



## MATHS

### BOOKS - CENGAGE MATHS (HINGLISH)

#### DIFFERENT PRODUCTS OF VECTORS AND THEIR GEOMETRICAL APPLICATIONS

##### Examples

1. Find the angle between the following pairs of vectors

$$3\hat{i} + 2\hat{j} - 6\hat{k}, 4\hat{i} - 3\hat{j} + \hat{k}, 2\hat{j} + 3\hat{k}, 3\hat{i} - 2\hat{j} + \hat{k}$$



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2. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-zero vectors such that  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c}$ , find the geometrical relation between the vectors.



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3. if  $\vec{r} \cdot \vec{i} = \vec{r} \cdot \vec{j} = \vec{r} \cdot \vec{k}$  and  $|\vec{r}| = 3$ , then find vector  $\vec{r}$ .



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4. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$ , then the value of  $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$  is



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5. if  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are mutually perpendicular vectors of equal magnitudes, then find the angle between vectors and  $\vec{a} + \vec{b} + \vec{c}$ .



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6. If  $|\vec{a}| + |\vec{b}| = |\vec{c}|$  and  $\vec{a} + \vec{b} = \vec{c}$  then find the angle between  $\vec{a}$  and  $\vec{b}$ .

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7. If three unit vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  satisfy  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ . Then find the angle between  $\vec{a}$  and  $\vec{b}$ .

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8. If  $\theta$  is the angle between the unit vectors  $\vec{a}$  and  $\vec{b}$ , then prove that

$$\text{i. } \cos\left(\frac{\theta}{2}\right) = \frac{1}{2} |\vec{a} + \vec{b}|$$

$$\text{ii. } \sin\left(\frac{\theta}{2}\right) = \frac{1}{2} |\vec{a} - \vec{b}|$$

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9. find the projection of the vector  $\hat{i} + 3\hat{j} + 7\hat{k}$  on the vector  $7\hat{i} - \hat{j} + 8\hat{k}$

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10. If the scalar projection of vector  $x\hat{i} - \hat{j} + \hat{k}$  on vector  $2\hat{i} - \hat{j} + 5\hat{k}$  is  $\frac{1}{\sqrt{30}}$ .

The find the value of x.

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11. If  $\vec{a} = x\hat{i} + (x - 1)\hat{j} + \hat{k}$  and  $\vec{b} = (x + 1)\hat{i} + \hat{j} + a\hat{k}$  make an acute angle  $\forall x \in R$ , then find the values of a.

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12. If  $\vec{a} \cdot \vec{i} = \vec{a} \cdot (\hat{i} + \hat{j}) = \vec{a} \cdot (\hat{i} + \hat{j} + \hat{k})$ . Then find the unit vector  $\vec{a}$ .

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13. Prove by vector method that  $\cos(A + B)\cos A \cos B - \sin A \sin B$

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14. In any triangle  $ABC$ , prove the projection formula  $a = b\cos C + c\cos B$  using vector method.

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15. Prove that an angle inscribed in a semi-circle is a right angle using vector method.

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16. Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle

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17. If  $a + 2b + 3c = 4$ , then find the least value of  $a^2 + b^2 + c^2$

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18. A unit vector  $a$  makes an angle  $\frac{\pi}{4}$  with z-axis. If  $a + i + j$  is a unit vector, then  $a$  can be equal to

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19. vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are of the same length and when taken pair-wise they form equal angles. If  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = \hat{j} + \hat{k}$  then find vector  $\vec{c}$ .

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20. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three mutually perpendicular unit vectors and  $\vec{d}$  is a unit vector which makes equal angular with  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ , then find the value of  $|\vec{a} + \vec{b} + \vec{c} + \vec{d}|^2$ .

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21. A particle acted on by constant forces  $4\vec{i} + \vec{j} - 3\vec{k}$  and  $3\vec{i} + \vec{j} - \vec{k}$  is displaced from the point  $\vec{i} + 2\vec{j} + 3\vec{k}$  to the point  $5\vec{i} + 4\vec{j} + \vec{k}$ . Find the total work done by the forces

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22. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are mutually perpendicular vectors of equal magnitude show that  $\vec{a} + \vec{b} + \vec{c}$  is equally inclined to  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$

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23. If  $\vec{a} = 4\hat{i} + 6\hat{j}$  and  $\vec{b} = 3\hat{i} + 4\hat{k}$  find the vector component of  $\vec{a}$  along  $\vec{b}$ .

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24. If  $|\vec{a}| = |\vec{b}| = |\vec{a} + \vec{b}| = 1$  then find the value of  $|\vec{a} - \vec{b}|$

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25. If  $\vec{a} = -\hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + 0\hat{j} + \hat{k}$  then find vector  $\vec{c}$  satisfying the following conditions, (i) that it is coplaner with  $\vec{a}$  and  $\vec{b}$ , (ii) that it is  $\perp$  to  $\vec{b}$  and (iii) that  $\vec{a} \cdot \vec{c} = 7$ .

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26. If  $\vec{a}, \vec{b}$  and  $\vec{c}$  are vectors such that  $|\vec{a}| = 3, |\vec{b}| = 4$  and  $|\vec{c}| = 5$  and  $(\vec{a} + \vec{b})$  is perpendicular to  $\vec{c}$ ,  $(\vec{a} + \vec{b} + \vec{c})$  is perpendicular to  $\vec{a}$  and  $(\vec{a} + \vec{b} + \vec{c})$  is perpendicular to  $\vec{b}$  then  $|\vec{a} + \vec{b} + \vec{c}| =$  (A)  $4\sqrt{3}$  (B)  $5\sqrt{2}$  (C) 2 (D) 12

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27. Prove that in a tetrahedron if two pairs of opposite edges are perpendicular, then the third pair is also perpendicular.

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28. In the isosceles triangle  $ABC$ ,  $\left| \vec{AB} \right| = \left| \vec{BC} \right| = 8$ , a point  $E$  divides  $AB$  internally in the ratio  $1:3$ , then the cosine of the angle between  $\vec{CE}$  and  $\vec{CA}$  is (where  $\left| \vec{CA} \right| = 12$ )

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29. An arc  $AC$  of a circle subtends a right angle at the center  $O$ . The point  $B$  divides the arc in the ratio  $1:2$ . If  $\vec{OA} = a$  and  $\vec{OB} = b$ , then the vector  $\vec{OC}$  in terms of  $a$  and  $b$ , is

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30. Vector  $\vec{OA} = \hat{i} + 2\hat{j} + 2\hat{k}$  turns through a right angle passing through the positive  $x$ -axis on the way. Show that the vector in its new position is

$$\frac{4\hat{i} - \hat{j} - \hat{k}}{\sqrt{2}}$$

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**31.** The base of the pyramid  $AOBC$  is an equilateral triangle  $OBC$  with each side equal to  $4\sqrt{2}$ ,  $O$  is the origin of reference,  $AO$  is perpendicular to the plane of  $OBC$  and  $|\vec{AO}| = 2$ . Then find the cosine of the angle between the skew straight lines, one passing through  $A$  and the midpoint of  $OB$  and the other passing through  $O$  and the midpoint of  $BC$ .

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**32.** Find  $|\vec{a} \times \vec{b}|$ , if  $\vec{a} = \hat{i} - 7\hat{j}$  and  $\vec{b} = 3\hat{i} - 2\hat{j} + 2\hat{k}$ .

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33. Let the vectors  $\vec{a}$  and  $\vec{b}$  be such that  $|\vec{a}| = 3$  and  $|\vec{b}| = \frac{\sqrt{2}}{3}$  then  $\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|}$  is a unit vector. If the angle between  $\vec{a}$  and  $\vec{b}$  is ?

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34. Prove that  $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2(\vec{a} \times \vec{b})$  also interpret this result.

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35. Let  $\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$ ,  $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$  and  $\vec{c} = 2\hat{i} - 2\hat{j} + 4\hat{k}$ . Find a vector  $\vec{d}$  which perpendicular to both  $\vec{a}$  and  $\vec{b}$  and  $|\vec{c} \cdot \vec{d}| = 15$ .

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36. If  $A, B$  and  $C$  are the vertices of a triangle  $ABC$ , then prove sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

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37. Using cross product of vectors, prove that

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

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38. Find a unit vector perpendicular to the plane determined by the points  $(1, -1, 2)$ ,  $(2, 0, -1)$  and  $(0, 2, 1)$

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39. If  $\vec{a}$  and  $\vec{b}$  are two vectors, then prove that  $(\vec{a} \times \vec{b})^2 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} \end{vmatrix}$

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40. If  $|\vec{a}| = 2$  then find the value of  $|\vec{a} \times \vec{i}|^2 + |\vec{a} \times \vec{j}|^2 + |\vec{a} \times \vec{k}|^2$



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41.  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$ ,  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$ ,  $\vec{a} \neq \vec{0}$ ,  $\vec{b} \neq \vec{0}$ ,  $\vec{a} \neq \lambda \vec{b}$  and  $\vec{a}$  is not perpendicular to  $\vec{b}$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .



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42.  $A, B, C$  and  $D$  are any four points in the space, then prove that

$$\left| \vec{AB} \times \vec{CD} + \vec{BC} \times \vec{AD} + \vec{CA} \times \vec{BD} \right| = 4 \text{ (area of } ABC \text{.)}$$



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43. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are the position vectors of the vertices  $A, B$  and  $C$  respectively, of  $\triangle ABC$ . Prove that the perpendicular distance of the

vertex  $A$  from the base  $BC$  of the triangle  $ABC$  is 
$$\frac{|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}|}{|\vec{c} - \vec{b}|}$$



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44. Using vectors, find the area of the triangle with vertices  $A(1, 1, 2)$ ,  $B(2, 3, 5)$  and  $C(1, 5, 5)$

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45. Find the area of the parallelogram whose adjacent sides are given by the vectors  $\vec{a} = \hat{i} - \hat{j} + 3\hat{k}$  and  $\vec{b} = 2\hat{i} - 7\hat{j} + \hat{k}$

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46. Area of a parallelogram, whose diagonals are  $3\hat{i} + \hat{j} - 2\hat{k}$  and  $\hat{i} - 3\hat{j} + 4\hat{k}$  will be:

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47. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three vectors such that  $\vec{a} \neq 0$ ,  $|\vec{a}| = |\vec{c}| = 1$ ,  $|\vec{b}| = 4$  and  $|\vec{b} \times \vec{c}| = \sqrt{15}$ . If  $\vec{b} - 2\vec{c} = \lambda\vec{a}$  then find the value of  $\lambda$ .

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48. Find the moment about  $(1,-1,-1)$  of the force  $3\hat{i} + 4\hat{j} - 5\hat{k}$  acting at  $(1,0,-2)$

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49. A rigid body is spinning about a fixed point  $(3,-2,-1)$  with an angular velocity of  $4 \text{ rad/s}$ , the axis of rotation being in the direction of  $(1,2,-2)$ . Find the velocity of the particle at point  $(4,1,1)$ .

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50. If  $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$  and  $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$  show that  $(\vec{a} - \vec{d})$  is parallel to  $(\vec{b} - \vec{c})$ . *It is given that  $\vec{a} \neq \vec{c}$  and  $\vec{b} \neq \vec{d}$ .*

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51. Show by a numerical example and geometrically also that  $\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$  does not imply  $\vec{b} = \vec{c}$ .

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52. If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are the position vectors of the vertices of a cycle quadrilateral ABCD, prove that

$$\frac{|\vec{a} \times \vec{b} + \vec{b} \times \vec{d} + \vec{d} \times \vec{a}|}{(\vec{b} - \vec{a}) \cdot (\vec{d} - \vec{a})} + \frac{|\vec{b} \times \vec{c} + \vec{c} \times \vec{d} + \vec{d} \times \vec{b}|}{(\vec{b} - \vec{c}) \cdot (\vec{d} - \vec{c})}$$

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53. The position vectors of the vertices of a quadrilateral with A as origin are  $B(\vec{b})$ ,  $D(\vec{d})$  and  $C(l\vec{b} + m\vec{d})$ . Prove that the area of the quadrilateral is  $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$ .

