

# MATHS

## BOOKS - RD SHARMA MATHS (HINGLISH)

### TANGENTS AND NORMALS

#### Solved Examples And Exercises

1. Show that the curves

$$\frac{x^2}{a^2 + \lambda_1} + \frac{y^2}{b^2 + \lambda_1} = 1 \quad \text{and}$$

$\frac{x^2}{a^2 + \lambda_2} + \frac{y^2}{b^2 + \lambda_2} = 1$  intersect at right angles.



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2. Find the condition for the following set of curves to intersect orthogonally:

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad \text{and} \quad xy = c^2 \quad \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

and  $\frac{x^2}{A^2} - \frac{y^2}{B^2} = 1.$



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3. Show that the following set of curves

intersect orthogonally: (i)

$$y = x^3 \text{ and } 6y = 7 - x^2, \quad \text{(ii)}$$

$$x^3 - 3xy^2 = -2 \text{ and } 3x^2y - y^3 = 2. \quad \text{(iii)}$$

$$x^2 + 4y^2 = 8 \text{ and } x^2 - 2y^2 = 4$$



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4. Find the angle of intersection of the

following curves :

$$(i) y^2 = x \text{ and } x^2 = y$$

$$(ii) y = x^2 \text{ and } x^2 + y^2 = 20$$

$$(iii) 2y^2 = x^3 \text{ and } y^2 = 32x$$



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5. Show that the curves  $4x = y^2$  and  $4xy = k$  cut at right angles, if  $k^2 = 512$ .



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6. Find the equation of the tangent to the curve  $\sqrt{x} + \sqrt{y} = a$ , at the point

$$\left(\frac{a^2}{4}, \frac{a^2}{4}\right).$$



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7. Find a point on the curve  $y = x^3 - 3x$  where the tangent is parallel to the chord joining  $(1, -2)$  and  $(2, 2)$ .



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8. Find the points on the curve  $xy + 4 = 0$  at which the tangents are inclined at an angle of

$45^0$  with the  $x$  – axis .



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**9.** Find the equation of normal line to the curve  $y = x^3 + 2x + 6$  which is parallel to the line  $x + 14y + 4 = 0$ .



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**10.** Find the slopes of the tangent and the normal to the following curves at the

indicated points:  $y = \sqrt{x^3} \text{ at } x = 4$

$y = \sqrt{x^3} \text{ at } x = 9$        $y = x^3 - x \text{ at } x = 2$

$y = 2x^2 + 3 \sin x \text{ at } x = 0$

$x = a(\theta - \sin \theta), y = a(1 + \cos \theta) \text{ at } \theta = -\frac{\pi}{2}$

$x = a \cos^3 \theta, y = a \sin^3 \theta \text{ at } \theta = \frac{\pi}{4}$

$x = a\left(\theta - \int \sin \theta\right), y = a(1 - \cos \theta) \text{ at } \theta = \frac{\pi}{2}$

$y = (\sin 2x + \cot x + 2) \text{ at } x = \frac{\pi}{2}$

$x^2 + 3y + y^2 = 5 \text{ at } (1, 1) \quad xy = 6 \text{ at } (1, 6)$



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11. If the tangent to the curve  $y = x^3 + ax + b$  at  $(1, -6)$  is parallel to the line  $x - y + 5 = 0$ , find  $a$  and  $b$



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12. Find the equation of the tangent to the curve  $x = \sin 3t, y = \cos 2t$  at  $t = \frac{\pi}{4}$ .



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**13.** Prove that  $\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 2$  touches the straight line  $\frac{x}{a} + \frac{y}{b} = 2$  for all  $n \in \mathbb{N}$ , at the point  $(a, b)$ .



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**14.** At what point on the circle  $x^2 + y^2 - 2x - 4y + 1 = 0$ , the tangent is parallel to x-axis.



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**15.** Find the point on the curve  $y = x^2$  where the slope of the tangent is equal to the  $x$  – coordinate of the point.



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**16.** At what point will be tangents to the curve  $y = 2x^3 - 15x^2 + 36x - 21$  be parallel to  $x$ -axis? Also, find the equations of the tangents to the curve at these points.



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**17.** If the straight line  $x \cos \alpha + y \sin \alpha = p$  touches the curve  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ , then prove that  $a^2 \cos^2 \alpha - b^2 \sin^2 \alpha = p^2$ .



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**18.** Find the point on the curve  $y = 3x^2 + 4$  at which the tangent is perpendicular to the line whose slope is  $-\frac{1}{6}$ .



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**19.** Find the equation of the normal to

$$y = 2x^3 - x^2 + 3 \text{ at } (1,4).$$



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**20.** Find the point on the curve

$$y = 3x^2 - 9x + 8 \text{ at which the tangents are}$$

equally inclined with the axes.



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21. Find the equation of the tangent to the curve  $x = \theta + \sin \theta$ ,  $y = 1 + \cos \theta$ , at  $\theta = \frac{\pi}{4}$



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22. Find the equation of the normal to the curve  $x^2 + 2y^2 - 4x - 6y + 8 = 0$  at the point whose abscissa is 2.



