find the domain and range of $R$
. Also, verify whether $R$ is (i) reflexive, (ii) symmetric (iii) transitive.

## - Watch Video Solution

12. Is it true that every relation which is symmetric and transitive is also reflexive? Give reasons.

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13. Let $A=\{1,2,3\}$ and $R=\{(1,2),(1,1),(2,3)\}$ be a relation on $A$.

What minimum number of ordered pairs may be added to $R$ so that it may become a transitive relation on $A$.

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14. Show that the relation $R$ defined by $R=\{(a, b): a-b$ is divisible by $3 ; a, b Z\}$ is an equivalence relation.

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15. Test whether the following relations $R_{1}, R_{2}$ and $R_{3}$, are (i) reflexive (ii) symmetric and (iii) transitive: $R_{1}$ on $Q_{0}$ defined by $(a, b) R_{1} a=\frac{1}{b} R_{2}$ on $Z \quad$ defined $\quad$ by $\quad(a, b) R_{2}|a-b| \leq 5 \quad R_{3} \quad$ on $\quad R \quad$ defined $\quad$ by $(a, b) R_{3} a^{2}-4 a b+3 b^{2}=0$

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16. Three relations $R_{1}, R_{2} a n d R_{3}$ are defined on set $A=\{a, b, c\}$ as follow:

$$
R_{1}=\{(a, a),(a, b),(a, c),(b, b),(b, c),(c, a),(c, b),(c, c)\}
$$

$R_{2}=\{(a, b),(b, a),(a, c),(c, a)\} \quad R_{3}=\{(a, b),(b, c),(c, a)\} \quad$ Find whether each of $R_{1}, R_{2}, R_{3}$ is reflexive, symmetric and transitive.

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17. Show that the relation $R$ on the set $A\{x Z ; 0 \leq 12\}$, given by $R=\{(a, b): a=b\}$, is an equivalence relation. Find the set of all elements related to 1 .
18. Let $n$ be a fixed positive integer. Define a relation $R$ on Z as follows: $(a, b) R a-b$ is divisible by $n$. Show that $R$ is an equivalence relation on Z.

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19. Let $Z$ be the set of all integers and $Z_{0}$ be the set of all non=zero integers. Let a relation $R$ on $Z x Z_{0}$ be defined as follows: $(a, b) R(c, d) a d=b c$ for all $(a, b),(c, d) Z x Z_{0}$ Prove that $R$ is an equivalence relation on $Z x Z_{0}$.

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20. Prove that every identity relation on a set is reflexive, but the converse is not necessarily true.
21. Let $Z$ be the set of integers. Show that the relation $R=\{(a, b): a, b Z$ and $a+b$ is even $\}$ is an equivalence relation on $Z$.

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22. If R is an equivalence relation on a set A , then $R^{-1}$ is A . reflexive only B. symmetric but not transitive C. equivalence D. None of these

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23. On the set N of all natural numbers, a relation R is defined as follows:
$\forall n, m \in N, n R m$ Each of the natural numbers $n$ and $m$ leaves the remainder less than 5 .Show that $R$ is an equivalence relation. Also, obtain the pairwise disjoint subsets determined by R.

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24. If $R_{1}$ and $R_{2}$ are equivalence relations in a set A , show that $R_{1} \cap R_{2}$ is also an equivalence relation.

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25. Let $Z$ be the set of all integers and $Z_{0}$ be the set of all non=zero integers. Let a relation $R$ on $Z \times Z_{0}$ be defined as follows: $(a, b) R(c, d) a d=b c$ for all $(a, b),(c, d) Z \times Z_{0}$ Prove that $R$ is an equivalence relation on $Z \times Z_{0}$.

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26. Let $R$ be the equivalence relation in the set $A=\{0,1,2,3,4,5\}$ given by $R=\{(a, b)$ : divides $(a-b)\}$. Write the equivalence class [ 0 ].

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27. An integer $m$ is said to be related to another integer $n$ if $m$ is a multiple of $n$. Check if the relation is symmetric, reflexive and transitive.

## - Watch Video Solution

28. Show that the relation $\geq$ on the set $R$ of all real numbers is reflexive and transitive but nut symmetric.

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29. $m$ is said to be related to $n$ if $m$ and $n$ are integers and $m-n$ is divisible by 13. Does this define an equivalence relation?

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30. Let $O$ be the origin. We define a relation between two points $P$ and $Q$ in a plane if $O P=O Q$. Show that the relation, so defined is an

## equivalence relation.

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31. Show that the relation $R$ defined by $R=\{(a, b): a-b$ is divisible by $3 ; a, b Z\}$ is an equivalence relation.

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32. Prove that a relation R on a set A is symmetric iff $R=R^{-1}$

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33. Three relations $R_{1}, R_{2}$ and $R_{3}$ are defined on set $A=\{a, b, c\}$ as follow:
$R_{1}=\{(a, a),(a, b),(a, c),(b, b),(b, c),(c, a),(c, b),(c, c)\}$
$R_{2}=\{(a, b),(b, a),(a, c),(c, a)\}$
$R_{3}=\{(a, b),(b, c),(c, a)\}$
Find whether each of $R_{1}, R_{2}, R_{3}$ is reflexive, symmetric and transitive.