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54. Let  $\vec{a}$  and  $\vec{b}$  be unit vectors such that  $|\vec{a} + \vec{b}| = \sqrt{3}$ . Then find the value of  $(2\vec{a} + 5\vec{b}) \cdot (3\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

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55.  $\hat{u}$  and  $\hat{v}$  are two non-collinear unit vectors such that  $\left| \frac{\hat{u} + \hat{v}}{2} + \hat{u} \times \hat{v} \right| = 1$ .

Prove that  $|\hat{u} \times \hat{v}| = \left| \frac{\hat{u} - \hat{v}}{2} \right|$ .

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56. In a  $\triangle ABC$  points D, E, F are taken on the sides BC, CA and AB respectively such that  $\frac{BD}{DC} = \frac{CE}{EA} = \frac{AF}{FB} = n$  prove that

$$\triangle DEF = \frac{n^2 - n + 1}{(n + 1)^2} \triangle ABC$$

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57. Let A, B, C be points with position vectors  $2\hat{i} - \hat{j} + \hat{k}$ ,  $\hat{i} + 2\hat{j} + \hat{k}$  and  $3\hat{i} + \hat{j} + 2\hat{k}$  respectively. Find the shortest distance between point B and plane OAC.

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58. Let  $\vec{a} = x\hat{i} + 12\hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} + 2x\hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} + \hat{k}$ . If the ordered set  $[\vec{b} \vec{c} \vec{a}]$  is left handed, then find the value of x.

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59. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors, then find the value of

$$\frac{\vec{a} \cdot (\vec{b} \times \vec{c})}{\vec{b} \cdot (\vec{c} \times \vec{a})} + \frac{\vec{b} \cdot (\vec{c} \times \vec{a})}{\vec{c} \cdot (\vec{a} \times \vec{b})} + \frac{\vec{c} \cdot (\vec{b} \times \vec{a})}{\vec{a} \cdot (\vec{b} \times \vec{c})}$$

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60. If the vectors  $2\hat{i} - 3\hat{j}$ ,  $\hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelepiped, then find the volume of the parallelepiped.

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61. The position vectors of the four angular points of a tetrahedron are  $A(\hat{j} + 2\hat{k})$ ,  $B(3\hat{i} + \hat{k})$ ,  $C(4\hat{i} + 3\hat{j} + 6\hat{k})$  and  $D(2\hat{i} + 3\hat{j} + 2\hat{k})$ . Find the volume of the tetrahedron ABCD.

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62. Let  $\vec{a}, \vec{b}, \vec{c}$  be three unit vectors and  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c} = 0$ . If the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$  then find the value of  $|\vec{a} \vec{b} \vec{c}|$



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63. Prove that  $[\vec{a} + \vec{b} \vec{b} + \vec{c} \vec{c} + \vec{a}] = 2[\vec{a} \vec{b} \vec{c}]$



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64. Show that :  $[\vec{l} \vec{m} \vec{n}] [\vec{a} \vec{b} \vec{c}] = \begin{vmatrix} \vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c} \end{vmatrix}$



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65. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} - \hat{k}$ , then find the value of

$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix}$$



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66. The value of  $a$  so that the volume of parallelepiped formed by vectors

$\hat{i} + a\hat{j} + \hat{k}$ ,  $\hat{j} + a\hat{k}$ ,  $a\hat{i} + \hat{k}$  becomes minimum is (A)  $\sqrt{93}$  (B) 2 (C)  $\frac{1}{\sqrt{3}}$  (D) 3



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67. If  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  are three non coplanar vectors then

$(\vec{u} + \vec{v} - \vec{w}) \cdot (\vec{u} - \vec{c}) \times (\vec{v} - \vec{w})$  equals (A)  $\vec{u} \cdot \vec{v} \times \vec{w}$  (B)  $\vec{u} \cdot \vec{w} \times \vec{v}$  (C)

$3\vec{u} \cdot \vec{u} \times \vec{w}$  (D) 0



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68. If  $\vec{a}$  and  $\vec{b}$  are two vectors, such that  $|\vec{a} \times \vec{b}| = 2$ , then find the value of  $[\vec{a}\vec{b}\vec{a} \times \vec{b}]$

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69. Find the altitude of a parallelepiped whose three coterminous edges are vectors  $\vec{A} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{B} = 2\hat{i} + 4\hat{j} - \hat{k}$  and  $\vec{C} = \hat{i} + \hat{j} + 3\hat{k}$  with  $\vec{A}$  and  $\vec{B}$  as the sides of the base of the parallelepiped.

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70. If  $[\vec{a}\vec{b}\vec{c}] = 2$ , then find the value of  $[(\vec{a} + 2\vec{b} - \vec{c})(\vec{a} - \vec{b})(\vec{a} - \vec{b} - \vec{c})]$

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71. If  $\vec{a}, \vec{b}, \vec{c}$  are mutually perpendicular vectors and  $\vec{a} = \alpha(\vec{a} \times \vec{b}) + \beta(\vec{b} \times \vec{c}) + \gamma(\vec{c} \times \vec{a})$  and  $[\vec{a}\vec{b}\vec{c}] = 1$  then  $\vec{\alpha} + \vec{\beta} + \vec{\gamma} =$  (A)

$|\vec{a}|^2$  (B) -  $|\vec{a}|^2$  (C) 0 (D) none of these

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72. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar vectors, then prove that

$(\vec{a} \cdot \vec{d})(\vec{b} \times \vec{c}) + (\vec{b} \cdot \vec{d})(\vec{c} \times \vec{a}) + (\vec{c} \cdot \vec{d})(\vec{a} \times \vec{b})$  is independent of  $\vec{d}$

where  $\vec{d}$  is a unit vector.

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73. Prove that vectors  $\vec{u} = (al + a_1l_1)\hat{i} + (am + a_1m_1)\hat{j} + (an + a_1n_1)\hat{k}$

$\vec{v} = (bl + b_1l_1)\hat{i} + (bm + b_1m_1)\hat{j} + (bn + b_1n_1)\hat{k}$

$\vec{w} = (cl + c_1l_1)\hat{i} + (cm + c_1m_1)\hat{j} + (cn + c_1n_1)\hat{k}$

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74. Let  $G_1$ ,  $G_2$  and  $G_3$  be the centroids of the triangular faces OBC, OCA and OAB, respectively, of a tetrahedron OABC. If  $V_1$  denotes the volume of

the tetrahedron  $OABC$  and  $V_2$  that of the parallelepiped with  $OG_1, OG_2$  and  $OG_3$  as three concurrent edges, then prove that  $4V_1 = 9V_2$ .

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75. Prove that :  $\vec{i} \times (\vec{a} \times \vec{i}) + \vec{j} \times (\vec{a} \times \vec{j}) + \vec{k} \times (\vec{a} \times \vec{k}) = 2\vec{a}$

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76. If  $\hat{i} \times [(\vec{a} - \hat{j}) \times \hat{i}] \times [(\vec{a} - \hat{k}) \times \hat{j}] + \vec{k} \times [(\vec{a} - \vec{i}) \times \hat{k}] = 0$ , then find vector  $\vec{a}$ .

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77. Prove that:  $[\vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a}] = [\vec{a} \vec{b} \vec{c}]^2$

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78. Prove that:  $(\vec{b} \times \vec{c}) \cdot (\vec{a} \times \vec{d}) + (\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{d}) + (\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 0$

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79. If  $\vec{b}$  and  $\vec{c}$  are two non-collinear such that  $\vec{a} \perp (\vec{b} \times \vec{c})$ . Then prove that  $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{c})$  is equal to  $|\vec{a}|^2 (\vec{b} \cdot \vec{c})$ .

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80. Find the vector of length 3 unit which is perpendicular to  $\hat{i} + \hat{j} + \hat{k}$  and lies in the plane of  $\hat{i} + \hat{j} + \hat{k}$  and  $2\hat{i} - 3\hat{j}$

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81. Let  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  be the non-coplanar unit vectors. The angle between  $\hat{b}$  and  $\hat{c}$  is  $\alpha$ , between  $\hat{c}$  and  $\hat{a}$  is  $\beta$  and between  $\hat{a}$  and  $\hat{b}$  is  $\gamma$ . If

$A(\hat{a}\cos\alpha)$ ,  $B(\hat{b}\cos\beta)$  and  $C(\hat{c}\cos\gamma)$ , then show that in triangle ABC,

$$\frac{|\hat{a} \times (\hat{b} \times \hat{c})|}{\sin A} = \frac{|\hat{b} \times (\hat{c} \times \hat{a})|}{\sin B} = \frac{|\hat{c} \times (\hat{a} \times \hat{b})|}{\sin C} = \frac{\Pi |\hat{a} \times (\hat{b} \times \hat{c})|}{\sum \sin\alpha - \cos\beta \cdot \cos\gamma \hat{n}_1}$$

where  $\hat{n}_1 = \frac{\hat{b} \times \hat{c}}{|\hat{b} \times \hat{c}|}$ ,  $\hat{n}_2 = \frac{\hat{c} \times \hat{a}}{|\hat{c} \times \hat{a}|}$  and  $\hat{n}_3 = \frac{\hat{a} \times \hat{b}}{|\hat{a} \times \hat{b}|}$

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82. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors, then prove that

$$\frac{|\hat{a} \times (\hat{b} \times \hat{c})|}{\sin A} = \frac{|\hat{b} \times (\hat{c} \times \hat{a})|}{\sin B} = \frac{|\hat{c} \times (\hat{a} \times \hat{b})|}{\sin C} = \frac{\Pi |\hat{a} \times (\hat{b} \times \hat{c})|}{|\sum \sin\alpha \cos\beta \cos\gamma \hat{n}_1|}$$

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83. If  $\vec{b}$  is not perpendicular to  $\vec{c}$ . Then find the vector  $\vec{r}$  satisfying the equation  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  and  $\vec{r} \cdot \vec{c} = 0$

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84. If  $\vec{a}$  and  $\vec{b}$  are two given vectors and  $k$  is any scalar, then find the vector  $\vec{r}$  satisfying  $\vec{r} \times \vec{a} + k\vec{r} = \vec{b}$ .

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85. If  $\vec{r} \cdot \vec{a} = 0$ ,  $\vec{r} \cdot \vec{b} = 1$  and  $[\vec{r} \vec{a} \vec{b}] = 1$ ,  $\vec{a} \cdot \vec{b} \neq 0$ ,  $(\vec{a} \cdot \vec{b})^2 - |\vec{a}|^2 |\vec{b}|^2 = 1$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .