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**23.** The equation of the tangent at (2,3) on the curve  $y^2 = ax^3 + b$  is  $y = 4x - 5$ . Find the values of  $a$  and  $b$



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**24.** Find the equation of the tangent line to the curve  $y = x^2 + 4x - 16$  which is parallel to the line  $3x - y + 1 = 0$ .



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25. If the straight line  $x \cos \alpha + y \sin \alpha = p$  touches the curve  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , then prove that  $a^2 \cos^2 \alpha + b^2 \sin^2 \alpha = p^2$ .



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26. Find the angle of intersection of the following curves:  $xy = 6$  and  $x^2y = 12$

$$y^2 = 4x \text{ and } x^2 = 4y$$



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27. Show that the curves  $x = y^2$  and  $xy = k$  cut at right angles, if  $8k^2 = 1$



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28. The curve  $y = ax^3 + bx^2 + cx + 5$  touches the x-axis at  $P(-2, 0)$  and cuts the y-axis at the point  $Q$  where its gradient is 3. Find the equation of the curve completely.



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**29.** Determine the quadratic curve  $y = f(x)$  if it touches the line  $y = x$  at the point  $x = 1$  and passes through the point  $(-1, 0)$ .



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**30.** Find all the tangents to the curve  $y = \cos(x + y)$ ,  $-2\pi \leq x \leq 2\pi$  that are parallel to the line  $x + 2y = 0$ .



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**31.** Find the equation of the normal to the curve  $y = (1 + x)^y + \sin^{-1}(\sin^2 x)$  at  $x = 0$ .



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**32.** Find the equation of the tangent to the curve  $y = (x^3 - 1)(x - 2)$  at the points where the curve cuts the x-axis.



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**33.** Show that the line  $\frac{x}{a} + \frac{y}{b} = 1$  touches the curve  $y = be^{-\frac{x}{a}}$  at the point where it crosses the y-axis.



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**34.** Find the equations of tangent and normal to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at  $(x_1, y_1)$



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**35.** Find the equation of the normal to the curve  $y = 2x^2 + 3 \sin x$  at  $x = 0$ .



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**36.** Find the coordinates of the points on the curve  $y = x^2 + 3x + 4$ , the tangents at which pass through the origin.



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**37.** Find the equations of the tangents drawn to the curve  $y^2 - 2x^2 - 4y + 8 = 0$ . from point  $(1, 2)$



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**38.** Find the equation(s) of normal(s) to the curve  $3x^2 - y^2 = 8$  which is (are) parallel to the line  $x + 3y = 4$ .



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**39.** Find the equation of the tangent line to the curve  $y = \sqrt{5x - 3} - 2$  which is parallel to the line  $4x - 2y + 3 = 0$



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**40.** Find the points on the curve  $4x^2 + 9y^2 = 1$ , where the tangents are perpendicular to the line  $2y + x = 0$ .



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**41.** Find the points on the curve  $9y^2 = x^3$  where normal to the curve makes equal intercepts with the axes.



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**42.** Prove that the curves  $xy = 4$  and  $x^2 + y^2 = 8$  touch each other.



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**43.** Prove that the curves  $y^2 = 4x$  and  $x^2 + y^2 - 6x + 1 = 0$  touch each other at the points  $(1, 2)$ .



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**44.** Show that the angle between the tangent at any point P and the line joining P to the origin O is same at all points on the curve  $\log(x^2 + y^2) = k \tan^{-1}\left(\frac{y}{x}\right)$



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**45.** Find the slopes of the tangent and the normal to the curve  $x^2 + 3yy^2 = 5$  at  $(1, 1)$



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**46.** Show that the tangents to the curve  $y = x^3 - 3$  at the points where  $x = 2$  and  $x = -2$  are parallel.



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**47.** Prove that the tangents to the curve  $y = x^2 - 5x + 6$  at the points  $(2, 0)$  and  $(3, 0)$  are at right angles.



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**48.** The slope of the curve  $2y^2 = ax^2 + bx$  at  $(1, -1)$  is  $-1$ . Find  $a, b$



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**49.** Find the points on the curve  $y = x^3 - 2x^2 - x$  at which the tangent lines are parallel to the line  $y = 3x - 2$



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**50.** At what points on the curve  $x^2 + y^2 - 2x - 4y + 1 = 0$ , the tangents are parallel to the  $y - a$  is?



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51. Find the required point be  $P(x_1, y_1)$ . The tangent to the curve  $\sqrt{x} + \sqrt{y} = 4$  at which tangent is equally inclined to the axes.



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52. Show that the curves  $2x = y^2$  and  $2xy = k$  cut at right angles, if  $k^2 = 8$ .



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**53.** Show that the curves

$xy = a^2$  and  $x^2 + y^2 = 2a^2$  touch each other



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**54.** Find the slopes of the tangent and the

normal to the curve  $x^2 + 3y + y^2 = 5$  at

$(1, 1)$



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**55.** Show that the tangents to the curve  $y = 2x^3 - 3$  at the points where  $x = 2$  and  $x = -2$  are parallel.



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**56.** Prove that the tangents to the curve  $y = x^2 - 5x + 6$  at the points  $(2, 0)$  and  $(3, 0)$  are at right angles.



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57. The slope of the curve  $2y^2 = ax^2 + b$  at  $(1, -1)$  is  $-1$ . Find  $a, b$ .