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34. Let a relation $R_{1}$ on the set R of real numbers be defined as $(a, b) \in R \Leftrightarrow 1+a b>0$ for all $a, b \in R$. Show that $R_{1}$ is reflexive and symmetric but not transitive.

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35. Let S be the set of all points in a plane and R be a relation on S defines as $R=\{(P, Q)$ : distance between $P$ and $Q$ is less than 2 units $\}$ Show that $R$ is reflexive and symmetric but not transitive.

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36. The following relations are defined on the set of real number: $a R b$ if $1+a b>0$ Find whether these relations are reflexive, symmetric or transitive.

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37. Prove that every identity relation on a set is reflexive, but the converse is not necessarily true.

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38. Let $R$ be a relation defined on the set of natural numbers N as $R=\{(x, y): x, y \in N, 2 x+y=41\}$ Find the domain and range of R. Also, verify whether R is (i) reflexive, (ii) symmetric (iii) transitive.

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39. Let $N$ denote the set of all natural numbers and $R$ be the relation on $N \times N$ defined by $(a, b) R(c, d) \Leftrightarrow a d(b+c)=b c(a+d)$. Check whether $R$ is an equivalence relation on $N \times N$

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40. Let N be the set of all natural numbers and let R be a relation on $N \times N \quad, \quad$ defined $\quad$ by $\quad(a, b) R(c, d) \Leftrightarrow a d=b c \quad$ for $\quad$ all $(a, b),(c, d) \in N \times N$. Show that $R$ is an equivalence relation on $N \times N$.

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41. Let $R$ be a relation on the set of all line in a plane defined by
$\left(l_{1}, l_{2}\right) \in R i$ is parallel to line $l_{2}$. Show that R is an equivalence relation.

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42. Each of the following defines a relation on N : $x \rightarrow y,(i) x, y \in N x+y=10 x, \int e \geq r,(i i i) \mathrm{x}, \mathrm{y}$ in $\mathrm{N} \mathrm{x}+4 \mathrm{y}=10, \mathrm{x}, \mathrm{y}$ in $\mathrm{N}^{\prime}$

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43. Let $A=\{a, b, c)$ and the relation R be defined on A as follows: $R=\{(a, a),(b, c),(a, b)\}$. Then, write minimum number of ordered pairs to be added in R to make it reflexive and transitive.

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44. Given the relation $R=\{(1,2),(2,3)$ on the set $A=\{1,2,3\}$, add a minimum number of ordered pairs so that the enlarged relation is symmetric, transitive and reflexive.

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45. Let $A=\{1,2,3, \ldots ., 9\}$ and $R$ be the relation in $A \times A$ defined by $(a, b) R(c, d)$ if $a+d=b+c$ for $(a, b),(c, d)$ in $A \times A$. Prove that $R$ is an equivalence relation. Also obtain the equivalence class [(2,5)].

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46. Prove that the relation $R$ on the set $N \times N$ defined by $(a, b) R(c, d) a+d=b+c$ for all $(a, b),(c, d) \in N \times N$ is an equivalence relation. Also, find the equivalence classes $[(2,3)]$ and $[(1,3)]$.

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47. Let $n$ be a positive integer. Prove that the relation R on the set Z of all integers numbers defined by $(x, y) \in R \Leftrightarrow x-y$ is divisible by $n$, is an equivalence relation on Z .

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48. Let T be the set of all triangles in a plane with R as relation in T given by $R=\left\{\left(T_{1}, T_{2}\right):(T)_{1} \cong T_{2}\right\}$. Show that R is an equivalence relation.

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49. If $R$ and $S$ are relations on a set $A$, then prove the following : $R$ and $S$ are symmetric $R \cap S$ and $R \cup S$ are symmetric $R$ is reflexive and $S$ is any relation $R \cup S$ is reflexive.

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50. Let $S$ be a relation on the set $R$ of all real numbers defined by $S=\left\{(a, b) R \times R: a^{2}+b^{2}=1\right\}$. Prove that $S$ is not an equivalence relation on $R$.

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51. Write the domain of the relation $R$ defined on the set $Z$ of integers as follows $(a, b) \in R \Leftrightarrow a^{2}+b^{2}=25$

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52. If $R$ and $S$ are transitive relations on a set $A$, then prove that $R \cup S$ may not be a transitive relation on $A$.

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53. Let $R$ be the equivalence relation in the set $A=\{0,1,2,3,4,5\}$ given by $R=\{(a, b)$ : divides $(a-b)\}$. Write the equivalence class [ 0 ].

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54. If $R=\{(x, y): x+2 y=8\}$ is a relation on N , write the range of R .
55. Let $Z$ be the set of all integers and $R$ be the relation on $Z$ defined as $R=\{(a, b) ; a, b \in Z$, and $(a-b)$ is divisible by 5.$\}$. Prove that $R$ is an equivalence relation.

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56. The union of two equivalence relations on a set is not necessarily an equivalence relation on the set.