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86. if vector  $\vec{x}$  satisfying  $\vec{x} \times \vec{a} + (\vec{x} \cdot \vec{b})\vec{c} = \vec{d}$  is given by

$$\vec{x} = \lambda \vec{a} + \vec{a} \times \frac{\vec{a} \times \left( \vec{d} \times \vec{c} \right)}{(\vec{a} \cdot \vec{c})|\vec{a}|^2}$$

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87. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non coplanar and non zero vectors and  $\vec{r}$  is any vector in space then  $[\vec{c}\vec{r}\vec{b}]\vec{a} + p\vec{a}\vec{r}\vec{c}]\vec{b} + [\vec{b}\vec{r}\vec{a}]\vec{c} =$  (A)  $[\vec{a}\vec{b}\vec{c}]$  (B)  $[\vec{a}\vec{b}\vec{c}]\vec{r}$  (C)  $\frac{\vec{r}}{[\vec{a}\vec{b}\vec{c}]}$  (D)  $\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

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88. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non coplanar and unit vectors such that  $\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\vec{b} + \vec{c}}{\sqrt{92}}$  then the angle between  $\vec{a}$  and  $\vec{b}$  is (A)  $\frac{3\pi}{4}$  (B)  $\frac{\pi}{4}$  (C)  $\frac{\pi}{2}$  (D)  $\pi$

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89. Prove that

$$\vec{R} + \frac{[\vec{R} \cdot (\vec{\beta} \times (\vec{\beta} \times \vec{\alpha}))]\vec{\alpha}}{|\vec{\alpha} \times \vec{\beta}|^2} + \frac{[\vec{R} \cdot (\vec{\alpha} \times (\vec{\alpha} \times \vec{\beta}))]\vec{\beta}}{|\vec{\alpha} \times \vec{\beta}|^2} = \frac{[\vec{R}\vec{\alpha}\vec{\beta}](\vec{\alpha} \times \vec{\beta})}{|\vec{\alpha} \times \vec{\beta}|^2}$$

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90. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar non-zero vectors, then prove that

$$(\vec{a} \cdot \vec{a})\vec{b} \times \vec{c} + (\vec{a} \cdot \vec{b})\vec{c} \times \vec{a} + (\vec{a} \cdot \vec{c})\vec{a} \times \vec{b} = [\vec{b}\vec{c}\vec{a}]\vec{a}$$

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91. Find a set of vectors reciprocal to the set  $-\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} - \hat{j} + \hat{k}$ ,  $\hat{i} + \hat{j} + \hat{k}$

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92. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be a set of non-coplanar vectors and  $\vec{a}'$ ,  $\vec{b}'$  and  $\vec{c}'$  be its reciprocal set.

prove that 
$$\vec{a} = \frac{\vec{b}' \times \vec{c}'}{[\vec{a}' \vec{b}' \vec{c}']}, \vec{b} = \frac{\vec{c}' \times \vec{a}'}{[\vec{a}' \vec{b}' \vec{c}']} \text{ and } \vec{c} = \frac{\vec{a}' \times \vec{b}'}{[\vec{a}' \vec{b}' \vec{c}']}$$

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93. Prove that  $\vec{a}' \times \vec{b}' + \vec{b}' \times \vec{c}' + \vec{c}' \times \vec{a}' = \frac{\vec{a} + \vec{b} + \vec{c}}{[\vec{a}\vec{b}\vec{c}]}$

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94. If  $\vec{a}, \vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and  $\vec{a}', \vec{b}'$  and  $\vec{c}'$  constitute the reciprocal system of vectors, then prove that

i.  $\vec{r} = (\vec{r} \cdot \vec{a}')\vec{a} + (\vec{r} \cdot \vec{b}')\vec{b} + (\vec{r} \cdot \vec{c}')\vec{c}$

ii.  $\vec{r} = (\vec{r} \cdot \vec{a})\vec{a}' + (\vec{r} \cdot \vec{b})\vec{b}' + (\vec{r} \cdot \vec{c})\vec{c}'$

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95. Find the angle between the following pairs of vectors

$$3\hat{i} + 2\hat{j} - 6\hat{k}, 4\hat{i} - 3\hat{j} + \hat{k}, 3\hat{i} - 2\hat{j} + \hat{k}$$

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96. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non - zero vectors such that  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c}$ , the find the geometrical relation between the vectors.

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97. if  $\vec{r} \cdot \vec{i} = \vec{r} \cdot \vec{j} = \vec{r} \cdot \vec{k}$  and  $|\vec{r}| = 3$ , then find vector  $\vec{r}$ .

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98. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$ , then the value of  $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$  is

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99. if  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are mutally perpendicular vectors of equal magnitudes, then find the angle between vectors and  $\vec{a} + \vec{b} = \vec{c}$ .

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100. If  $|\vec{a}| = |\vec{b}| = |\vec{c}|$  and  $\vec{a} + \vec{b} = \vec{c}$  then find the angle between  $\vec{a}$  and  $\vec{b}$ .

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101. If three unit vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  satisfy  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ . Then find the angle between  $\vec{a}$  and  $\vec{b}$ .

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102. If  $\theta$  is the angle between the unit vectors  $\vec{a}$  and  $\vec{b}$ , then prove that

i.  $\cos\left(\frac{\theta}{2}\right) = \frac{1}{2}|\vec{a} + \vec{b}|$

ii.  $\sin\left(\frac{\theta}{2}\right) = \frac{1}{2}|\vec{a} - \vec{b}|$

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103. find the projection of the vector  $\hat{i} + 3\hat{j} = 7\hat{k}$  on the vector  $7\hat{i} - \hat{j} + 8\hat{k}$

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104. If the scalar projection of vector  $x\hat{i} - \hat{j} + \hat{k}$  on vector  $2\hat{i} - \hat{j} + 5\hat{k}$  is  $\frac{1}{\sqrt{30}}$ .

The find the value of x.

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105. If  $\vec{a} = x\hat{i} + (x - 1)\hat{j} + \hat{k}$  and  $\vec{b} = (x + 1)\hat{i} + \hat{j} + \hat{k}$  make an acute angle

$\forall x \in R$ , then find the values of a.

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106. If  $\vec{a} \cdot \vec{i} = \vec{a} \cdot (\hat{i} + \hat{j}) = \vec{a} \cdot (\hat{i} + \hat{j} + \hat{k})$ . Then find the unit vector  $\vec{a}$ .

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107. Prove by vector method that  $\cos(A + B)\cos A\cos B - \sin A\sin B$

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108. In any triangle  $ABC$ , prove the projection formula  $a = b\cos C + c\cos B$  using vector method.

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109. Prove that an angle inscribed in a semi-circle is a right angle using vector method.

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110. Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle

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111. If  $a + 2b + 3c = 4$ , then find the least value of  $a^2 + b^2 + c^2$ .

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112. A unit vector  $a$  makes an angle  $\frac{\pi}{4}$  with z-axis. If  $a + i + j$  is a unit vector, then  $a$  can be equal to

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113. vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are of the same length and when taken pair-wise they form equal angles. If  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = \hat{j} + \hat{k}$  then find vector  $\vec{c}$ .

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114. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three mutually perpendicular unit vectors and  $\vec{d}$  is a unit vector which makes equal angle with  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ , then find the value

of  $|\vec{a} + \vec{b} + \vec{c} + \vec{d}|^2$ .



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115. A particle acted on by constant forces  $4\hat{i} = \hat{j} - 3\hat{k}$  and  $3\hat{i} + \hat{j} - \hat{k}$  is displaced from the point  $\hat{i} + 2\hat{j} + 3\hat{k} \rightarrow 5\hat{i} + 4\hat{j} + \hat{k}$ . Find the work done



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116. If  $\vec{a}, \vec{b}, \vec{c}$  are mutually perpendicular vectors of equal magnitude show that  $\vec{a} + \vec{b} + \vec{c}$  is equally inclined to  $\vec{a}, \vec{b}$  and  $\vec{c}$



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117. If  $\vec{a} = 4\hat{i} + 6\hat{j}$  and  $\vec{b} = 3\hat{i} + 4\hat{k}$  find the vector component of  $\vec{a}$  along  $\vec{b}$ .



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118. If  $|\vec{a}| = |\vec{b}| = |\vec{a} + \vec{b}| = 1$  then find the value of  $|\vec{a} - \vec{b}|$

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119. If  $\vec{a} = -\hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + 0\hat{j} + \hat{k}$  then find vector  $\vec{c}$  satisfying the following conditions, (i) that it is coplaner with  $\vec{a}$  and  $\vec{b}$ , (ii) that it is  $\perp$  to  $\vec{b}$  and (iii) that  $\vec{a} \cdot \vec{c} = 7$ .

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120. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are vectors such that  $|\vec{a}| = 3$ ,  $|\vec{b}| = 4$  and  $|\vec{c}| = 5$ , and  $(\vec{a} + \vec{b})$  is perpendicular to  $\vec{c}$ ,  $(\vec{b} + \vec{c})$  is perpendicular to  $\vec{a}$  and  $(\vec{c} + \vec{a})$  is perpendicular to  $\vec{b}$ . Then find the value of  $|\vec{a} + \vec{b} + \vec{c}|$ .

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**121.** Prove that in a tetrahedron if two pairs of opposite edges are perpendicular, then the third pair is also perpendicular.

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**122.** In the isosceles triangle  $ABC$ ,  $\left| \vec{AB} \right| = \left| \vec{BC} \right| = 8$ , a point  $E$  divides  $AB$  internally in the ratio  $1:3$ , then the cosine of the angle between  $\vec{CE}$  and  $\vec{CA}$  is (where  $\left| \vec{CA} \right| = 12$ )

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**123.** An arc  $AC$  of a circle subtends a right angle at the center  $O$ . The point  $B$  divides the arc in the ratio  $1:2$ . If  $\vec{OA} = a$  &  $\vec{OB} = b$ . then the vector  $\vec{OC}$  in terms of  $a$  &  $b$ , is

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124. Vector  $\vec{OA} = \hat{i} + 2\hat{j} + 2\hat{k}$  turns through a right angle passing through the positive x-axis on the way. Show that the vector in its new position is  $\frac{4\hat{i} - \hat{j} - \hat{k}}{\sqrt{2}}$ .

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125. The base of the pyramid  $AOBC$  is an equilateral triangle  $OBC$  with each side equal to  $4\sqrt{2}$ ,  $O$  is the origin of reference,  $AO$  is perpendicular to the plane of  $OBC$  and  $|\vec{AO}| = 2$ . Then find the cosine of the angle between the skew straight lines, one passing through  $A$  and the midpoint of  $OB$  and the other passing through  $O$  and the midpoint of  $BC$ .

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126. Find  $\vec{a} \times \vec{b}$  and  $|\vec{a} \times \vec{b}|$  if  $\vec{a} = \hat{i} - 7\hat{j} + 7\hat{k}$  and  $\vec{b} = 3\hat{i} - 2\hat{j} + 2\hat{k}$ .

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127. Let the vectors  $\vec{a}$  and  $\vec{b}$  be such that  $|\vec{a}| = 3$  and  $|\vec{b}| = \frac{\sqrt{2}}{3}$  then  $\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|}$  is a unit vector. If the angle between  $\vec{a}$  and  $\vec{b}$  is ?

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128. Prove that  $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2(\vec{a} \times \vec{b})$  also interpret this result.

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129. Let  $\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$ ,  $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$  and  $\vec{c} = 2\hat{i} - 2\hat{j} + 4\hat{k}$ . Find a vector  $\vec{d}$  which perpendicular to both  $\vec{a}$  and  $\vec{b}$  and  $\vec{c} \cdot \vec{d} = 15$ .

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130. If  $A, B$  and  $C$  are the vertices of a triangle  $ABC$ , then prove sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

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**131.** Using cross product of vectors, prove that

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

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**132.** Find a unit vector perpendicular to the plane determined by the points  $(1, -1, 2)$ ,  $(2, 0, -1)$  and  $(0, 2, 1)$

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**133.** If  $\vec{a}$  and  $\vec{b}$  are two vectors, then prove that

$$(\vec{a} \times \vec{b})^2 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} \end{vmatrix}$$

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134. If  $|\vec{a}| = 2$  then find the value of  $|\vec{a} \times \vec{i}|^2 + |\vec{a} \times \vec{j}|^2 + |\vec{a} \times \vec{k}|^2$

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135.  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$ ,  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$ ,  $\vec{a} \neq \vec{0}$ ,  $\vec{b} \neq \vec{0}$ ,  $\vec{a} \neq \lambda \vec{b}$  and  $\vec{a}$  is not perpendicular to  $\vec{b}$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .

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136.  $A, B, C$  and  $D$  are any four points in the space, then prove that

$$\left| \vec{AB} \times \vec{CD} + \vec{BC} \times \vec{AD} + \vec{CA} \times \vec{BD} \right| = 4 \text{ (area of } ABC \text{.)}$$

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137. If  $\vec{a}, \vec{b}$  and  $\vec{c}$  are the position vectors of the vertices  $A, B$  and  $C$  respectively, of  $\triangle ABC$ . Prove that the perpendicular distance of the

vertex A from the base BC of the triangle ABC is  $\frac{|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}|}{|\vec{c} - \vec{b}|}$

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**138.** Using vectors, find the area of the triangle with vertices  $A(1, 1, 2)$ ,  $B(2, 3, 5)$  and  $C(1, 5, 5)$

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**139.** Find the area of the parallelogram whose adjacent sides are given by the vectors  $\vec{a} = \hat{i} - \hat{j} + 3\hat{k}$  and  $\vec{b} = 2\hat{i} - 7\hat{j} + \hat{k}$

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**140.** find the area of a parallelogram whose diagonals are  $\vec{a} = 3\hat{i} + \hat{j} - 2\hat{k}$  and  $\vec{b} = \hat{i} - 3\hat{j} + 4\hat{k}$ .