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58. Find the slope of the normal to the curve  $x = 1 - a \sin \theta, y = b \cos^2 \theta$  at  $\theta = \frac{\pi}{2}$ .



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**59.** Find the slope of the normal to the curve

$$x = a \cos^3 \theta, y = a \sin^3 \theta \text{ at } \theta = \frac{\pi}{4}.$$



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**60.** Find the points on the curve

$$y = x^3 - 2x^2 - x \text{ at which the tangent lines are parallel to the line } y = 3x - 2.$$



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**61.** Find the point on the curve  $y = 2x^2 - 6x - 4$  at which the tangent is parallel to the x-axis.



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**62.** At what points on the curve  $x^2 + y^2 - 2x - 4y + 1 = 0$ , the tangents are parallel to the  $y - a$  is?



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**63.** For which value of  $m$  is the line  $y = mx + 1$  a tangent to the curve  $y^2 = 4x$

A.  $1/2$

B. 1

C. 2

D. 3

**Answer: Option 2**



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64. Find points on the curve  $\frac{x^2}{9} + \frac{y^2}{16} = 1$  at

which the tangents are parallel to the y-axis.

A. (0,4) & (0,-4)

B. (4,0) & (-4,0)

C. (3,0) & (-3,0)

D. (0,3) & (0,-3)

**Answer: Option C**

**Points are (3, 0) and ( - 3, 0).**



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**65.** Find a point on the curve  $y = (x - 3)^2$ , where the tangent is parallel to the line joining  $(4, 1)$  and  $(3, 0)$ .



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**66.** Find the required point be  $P(x_1, y_1)$ . The tangent to the curve  $\sqrt{x} + \sqrt{y} = 4$  at which tangent is equally inclined to the axes.



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67. Find the points on the curve  $4x^2 + 9y^2 = 1$ , where the tangents are perpendicular to the line  $2y + x = 0$



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68. Find the point on the curve  $y = x^3 - 11x + 5$  at which the tangent has the equation  $y = x - 11$



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**69.** Find the points on the curve  $9y^2 = x^3$  where normal to the curve makes equal intercepts with the axes.



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**70.** Find the slopes of the tangent and the normal to the curve  $y = \sqrt{x^3}$  at  $x = 4$



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71. Find the slopes of the tangent and the normal to the curve  $y = \sqrt{x}$  at  $x = 9$



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72. Find the slopes of the tangent and the normal to the curve  $y = x^3 - x$  at  $x = 2$



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**73.** Find the slopes of the tangent and the normal to the curve  $y = 2x^2 + 3\sin x$  at  $x = 0$



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**74.** Find the slopes of the tangent and the normal to the curve  $x = a(\theta - \sin \theta)$  ,  
 $y = a(1 + \cos \theta)$  at  $\theta = -\pi/2$



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75. Find the slopes of the tangent and the normal to the curve  $x = a \cos^3 \theta$ ,  $y = a \sin^3 \theta$  at  $\theta = \pi/4$



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76. Find the slopes of the tangent and the normal to the curve  $x = a(\theta - \sin \theta)$ ,  $y = a(1 - \cos \theta)$  at  $\theta = \pi/2$



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77. Find the slopes of the tangent and the normal to the curve  $y = (\sin 2x + \cot x + 2)^2$  at  $x = \pi / 2$



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78. Find the slopes of the tangent and the normal to the curve  $x^2 + 3y + y^2 = 5$  at  $(1, 1)$



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**79.** Find the slopes of the tangent and the normal to the curve  $xy = 6$  at  $(1, 6)$



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**80.** Find the values of  $a$  and  $b$  if the slope of the tangent to the curve  $xy + ax + by = 2$  at  $(1, 1)$  is 2.



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**81.** If the tangent to the curve  $y = x^3 + ax + b$  at  $(1, -6)$  is parallel to the line  $x - y + 5 = 0$ , find  $a$  and  $b$ .



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**82.** Find a point on the curve  $y = x^3 - 3x$  where the tangent is parallel to the chord joining  $(1, -2)$  and  $(2, 2)$ .



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**83.** Find the points on the curve  $x^3 - 2x^2 - 2x$  at which the tangent lines are parallel to the line  $y = 2x - 3$ .



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**84.** Find the points on the curve  $y^2 = 2x^3$  at which the slope of the tangent is 3.



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**85.** Find the points on the curve  $xy + 4 = 0$  at which the tangents are inclined at an angle of  $45^\circ$  with the x-axis.



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**86.** Find the point on the curve  $y = x^2$  where the slope of the tangent is equal to the x-coordinate of the point.



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**87.** At what points on the circle  $x^2 + y^2 - 2x - 4y + 1 = 0$ , the tangent is parallel to the x-axis.



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**88.** At what point of the curve  $y = x^2$  does the tangent make an angle of  $45^\circ$  with the x-axis?



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**89.** Find the points on the curve  $y = 3x^2 - 9x + 8$  at which the tangents are equally inclined with the axes.



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**90.** At what points on the curve  $y = 2x^2 - x + 1$  is the tangent parallel to the line  $y = 3x + 4$ ?



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91. Find the point on the curve  $y = 3x^2 + 4$  at which the tangent is perpendicular to the line whose slope is  $-\frac{1}{6}$ .