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57. Let $A$ be the set of all students of a boys school. Show that the relation $R$ on $A$ given by $R=\{(a, b): a$ is sister of $b\}$ is empty relation and $R^{\prime}=\{(a, b)$ : the difference between the heights of $a$ and $b$ is less than 5 meters\} is the universal relation.
58. Prove that a relation $R$ on a set $A$ is symmetric iff $R=R^{-1}$.

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59. The relation $R$ on the set $N$ of all natural numbers defined by $(x, y) \in R \Leftrightarrow x$ divides $y$, for all $x, y \in N$ is transitive.

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60. Three relations $R_{1}, R_{2} a n d R_{3}$ are defined on set $A=\{a, b, c\}$ as follow:

$$
R_{1}=\{(a, a),(a, b),(a, c),(b, b),(b, c),(c, a),(c, b),(c, c)\}
$$

$R_{2}=\{(a, b),(b, a),(a, c),(c, a)\} \quad R_{3}=\{(a, b),(b, c),(c, a)\} \quad$ Find whether each of $R_{1}, R_{2}, R_{3}$ is reflexive, symmetric and transitive.

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61. Show that the relation $R$ on the set $A=\{1,2,3\}$ given by $R=\{(1,1),(2,2),(3,3),(1,2),(2,3)\}$ is reflexive but neither symmetric nor transitive.

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62. Show that the relation $R$ on the set $A=\{1,2,3\}$ given by $R=\{(1,2),(2,1)\}$ is symmetric but neither reflexive nor transitive.

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63. Check the following relations $R$ and $S$ for reflexivity, symmetry and transitivity: (i) $a R b$ iff $b$ is divisible by $a, a, b \in N$ (ii) $l_{1} S l_{2}$ iff $l_{1} \perp l_{2}$, where $l_{1}$ and $l_{2}$ are straight lines in a plane.

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64. Let a relation $R_{1}$ on the set $R$ of real numbers be defined as $(a, b) \in R_{1} \Leftrightarrow 1+a b>0$ for all $a, b \in R$. Show that $R_{1}$ is reflexive and symmetric but not transitive.

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65. Determine whether Relation $R$ on the set $A=\{1,2,3,, 13,14\}$ defined as $R=\{(x, y): 3 x-y=0\}$ is reflexive, symmetric or transitive.

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66. Determine whether Relation $R$ on the set $N$ of all natural numbers defined as $R=\{(x, y): y=x+5$ and $x<4\}$ is reflexive, symmetric or transitive.

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67. Determine whether Relation $R$ on the set $A=\{1,2,3,4,5,6\}$ defined as $R=\{(x, y): y$ is divisible by $x\}$ is reflexive, symmetric or transitive.

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68. Determine whether Relation $R$ on the set $Z$ of all integer defined as $R=\{(x, y):(x-y)=$ integer $\}$ is reflexive, symmetric or transitive.

## - Watch Video Solution

69. Show that the relation $R$ on $R$ defined as $R=\{(a, b): a \leq b\}$, is reflexive and transitive but not symmetric.

## - Watch Video Solution

70. Let S be the set of all points in a plane and R be a relation on S defines as $R=\{(P, Q)$ : distance between $P$ and $Q$ is less than 2 units $\}$ Show that $R$ is reflexive and symmetric but not transitive.

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71. Let $X=\{1,2,3,4,5,6,7,8,9\}$, Let $R_{1}$ be a relation on $X$ given by $R_{1}=\{(x, y): x-y$ is divisible by 3$\}$ and $R_{2}$ be another relation on $X$ given by $R_{2}=\{(x, y):\{x, y\} \subset\{1,4,7\}$ or $\{x, y\} \subset\{2,5,8\}$ or $\{x, y\} \subset\{3,6,9\}\}$. Show that $R_{1}=R_{2}$.

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72. Show that the relations $R$ on the set $R$ of all real numbers, defined as
$R=\left\{(a, b): a \leq b^{2}\right\}$ is neither reflexive nor symmetric nor transitive.

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73. Let $A=\{1,2,3\}$. Then, show that the number of relations containing ( 1,2 ) and $(2,3)$ which are reflexive and transitive but not symmetric is three.

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74. Let $A$ be the set of all human beings in a town at a particular time. Determine whether Relation $R=\{(x, y): x$ and $y$ work at the same place is reflexive, symmetric and transitive:

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75. Let $A$ be the set of all human beings in a town at a particular time. Determine whether Relation $R=\{(x, y): x$ and $y$ live in the same locality\} is reflexive, symmetric and transitive:

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76. Let $A$ be the set of all human beings in a town at a particular time. Determine whether Relation $R=\{(x, y): x$ is wife of $y\}$ is reflexive, symmetric and transitive:

## - Watch Video Solution

77. Let $A$ be the set of all human beings in a town at a particular time. Determine whether Relation $R=\{(x, y): x$ is father of $y\}$ is reflexive, symmetric and transitive:

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78. $R_{1}=\{(a, a),(a, b),(a, c),(b, b),(b, c),(c, a),(c, b),(c, c)\}$ is defined on set $A=\{a, b, c\}$. Find whether or not it is (i) reflexive (ii) symmetric (iii) transitive.

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79. $R_{2}=\{(a, a)\}$ is defined on set $A=\{a, b, c\}$. Find whether or not it is (i) reflexive (ii) symmetric (iii) transitive.