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**141.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three vectors such that  $\vec{a} \neq 0$ ,  $|\vec{a}| = |\vec{c}| = 1$ ,  $|\vec{b}| = 4$  and  $|\vec{b} \times \vec{c}| = \sqrt{15}$ . If  $\vec{b} - 2\vec{c} = \lambda\vec{a}$  then find the value of  $\lambda$ .



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**142.** Find the moment about  $(1,-1,-1)$  of the force  $3\hat{i} + 4\hat{j} - 5\hat{k}$  acting at  $(1,0,-2)$



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**143.** A rigid body is spinning about a fixed point  $(3,-2,-1)$  with an angular velocity of  $4$  rad/s, the axis of rotation being in the direction of  $(1,2,-2)$ . Find the velocity of the particle at point  $(4,1,1)$ .



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144. If  $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$  and  $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$  show that  $(\vec{a} - \vec{d})$  is parallel to  $(\vec{b} - \vec{c})$ . It is given that  $\vec{a} \neq \vec{c}$  and  $\vec{b} \neq \vec{d}$ .

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145. Show by a numerical example and geometrically also that  $\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$  does not imply  $\vec{b} = \vec{c}$ .

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146. If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are the position vectors of the vertices of a cycle quadrilateral ABCD, prove that

$$\frac{|\vec{a} \times \vec{b} + \vec{b} \times \vec{d} + \vec{d} \times \vec{a}|}{(\vec{b} - \vec{a}) \cdot (\vec{d} - \vec{a})} + \frac{|\vec{b} \times \vec{c} + \vec{c} \times \vec{d} + \vec{d} \times \vec{b}|}{(\vec{b} - \vec{c}) \cdot (\vec{d} - \vec{c})}$$

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147. The position vectors of the vertices of a quadrilateral with A as origin are  $B(\vec{b})$ ,  $D(\vec{d})$  and  $C(l\vec{b} + m\vec{d})$ . Prove that the area of the quadrilateral is  $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$ .

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148. Let  $\vec{a}$  and  $\vec{b}$  be unit vectors such that  $|\vec{a} + \vec{b}| = \sqrt{3}$ , then the value of  $(2\vec{a} + 5\vec{b}) \cdot (3\vec{a} + \vec{b} + \vec{a} \times \vec{b}) =$

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149.  $\hat{u}$  and  $\hat{v}$  are two non-collinear unit vectors such that  $\left| \frac{\hat{u} + \hat{v}}{2} + \hat{u} \times \hat{v} \right| = 1$ . Prove that  $|\hat{u} \times \hat{v}| = \left| \frac{\hat{u} - \hat{v}}{2} \right|$

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150. In a  $\triangle ABC$  points D, E, F are taken on the sides BC, CA and AB respectively such that  $\frac{BD}{DC} = \frac{CE}{EA} = \frac{AF}{FB} = n$  prove that  $\triangle DEF = \frac{n^2 - n + 1}{(n + 1)^2} \triangle ABC$

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151. Let A, B, C be points with position vectors  $2\hat{i} - \hat{j} + \hat{k}$ ,  $\hat{i} + 2\hat{j} + \hat{k}$  and  $3\hat{i} + \hat{j} + 2\hat{k}$  respectively. Find the shortest distance between point B and plane OAC.

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152. Let  $\vec{a} = x\hat{i} + 12\hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} + 2x\hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} + \hat{k}$ . If the ordered set  $[\vec{b} \vec{c} \vec{a}]$  is left handed, then find the value of x.

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153. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors, then find the value of

$$\frac{\vec{a} \cdot (\vec{b} \times \vec{c})}{\vec{b} \cdot (\vec{c} \times \vec{a})} + \frac{\vec{b} \cdot (\vec{c} \times \vec{a})}{\vec{c} \cdot (\vec{a} \times \vec{b})} + \frac{\vec{c} \cdot (\vec{b} \times \vec{a})}{\vec{a} \cdot (\vec{b} \times \vec{c})}$$



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154. If the vectors  $2\hat{i} - 3\hat{j}$ ,  $\hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelepiped, then find the volume of the parallelepiped.



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155. The position vectors of the four angular points of a tetrahedron are  $A(\hat{j} + 2\hat{k})$ ,  $B(3\hat{i} + \hat{k})$ ,  $C(4\hat{i} + 3\hat{j} + 6\hat{k})$  and  $D(2\hat{i} + 3\hat{j} + 2\hat{k})$ . Find the volume of the tetrahedron ABCD.



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156. Let  $\vec{a}, \vec{b}, \vec{c}$  be three unit vectors and  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c} = 0$ . If the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$  then find the value of  $|\vec{a} \vec{b} \vec{c}|$



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157. Prove that  $[\vec{a} + \vec{b} \vec{b} + \vec{c} \vec{c} + \vec{a}] = 2[\vec{a} \vec{b} \vec{c}]$



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158. Show that :  $[\vec{l} \vec{m} \vec{n}] [\vec{a} \vec{b} \vec{c}] = \begin{vmatrix} \vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c} \end{vmatrix}$



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159. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} - \hat{k}$ , then find the value of

$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix}$$



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160. find the value of  $a$  so that the volume of the parallelepiped formed by vectors  $\hat{i} + a\hat{j} + \hat{k}$ ,  $\hat{j} + a\hat{k}$  and  $a\hat{i} + \hat{k}$  becomes minimum.



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161. If  $\vec{u}$ ,  $\vec{v}$ , and  $\vec{w}$  are three non-coplanar vectors, then prove that

$$(\vec{u} + \vec{v} - \vec{w}) \cdot (\vec{u} - \vec{v}) \times (\vec{v} - \vec{w}) = \vec{u} \cdot \vec{v} \times \vec{w}$$



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162. If  $\vec{a}$  and  $\vec{b}$  are two vectors, such that  $|\vec{a} \times \vec{b}| = 2$ , then find the value of  $[\vec{a}\vec{b}\vec{a} \times \vec{b}]$

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163. Find the altitude of a parallelepiped whose three coterminous edges are vectors  $\vec{A} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{B} = 2\hat{i} + 4\hat{j} - \hat{k}$  and  $\vec{C} = \hat{i} + \hat{j} + 3\hat{k}$  with  $\vec{A}$  and  $\vec{B}$  as the sides of the base of the parallelepiped.

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164. If  $[\vec{a}\vec{b}\vec{c}] = 2$ , then find the value of  $[(\vec{a} + 2\vec{b} - \vec{c})(\vec{a} - \vec{b})(\vec{a} - \vec{b} - \vec{c})]$

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165. If  $\vec{a}, \vec{b}, \vec{c}$  are mutually perpendicular vectors and  $\vec{a} = \alpha(\vec{a} \times \vec{b}) + \beta(\vec{b} \times \vec{c}) + \gamma(\vec{c} \times \vec{a})$  and  $[\vec{a}\vec{b}\vec{c}] = 1$  then  $\vec{\alpha} + \vec{\beta} + \vec{\gamma} =$  (A)

$|\vec{a}|^2$  (B)  $-\ |\vec{a}|^2$  (C) 0 (D) none of these

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166. If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are non-coplanar vectors, then prove that

$(\vec{a} \cdot \vec{d})(\vec{b} \times \vec{c}) + (\vec{b} \cdot \vec{d})(\vec{c} \times \vec{a}) + (\vec{c} \cdot \vec{d})(\vec{a} \times \vec{b})$  is independent of  $\vec{d}$

where  $\vec{d}$  is a unit vector.

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167. Prove that vectors

$$\vec{u} = (al + a_1l_1)\hat{i} + (am + a_1m_1)\hat{j} + (an + a_1n_1)\hat{k}$$

$$\vec{v} = (bl + b_1l_1)\hat{i} + (bm + b_1m_1)\hat{j} + (bn + b_1n_1)\hat{k}$$

$$\vec{w} = (wl + c_1l_1)\hat{i} + (cm + c_1m_1)\hat{j} + (cn + c_1n_1)\hat{k}$$

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**168.** Let  $G_1, G_2$  and  $G_3$  be the centroids of the triangular faces OBC, OCA and OAB, respectively, of a tetrahedron OABC. If  $V_1$  denotes the volume of the tetrahedron OABC and  $V_2$  that of the parallelepiped with  $OG_1, OG_2$  and  $OG_3$  as three concurrent edges, then prove that  $4V_2 = 9V_1$ .



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**169.** Prove that  $\hat{i} \times (\vec{a} \times \vec{i}) + \hat{j} \times (\vec{a} \times \vec{j}) + \hat{k} \times (\vec{a} \times \vec{k}) = 2\vec{a}$



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**170.** If  $\hat{i} \times [(\vec{a} - \hat{j}) \times \hat{i}] + \hat{j} \times [(\vec{a} - \hat{k}) \times \hat{j}] + \hat{k} \times [(\vec{a} - \hat{i}) \times \hat{k}] = 0$ , then find vector  $\vec{a}$ .



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171. Prove that:  $[\vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a}] = [\vec{a} \vec{b} \vec{c}]^2$

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172. For any four vectors prove that

$$(\vec{b} \times \vec{c}) \cdot (\vec{a} \times \vec{d}) + (\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{d}) + (\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 0$$

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173. If  $\vec{b}$  and  $\vec{c}$  are two non-collinear such that  $\vec{a} \perp (\vec{b} \times \vec{c})$ . Then prove that  $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{c})$  is equal to  $|\vec{a}|^2(\vec{b} \cdot \vec{c})$ .

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174. Find the vector of length 3 unit which is perpendicular to  $\hat{i} + \hat{j} + \hat{k}$  and lies in the plane of  $\hat{i} + \hat{j} + \hat{k}$  and  $2\hat{i} - 3\hat{j}$

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**175.** Let  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  be the non-coplanar unit vectors. The angle between  $\hat{b}$  and  $\hat{c}$  is  $\alpha$ , between  $\hat{c}$  and  $\hat{a}$  is  $\beta$  and between  $\hat{a}$  and  $\hat{b}$  is  $\gamma$ . If

$A(\hat{a}\cos\alpha)$ ,  $B(\hat{b}\cos\beta)$  and  $C(\hat{c}\cos\gamma)$ , then show that in triangle ABC,

$$\frac{|\hat{a} \times (\hat{b} \times \hat{c})|}{\sin A} = \frac{|\hat{b} \times (\hat{c} \times \hat{a})|}{\sin B} = \frac{|\hat{c} \times (\hat{a} \times \hat{b})|}{\sin C} = \frac{\Pi |\hat{a} \times (\hat{b} \times \hat{c})|}{\Sigma \sin\alpha - \cos\beta \cdot \cos\gamma \hat{n}_1}$$

where  $\hat{n}_1 = \frac{\hat{b} \times \hat{c}}{|\hat{b} \times \hat{c}|}$ ,  $\hat{n}_2 = \frac{\hat{c} \times \hat{a}}{|\hat{c} \times \hat{a}|}$  and  $\hat{n}_3 = \frac{\hat{a} \times \hat{b}}{|\hat{a} \times \hat{b}|}$

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**176.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors, then prove that

$$\frac{|\hat{a} \times (\hat{b} \times \hat{c})|}{\sin A} = \frac{|\hat{b} \times (\hat{c} \times \hat{a})|}{\sin B} = \frac{|\hat{c} \times (\hat{a} \times \hat{b})|}{\sin C} = \frac{\Pi |\hat{a} \times (\hat{b} \times \hat{c})|}{|\Sigma \sin\alpha \cos\beta \cos\gamma \hat{n}_1|}$$

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177. If  $\vec{b}$  is not perpendicular to  $\vec{c}$ . Then find the vector  $\vec{r}$  satisfying the equation  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  and  $\vec{r} \cdot \vec{c} = 0$

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178. If  $\vec{a}$  and  $\vec{b}$  are two given vectors and  $k$  is any scalar, then find the vector  $\vec{r}$  satisfying  $\vec{r} \times \vec{a} + k\vec{r} = \vec{b}$ .

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179. If  $\vec{r} \cdot \vec{a} = 0$ ,  $\vec{r} \cdot \vec{b} = 1$  and  $[\vec{r} \vec{a} \vec{b}] = 1$ ,  $\vec{a} \cdot \vec{b} \neq 0$ ,  $(\vec{a} \cdot \vec{b})^2 - |\vec{a}|^2 |\vec{b}|^2 = 1$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .