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92. Find the points on the curve  $x^2 + y^2 = 13$ , the tangent at each one of which is parallel to the line  $2x + 3y = 7$ .



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**93.** Find the points on the curve  $2a^2y = x^3 - 3ax^2$  where the tangent is parallel to x-axis.



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**94.** At what points on the curve  $y = x^2 - 4x + 5$  is the tangent perpendicular to the line  $2y + x = 7$ ?



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**95.** Find the points on the curve  $\frac{x^2}{4} + \frac{y^2}{25} = 1$  at which the tangents are parallel to the x-axis and y-axis.



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**96.** Find the points on the curve  $x^2 + y^2 - 2x - 3 = 0$  at which the tangents are parallel to the x-axis and y-axis.



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**97.** Find the points on the curve  $\frac{x^2}{9} + \frac{y^2}{16} = 1$  at which the tangents are parallel to the x-axis and y-axis.



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**98.** Show that the tangents to the curve  $y = 7x^3 + 11$  at the points  $x = 2$  and  $x = -2$  are parallel.



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**99.** Find the points on the curve  $y = x^3$  where the slope of the tangent is equal to  $x$ -coordinate of the point.



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**100.** Find the equation of the tangent to the curve  $y = -5x^2 + 6x + 7$  at the point  $(1/2, 35/4)$ .



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**101.** Find the equation of the tangent and normal to the parabola  $y^2 = 4ax$  at the point  $(at^2, 2at)$ .



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**102.** Find the equation of the normal to the curve  $y = 2x^2 + 3 \sin x$  at  $x = 0$ .



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**103.** Find the equations of the tangent and the normal to  $16x^2 + 9y^2 = 144$  at  $(x_1, y_1)$  where  $x_1 = 2$  and  $y_1 > 0$ .



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**104.** Find the equations of tangent and normal to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at  $(x_1, y_1)$



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**105.** Find the equation of the tangent line to the curve  $x = 1 - \cos \theta$ ,  $y = \theta - \sin \theta$  at  $\theta = \pi/4$ .



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**106.** Find the equations of the tangent and the normal at the point ' $t$ ' on the curve  $x = a s \in^3 t$ ,  $y = b \cos^3 t$ .



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**107.** Show that the line  $\frac{x}{a} + \frac{y}{b} = 1$  touches the curve  $y = be^{-\frac{x}{a}}$  at the point where it crosses the y-axis.



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**108.** Find the equation of the tangent to the curve  $y = \frac{x - 7}{(x - 2)(x - 3)}$  at the point where it cuts the x-axis.



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**109.** Find the equation of the tangent to the curve  $y = (x^3 - 1)(x - 2)$  at the points where the curve cuts the x-axis.



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**110.** Find the equation of the tangent line to the curve  $y = \sqrt{5x - 3} - 2$  which is parallel to the line  $4x - 2y + 3 = 0$ .



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**111.** Find the equation of tangent line to  $y = 2x^2 + 7$  which is parallel to the line  $4x - y + 3 = 0$ .



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**112.** Find the equation(s) of normal(s) to the curve  $3x^2 - y^2 = 8$  which is (are) parallel to the line  $x + 3y = 4$ .



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**113.** Find the equation of normal line to the curve  $y = x^3 + 2x + 6$  which is parallel to the line  $x + 14y + 4 = 0$ .



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**114.** Find the equations of the tangents drawn to the curve  $y^2 - 2x^3 - 4y + 8 = 0$ .



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**115.** Find the equation of the normal to the curve  $x^2 = 4y$  which passes through the point (1, 2).



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**116.** Find the coordinates of the points on the curve  $y = x^2 + 3x + 4$  , the tangents at which pass through the origin.



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**117.** For the curve  $y = 4x^3 - 2x^5$  find all points at which the tangent passes through the origin.



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**118.** Find the equation of all lines having slope 1 that are tangents to the curve

$$y = \frac{1}{x-1}, x \neq 1.$$



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**119.** Prove that all normals to the curve  $x = a \cos t + at \sin t$ ,  $y = a \sin t - at \cos t$  are at a distance  $a$  from the origin.



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**120.** Find the equation of the normal to the curve  $y = (1 + x)^y + \sin^{-1}(\sin^2 x)$  at  $x = 0$ .



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**121.** Find all the tangents to the curve  $y = \cos(x + y)$ ,  $-2\pi \leq x \leq 2\pi$  that are parallel to the line  $x + 2y = 0$ . xyz



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**122.** The curve  $y = ax^3 + bx^2 + cx + 5$  touches the x-axis at  $P(-2, 0)$  and cuts the y-axis at the point  $Q$  where its gradient is 3. Find the equation of the curve completely.



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**123.** Determine the quadratic curve  $y = f(x)$  if it touches the line  $y = x$  at the point  $x = 1$  and passes through the point  $(-1, 0)$ .



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**124.** Find the equation of the tangent to the curve  $\sqrt{x} + \sqrt{y} = a$ , at the point  $(a^2/4, a^2/4)$ .



