



MATHS

BOOKS - CENGAGE MATHS (HINGLISH)

COMPLEX NUMBERS

Single correct Answer

1. The value of $\sum_{n=0}^{100} i^{n!}$ equals (where $i = \sqrt{-1}$)

A. -1

B. i

C. $2i + 95$

D. $97 + i$

Answer: C



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2. Suppose n is a natural number such that

$$\left| i + 2i^2 + 3i^3 + \dots + ni^n \right| = 18\sqrt{2} \text{ where } i \text{ is the square root of } -1. \text{ Then } n$$

is

A. 9

B. 18

C. 36

D. 72

Answer: C



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3. Let $i = \sqrt{-1}$. Define a sequence of complex number by

$$z_1 = 0, z_{n+1} = (z_n)^2 + i \text{ for } n \geq 1. \text{ In the complex plane, how far from the}$$

origin is z_{111} ?

A. 1

B. 2

C. 3

D. 4

Answer: B



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4. The complex number, $z = \frac{(-\sqrt{3} + 3i)(1 - i)}{(3 + \sqrt{3}i)(i)(\sqrt{3} + \sqrt{3}i)}$

A. lies on real axis

B. lies on imaginary axis

C. lies in first quadrant

D. lies in second quadrant

Answer: B



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5. a, b, c are positive real numbers forming a G.P. If $ax^2 + 2bx + c = 0$ and $dx^2 + 2ex + f = 0$ have a common root, then prove that $d/a, e/b, f/c$ are in A.P.

A. A. P.

B. G. P.

C. H. P.

D. None of these

Answer: C



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6. The equation $Z^3 + iZ - 1 = 0$ has

A. three real roots

B. one real roots

C. no real roots

D. no real or complex roots

Answer: C



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7. If a, b are complex numbers and one of the roots of the equation $x^2 + ax + b = 0$ is purely real whereas the other is purely imaginary, and $a^2 - \bar{a}^2 = kb$, then k is

A. 2

B. 4

C. 6

D. 8

Answer: B

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8. If Z^5 is a non-real complex number, then find the minimum value of

$$\frac{\operatorname{Im} z^5}{\operatorname{Im}^5 z}$$

A. -1

B. -2

C. -4

D. -5

Answer: C

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9. For any complex numbers

$$z_1, z_2 \text{ and } z_3, z_3 \operatorname{Im} \left(\overline{z_2 z_3} \right) + z_2 \operatorname{Im} \left(\overline{z_3 z_1} \right) + z_1 \operatorname{Im} \left(\overline{z_1 z_2} \right) \text{ is}$$

A. 0

B. $z_1 + z_2 + z_3$

C. $z_1 z_2 z_3$

D. $\left(\frac{z_1 + z_2 + z_3}{z_1 z_2 z_3} \right)$

Answer: A

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10. The modulus and amplitude of $\frac{1 + 2i}{1 - (1 - i)^2}$ are

A. $\sqrt{2}$ and $\frac{\pi}{6}$

B. 1 and $\frac{\pi}{4}$

C. 1 and 0

D. 1 and $\frac{\pi}{3}$

Answer: C

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11. If the argument of $(z - a)(\bar{z} - b)$ is equal to that $\left(\frac{(\sqrt{3} + i)(1 + \sqrt{3}i)}{1 + i} \right)$

where a, b, c are two real number and \bar{z} is the complex conjugate o the complex number z , find the locus of z in the Argand diagram. Find the

value of a and b so that locus becomes a circle having its centre at

$$\frac{1}{2}(3 + i)$$

A. (3, 2)

B. (2, 1)

C. (2, 3)

D. (2, 4)

Answer: B



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12. If a complex number z satisfies $|z|^2 + \frac{4}{(|z|)^2} - 2\left(\frac{z}{\bar{z}} + \frac{\bar{z}}{z}\right) - 16 = 0$, then the maximum value of $|z|$ is

A. $\sqrt{6} + 1$

B. 4

C. $2 + \sqrt{6}$

D. 6

Answer: C



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13. If $\cos\alpha + \cos\beta + \cos\gamma = 0 = \sin\alpha + \sin\beta + \sin\gamma$, then $\frac{\sin 3\alpha + \sin 3\beta + \sin 3\gamma}{\sin(\alpha + \beta + \gamma)}$

is equal to

A. 1

B. -1

C. 3

D. -3

Answer: C



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14. The least value of $|z - 3 - 4i|^2 + |z + 2 - 7i|^2 + |z - 5 + 2i|^2$ occurs when

$z =$

A. $1 + 3i$

B. $3 + 3i$

C. $3 + 4i$

D. None of these

Answer: D



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15. The roots of the equation $x^4 - 2x^2 + 4 = 0$ are the vertices of a :

- A. square inscribed in a circle of radius 2
- B. rectangle inscribed in a circle of radius 2
- C. square inscribed in a circle of radius $\sqrt{2}$
- D. rectangle inscribed in a circle of radius $\sqrt{2}$

Answer: D



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16. If z_1, z_2 are complex numbers such that $Re(z_1) = |z_1 - 2|$,

$Re(z_2) = |z_2 - 2|$ and $arg(z_1 - z_2) = \pi/3$, then $Im(z_1 + z_2) =$

- A. $2/\sqrt{3}$
- B. $4/\sqrt{3}$
- C. $2/\sqrt{3}$
- D. $\sqrt{3}$

Answer: B



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17. If $z = e^{\frac{2\pi i}{5}}$, then $1 + z + z^2 + z^3 + 5z^4 + 4z^5 + 4z^6 + 4z^7 + 4z^8 + 5z^9 =$

A. 0

B. $4z^3$

C. $5z^4$

D. $-4z^2$

Answer: C



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18. If $z = (3 + 7i)(a + ib)$, where $a, b \in \mathbb{Z} - \{0\}$, is purely imaginary, then minimum value of $|z|^2$ is

A. 74

B. 45

C. 65

D. 58

Answer: D

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19. Let z be a complex number satisfying $|z + 16| = 4|z + 1|$. Then

A. $|z| = 4$

B. $|z| = 5$

C. $|z| = 6$

D. $3 < |z| < 68$

Answer: A

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20. If $|z| = 1$ and $z' = \frac{1 + z^2}{z}$, then

A. z' lie on a line not passing through origin

B. $|z'| = \sqrt{2}$

C. $\text{Re}(z') = 0$

D. $\text{Im}(z') = 0$

Answer: D



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21. a, b, c are three complex numbers on the unit circle $|z| = 1$, such that $abc = a + b + c$. Then $|ab + bc + ca|$ is equal to

A. 3

B. 6

C. 1

D. 2

Answer: C



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22. If $|z_1| = |z_2| = |z_3| = 1$ then value of $|z_1 - z_3|^2 + |z_3 - z_1|^2 + |z_1 - z_2|^2$ cannot exceed

A. 6

B. 9

C. 12

D. none of these

Answer: B



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23. Number of ordered pairs $(s), (a, b)$ of real numbers such that $(a + ib)^{2008} = a - ib$ holds good is

- A. 2008
- B. 2009
- C. 2010
- D. 1

Answer: C



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24. The region represented by the inequality $|2z-3i| < |3z-2i|$ is

- A. the unit disc with its centre at $z = 0$
- B. the exterior of the unit circle with its centre at $z = 0$
- C. the interior of a square of side 2 units with its centre at $z = 0$
- D. none of these

Answer: B



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25. If ω is any complex number such that $z\omega = |z|^2$ and $|z - \bar{z}| + |\omega + \bar{\omega}| = 4$, then as ω varies, then the area bounded by the locus of z is

A. 4 sq. units

B. 8 sq. units

C. 16 sq. units

D. 12 sq. units

Answer: B



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26. If $az^2 + bz + 1 = 0$, where $a, b \in \mathbb{C}$, $|a| = \frac{1}{2}$ and have a root α such that $|\alpha| = 1$ then $|a\bar{b} - b| =$

A. $1/4$

B. $1/2$

C. $5/4$

D. $3/4$

Answer: D



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27. Let p and q are complex numbers such that $|p| + |q| < 1$. If z_1 and z_2 are the roots of the $z^2 + pz + q = 0$, then which one of the following is correct ?

A. $|z_1| < 1$ and $|z_2| < 1$

B. $|z_1| > 1$ and $|z_2| > 1$

C. If $|z_1| < 1$, then $|z_2| > 1$ and vice versa

D. Nothing definite can be said

Answer: A

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28. If z and w are two complex numbers simultaneously satisfying the equations, $z^3 + w^5 = 0$ and $z^2 + \bar{w}^4 = 1$, then

A. z and w both are purely real

B. z is purely real and w is purely imaginary

C. w is purely real and z is purely imaginary

D. z and w both are imaginary

Answer: A

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29. All complex numbers 'z' which satisfy the relation

$|z - |z + 1|| = |z + |z - 1| |$ on the complex plane lie on the

A. $y = x$

B. $y = -x$

C. circle $x^2 + y^2 = 1$

D. line $x = 0$ or on a line segment joining $(-1, 0) \rightarrow (1, 0)$

Answer: D



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30. If z_1, z_2 are two complex numbers such that $\left| \frac{z_1 - z_2}{z_1 + z_2} \right| = 1$ and

$iz_1 = Kz_2$, where $K \in \mathbb{R}$, then the angle between $z_1 - z_2$ and $z_1 + z_2$ is

A. $\tan^{-1} \left(\frac{2K}{K^2 + 1} \right)$

B. $\tan^{-1} \left(\frac{2K}{1 - K^2} \right)$

C. $-2\tan^{-1}K$

D. $2\tan^{-1}K$

Answer: D



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31. If $z + \frac{1}{z} = 2\cos 6^\circ$, then $z^{1000} + \frac{1}{z^{1000}} + 1$ is equal to

A. 0

B. 1

C. -1

D. 2

Answer: A



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32. Let z_1 and z_2 be two complex numbers with α and β as their principal arguments such that $\alpha + \beta$ then principal $\arg(z_1 z_2)$ is given by:

A. $\alpha + \beta + \pi$

B. $\alpha + \beta - \pi$

C. $\alpha + \beta - 2\pi$

D. $\alpha + \beta$

Answer: C



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33. Let $\arg(z_k) = \frac{(2k+1)\pi}{n}$ where $k = 1, 2, \dots, n$. If $\arg(z_1, z_2, z_3, \dots, z_n) = \pi$, then n must be of form ($m \in \mathbb{Z}$)

A. $4m$

B. $2m - 1$

C. $2m$

D. None of these

Answer: B

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34. Suppose two complex numbers $z = a + ib$, $w = c + id$ satisfy the equation $\frac{z + w}{z} = \frac{w}{z + w}$. Then

- A. both a and c are zeros
- B. both b and d are zeros
- C. both b and d must be non zeros
- D. at least one of b and d is non zero

Answer: D

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35. If $|z| = 1$ and $z \neq \pm 1$, then one of the possible value of $\arg(z) - \arg(z + 1) - \arg(z - 1)$, is

A. $-\pi/6$

B. $\pi/3$

C. $-\pi/2$

D. $\pi/4$

Answer: C



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36. If $\arg(z^{3/8}) = \frac{1}{2}\arg(z^2 + \bar{z}^{1/2})$, then which of the following is not possible ?

A. $|z| = 1$

B. $z = \bar{z}$

C. $\arg(z) = 0$

D. None of these

Answer: D



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37. z_1, z_2 are two distinct points in complex plane such that $2|z_1| = 3|z_2|$

and $z \in C$ be any point $z = \frac{2z_1}{3z_2} + \frac{3z_2}{2z_1}$ such that

A. $-1 \leq \operatorname{Re} z \leq 1$

B. $-2 \leq \operatorname{Re} z \leq 2$

C. $-3 \leq \operatorname{Re} z \leq 3$

D. None of these

Answer: B



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38. If $\alpha, \beta, \gamma \in \{1, \omega, \omega^2\}$ (where ω and ω^2 are imaginary cube roots of unity), then number of triplets (α, β, γ) such that $\left| \frac{a\alpha + b\beta + c\gamma}{a\beta + b\gamma + c\alpha} \right| = 1$ is

- A. 3
- B. 6
- C. 9
- D. 12

Answer: C



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39. The value of $\left(3\sqrt{3} + \left(3^{5/6}\right)i\right)^3$ is (where $i = \sqrt{-1}$)

- A. 24
- B. -24
- C. -22

D. -21

Answer: B



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40. If $\omega \neq 1$ is a cube root of unity and $a + b = 21$, $a^3 + b^3 = 105$, then the value of $(a\omega^2 + b\omega)(a\omega + b\omega^2)$ is be equal to

A. 3

B. 5

C. 7

D. 35

Answer: B



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41. If $z = \frac{1}{2}(\sqrt{3} - i)$, then the least possible integral value of m such that $(z^{101} + i^{109})^{106} = z^{m+1}$ is

A. 11

B. 7

C. 8

D. 9

Answer: D



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42. If $y_1 = \max ||z - \omega| - |z - \omega^2| |$, where $|z| = 2$ and $y_2 = \max ||z - \omega| - |z - \omega^2| |$, where $|z| = \frac{1}{2}$ and ω and ω^2 are complex cube roots of unity, then

A. $y_1 = \sqrt{3}, y_2 = \sqrt{3}$

B. $y_1 < \sqrt{3}, y_2 = \sqrt{3}$

C. $y_1 = \sqrt{3}, y_2 < \sqrt{3}$

D. $y_1 > 3, y_2 < \sqrt{3}$

Answer: C



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43. Let $1, \omega$ and ω^2 be the cube roots of unity. The least possible degree of a polynomial, with real coefficients having $2\omega^2, 3 + 4\omega, 3 + 4\omega^2$ and $5 - \omega - \omega^2$ as roots is -

A. 4

B. 5

C. 6

D. 7

Answer: B



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44. Number of imaginary complex numbers satisfying the equation,
 $z^2 = \bar{z}2^{1-|z|}$ is

A. 0

B. 1

C. 2

D. 3

Answer: C



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45. Least positive argument of the 4th root of the complex number
 $2 - i\sqrt{12}$ is

A. $\pi/6$

B. $5\pi/12$

C. $7\pi/12$

D. $11\pi/12$

Answer: B



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46. A root of unity is a complex number that is a solution to the equation, $z^n = 1$ for some positive integer n . Number of roots of unity that are also the roots of the equation $z^2 + az + b = 0$, for some integer a and b is

A. 6

B. 8

C. 9

D. 10

Answer: B



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47. If z is a complex number satisfying the equation $z^6 + z^3 + 1 = 0$. If this equation has a root $re^{i\theta}$ with $90^\circ < \theta < 180^\circ$ then the value of θ is

A. 100°

B. 110°

C. 160°

D. 170°

Answer: C



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48. Suppose A is a complex number and $n \in \mathbb{N}$, such that $A^n = (A + 1)^n = 1$, then the least value of n is 3 b. 6 c. 9 d. 12

A. 3

B. 6

C. 9

D. 12

Answer: B



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49. If $z_1, z_2, z_3, \dots, z_n$ are in G.P with first term as unity such that $z_1 + z_2 + z_3 + \dots + z_n = 0$. Now if $z_1, z_2, z_3, \dots, z_n$ represents the vertices of n -polygon, then the distance between incentre and circumcentre of the polygon is

A. 0

B. $|z_1|$

C. $2|z_1|$

D. none of these

Answer: A



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50. If $|z - 1 - i| = 1$, then the locus of a point represented by the complex number $5(z - i) - 6$ is

- A. circle with centre $(1, 0)$ and radius 3
- B. circle with centre $(-1, 0)$ and radius 5
- C. line passing through origin
- D. line passing through $(-1, 0)$

Answer: B

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51. Let $z \in C$ and if $A = \left\{ z : \arg(z) = \frac{\pi}{4} \right\}$ and $B = \left\{ z : \arg(z - 3 - 3i) = \frac{2\pi}{3} \right\}$.

Then $n(A \cap B) =$

- A. 1

B. 2

C. 3

D. 0

Answer: D



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52. $\theta \in [0, 2\pi]$ and z_1, z_2, z_3 are three complex numbers such that they are collinear and $(1 + |\sin\theta|)z_1 + (|\cos\theta| - 1)z_2 - \sqrt{2}z_3 = 0$. If at least one of the complex numbers z_1, z_2, z_3 is nonzero, then number of possible values of θ is

A. Infinite

B. 4

C. 2

D. 8

Answer: B



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53. Let ' z ' be a complex number and ' a ' be a real parameter such that $z^2 + az + a^2 = 0$, then which of the following is not true ?

A. locus of z is a pair of straight lines

B. $|z| = |a|$

C. $\arg(z) = \pm \frac{2\pi}{3}$

D. None of these

Answer: D



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54. Let $z = x + iy$ then locus of moving point $P(z) \frac{1 + \bar{z}}{z} \in R$, is

A. union of lines with equations $x = 0$ and $y = -1/2$ but excluding origin.

B. union of lines with equations $x = 0$ and $y = 1/2$ but excluding origin.

C. union of lines with equations $x = -1/2$ and $y = 0$ but excluding origin.

D. union of lines with equations $x = 1/2$ and $y = 0$ but excluding origin.

Answer: C



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55. Let $A(z_1)$ and $B(z_2)$ are two distinct non-real complex numbers in the argand plane such that $\frac{z_1}{z_2} + \frac{\bar{z}_1}{z_2} = 2$. The value of $|\angle ABO|$ is

A. $\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{2}$

D. None of these

Answer: C

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56. Complex numbers z_1 and z_2 satisfy $|z_1| = 2$ and $|z_2| = 3$. If the included angle of their corresponding vectors is 60° , then the value of

$$19 \left| \frac{z_1 - z_2}{z_1 + z_2} \right|^2 \text{ is}$$

A. 5

B. 6

C. 7

D. 8

Answer: C

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57. Let $A(2, 0)$ and $B(z)$ are two points on the circle $|z| = 2$. $M(z')$ is the point on AB . If the point \bar{z}' lies on the median of the triangle OAB where O is origin, then $\arg(z')$ is

A. $\tan^{-1}\left(\frac{\sqrt{15}}{5}\right)$

B. $\tan^{-1}(\sqrt{15})$

C. $\tan^{-1}\left(\frac{5}{\sqrt{15}}\right)$

D. $\frac{\pi}{2}$

Answer: A

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58. If $A(z_1), B(z_2), C(z_3)$ are vertices of a triangle such that $z_3 = \frac{z_2 - iz_1}{1 - i}$ and $|z_1| = 3, |z_2| = 4$ and $|z_2 + iz_1| = |z_1| + |z_2|$, then area of triangle ABC is

A. $\frac{5}{2}$

B. 0

C. $\frac{25}{2}$

D. $\frac{25}{4}$

Answer: D



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59. Let O, A, B be three collinear points such that $OA \cdot OB = 1$. If O and B represent the complex numbers O and z , then A represents

A. $\frac{1}{\bar{z}}$

B. $\frac{1}{z}$

C. \bar{z}

D. z^2

Answer: A

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60. If the tangents at z_1, z_2 on the circle $|z - z_0| = r$ intersect at z_3 , then

$$\frac{(z_3 - z_1)(z_0 - z_2)}{(z_0 - z_1)(z_3 - z_2)} \text{ equals}$$

A. 1

B. -1

C. i

D. $-i$

Answer: B

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61. If z_1, z_2 and z_3 are the vertices of $\triangle ABC$, which is not right angled triangle taken in anti-clock wise direction and z_0 is the circumcentre, then

$\left(\frac{z_0 - z_1}{z_0 - z_2}\right) \frac{\sin 2A}{\sin 2B} + \left(\frac{z_0 - z_3}{z_0 - z_2}\right) \frac{\sin 2C}{\sin 2B}$ is equal to

A. 0

B. 1

C. -1

D. 2

Answer: C



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62. Let P denotes a complex number $z = r(\cos\theta + i\sin\theta)$ on the Argand's plane, and Q denotes a complex number

$\sqrt{2}|z|^2 \left(\cos\left(\theta + \frac{\pi}{4}\right) + i\sin\left(\theta + \frac{\pi}{4}\right) \right)$. If ' O ' is the origin, then ΔOPQ is

A. isosceles but not right angled

B. right angled but not isosceles

C. right isosceles

D. equilateral

Answer: C



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Multiple Correct Answer

1. Complex numbers whose real and imaginary parts x and y are integers and satisfy the equation $3x^2 - |xy| - 2y^2 + 7 = 0$

A. do not exist

B. exist and have equal modulus

C. form two conjugate pairs

D. do not form conjugate pairs

Answer: B::C



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2. If $a, b, c, d \in R$ and all the three roots of $az^3 + bz^2 + cZ + d = 0$ have negative real parts, then

A. $ab > 0$

B. $bc > 0$

C. $ad > 0$

D. $bc - ad > 0$

Answer: A::B::C



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3. Suppose three real numbers a, b, c are in $G. P.$ Let $z = \frac{a + ib}{c - ib}$. Then