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180. if vector  $\vec{x}$  satisfying  $\vec{x} \times \vec{a} + (\vec{x} \cdot \vec{b})\vec{c} = \vec{d}$  is given by

$$\vec{x} = \lambda \vec{a} + \vec{a} \times \frac{\vec{a} \times (\vec{d} \times \vec{c})}{(\vec{a} \cdot \vec{c})|\vec{a}|^2}$$

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181.  $\vec{a}, \vec{b}$  and  $\vec{c}$  are three non-coplanar vectors and  $\vec{r}$  is any arbitrary vector. Prove that  $[\vec{b}\vec{c}\vec{r}]\vec{a} + [\vec{c}\vec{a}\vec{r}]\vec{b} + [\vec{a}\vec{b}\vec{r}]\vec{c} = [\vec{a}\vec{b}\vec{c}]\vec{r}$ .

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182. If  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non-coplanar unit vectors such that

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\vec{b} \times \vec{c}}{\sqrt{2}}, \vec{b} \text{ and } \vec{c} \text{ are non-parallel, then prove that the}$$

angle between  $\vec{a}$  and  $\vec{b}$  is  $3\pi/4$

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183.

Prove

that

$$\vec{R} + \frac{[\vec{R} \cdot (\vec{\beta} \times (\vec{\beta} \times \vec{\alpha}))] \vec{\alpha}}{|\vec{\alpha} \times \vec{\beta}|^2} + \frac{[\vec{R} \cdot (\vec{\alpha} \times (\vec{\alpha} \times \vec{\beta}))] \vec{\beta}}{|\vec{\alpha} \times \vec{\beta}|^2} = \frac{[\vec{R} \vec{\alpha} \vec{\beta}] (\vec{\alpha} \times \vec{\beta})}{|\vec{\alpha} \times \vec{\beta}|^2}$$



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184. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar non-zero vectors, then prove that  $(\vec{a} \cdot \vec{a})\vec{b} \times \vec{c} + (\vec{a} \cdot \vec{b})\vec{c} \times \vec{a} + (\vec{a} \cdot \vec{c})\vec{a} \times \vec{b} = [\vec{b} \vec{c} \vec{a}] \vec{a}$



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185. Find a set of vectors reciprocal to the set  $-\hat{i} + \hat{j} + \hat{k}, \hat{i} + \hat{k}, \hat{i} + \hat{j} + \hat{k}$



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186. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be a set of non-coplanar vectors and  $\vec{a}'$ ,  $\vec{b}'$  and  $\vec{c}'$  be its reciprocal set.

prove that  $\vec{a} = \frac{\vec{b}' \times \vec{c}'}{[\vec{a}' \vec{b}' \vec{c}]}$ ,  $\vec{b} = \frac{\vec{c}' \times \vec{a}'}{[\vec{a}' \vec{b}' \vec{c}]}$  and  $\vec{c} = \frac{\vec{a}' \times \vec{b}'}{[\vec{a}' \vec{b}' \vec{c}]}$

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**187.** If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{a}', \vec{b}', \vec{c}'$  are reciprocal system of vectors, then prove

that  $\vec{a}' \times \vec{b}' + \vec{b}' \times \vec{c}' + \vec{c}' \times \vec{a}' = \frac{\vec{a} + \vec{b} + \vec{c}}{[\vec{a} \vec{b} \vec{c}]}$

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**188.** If  $\vec{a}, \vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and  $\vec{a}', \vec{b}'$  and  $\vec{c}'$  constitute the reciprocal system of vectors, then prove that

i.  $\vec{r} = (\vec{r} \cdot \vec{a}')\vec{a} + (\vec{r} \cdot \vec{b}')\vec{b} + (\vec{r} \cdot \vec{c}')\vec{c}$

ii.  $\vec{r} = (\vec{r} \cdot \vec{a})\vec{a}' + (\vec{r} \cdot \vec{b})\vec{b}' + (\vec{r} \cdot \vec{c})\vec{c}'$

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1. Find  $|\vec{a}|$  and  $|\vec{b}|$  if  $(\vec{a}+\vec{b})\cdot(\vec{a}-\vec{b})=8$  and  $|\vec{a}|=8|\vec{b}|$ .

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2. Show that  $|\vec{a}|\vec{b} + |\vec{b}|\vec{a}$  is perpendicular to  $|\vec{a}|\vec{b} - |\vec{b}|\vec{a}$  for any two non zero vectors  $\vec{a}$  and  $\vec{b}$ .

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3. If the vectors  $A, B, C$  of a triangle  $ABC$  are  $(1, 2, 3), (-1, 0, 0), (0, 1, 2)$ , respectively then find  $\angle ABC$ .

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4. If  $|\vec{a}| = 3, |\vec{b}| = 4$  and the angle between  $\vec{a}$  and  $\vec{b}$  is  $120^\circ$ . Then find the value of  $|4\vec{a} + 3\vec{b}|$





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5. If vectors  $\hat{i} - 2x\hat{j} - 3y\hat{k}$  and  $\hat{i} + 3x\hat{j} + 2y\hat{k}$  are orthogonal to each other, then find the locus of the point  $(x,y)$ .



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6. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be pairwise mutually perpendicular vectors, such that  $|\vec{a}| = 1$ ,  $|\vec{b}| = 2$ ,  $|\vec{c}| = 2$ , then find the length of  $\vec{a} + \vec{b} + \vec{c}$ .



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7. If  $\vec{a} + \vec{b} + \vec{c} = 0$ ,  $|\vec{a}| = 3$ ,  $|\vec{b}| = 5$ ,  $|\vec{c}| = 7$ , then find the angle between  $\vec{a}$  and  $\vec{b}$ .



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8. If the angle between unit vectors  $\vec{a}$  and  $\vec{b}$  is  $60^\circ$ . Then find the value of  $|\vec{a} - \vec{b}|$ .

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9. Let  $\vec{u} = h\hat{i} + \hat{j}$ ,  $\vec{v} = \hat{i} - \hat{j}$  and  $\vec{w} = \hat{i} + 2\hat{j} + 3\hat{k}$ . If  $\hat{n}$  is a unit vector such that  $\vec{u} \cdot \hat{n} = 0$  and  $\vec{v} \cdot \hat{n} = 0$ ,  $|\vec{w} \cdot \hat{n}|$  is equal to (A) 0 (B) 1 (C) 2 (D) 3

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10.  $A, B, C, D$  are any four points, prove that  $\vec{AB}\vec{CD} + \vec{BC}\vec{AD} + \vec{CA}\vec{BD} = 0$ .

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11.  $P(1, 0, -1), Q(2, 0, -3), R(-1, 2, 0)$  and  $S(-2, -1, 1)$ , then find the projection length of  $\vec{PQ}$  on  $\vec{RS}$ .

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12. If the vectors  $3\vec{p} + \vec{q}$ ,  $5\vec{p} - 3\vec{q}$  and  $2\vec{p} + \vec{q}$ ,  $4\vec{p} - 2\vec{q}$  are pairs of mutually perpendicular vectors, then find the angle between vectors  $\vec{p}$  and  $\vec{q}$ .

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13. Let  $\vec{A}$  and  $\vec{B}$  be two non-parallel unit vectors in a plane. If  $(\alpha\vec{A} + \vec{B})$  bisects the internal angle between  $\vec{A}$  and  $\vec{B}$  then find the value of  $\alpha$ .

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14. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = \vec{x}$ ,  $\vec{a} \cdot \vec{x} = 1$ ,  $\vec{b} \cdot \vec{x} = \frac{3}{2}$ ,  $|\vec{x}| = 2$  then find the angle between  $\vec{c}$  and  $\vec{x}$ .

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15. If  $\vec{a}$  and  $\vec{b}$  are unit vectors, then find the greatest value of  $|\vec{a} + \vec{b}| + |\vec{a} - \vec{b}|$ .

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16. Constant forces  $P_1 = \hat{i} - \hat{j} + \hat{k}$ ,  $P_2 = -\hat{i} + 2\hat{j} - \hat{k}$  and  $P_3 = \hat{j} - \hat{k}$  act on a particle at a point A. Determine the work done when particle is displaced from position  $A(4\hat{i} - 3\hat{j} - 2\hat{k})$  to  $B(6\hat{i} + \hat{j} - 3\hat{k})$

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17. Find  $|\vec{a}|$  and  $|\vec{b}|$  if  $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = 8$  and  $|\vec{a}| = 8|\vec{b}|$ .

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18. If  $A, B, C, D$  are four distinct point in space such that  $AB$  is not perpendicular to  $CD$  and satisfies



$\vec{AB}\vec{CD} = k\left(|\vec{AD}|^2 + |\vec{BC}|^2 - |\vec{AC}|^2 = |\vec{BD}|^2\right)$ , then find the value of  $k$

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19. If  $\vec{a} = 2\hat{i} + 3\hat{j} - 5\hat{k}$ ,  $\vec{b} = m\hat{i} + n\hat{j} + 12\hat{k}$  and  $\vec{a} \times \vec{b} = \vec{0}$  then find  $(m,n)$

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20. Find  $\vec{a} \cdot \vec{b}$  if  $|\vec{a}|=2$ ,  $|\vec{b}|=5$ ,  $a$  and  $|\vec{a} \times \vec{b}|=8$

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21. If  $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} \neq 0$  where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are coplanar vectors, then for some scalar  $k$  prove that  $\vec{a} + \vec{c} = k\vec{b}$ .

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22. If  $\vec{a} = 2\vec{j} + 3\vec{j} - \vec{k}$ ,  $\vec{b} = -\vec{i} + 2\vec{j} - 4\vec{k}$  and  $\vec{c} = \vec{i} + \vec{j} + \vec{k}$ , then find the value of  $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{c})$



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23. If the vectors  $\vec{a}$ ,  $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$  and  $\vec{b} = \hat{j}$  are such that  $\vec{a}$ ,  $\vec{c}$  and  $\vec{b}$  form a right handed system then  $\vec{c}$  is (A)  $z\hat{i} - x\hat{k}$  (B)  $\vec{0}$  (C)  $y\hat{j}$  (D)  $-z\hat{i} + x\hat{k}$



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24. given that  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c}$ ,  $\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$  and  $\vec{a}$  is not a zero vector. Show that  $\vec{b} = \vec{c}$ .



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25. Show that  $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2\vec{a} \times \vec{b}$  and give a geometrical interpretation of it.



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26. If  $\vec{x}$  and  $\vec{y}$  are unit vectors and  $|\vec{z}| = \frac{2}{\sqrt{7}}$  such that  $\vec{z} + \vec{z} \times \vec{x} = \vec{y}$  then find the angle  $\theta$  between  $\vec{x}$  and  $\vec{z}$



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27. prove that  $(\vec{a} \cdot \hat{i})(\vec{a} \times \hat{i}) + (\vec{a} \cdot \hat{j})(\vec{a} \times \hat{j}) + (\vec{a} \cdot \hat{k})(\vec{a} \times \hat{k}) = \vec{0}$



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28. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-zero vectors such that  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$  and  $\lambda \vec{b} \times \vec{a} \times \vec{a} + \vec{b} \times \vec{c} + \vec{c} + \vec{a} = \vec{0}$  then find the value of  $\lambda$ .



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29. A particle has an angular speed of 3 rad/s and the axis of rotation passes through the points  $(1, 1, 2)$  and  $(1, 2, -2)$ . Find the velocity of the particle at point  $P(3, 6, 4)$ .

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30. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be unit vectors such that  $\vec{a} \cdot \vec{b} = 0 = \vec{a} \cdot \vec{c}$ . If the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{6}$  then find  $\vec{a}$ .

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31. If  $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2 = 144$  and  $|\vec{a}| = 4$ , then  $|\vec{b}|$  is equal to .....

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32. Given  $|\vec{a}| = |\vec{b}| = 1$  and  $|\vec{a} + \vec{b}| = \sqrt{3}$  if  $\vec{c}$  is a vector such that  $\vec{c} - \vec{a} - 2\vec{b} = 3(\vec{a} \times \vec{b})$  then find the value of  $\vec{c} \cdot \text{Vecb}$ .