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**125.** Find the equation of the normal to

$$y = 2x^3 - x^2 + 3 \text{ at } (1, 4).$$



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**126.** Find the equations of the tangent and the

normal to the curve

$$y = x^4 - bx^3 + 13x^2 - 10x + 5 \text{ at } (0, 5) \text{ at}$$

the indicated points



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**127.** Find the equations of the tangent and the normal to the curve  $y = x^4 - 6x^3 + 13x^2 - 10x + 5$  at  $x = 1$  at the indicated points



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**128.** Find the equations of the tangent and the normal to the curve  $y = x^2$  at  $(0, 0)$  at the indicated points



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**129.** Find the equations of the tangent and the normal to the curve  $y = 2x^2 - 3x - 1$  at  $(1, -2)$  at the indicated points



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**130.** Find the equations of the tangent and the normal to the curve  $y^2 = \frac{x^3}{4-x}$  at  $(2, -2)$  at the indicated points



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**131.** Find the equations of the tangent and the normal to the curve  $y = x^2 + 4x + 1$  at  $x = 3$  at the indicated points



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**132.** Find the equations of the tangent and the normal to the curve  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at  $(a \cos \theta, b \sin \theta)$  at the indicated points



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**133.** Find the equations of the tangent and the normal to the curve  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  at  $(a \sec \theta, b \tan \theta)$  at the indicated points.



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**134.** Find the equations of the tangent and the normal to the curve  $y^2 = 4ax$  at  $(a/m^2, 2a/m)$  at the indicated points



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**135.** Find the equations of the tangent and the normal to the curve  $c^2(x^2 + y^2) = x^2 y^2$  at  $\left(\frac{c}{\cos \theta}, \frac{c}{\sin \theta}\right)$  at the indicated points



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**136.** Find the equations of the tangent and the normal to the curve  $xy = c^2$  at  $(ct, c/t)$  at the indicated points.



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**137.** Find the equations of the tangent and the normal to the curve  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at  $(x_1, y_1)$  at the indicated points.



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**138.** Find the equation of the normal to the curve  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  at  $(x_0, y_0)$



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**139.** Find the equations of the tangent and the normal to the curve  $x^{2/3} + y^{2/3} = 2$  at  $(1, 1)$  at indicated points.



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**140.** Find the equations of the tangent and the normal to the curve  $x^2 = 4y$  at  $(2, 1)$  at indicated points.



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**141.** Find the equations of the tangent and the normal to the curve  $y^2 = 4x$  at  $(1, 2)$  at indicated points.



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**142.** Find the equations of the tangent and the normal to the curve  $4x^2 + 9y^2 = 36$  at  $(3 \cos \theta, 2 \sin \theta)$  at indicated points.



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**143.** Find the equations of the tangent and the normal to the curve  $y^2 = 4ax$  at  $(x_1, y_1)$  at indicated points.



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**144.** Find the equations of the tangent and the normal to the curve  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  at  $(\sqrt{2}a, b)$  at indicated points.



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**145.** Find the equation of the tangent to the curve  $x = \theta + \sin \theta$  ,  $y = 1 + \cos \theta$  at  $\theta = \pi / 4$ .



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**146.** Find the equations of the tangent and the normal to the curve  $x = \theta + \sin \theta$  ,  $y = 1 + \cos \theta$  at  $\theta = \pi / 2$  at indicated points.



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**147.** Find the equation of tangent and normal

to the curve  $x = \frac{2at^2}{(1+t^2)}$ ,  $y = \frac{2at^3}{(1+t^2)}$  at

the point for which  $t = \frac{1}{2}$ .



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**148.** Find the equations of the tangent and the

normal to the curve  $x = at^2$ ,  $y = 2at$  at

$t = 1$ .



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**149.** Find the equations of the tangent and the normal to the curve  $x = a \sec t$ ,  $y = b \tan t$  at  $t$  at indicated points.



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**150.** Find the equations of the tangent and the normal to the curve  $x = a(\theta + \sin \theta)$ ,  $y = a(1 - \cos \theta)$  at  $\theta$  at indicated points.



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**151.** Find the equations of the tangent and the normal to the curve

$$x = 3 \cos \theta - \cos^3 \theta, \quad y = 3 \sin \theta - \sin^3 \theta$$



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**152.** Find the equation of the normal to the curve  $x^2 + 2y^2 - 4x - 6y + 8 = 0$  at the point whose abscissa is 2.



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**153.** Find the equation of the normal to the curve  $ay^2 = x^3$  at the point  $(am^2, am^3)$ .



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**154.** The equation of the tangent at  $(2, 3)$  on the curve  $y^2 = ax^3 + b$  is  $y = 4x - 5$ . Find the values of  $a$  and  $b$ .



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**155.** Find the equation of the tangent line to the curve  $y = x^2 + 4x - 16$  which is parallel to the line  $3x - y + 1 = 0$ .



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**156.** Find the equation of normal line to the curve  $y = x^3 + 2x + 6$  which is parallel to the line  $x + 14y + 4 = 0$ .



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**157.** Determine the equation(s) of tangent(s) line to the curve  $y = 4x^3 - 3x + 5$  which are perpendicular to the line  $9y + x + 3 = 0$



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**158.** Find the equation of a normal to the curve  $y = x(\log)_e x$  which is parallel to the line  $2x - 2y + 3 = 0$ .