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80. $R_{3}=\{(b, c)\}$ is defined on set $A=\{a, b, c\}$. Find whether or not it is (i) reflexive (ii) symmetric (iii) transitive.

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81. Test whether, $R_{1}$ on $Q_{0}$ defined by $(a, b) \in R_{1} \Leftrightarrow a=1 / b$ is (i) reflexive (ii) symmetric and (iii) transitive:

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82. Test whether, $R_{2}$ on $Z$ defined by $(a, b) \in R_{2} \Leftrightarrow|a-b| \leq 5$ is (i) reflexive (ii) symmetric and (iii) transitive.
83. Test whether, $R_{3}$ on $R$ defined by
$(a, b) \in R_{3} \Leftrightarrow a^{2}-4 a b+3 b^{2}=0$.

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84. Find whether or not $R_{1}=\{(1,1),(1,3),(3,1),(2,2),(2,1)$,
$(3,3)\}$, on $A=\{1,2,3\}$ is (i) reflexive (ii) symmetric (iii) transitive.

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85. Find whether or not $R_{2}=\{(2,2),(3,1),(1,3)\}$, on $A=\{1,2,3\}$ is (i) reflexive (ii) symmetric (iii) transitive.

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86. Find whether or not $R_{3}=\{(1,3),(3,3)\}$, on $A=\{1,2,3\}$ is (i) reflexive (ii) symmetric (iii) transitive.

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87. $a R b$ if $a-b>0$ is defined on the set of real numbers, find whether it is reflexive, symmetric or transitive.

## - Watch Video Solution

88. $a R b$ iff $1+a b>0$ is defined on the set of real numbers, find whether it is reflexive, symmetric or transitive.

## - Watch Video Solution

89. $a R b$ if $|a| \leq b$ is defined on the set of real numbers, find whether it is reflexive, symmetric or transitive.
90. Check whether the relation $R$ defined on the set $A=\{1,2,3,4,5,6\} \quad$ as $\quad R=\{(a, b): b=a+1\} \quad$ is reflexive, symmetric or transitive.

## - Watch Video Solution

91. Check whether the relation $R$ on $R$ defined by $R=\left\{(a, b): a \leq b^{3}\right\}$ is reflexive, symmetric or transitive.

## - Watch Video Solution

92. Prove that every identity relation on a set is reflexive, but the converse is not necessarily true.

## - Watch Video Solution

93. If $A=\{1,2,3,4\}$ define relations on $A$ which have properties of being reflexive, transitive but not symmetric.

## - Watch Video Solution

94. If $A=\{1,2,3,4\}$ define relations on $A$ which have properties of being symmetric but neither reflexive nor transitive.

## - Watch Video Solution

95. If $A=\{1,2,3,4\}$ define relations on $A$ which have properties of being reflexive, symmetric and transitive.

## - Watch Video Solution

96. Let $R$ be a relation defined on the set of natural numbers $N$ as
$R=\{(x, y): x, y \in N, 2 x+y=41\}$ Find the domain and range of $R$
. Also, verify whether $R$ is (i) reflexive, (ii) symmetric (iii) transitive.
97. Is it true that every relation which is symmetric and transitive is also reflexive? Give reasons.

## - Watch Video Solution

98. An integer $m$ is said to be related to another integer $n$ if $m$ is a multiple of $n$. Check if the relation is symmetric, reflexive and transitive.

## - Watch Video Solution

99. Show that the relation " $\geq$ " on the set $R$ of all real numbers is reflexive and transitive but not symmetric.

## - Watch Video Solution

100. Give an example of a relation which is reflexive and symmetric but not transitive.

## - Watch Video Solution

101. Give an example of a relation which is reflexive and transitive but not symmetric.

## - Watch Video Solution

102. Give an example of a relation which is symmetric and transitive but not reflexive.

## - Watch Video Solution

103. Give an example of a relation which is symmetric but neither reflexive nor transitive.
104. Give an example of a relation which is transitive but neither reflexive nor symmetric.

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105. Given the relation $R=\{(1,2),(2,3)\}$ on the set $A=\{1,2,3\}$, add a minimum number of ordered pairs so that the enlarged relation is symmetric, transitive and reflexive.

## - Watch Video Solution

106. Let $A=\{1,2,3\}$ and $R=\{(1,2),(1,1),(2,3)\}$ be a relation on $A$. What minimum number of ordered pairs may be added to $R$ so that it may become a transitive relation on $A$.
107. Let $A=\{a, b, c)$ and the relation R be defined on A as follows: $R=\{(a, a),(b, c),(a, b)\}$. Then, write minimum number of ordered pairs to be added in R to make it reflexive and transitive.

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108. Each of the following defines a relation on $N$ : (i) $x>y, x, y \in N$
(ii) $x+y=10, x, y \in N$
(iii) $x y$ is square of an integer, $x, y \in N$
(iv) $x+4 y=10, x, y \in N$

Determine which of the above relations are reflexive, symmetric and transitive.

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109. Let $R$ be a relation on the set of all lines in a plane defined by $\left(l_{1}, l_{2}\right) \in R \ll>$ line $l_{1}$ is parallel to line $l_{2}$. Show that $R$ is an equivalence relation.