A. $z = \frac{ib}{c}$

B. $z = \frac{ia}{b}$

$$C. z = \frac{ia}{c}$$

$$D. z = 0$$

Answer: A::B



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4. w_1, w_2 be roots of $(a + \bar{c})z^2 + (b + \bar{b})z + (\bar{a} + c) = 0$. If $|z_1| < 1$, $|z_2| < 1$, then

A. $|w_1| < 1$

B. $|w_1| = 1$

C. $|w_2| < 1$

D. $|w_2| = 1$

Answer: B::D



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5. A complex number z satisfies the equation $\left|z^2 - 9\right| + \left|z^2\right| = 41$, then the true statements among the following are

- A. $|Z + 3| + |Z - 3| = 10$
- B. $|Z + 3| + |Z - 3| = 8$
- C. Maximum value of $|Z|$ is 5
- D. Maximum value of $|Z|$ is 6

Answer: A:C



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6. Let a, b, c be distinct complex numbers with $|a| = |b| = |c| = 1$ and z_1, z_2 be the roots of the equation $az^2 + bz + c = 0$ with $\left|z_1\right| = 1$. Let P and Q represent the complex numbers z_1 and z_2 in the Argand plane with $\angle POQ = \theta, 0^\circ < 180^\circ$ (where O being the origin). Then

A. $b^2 = ac, \theta = \frac{2\pi}{3}$

$$B. \theta = \frac{2\pi}{3}, PQ = \sqrt{3}$$

$$C. PQ = 2\sqrt{3}, b^2 = ac$$

$$D. \theta = \frac{\pi}{3}, b^2 = ac$$

Answer: A::B



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7. Let $Z_1 = x_1 + iy_1$, $Z_2 = x_2 + iy_2$ be complex numbers in fourth quadrant of argand plane and $|Z_1| = |Z_2| = 1$, $\text{Re}(Z_1 Z_2) = 0$. The complex numbers $Z_3 = x_1 + ix_2$, $Z_4 = y_1 + iy_2$, $Z_5 = x_1 + iy_2$, $Z_6 = x_6 + iy$, will always satisfy

$$A. |Z_4| = 1$$

$$B. \arg(Z_1 Z_4) = -\pi/2$$

$$C. \frac{Z_5}{\cos(\arg Z_1)} + \frac{Z_6}{\sin(\arg Z_1)} \text{ is purely real}$$

$$D. Z_5^2 + (\bar{Z}_6)^2 \text{ is purely imaginary}$$

Answer: A::B::C::D



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8. If the imaginary part of $\frac{z-3}{e^{i\theta}} + \frac{e^{i\theta}}{z-3}$ is zero, then z can lie on

- A. a circle with unit radius
- B. a circle with radius 3 units
- C. a straight line through the point (3, 0)
- D. a parabola with the vertex (3, 0)

Answer: A::C



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9. If α is the fifth root of unity, then :

A. $\left| 1 + \alpha + \alpha^2 + \alpha^3 + \alpha^4 \right| = 0$

$$\text{B. } |1 + \alpha + \alpha^2 + \alpha^3| = 1$$

$$\text{C. } |1 + \alpha + \alpha^2| = 2\cos\frac{\pi}{5}$$

$$\text{D. } |1 + \alpha| = 2\cos\frac{\pi}{10}$$

Answer: A::B::C

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10. If z_1, z_2, z_3 are any three roots of the equation $z^6 = (z + 1)^6$, then

$\arg\left(\frac{z_1 - z_3}{z_2 - z_3}\right)$ can be equal to

A. 0

B. π

C. $\frac{\pi}{4}$

D. $-\frac{\pi}{4}$

Answer: A::B

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11. Let z_1, z_2, z_3 are the vertices of ΔABC , respectively, such that $\frac{z_3 - z_2}{z_1 - z_2}$ is purely imaginary number. A square on side AC is drawn outwardly. $P(z_4)$ is the centre of square, then

A. $|z_1 - z_2| = |z_2 - z_4|$

B. $\arg\left(\frac{z_1 - z_2}{z_4 - z_2}\right) + \arg\left(\frac{z_3 - z_2}{z_4 - z_2}\right) = +\frac{\pi}{2}$

C. $\arg\left(\frac{z_1 - z_2}{z_4 - z_2}\right) + \arg\left(\frac{z_3 - z_2}{z_4 - z_2}\right) = 0$

D. z_1, z_2, z_3 and z_4 lie on a circle

Answer: C::D

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Matching Column

1. z_1, z_2, z_3 are vertices of a triangle. Match the condition in List I with type of triangle in List II.

| List I | | List II | |
|--------|---|---------|--|
| (p) | $z_1^2 + z_2^2 + z_3^2 = z_2z_3 + z_3z_1 + z_1z_2$ | (1) | right angled but not necessarily isosceles |
| (q) | $\operatorname{Re}\left(\frac{z_3 - z_1}{z_3 - z_2}\right) = 0$ | (2) | obtuse angled |
| (r) | $\operatorname{Re}\left(\frac{z_3 - z_1}{z_3 - z_2}\right) < 0$ | (3) | isosceles and right angled |
| (s) | $\frac{z_3 - z_1}{z_3 - z_2} = i$ | (4) | equilateral |

Codes

A. $\begin{matrix} p & q & r & s \\ 3 & 2 & 1 & 4 \end{matrix}$

B. $\begin{matrix} p & q & r & s \\ 1 & 2 & 4 & 3 \end{matrix}$

C. $\begin{matrix} p & q & r & s \\ 4 & 1 & 2 & 3 \end{matrix}$

D. $\begin{matrix} p & q & r & s \\ 2 & 1 & 4 & 3 \end{matrix}$

Answer: C

Comprehension

1. Consider the region R in the Argand plane described by the complex number Z satisfying the inequalities $|Z - 2| \leq |Z - 4|$, $|Z - 3| \leq |Z + 3|$, $|Z - i| \leq |Z - 3i|$, $|Z + i| \leq |Z + 3i|$

Answer the following questions :

The maximum value of $|Z|$ for any Z in R is

A. 5

B. 3

C. 1

D. $\sqrt{13}$

Answer: D

2. Consider the region R in the Argand plane described by the complex number Z satisfying the inequalities $|Z - 2| \leq |Z - 4|$, $|Z - 3| \leq |Z + 3|$, $|Z - i| \leq |Z - 3i|$, $|Z + i| \leq |Z + 3i|$

Answer the following questions :

The maximum value of $|Z|$ for any Z in R is

A. 5

B. 14

C. $\sqrt{13}$

D. 12

Answer: A



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3. Consider the region R in the Argand plane described by the complex number Z satisfying the inequalities $|Z - 2| \leq |Z - 4|$, $|Z - 3| \leq |Z + 3|$, $|Z - i| \leq |Z - 3i|$, $|Z + i| \leq |Z + 3i|$

Answer the following questions :

Minimum of $|Z_1 - Z_2|$ given that Z_1, Z_2 are any two complex numbers lying in the region R is

A. 0

B. 5

C. $\sqrt{13}$

D. 3

Answer: A



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4. Let z_1 and z_2 be complex numbers such that $z_1^2 - 4z_2 = 16 + 20i$ and the roots α and β of $x^2 + z_1x + z_2 + m = 0$ for some complex number m satisfies $|\alpha - \beta| = 2\sqrt{7}$.

The locus of the complex number m is a curve

A. straight line

B. circle

C. ellipse

D. hyperbola

Answer: B



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5. Let z_1 and z_2 be complex numbers such that $z_1^2 - 4z_2 = 16 + 20i$ and the roots α and β of $x^2 + z_1x + z_2 + m = 0$ for some complex number m satisfies $|\alpha - \beta| = 2\sqrt{7}$.

The maximum value of $|m|$ is

A. 14

B. $2\sqrt{7}$

C. $7 + \sqrt{41}$

D. $2\sqrt{6} - 4$

Answer: C



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6. Let z_1 and z_2 be complex numbers such that $z_1^2 - 4z_2 = 16 + 20i$ and the roots α and β of $x^2 + z_1x + z_2 + m = 0$ for some complex number m satisfies $|\alpha - \beta| = 2\sqrt{7}$. The value of $|m|$, when $\arg(m)$ is maximum

A. 7

B. $28 - \sqrt{41}$

C. $\sqrt{41}$

D. $2\sqrt{6} - 4$

Answer: D



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7. The locus of any point $P(z)$ on argand plane is $\arg\left(\frac{z - 5i}{z + 5i}\right) = \frac{\pi}{4}$.

Then the length of the arc described by the locus of $P(z)$ is

A. $10\sqrt{2}\pi$

B. $\frac{15\pi}{\sqrt{2}}$

C. $\frac{5\pi}{\sqrt{2}}$

D. $5\sqrt{2}\pi$

Answer: B



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8. The locus of any point $P(z)$ on argand plane is $\arg\left(\frac{z - 5i}{z + 5i}\right) = \frac{\pi}{4}$.

Total number of integral points inside the region bounded by the locus of $P(z)$ and imaginary axis on the argand plane is

A. 62

B. 74

C. 136

D. 138

Answer: C



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9. The locus of any point $P(z)$ on argand plane is $\arg\left(\frac{z - 5i}{z + 5i}\right) = \frac{\pi}{4}$.

Area of the region bounded by the locus of a complex number Z

satisfying $\arg\left(\frac{z + 5i}{z - 5i}\right) = \pm \frac{\pi}{4}$

A. $75\pi + 50$

B. 75π

C. $\frac{75\pi}{2} + 25$

D. $\frac{75\pi}{2}$

Answer: A



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10. A person walks $2\sqrt{2}$ units away from origin in south west direction ($S45^\circ W$) to reach A , then walks $\sqrt{2}$ units in south east direction ($S45^\circ E$) to reach B . From B he travel is 4 units horizontally towards east to reach C . Then he travels along a circular path with centre at origin through an angle of $2\pi/3$ in anti-clockwise direction to reach his destination D .

Let the complex number Z represents C in argand plane. then $\arg(Z) =$

A. $-\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. $-\frac{\pi}{4}$

D. $\frac{\pi}{3}$

Answer: C

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11. A person walks $2\sqrt{2}$ units away from origin in south west direction ($S45^\circ W$) to reach A , then walks $\sqrt{2}$ units in south east direction ($S45^\circ E$) to reach B . From B he travel is 4 units horizontally towards east to reach C . Then he travels along a circular path with centre at origin through an angle of $2\pi/3$ in anti-clockwise direction to reach his destination D .

Position of D in argand plane is (w is an imaginary cube root of unity)

A. $(3 + i)\omega$

B. $-(1 + i)\omega^2$

C. $3(1 - i)\omega$

D. $(1 - 3i)\omega$

Answer: C

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1. Evaluate :

(i) i^{135}

(ii) $i^{\frac{1}{47}}$

(iii) $(-\sqrt{-1})^{4n+3}, n \in N$

(iv) $\sqrt{-25} + 3\sqrt{-4} + 2\sqrt{-9}$



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2. Find the value of $i^n + i^{n+1} + i^{n+2} + i^{n+3}$ for all $n \in N$.

A. 0

B. i

C. $-i$

D. $2i^n$

Answer: A

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3. Find the value of $1 + i^2 + i^4 + i^6 + \dots + i^{2n}$

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4. Show that the polynomial $x^{4p} + x^{4q+1} + x^{4r+2} + x^{4s+3}$ is divisible by $x^3 + x^2 + x + 1$, where $p, q, r, s \in \mathbb{N}$.

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5. Solve:

$$ix^2 - 3x - 2i = 0,$$

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6. If $z = 4 + i\sqrt{7}$, then find the value of $z^3 - 4z^2 - 9z + 91$.

A. 23

B. i

C. -1

D. 0

Answer: C

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7. Express each of the following in the standard form $a + ib$

(i) $\frac{5 + 4i}{4 + 5i}$ (ii) $\frac{(1 + i)^2}{3 - i}$ (iii) $\frac{1}{1 - \cos\theta + 2i\sin\theta}$

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8. The root of the equation $2(1 + i)x^2 - 4(2 - i)x - 5 - 3i = 0$, where $i = \sqrt{-1}$, which has greater modulus is

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9. Find the value of $(1 + i)^6 + (1 - i)^6$

A. $16i$

B. 0

C. $-16i$

D. 1

Answer: B



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10. If $\left(\frac{1+i}{1-i}\right)^m = 1$, then find the least positive integral value of m .



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11. Prove that the triangle formed by the points 1 , $\frac{1+i}{\sqrt{2}}$, and i as vertices in the Argand diagram is isosceles.

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12. Find the value of θ if $\frac{3 + 2i\sin\theta}{1 - 2i\sin\theta}$ is purely real or purely imaginary.

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13. If the imaginary part of $(2z + 1)/(iz + 1)$ is -2 , then find the locus of the point representing in the complex plane.

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14. If z is a complex number such that $|z - \bar{z}| + |z + \bar{z}| = 4$ then find the area bounded by the locus of z .

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15. If $(x + iy)^5 = p + iq$, then prove that $(y + ix)^5 = q + ip$.

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16. If $z = x + iy$ lies in the third quadrant, then prove that $\frac{\bar{z}}{z}$ also lies in the third quadrant when $y < x < 0$.

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17. Prove that $\left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^5 + \left(\frac{\sqrt{3}}{2} - \frac{i}{2}\right)^5$ is purely real.

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18. Find the relation if z_1, z_2, z_3, z_4 are the affixes of the vertices of a parallelogram taken in order.

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19. Let z_1, z_2, z_3 be three complex numbers and a, b, c be real numbers not all zero, such that $a + b + c = 0$ and $az_1 + bz_2 + cz_3 = 0$. Show that z_1, z_2, z_3 are collinear.

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20. Find real values of x and y for which the complex numbers $-3 + ix^2y$ and $x^2 + y + 4i$ are conjugate of each other.

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21. Given that $x, y \in R$. Solve:
$$\frac{x}{1+2i} + \frac{y}{3+2i} = \frac{5+6i}{8i-1}$$

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22. If $(x + iy)^3 = u + iv$, then show that $\frac{u}{x} + \frac{v}{y} = 4(x^2 - y^2)$.

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23. Let z be a complex number satisfying the equation $z^3 - (3 + i)z + m + 2i = 0$, where $m \in \mathbb{R}$. Suppose the equation has a real root. Then root non-real root.

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24. Show that the equation $Z^4 + 2Z^3 + 3Z^2 + 4Z + 5 = 0$ has no root which is either purely real or purely imaginary.

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25. Find the square roots of the following:

(i) $7 - 24i$ (ii) $5 + 12i$

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26. Find all possible values of $\sqrt{i} + \sqrt{-i}$

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27. Solve the following for z : $z^2 - (3 - 2i)z = (5i - 5)$

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28. Solve the equation $(x - 1)^3 + 8 = 0$ in the set C of all complex numbers.

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29. If n is an odd integer that is greater than or equal to 3 but not a multiple of 3, then prove that $(x + 1)^n - x^n - 1$ is divisible by $x^3 + x^2 + x + 1$.

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30. ω is an imaginary root of unity.

Prove that

$$(i) \left(a + b\omega + c\omega^2\right)^3 + \left(a + b\omega^2 + c\omega\right)^3 = (2a - b - c)(2b - a - c)(2c - a - b)$$

(ii) If $a + b + c = 0$ then prove that

$$\left(a + b\omega + c\omega^2\right)^3 + \left(a + b\omega^2 + c\omega\right)^3 = 27abc.$$

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31. Find the complex number ω satisfying the equation $z^3 - 8i$ and lying in the second quadrant on the complex plane.

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32. $\frac{1}{a + \omega} + \frac{1}{b + \omega} + \frac{1}{c + \omega} + \frac{1}{d + \omega} = \frac{1}{\omega}$ where, $a, b, c, d, \in \mathbb{R}$ and ω is a complex cube root of unity then find the value of $\sum \frac{1}{a^2 - a + 1}$

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33. Write the following complex number in polar form :

(i) $-3\sqrt{2} + 3\sqrt{2}i$

(ii) $1 + i$

(iii) $\frac{1 + 7i}{(2 - i)^2}$



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34. Let $z_1 = \cos 12^\circ + i \sin 12^\circ$ and $z_2 = \cos 48^\circ + i \sin 48^\circ$. Write complex number $(z_1 + z_2)$ in polar form. Find its modulus and argument.



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35. Convert the complex number $z = 1 + \frac{\cos(8\pi)}{5} + i \frac{\sin(8\pi)}{5}$ in polar form. Find its modulus and argument.



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36. Let z and w be two nonzero complex numbers such that

$$|z| = |w| \text{ and } \arg(z) + \arg(w) = \pi$$

Then prove that $z = -w$



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37. Find nonzero integral solutions of $|1 - i|^x = 2^x$



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38. Let z be a complex number satisfying $|z| = 3|z - 1|$. Then prove that

$$\left| z - \frac{9}{8} \right| = \frac{3}{8}$$



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39. If complex number $z = x + iy$ satisfies the equation $\operatorname{Re}(z + 1) = |z - 1|$,

then prove that z lies on $y^2 = 4x$.



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40. Solve the equation $|z| = z + 1 + 2i$



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41. Find the range of real number α for which the equation $z + \alpha|z - 1| + 2i = 0$ has a solution.



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42. Find the Area bounded by complex numbers $\arg|z| \leq \frac{\pi}{4}$ and $|z - 1| < |z - 3|$



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43. Prove that triangle by complex numbers z_1, z_2 and z_3 is equilateral if

$$|z_1| = |z_2| = |z_3| \text{ and } z_1 + z_2 + z_3 = 0$$



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44. Show that $e^{2mi\theta} \left(\frac{icot\theta + 1}{icot\theta - 1} \right)^m = 1$.



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45. $Z_1 \neq Z_2$ are two points in an Argand plane. If $a|Z_1| = b|Z_2|$, then prove that $\frac{aZ_1 - bZ_2}{aZ_1 + bZ_2}$ is purely imaginary.



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46. Find the real part of $(1 - i)^{-i}$.



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47. If $(\sqrt{8} + i)^{50} = 3^{49}(a + ib)$, then find the value of $a^2 + b^2$.

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48. Show that $(x^2 + y^2)^4 = (x^4 - 6x^2y^2 + y^4)^2 + (4x^3y - 4xy^3)^2$

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49. If $\arg(z_1) = 170^\circ$ and $\arg(z_2) = 70^\circ$, then find the principal argument of $z_1 z_2$.

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50. Find the value of expression $\left(\frac{\cos\pi}{2} + is \in \frac{\pi}{2}\right) \left(\frac{\cos\pi}{2^2} + is \in \frac{\pi}{2^2}\right) \rightarrow \infty$

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51. Find the principal argument of the complex number $\frac{(1+i)^5(1+\sqrt{3}i)^2}{-1i(-\sqrt{3}+i)}$

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52. If $z = \frac{(\sqrt{3}+i)^{17}}{(1-i)^{50}}$, then find $\text{amp}(z)$.

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53. If $z = x + iy$ and $w = \frac{1-iz}{z-i}$, show that $|w| = 1$ is purely real.

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54. It is given the complex numbers z_1 and z_2 , $|z_1| = 2$ and $|z_2| = 3$. If the included angle of their corresponding vectors is 60° , then find value of

$$\left| \frac{z_1 + z_2}{z_1 - z_2} \right|$$



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55. Solve the equation $z^3 = \bar{z}$ ($z \neq 0$)



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56. If $2z_1/3z_2$ is a purely imaginary number, then find the value of

$$\left| \frac{z_1 - z_2}{z_1 + z_2} \right|$$



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57. Find the complex number satisfying the system of equations

$$z^3 + \omega^7 = 0 \text{ and } z^5 \omega^{11} = 1.$$



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58. Express the following in $a + ib$ form:

(i) $\left(\frac{\cos\theta + i\sin\theta}{\sin\theta + i\cos\theta}\right)^4$

(ii) $\frac{(\cos 2\theta - i\sin 2\theta)^4(\cos 4\theta + i\sin 4\theta)^{-5}}{(\cos 3\theta + i\sin 3\theta)^{-2}(\cos 3\theta - i\sin 3\theta)^{-9}}$

(iii) $\frac{(\sin\pi/8 + i\cos\pi/8)^8}{(\sin\pi/8 - i\cos\pi/8)^8}$

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59. If $z = \left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^5 + \left(\frac{\sqrt{3}}{2} - \frac{i}{2}\right)^5$, then prove that $\text{Im}(z) = 0$

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60. Prove that the roots of the equation $x^4 - 2x^2 + 4 = 0$ forms a rectangle.

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61. If $z + 1/z = 2\cos\theta$, prove that $\left| \frac{(z^{2n} - 1)}{(z^{2n} + 1)} \right| = |\tan n\theta|$

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62. If $z = x + iy$ is a complex number with $x, y \in \mathbb{Q}$ and $|z| = 1$, then show that $|z^{2n} - 1|$ is a rational number for every $n \in \mathbb{N}$.