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**159.** Find the equation of the tangent line to the curve  $y = x^2 - 2x + 7$  which is parallel to the line  $2x - y + 9 = 0$



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**160.** Find the equation of the tangent line to the curve  $y = x^2 - 2x + 7$  which is perpendicular to the line  $5y - 15x = 13$ .



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**161.** Find the equations of all lines having slope 2 and that are tangent to the curve

$$y = \frac{1}{x - 3}, \quad x \neq 3.$$



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**162.** Find the equations of all lines of slope zero and that are tangent to the curve

$$y = \frac{1}{x^2 - 2x + 3}.$$



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**163.** Find the equation of the tangent to the curve  $y = \sqrt{3x - 2}$  which is parallel to the line  $4x - 2y + 5 = 0$



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**164.** Find the equation of the tangent to the curve  $x^2 + 3y - 3 = 0$  , which is parallel to the line  $y = 4x - 5$  .



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**165.** Find the value of  $n \in \mathbb{N}$  such that the curve  $\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 2$  touches the straight line  $\frac{x}{a} + \frac{y}{b} = 2$  at the point  $(a, b)$ .



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**166.** Find the equation of the tangent to the curve  $x = \sin 3t$ ,  $y = \cos 2t$  at  $t = \frac{\pi}{4}$ .



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**167.** At what points will be tangents to the curve  $y = 2x^3 - 15x^2 + 36x - 21$  be parallel to x-axis? Also, find the equations of the tangents to the curve at these points.



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**168.** Find the equation of the tangents to the curve  $3x^2 - y^2 = 8$ , which passes through the point  $\left(\frac{4}{3}, 0\right)$ .



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**169.** Find the angle of intersection of  $xy = 6$   
and  $x^2y = 12$



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**170.** Find the angle of intersection of  $y^2 = 4x$   
and  $x^2 = 4y$



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**171.** Find the angle between the parabolas  $y^2 = 4ax$  and  $x^2 = 4by$  at their point of intersection other than the origin.



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**172.** Show that the curves  $x = y^2$  and  $xy = k$  cut at right angles, if  $8k^2 = 1$ .



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**173.** Find the value of  $p$  for which curves  $x^2 = 9p(9 - y)$  and  $x^2 = p(y + 1)$  cut each other at right angles.



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**174.** Show that the curves  $xy = a^2$  and  $x^2 + y^2 = 2a^2$  touch each other.



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**175.** Show the condition that the curves  $ax^2 + by^2 = 1$  and  $a'x^2 + b'y^2 = 1$  should intersect orthogonally



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**176.** If the straight line  $x \cos \alpha + y \sin \alpha = p$  touches the curve  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , then prove that  $a^2 \cos^2 \alpha + b^2 \sin^2 \alpha = p^2$ .



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**177.** Show that the angle between the tangent at any point  $P$  and the line joining  $P$  to the origin  $O$  is the same at all points on the curve  $\log(x^2 + y^2) = k \tan^{-1}\left(\frac{y}{x}\right)$ .



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**178.** Find the angle of intersection of the curves  $y^2 = x$  and  $x^2 = y$



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**179.** Find the angle of intersection of curve

$$y = x^2 \text{ and } x^2 + y^2 = 20$$



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**180.** Find the angle of intersection of curve

$$2y^2 = x^3 \text{ and } y^2 = 32x$$



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**181.** Find the angle of intersection of curve

$$x^2 + y^2 - 4x - 1 = 0 \quad \text{and}$$

$$x^2 + y^2 - 2y - 9 = 0$$



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**182.** Find the angle of intersection of curve

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \text{ and } x^2 + y^2 = ab$$



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**183.** Find the angle of intersection of curve

$$x^2 + 4y^2 = 8 \text{ and } x^2 - 2y^2 = 2$$



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**184.** Find the angle of intersection of curve

$$x^2 = 27y \text{ and } y^2 = 8x$$



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**185.** Find the angle of intersection of curve

$$x^2 + y^2 = 2x \text{ and } y^2 = x$$



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**186.** Find the angle of intersection of curve

$$y = 4 - x^2 \text{ and } y = x^2$$



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**187.** Show that  $y = x^3$  and  $6y = 7 - x^2$

intersect orthogonally:



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**188.** Show that  $x^3 - 3xy^2 = -2$  and  $3x^2y - y^3 = 2$  intersect orthogonally:



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**189.** Show that  $x^2 + 4y^2 = 8$  and  $x^2 - 2y^2 = 4$  intersect orthogonally



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**190.** Show that  $x^2 = 4y$  and  $4y + x^2 = 8$  intersect orthogonally at  $(2, 1)$



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**191.** Show that  $x^2 = y$  and  $x^3 + 6y = 7$  intersect orthogonally at  $(1, 1)$



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**192.** Show that  $y^2 = 8x$  and  $2x^2 + y^2 = 10$  at  $(1, 2\sqrt{2})$



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**193.** Show that the curves  $4x = y^2$  and  $4xy = k$  cut at right angles, if  $k^2 = 512$ .



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**194.** Show that the curves  $2x = y^2$  and  $2xy = k$  cut at right angles, if  $k^2 = 8$ .



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**195.** Prove that the curves  $xy = 4$  and  $x^2 + y^2 = 8$  touch each other.



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**196.** Prove that the curves  $y^2 = 4x$  and  $x^2 + y^2 - 6x + 1 = 0$  touch each other at the points  $(1, 2)$ .