## (D) Watch Video Solution

110. Show that the relation 'is congruent to' on the set of all triangles in a plane is an equivalence relation

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111. Show that the relation $R$ defined on the set $A$ of all triangles in a plane as $R=\left\{\left(T_{1}, T_{2}\right): T_{1}\right.$ is similar to $\left.T_{2}\right)$ is an equivalence relation. Consider three right angle triangle $T_{1}$ with sides $3,4,5 ; T_{2}$ with sides $5,12,13$ and $T_{3}$ with sides $6,8,10$. Which triangles among $T_{1}, T_{2}$ and $T_{3}$ are related?

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112. Let $n$ be a positive integer. Prove that the relation $R$ on the set $Z$ of all integers numbers defined by $(x, y) \in R \Leftrightarrow x-y$ is divisible by $n$, is an equivalence relation on Z .

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113. Show that the relation $R$ on the set $A$ of all the books in a library of a college given by $R=\{(x, y): x$ and $y$ have the same number of pages $\}$, is an equivalence relation.

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114. Show that the relation $R$ on the set $A=\{1,2,3,4,5\}$, given by $R=\{(a, b):|a-b|$ is even $\}$, is an equivalence relation. Show that all the elements of $\{1,3,5\}$ are related to each other and all the elements of $\{2,4\}$ are related to each other. But, no element of $\{1,3,5\}$ is related to any element of $\{2,4\}$.

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115. Show that the relation $R$ on the set $A=\{x \in Z: 0 \leq x \leq 12\}$, given by $R=\{(a, b):|a-b|$ is a multiple of 4$\}$ is an equivalence
relation. Find the set of all elements related to 1 i.e. equivalence class [1].

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116. Show that the relation $R$ on the set $A$ of points in a plane, given by $R=\{(P, Q):$ Distance of the point $P$ from the origin is same as the distance of the point $Q$ from the origin\}, is an equivalence relation. Further show that the set of all points related to a point $P \neq(0,0)$ is the circle passing through $P$ with origin as centre.

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117. Prove that the relation $R$ on the set $N \times N$ defined by $(a, b) R \Leftrightarrow(c, d) a+d=b+c$ for all $(a, b),(c, d) \in N \times N$ is an equivalence relation. Also, find the equivalence classes $[(2,3)]$ and $[(1,3)]$.

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118. Let $A=\{1,2,3,, 9\}$ and $R$ be the relation on $A \times A$ defined by $(a, b) R(c, d)$ if $a+d=b+c$ for all $(a, b),(c, d) \in A \times A$. Prove that $R$ is an equivalence relation and also obtain the equivalence class $[(2,5)]$.

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119. Let $N$ be the set of all natural numbers and let $R$ be a relation on
$N \times N \quad, \quad$ defined $\quad$ by $\quad(a, b) R(c, d) \Leftrightarrow a d=b c \quad$ for $\quad$ all
$(a, b),(c, d) \in N \times N$. Show that $R$ is an equivalence relation on
$N \times N$. Also, find the equivalence class [(2,6)].

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120. Let $N$ denote the set of all natural numbers and R be the relation on
$N x N$ defined by $(a, b) R(c, d) \Leftrightarrow a d(b+c)=b c(a+d)$. Check whether R is an equivalence relation on $N x N$.
121. Prove that the relation congruence modulo m on the set $Z$ of all integers is an equivalence relation.

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122. Show that the number of equivalence relations on the set $\{1,2,3\}$ containing $(1,2)$ and $(2,1)$ is two.

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123. Given a non-empty set $X$, consider $P(X)$ which is the set of all subsets of $X$. Define a relation in $P(X)$ as follows: For subsets $A, B$ in $P(X), \quad A R B$ if $A \subset B$. Is $R$ an equivalence relation on $P(X)$ ? Justify your answer.
124. Let $R$ be the equivalence relation in the set $A=\{0,1,2,3,4,5\}$ given by $R=\{(a, b): 2$ divides $(a-b)\}$. Write the equivalence class [0].

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125. On the set $N$ of all natural numbers, a relation $R$ is defined as follows: $n R m$ <=> Each of the natural numbers $n$ and $m$ leaves the same remainder less than 5 when divided by 5 . Show that $R$ is an equivalence relation. Also, obtain the pairwise disjoint subsets determined by $R$.

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126. Show that the relation $R$ defined by $R=\{(a, b): a-b$ is divisible by $3 ; a, b Z\}$ is an equivalence relation.

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127. Show that the relation $R$ on the set $Z$ of integers, given by $R=\{(a, b): 2$ divides $a-b\}$, is an equivalence relation.

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128. Prove that the relation $R$ on $Z$ defined by $(a, b) \in R \Leftrightarrow a-b$ is divisible by 5 is an equivalence relation on $Z$.

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129. Let $n$ be a fixed positive integer. Define a relation $R$ on $Z$ as follows:
$(a, b) \in R \Leftrightarrow a-b$ is divisible by $n$. Show that $R$ is an equivalence relation on $Z$.

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130. Let $Z$ be the set of integers. Show that the relation $R=\{(a, b): a, b \in Z$ and $a+b$ is even $\}$ is an equivalence relation on $Z$.