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63. If $z = \cos\theta + i\sin\theta$ is a root of the equation $a_0z^n + a_2z^{n-2} + \dots + a_{n-1}z + a_n = 0$, then prove that $a_0 + a_1\cos\theta + a_2\cos^2\theta + \dots + a_n\cos n\theta = 0$ and $a_1\sin\theta + a_2\sin^2\theta + \dots + a_n\sin n\theta = 0$

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64. If $|z_1| = 1$, $|z_2| = 2$, $|z_3| = 3$, and $|9z_1z_2 + 4z_1z_3 + z_2z_3 + 3| = 12$, then find the value of $|z_1 + z_2 + z_3 + 3|$



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65. If α and β are different complex numbers with $|\beta| = 1$, then find $\left| \frac{\beta - \alpha}{1 - \bar{\alpha}\beta} \right|$.



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66. Prove that $|z_1 + z_2|^2 = |z_1|^2$, if z_1/z_2 is purely imaginary.



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67. Let $\left| \frac{z_1 - 2z_2}{2 - z_1z_2} \right| = 1$ and $|z_2| \neq 1$, where z_1 and z_2 are complex numbers. shown that $|z_1| = 2$



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68. If z_1 and z_2 are two complex numbers and $c > 0$, then prove that

$$|z_1 + z_2|^2 \leq (1 + c)|z_1|^2 + (1 + c^{-1})|z_2|^2$$

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69. If z_1, z_2, z_3, z_4 are the affixes of four points in the Argand plane, z is the affix of a point such that $|z - z_1| = |z - z_2| = |z - z_3| = |z - z_4|$, then prove that z_1, z_2, z_3, z_4 are concyclic.

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70. If $|z_1 + z_2| = |z_1| + |z_2|$, then prove that $\arg(z_1) = \arg(z_2)$ if $|z_1 - z_2| = |z_1| + |z_2|$, then prove that $\arg(z_1) = \arg(z_2) = \pi$

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71. Show that the area of the triangle on the Argand diagram formed by the complex number z , iz and $z + iz$ is $\frac{1}{2}|z|^2$

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72. Find the minimum value of $|z - 1|$ if $||z - 3| - |z + 1|| = 2$.

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73. Find the greatest and the least value of $|z_1 + z_2|$ if $z_1 = 24 + 7i$ and $|z_2| = 6$.

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74. If z is a complex number, then find the minimum value of $|z| + |z - 1| + |2z - 3|$.

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75. If $|z_1 - 1| \leq 1$, $|z_2 - 2| \leq 2$, $|z_3| \leq 3$, then find the greatest value of $|z_1 + z_2 + z_3|$.

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76. Prove that following inequalities:

(i) $\left| \frac{z}{|z|} - 1 \right| \leq |\arg z|$ (ii) $|z - 1| \leq |z| |\arg z| + |z| - 1$

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77. Identify the locus of z if $z = a + \frac{r^2}{z - a}$, $r > 0$.

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78. If z is any complex number such that $|3z - 2| + |3z + 2| = 4$, then identify the locus of z .

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79. If $|z| = 1$ and let $\omega = \frac{(1 - z)^2}{1 - z^2}$, then prove that the locus of ω is equivalent to $|z - 2| = |z + 2|$.

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80. Let z be a complex number having the argument $\theta, 0$

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81. How many solutions the system of equations $||z + 4| - |z - 3i|| = 5$ and $|z| = 4$ has?

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82. Prove that $|z - z_1|^2 + |z - z_2|^2 = a$ will represent a real circle [with center $(\frac{|z_1 + z_2|^2}{2} +)$] on the Argand plane if $2a \geq |z_1 - z_1|^2$

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83. If $|z - 2 - 3i|^2 + |z - 5 - 7i|^2 = \lambda$ represents the equation of circle with least radius, then find the value of λ .

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84. If $\frac{|2z - 3|}{|z - i|} = k$ is the equation of circle with complex number 'i' lying inside the circle, find the values of K.

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85. Find the point of intersection of the curves

$$\arg(z - 3i) = \frac{3\pi}{4} \text{ and } \arg(2z + 1 - 2i) = \pi/4.$$

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86. If complex numbers z_1, z_2 and z_3 are such that $|z_1| = |z_2| = |z_3|$, then

prove that $\arg\left(\frac{z_2}{z_1}\right) = \arg\left(\frac{z_2 - z_3}{z_1 - z_3}\right)^2$

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87. If the triangle formed by complex numbers z_1, z_2 and z_3 is equilateral

then prove that $\frac{z_2 + z_3 - 2z_1}{z_3 - z_2}$ is purely imaginary number

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88. Show that the equation of a circle passing through the origin and having intercepts a and b on real and imaginary axis, respectively, on the

argand plane is $\operatorname{Re}\left(\frac{z-a}{z-ib}\right) = 0$



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89. The triangle formed by $A(z_1)$, $B(z_2)$ and $C(z_3)$ has its circumcentre at origin. If the perpendicular from A to BC intersects the circumference at z_4 then the value of $z_1z_4 + z_2z_3$ is



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90. Let vertices of an acute-angled triangle be $A(z_1)$, $B(z_2)$, and $C(z_3)$. If the origin O is the orthocentre of the triangle, then prove that

$$z_1(z_2)_2 + (z_1)_2z_2 = z_2(z_3)_3 + (z_2)_3z_3 = z_3(z_1)_1 + (z_3)_1z_1$$



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91. If z_1, z_2, z_3 are three complex numbers such that $5z_1 - 13z_2 + 8z_3 = 0$,

then prove that $\left| \frac{z_1(z_2 - z_3)}{z_2(z_3 - z_1)} \right| = 0$

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92. If $z = z_0 + A(z - z_0)$, where A is a constant, then prove that locus of z is a straight line.

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93. z_1 and z_2 are the roots of $3z^2 + 3z + b = 0$. If $O(0), (z_1), (z_2)$ form an equilateral triangle, then find the value of b .

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94. Let z_1, z_2 and z_3 be three complex number such that

$$|z_1 - 1| = |z_2 - 1| = |z_3 - 1| \text{ and } \arg\left(\frac{z_3 - z_1}{z_2 - z_1}\right) = \frac{\pi}{6}$$

then prove that $z_2^3 + z_3^3 + 1 = z_2 + z_3 + z_2z_3$.



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95. Let the complex numbers z_1, z_2 and z_3 be the vertices of an equilateral triangle. If z_0 is the circumcentre of the triangle, then prove that $z_1^2 + z_2^2 + z_3^2 = 3z_0^2$.



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96. In the Argands plane what is the locus of $z (\neq 1)$ such that

$$\arg\left\{\frac{3}{2}\left(\frac{2z^2 - 5z + 3}{2z^2 - z - 2}\right)\right\} = \frac{2\pi}{3}$$



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97. If $\left(\frac{3-z_1}{2-z_1}\right)\left(\frac{2-z_2}{3-z_2}\right) = k(k > 0)$, then prove that points $A(z_1)$, $B(z_2)$, $C(3)$, and $D(2)$ (taken in clockwise sense) are concyclic.

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98. If z_1, z_2, z_3 are complex numbers such that $\left(2/z_1\right) = \left(1/z_2\right) + \left(1/z_3\right)$, then show that the points represented by z_1, z_2, z_3 lie on a circle passing through the origin.

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99. $A(z_1), B(z_2), C(z_3)$ are the vertices of the triangle ABC (in anticlockwise). If $\angle ABC = \pi/4$ and $AB = \sqrt{2}(BC)$, then prove that $z_2 = z_3 + i(z_1 - z_3)$

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100. If one of the vertices of the square circumscribing the circle

$|z - 1| = \sqrt{2}$ is $2 + \sqrt{3}i$. Find the other vertices of square



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101. Let $z_1 = 10 + 6i$ and $z_2 = 4 + 6i$. If z is any complex number such that

the argument of $\frac{(z - z_1)}{(z - z_2)}$ is $\frac{\pi}{4}$, then prove that $|z - 7 - 9i| = 3\sqrt{2}$.



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102. Complex numbers of z_1, z_2, z_3 are the vertices A, B, C respectively, of

an isosceles right-angled triangle with right angle at C. show that

$$(z_1 - z_2)^2 = 2(z_1 - z_3)(z_3 - z_2)$$



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103. Let z_1, z_2 and z_3 represent the vertices $A, B,$ and C of the triangle ABC , respectively, in the Argand plane, such that $|z_1| = |z_2| = 5$. Prove that $z_1 \sin 2A + z_2 \sin 2B + z_3 \sin 2C = 0$.

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104. If $a = \cos(2\pi/7) + is \in (2\pi/7)$, then find the quadratic equation whose roots are $\alpha = a + a^2 + a^4$ and $\beta = a^3 + a^5 + a^7$.

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105. If ω is an imaginary fifth root of unity, then find the value of $\log_2 \left| 1 + \omega + \omega^2 + \omega^3 - 1/\omega \right|$.

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106. If $1, \alpha_1, \alpha_2, \alpha_3, \dots, \alpha_8$ are ninth roots of unity (taken in counter-clockwise sequence in the Argand plane). Then find the value of $|(2 - \alpha_1)(2 - \alpha_3)(2 - \alpha_5)(2 - \alpha_7)|$.



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107. find the sum of squares of all roots of the equation.

$$x^8 - x^7 + x^6 - x^5 + x^4 - x^3 + x^2 - x + 1 = 0$$



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108. Find roots of the equation $(z + 1)^5 = (z - 1)^5$.



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109. If the roots of $(z - 1)^n = i(z + 1)^n$ are plotted in the Argand plane, then prove that they are collinear.

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110. Let $1, z_1, z_2, z_3, \dots, z_{n-1}$ be the n th roots of unity. Then prove that

$$(1 - z_1)(1 - z_2) \dots (1 - z_{n-1}) = n. \quad \text{Also, deduce that}$$

$$\sin \frac{\pi}{n} \sin \frac{2\pi}{n} \sin \frac{3\pi}{n} \dots \sin \frac{(n-1)\pi}{n} = \frac{\pi}{2^{n-1}}$$

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111. if ω and ω^2 are the nonreal cube roots of unity and

$$[1/(a + \omega)] + [1/(b + \omega)] + [1/(c + \omega)] = 2\omega^2 \quad \text{and}$$

$$[1/(a + \omega)^2] + [1/(b + \omega)^2] + [1/(c + \omega)^2] = 2\omega, \text{ then find the value of}$$

$$[1/(a + 1)] + [1/(b + 1)] + [1/(c + 1)]$$

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112. If z_1 and z_2 are complex numbers and $u = \sqrt{z_1 z_2}$, then prove that

$$|z_1| + |z_2| = \left| \frac{z_1 + z_2}{2} + u \right| + \left| \frac{z_1 + z_2}{2} - u \right|$$



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113. If a is a complex number such that $|a| = 1$, then find the value of a , so that equation $az^2 + z + 1 = 0$ has one purely imaginary root.



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114. Let z and z_0 be two complex numbers. It is given that $|z| = 1$ and that numbers $z, z_0, z\bar{z}_0$, and 1 are represented in an Argand diagram by the points P, P_0, Q, A and the origin respectively. Show that the triangles POP_0 and AOQ are congruent. Hence, or otherwise, prove that

$$|z - z_0| = |z\bar{z}_0 - 1|$$



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115. Let a, b , and c be any three nonzero complex numbers. If $|z| = 1$ and z' satisfies the equation $az^2 + bz + c = 0$, prove that

$$aa = cc \text{ and } |a||b| = \sqrt{ac(b)^2}$$

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116. Let x_1, x_2 are the roots of the quadratic equation $x^2 + ax + b = 0$, where a, b , are complex numbers and y_1, y_2 are the roots of the quadratic equation $y^2 + |a|y + |b| = 0$. If $|x_1| = |x_2| = 1$, then prove that $|y_1| = |y_2| = 1$

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117. If $\alpha = (z - i)/(z + i)$ show that, when z lies above the real axis, α will lie within the unit circle which has centre at the origin. Find the locus of α as z travels on the real axis from $-\infty$ to $+\infty$

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118. If $|z| \leq 1$ and $|w| < 1$, then shown that

$$|z - w|^2 < (|z| - |w|)^2 + (\arg z - \arg w)^2$$

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119. Prove that the distance of the roots of the equation

$$|\sin\theta_1|z^3 + |\sin\theta_2|z^2 + |\sin\theta_3|z + |\sin\theta_4| = 3\sin\theta_4 = 0 \text{ is greater than } 2/3.$$

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120. If $|z - (4 + 3i)| = 1$, then find the complex number z for each of the following cases:

(i) $|z|$ is least

(ii) $|z|$ is greatest

(iii) $\arg(z)$ is least

(iv) $\arg(z)$ is greatest

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121. If a, b, c , and u, v, w are complex numbers representing the vertices of two triangles such that they are similar, then prove that $\frac{a - c}{a - b} = \frac{u - w}{u - v}$

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122. Let z_1 and z_2 be the roots of the equation $z^2 + pz + q = 0$ where the coefficient p and q may be complex numbers. Let A and B represent z_1 and z_2 in the complex plane. If $\angle AOB = \alpha \neq 0$ and $OA = OB$, where O is the origin, prove that

$$p^2 = 4q \cos^2\left(\frac{\alpha}{2}\right)$$

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123. The altitudes from the vertices A, B and C of the triangle ABC meet its circumcircle at D, E and F , respectively. The complex numbers representing the points D, E , and F are z_1, z_2 and z_3 , respectively. If $(z_3 - z_1)/(z_2 - z_1)$ is purely real, then show that triangle ABC is right-angled at A .

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124. Let A,B, C,D be four concyclic points in order in which $AD:AB=CD: CB$. If A,B,C are representing by complex numbers a,b,c respectively find the complex number associated with point D.

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125. If $n \geq 3$ and $\alpha_1, \alpha_2, \dots, \alpha_{n-1}$ are nth roots of unity , then find the sum $\sum_{1 \leq i < j \leq n-1} \alpha_i \alpha_j$

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Exercise 3.1

1. Is the following computation correct? If not give the correct

computation:
$$\left[\sqrt{-2} \sqrt{-3} \right] = \sqrt{(-2) \cdot (-3)} = \sqrt{6}$$



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2. Find the value of $\frac{i^{592} + i^{590} + i^{588} + i^{586} + i^{584}}{i^{582} + i^{580} + i^{578} + i^{576} + i^{574}} - 1$

A. -2

B. 0

C. 2

D. -1

Answer: A



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3. The value of $i^{1+3+5+\dots+(2n+1)}$ is, If n is odd.

A. i

B. 1

C. -1

D. $-i$

Answer: B



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4. Find the value of $x^4 + 9x^3 + 35x^2 - x + 4$ for $x = -5 + 2\sqrt{-4}$.



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Exercise 3.2

1. प्रश्न 11 से 13 तक कि सम्मिश्र संख्याओं में प्रत्येक का गुणात्मक प्रतिलोम ज्ञात कीजिए ।

$4 - 3i$



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2. Express the following complex numbers in $a + ib$ form: $\frac{(3 - 2i)(2 + 3i)}{(1 + 2i)(2 - i)}$

(ii) $\frac{2 - \sqrt{-25}}{1 - \sqrt{-16}}$



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3. Find the least positive integer n such that $\left(\frac{2i}{1+i}\right)^n$ is a positive integer.

A. $n = 6$

B. $n = 5$

C. $n = 8$

D. $n = 4$

Answer: C



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4. If one root of the equation $z^2 - az + a - 1 = 0$ is $(1 + i)$, where a is a complex number then find the root.

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5. Prove that quadrilateral formed by the complex numbers which are roots of the equation $z^4 - z^3 + 2z^2 - z + 1 = 0$ is an equilateral trapezium.

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6. If Z^5 is a non-real complex number, then find the minimum value of $\frac{\text{Im}z^5}{\text{Im}^5z}$

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7. Find the real numbers x and y , if $(x - iy)(3 + 5i)$ is the conjugate of $-6 - 24i$

A. $x = -2, y = 2$

B. $x = -3, y = 3$

C. $x = 3, y = -3$

D. $x = -4, y = 1$

Answer: C

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8. If z_1, z_2, z_3 are three nonzero complex numbers such that $z_3 = (1 - \lambda)z_1 + \lambda z_2$ where $\lambda \in \mathbb{R} - \{0\}$, then prove that points corresponding to z_1, z_2 and z_3 are collinear.

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9. If n_1, n_2 are positive integers, then $(1 + i)^{n_1} + (1 + i^3)^{n_1} + (1 + i^5)^{n_2} + (1 + i^7)^{n_2}$ is real if and only if :

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Exercise 3.3

1. If $(a + b) - i(3a + 2b) = 5 + 2i$, then find a and b

A. $a = 12, b = -17$

B. $a = -12, b = -17$

C. $a = 12, b = 17$

D. $a = -12, b = 17$

Answer: D

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2. Find all non zero complex numbers z satisfying $\bar{z} = iz^2$

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3. If a, b, c are nonzero real numbers and $az^2 = bz + c + i = 0$ has purely imaginary roots, then prove that $a = b^2$.

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4. If the sum of square of roots of equation $x^2 + (p + iq)x + 3i = 0$ is 8, then find $|p| + |q|$, where p and q are real.

A. 3

B. 1

C. 4

D. 2

Answer: C

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5. Find the square root $9 + 40i$.



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6. Simplify: $\frac{\sqrt{5+12i} + \sqrt{5-12i}}{\sqrt{5+12i} - \sqrt{5-12i}}$



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7. If $\sqrt{x+iy} = \pm(a+ib)$, then find $\sqrt{x-iy}$.



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Exercise 3.4

1. if α and β are imaginary cube root of unity then prove

$$(\alpha)^4 + (\beta)^4 + (\alpha)^{-1} \cdot (\beta)^{-1} = 0$$



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2. If ω is a complex cube roots of unity, then find the value of the $(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^8) \dots$ to $2n$ factors.

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3. Write the complex number in $a + ib$ form using cube roots of unity: (a)

$$\left(-\frac{1}{2} + \frac{\sqrt{3}}{2}i\right)^{1000} \quad \text{(b) If } z = \frac{(\sqrt{3} + i)^{17}}{(1 - i)^{50}} \quad \text{(c) } (i + \sqrt{3})^{100} + (i + \sqrt{3})^{100} + 2^{100}$$

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4. If $z + z^{-1} = 1$, then find the value of $z^{100} + z^{-100}$.

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5. Find the common roots of $x^{12} - 1 = 0$ and $x^4 + x^2 + 1 = 0$

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6. if α, β, γ are the roots of $x^3 - 3x^2 + 3x + 7 = 0$ then $\frac{\alpha - 1}{\beta - 1} + \frac{\beta - 1}{\gamma - 1} + \frac{\gamma - 1}{\alpha - 1}$

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7. Prove that $t^2 + 3t + 3$ is a factor of $(t + 1)^{n+1} + (t + 2)^{2n-1}$ for all intergral values of $n \in \mathbb{N}$.

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Exercise 3.5

1. Find the pricipal argument of each of the following:

(a) $-1 - i\sqrt{3}$

(b) $\frac{1 + \sqrt{3}i}{3 + i}$

(c) $\sin\alpha + i(1 - \cos\alpha), 0 > \alpha > \pi$

(d) $(1 + i\sqrt{3})^2$

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2. Find the modulus, argument, and the principal argument of the complex numbers. (i) $(\tan 1 - i)^2$

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3. If $\frac{3\pi}{2} < \alpha < 2\pi$, find the modulus and argument of $(1 - \cos 2\alpha) + i \sin 2\alpha$.

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4. Find the principal argument of the complex number

$$\frac{\sin(6\pi)}{5} + i \left(1 + \frac{\cos(6\pi)}{5} \right)$$

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5. If $z = re^{i\theta}$, then prove that $|e^{iz}| = e^{-rs \int h\eta}$.

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6. Find the complex number z satisfying $\operatorname{Re}(z^2) = 0, |z| = \sqrt{3}$.

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7. If $|z - i\operatorname{Re}(z)| = |z - \operatorname{Im}(z)|$, then prove that z , lies on the bisectors of the quadrants.

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8. Find the locus of the points representing the complex number z for which $|z + 5|^2 = |z - 5|^2 = 10$.

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9. Solve : $z^2 + |z| = 0$.

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10. Let $z = x + iy$ be a complex number, where x and y are real numbers. Let A and B be the sets defined by $A = \{z: |z| \leq 2\}$ and $B = \{z: (1 - i)z + (1 + i)\bar{z} \geq 4\}$. Find the area of region $A \cup B$.

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11. Real part of $(e^e)^{i\theta}$ is

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12. Prove that $z = i^i$, where $i = \sqrt{-1}$, is purely real.