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33. Find the moment of  $\vec{F}$  about point  $(2, -1, 3)$ , where force  $\vec{F} = 3\hat{i} + 2\hat{j} - 4\hat{k}$  is acting on point  $(1, -1, 2)$ .



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34. If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are four non-coplanar unit vectors such that  $\vec{d}$  makes equal angles with all the three vectors  $\vec{a}, \vec{b}, \vec{c}$  then prove that  $[\vec{d}\vec{a}\vec{b}] = [\vec{d}\vec{c}\vec{b}] = [\vec{d}\vec{c}\vec{a}]$



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35. If  $\vec{l}, \vec{m}, \vec{n}$  are three non coplanar vectors prove that  $[\vec{l} \text{ vecm vecn}]$   
 $(\text{vecaxxvecb}) = |(\text{vec1.vec1}, \text{vec1.vecb}, \text{vec1}), (\text{vecm.vec1}, \text{vecm.vecb}, \text{vecm}),$   
 $(\text{vecn.vec1}, \text{vecn.vecb}, \text{vecn})|$



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36. if the volume of a parallelepiped whose adjacent edges are  $\vec{a} = 2\hat{i} + 3\hat{j} + 4\hat{k}$ ,  $\vec{b} = \hat{i} + \alpha\hat{j} + 2\hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} + \alpha\hat{k}$  then find of  $\alpha$  if  $(\alpha > 0)$

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37. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$  then find vector  $\vec{c}$  such that  $\vec{a} \cdot \vec{a} = 2$  and  $\vec{a} \times \vec{c} = \vec{b}$

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38. If  $\vec{x} \cdot \vec{a} = 0$ ,  $\vec{x} \cdot \vec{b} = 0$  and  $\vec{x} \cdot \vec{c} = 0$  for some non zero vector  $\vec{x}$  then show that  $[\vec{a}\vec{b}\vec{c}] = 0$

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39. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$  then find the vector  $\vec{c}$  such that  $\vec{a} \cdot \vec{c} = 2$  and  $\vec{a} \times \vec{c} = \vec{b}$ .

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40. If  $\vec{a}, \vec{b}$  and  $\vec{c}$  are three vectors such that  $\vec{a} \times \vec{b} = \vec{c}, \vec{b} \times \vec{c} = \vec{a}, \vec{c} \times \vec{a} = \vec{b}$  then prove that  $|\vec{a}| = |\vec{b}| = |\vec{c}|$

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41. If  $\vec{a} = \vec{P} + \vec{q}, \vec{P} \times \vec{b} = \vec{0}$  and  $\vec{q} \cdot \text{Vecb} = 0$  then prove that 
$$\frac{\vec{b} \times (\vec{a} \times \vec{b})}{\vec{b} \cdot \vec{b}} = \vec{q}$$

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42. prove that  $(\vec{a} \cdot (\vec{b} \times \hat{i}))\hat{i} + (\vec{a} \cdot (\vec{b} \times \hat{j}))\hat{j} + (\vec{a} \cdot (\vec{b} \times \hat{k}))\hat{k} = \vec{a} \times \vec{b}$

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43. for any four vectors  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  prove that

$$\vec{d} \cdot (\vec{a} \times (\vec{b} \times (\vec{c} \times \vec{d}))) = (\vec{b} \cdot \vec{d}) [\vec{a} \vec{c} \vec{d}]$$

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44. If  $\vec{a}$  and  $\vec{b}$  be two non-collinear unit vectors such that

$$\vec{a} \times (\vec{a} \times \vec{b}) = \frac{1}{2} \vec{b}$$
 then find the angle between  $\vec{a}$  and  $\vec{b}$ .

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45. show that  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$  if and only if  $\vec{a}$  and  $\vec{c}$  are collinear or  $(\vec{a} \times \vec{c}) \times \vec{b} \times \vec{0}$

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46. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be the non zero vectors such that  $(\vec{a} \times \vec{b}) \times \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}$ . If  $\theta$  is the acute angle between the vectors  $\vec{b}$  and  $\vec{a}$  then  $\theta$  equals (A)  $\frac{1}{3}$  (B)  $\frac{\sqrt{2}}{3}$  (C)  $\frac{2}{3}$  (D)  $2\frac{\sqrt{2}}{3}$

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47. If  $\vec{p}$ ,  $\vec{q}$ ,  $\vec{r}$  denote vectors  $\vec{b} \times \vec{c}$ ,  $\vec{c} \times \vec{a}$ ,  $\vec{a} \times \vec{b}$ . Respectively, show that  $\vec{a}$  is parallel to  $\vec{q} \times \vec{r}$ ,  $\vec{b}$  is parallel to  $\vec{r} \times \vec{p}$ ,  $\vec{c}$  is parallel to  $\vec{p} \times \vec{q}$ .

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48. Let  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  be non-coplanar vectors and let equations  $\vec{a}'$ ,  $\vec{b}'$ ,  $\vec{c}'$  are reciprocal system of vector  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  then prove that  $\vec{a} \times \vec{a}' + \vec{b} \times \vec{b}' + \vec{c} \times \vec{c}'$  is a null vector.

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49. Given unit vectors  $\hat{m}$  and  $\hat{n}$  such that angle between  $\hat{m}$  and  $\hat{n}$  is  $\alpha$  and angle between  $\hat{p}$  and

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50.  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are three unit vectors and every two are inclined to each other at an angle  $\cos^{-1}(3/5)$ . If  $\vec{a} \times \vec{b} = p\vec{a} + q\vec{b} + r\vec{c}$ , where  $p, q, r$  are scalars, then find the value of  $q$ .

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51. Let  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  be three non-zero vectors such that  $\vec{c}$  is a unit vector perpendicular to both

vectors,  $\vec{a}$  and  $\vec{b}$ . If the angle between  $\vec{a}$  and  $\vec{b}$  is  $\pi/6$  then  $\left| \begin{matrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{matrix} \right|^2$  is

equal to

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52. If 
$$\begin{vmatrix} (a-x)^2 & (a-y)^2 & (a-z)^2 \\ (b-x)^2 & (b-y)^2 & (b-z)^2 \\ (c-x)^2 & (c-y)^2 & (c-z)^2 \end{vmatrix} = 0$$
 and vectors  $\vec{A}, \vec{B}$  and  $\vec{C}$ , where

$\vec{A} = a^2\hat{i} = a\hat{j} + \hat{k}$  etc. are non-coplanar, then prove that vectors  $\vec{X}, \vec{Y}$  and  $\vec{Z}$  where  $\vec{X} = x^2\hat{i} + x\hat{j} + \hat{k}$ . etc. may be coplanar.

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53. OABC is a tetrahedron where O is the origin and A,B,C have position vectors  $\vec{a}, \vec{b}, \vec{c}$  respectively prove that circumcentre of tetrahedron OABC is  $(a^2(\vec{b} \times \vec{c}) + b^2(\vec{c} \times \vec{a}) + c^2(\vec{a} \times \vec{b})) / (2[\vec{a} \cdot (\vec{b} \times \vec{c})])$

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54. Let  $k$  be the length of any edge of a regular tetrahedron (a tetrahedron whose edges are equal in length is called a regular

tetrahedron). Show that the angle between any edge and a face not containing the edge is  $\cos^{-1}(1/\sqrt{3})$ .

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55. In  $\triangle ABC$ , a point  $P$  is taken on  $AB$  such that  $AP/BP = 1/3$  and point  $Q$  is taken on  $BC$  such that  $CQ/BQ = 3/1$ . If  $R$  is the point of intersection of the lines  $AQ$  and  $CP$ , using vector method, find the area of  $\triangle ABC$  if the area of  $\triangle BRC$  is 1 unit

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56. Let  $O$  be an interior point of  $\triangle ABC$  such that  $OA + 2OB + 3OC = 0$ . Then the ratio of area of  $\triangle ABC$  to area of  $\triangle AOC$  is

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57. The lengths of two opposite edges of a tetrahedron are  $a$  and  $b$ ; the shortest distance between these edges is  $d$ , and the angle between them is  $\theta$ . Prove using vectors that the volume of the tetrahedron is  $\frac{abd \sin \theta}{6}$ .

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58. Find the volume of a parallelepiped having three coterminal vectors of equal magnitude  $|a|$  and equal inclination  $\theta$  with each other.

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59. Let  $\vec{p}$  and  $\vec{q}$  any two orthogonal vectors of equal magnitude 4 each. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be any three vectors of lengths  $7\sqrt{15}$  and  $2\sqrt{33}$ , mutually perpendicular to each other. Then find the distance of the vector

$$\begin{aligned}
 & (\vec{a} \cdot \vec{p})\vec{p} + (\vec{a} \cdot \vec{q})\vec{q} + (\vec{a} \cdot (\vec{p} \times \vec{q}))(\vec{p} \times \vec{q}) + (\vec{b} \cdot \vec{p})\vec{p} + (\vec{b} \cdot \vec{q})\vec{q} + (\vec{b} \cdot (\vec{p} \times \vec{q}))(\vec{p} \times \vec{q}) \\
 & + (\vec{c} \cdot \vec{p})\vec{p} + (\vec{c} \cdot \vec{q})\vec{q} + (\vec{c} \cdot (\vec{p} \times \vec{q}))(\vec{p} \times \vec{q})
 \end{aligned}$$

from the origin.

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**60.** Given that  $\vec{A}, \vec{B}, \vec{C}$  form triangle such that  $\vec{A} = \vec{B} + \vec{C}$ . Find a,b,c,d such that area of the triangle is  $5\sqrt{6}$  where  $\vec{A} = a\vec{i} + b\vec{j} + c\vec{k}, \vec{B} = d\vec{i} + 3\vec{j} + 3\vec{k}$  and  $\vec{C} = 3\vec{i} + \vec{j} - 2\vec{k}$ .

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**61.** A line  $l$  is passing through the point  $\vec{b}$  and is parallel to vector  $\vec{c}$ . Determine the distance of point  $A(\vec{a})$  from the line  $l$  in from

$$\left| \vec{b} - \vec{a} + \frac{(\vec{a} - \vec{b})\vec{c}}{|\vec{c}|^2} \vec{c} \right| \text{ or } \frac{|(\vec{b} - \vec{a}) \times \vec{c}|}{|\vec{c}|}$$

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62. If  $\vec{e}_1, \vec{e}_2, \vec{e}_3$  and  $\vec{E}_1, \vec{E}_2, \vec{E}_3$  are two sets of vectors such that  $\vec{e}_i \cdot \vec{E}_j = 1$ , if  $i = j$  and  $\vec{e}_i \cdot \vec{E}_j = 0$  and if  $i \neq j$ , then prove that  $[\vec{e}_1 \vec{e}_2 \vec{e}_3][\vec{E}_1 \vec{E}_2 \vec{E}_3] = 1$ .

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63. In a quadrilateral ABCD, it is given that  $AB \perp CD$  and the diagonals AC and BD are perpendicular to each other. Show that  $AD \cdot BC \geq AB \cdot CD$ .

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64. OABC is regular tetrahedron in which D is the circumcentre of OAB and E is the midpoint of edge AC. Prove that DE is equal to half the edge of tetrahedron.