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131. $m$ is said to be related to $n$ if $m$ and $n$ are integers and $m-n$ is divisible by 13 . Does this define an equivalence relation?

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132. Let $R$ be a relation on the set $A$ of ordered pairs of integers defined by $(x, y) R(u, v)$ iff $x v=y u$. Show that $R$ is an equivalence relation.

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133. Show that the relation $R$ on the set $A=\{x \in Z ; 0 \leq x \leq 12\}$, given by $R=\{(a, b): a=b\}$, is an equivalence relation. Find the set of
all elements related to 1 .

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134. Let $L$ be the set of all lines in $X Y$-plane and $R$ be the relation in $L$ defined as $R=\left\{\left(L_{1}, L_{2}\right): L_{1}\right.$ is parallel to $\left.L_{2}\right\}$. Show that $R$ is an equivalence relation. Find the set of all lines related to the line $y=2 x+4$.

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135. Show that the relation $R$, defined on the set $A$ of all polygons as $R=\left\{\left(P_{1}, P_{2}\right): P_{1}\right.$ and $P_{2}$ have same number of sides $\}$, is an equivalence relation. What is the set of all elements in $A$ related to the right angle triangle $T$ with sides 3,4 and 5 ?

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136. Let $O$ be the origin. We define a relation between two points $P$ and $Q$ in a plane if $O P=O Q$. Show that the relation, so defined is an equivalence relation.

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137. Let $R$ be the relation defined on the set $A=\{1,2,3,4,5,6,7\}$ by $R=\{(a, b)$ : both $a$ and $b$ are either odd or even $\}$. Show that $R$ is an equivalence relation. Further, show that all the elements of the subset $\{1$, $3,5,7\}$ are related to each other and all the elements of the subset $\{2,4$, $6\}$ are related to each other, but no element of the subset $\{1,3,5,7\}$ is related to any element of the subset $\{2,4,6\}$.

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138. Let $S$ be a relation on the set $R$ of all real numbers defined by $S=\left\{(a, b) \in R \times R: a^{2}+b^{2}=1\right\}$. Prove that $S$ is not an equivalence relation on $R$.

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139. Let $Z$ be the set of all integers and $Z_{0}$ be the set of all non-zero integers. Let a relation $R$ on $Z \times Z_{0}$ be defined as follows: $(a, b) R(c, d) \Leftrightarrow a d=b c$ for all $(a, b),(c, d) \in Z \times Z_{0}$ Prove that $R$ is an equivalence relation on $Z \times Z_{0}$

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140. If $R$ and $S$ are relations on a set $A$, then prove the following: $R$ and $S$ are symmetric $\Rightarrow R \cap S$ and $R \cup S$ are symmetric (ii) $R$ is reflexive and $S$ is any relation $\Rightarrow R \cup S$ is reflexive.

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141. If $R$ and $S$ are transitive relations on a set $A$, then prove that $R \cup S$ may not be a transitive relation on $A$.
142. Write the domain of the relation $R$ defined on the set $Z$ of integers as follows: $(a, b) \in R \Leftrightarrow a^{2}+b^{2}=25$

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143. If $R=\left\{(x, y): x^{2}+y^{2} \leq 4 ; x, y \in Z\right\}$ is a relation on $Z$, write the domain of $R$.

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144. Write the identity relation on set $A=\{a, b, c\}$.

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145. Write the smallest reflexive relation on set $A=\{1,2,3,4\}$.
146. If $R=\{(x, y): x+2 y=8\}$ is a relation on $N$, then write the range of $R$.

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147. If $R$ is a symmetric relation on a set $A$, then write a relation between $R$ and $R^{-1}$.

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148. Let $R=\left\{(x, y):\left|x^{2}-y^{2}\right|<1\right\}$ be a relation on set $A=\{1,2,3,4,5\}$. Write $R$ as a set of ordered pairs.

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149. If $A=\{2,3,4\}, B=\{1,3,7\}$ and $\mathrm{R}=\{(\mathrm{x}, \mathrm{y}): \mathrm{x}$ in $\mathrm{A}, \backslash \mathrm{y}$ in $\mathrm{B} \backslash \mathrm{an} \mathrm{d} \backslash$ X

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150. Let $A=\{3,5,7\}, B=\{2,6,10\}$ and $R$ be a relation from $A$ to $B$ defined by $R=\{(x, y): x$ and $y$ are relatively prime. $\}$ Then, write $R$ and $R^{-1}$.

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151. Define a reflexive relation.

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152. Define a symmetric relation.
153. Define a transitive relation.

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154. Define an equivalence relation.

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155. If $A=\{3,5,7\}$ and $B=\{2,4,9\}$ and $R$ is a relation given by is less than, write $R$ as a set ordered pairs.

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156. $A=\{1,2,3,4,5,6,7\}$ and if $R=\{(x, y): y$ is one half of $x ; x, y \in A\}$ is a relation on $A$, then write $R$ as a set of ordered pairs.
157. Let $A=\{2,3,4,5\}$ and $B=\{1,3,4\}$. If $R$ is the relation from $A$ to $B$ given by $a R b$ iff $a$ is a divisor of $b$. Write $R$ as a set of ordered pairs.