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1. For $z_1 = \sqrt[6]{(1-i)/(1+i\sqrt{3})}$, $z_2 = \sqrt[6]{(1-i)/(\sqrt{3}+i)}$,
 $z_3 = \sqrt[6]{(1+i)/(\sqrt{3}-i)}$, prove that $|z_1| = |z_2| = |z_3|$

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2. If $\sqrt{3} + i = (a + ib)/(c + id)$, then find the value of $\tan^{-1}(b/a)\tan^{-1}(d/c)$

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3. If z_1, z_2 and z_3, z_4 are two pairs of conjugate complex numbers then

$$\arg\left(\frac{z_1}{z_4}\right) + \arg\left(\frac{z_2}{z_3}\right) =$$

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4. Find the modulus, argument, and the principal argument of the complex numbers. $(\tan 1 - i)^2 \frac{i - 1}{i \left(1 - \frac{\cos(2\pi)}{5}\right) + s} \in n \frac{2\pi}{5}$

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5. If $(1 + i)(1 + 2i)(1 + 3i) \dots (1 + ni) = x + iy$, then show that

$$2 \times 5 \times 10 \times \dots \times (1 + n^2) = x^2 + y^2$$

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6. If $a + ib = \frac{(x + i)^2}{2x + 1}$, prove that $a^2 + b^2 = \frac{(x + i)^2}{(2x + 1)^2}$

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7. Let z be a complex number satisfying the equation $(z^3 + 3)^2 = -16$,

then find the value of $|z|$.



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8. If θ is real and z_1, z_2 are connected by $z_1^2 + z_2^2 + 2z_1z_2\cos\theta = 0$, then prove that the triangle formed by vertices O, z_1 and z_2 is isosceles.



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9. If $|z_1 - z_0| = |z_2 - z_1| = \pi/2$, then find z_0



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10. Show that $\left| \frac{z-2}{z-3} \right| = 2$ represents a circle. Find its centre and radius.



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1. Express the following in $a + ib$ form: (a) $\frac{(\cos\alpha + i\sin\alpha)^4}{(\sin\beta + i\cos\beta)^5}$ (b)

$$\left(\frac{1 + \cos\phi + i\sin\phi}{1 + \cos\phi - i\sin\phi}\right)^n \quad \text{(c)} \quad \frac{(\cos\alpha + i\sin\alpha)(\cos\beta + i\sin\beta)}{(\cos\gamma + i\sin\gamma)(\cos\delta + i\sin\delta)}$$

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2. Find the value of following expression: $\left[\frac{1 - \frac{\cos\pi}{10} + i\frac{\sin\pi}{10}}{1 - \frac{\cos\pi}{10} - i\frac{\sin\pi}{10}} \right]^{10}$

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3. If $iz^4 + 1 = 0$, then prove that z can take the value $\cos\pi/8 + is \in \pi/8$.

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4. Prove that (a) $(1 + i)^n + (1 - i)^n = 2^{\frac{n+2}{2}} \cdot \cos\left(\frac{n\pi}{4}\right)$, where n is a positive integer. (b) $(1 + i\sqrt{3})^n + (1 - i\sqrt{3})^n = 2^{n+1} \cos\left(\frac{n\pi}{3}\right)$, where n is a positive integer

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5. If $z = (a + ib)^5 + (b + ia)^5$, then prove that $Re(z) = Im(z)$, where $a, b \in R$

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6. If $\cos \alpha + \cos \beta + \cos \gamma = 0$ and also $\sin \alpha + \sin \beta + \sin \gamma = 0$, then prove that.

(a) $\cos 2\alpha + \cos 2\beta + \cos 2\gamma = \sin 2\alpha + \sin 2\beta + \sin 2\gamma = 0$ (b)

$\sin 3\alpha + \sin 3\beta + \sin 3\gamma = 3\sin(\alpha + \beta + \gamma)$ (c)

$\cos 3\alpha + \cos 3\beta + \cos 3\gamma = 3\cos(\alpha + \beta + \gamma)$

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Exercise 3.8

1. a, b, c are three complex numbers on the unit circle $|z| = 1$, such that $abc = a + b + c$. Then find the value of $|ab + bc + ca|$.

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2. Let z be not a real number such that $(1 + z + z^2)/(1 - z + z^2) \in \mathbb{R}$, then prove that $|z| = 1$.

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3. If z_1, z_2, z_3 are distinct nonzero complex numbers and $a, b, c \in \mathbb{R}^+$ such

that $\frac{a}{|z_1 - z_2|} = \frac{b}{|z_2 - z_3|} = \frac{c}{|z_3 - z_1|}$. Then find the value of $\frac{a^2}{|z_1 - z_2|} + \frac{b^2}{|z_2 - z_3|} + \frac{c^2}{|z_3 - z_1|}$.

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4. If z_1 and z_2 are two complex numbers such that $|z_1| < 1 < |z_2|$, then prove that $\left| \frac{(1 - z_1 \bar{z}_2)}{(z_1 - z_2)} \right| < 1$

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5. if $|z_1 + z_2| = |z_1| + |z_2|$, then prove that $\arg(z_1) = \arg(z_2)$ if $|z_1 - z_2| = |z_1| + |z_2|$, then prove that $\arg(z_1) = \arg(z_2) = \pi$

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6. For any complex number z , find the minimum value of $|z| + |z - 2i|$

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7. If z is any complex number such that $|z + 4| \leq 3$, then find the greatest value of $|z + 1|$

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8. $Z \in \mathbb{C}$ satisfies the condition $|Z| > 3$. Then find the least value of

$$\left| Z + \frac{1}{Z} \right|$$

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9. If a, b, c are nonzero complex numbers of equal moduli and satisfy

$az^2 + bz + c = 0$, then prove that $(\sqrt{5} - 1)/2 \leq |z| \leq (\sqrt{5} + 1)/2$.

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10. If $|z| \leq 4$ then find the maximum value of $|iz + 3 - 4i|$

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11. Let $z_1, z_2, z_3, \dots, z_n$ be the complex numbers such that

$$|z_1| = |z_2| = \dots = |z_n| = 1. \text{ It bgt If } z = \left(\sum_{k=1}^n z_k \right) \left(\sum_{k=1}^n \frac{1}{z_k} \right) \text{ then prove}$$

that (a) z is a real number (b) $0 < z \leq n^2$

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Exercise 3.9

1. If $\omega = z/[z - (1/3)i]$ and $|\omega| = 1$, then find the locus of z .

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2. If $\text{Im} \left(\frac{z-1}{e^{\theta i}} + \frac{e^{\theta i}}{z-1} \right) = 0$, then find the locus of z .

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3. For three non-colliner complex numbers Z, Z_1 and Z_2 prove that

$$\left| Z - \frac{Z_1 + Z_2}{2} \right|^2 + \left| \frac{Z_1 - Z_2}{2} \right|^2 = \frac{1}{2} |Z - Z_1|^2 + \frac{1}{2} |Z - Z_2|^2$$

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4. If $|z - 1| + |z + 3| \leq 8$, then prove that z lies on the circle.

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5. If $z = \frac{3}{2 + \cos\theta + i\sin\theta}$, then prove that z lies on the circle.

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6. How many solutions system of equations,
 $\arg(z + 3 - 2i) = -\pi/4$ and $|z + 4| - |z - 3i| = 5$ has ?

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7. Prove that equation of perpendicular bisector of line segment joining complex numbers z_1 and z_2 is $z(\bar{z}_2 - \bar{z}_1) + \bar{z}(z_2 + z_1) + |z_1|^2 - |z_2|^2 = 0$

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8. If complex number z lies on the curve $|z - (-1 + i)| = 1$, then find the locus of the complex number $w = \frac{z + i}{1 - i}$, $i = \sqrt{-1}$.

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Exercise 3.10

1. If z_1, z_2, z_3 and z_4 taken in order vertices of a rhombus, then proves that

$$\operatorname{Re} \left(\frac{z_3 - z_1}{z_4 - z_2} \right) = 0$$

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2. Find the locus of point z if $z, i, \text{ and } iz$, are collinear.

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3. If $|z| = 2$ and $\frac{z_1 - z_3}{z_2 - z_3} = \frac{z - 2}{z + 3}$, then prove that z_1, z_2, z_3 are vertices of a right angled triangle.

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4. Three vertices of triangle are complex number α, β and γ . Then prove that the perpendicular from the point α to opposite side is given by the equation $\operatorname{Re}\left(\frac{z - \alpha}{\beta - \gamma}\right) = 0$ where z is complex number of any point on the perpendicular.

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5. Prove that the complex numbers z_1, z_2 and the origin form an equilateral triangle only if $z_1^2 + z_2^2 - z_1z_2 = 0$.

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6. The center of a regular polygon of n sides is located at the point $z=0$, and one of its vertex z_1 is known. If z_2 be the vertex adjacent to z_1 , then z_2 is equal to

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7. If one vertices of the triangle having maximum area that can be inscribed in the circle $|z - i| = 5$ is $3-3i$, then find the other vertices of the triangle.

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8. Consider the circle $|z|=r$ in the Argand plane, which is in fact the incircle of triangle ABC. If contact points opposite to the vertices A,B,C are $A_1(z_1)$, $B_1(z_2)$ and $C_1(z_3)$, obtain the complex numbers associated with the vertices A,B,C in terms of z_1, z_2 and z_3 .

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9. P is a point on the argand diagram on the circle with OP as diameter two points taken such that $\angle POQ = \angle QOR = \theta$ If O is the origin and P, Q, R are represented by complex z_1, z_2, z_3 respectively then show that $z_2^2 \cos 2\theta = z_1 z_3 \cos^2 \theta$

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10. The center of the arc represented by $\arg \left[\frac{z - 3i}{z - 2i + 4} \right] = \frac{\pi}{4}$

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Exercise 3.11

1. If α is complex fifth root of unity and $(1 + \alpha + \alpha^2 + \alpha^3)^{2005} = p + q\alpha + r\alpha^2 + s\alpha^3$ (where p, q, r, s are real), then find the value of $p + q + r + s$.

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2. Find the number of roots of the equation $z^{15} = 1$ satisfying $|\arg z| < \pi/2$.

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3. If z is nonreal root of $[-1]^{1/7}$ then, find the value of $z^{86} + z^{175} + z^{289}$

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4. Given α, β , respectively, the fifth and the fourth non-real roots of unity, then find the value of $(1 + \alpha)(1 + \beta)(1 + \alpha^2)(1 + \beta^2)(1 + \alpha^4)(1 + \beta^4)$

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5. If the six roots of $x^6 = -64$ are written in the form $a + ib$, where a and b are real, then the product of those roots for which $a < 0$ is

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6. If $z_r: r = 1, 2, 3, \dots, 50$ are the roots of the equation $\sum_{r=0}^{50} z^r = 0$, then find

the value of $\sum_{r=1}^{50} 1/(z_r - 1)$

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Exercise (Single)

1. If $a < 0, b > 0$, then $\sqrt{-a}\sqrt{b}$ equal to

A. $-\sqrt{|a|b}$

B. $\sqrt{|a|b} i$

C. $\sqrt{|a|b}$

D. none of these

Answer: B



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2. Consider the equation $10z^2 - 3iz - k = 0$, where z is a following complex variable and $i^2 = -1$. Which of the following statements is true? For real complex numbers k , both roots are purely imaginary. For all complex numbers k , neither both roots is real. For all purely imaginary numbers k , both roots are real and irrational. For real negative numbers k , both roots are purely imaginary.

A. For real positive numbers k , both roots are purely imaginary

B. For all complex numbers k , neither root is real .

C. For real negative numbers k , both roots are real and irrational .

D. For real negative numbers k , both roots are purely imaginary.

Answer: D



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3. The number of solutions of the equation $z^2 + z = 0$ where z is a complex number, is

A. 1

B. 2

C. 3

D. 4

Answer: D



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4. If center of a regular hexagon is at the origin and one of the vertices on the Argand diagram is $1 + 2i$, then its perimeter is $2\sqrt{5}$ b. $6\sqrt{2}$ c. $4\sqrt{5}$ d. $6\sqrt{5}$

A. $2\sqrt{5}$

B. $6\sqrt{5}$

C. $4\sqrt{5}$

D. $6\sqrt{5}$

Answer: D



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5. If x and y are complex numbers, then the system of equations $(1 + i)x + (1 - i)y = 1$, $2ix + 2y = 1 + i$ has

A. unique solution

B. no solution

C. infinite number of solutions

D. none of these

Answer: C



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6. The point $z_1 = 3 + \sqrt{3}i$ and $z_2 = 2\sqrt{3} + 6i$ are given on the complex plane. The complex number lying on the bisector of the angle formed by the vectors z_1 and z_2 is

A. $z = \frac{(3 + 2\sqrt{3})}{2} + \frac{\sqrt{3} + 2}{2}i$

B. $z = 5 + 5i$

C. $z = -1 - i$

D. none of these

Answer: B



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7. The polynomial $x^6 + 4x^5 + 3x^4 + 2x^3 + x + 1$ is divisible by _____ where w is the cube root of unity $x + \omega$ b. $x + \omega^2$ c. $(x + \omega)(x + \omega^2)$ d. $(x - \omega)(x - \omega^2)$ where ω is one of the imaginary cube roots of unity.

A. $x + \omega$

B. $x + \omega^2$

C. $(x + \omega)(x + \omega^2)$

D. $(x + \omega)(x - \omega^2)$

Answer: D



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8. Dividing $f(z)$ by $z - i$, we obtain the remainder i and dividing it by $z + i$, we get the remainder $1 + i$, then remainder upon the division of $f(z)$ by $z^2 + 1$ is

A. $\frac{1}{2}(z + 1) + i$

B. $\frac{1}{2}(iz + 1) + i$

C. $\frac{1}{2}(iz - 1) + i$

D. $\frac{1}{2}(z + i) + 1$

Answer: B



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9. The complex number $\sin(x) + i\cos(2x)$ and $\cos(x) - i\sin(2x)$ are conjugate to each other for

A. $x = n\pi, n \in Z$

B. $x = 0$

C. $x = (n + 1/2)\pi, n \in Z$

D. no value of x

Answer: D

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10. If the equation $z^4 + a_1z^3 + a_2z^2 + a_3z + a_4 = 0$ where a_1, a_2, a_3, a_4 are real coefficients different from zero has a pure imaginary root then the expression $\frac{a_1}{a_1a_2} + \frac{a_1a_4}{a_2a_3}$ has the value equal to

A. 0

B. 1

C. -2

D. 2

Answer: B

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11. If $z_1, z_2 \in C, z_1^2 \in R, z_1(z_1^2 - 3z_2^2) = 2$ and $z_2(3z_1^2 - z_2^2) = 11$, then the value of $z_1^2 + z_2^2$ is

A. 10

B. 12

C. 5

D. 8

Answer: C

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12. If $a^2 + b^2 = 1$ then $\frac{1 + b + ia}{1 + b - ia} =$

A. $a + ib$

B. $a + ia$

C. $b + ia$

D. $b + ib$

Answer: C

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13. If $z(1+a) = b+ic$ and $a^2 + b^2 + c^2 = 1$, then $[(1+iz)/(1-iz)] = \frac{a+ib}{1+c}$ b.

$\frac{b-ic}{1+a}$ c. $\frac{a+ic}{1+b}$ d. none of these

A. $\frac{a+ib}{1+c}$

B. $\frac{b-ic}{1+a}$

C. $\frac{a+ic}{1+b}$

D. none of these

Answer: A



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14. If a and b are complex and one of the roots of the equation $x^2 + ax + b = 0$ is purely real whereas the other is purely imaginary, then

A. $a^2 - (\bar{a})^2 = 4b$

B. $a^2 - (\bar{a})^2 = 2b$

C. $b^2 - (\bar{a})^2 = 2a$

D. $b^2 - (\bar{b})^2 = 2a$

Answer: A



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15. If $z = (\lambda + 3) + i\sqrt{(5 - \lambda^2)}$; then the locus of z is

A. ellipse

B. semicircle

C. parabola

D. none of these

Answer: B



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16. Let $z = 1 - t + i\sqrt{t^2 + t + 2}$, where t is a real parameter. the locus of the z in argand plane is

- A. a hyperbola
- B. an ellipse
- C. a straight line
- D. none of these

Answer: A



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17. If z_1 and z_2 are the complex roots of the equation $(x - 3)^3 + 1 = 0$, then $z_1 + z_2$ equal to

- A. 1
- B. 3
- C. 5

D. 7

Answer: D



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18. Which of the following is equal to $\sqrt[3]{-1}$?

A. $\frac{\sqrt{3} + \sqrt{-1}}{2}$

B. $\frac{-\sqrt{3} + \sqrt{-1}}{\sqrt{-4}}$

C. $\frac{\sqrt{3} - \sqrt{-1}}{\sqrt{-4}}$

D. $-\sqrt{-1}$

Answer: B



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19. If $x^2 + x + 1 = 0$ then the value of

$$\left(x + \frac{1}{x}\right)^2 + \left(x^2 + \frac{1}{x^2}\right)^2 + \dots + \left(x^{27} + \frac{1}{x^{27}}\right)^2 \text{ is}$$

A. 27

B. 72

C. 45

D. 54

Answer: D



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20. Sum of common roots of the equations $z^3 + 2z^2 + 2z + 1 = 0$ and

$$z^{1985} + z^{100} + 1 = 0 \text{ is}$$

A. -1

B. 1

C. 0

D. 1

Answer: A



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21. If $5x^3 + Mx + N, M, N \in R$ is divisible by $x^2 + x + 1$, then the value of $M + N$ is

A. 5

B. 4

C. -4

D. -5

Answer: D



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22. If $z = x + iy$ and $x^2 + y^2 = 16$, then the range of $||x| - |y||$ is [0, 4] b. [0, 2] c. [2, 4] d. none of these

A. [0, 4]

B. [0, 2]

C. [2, 4]

D. none of these

Answer: A



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23. If z is a complex number satisfying the equation $z^6 - 6z^3 + 25 = 0$, then the value of $|z|$ is

A. $5^{1/3}$

B. $25^{1/3}$

C. $125^{1/3}$

D. $625^{1/3}$

Answer: A



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24. If $8iz + 12z^2 - 18z + 27i = 0$, then $|z| = \frac{3}{2}$ b. $|z| = \frac{2}{3}$ c. $|z| = 1$ d. $|z| = \frac{3}{4}$

A. $|z| = \frac{3}{2}$

B. $|z| = \frac{3}{4}$

C. $|z| = 1$

D. $|z| = \frac{3}{4}$

Answer: A



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25. Let z_1 and z_2 be complex numbers such that $z_1 \neq z_2$ and $|z_1| = |z_2|$. If z_1 has positive real part and z_2 has negative imaginary part, then $\frac{z_1 + z_2}{z_1 - z_2}$ may be zero (b) real and positive real and negative (d) purely imaginary

- A. purely imaginary
- B. real and positive
- C. real and negative
- D. none of these

Answer: A



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26. $|z_1| = |z_2|$ and $\arg\left(\frac{z_1}{z_2}\right) = \pi$, then $z_1 + z_2$ is equal to

- A. 0
- B. purely imaginary

C. purely real

D. none of these

Answer: A



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27. If for complex numbers z_1 and z_2 , $\arg(z_1) - \arg(z_2) = 0$ then $|z_1 - z_2|$ is equal to

A. $|z_1| + |z_2|$

B. $|z_1| - |z_2|$

C. $||z_1| - |z_2||$

D. 0

Answer: C



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28. If $\left| \frac{z_1}{z_2} \right| = 1$ and $\arg(z_1 z_2) = 0$, then

A. $z_1 = z_2$

B. $|z_2|^2 = z_1 z_2$

C. $z_1 z_2 = 1$

D. more than 8

Answer: B



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29. Suppose A is a complex number and $n \in \mathbb{N}$, such that $A^n = (A + 1)^n = 1$, then the least value of n is 3 b. 6 c. 9 d. 12

A. 3

B. 6

C. 9

D. 12

Answer: B



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30. Let z, w be complex numbers such that $\bar{z} + i\bar{w} = 0$ and $\arg zw = \pi$ Then $\arg z$ equals

A. 4

B. 6

C. 8

D. more than 8

Answer: C



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31. Let z, w be complex numbers such that $\bar{z} + i\bar{w} = 0$ and $\arg zw = \pi$ Then $\arg z$ equals

A. $\frac{\pi}{4}$

B. $\frac{\pi}{2}$

C. $\frac{3\pi}{4}$

D. $\frac{5\pi}{4}$

Answer: C



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32. If $z = (3 + 7i)(a + ib)$ where $a, b \in \mathbb{Z} - \{0\}$, is purely imaginary, then the minimum value of $|z|$ is

A. 74

B. 45

C. 58

D. 65

Answer: C

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33. If $(\cos\theta + i\sin\theta)(\cos 2\theta + i\sin 2\theta)\dots(\cos n\theta + i\sin n\theta) = 1$ then the value of θ is :

