

## MATHS

# **BOOKS - RD SHARMA MATHS (HINGLISH)**

# UNDERSTANDING PHASE-III (SPECIAL TYPES OF QUADRILATERALS)

## Others

1. In a parallelogram the sum of any two adjacent angles is

 $180^0\cdot$ 

2. In a parallelogram, two adjacent angles are supplementary.

<b>Watch Video Solution</b>
<b>3.</b> Two adjacent angles of a parallelogram are equal. What is the measure of each?
<b>Watch Video Solution</b>
<b>4.</b> In a parallelogram $ABCD, \ \angle D = 115^0, \$ determine the measure of $\angle A \ and \ \angle B$ .

5. Two adjacent angles of a parallelogram are as 2:3. Find

the measures of all the angles.



7. In a parallelogram ABCD, the bisectors of  $\angle A$  and  $\angle B$ 

meet at O. Find  $\angle AOB$ .



**8.** Given below is a parallelogram ABCD. Complete each statement along with the definition or property used.

(i)AD =

(ii)  $\angle DCB =$ 

(iii)OC =

(iv)  $\angle DAB + \angle CDA =$ 





**9.** Two opposite angles of a parallelogram are  $(3x-2)^{\circ}$  and  $(50-x)^{\circ}$ . Find the measure of each angle of the parallelogram.

Watch Video Solution

10. If an angle of a parallelogram is two-third of its adjacent

angle, find the angles of the parallelogram.



**11.** The measure of one angle of a parallelogram is  $70^{0}$ . What

are the measures of the remaining angles?



12. Two adjacent angles of a parallelogram are as 1:2. Find the

measures of all the angles of the parallelogram.



 $\angle B, \ \angle C \ and \ \angle D$ .

15. The sum of two opposite angles of a parallelogram is

 $130^{\circ}$  . Find all the angles of the parallelogram.



**16.** All the angles of a quadrilateral are equal to each other. Find the measure of each. Is the quadrilateral a parallelogram? What special type of parallelogram is it?



**17.** Two adjacent sides of a parallelogram is 150cm. One of its sides is greater than the other by 25cm. Find the length of the sides of the parallelogram.

**18.** The perimeter of a parallelogram is 150cm. One of its sides is greater than the other by 25cm. Find the length of the sides of the parallelogram.

Watch Video Solution

**19.** The shorter side of a parallelogram is 4.8cm and the longer side is half as much again as the shorter side. Find the perimeter of the parallelogram.



20. Two adjacent angles of a parallelogram are  $(3x-4)^\circ and \ (3x+10)^\circ \cdot$  Find the angles of the

parallelogram.



**21.** In a parallelogram ABCD, the diagonals bisect each other at O. If  $\angle ABC = 30^{0}, \angle BDC = 10^{0} and \angle CAB = 70^{0}$ , Find:  $\angle DAB, \angle ADC, \angle BCD, \angle AOD, \angle DOC, \angle BOC, \angle AOB$ ,  $\angle ACD, \angle CAB, \angle ADB$ Given that

 $igtriangle ABC = 30^2, igtriangle ABC = igtriangle ADC = 30^0$ 

[We know that measure of opposite angles are equal in a parallelogram]

 $\angle BDC = 10^0$ 

 $\angle CAB = 70^{0}$ 

 $\angle BDA = \angle ADB = \angle ADC - \angle BDC$ 

 $30^2 - 10^2 = 20^2$ 

 $\angle DAB = 180^0 - 30^0 = 150^0$ 

 $\angle ADB = \angle DBC = 20^0$  (alternate angles)

 $\angle BCD = \angle DAB = 150^{\circ}$ 

[we know, opposite angles are equal in a parallelogram]

 $\angle DBA = \angle BDC = 10^0$ 

[we know, Alternate interior angles are equal]

 $\ln \Delta ABC$ 

 $\angle CAB + \angle ABC + \angle BCA = 180^{\circ}$ 

[since, sum of all angles of a triangle is 180^0]  $70^0 + 30^0 + \angle BCA = 180^0$   $\angle BCA = 180^0 - 100^0 = 80^0$   $\angle DAB = \angle DAC + \angle CAB = 70^0 + 80^0 = 150^0$   $\angle BCD = 150^0$  (opposite angle of the parallelogram)  $\angle DCA = \angle CAB = 70^0$ In  $\Delta DOC \angle BDC + \angle ACD + \angle DOC = 180^0$  [since, sum of all angles of a triangle is 180<sup>^</sup>0]

$$10^0 + 70^0 + \angle DOC = 180^0$$

$$\angle DOC = 180^0 - 80^0$$

 $\angle ACB = 80^0$ 

Watch Video Solution

**22.** The angle between the altitudes of a parallelogram, through the same vertex of an obtuse angle of the parallelogram is  $60^{0}$ . Find the angles of parallelogram.

Watch Video Solution

23. Diagonals of a parallelogram ABCD intersect at  $\dot{OAL} and CM$  are perpendiculars to BD such that

L and M lie on BD. IS AL = CM? why or why not?

**Watch Video Solution** 

24. Point E and F lie on diagonals AC of a parallelogram ABCD such that AnE = CF. What type of quadrilateral is BFDE? From the given figure we see that BFDE is also a parallelogram.

Watch Video Solution

**25.** In a parallelogram ABCD, AB = 10cm, AD = 6cm. The bisector of  $\angle A$  meets DC in E, AE and BC produced meet at F. Find the length `C Foot 26. In Figure, ABCD is a rhombus with  $\angle ABC = 56^{\circ}$ . Determine  $\angle ACD$ .