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**197.** Find the condition for the following set of curves to intersect orthogonally:

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad \text{and} \quad xy = c^2 \quad \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

and  $\frac{x^2}{A^2} - \frac{y^2}{B^2} = 1$ .



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**198.** Find the condition for the two concentric ellipses

$a_1x^2 + b_1y^2 = 1$  and  $a_2x^2 + b_2y^2 = 1$  to intersect orthogonally.



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**199.** If the straight line  $x \cos \alpha + y \sin \alpha = p$

touches the curve  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , then prove

that  $a^2 \cos^2 \alpha + b^2 \sin^2 \alpha = p^2$ .



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**200.** Find the point on the curve  $y = x^2 - 2x + 3$ , where the tangent is parallel to x-axis.



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**201.** Find the slope of the tangent to the curve  $x = t^2 + 3t - 8, y = 2t^2 - 2t - 5$  at  $t = 2$ .



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**202.** If the tangent line at a point  $(x, y)$  on the curve  $y = f(x)$  is parallel to x-axis, then write the value of  $\frac{dy}{dx}$ .



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**203.** Write the value of  $\frac{dy}{dx}$ , if the normal to the curve  $y = f(x)$  at  $(x, y)$  is parallel to y-axis.



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**204.** If the tangent to a curve at a point  $(x, y)$  is equally inclined to the coordinate axes, then write the value of  $\frac{dy}{dx}$ .



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**205.** If the tangent line at a point  $(x, y)$  on the curve  $y = f(x)$  is parallel to y-axis, find the value of  $\frac{dx}{dy}$ .



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**206.** Find the slope of the normal at the point

' $t$ ' on the curve  $x = \frac{1}{t}$ ,  $y = t$ .



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**207.** Write the coordinates of the point on the

curve  $y^2 = x$  where the tangent line makes an

angle  $\frac{\pi}{4}$  with x-axis.



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**208.** Write the angle made by the tangent to the curve  $x = e^t \cot t$ ,  $y = e^t \sin t$  at  $t = \frac{\pi}{4}$  with the x-axis.



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**209.** Write the equation of the normal to the curve  $y = x + \sin x \cos x$  at  $x = \frac{\pi}{2}$ .



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**210.** Find the coordinates of the point on the curve  $y^2 = 3 - 4x$  where tangent is parallel to the line  $2x + y - 2 = 0$ .



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**211.** Write the equation of the tangent to the curve  $y = x^2 - x + 2$  at the point where it crosses the y-axis.



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**212.** Write the angle between the curves  $y^2 = 4x$  and  $x^2 = 2y - 3$  at the point  $(1, 2)$ .



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**213.** Write the angle between the curves  $y = e^{-x}$  and  $y = e^x$  at their point of intersection.



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**214.** Write the slope of the normal to the curve

$$y = \frac{1}{x} \text{ at the point } \left( 3, \frac{1}{3} \right)$$



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**215.** Write the coordinates of the point at

which the tangent to the curve

$y = 2x^2 - x + 1$  is parallel to the line

$$y = 3x + 9.$$



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**216.** Write the equation of the normal to the curve  $y = \cos x$  at  $(0, 1)$  .



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**217.** The equation to the normal to the curve  $y = \sin x$  at  $(0, 0)$  is  $x = 0$  (b)  $y = 0$  (c)  $x + y = 0$  (d)  $x - y = 0$



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**218.** Find the equation of the tangent to the curve  $y = x - \sin x \cos x$  at  $x = \frac{\pi}{2}$



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**219.** The equation of the normal to the curve

$y = x(2 - x)$  at the point  $(2, 0)$  is

$x - 2y = 2$  (b)  $x - 2y + 2 = 0$  (c)

$2x + y = 4$  (d)  $2x + y - 4 = 0$



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**220.** The point on the curve  $y^2 = x$  where tangent makes  $45^\circ$  angle with x-axis is  
(1/2, 1/4) (b) (1/4, 1/2) (c) (4, 2) (d)  
(1, 1)



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**221.** If the tangent to the curve  $x = at^2, y = 2at$  is perpendicular to x-axis, then its point of contact is (a, a) (b) (0, a)  
(c) (0, 0) (d) (a, 0)



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**222.** The point on the curve  $y = x^2 - 3x + 2$  where tangent is perpendicular to  $y = x$  is  
(a)  $(0, 2)$  (b)  $(1, 0)$  (c)  $(-1, 6)$  (d)  $(2, -2)$



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**223.** The point on the curve  $y = 12x - x^2$  where the slope of the tangent is zero will be  
(a)  $(0, 0)$  (b)  $(2, 16)$  (c)  $(3, 9)$  (d)  $(6, 36)$



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**224.** The angle between the curves  $y^2 = x$  and  $x^2 = y$  at  $(1, 1)$  is  $\frac{\tan^{-1} 4}{3}$  (b)  $\frac{\tan^{-1} 3}{4}$  (c)  $90^\circ$  (d)  $45^\circ$



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**225.** The equation of the normal to the curve  $3x^2 - y^2 = 8$  which is parallel to  $x + 3y = 8$  is  $x - 3y = 8$  (b)  $x - 3y + 8 = 0$  (c)  $x + 3y \pm 8 = 0$  (d)  $x + 3y = 0$