A. $4m\pi$

B. $\frac{2m\pi}{n(n+1)}$

C. $\frac{4m\pi}{n(n+1)}$

D. $\frac{m\pi}{n(n+1)}$

Answer: C

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34. Given $z = (1 + i\sqrt{3})^{100}$, then $[RE(z)/IM(z)]$ equals 2^{100} b. 2^{50} c. $\frac{1}{\sqrt{3}}$ d. $\sqrt{3}$

A. 2^{100}

B. 2^{50}

C. $\frac{1}{\sqrt{3}}$

D. $\sqrt{3}$

Answer: C



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35. The expression $\left[\frac{1 + \sin\left(\frac{\pi}{8}\right) + i\cos\left(\frac{\pi}{8}\right)}{1 + \sin\left(\frac{\pi}{8}\right) - i\cos\left(\frac{\pi}{8}\right)} \right]^8$ is equal is

A. 1

B. -1

C. i

D. $-i$

Answer: B



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36. The number of complex numbers z satisfying $|z - 3 - i| = |z - 9 - i|$ and $|z - 3 + 3i| = 3$ are a. one b. two c. four d. none of these

A. one

B. two

C. four

D. none of these

Answer: A



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37. $P(z)$ be a variable point in the Argand plane such that $|z| = m \in i\mu m\{|z - 1|, |z + 1|\}$, then $z + z$ will be equal to a. -1 or 1 b. 1 but not equal to -1 c. -1 but not equal to 1 d. none of these

A. -1 or 1

B. 1 but not equal to -1

C. -1 but not equal to 1

D. none of these

Answer: A



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38. if $\left|z^2 - 1\right| = |z|^2 + 1$ then z lies on

A. a circle

B. a parabola

C. an ellipse

D. none of these

Answer: D



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39. If $z = x + iy$ ($x, y \in R, x \neq -\frac{1}{2}$), the number of values of z satisfying

$$|z|^n = z^2|z|^{n-2} + z|z|^{n-2} + 1. \quad (n \in N, n > 1)$$
 is

A. 0

B. 1

C. 2

D. 3

Answer: B



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40. Number of solutions of the equation $z^3 + \frac{3(\bar{z})^2}{|z|} = 0$ where z is a complex number is

A. 2

B. 3

C. 6

D. 5

Answer: D



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41. Number of ordered pairs(s) (a, b) of real numbers such that $(a + ib)^{2008} = a - ib$ holds good is

A. 2008

B. 2009

C. 2010

D. 1

Answer: C



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42. The equation $az^3 + bz^2 + \bar{b}z + \bar{a} = 0$ has a root α , where a, b, z and α belong to the set of complex numbers. The number value of $|\alpha|$

A. is $1/2$

B. is 1

C. is 2

D. can't be determined

Answer: B



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43. If $k > 0$, $|z| = w = k$, and $\alpha = \frac{z - \bar{w}}{k^2 + z\bar{w}}$, then $Re(\alpha)$ (A) 0 (B) $\frac{k}{2}$ (C) k (D)

None of these

A. 0

B. $k/2$

C. k

D. none of these

Answer: A



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44. z_1 and z_2 are two distinct points in an Argand plane. If $a|z_1| = b|z_2|$ (where $a, b \in R$), then the point $(az_1/bz_2) + (bz_2/az_1)$ is a point on the line segment $[-2, 2]$ of the real axis line segment $[-2, 2]$ of the imaginary axis unit circle $|z| = 1$ the line with $argz = \tan^{-1}2$

A. line segment $[-2, 2]$ of the real axis

B. line segment $[-2, 2]$ of the imaginary axis

C. unit circle $|z| = 1$

D. the line with $\arg z = \tan^{-1}2$

Answer: A



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45. If z is a complex number such that $-\frac{\pi}{2} < \arg z \leq \frac{\pi}{2}$, then which of the following inequalities is true?

A. $|z - \bar{z}| \leq |z|(argz - arg\bar{z})$

B. $|z - \bar{z}| \geq |z|(argz - arg\bar{z})$

C. $|z - \bar{z}| < (argz - arg\bar{z})$

D. None of these

Answer: A



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46. If $\cos\alpha + 2\cos\beta + 3\cos\gamma = \sin\alpha + 2\sin\beta + 3\sin\gamma = 0$, then the value of $\sin 3\alpha + 8\sin 3\beta + 27\sin 3\gamma$ is

- A. $\sin(\alpha + \beta + \gamma)$
- B. $3\sin(\alpha + \beta + \gamma)$
- C. $18\sin(\alpha + \beta + \gamma)$
- D. $\sin(\alpha + \beta + \gamma)$

Answer: C

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47. If α, β be the roots of the equation $u^2 - 2u + 2 = 0$ and if $\cot\theta = x + 1$,

then $\frac{(x + \alpha)^n - (x + \beta)^n}{\alpha - \beta}$ is equal to (a) $\begin{pmatrix} \sin n\theta \\ \sin^n \theta \end{pmatrix}$ (b) $\begin{pmatrix} \cos n\theta \\ \cos^n \theta \end{pmatrix}$ (c)

$\begin{pmatrix} \sin n\theta \\ \cos^n \theta \end{pmatrix}$ (d) $\begin{pmatrix} \cos n\theta \\ \sin^n \theta \end{pmatrix}$

A. $\frac{\sin n\theta}{\sin^n \theta}$

B. $\frac{\cos n\theta}{\cos^n \theta}$

C. $\frac{\sin n\theta}{\cos^n \theta}$

D. $\frac{\cos n\theta}{\sin^n \theta}$

Answer: A



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48. If $z = (i)^{(i)^i}$ where $i = \sqrt{-1}$, then $|z|$ is equal to

A. 1

B. $e^{-\pi/2}$

C. $e^{-\pi}$

D. none of these

Answer: A



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49. If $z = i \log(2 - \sqrt{-3})$, then $\cos z =$

A. -1

B. -1/2

C. 1

D. 2

Answer: D



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50. If $|z| = 1$, then the point representing the complex number $-1 + 3z$ will lie on a. a circle b. a parabola c. a straight line d. a hyperbola

A. a circle

B. a straight line

C. a parabola

D. a hyperbola

Answer: A



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51. The locus of point z satisfying $Re\left(\frac{1}{z}\right) = k$, where k is a nonzero real number, is a. a straight line b. a circle c. an ellipse d. a hyperbola

A. a stringht line

B. a circle

C. an ellispe

D. a hyperbola

Answer: B



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52. If z is complex number, then the locus of z satisfying the condition $|2z - 1| = |z - 1|$ is perpendicular bisector of line segment joining $1/2$ and 1
circle parabola none of the above curves

A. perpendicular bisector of line segment joining $1/2$ and 1

B. circle

C. parabola

D. none of the above curves

Answer: B



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53. The greatest positive argument of complex number satisfying

$$|z - 4| = \operatorname{Re}(z) \text{ is } \frac{\pi}{3} \text{ b. } \frac{2\pi}{3} \text{ c. } \frac{\pi}{2} \text{ d. } \frac{\pi}{4}$$

A. $\frac{\pi}{3}$

B. $\frac{2\pi}{3}$

C. $\frac{\pi}{2}$

D. $\frac{\pi}{4}$

Answer: D



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54. If t and c are two complex numbers such that $|t| \neq |c|$, $|t| = 1$ and $z = (at + b)/(t - c)$, $z = x + iy$. Locus of z is (where a, b are complex numbers) a. line segment b. straight line c. circle d. none of these

A. line segment

B. straight line

C. circle

D. none of these

Answer: C



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55. If $z^2 + z|z| + |z^2| = 0$, then the locus z is a. a circle b. a straight line c. a pair of straight line d. none of these

- A. a circle
- B. a straight line
- C. a pair of straight line
- D. none of these

Answer: C

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56. Let C_1 and C_2 are concentric circles of radius 1 and $\frac{8}{3}$ respectively having centre at $(3, 0)$ on the argand plane. If the complex number z

satisfies the inequality $\log_{\frac{1}{3}} \left(\frac{|z - 3|^2 + 2}{11|z - 3| - 2} \right) > 1$, then

- A. z lies outside C_1 but inside C_2

B. z line inside of both C_1 and C_2

C. z line outside both C_1 and C_2

D. none of these

Answer: A



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57. If $|z - 2 - i| = |z| \sin\left(\frac{\pi}{4} - \arg z\right)$, where $i = \sqrt{-1}$, then locus of z, is

A. a pair of straight lines

B. circle

C. parabola

D. ellipse

Answer: C



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58. If $|z - 1| \leq 2$ and $|\omega z - 1 - \omega^2| = a$ (where ω is a cube root of unity), then

complete set of values of a is $0 \leq a \leq 2$ b. $\frac{1}{2} \leq a \leq \frac{\sqrt{3}}{2}$ c.

$\frac{\sqrt{3}}{2} - \frac{1}{2} \leq a \leq \frac{1}{2} + \frac{\sqrt{3}}{2}$ d. $0 \leq a \leq 4$

A. $0 \leq a \leq 2$

B. $\frac{1}{2} \leq a \leq \frac{\sqrt{3}}{2}$

C. $\frac{\sqrt{3}}{2} - \frac{1}{2} \leq a \leq \frac{1}{2} + \frac{\sqrt{3}}{2}$

D. $0 \leq a \leq 4$

Answer: D



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59. If $|z^2 - 3| = 3|z|$, then the maximum value of $|z|$ is 1 b. $\frac{3 + \sqrt{21}}{2}$ c.

$\frac{\sqrt{21} - 3}{2}$ d. none of these

A. 1

B. $\frac{3 + \sqrt{21}}{2}$

C. $\frac{\sqrt{21} - 3}{2}$

D. none of these

Answer: B



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60. If $|2z - 1| = |z - 2|$ and z_1, z_2, z_3 are complex numbers such that $|z_1 - z_2| < \alpha, |z_2 - z_3| < \beta, |z_3 - z_1| > 2|z_1 - z_2|$

A. $< |z|$

B. $< 2|z|$

C. $> |z|$

D. $> 2|z|$

Answer: B



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61. If z_1 is a root of the equation

$$a_0z^n + a_1z^{n-1} + \dots + a_{n-1}z + a_n = 3, \text{ where } |a_i| < 2f \text{ or } i = 0, 1, \dots, n, \text{ then } |z| = \frac{3}{2}$$

b. $|z| < \frac{1}{4}$ c. $|z| > \frac{1}{4}$ d. $|z| < \frac{1}{3}$

A. $|z_1| > \frac{1}{2}$

B. $|z_1| < \frac{1}{2}$

C. $|z_1| > \frac{1}{4}$

D. $|z| < \frac{1}{2}$

Answer: A



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62. If $|z| <$

A. less than 1

B. $\sqrt{2} + 1$

C. $\sqrt{2} - 1$

D. none of these

Answer: A



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63. Let $|z_r - r| \leq r$, for all $r = 1, 2, 3, \dots, n$. Then $\left| \sum_{r=1}^n z_r \right|$ is less than

A. n

B. $2n$

C. $n(n+1)$

D. $\frac{n(n+1)}{2}$

Answer: C



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64. All the roots of the equation $11z^{10} + 10iz^9 + 10iz - 11 = 0$ lie

A. inside $|z| = 1$

B. one $|z| = 1$

C. outside $|z| = 1$

D. cannot say

Answer: B



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65. Let $\lambda \in \mathbb{R}$. If the origin and the non-real roots of $2z^2 + 2z + \lambda = 0$ form the three vertices of an equilateral triangle in the Argand lane, then λ is

A. 1

B. $\frac{2}{3}$

C. 2

D. -1

Answer: B



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66. The roots of the equation $t^3 + 3at^2 + 3bt + c = 0$ are z_1, z_2, z_3 which represent the vertices of an equilateral triangle. Then $a^2 = 3b$ b. $b^2 = a$ c. $a^2 = b$ d. $b^2 = 3a$

A. $a^2 = 3b$

B. $b^2 = a$

C. $a^2 = a$

D. $b^2 = 3a$

Answer: C



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67. The roots of the cubic equation $(z + ab)^3 = a^3$, $a \neq 0$ represents the vertices of an equilateral triangle of sides of length

A. $\frac{1}{\sqrt{3}}|ab|$

B. $\sqrt{3}|a|$

C. $\sqrt{3}|b|$

D. $|a|$

Answer: B



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68. If $|z_1| = |z_2| = |z_3| = 1$ and $z_1 + z_2 + z_3 = 0$ then the area of the triangle whose vertices are z_1, z_2, z_3 is

A. $3\sqrt{3}/4$

B. $\sqrt{3}/4$

C. 1

D. 2

Answer: A



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69. Let z and ω be two complex numbers such that $|z| \leq 1$, $|\omega| \leq 1$ and

$|z + i\omega| = |z_1 - z_2|$ is equal to

A. $\frac{2}{3}$

B. $\frac{\sqrt{5}}{3}$

C. $\frac{3}{2}$

D. $\frac{2\sqrt{5}}{3}$

Answer: C



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70. Let z_1, z_2, z_3, z_4 are distinct complex numbers satisfying $|z| = 1$ and $4z_3 = 3(z_1 + z_2)$, then $|z_1 - z_2|$ is equal to

- A. 1 or i
- B. i or $-i$
- C. 1 or i
- D. i or -1

Answer: D



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71. z_1, z_2, z_3, z_4 are distinct complex numbers representing the vertices of a quadrilateral $ABCD$ taken in order. If $z_1 - z_4 = z_2 - z_3$ and $\arg\left[\frac{(z_4 - z_1)}{(z_2 - z_1)}\right] = \pi/2$, the quadrilateral is

- A. rectangle
- B. rhombus

C. square

D. trapezium

Answer: A



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72. If $k + |k + z^2| = |z|^2$ ($k \in \mathbb{R}^-$), then possible argument of z is

A. 0

B. π

C. $\pi/2$

D. none of these

Answer: C



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73. If z_1, z_2, z_3 are the vertices of an equilateral triangle ABC such that

$|z_1 - i| = |z_2 - i| = |z_3 - i|$, then $|z_1 + z_2 + z_3|$ equals to

A. $3\sqrt{3}$

B. $\sqrt{3}$

C. 3

D. $\frac{1}{3\sqrt{3}}$

Answer: C



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74. If z is a complex number having least absolute value and

$|z - 2 + 2i| = \frac{1}{\sqrt{2}}$, then $z =$

A. $(2 - 1/\sqrt{2})(1 - i)$

B. $(2 - 1/\sqrt{2})(1 + i)$

C. $(2 + 1/\sqrt{2})(1 - i)$

D. $(2 + 1/\sqrt{2})(1 + i)$

Answer: A



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75. If z is a complex number lying in the fourth quadrant of Argand plane and $|\frac{z}{k+1} + 2i| > \sqrt{2}$ for all real value of $k (k \neq -1)$, then range of

$\arg(z)$ is $\left(\frac{\pi}{8}, 0\right)$ b. $\left(\frac{\pi}{6}, 0\right)$ c. $\left(\frac{\pi}{4}, 0\right)$ d. none of these

A. $\left(-\frac{\pi}{8}, 0\right)$

B. $\left(-\frac{\pi}{6}, 0\right)$

C. $\left(-\frac{\pi}{4}, 0\right)$

D. None of these

Answer: C



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76. If $|z_2 + iz_1| = |z_1| + |z_2|$ and $|z_1| = 3$ and $|z_2| = 4$, then the area of ABC , if affixes of $A, B,$ and C are $z_1, z_2,$ and $\left[\frac{z_2 - iz_1}{1 - i}\right]$ respectively, is $\frac{5}{2}$ b. 0 c. $\frac{25}{2}$ d. $\frac{25}{4}$

A. $\frac{5}{2}$

B. 0

C. $\frac{25}{2}$

D. $\frac{25}{4}$

Answer: D



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77. If a complex number z satisfies $|2z + 10 + 10i| \leq 5\sqrt{3} - 5$, then the least principal argument of z is : (a) $-\frac{5\pi}{6}$ (b) $\frac{11\pi}{12}$ (c) $-\frac{3\pi}{4}$ (d) $-\frac{2\pi}{3}$

A. $-\frac{5\pi}{6}$

B. $-\frac{11\pi}{12}$

C. $-\frac{3\pi}{4}$

D. $-\frac{2\pi}{3}$

Answer: A



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78. If 'z', lies on the circle $|z - 2i| = 2\sqrt{2}$, then the value of $\arg\left(\frac{z - 2}{z + 2}\right)$ is the equal to

A. $\frac{\pi}{3}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{6}$

D. $\frac{\pi}{2}$

Answer: B



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79. z_1 and z_2 , lie on a circle with centre at origin. The point of intersection of the tangents at z_1 and z_2 is given by

A. $\frac{1}{2}(\bar{z}_1 + \bar{z}_2)$

B. $\frac{2z_1z_2}{z_1 + z_2}$

C.

D.

Answer: B



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80. If $\arg\left(\frac{z_1 - \frac{z}{|z|}}{\frac{z}{|z|}}\right) = \frac{\pi}{2}$ and $\left|\frac{z}{|z|} - z_1\right| = 3$, then $|z_1|$ equals to

A. $\sqrt{26}$

B. $\sqrt{10}$

C. $\sqrt{3}$

D. $2\sqrt{2}$

Answer: B



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81. The maximum area of the triangle formed by the complex coordinates

z, z_1, z_2 which satisfy the relations $|z - z_1| = |z - z_2|$ and $\left| z - \frac{z_1 + z_2}{2} \right| \leq r$

,where $r > \left| z_1 - z_2 \right|$ is

A. $\frac{1}{2} \left| z_1 - z_2 \right|^2$

B. $\frac{1}{2} \left| z_1 - z_2 \right| r$

C. $\frac{1}{2} \left| z_1 - z_2 \right|^2 r^2$

D. $\frac{1}{2} \left| z_1 - z_2 \right|^2$

Answer: B



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82. Consider the region S of complex numbers z such that $\left|z^2 - az + 1\right| = 1$, where $|z| = 1$. Then area of S in the Argand plane is

- A. $\pi + 8$
- B. $\pi + 4$
- C. $2\pi + 4$
- D. $\pi + 6$

Answer: A

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83. The complex number associated with the vertices A, B, C of ΔABC are $e^{i\theta}, \omega, \bar{\omega}$, respectively [where $\omega, \bar{\omega}$ are the complex cube roots of unity and $\cos\theta > \operatorname{Re}(\omega)$], then the complex number of the point where angle bisector of A meets circumcircle of the triangle, is

A. $e^{i\theta}$

B. $e^{-i\theta}$

C. $\omega, \bar{\omega}$

D. $\omega + \bar{\omega}$

Answer: D



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84. If p and q are distinct prime numbers, then the number of distinct imaginary numbers which are p th as well as q th roots of unity are.
min (p, q) b. $\min(p, q)$ c. 1 d. zero

A. $\min(p, q)$

B. $\max(p, q)$

C. 1

D. zero

Answer: D



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85. Given z is a complex number with modulus 1. Then the equation $[(1 + ia)/(1 - ia)]^4 = z$ has all roots real and distinct two real and two imaginary three roots two imaginary one root real and three imaginary

- A. all roots real and distinct
- B. two real and two imaginary
- C. three roots real and one imaginary
- D. one root real and three imaginary

Answer: A



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86. The value of z satisfying the equation $\log z + \log z^2 + \dots + \log z^n = 0$ is

A. $\cos. \frac{4m\pi}{n(n+1)} + i\sin. \frac{4m\pi}{n(n+1)}, m = 0, 1, 2, \dots$

B. $\cos. \frac{4m\pi}{n(n+1)} - i\sin. \frac{4m\pi}{n(n+1)}, m = 0, 1, 2, \dots$

C. $\sin. \frac{4m\pi}{n} + i\cos. \frac{4m\pi}{n}, m = 0, 1, 2, \dots$

D. 0

Answer: A



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87. If $n \in N > 1$, then the sum of real part of roots of $z^n = (z+1)^n$ is

equal to $\frac{n}{2}$ b. $\frac{(n-1)}{2}$ c. $\frac{n}{2}$ d. $\frac{(1-n)}{2}$

A. $\frac{n}{2}$

B. $\frac{(n-1)}{2}$

C. $-\frac{n}{2}$

D. $\frac{(1-n)}{2}$

Answer: D



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88. Which of the following represents a points in an Argand pane, equidistant from the roots of the equation $(z + 1)^4 = 16z^4$? $(0, 0)$ b.

$\left(-\frac{1}{3}, 0\right)$ c. $\left(\frac{1}{3}, 0\right)$ d. $\left(0, \frac{2}{\sqrt{5}}\right)$

A. $(0, 0)$

B. $\left(-\frac{1}{3}, 0\right)$

C. $\left(\frac{1}{3}, 0\right)$

D. $\left(0, \frac{2}{\sqrt{5}}\right)$

Answer: C



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89. Let a be a complex number such that $|a| < 1$ and z_1, z_2, \dots be vertices of a polygon such that $z_k = 1 + a + a^2 + a^3 + \dots + a^{k-1}$.