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158. State the reason for the relation $R$ on the set $\{1,2,3\}$ given by $R=\{(1,2),(2,1)\}$ not to be transitive.

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159. Let $R=\left\{\left(a, a^{3}\right): a\right.$ is a prime number less than 5$\}$ be a relation. Find the range of $R$.

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160. Let $R$ be the relation in the set $Z$ of integers given by $R=\{(a, b): 2$ divides $a-b\}$. Show that the relation $R$ transitive ? Write the equivalence class [0].

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161. For the set $A=\{1,2,3\}$, define a relation $R$ on the set $A$ as follows: $R=\{(1,1),(2,2),(3,3),(1,3)\}$ Write the ordered pairs to be added to $R$ to make the smallest equivalence relation.

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162. Let $A=\{0,1,2,3\}$ and $R$ be a relation on $A$ defined as $R=\{(0,0),(0,1),(0,3),(1,0),(1,1),(2,2),(3,0),(3,3)\}$, is $R$ reflexive? symmetric transitive?

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163. If the relation R be defined on the set $A=\{1,2,3,4,5\}$ by $R=\left\{(a, b):\left|a^{2}-b^{2}\right|<8\right\}$. Then, R is given by ........

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164. Let the relation $R$ be defined in $N$ by aRb, if $2 a+3 b=30$. Then $R=$ ...... .

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165. Write the smallest equivalence relation on the set $A=\{1,2,3\}$.

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166. Let $R$ be a relation on the set $N$ given by $R=\{(a, b): a=b-2, b>6\}$. Then, $(2,4) \in R$ (b) $(3,8) \in R$ (c) $(6,8) \in R(\mathrm{~d})(8,7) \in R$

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167. Which of the following is not an equivalence relation on $Z$ ? $a R b \Leftrightarrow a+b$ is an even integer (b) $a R b \Leftrightarrow a-b$ is an even integer (c) $a R b \Leftrightarrow a=b$

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168. $R$ is a relation on the set $Z$ of integers and it is given by $(x, y) \in R \Leftrightarrow|x-y| \leq 1$. Then, $R$ is (a) reflexive and transitive (b) reflexive and symmetric (c) symmetric and transitive (d) an equivalence relation

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169. Let $R=\{(1,3),(4,2),(2,4),(2,3),(3,1)\}$ be a relation on the set $A=\{1,2$, $3,4\}$. The relation $R$ is

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170. Let $R$ be the relation over the set of all straight lines in a plane such that $l_{1} R l_{2} \Leftrightarrow l_{1} \perp l_{2}$. Then, $R$ is (a) symmetric (b) reflexive (c) transitive (d) an equivalence relation

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171. Let $A=\{1,2,3\}$ Then number of relations containing $(1,2) \operatorname{and}(1,3)$ which are reflexive and symmetric but not transitive is (A) 1 (B) 2 (C) 3 (D) 4

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172. The relation ' $R$ ' in $N \times N$ such that
$(a, b) R(c, d) \Leftrightarrow a+d=b+c$ is reflexive but not symmetric reflexive and transitive but not symmetric an equivalence relation (d) none of these
173. If $A=\{1,2,3\}, B=\{1,4,6,9\}$ and $R$ is a relation from $A$ to $B$ defined by ' $x$ is greater than $y$ '. The range of $R$ is (a) $\{1,4,6,9\}$ (b) $\{4,6,9\}$ (c) $\{1\}$ (d) none of these

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174. A relation $R$ is defined from $\{2,3,4,5\}$ to $\{3,6,7,10\}$ by : $x R y \Leftrightarrow x$ is relatively prime to $y$. Then, domain of $R$ is (a) $\{2,3,5\}$ (b) $\{3,5\}$ (c) $\{2,3,4\}$ (d) $\{2,3,4,5\}$

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175. A relation $\varphi$ from $C$ to $R$ is defined by $x \varphi y \Leftrightarrow|x|=y$. Which one is correct?
(a) $(2+3 i) \varphi 13$
(b) $3 \varphi(-3)$
(c) $(1+i) \varphi 2$
(d) $i \varphi 1$

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176. Let $R$ be a relation on $N$ defined by $x+2 y=8$. The domain of $R$ is
A. $\{2,4,8\}$
B. $\{2,4,6,8\}$
C. $\{2,4,6\}$
D. $\{1,2,3,4\}$

Answer: C) $\{2,4,6\}$

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177. $R$ is a relation from $\{11,12,13\}$ to $\{8,10,12\}$ defined by $y=x-3$. Then, $R^{-1}$ is (a) $\{(8,11),(10,13)\}(\mathrm{b})\{(11,8),(13,10)\}(\mathrm{c})\{(10,13),(8,11),(8$, $10)\}$ (d) none of these
178. Let $R=\{(a, a),(b, b),(c, c),(a, b)\}$ be a relation on set $A=\{a, b, c\}$. Then, $R$ is (a) identity relation (b) reflexive (c) symmetric (d) equivalence

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179. Let $A=\{1,2,3\}$ and $R=\{(1,2),(2,3),(1,3)\}$ be a relation on $A$. Then, $R$ is (a)neither reflexive nor transitive (b)neither symmetric nor transitive (c) transitive (d) none of these