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**226.** The equation of tangent at those points where the curve  $y = x^2 - 3x + 2$  meets x-axis

are  $x - y + 2 = 0 = x - y - 1$  (b)

$x + y - 1 = 0 = x - y - 2$  (c)

$x - y - 1 = 0 = x - y$  (d)

$x - y = 0 = x + y$



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**227.** The slope of the tangent to the curve  $x = t^2 + 3t - 8$ ,  $y = 2t^2 - 2t - 5$  at point  $(2, -1)$  is (a)  $22/7$  (b)  $6/7$  (c)  $-6$  (d)  $7/6$



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**228.** At what points the slope of the tangent to the curve  $x^2 + y^2 - 2x - 3 = 0$  is zero (a)  $(3, 0), (-1, 0)$  (b)  $(3, 0), (1, 2)$  (c)  $(-1, 0), (1, 2)$  (d)  $(1, 2), (1, -2)$



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**229.** The angle of intersection of the curves  $xy = a^2$  and  $x^2 - y^2 = 2a^2$  is zero (a)  $0^\circ$  (b)  $45^\circ$  (c)  $90^\circ$  (d)  $30^\circ$



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**230.** If the curve  $ay + x^2 = 7$  and  $x^3 = y$  cut orthogonally at  $(1, 1)$ , then  $a$  is equal to (a) 1 (b) -6 (c) 6 (d) 0



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**231.** If the line  $y = x$  touches the curve  $y = x^2 + bx + c$  at a point  $(1, 1)$  then  
 $b = 1, c = 2$  (b)  $b = -1, c = 1$  (c)  
 $b = 2, c = 1$  (d)  $b = -2, c = 1$



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**232.** The slope of the tangent to the curve  $x = 3t^2 + 1, y = t^3 - 1$  at  $x = 1$  is  $1/2$  (b)  $0$   
(c)  $-2$  (d)  $\infty$



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**233.** The curves  $y = ae^x$  and  $y = be^{-x}$  cut orthogonally, if  $a = b$  (b)  $a = -b$  (c)  $ab = 1$   
(d)  $ab = 2$



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**234.** The equation of the normal to the curve  $x = a \cos^3 \theta$ ,  $y = a \sin^3 \theta$  at the point  $\theta = \pi/4$  is  $x = 0$  (b)  $y = 0$  (c)  $x = y$  (d)  
 $x + y = a$



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**235.** If the curves  $y = 2e^x$  and  $y = ae^{-x}$  intersect orthogonally, then  $a =$  (a)  $1/2$  (b)  $-1/2$  (c)  $2$  (d)  $2e^2$



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**236.** The point on the curve  $y = 6x - x^2$  at which the tangent to the curve is inclined at  $\pi/4$  to the line  $x + y = 0$  is (a)  $(-3, -27)$  (b)  $(3, 9)$  (c)  $(7/2, 35/4)$  (d)  $(0, 0)$



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**237.** The angle of intersection of the parabola

$y^2 = 4ax$  and  $x^2 = 4ay$  at the origin is  $\pi/6$

(b)  $\pi/3$  (c)  $\pi/2$  (d)  $\pi/4$



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**238.** The angle of intersection of the curves

$y = 2s \in^2 x$  and  $y = \cos 2x$  at  $x = \frac{\pi}{6}$  is

$\pi/4$  (b)  $\pi/2$  (c)  $\pi/3$  (d)  $\pi/6$



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**239.** Any tangent to the curve  $y = 2x^7 + 3x + 5$  (a) is parallel to x-axis (b) is parallel to y-axis (c) makes an acute angle with x-axis (d) makes an obtuse angle with x-axis.



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**240.** The point on the curve  $9y^2 = x^3$ , where the normal to the curve makes equal

intercepts with the axes is  $(4, \pm 8/3)$  (b)

$(-4, 8/3)$  (c)  $(-4, -8/3)$  (d)  $(8/3, 4)$



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**241.** The slope of the tangent to the curve

$x = t^2 + 3t - 8$ ,  $y = 2t^2 - 2t - 5$  at the

point  $(2, -1)$  is  $22/7$  (b)  $6/7$  (c)  $7/6$  (d)

$-6/7$



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**242.** The line  $y = mx + 1$  is a tangent to the curve  $y^2 = 4x$ , if the value of  $m$  is (a) 1 (b) 2 (c) 3 (d)  $1/2$



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**243.** The normal at the point (1,1) on the curve  $2y + x^2 = 3$  is (A)  $x + y = 0$  (B)  $xy = 0$  (C)  $x + y + 1 = 0$  (D)  $xy = 0$



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**244.** The normal to the curve  $x^2 = 4y$  passing through  $(1,2)$  is (A)  $x + y = 3$  (B)  $xy = 3$  (C)  $x + y = 1$   
(D)  $xy = 1$



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## Others

**1.** Show that the curves

$$\frac{x^2}{a^2 + \lambda_1} + \frac{y^2}{b^2 + \lambda_1} = 1 \quad \text{and}$$

$\frac{x^2}{a^2 + \lambda_2} + \frac{y^2}{b^2 + \lambda_2} = 1$  intersect at right angles.



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