Watch Video Solution

27. One of the diagonals of a rhombus is equal to one of its

sides. Find the angles of the rhombus.



**28.** ABCD is a rhombus in which the altitude from D to side

AB bisects AB. Find the angles of the rhombus.



29. Construct a rhombus whose diagonals are 10cm and 8cm.



**31.** Fill in the blanks, in each of the following, so as to make the statement true: (i)A rhombus is a parallelogram in which.... (ii)A square is a rhombus in which.... (iii)A rhombus has all its sides of ...... length. (iv)The diagonals of a rhombus..... each other at... angles. (v)If the diagonals of a parallelogram bisect each other at right angles, then it is a....



each other. Is such a quadrilateral always a rhombus? If your answer is 'No', draw a figure to justify your answer.



**34.** ABCD is a rhombus. If  $\angle ACB = 40^{\circ}$ , find  $\angle ADB$ .





35. If the diagonals of a rhombus are 12cm and 16cm, find the

length of each side.

Watch Video Solution

**36.** Construct a rhombus whose diagonals are of length 10cm

and 6cm.

Watch Video Solution

**37.** Draw a rhombus, having each side of length 3.5cm and

one of the angle as  $40^{0}$ .



**38.** One side of a rhombus is a length of 4cm and the length

of an altitude is 3.2cm. Draw the rhombus.

Watch Video Solution

39. Draw a rhombus, having each side of length 3.5cm and

one of the angle as  $40^{0}$ .

**Watch Video Solution** 

40. One side of a rhombus is of length 4cm and the length of

an altitude is 3.2cm. Draw the rhombus.

**41.** Show that each diagonal of a rhombus bisects the angle through which it passes. Let ABCD be a rhombus whose diagonal AC and BD intersect each other at O.

 $\mathsf{In} \ \bigtriangleup AOD \ \mathsf{and} \ \bigtriangleup AOB$ 

AD = AB(sides of rhombus are equal)

AO = AO(common side)

DO = OB(diagonals bisect each other)

 $\triangle AOD \cong \triangle AOB$ 

 $\angle DAO = \angle BAO$ (cpct)

 $\angle ABO = \angle CBO$ 

 $\angle ADO = \angle CDO$ 

Hence proved



**42.** ABCD is a rhombus whose diagonals intersect at O. If AB = 10cm, diagonals  $BD = 16\ cm$ , find the length of diagonal AC

Watch Video Solution
43.
<b>Vatch Video Solution</b>
<b>44.</b> In Figure, $RENT$ is a rectangle. Its diagonals meet at $O$

Find x, if OR = 2x + 4 and OT = 3x + 1.

**45.** PQRS is a square. PR and SQ intersect at O. State the measure of  $\angle POQ$ .



**47.** ABCD is a rectangle with  $\angle BAC = 32^{0}$ . Determine  $\angle DBC$ .



**48.** The diagonals of a rectangle ABCD meet at O. If  $\angle BOC = 44^{\circ}$ , find  $\angle OAD$ .



**49.** In Figure, ABCD is a rectangle. BM and DN are perpendicular from B and D respectively on AC. Prove that  $MBC \cong DNA$  (ii) BM = DN

Watch Video Solution

50. The diagonals of a rectangle ABCD intersect in  $O_{\cdot}$  If

 $\angle BOC = 68^0$ , find  $\angle ODA$ .



**51.** The adjacent figure PQRS is a trapezium in which  $SP \mid \mid RQ$ , find the measures of  $\angle P$  and  $\angle R$ .

### Watch Video Solution

**52.** Which of the following statements are true for a rectangle? It has two pairs of equal sides. It has all its sides of equal length. Its diagonals are equal. Its diagonals bisect each other. Its diagonals are perpendicular. Its diagonals are perpendicular and bisect each other. Its diagonals are equal and bisect each other. Its diagonals are equal and perpendicular, and bisect each other. All rectangles are squares. All rhombuses are parallelograms. All squares are not

parallelograms. A rectangle is a parallelogram with one of its

angles equal to right angles.



**53.** Which of the following statements are true for a square? It is a rectangle. It has all its sides of equal length. Its diagonals bisect each other at a right angle. Its diagonals are equal to its sides.



**54.** Fill in the blanks in each of the following, so as to make the statement true: A rectangle is a parallelogram in which....

A square is a rhombus in which.... A square is a rectangle is

which....



**56.** In a rectangle ABCD, prove that  $ACB \cong CAD$ .



**57.** The sides of a rectangle are in the ratio 2:3, and its perimeter is 20cm. Draw the rectangle.



58. The sides of a rectangle are in the 4:5. Find its sides if the

perimeter is 90cm.



59. What is the length of a diagonal of a rectangle whose

sides are 5 cm and 12 cm long?

**60.** Construct a rectangle of side 8cm and diagonal 10 cm.

<b>Watch Video Solution</b>
<b>61.</b> Construct a square of side 4.8 cm.
Watch Video Solution
<b>62.</b> Identify all the quadrilaterals that have: (a) four sides of

equal length (b) four right angles



**63.** Q3) Explain how a square is: (a) a quadrilateral (b) a parallelogram (c) a rhombus (d) a rectangle



**64.** Name the quadrilaterals whose diagonals (i) bisect each other (ii) are perpendicular bisectors of each other (iii) are equal



**65.** ABC is a right-angled triangle and O is the mid-point of the side opposite to the right angle. Explain why O is equidistant from A, B and C.



**66.** To make a concrete rectangular slab the man should ensure?.