Then, the vertices of the polygon lie within a circle.

A. $\left| z - \frac{1}{1-a} \right| = \frac{1}{|a-1|}$

B. $\left| z + \frac{1}{a+1} \right| = \frac{1}{|a+1|}$

C. $\left| z - \frac{1}{1-a} \right| = |a-1|$

D. $\left| z + \frac{1}{1-a} \right| = |a-1|$

Answer: A



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Exercise (Multiple)

1. If $z = \omega, \omega^2$ where ω is a non-real complex cube root of unity, are two vertices of an equilateral triangle in the Argand plane, then the third

vertex may be represented by $z = 1$ b. $z = 0$ c. $z = -2$ d. $z = -1$

A. $z = 1$

B. $z = 0$

C. $z = -2$

D. $z = -1$

Answer: A:C



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2. If $\arg(z_1 z_2) = 0$ and $|z_1| = |z_2| = 1$, then $z_1 + z_2 = 0$ b. $z_1 z_2 = 1$ c. $z_1 = z_2$

d. none of these

A. $z_1 + z_2 = 0$

B. $z_1 z_2 = 1$

C. $z_1 = \bar{z}_2$

D. none of these

Answer: B::C



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3. If $\sqrt{5 - 12i} + \sqrt{5 - 12i} = z$, then principal value of $\arg z$ can be $\frac{\pi}{4}$ b. $\frac{\pi}{4}$ c.

$\frac{3\pi}{4}$ d. $-\frac{3\pi}{4}$

A. $-\frac{\pi}{4}$

B. $\frac{\pi}{4}$

C. $\frac{3\pi}{4}$

D. $-\frac{3\pi}{4}$

Answer: A::B::C::D



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4. Values (s) $(-i)^{1/3}$ is/are $\frac{\sqrt{3} - i}{2}$ b. $\frac{\sqrt{3} + i}{2}$ c. $\frac{-\sqrt{3} - i}{2}$ d. $\frac{-\sqrt{3} + i}{2}$

$$A. \frac{\sqrt{3} - i}{2}$$

$$B. \frac{\sqrt{3} + i}{2}$$

$$C. \frac{-\sqrt{3} - i}{2}$$

$$D. \frac{-\sqrt{3} + i}{2}$$

Answer: A:C



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5. If $a^3 + b^3 + 6abc = 8c^3$ & ω is a cube root of unity then: a, b, c are in AP

(b) a, b, c , are in HP $a + b\omega - 2c\omega^2 = 0$ $a + b\omega^2 - 2c\omega = 0$

A. a, c, b are in A.P

B. a, c, b are in H.P

C. $a + b\omega - 2c\omega^2 = 0$

D. $a + b\omega^2 - 2c\omega = 0$

Answer: A::C::D



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6. Let z_1 and z_2 be two non-zero complex number such that $|z_1 + z_2| = |z_1| = |z_2|$. Then $\frac{z_1}{z_2}$ can be equal to (ω is imaginary cube root of unity).

A. $1 + \omega$

B. $1 + \omega^2$

C. ω

D. ω^2

Answer: C::D



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7. If $p = a + b\omega + c\omega^2$, $q = b + c\omega + a\omega^2$, and $r = c + a\omega + b\omega^2$, where $a, b, c \neq 0$ and ω is the complex cube root of unity, then .

A. If p, q, r lie on the circle $|z|=2$, the triangle formed by these points is equilateral.

B. $p^2 + q^2 + r^2 = a^2 + b^2 + c^2$

C. $p^2 + q^2 + r^2 = 2(pq + qr + rp)$

D. none of these

Answer: A:C

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8. Let $P(x)$ and $Q(x)$ be two polynomials. Suppose that

$f(x) = P(x^3) + xQ(x^3)$ is divisible by $x^2 + x + 1$, then

A. $P(x)$ is divisible by $(x-1)$, but $Q(x)$ is not divisible by $x-1$

B. $Q(x)$ is divisible by $(x-1)$, but $P(x)$ is not divisible by $x-1$

C. Both $P(x)$ and $Q(x)$ are divisible by $x-1$

D. $f(x)$ is divisible by $x-1$

Answer: C::D



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9. If α is a complex constant such that $az^2 + z + \alpha = 0$ has a real root, then

$\alpha + \bar{\alpha} = 1$ $\alpha + \bar{\alpha} = 0$ $\alpha + \bar{\alpha} = -1$ the absolute value of the real root is 1

A. $\alpha + \bar{\alpha} = 1$

B. $\alpha + \bar{\alpha} = 0$

C. $\alpha + \bar{\alpha} = -1$

D. the absolute value of the real root is 1

Answer: A::C::D



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10. If $z^3 + 3 + 2i(z + (-1 + ia)) = 0$ has on erreal roots, then the value of a lies in the interval ($a \in R$) a. $(-2, 1)$ b. $(-1, 0)$ c. $(0, 1)$ d. $(-2, 3)$

A. $(2, -1)$

B. $(-1, 0)$

C. $(0, 1)$

D. $(-2, 3)$

Answer: A::B::D



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11. Given that the complex numbers which satisfy the equation

$|zz^3| + |zz^3| = 350$ form a rectangle in the Argand plane with the length

of its diagonal having an integral number of units, then area of rectangle

is 48 sq. units if z_1, z_2, z_3, z_4 are vertices of rectangle, then

$z_1 + z_2 + z_3 + z_4 = 0$ rectangle is symmetrical about the real axis

$$\arg(z_1 - z_3) = \frac{\pi}{4} \text{ or } \frac{3\pi}{4}$$

A. area of rectangle is 48 sq units.

B. if z_1, z_2, z_3, z_4 are vertices of rectangle, then $z_1 + z_2 + z_3 + z_4 = 0$

C. rectangle is symmetrical about the real axis .

D. None of these

Answer: A::B::C

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12. If the points $A(z)$, $B(-z)$, and $C(1-z)$ are the vertices of an equilateral triangle ABC , then sum of possible z is $1/2$ sum of possible z is 1 product of possible z is $1/4$ product of possible z is

A. sum of possible z is $1/2$

B. sum of possible z is

C. product of possible z is $1/4$

D. product of possible z is $1/2$.

Answer: A::C



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13. If $|z - 3| = \min\{|z - 1|, |z - 5|\}$, then $\operatorname{Re}(z)$ equals to

A. 2

B. $\frac{5}{2}$

C. $\frac{7}{2}$

D. 4

Answer: A::D



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14. If z_1, z_2 are two complex numbers ($z_1 \neq z_2$) satisfying

$$\left| z_1^2 - z_2^2 \right| = \left| \bar{z}_1^2 + \bar{z}_2^2 - 2\bar{z}_1\bar{z}_2 \right|, \text{ then}$$

A. $\frac{z_1}{z_2}$ is purely imaginary

B. $\frac{z_1}{z_2}$ is purely real

C. $\left| \arg z_1 - \arg z_2 \right| = \pi$

D. $\left| \arg z_1 - \arg z_2 \right| = \frac{\pi}{2}$

Answer: A::D



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15. If $z_1 = a + ib$ and $z_2 = c + id$ are complex numbers such that $|z_1| = |z_2| = 1$ and $\operatorname{Re}(z_1 \bar{z}_2) = 0$, then the pair of complex numbers $\omega_1 = a + ic$ and $\omega_2 = b + id$ satisfies

A. $|\omega_1| = 1$

B. $|\omega_2| = 1$

C. $\operatorname{Re}(\omega_1 \bar{\omega}_2) = 0$

D. $\operatorname{Im}(\omega_1 \bar{\omega}_2) = 0$

Answer: A::B::C



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16. Let z_1 and z_2 be complex numbers such that $z_1 \neq z_2$ and $|z_1| = |z_2|$. If z_1 has positive real part and z_2 has negative imaginary part, then $\frac{z_1 + z_2}{z_1 - z_2}$ may be zero (b) real and positive real and negative (d) purely imaginary

- A. zero
- B. real and positive
- C. real and negative
- D. purely imaginary

Answer: A::D



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17. If $|z_1| = \sqrt{2}$, $|z_2| = \sqrt{3}$ and $|z_1 + z_2| = \sqrt{(5 - 2\sqrt{3})}$ then $\arg\left(\frac{z_1}{z_2}\right)$ (not necessarily principal)

A. $\frac{3\pi}{4}$

B. $\frac{2\pi}{3}$

C. $\frac{5\pi}{4}$

D. $\frac{5}{2}$

Answer: A:C

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18. Let four points z_1, z_2, z_3, z_4 be in complex plane such that $|z_2| = 1$,

$|z_1| \leq 1$ and $|z_3| \leq 1$. If $z_3 = \frac{z_2(z_1 - z_4)}{\bar{z}_1 z_4 - 1}$, then $|z_4|$ can be

A. 2

B. $\frac{2}{5}$

C. $\frac{1}{3}$

D. $\frac{5}{2}$

Answer: B::C



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19. A rectangle of maximum area is inscribed in the circle $|z - 3 - 4i| = 1$. If one vertex of the rectangle is $4 + 4i$, then another adjacent vertex of this rectangle can be $2 + 4i$ b. $3 + 5i$ c. $3 + 3i$ d. $3 - 3i$

A. $2 + 4i$

B. $3 + 5i$

C. $3 + 3i$

D. $3 - 3i$

Answer: B::C



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20. If $|z_1| = 15$ and $|z_2 - 3 - 4i| = 5$, then $\left(|z_1 - z_2|\right)_{\min} = 5$ b.
 $\left(|z_1 - z_2|\right)_{\min} = 10$ c. $\left(|z_1 - z_2|\right)_{\max} = 20$ d. $\left(|z_1 - z_2|\right)_{\max} = 25$

A. $|z_1 - z_2|_{\min} = 5$

B. $|z_1 - z_2|_{\min} = 10$

C. $|z_1 - z_2|_{\min} = 20$

D. $|z_1 - z_2|_{\min} = 25$

Answer: A:D

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21. $P(z_1)$, $Q(z_2)$, $R(z_3)$ and $S(z_4)$ are four complex numbers representing the vertices of a rhombus taken in order on the complex plane, then which one of the following is/are correct?

A. $\frac{z_1 - z_4}{z_2 - z_3}$ is purely real

$$\text{B. } \operatorname{amp} \frac{z_1 - z_4}{z_2 - z_4} = \operatorname{amp} \frac{z_2 - z_4}{z_3 - z_4}$$

$$\text{C. } \frac{z_1 - z_3}{z_2 - z_4} \text{ is purely imaginary}$$

$$\text{D. is not necessary that } |z_1 - z_3| \neq |z_2 - z_4|$$

Answer: A::B::C::D

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22. If $\arg(z + a) = \pi/6$ and $\arg(z - a) = 2\pi/3$ ($a \in \mathbb{R}^+$), then

A. $|z| = a$

B. $|z| = 2a$

C. $\arg(z) = \frac{\pi}{2}$

D. $\arg(z) = \frac{\pi}{3}$

Answer: A::D

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23. If a complex number z satisfies $|z| = 1$ and $\arg(z - 1) = \frac{2\pi}{3}$, then (ω is complex imaginary number)

A. $z^2 + z$ is purely imaginary number

B. $z = -\omega^2$

C. $z = -\omega$

D. $|z - 1| = 1$ then,

Answer: A::B::D



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24. If $|z - 1| = 1$, then

A. $\arg((z - 1 - i)/z)$ can be equal to $-\pi/4$

B. $(z - 2)/z$ is purely imaginary number

C. $(z - 2)/z$ is purely real number

D. if $\arg(z) = \theta$, where $z \neq 0$ and θ is acute, then $1 - 2/z = i \tan \theta$

Answer: A::B::D

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25. If $z_1 = 5 + 12i$ and $|z_2| = 4$, then

A. maximum $\left(|z_1 + iz_2| \right) = 17$

B. minimum $\left(|z_1 + (1 + i)z_2| \right) = 13 - 4\sqrt{2}$

C. minimum $\left| \frac{z_1}{z_2 + \frac{4}{z_2}} \right| = \frac{13}{4}$

D. maximum $\left| \frac{z_1}{z_2 + \frac{4}{z_2}} \right| = \frac{13}{3}$

Answer: A::B::D





26. Let z_1, z_2, z_3 be the three nonzero complex numbers such that

$$z_2 \neq 1, a = |z_1|, b = |z_2| \text{ and } c = |z_3|. \text{ Let } \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0 \text{ Then}$$

A. $\arg\left(\frac{z_3}{z_2}\right) = \arg\left(\frac{z_3 - z_1}{z_2 - z_1}\right)$

B. ortho centre of triangle formed by z_1, z_2, z_3 is $z_1 + z_2 + z_3$

C. if triangle formed by z_1, z_2, z_3 is equilateral then $z_1 + z_2 + z_3 = \frac{3\sqrt{3}}{2} |z_1|^2$

D. if triangle formed by z_1, z_2, z_3 is equilateral, then $z_1 + z_2 + z_3 = 0$

Answer: A::B::D



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27. z_1 and z_2 are the roots of the equation $z^2 - az + b = 0$ where

$|z_1| = |z_2| = 1$ and a, b are nonzero complex numbers, then

A. $|a| \leq 1$

B. $|a| \leq 2$

C. $2\arg(a) = \arg(b)$

D. $\arg(a) = 2\arg(b)$

Answer: B::C



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28. If $\left| \frac{(z - z_1)}{(z - z_2)} \right| = 3$, where z_1 and z_2 are fixed complex numbers and z is a variable complex number, then z lies on a

A. circle with z_1 as its interior point

B. circle with z_2 as its interior point

C. circle with z_1 as its exterior point

D. circle with z_2 as its exterior point

Answer: B::C



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29. If $z = x + iy$, then the equation $|(2z - i)/(z + 1)| = m$ represents a circle, then m can be 1/2 b. 1 c. 2 d. 3

A. 1/2

B. 1

C. 2

D. 3

Answer: A::B::C



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30. System of equations $|z + 3| - |z - 3| = 6$ and $|z - 4| = r$ where $r \in R^+$ has

A. one solution if $r > 1$

B. one solution if $r > 1$

C. two solutions if $r = 1$

D. at least one solution

Answer: A::C::D



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31. Let the equation of a ray be $|z - 2| - |z - 1 - i| = \sqrt{2}$. If the ray strikes the y-axis, then the equation of the reflected ray (including or excluding the point of incidence) is .

A. $\arg(z - 2i) = \frac{\pi}{4}$

B. $|z - 2i| - |z - 1 - i| = \sqrt{2}$

C. $\arg(z - 2i) = \frac{3\pi}{4}$

D. $|z - 1i| - |z - 1 - 3i| = 2\sqrt{2}$

Answer: A::B



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32. Given that the two curves $\arg(z) = \frac{\pi}{6}$ and $|z - 2\sqrt{3}i| = r$ intersect in two distinct points, then $[r] \neq 2$ b. `0

- A. $[r] \neq 2$ where $[.]$ represents greatest integer
- B. $0 < r < 3$
- C. $r = 6$
- D. $3 < r < 2\sqrt{3}$

Answer: A:D



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33. On the Argand plane ,let $z_1 = -2 + 3z$, $z_2 = -2 - 3z$ and $|z| = 1$. Then

- A. z_1 moves on circle with centre at $(-2, 0)$ and radius 3
- B. z_1 and z_2 describe the same locus
- C. z_1 and z_2 move on differenet circles

D. $z_1 - z_2$ moves on a circle concentric with $|z| = 1$

Answer: A::B::D



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34. Let $S = \{z: x = x + iy, y \geq 0, |z - z_0| \leq 1\}$, where $|z_0| = |z_0 - \omega| = |z_0 - \omega^2|$, ω and ω^2 are non-real cube roots of unity.

Then

A. $z_0 = -1$

B. $z_0 = -1/2$

C. if $z \in S$, then least value of $|z|$ is 1

D. $|\arg(\omega - z_0)| = \pi/3$

Answer: A::D



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35. If P and Q are represented by the complex numbers z_1 and z_2 such that $\left|1/z_2 + 1/z_1\right| = \left|1/z_2 - 1/z_1\right|$, then

A. ΔOPQ (where O is the origin) is equilateral.

B. ΔOPQ is right angled

C. the circumcentre of ΔOPQ is $\frac{1}{2}(z_1 + z_2)$

D. the circumcentre of ΔOPQ is $\frac{1}{2}(z_1 - z_2)$

Answer: B::C



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36. Locus of complex number satisfying are $\arg[(z - 5 + 4i)/(z + 3 - 2i)] = -\pi/4$ is the arc of a circle

A. whose radius is $5\sqrt{2}$

B. whose radius is 5

C. whose length (of arc) is $\frac{15\pi}{\sqrt{2}}$

D. whose centre is $-2-5i$

Answer: A::B::C



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37. Equation of tangent drawn to circle $|z| = r$ at the point $A(z_0)$, is

A. $Re\left(\frac{z}{z_0}\right) = 1$

B. $z\bar{z}_0 + z_0\bar{z} = 2r^3$

C. $Im\left(\frac{z}{z_0}\right) = 1$

D. $Im\left(\frac{z_0}{z}\right) = 1$

Answer: A::B



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38. If n is a natural number > 2 , such that $z^n = (z + 1)^n$, then

A. roots of equation lie on a straight line parallel to the y-axis

B. roots of equation lie on a straight line parallel to the x-axis

C. sum of the real parts of the roots is $-\frac{n-1}{2}$

D. none of these

Answer: A:C



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39. If $|z - (1/z)| = 1$, then $(|z|)_{\max} = \frac{1 + \sqrt{5}}{2}$ b. $(|z|)_{\min} = \frac{\sqrt{5} - 1}{2}$ c.
 $(|z|)_{\max} = \frac{\sqrt{5} - 2}{2}$ d. $(|z|)_{\min} = \frac{\sqrt{5} - 1}{\sqrt{2}}$

A. $|z|_{\max} = \frac{1 + \sqrt{5}}{2}$

B. $|z|_{\min} = \frac{\sqrt{5} - 1}{2}$

$$C. |z|_{\max} = \frac{\sqrt{4} - 2}{2}$$

$$D. |z|_{\min} = \frac{\sqrt{5} - 1}{2}$$

Answer: A::B



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40. If $1, z_1, z_2, z_3, \dots, z_{n-1}$ be the n th roots of unity and ω be a non-real

complex cube root of unity then the product $\prod_{r=1}^{n-1} (\omega - z_r)$ can be equal to

A. 0

B. 1

C. -1

D. $1 + \omega$

Answer: A::B::C



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41. Let z be a complex number satisfying equation $z^p - z^{-q}$, where $p, q \in \mathbb{N}$, then if $p = q$, then number of solutions of equation will be infinite. if $p = q$, then number of solutions of equation will be finite. if $p \neq q$, then number of solutions of equation will be $p + q + 1$. if $p \neq q$, then number of solutions of equation will be $p + q$.

- A. if $p=q$, then number of solution of equation will infinite.
- B. if $p=q$, then number of solutions of equation will finite
- C. if $p \neq q$, then number of solutions of equation will $p + q + 1$.
- D. if $p \neq q$, then number of solutions of equation will be $p + q$

Answer: A::B

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42. Which of the following is true ?

- A. The number of common roots of $z^{144} = 1$ and $z^{24} = 1$ is 24

B. The number of common roots of $z^{360} = 1$ and $z^{315} = 1$ is 45

C. The number of roots common to $z^{24} = 1$, $z^{20} = 1$ and $z^{56} = 1$ is 4

D. The number of roots common to $z^{27} = 1$, $z^{125} = 1$ and $z^{49} = 1$ is 1

Answer: A::B::C::D



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43. If from a point P representing the complex number z_1 on the curve $|z| = 2$, two tangents are drawn from P to the curve $|z| = 1$, meeting at points $Q(z_2)$ and $R(z_3)$, then :

A. complex number $(z_1 + z_2 + z_3)/3$ will be on the curve $|z| = 1$

B.
$$\left(\frac{4}{\bar{z}_1} + \frac{1}{\bar{z}_2} + \frac{1}{\bar{z}_3} \right) \left(\frac{4}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} \right) = 9$$

C.
$$\arg \left(\frac{z_2}{z_3} \right) = \frac{2\pi}{3}$$

D. orthocentre and circumcenter of ΔPQR will coincide

Answer: A::B::C::D



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44. A complex number z is rotated in anticlockwise direction by an angle α and we get z' and if the same complex number z is rotated by an angle α in clockwise direction and we get z'' then

A. z', z', z'' are in G.P

B. z', z', z'' are H.P

C. $z' + z'' = 2z\cos\alpha$

D. $z'^2 + z''^2 = 2z^2\cos 2\alpha$

Answer: A::C::D



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45. z_1, z_2, z_3 and z'_1, z'_2, z'_3 are nonzero complex numbers such that $z_3 = (1 - \lambda)z_1 + \lambda z_2$ and $z'_3 = (1 - \mu)z'_1 + \mu z'_2$, then which of the following statements is/are true?