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65. If  $A(\vec{a})$ ,  $B(\vec{b})$  and  $C(\vec{c})$  are three non-collinear points and origin does not lie in the plane of the points A, B and C, then for any point  $P(\vec{P})$  in the plane of the  $\triangle ABC$  such that vector  $\vec{OP}$  is  $\perp$  to plane of  $\triangle ABC$ , show that  $\vec{OP} = \frac{[\vec{a}\vec{b}\vec{c}](\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})}{4\Delta^2}$

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66. If  $\vec{a}, \vec{b}, \vec{c}$  are three given non-coplanar vectors and any arbitrary vector  $\vec{r}$  in space, where

$$\Delta_1 = \begin{vmatrix} \vec{r} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{r} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{r} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c} \end{vmatrix}, \Delta_2 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{r} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{r} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{r} \cdot \vec{c} & \vec{c} \cdot \vec{c} \end{vmatrix}$$

$$\Delta_3 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{r} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{r} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{r} \cdot \vec{c} \end{vmatrix}, \Delta = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c} \end{vmatrix}, \text{ then prove that } \vec{r} = \frac{\Delta_1}{\Delta} \vec{a} + \frac{\Delta_2}{\Delta} \vec{b} + \frac{\Delta_3}{\Delta} \vec{c}$$

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67. Two vectors in space are equal only if they have equal component in a. a given direction b. two given directions c. three given directions d. in any arbitrary direction

- A. a given direction
- B. two given directions
- C. three given direction
- D. in any arbitrary direaction

**Answer: c**



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68. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be the three vectors having magnitudes, 1,5 and 3, respectively, such that the angle between  $\vec{a}$  and  $\vec{b}$  is  $\theta$  and  $\vec{a} \times (\vec{a} \times \vec{b}) = \vec{c}$ . Then  $\tan\theta$  is equal to

- A. 0

B.  $\frac{2}{3}$

C.  $\frac{3}{5}$

D.  $\frac{3}{4}$

**Answer: d**



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69. Let  $\vec{a}, \vec{b}, \vec{c}$  be three vectors of equal magnitude such that the angle

between each pair is  $\frac{\pi}{3}$ . If  $\left| \vec{a} + \vec{b} + \vec{c} \right| = \sqrt{6}$ , then  $|\vec{a}| =$

A. 2

B. -1

C. 1

D.  $\sqrt{6}/3$

**Answer: c**



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70. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are three mutually perpendicular vectors, then the vector which is equally inclined to these vectors is (A)  $\vec{a} + \vec{b} + \vec{c}$  (B)

$\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|} + \vec{\gamma} |\vec{c}|$  (C)  $\frac{\vec{a}}{|\vec{a}|^2} + \frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{c}}{|\vec{c}|^2}$  (D)  $|\vec{a}| \vec{a} - |\vec{b}| \vec{b} + |\vec{c}| \vec{c}$

A.  $\vec{a} + \vec{b} + \vec{c}$

B.  $\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|} + \frac{\vec{c}}{|\vec{c}|}$

C.  $\frac{\vec{a}}{|\vec{a}|^2} + \frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{c}}{|\vec{c}|^2}$

D.  $|\vec{a}| \vec{a} - |\vec{b}| \vec{b} + |\vec{c}| \vec{c}$

Answer: b



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71. Let  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = 2\hat{i} - \hat{k}$ . Then the point of intersection of the lines  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$  and  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  is (A) (3, -1, 10) (B) (3, 1, -1) (C) (-3, 1, 1) (D) (-3, -1, -10)

A.  $\hat{i} - \hat{j} + \hat{k}$

B.  $3\hat{i} - \hat{j} + \hat{k}$

C.  $3\hat{i} + \hat{j} - \hat{k}$

D.  $\hat{i} - \hat{j} - \hat{k}$

Answer: c



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72. If  $\vec{a}$  and  $\vec{b}$  are two vectors, such that  $\vec{a} \cdot \vec{b} < 0$  and  $|\vec{a} \cdot \vec{b}| = |\vec{a} \times \vec{b}|$  then the angle between angles between the vectors  $\vec{a}$  and  $\vec{b}$  is

A.  $\pi$

B.  $7\pi/4$

C.  $\pi/4$

D.  $3\pi/4$

**Answer: d**



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73. If  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  are three unit vectors such that  $\hat{a} + \hat{b} + \hat{c}$  is also a unit vector and  $\theta_1, \theta_2$  and  $\theta_3$  are angles between the vectors  $\hat{a}, \hat{b}, \hat{c}$  and  $\hat{c}, \hat{a}$ , respectively then among  $\theta_1, \theta_2$  and  $\theta_3$

- A. all are acute angles
- B. all are right angles
- C. at least one is obtuse angle
- D. none of these

**Answer: c**



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74. If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors such that  $\vec{a} \cdot \vec{b} = 0 = \vec{a} \cdot \vec{c}$  and the angle between  $\vec{b}$  and  $\vec{c}$  is  $\pi/3$  then the value of  $|\vec{a} \times \vec{b} - \vec{a} \times \vec{c}|$  is

A.  $1/2$

B. 1

C. 2

D. none of these

**Answer: b**



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75. P ( $\vec{p}$ ) and Q ( $\vec{q}$ ) are the position vectors of two fixed points and R ( $\vec{r}$ ) is the position vector of a variable point. If R moves such that  $(\vec{r} - \vec{p}) \times (\vec{r} - \vec{q}) = \vec{0}$  then the locus of R is

A. a plane containing the origin  $O$  and parallel to two non-collinear

vectors  $\vec{OP}$  and  $\vec{OQ}$

B. the surface of a sphere described on  $PQ$  as its diameter

C. a line passing through points  $P$  and  $Q$

D. a set of lines parallel to line  $PQ$

**Answer: c**



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76. Two adjacent sides of a parallelogram  $ABCD$  are

$2\hat{i} + 4\hat{j} - 5\hat{k}$  and  $\hat{i} + 2\hat{j} + 3\hat{k}$ . Then the value of  $\left| \vec{AC} \times \vec{BD} \right|$  is

A.  $20\sqrt{5}$

B.  $22\sqrt{5}$

C.  $24\sqrt{5}$

D.  $26\sqrt{5}$

**Answer: b**



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77. If  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  are three unit vectors inclined to each other at an angle  $\theta$ .

The maximum value of  $\theta$  is

A.  $\frac{\pi}{3}$

B.  $\frac{\pi}{2}$

C.  $\frac{2\pi}{3}$

D.  $\frac{5\pi}{5}$

**Answer: c**



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78. Let the pair of vector  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ ,  $\vec{c}d$  each determine a plane. Then the planes are parallel if



A.  $(\vec{a} \times \vec{c}) \times (\vec{b} \times \vec{d}) = \vec{0}$

B.  $(\vec{a} \times \vec{c}) \cdot (\vec{b} \times \vec{d}) = \vec{0}$

C.  $(\vec{a} \times \vec{c}) \times (\vec{c} \times \vec{d}) = \vec{0}$

D.  $(\vec{a} \times \vec{c}) \cdot (\vec{c} \times \vec{d}) = \vec{0}$

**Answer: c**

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79. If  $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = 0$  where  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non-coplanar, then

A.  $\vec{r} \perp (\vec{c} \times \vec{a})$

B.  $\vec{r} \perp (\vec{a} \times \vec{b})$

C.  $\vec{r} \perp (\vec{b} \times \vec{c})$

D.  $\vec{r} = \vec{0}$

**Answer: d**

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80. If  $\vec{a}$  satisfies  $\vec{a} \times (\hat{i} + 2\hat{j} + \hat{k}) = \hat{i} - \hat{k}$  then  $\vec{a}$  is equal to

A.  $\lambda\hat{i} + (2\lambda - 1)\hat{j} + \lambda\hat{k}, \lambda \in R$

B.  $\lambda\hat{i} + (1 - 2\lambda)\hat{j} + \lambda\hat{k}, \lambda \in R$

C.  $\lambda\hat{i} + (2\lambda + 1)\hat{j} + \lambda\hat{k}, \lambda \in R$

D.  $\lambda\hat{i} + (1 + 2\lambda)\hat{j} + \lambda\hat{k}, \lambda \in R$

Answer: c



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81. Vectors  $3\vec{a} - 5\vec{b}$  and  $2\vec{a} + \vec{b}$  are mutually perpendicular. If  $\vec{a} + 4\vec{b}$  and  $\vec{b} - \vec{a}$  are also mutually perpendicular, then the cosine of the angle between  $\vec{a}$  and  $\vec{b}$  is

A.  $\frac{19}{5\sqrt{43}}$

B.  $\frac{19}{3\sqrt{43}}$

C.  $\frac{19}{\sqrt{45}}$

D.  $\frac{19}{6\sqrt{43}}$

**Answer: a**

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**82.** The units vectors orthogonal to the vector  $-\hat{i} + 2\hat{j} + 2\hat{k}$  and making equal angles with the X and Y axes is/are) :

A.  $\pm \frac{1}{3}(2\hat{i} + 2\hat{j} - \hat{k})$

B.  $\frac{19}{5\sqrt{43}}$

C.  $\pm \frac{1}{3}(\hat{i} + \hat{j} - \hat{k})$

D. none of these

**Answer: a**

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83. The value of  $x$  for which the angle between  $\vec{a} = 2x^2\hat{i} + 4x\hat{j} = \hat{k} + \hat{k}$  and  $\vec{b} = 7\hat{i} - 2\hat{j} = x\hat{k}$ , is obtuse and the angle between  $\vec{b}$  and the z-axis is acute and less than  $\pi/6$ , are

A.  $a < x < 1/2$

B.  $1/2 < x < 15$

C.  $x < 1/2$  or  $x < 0$

D. none of these

Answer: b



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84. If vectors  $\vec{a}$  and  $\vec{b}$  are two adjacent sides of parallelogram then the vector representing the altitude of the parallelogram which is

perpendicular to  $\vec{a}$  is (A)  $\vec{b} + \frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$  (B)  $\frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2}$  (C)  $\vec{b} - \frac{\vec{b} \cdot \vec{a}}{(|\vec{a}|)^2}$  (D)

$$\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$$

A.  $\vec{b} + \frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$

B.  $\frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2}$

C.  $\vec{b} - \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}$

D.  $\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$

**Answer: a**

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85. A parallelogram is constructed on  $3\vec{a} + \vec{b}$  and  $\vec{a} - 4\vec{b}$ , where  $|\vec{a}| = 6$  and  $|\vec{b}| = 8$  and  $\vec{a}$  and  $\vec{b}$  are anti parallel then the length of the longer diagonal is (A) 40 (B) 64 (C) 32 (D) 48

A. 40

B. 64

C. 32

D. 48

**Answer: c**



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**86.** Let  $\vec{a} \cdot \vec{b} = 0$  where  $\vec{a}$  and  $\vec{b}$  are unit vectors and the vector  $\vec{c}$  is inclined at an angle  $\theta$  to both  $\vec{a}$  and  $\vec{b}$ . If  $\vec{c} = m\vec{a} + n\vec{b} + p(\vec{a} \times \vec{b})$ , ( $m, n, p \in R$ ) then

A.  $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$

B.  $\frac{\pi}{4} \leq \theta \leq \frac{3\pi}{4}$

C.  $0 \leq \theta \leq \frac{\pi}{4}$

D.  $0 \leq \theta \leq \frac{3\pi}{4}$

Answer: a



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87.  $\vec{a}$  and  $\vec{c}$  are unit vectors and  $|\vec{b}| = 4$  the angle between  $\vec{a}$  and  $\vec{b}$  is  $\cos^{-1}(1/4)$  and  $\vec{b} - 2\vec{c} = \lambda\vec{a}$  the value of  $\lambda$  is

A. 3, -4

B.  $1/4, 3/4$

C. -3, 4

D.  $-1/4, \frac{3}{4}$

Answer: a



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88. Let the position vectors of the points  $P$  and  $Q$  be  $4\hat{i} + \hat{j} + \lambda\hat{k}$  and  $2\hat{i} - \hat{j} + \lambda\hat{k}$ , respectively. Vector  $\hat{i} - \hat{j} + 6\hat{k}$  is perpendicular to

the plane containing the origin and the points  $P$  and  $Q$ . Then  $\lambda$  equals  $1/2$

b.  $1/2$  c. 1 d. none of these

A.  $-1/2$

B.  $1/2$

C. 1

D. none of these

**Answer: a**



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89. A vector of magnitude  $\sqrt{2}$  coplanar with the vectors  $\vec{a} = \hat{i} + \hat{j} + 2\hat{k}$  and  $\vec{b} = \hat{i} + \hat{j} + \hat{k}$ , and perpendicular to the vector  $\vec{c} = \hat{i} + \hat{j} + \hat{k}$  is

A.  $-\hat{j} + \hat{k}$

B.  $\hat{i}$  and  $\hat{k}$

C.  $\hat{i} - \hat{k}$



D. hati- hatj`

**Answer: a**



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90. Let  $P$  be a point interior to the acute triangle  $ABC$ . If  $\vec{PA} + \vec{PB} + \vec{PC}$  is a null vector, then w.r.t triangle  $ABC$ , point  $P$  is its a. centroid b. orthocentre c. incentre d. circumcentre