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180. If $R$ is the largest equivalence relation on a set $A$ and $S$ is any relation on $A$, then $R \subset S$ (b) $S \subset R$ (c) $R=S$ (d) none of these

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181. If $R$ is a relation on the set $A=\{1,2,3,4,5,6,7,8,9\}$ given by $x R y \Leftrightarrow y=3 x$, then $R=$ (a) $\{(3,1),(6,2),(8,2),(9,3)\}$ (b) $\{(3,1),(6,2)$, $(9,3)\}(b)\{(3,1),(2,6),(3,9)$ (d) none of these

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182. If $R$ is a relation on the set $A=\{1,2,3\}$ given by $R=(1,1),(2,2),(3,3)$, then $R$ is (a) reflexive (b) symmetric (c) transitive (d) all the three options

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183. If $A=\{a, b, c, d\}$, then a relation $R=\{(a, b),(b, a),(a, a)\}$ on $A$ is (a)symmetric and transitive only (b)reflexive and transitive only (c) symmetric only (d) transitive only

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184. If $A=\{1,2,3\}$, then a relation $R=\{(2,3)\}$ on $A$ is (a) symmetric and transitive only (b) symmetric only (c) transitive only (d) none of these

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185. Let $R$ be the relation on the set $A=\{1,2,3,4\}$ given by $R=\{(1,2),(2,2),(1,1),(4,4),(1,3),(3,3),(3,2)\}$. Then, $R$ is reflexive and symmetric but not transitive (b) $R$ is reflexive and transitive but not symmetric (c) $R$ is symmetric and transitive but not reflexive (d) $R$ is an equivalence relation

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186. Let $A=\{1,2,3\}$. Then number of equivalence relations containing $(1,2)$ is (A) 1 (B) 2 (C) 3 (D) 4

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187. The relation $R=\{(1,1),(2,2),(3,3)\}$ on the set $\{1,2,3\}$ is (a) symmetric only (b) reflexive only (c) an equivalence relation (d) transitive only

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188. $S$ is a relation over the set $R$ of all real numbers and it is given by $(a, b) \in S \Leftrightarrow a b \geq 0$. Then, $S$ is symmetric and transitive only reflexive and symmetric only (c) antisymmetric relation (d) an equivalence relation

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189. In the set $Z$ of all integers, which of the following relation $R$ is not an equivalence relation? $x R y$ : if $x \leq y$ (b) $x R y$ : if $x=y$ (c) $x R y$ : if $x-y$ is an even integer (d) $x R y$ : if $x=y(\bmod 3)$

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190. Let $A=\{1,2,3\}$ and consider the relation $R=\{(1,1),(2,2),(3,3),(1,2),(2,3),(1,3)\}$. Then, $R$ is (a) reflexive but not symmetric (b) reflexive but not transitive (c) symmetric and transitive (d) neither symmetric nor transitive

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191. The relation $S$ defined on the set $R$ of all real number by the rule $a S b$ iff $a \geq b$ is (a) equivalence relation (b)reflexive, transitive but not symmetric (c)symmetric, transitive but not reflexive (d) neither transitive nor reflexive but symmetric

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192. The maximum number of equivalence relations on the set $A=\{1,2,3\}$ are
193. Let $R$ be a relation on the set $N$ of natural numbers defined by $n R m$ if $n$ divides $m$. Then, $R$ is
A. Reflexive and Symmetric
B. Symmetric and Transitive
C. Equivalence
D. Reflexive and Transitive but not Symmetric

## Answer: D

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194. Let $L$ denote the set of all straight lines in a plane. Let a relation $R$ be defined by $l R m$ if and only if $l$ is perpendicular to $m f$ or all, $l, m \in L$. Then, $R$ is (a) reflexive (b) symmetric (c) transitive (d) none of these
195. Let $T$ be the set of all triangles in the Euclidean plane, and let a relation $R$ on $T$ be defined as $a R b$ if $a$ is congruent to $b$ for all $a, b \in T$
. Then, $R$ is (a) reflexive but not symmetric (b) transitive but not symmetric (c) equivalence (d) none of these

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196. Let $R$ be a relation defined by $R=\{(a, b): a \geq b, a, b \in R\}$. The relation $R$ is (a) reflexive, symmetric and transitive (b) reflexive, transitive but not symmetric (c) symmetric, transitive but not reflexive (d) neither transitive nor reflexive but symmetric

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197. For real numbers x and y , we write $x \cdot y$, if $x-y+\sqrt{2}$ is an irrational number. Then, the relation • is an equivalence relation.
198. If $A=\{a, b, c\}$, then the relation $R=\{(b, c)\}$ on $A$ is (a) reflexive only (b) symmetric only (c) transitive only (d) reflexive and transitive only

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2. Let $A=\{2,3,4,5,, 17,18\}$. Let ' ' be the equivalence relation on $A \times A$, cartesian product of $A$ with itself, defined by $(a, b)(c, d)$ iff $a d=b c$. Then, the number of ordered pairs of the equivalence class of $(3,2)$ is (a) 4 (b) 5 (c) 6 (d) 7

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