A. If $\lambda, \mu \in \mathbb{R} - \{0\}$, then z_1, z_2 and z_3 are collinear and z'_1, z'_2, z'_3 are collinear separately.

B. If λ, μ are complex numbers, where $\lambda = \mu$, then triangles formed by points z_1, z_2, z_3 and z'_1, z'_2, z'_3 are similar.

C. If λ, μ are distinct complex numbers, then points z_1, z_2, z_3 and z'_1, z'_2, z'_3 are not connected by any well defined geometry.

D. If $0 < \lambda < 1$, then z_3 divides the line joining z_1 and z_2 internally and if $\mu > 1$, then z'_3 divides the line joining z'_1, z'_2 externally.

Answer: A::B::C::D



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46. Given $z = f(x) + ig(x)$ where $f, g: (0, 1) \rightarrow \mathbb{R}$ are real valued functions. Then

which of the following does not hold good? $z = \frac{1}{1 - ix} + i\frac{1}{1 + ix}$ b.

$z = \frac{1}{1 + ix} + i\frac{1}{1 - ix}$ c. $z = \frac{1}{1 + ix} + i\frac{1}{1 + ix}$ d. $z = \frac{1}{1 - ix} + i\frac{1}{1 - ix}$

A. $z = \frac{1}{1 - ix} + i\left(\frac{1}{1 + ix}\right)$

B. $z = \frac{1}{1 + ix} + i\left(\frac{1}{1 - ix}\right)$

C. $z = \frac{1}{1 + ix} + i\left(\frac{1}{1 + ix}\right)$

D. $z = \frac{1}{1 - ix} + i\left(\frac{1}{1 - ix}\right)$

Answer: A::C::D



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47. Let a, b, c be distinct complex numbers with $|a| = |b| = |c| = 1$ and z_1, z_2 be the roots of the equation $az^2 + bz + c = 0$ with $|z_1| = 1$. Let P and Q represent the complex numbers z_1 and z_2 in the Argand plane with $\angle POQ = \theta, 0^\circ < 180^\circ$ (where O being the origin). Then

A. $b^2 = ac$

B. $PQ = \sqrt{3}$

C. $\theta = \frac{\pi}{3}$

D. $\theta = \frac{2\pi}{3}$

Answer: A::B::D

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48. If $a, b, c, d \in R$ and all the three roots of $az^3 + bz^2 + cZ + d = 0$ have negative real parts, then

A. $ab > 0$

B. $bv > 0$

C. $ad > 0$

D. $bc - ad > 0$

Answer: A::B::C::D

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49. If $\frac{3}{2 + e^{i\theta}} = ax + iby$, then the locus of $P(x, y)$ will represent

- A. ellipse of $a=1, b=2$
- B. circle if $a=b=1$
- C. pair of straight line if $a=1, b=0$
- D. None of these

Answer: A::B::C

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Exercise (Comprehension)

1. Consider the complex number $z = (1 - i\sin\theta)/(1 + i\cos\theta)$.

The value of θ for which z is purely real are

A. $n\pi - \frac{\pi}{4}, n \in I$

B. $n\pi + \frac{\pi}{4}, n \in I$

C. $n\pi, n \in I$

D. None of these

Answer: A

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2. Consider the complex number $z = (1 - i\sin\theta)/(1 + i\cos\theta)$.

The value of θ for which z is purely imaginary are

A. $n\pi - \frac{\pi}{4}, n \in I$

B. $n\pi + \frac{\pi}{4}, n \in I$

C. $n\pi, n \in I$

D. no real values of θ

Answer: D

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3. Consider the complex number $z = (1 - i\sin\theta)/(1 + i\cos\theta)$.

The value of θ for which z is unimodular give by

A. $n\pi \pm \frac{\pi}{6}, n \in I$

B. $n\pi \pm \frac{\pi}{3}, n \in I$

C. $n\pi \pm \frac{\pi}{4}, n \in I$

D. no real values of θ

Answer: C

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4. Consider the complex number $z = (1 - i\sin\theta)/(1 + i\cos\theta)$.

If argument of z is $\pi/4$, then

A. $\theta = n\pi, n \in I$ only

B. $\theta = (2n + 1), n \in I$ only

C. both $\theta = n\pi$ and $\theta = (2n + 1)\frac{\pi}{2}, n \in I$

D. none of these

Answer: D



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5. Consider the complex numbers z_1 and z_2 satisfying the relation

$$|z_1 + z_2|^2 = |z_1|^2 + |z_2|^2$$

Complex number $z_1 \bar{z}_2$ is

A. purely real

B. purely imaginary

C. zero

D. none of these

Answer: B



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6. Consider the complex numbers z_1 and z_2 Satisfying the relation

$$|z_1 + z_2|^2 = |z_1|^2 + |z_2|^2$$

Complex number z_1/z_2 is

- A. purely real
- B. purely imaginary
- C. zero
- D. none of these

Answer: B



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7. Consider the complex numbers z_1 and z_2 Satisfying the relation

$$|z_1 + z_2|^2 = |z_1|^2 + |z_2|^2$$

One of the possible argument of complex number $i(z_1/z_2)$

A. $\frac{\pi}{2}$

B. $-\frac{\pi}{2}$

C. 0

D. none of these

Answer: C



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8. Consider the complex numbers z_1 and z_2 Satisfying the relation

$$\left|z_1 + z_2\right|^2 = \left|z_1\right|^2 + \left|z_2\right|^2$$
 Possible difference between the argument of z_1

and z_2 is

A. 0

B. π

C. $-\frac{\pi}{2}$

D. none of these

Answer: C



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9. Let z be a complex number satisfying $z^2 + 2z\lambda + 1 = 0$, where λ is a parameter which can take any real value.

The roots of this equation lie on a certain circle if

A. $-1 < \lambda < 1$

B. $\lambda > 1$

C. $\lambda < 1$

D. none of these

Answer: A



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10. Let z be a complex number satisfying $z^2 + 2z\lambda + 1 = 0$, where λ is a parameter which can take any real value.

One root lies inside the unit circle and one outside if

A. $-1 < \lambda < 1$

B. $\lambda > 1$

C. $\lambda < 1$

D. none of these

Answer: B



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11. Let z be a complex number satisfying $z^2 + 2z\lambda + 1 = 0$, where λ is a parameter which can take any real value.

For every large value of λ the roots are approximately.

A. $-2\lambda, 1/\lambda$

B. $-\lambda, -1/\lambda$

C. $-2\lambda, -\frac{1}{2\lambda}$

D. none of these

Answer: C

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12. The roots of the equation $z^4 + az^3 + (12 + 9i)z^2 + bz = 0$ (where a and b are complex numbers) are the vertices of a square. Then

The value of $|a - b|$ is

A. $5\sqrt{5}$

B. $\sqrt{130}$

C. 12

D. $\sqrt{175}$

Answer: B



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13. The roots of the equation $z^4 + az^3 + (12 + 9i)z^2 + bz = 0$ (where a and b are complex numbers) are the vertices of a square. Then The area of the square is

- A. 25 sq.units
- B. 20 sq.units
- C. 5 sq.unit
- D. 4 sq .units

Answer: C



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14. Consider a quadratic equaiton $az^2 + bz + c = 0$, where a, b, c are complex number.

The condition that the equation has one purely imaginary root is

A. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{a} - \bar{a}b)$

B. $(c\bar{c} - a\bar{c})^2 = (b\bar{c} - c\bar{a})^2(a\bar{b} + \bar{a}b)$

C. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{b} + \bar{a}b)$

D. None of these

Answer: A



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15. Consider a quadratic equation $az^2 + bz + c = 0$, where a, b, c are complex numbers. If the equation has two purely imaginary roots, then which of the following is not true.

A. $a\bar{b}$ is purely imaginary

B. $b\bar{c}$ is purely imaginary

C. $c\bar{a}$ is purely real

D. none of these

Answer: D



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16. Consider a quadratic equation $az^2 + bz + c = 0$, where a, b, c are complex numbers.

The condition that the equation has one purely real root is

A. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{a} - \bar{a}b)$

B. $(c\bar{c} - a\bar{c})^2 = (b\bar{c} - c\bar{a})^2(a\bar{b} + \bar{a}b)$

C. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{b} + \bar{a}b)$

D. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} - c\bar{b})(a\bar{b} - \bar{a}b)$

Answer: D



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17. Suppose z and ω are two complex number such that $|z + i\omega| = 2$. Which of the following is ture about $|z|$ and $|\omega|$?

A. $|z| = |\omega| = \frac{1}{2}$

B. $|z| = \frac{1}{2}, |\omega|, |\omega| = \frac{3}{4}$

C. $|z| = |\omega| = \frac{3}{4}$

D. $|z| = |\omega| = 1$

Answer: D



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18. Suppose z and ω are two complex number such that Which of the following is true for z and ω ?

A. $Re(z) = Re(\omega) = \frac{1}{2}$

B. $Im(z) = Im(\omega)$

C. $Re(z) = Im(\omega)$

D. $Im(z) = Re(\omega)$

Answer: D



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19. Suppose z and ω are two complex number such that $|z| \leq 1$, $|\omega| \leq 1$ and $|z + i\omega| = |z - i\bar{\omega}| = 2$ The complex number of ω can be

A. 1 or -i

B. -1

C. i or $-i$

D. ω or ω^2 (where ω is the cube root of unity)

Answer: C



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20. Consider the equation of line $a\bar{z} + a\bar{z} + a\bar{z} + b = 0$, where b is a real parameter and a is fixed non-zero complex number.

The intercept of line on real axis is given by

A. $\frac{-2b}{a + \bar{a}}$

B. $\frac{-b}{2(a + \bar{a})}$

C. $\frac{-b}{a + \bar{a}}$

D. $\frac{b}{a + \bar{a}}$

Answer: C



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21. Consider the equation of line $a\bar{z} + a\bar{z} + a\bar{z} + b = 0$, where b is a real parameter and a is fixed non-zero complex number.

The intercept of line on imaginary axis is given by

A. $\frac{b}{\bar{a} - a}$

B. $\frac{2b}{\bar{a} - a}$

C. $\frac{b}{2(\bar{a} - a)}$

D. $\frac{b}{a - \bar{a}}$

Answer: D



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22. Consider the equation of line $a\bar{z} + \bar{a}z + b = 0$, where b is a real parameter and a is fixed non-zero complex number.

The locus of mid-point of the line intercepted between real and imaginary axis is given by

—

A. $az - \bar{a}z = 0$

—

B. $az + \bar{a}z = 0$

—

C. $az - \bar{a}z + b = 0$

—

D. $az - \bar{a}z + 2b = 0$

Answer: B



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23. Consider the equation $az + bz + c = 0$, where $a, b, c \in \mathbb{Z}$

If $|a| \neq |b|$, then z represents

- A. circle
- B. straight line
- C. one point
- D. ellipse

Answer: C



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24. Consider the equation $az + bz + c = 0$, where $a, b, c \in \mathbb{Z}$

If $|a| = |b|$ and $\bar{a}c \neq b\bar{c}$, then z has

A. infinite solutions

B. no solutions

C. finite solutions

D. cannot say anything

Answer: B



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—

25. Consider the equation $ax + by + c = 0$, where $a, b, c \in \mathbb{Z}$

If $|a| = |b| \neq 0$ and $ax + b\bar{c} + c = 0$ represents

A. an ellipse

B. a circle

C. a point

D. a straight line

Answer: D



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26. Complex numbers z satisfy the equation $|z - (4/z)| = 2$

The difference between the least and the greatest moduli of complex number is

A. 2

B. 4

C. 1

D. 3

Answer: A



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27. Complex numbers z satisfy the equation $|z - (4/z)| = 2$

The value of $\arg\left(\frac{z_1}{z_2}\right)$ where z_1 and z_2 are complex numbers with the greatest and the least moduli, can be

A. 2π

B. π

C. $\pi/2$

D. none of these

Answer: B



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28. Complex numbers z satisfy the equation $|z - (4/z)| = 2$

Locus of z if $|z - z_1| = |z - z_2|$, where z_1 and z_2 are complex numbers with the greatest and the least moduli, is

A. line parallel to the real axis

B. line parallel to the imaginary axis

C. line having a positive slope

D. line having a negative slope

Answer: B



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29. In an Agrad plane z_1, z_2 and z_3 are, respectively, the vertices of an isosceles triangle ABC with $AC = BC$ and $\angle CAB = \theta$. If z_4 is incentre of triangle, then

The value of $AB \times AC / (IA)^2$ is

A.
$$\frac{(z_2 - z_1)(z_3 - z_1)}{(z_4 - z_1)^2}$$

B.
$$\frac{(z_2 - z_1)(z_1 - z_3)}{(z_4 - z_1)^2}$$

C.
$$\frac{(z_4 - z_1)^2}{(z_2 - z_1)(z_3 - z_1)}$$

D. none of these

Answer: A



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30. In an Argand plane z_1, z_2 and z_3 are, respectively, the vertices of an isosceles triangle ABC with $AC = BC$ and $\angle CAB = \theta$. If z_4 is incentre of triangle, then

The value of $(z_4 - z_1)^2(\cos\theta + 1)\sec\theta$ is

A.
$$\frac{(z_2 - z_1)(z_3 - z_1)}{(z_4 - z_1)}$$

B.
$$(z_2 - z_1)(z_3 - z_1)$$

C.
$$(z_2 - z_1)(z_3 - z_1)^2$$

D.
$$\frac{(z_2 - z_1)(z_1 - z_3)}{(z_4 - z_1)^2}$$

Answer: B



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31. In an Argand plane z_1, z_2 and z_3 are, respectively, the vertices of an isosceles triangle ABC with $AC = BC$ and $\angle CAB = \theta$. If z_4 is incentre of

triangle, then

The value of $(z_2 - z_1)^2 \tan \theta \tan \theta/2$ is

A. $(z_1 + z_2 - 2z_3)$

B. $(z_1 + z_2 - z_3)(z_1 + z_2 - z_4)$

C. $-(z_1 + z_2 - 2z_3)(z_1 + z_2 - 2z_4)$

D. $z_4 = \sqrt{z_2 z_3}$

Answer: C



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32. $A(z_1), B(z_2)$ and $C(z_3)$ are the vertices of triangle ABC inscribed in the circle $|z|=2$, internal angle bisector of angle A meets the circumcircle again at $D(z_4)$. Point D is:

A. $z_4 = \frac{1}{z_2} + \frac{1}{z_3}$

B. $\sqrt{\frac{z_2 + z_3}{z_1}}$

$$C. \sqrt{\frac{z_2 z_3}{z_1}}$$

$$D. z_4 = \sqrt{z_2 z_3}$$

Answer: D



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33. $A(z_1), B(z_2)$ and $C(z_3)$ are the vertices of triangle ABC inscribed in the circle $|z|=2$, internal angle bisector of angle A meets the circumcircle again at $D(z_4)$. Point D is:

A. $\frac{\pi}{2}$

B. $\frac{\pi}{3}$

C. $\frac{\pi}{2}$

D. $\frac{2\pi}{3}$

Answer: C



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34. $A(z_1), B(z_2)$ and $C(z_3)$ are the vertices of triangle ABC inscribed in the circle $|z|=2$, internal angle bisector of angle A meets the circumcircle again at $D(z_4)$. Point D is:

A. H.M of z_2 and z_3

B. A.M of z_2 and z_3

C. G.M of z_2 and z_3

D. none of these

Answer: C



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MATRIX MATCH TYPE

1. The graph of the quadratic function $y = ax^2 + bx + c$ is as shown in the following figure.



Now, match the complex numbers given in List I with the corresponding arguments in List II.



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2. Let z_1, z_2 and z_3 be the vertices of triangle. Then match following lists.



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3. Match following lists.



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4. Complex number z satisfies the equation $||z - 5i| + m|z - 12i| - |z| = n$.

Then match the value of m and n in List I with the corresponding locus in List II.



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5. Complex number z lies on the curve $S \equiv \arg \frac{g(z + 3)}{z + 3i} = -\frac{\pi}{4}$

Now, match the locus in List I with its number of points of intersection with the curve S in List II.



- A. a b c d
(1) p q p r
- B. a b c d
(2) s r q p
- C. a b c d
(3) q p q r
- D. a b c d
(4) s p q r

Answer: A



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6. Consider sets $A = \{z \in C: z^{27} - 1 = 0\}$ and $B = \{z \in C: z^{36} - 1 = 0\}$

Now ,match the following lists.



- A. a b c d
(1) p q p r
- B. a b c d
(2) r q s p
- C. a b c d
(3) q p q r
- D. a b c d
(4) s p q r

Answer: B



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7. Match the statements in List I with those in List II

[Note: Here z take the values in the complex place and $\text{Im}(z)$ and $\text{Re}(z)$

denote, respectively, the imaginary part and the real part of z].



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8. Let $z_k = \cos\left(\frac{2k\pi}{10}\right) - i\sin\left(\frac{2k\pi}{10}\right)$, $k = 1, 2, \dots, 9$



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9. Match the statements/experssions given in List I with the values given in List II.



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Exercise (Numerical)

1. If $x = a + bi$ is a complex number such that $x^2 = 3 + 4i$ and $x^3 = 2 + 1i$, where $i = \sqrt{-1}$, then $(a + b)$ equal to _____.

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2. If the complex numbers x and y satisfy $x^3 - y^3 = 98i$ and $x - y = 7i$, then $xy = a + ib$, where $a, b, \in \mathbb{R}$. The value of $(a + b)/3$ equals _____.

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3. If $x = \omega - \omega^2 - 2$ then, the value of $x^4 + 3x^3 + 2x^2 - 11x - 6$ is (where ω is a imaginary cube root of unity)

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4. Let $z = 9 + bi$, where b is nonzero real and $i^2 = -1$. If the imaginary part of z^2 and z^3 are equal, then $b/3$ is _____.



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5. Modulus of nonzero complex number z satisfying $\bar{z} + z = 0$ and $|z|^2 - 4iz = z^2$ is _____.



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6. If the expression $(1 + ir)^3$ is of the form of $s(1 + i)$ for some real 's' where 'r' is also real and $i = \sqrt{-1}$



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7. If complex number $z(z \neq 2)$ satisfies the equation $z^2 = 4z + |z|^2 + \frac{16}{|z|^3}$, then the value of $|z|^4$ is _____.



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8. The complex number z satisfies $z + |z| = 2 + 8i$. find the value of $|z| - 8$

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9. Let $|z| = 2$ and $w = \frac{z+1}{z-1}$, where $z, w \in C$ (where C is the set of complex numbers). Then product of least and greatest value of modulus of w is _____.

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10. If z is a complex number satisfying $z^4 + z^3 + 2z^2 + z + 1 = 0$ then the set of possible values of z is

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11. Let $1, \omega, \omega^2$ be the cube roots of unity. The least possible degree of a polynomial with real coefficients having roots

$2\omega, (2 + 3\omega), (2 + 3\omega^2), (2 - \omega - \omega^2)$ is _____.

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12. If ω is the imaginary cube roots of unity, then the number of pair of integers (a,b) such that $|a\omega + b| = 1$ is _____.

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13. Suppose that z is a complex number the satisfies $|z - 2 - 2i| \leq 1$. The maximum value of $|2iz + 4|$ is equal to _____.

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14. If $|z + 2 - i| = 5$ and maximum value of $|3z + 9 - 7i|$ is M , then the value of M is _____.

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15. Let $Z_1 = (8 + i)\sin\theta + (7 + 4i)\cos\theta$ and $Z_2 = (1 + 8i)\sin\theta + (4 + 7i)\cos\theta$ are two complex numbers. If $Z_1 \cdot Z_2 = a + ib$ where $a, b \in R$ then the largest value of $(a + b) \forall \theta \in R$, is



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16. Let $A = \{a \in R\}$ the equation $(1 + 2i)x^3 - 2(3 + i)x^2 + (5 - 4i)x + a^2 = 0$ has at least one real root. Then the value of $\frac{\sum a^2}{2}$ is _____.



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17. Find the minimum value of the expression $E = |z|^2 + |z - 3|^2 + |z - 6i|^2$ (where $z = x + iy, x, y \in R$)



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18. If z_1 lies on $|z - 3| + |z + 3| = 8$ such that $\arg z_1 = \pi/6$, then $37|z_1|^2 =$ _____.

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19. If z satisfies the condition $\arg(z + i) = \frac{\pi}{4}$. Then the minimum value of $|z + 1 - i| + |z - 2 + 3i|$ is _____.

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20. Let $\omega \neq 1$ be a complex cube root of unity. If

$(4 + 5\omega + 6\omega^2)^{n^2+2} + (6 + 5\omega^2 + 4\omega)^{n^2+2} + (5 + 6\omega + 4\omega^2)^{n^2+2} = 0$, and $n \in N$, where $n \in [1, 100]$, then number of values of n is _____.

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21. Let z be a non-real complex number which satisfies the equation

$$z^{23} = 1. \text{ Then the value of } \sum_{k=1}^{22} \frac{1}{1 + z^{8k} + z^{16k}}$$

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22. If z, z_1 and z_2 are complex numbers such that $z = z_1 z_2$ and $|\bar{z}_2 - z_1| \leq 1$, then maximum value of $|z| - \operatorname{Re}(z)$ is _____.

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23. Let z_1, z_2 and z_3 be three complex numbers such that $z_1 + z_2 + z_3 = z_1 z_2 + z_2 z_3 + z_1 z_3 = z_1 z_2 z_3 = 1$. Then the area of triangle formed by points $A(z_1), B(z_2)$ and $C(z_3)$ in complex plane is _____.

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24. Let α be the non-real 5th root of unity. If z_1 and z_2 are two complex numbers lying on $|z| = 2$, then the value of $\sum_{t=0}^4 |z_1 + \alpha^t z_2|^2$ is _____.

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25. Let $z_1, z_2, z_3 \in \mathbb{C}$ such that $|z_1| = |z_2| = |z_3| = |z_1 + z_2 + z_3| = 4$.

If $|z_1 - z_2| = |z_1 + z_3|$ and $z_2 \neq z_3$, then values of $|z_1 + z_2| \cdot |z_1 + z_3|$ is _____.

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26. Let $A(z_1)$ and $B(z_2)$ be lying on the curve $|z - 3 - 4i| = 5$, where $|z_1|$ is maximum. Now, $A(z_1)$ is rotated about the origin in anticlockwise direction through 90° reaching at $P(z_0)$. If A, B and P are collinear then the value of $(|z_0 - z_1| \cdot |z_0 - z_2|)$ is _____.

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27. If z_1, z_2, z_3 are three points lying on the circle $|z| = 2$ then the minimum value of the expression $|z_1| |z_2|^2 + |z_2 + z_3|^2 + |z_3 + z_1|^2 =$

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28. Minimum value of $|z_1 + 1| + |z_2 + 1| + |z_1 z_2 + 1|$ if $|z_1| = 1$ and $|z_2| = 1$ is _____.

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29. If $|z_1| = 2$ and $(1 - i)z_2 + (1 + i)\bar{z}_2 = 8\sqrt{2}$, then the minimum value of $|z_1 - z_2|$ is _____.

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30. Given that $1 + 2|z|^2 = |z^2 + 1|^2 + 2|z + 1|^2$, then the value of $|z(z + 1)|$ is _____.



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JEE Main Previous Year

1. If $\left| z - \frac{4}{z} \right| = 2$, then the maximum value of $|Z|$ is equal to (1) $\sqrt{3} + 1$ (2) $\sqrt{5} + 1$ (3) 2 (4) $2 + \sqrt{2}$

A. $\sqrt{3} + 1$

B. $\sqrt{5} + 1$

C. 2

D. $2 + \sqrt{2}$

Answer: B



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2. The number of complex numbers z such that $|z| = |z + 1| = |zi|$ equals

(1) 1 (2) 2 (3) ∞ (4) 0

A. ∞

B. 0

C. 1

D. 2

Answer: C



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3. Let α, β be real and z be a complex number. If $z^2 + \alpha z + \beta = 0$ has two distinct roots on the line $\text{Re } z = 1$, then it is necessary that : (1) $b \in (0, 1)$

(2) $b \in (-1, 0)$ (3) $|b| = 1$ (4) $b \in (1, \infty)$

A. $\beta \in (1, \infty)$

B. $\beta \in (0, 1)$

C. $\beta \in (-1, 0)$

D. $|\beta| = 1$

Answer: A



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4. If $\omega (\neq 1)$ is a cube root of unity, and $(1 + \omega)^7 = A + B\omega$. Then (A, B) equals

A. $(-1, 1)$

B. $(0, 1)$

C. $(1, 1)$

D. $(1, 0)$

Answer: C



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5. If $z \neq 1$ and $\frac{z^2}{z-1}$ is real, then the point represented by the complex number z lies (1) either on the real axis or on a circle passing through the origin (2) on a circle with centre at the origin (3) either on the real axis or on a circle not passing through the origin (4) on the imaginary axis

- A. either on the real axis or on a circle passing through the origin.
- B. on a circle with centre at the origin.
- C. either on the real axis or on a circle not passing through the origin .
- D. on the imaginary axis .

Answer: A

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6. If z is a complex number of unit modulus and argument θ , then

$\arg\left(\frac{1+z}{1+\bar{z}}\right)$ equal (1) $\frac{\pi}{2} - \theta$ (2) θ (3) $\pi - \theta$ (4) $-\theta$

A. $-\theta$

B. $\frac{\pi}{2} - \theta$

C. θ

D. $\pi - \theta$

Answer: C

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7. If z is a complex number such that $|z| \geq 2$ then the minimum value of

$$\left| z + \frac{1}{2} \right| \text{ is}$$

A. is equal to $\frac{5}{2}$

B. lies in the interval (1,2)

C. is strictly greater than $\frac{5}{2}$

D. is strictly greater than $\frac{3}{2}$ but less than $\frac{5}{2}$

Answer: B

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8. If z_1 and z_2 are two complex numbers such that $\frac{z_1 - 2z_2}{2 - z_1z_2}$ is unimodular

whereas z_1 is not unimodular then $|z_1| =$

A. Straight line parallel to x-axis

B. straight line parallel to y-axis

C. circle of radius 2

D. circle of radius $\sqrt{2}$

Answer: C



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9. A value of θ for which $\frac{2 + 3i\sin\theta}{1 - 2i\sin\theta}$ purely imaginary, is : (1) $\frac{\pi}{3}$ (2) $\frac{\pi}{6}$ (3)

$\sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$ (4) $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$

A. $\frac{\pi}{6}$

B. $\sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$

C. $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$

D. $\frac{\pi}{3}$

Answer: C



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10. Let ω be a complex number such that $2\omega + 1 = z$ where $z = \sqrt{-3}$.

If $\left|1111 - \omega^2 - 1\omega^21\omega^2\omega^7\right| = 3k$, then k is equal to : -1 (2) 1 (3) $-z$ (4) z

A. 1

B. z

C. $-z$

D. -1

Answer: B



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11. If $\alpha, \beta \in C$ are distinct roots of the equation $x^2 + 1 = 0$ then $\alpha^{101} + \beta^{107}$ is equal to

A. 2

B. -1

C. 0

D. 1

Answer: D



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1. Let $z = x + iy$ be a complex number where x and y are integers. Then, the area of the rectangle whose vertices are the roots of the equation $zz^3 + z\bar{z}^3 = 350$ is 48 (b) 32 (c) 40 (d) 80

A. 48

B. 32

C. 40

D. 80

Answer: A



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2. Let z be a complex number such that the imaginary part of z is nonzero and $a = z^2 + z + 1$ is real. Then a cannot take the value (A) -1 (B) 1 3 (C) 1 2 (D) 3 4

A. -1

B. $\frac{1}{3}$

C. $\frac{1}{2}$

D. $\frac{3}{4}$

Answer: D

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3. Let complex numbers α and $\frac{1}{\alpha}$ lies on circle $(x - x_0)^2 + (y - y_0)^2 = r^2$ and $(x - x_0)^2 + (y - y_0)^2 = 4r^2$ respectively. If

$z_0 = x_0 + iy_0$ satisfies the equation $2|z_0|^2 = r^2 + 2$ then $|\alpha|$ is equal to (a)

$\frac{1}{\sqrt{2}}$ (b) $\frac{1}{2}$ (c) $\frac{1}{\sqrt{7}}$ (d) $\frac{1}{3}$

A. $1/\sqrt{2}$

B. $1/2$

C. $1/\sqrt{7}$

D. $1/3$

Answer: C



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4. Let Z_1 and Z_2 , be two distinct complex numbers and let $w = (1 - t)z_1 + tz_2$ for some number "t" with $0 < t < 1$

A. $|z - z_1| + |z - z_2| = |z_1 - z_2|$

B. $(z - z_1) = (z - z_2)$

C. $\begin{vmatrix} z - z_1 & \bar{z} - \bar{z}_1 \\ z_2 - z_1 & \bar{z}_2 - \bar{z}_1 \end{vmatrix} = 0$

D. $\arg(z - z_1) = \arg(z_2 - z_1)$

Answer: A::C::D



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5. Let $w = (\sqrt{3} + \frac{i}{2})$ and $P = \{w^n : n = 1, 2, 3, \dots\}$, Further

$H_1 = \left\{z \in \mathbb{C} : \operatorname{Re}(z) > \frac{1}{2}\right\}$ and $H_2 = \left\{z \in \mathbb{C} : \operatorname{Re}(z) < -\frac{1}{2}\right\}$ Where \mathbb{C} is

set of all complex numbers. If $z_1 \in P \cap H_1, z_2 \in P \cap H_2$ and O represent

the origin, then $\angle Z_1 O Z_2 =$

A. $\pi/2$

B. $\pi/6$

C. $2\pi/3$

D. $5\pi/6$

Answer: C::D

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6. Let $a, b \in \mathbb{R}$ and $a^2 + b^2 \neq 0$. Suppose

$S = \left\{z \in \mathbb{C} : z = \frac{1}{a + ibt}, t \in \mathbb{R}, t \neq 0\right\}$, where $i = \sqrt{-1}$. If $z = x + iy$ and z in

S , then (x, y) lies on

A. the circle with radius $\frac{1}{2a}$ and centre $\left(\frac{1}{2a}, 0\right)$ for $a > 0, b \neq 0$

B. the circle with radius $-\frac{1}{2a}$ and centre $\left(-\frac{1}{2}, 0\right)$ $a < 0, b \neq 0$

C. the axis for $a \neq 0, b = 0$

D. the y-axis for $a = 0, b \neq 0$

Answer: A::C::D



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7. Let a, b, x and y be real numbers such that $a - b = 1$ and $y \neq 0$. If the

complex number $z = x + iy$ satisfies $\operatorname{Im}\left(\frac{az + b}{z + 1}\right) = y$, then which of the

following is (are) possible value(s) of x ? (a) $-1 - \sqrt{1 - y^2}$ (b) $1 + \sqrt{1 + y^2}$

(c) $-1 + \sqrt{1 - y^2}$ (d) $-1 - \sqrt{1 + y^2}$

A. $-1 - \sqrt{1 - y^2}$

B. $1 + \sqrt{1 + y^2}$

C. $1 - \sqrt{1 + y^2}$

$$D. -1 + \sqrt{1 - y^2}$$

Answer: A:D



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8. For a non-zero complex number z , let $\arg(z)$ denote the principal argument with $-\pi < \arg(z) \leq \pi$. Then, which of the following statement(s) is (are) FALSE? $\arg(-1, -i) = \frac{\pi}{4}$, where $i = \sqrt{-1}$ (b) The function $f: \mathbb{R} \rightarrow (-\pi, \pi]$, defined by $f(t) = \arg(-1 + it)$ for all $t \in \mathbb{R}$, is continuous at all points of \mathbb{R} , where $i = \sqrt{-1}$ (c) For any two non-zero complex numbers z_1 and z_2 , $\arg\left(\frac{z_1}{z_2}\right) - \arg(z_1) + \arg(z_2)$ is an integer multiple of 2π (d) For any three given distinct complex numbers z_1, z_2 and z_3 , the locus of the point z satisfying the condition $\arg\left(\frac{(z - z_1)(z_2 - z_3)}{(z - z_3)(z_2 - z_1)}\right) = \pi$, lies on a straight line

A. $\arg(-1 - i) = \frac{\pi}{4}$, where $i = \sqrt{-1}$

B. The function $f: \mathbb{R} \rightarrow (-\pi, \pi]$, defined by $f(t) = \arg(-1 + it)$ for all

$t \in \mathbb{R}$, is continuous at all points of \mathbb{R} , where $i = \sqrt{-1}$

C. For any two non-zero complex numbers z_1 and

z_2 , $\arg\left(\frac{z_1}{z_2}\right) - \arg(z_1) + \arg(z_2)$ is an integer multiple of 2π

D. For any three given distinct complex numbers z_1, z_2 and z_3 the

locus of the point z satisfying the condition $\left(\frac{(z - z_1)(z_2 - z_3)}{(z - z_3)(z_2 - z_1)}\right) = \pi$

, lies on a straight line.

Answer: A::B::D



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9. Let s, t, r be non-zero complex numbers and L be the set of solutions

$z = x + iy$ ($x, y \in \mathbb{R}$, $i = \sqrt{-1}$) of the equation $sz + tz + r = 0$, where

$z = x - iy$. Then, which of the following statement(s) is (are) TRUE? If L has

exactly one element, then $|s| \neq |t|$ (b) If $|s| = |t|$, then L has infinitely many

elements (c) The number of elements in $\ln\{z: |z - 1 + i| = 5\}$ is at most 2

(d) If L has more than one element, then L has infinitely many elements

A. If L has exactly one element, then $|s| \neq |t|$

B. If $|s| = |t|$ then L has infinitely many elements

C. The number of elements in $L \cap \{z: |z - 1 + i| = 5\}$ is at most 2

D. If L has most than one elements, then L has infinitely many elements.

Answer: A::C::D



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10. Let $S = S_1 \cap S_2 \cap S_3$, where

$$s_1 = \{z \in C: |z| < 4\}, S_2 = \left\{ z \in C: \ln \left[\frac{z - 1 + \sqrt{3}i}{1 - \sqrt{3}i} \right] > 0 \right\} \text{ and } S_3 = \{z \in C: \operatorname{Re} z > 0\}$$

A. $\frac{10\pi}{3}$

B. $\frac{20\pi}{3}$

C. $\frac{16\pi}{3}$

D. $\frac{32\pi}{3}$

Answer: B



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11. Let $S = S_1 \cap S_2 \cap S_3$, where $S_1 = \{z \in \mathbb{C} : |z| < 4\}$,

$$S_2 = \left\{ z \in \mathbb{C} : \operatorname{Im} \left[\frac{z - 1 + \sqrt{3}i}{1 - \sqrt{3}i} \right] > 0 \right\} \text{ and } S_3 = \{z \in \mathbb{C} : \operatorname{Re} z > 0\}$$

$$\min_{z \in S} |1 - 3i - z| =$$

A. $\frac{2 - \sqrt{3}}{2}$

B. $\frac{2 + \sqrt{3}}{2}$

C. $\frac{3 - \sqrt{3}}{2}$

D. $\frac{3 + \sqrt{3}}{2}$

Answer: C

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12. Let ω be the complex number $\cos\left(\frac{2\pi}{3}\right) + i\sin\left(\frac{2\pi}{3}\right)$. Then the number of distinct complex numbers z satisfying

$$\Delta = \begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0 \text{ is}$$

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13. If z is any complex number satisfying $|z - 3 - 2i| \leq 2$ then the maximum value of $|2z - 6 + 5i|$ is

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14. For any integer k , let $\alpha_k = \frac{\cos(k\pi)}{7} + i \sin. \frac{k\pi}{7}$, where $I = \sqrt{-1}$. Value of

the expression $\frac{\sum_{k=1}^{12} |\alpha_{k+1} - \alpha_k|}{\sum_{k=1}^3 |\alpha_{4k-1} - \alpha_{4k-2}|}$ is _____.

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Question Bank

1. It is given that complex numbers z_1 and z_2 satisfy $|z_1| = 2$ and $|z_2| = 3$.

If the included angle of their corresponding vectors is 60° then $\left| \frac{z_1 + z_2}{z_1 - z_2} \right|$

can be expressed on $\frac{\sqrt{N}}{7}$ where N is natural number then N equals

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2. If ω is any complex number such that $z\omega = |z|^2$ and $|z - \bar{z}| + |\omega + \bar{\omega}| = 4$,

then as ω varies, then the area of locus of z is

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3. If m is the minimum value of $|z| + |2z - \omega|$ where $|\omega| = 1$, then $4m$ is equal to

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4. If $(2 - 3i)$ is a root of the equation $x^3 - bx^2 + 25x + d = 0$ (where b and d are real and $i = \sqrt{-1}$), then value of b is equal to

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5. If the area 'bounded by the locus of z satisfying $\arg(z) = 0$,

$\operatorname{Im}\left(\frac{1 + \sqrt{3}i}{z}\right) = 0$ and $\arg(z - 2) = \frac{2\pi}{3}$ is \sqrt{k} , then k is equal to

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6. The circle $|z + 3| = 1$ touches $|z - \sqrt{7}i| = r$. Then sum of possible values of r is

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7. Let $i = \sqrt{-1}$. The absolute value of product of the real part of the roots of $z^2 - z = 5 - 5i$ is

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8. If $|z_1| = 1$, $|z_2| = 2$, $|z_3| = 3$ and $|9z_1z_2 + 4z_1z_3 + z_2z_3| = 12$ then the value of $|z_1 + z_2 + z_3|$ is equal to

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9. $\left[\frac{-1 + i\sqrt{3}}{2}\right]^6 + \left[\frac{-1 - i\sqrt{3}}{2}\right]^6 + \left[\frac{-1 + i\sqrt{3}}{2}\right]^5 + \left[\frac{-1 - i\sqrt{3}}{2}\right]^5$ is equal to

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10. Let $A = \{a \in \mathbb{R} \mid \text{the equation } (1 + 2i)x^3 - 2(3 + i)x^2 + (5 - 4i)x + 2a^2 = 0\}$ has at least one real root. Find the value of $\sum_{a \in A} a^2$.

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11. If $|Z - i| \leq 2$ and $Z_1 = 5 + 3i$, then the maximum value of $|iZ + Z_1|$ is

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12. If P is the affix of z in the Argand diagram and P moves so that $\frac{z - i}{z - 1}$ is always purely imaginary, then the locus of z is a circle whose radius is

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13. The imaginary part of complex number z satisfying $|z - 1 - 2i| \leq 1$ and having the least positive argument, is



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14. Number of complex numbers z satisfying $z^3 = \bar{z}$ is



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15. Let $z = 9 + bi$ where b is non zero real and $i^2 = -1$. If the imaginary part of z^2 and z^3 are equal, then b^2 equals



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16. The value of $e^{i\pi} \cdot (-i)$ is equal to



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17. Number of complex numbers z such that $|z| = 1$ (and) $\left| \frac{z}{\bar{z}} + \frac{\bar{z}}{z} \right| = 1$ is



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18. The straight line $(1 + 2i)z + (2i - 1)\bar{z} = 10i$ on the complex plane, has intercept on the imaginary axis equal to

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19. If m and n are the smallest positive integers satisfying the relation

$\left(2C(is)\frac{\pi}{6}\right)^m = \left(4C(is)\frac{\pi}{4}\right)^n$, then $(m + n)$ has the value equal to

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20. $\left(\sqrt{3}(3) + \left(\frac{5}{36}\right)i\right)^3$ is an integer where $i = \sqrt{-1}$. The absolute value of the integer is equal to

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21. If $x = a + bi$ is a complex number such that $x^2 = 3 + 4i$ and $x^3 = 2 + 11i$ where $i = \sqrt{-1}$, then $(a + b)$ equal to

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22. If the complex number z satisfies the condition $|z| \geq 3$, then the least value of $\left|z + \frac{1}{z}\right|$ is equal to

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23. Number of roots of $z^{201} = 7$ where $\operatorname{Re}(z) > 0$ is

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24. If $\left|\frac{z-1}{z-4}\right| = 2$ and $\left|\frac{w-4}{w-1}\right| = 2$, then the value of $|z-w|_{\max} + |z-w|_{\min}$ is

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25. If ω be a non-real cube root of unity, then the absolute value of

$$\cos \left[\left((1 - \omega)(1 - \omega^2) + (2 - \omega)(2 - \omega^2) \dots + (2017 - \omega)(2017 - \omega^2) \right) \cdot \frac{\pi}{2017} \right]$$

is

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26. If $0 \leq \arg z \leq \frac{\pi}{4}$, then the least value of $\sqrt{2}|2z - 4i|$ is

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27. If $z_1 \neq 0$ and z_2 be two complex numbers such that z_2 is a purely

imaginary number, then $\left| \frac{2z_1 + 3z_2}{2z_1 - 3z_2} \right|$ is equal to

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28. If $|z - 1| = 2$ and $|w - \vec{i}| = 3$, where $(i = \sqrt{-1})$ then the maximum value of $|z - w|$ is $a + \sqrt{2}$ then the value of a is

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29. If z_1, z_2, z_3 are the roots of the equation $z^3 - z^2(1 + 3i) + z(3i - 2) + 2 = 0$, then $Im(z_1) + Im(z_2) + Im(z_3)$ is

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30. Modulus of non-zero complex number z satisfying $z + \bar{z} = 0, |z| - 4zi = z^2$ is

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