A. centroid

B. orthocentre

C. incentre

D. circumcentre

**Answer: a**



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91. G is the centroid of triangle ABC and  $A_1$  and  $B_1$  are the midpoints of sides AB and AC, respectively. If  $\Delta_1$  is the area of quadrilateral  $GA_1AB_1$  and  $\Delta$  is the area of triangle ABC, then  $\frac{\Delta}{\Delta_1}$  is equal to

A.  $\frac{3}{2}$

B. 3

C.  $\frac{1}{3}$

D. none of these

**Answer: b**



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92. Points  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are coplanar and  $(\sin\alpha)\vec{a} + (2\sin2\beta)\vec{b} + (3\sin3\gamma)\vec{c} - \vec{d} = \vec{0}$ . Then the least value of  $\sin^2\alpha + \sin^22\beta + \sin^23\gamma$  is

A.  $1/14$

B. 14

C. 6

D.  $1/\sqrt{6}$

**Answer: a**



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93. If  $\vec{a}$  and  $\vec{b}$  are any two vectors of magnitudes 1 and 2, respectively, and  $(1 - 3\vec{a} \cdot \vec{b})^2 + |2\vec{a} + \vec{b} + 3(\vec{a} \times \vec{b})|^2 = 47$  then the angle between  $\vec{a}$  and  $\vec{b}$  is

A.  $\pi/3$

B.  $\pi - \cos^{-1}(1/4)$

C.  $\frac{2\pi}{3}$

D.  $\cos^{-1}(1/4)$

**Answer: c**



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94. If  $\vec{a}$  and  $\vec{b}$  are any two vectors of magnitude 2 and 3 respectively such that  $|2(\vec{a} \times \vec{b})| + |3(\vec{a} \cdot \vec{b})| = k$  then the maximum value of  $k$  is

A.  $\sqrt{13}$

B.  $2\sqrt{13}$

C.  $6\sqrt{13}$

D.  $10\sqrt{13}$

Answer: c



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95.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors such that  $|\vec{a} + \vec{b} + 3\vec{c}| = 4$  Angle between  $\vec{a}$  and  $\vec{b}$  is  $\theta_1$ , between  $\vec{b}$  and  $\vec{c}$  is  $\theta_2$  and between  $\vec{a}$  and  $\vec{b}$  varies  $[\pi/6, 2\pi/3]$ . Then the maximum value of  $\cos\theta_1 + 3\cos\theta_2$  is

A. 3

B. 4

C.  $2\sqrt{2}$

D. 6

**Answer: b**



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96. If the vector product of a constant vector  $\vec{OA}$  with a variable vector  $\vec{OB}$  in a fixed plane  $OAB$  be a constant vector, then the locus of  $B$  is a straight line perpendicular to  $\vec{OA}$  b. a circle with centre  $O$  and radius equal to  $|\vec{OA}|$  c. a straight line parallel to  $\vec{OA}$  d. none of these

A. a straight line perpendicular to  $\vec{OA}$

B. a circle with centre  $O$  and radius equal to  $|\vec{OA}|$

C. a straight line parallel to  $\vec{OA}$

D. none of these

**Answer: c**

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97. Let  $\vec{u}, \vec{v}, \vec{w}$  be such that  $|\vec{u}| = 1, |\vec{v}| = 2, |\vec{w}| = 3$ . If the projection of  $\vec{v}$  along  $\vec{u}$  is equal to that of  $\vec{w}$  along  $\vec{v}$ ,  $\vec{w}$  are perpendicular to each other then  $|\vec{u} - \vec{v} + \vec{w}|$  equals (A) 2 (B)  $\sqrt{7}$  (C)  $\sqrt{14}$  (D) 14

A. 2

B.  $\sqrt{7}$

C.  $\sqrt{14}$

D. 14

**Answer: c**

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98. If the two adjacent sides of two rectangles are represented by

vectors  $\vec{p} = 5\vec{a} - 3\vec{b}$ ,  $\vec{q} = -\vec{a} - 2\vec{b}$  and  $\vec{r} = -4\vec{a} - \vec{b}$ ,  $\vec{s} = -\vec{a} + \vec{b}$ ,

respectively, then the angle between the vectors

$\vec{x} = \frac{1}{3}(\vec{p} + \vec{r} + \vec{s})$  and  $\vec{y} = \frac{1}{5}(\vec{r} + \vec{s})$  is

A.  $-\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$

B.  $\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$

C.  $\pi\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$

D. cannot of these

Answer: b



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99. If  $\vec{\alpha} \perp (\vec{b} \times \vec{c})$ , then  $(\vec{\alpha} \times \vec{b}) \cdot (\vec{\alpha} \times \vec{c}) =$  (A)  $|\vec{\alpha}|^2(\vec{b} \cdot \vec{c})$  (B)

$|\vec{b}|^2(\vec{c} \cdot \vec{\alpha})$  (C)  $|\vec{c}|^2(\vec{\alpha} \cdot \vec{b})$  (D)  $|\vec{\alpha}||\vec{b}||\vec{c}|$

A.  $|\vec{\alpha}|^2(\vec{\beta} \cdot \vec{\gamma})$

B.  $|\vec{\beta}|^2(\vec{\gamma} \cdot \vec{\alpha})$

C.  $|\vec{\gamma}|^2(\vec{\alpha} \cdot \vec{\beta})$

D.  $|\vec{\alpha}||\vec{\beta}||\vec{\gamma}|$

**Answer: a**



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**100.** The position vectors of points A, B and C are  $\hat{i} + \hat{j}$ ,  $\hat{i} + 5\hat{j} - \hat{k}$  and  $2\hat{i} + 3\hat{j} + 5\hat{k}$ , respectively the greatest angle of triangle ABC is

A.  $120^\circ$

B.  $90^\circ$

C.  $\cos^{-1}(3/4)$

D. none of these



**Answer: b**



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**101.** Given three vectors  $e\vec{a}, \vec{b}$  and  $\vec{c}$  two of which are non-collinear.

Further if  $(\vec{a} + \vec{b})$  is collinear with  $\vec{c}$ ,  $(\vec{b} + \vec{c})$  is collinear with

$\vec{a}$ ,  $|\vec{a}| = |\vec{b}| = |\vec{c}| = \sqrt{2}$  find the value of  $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$

A. 3

B. -3

C. 0

D. cannot of these

**Answer: b**



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102. If  $\vec{a}$  and  $\vec{b}$  are unit vectors such that

$(\vec{a} + \vec{b}) \cdot (2\vec{a} + 3\vec{b}) \times (3\vec{a} - 2\vec{b}) = \vec{0}$  then angle between  $\vec{a}$  and  $\vec{b}$  is

A. 0

B.  $\pi/2$

C.  $\pi$

D. indeterminate

Answer: d



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103. If in a right-angled triangle  $ABC$ , the hypotenuse

$AB = p$ , then  $\vec{AB}\vec{AC} + \vec{BC}\vec{BA} + \vec{CA}\vec{CB}$  is equal to  $2p^2$  b.  $\frac{p^2}{2}$  c.  $p^2$  d. none of

these

A.  $2p^2$

B.  $\frac{p^2}{2}$

C.  $p^2$

D. none of these

Answer: c

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104. Resolved part of vector  $\vec{a}$  and along vector  $\vec{b}$  is  $\vec{a}_1$  and that perpendicular to  $\vec{b}$  is  $\vec{a}_2$  then  $\vec{a}_1 \times \vec{a}_2$  is equal to

A.  $\frac{(\vec{a} \times \vec{b}) \cdot \vec{b}}{|\vec{b}|^2}$

B.  $\frac{(\vec{a} \cdot \vec{b})\vec{a}}{|\vec{a}|^2}$

C.  $\frac{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}{|\vec{b}|^2}$

D.  $\frac{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}{|\vec{b} \times \vec{a}|}$

**Answer: c**



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**105.** Let  $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$  and  $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$  be three vectors. A vector in the plane of  $\vec{b}$  and  $\vec{c}$  whose projection on  $\vec{a}$  is of magnitude

$\sqrt{\left(\frac{2}{3}\right)}$  is (A)  $2\hat{i} + 3\hat{j} + 3\hat{k}$  (B)  $2\hat{i} + 3\hat{j} - 3\hat{k}$  (C)  $-2\hat{i} - \hat{j} + 5\hat{k}$  (D)  $2\hat{i} + \hat{j} + 5\hat{k}$

A.  $2\hat{i} + 3\hat{j} - 3\hat{k}$

B.  $-2\hat{i} - \hat{j} + 5\hat{k}$

C.  $2\hat{i} + 3\hat{j} + 3\hat{k}$

D.  $2\hat{i} + \hat{j} + 5\hat{k}$

**Answer: b**



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106. If  $P$  is any arbitrary point on the circumcircle of the equilateral triangle of side length  $l$  units, then  $|\vec{PA}|^2 + |\vec{PB}|^2 + |\vec{PC}|^2$  is always equal to  $2l^2$  b.  $2\sqrt{3}l^2$  c.  $l^2$  d.  $3l^2$

A.  $2l^2$

B.  $2\sqrt{3}l^2$

C.  $l^2$

D.  $3l^2$

Answer: a



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107. If  $\vec{r}$  and  $\vec{s}$  are non-zero constant vectors and the scalar  $b$  is chosen such that  $|\vec{r} + b\vec{s}|$  is minimum, then the value of  $|b\vec{s}|^2 + |\vec{r} + b\vec{s}|^2$  is equal to

A.  $2|\vec{r}|^2$

B.  $|\vec{r}|^2/2$

C.  $3|\vec{r}|^2$

D.  $|\vec{r}|^2$

**Answer: b**

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**108.**  $\vec{a}$  and  $\vec{b}$  are two unit vectors that are mutually perpendicular. A unit vector that is equally inclined to  $\vec{a}$ ,  $\vec{b}$  and  $\vec{a} \times \vec{b}$  is equal to

A.  $\frac{1}{\sqrt{2}}(\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

B.  $\frac{1}{2}(\vec{a} \times \vec{b} + \vec{a} + \vec{b})$

C.  $\frac{1}{\sqrt{3}}(\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

D.  $\frac{1}{3}(\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

**Answer: a**

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109. Given that  $\vec{a}, \vec{b}, \vec{p}, \vec{q}$  are four vectors such that  $\vec{a} + \vec{b} = \mu\vec{p}$ ,  $\vec{b} \cdot \vec{q} = 0$  and  $(\vec{b})^2$  where  $\mu$  is a scalar. Then  $|(\vec{a} \cdot \vec{q})\vec{p} - (\vec{p} \cdot \vec{q})\vec{a}|$  is equal to

- A.  $2|\vec{p}\vec{q}|$
- B.  $(1/2)|\vec{p} \cdot \vec{q}|$
- C.  $|\vec{p} \times \vec{q}|$
- D.  $|\vec{p} \cdot \vec{q}|$

Answer: d



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110. The position vectors of the vertices A, B and C of a triangle are three unit vectors  $\vec{a}, \vec{b}$  and  $\vec{c}$  respectively. A vector  $\vec{d}$  is such that  $\vec{d} \cdot \vec{a} = \vec{d} \cdot \vec{b}$  and  $\vec{d} \cdot \vec{c} = \lambda(\vec{b} + \vec{c})$ . Then triangle ABC is

A. acute angled

B. obtuse angled

C. right angled

D. none of these

**Answer: a**



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111. If  $a$  is real constant  $A, B$  and  $C$  are variable angles and  $\sqrt{a^2 - 4\tan A} + a\tan B + \sqrt{a^2 + 4\tan C} = 6a$ , then the least value of  $\tan^2 A + \tan^2 B + \tan^2 C$  is 6 b. 10 c. 12 d. 3

A. 6

B. 10

C. 12

D. 3



**Answer: d**



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112. The vertex A of triangle ABC is on the line  $\vec{r} = \hat{i} + \hat{j} + \lambda\hat{k}$  and the vertices B and C have respective position vectors  $\hat{i}$  and  $\hat{j}$ . Let  $\Delta$  be the area of the triangle and  $\Delta \in \left[ \frac{3}{2}, \sqrt{33}/2 \right]$  then the range of value of  $\lambda$  corresponding to A is

- A.  $[-8, -4] \cup [4, 8]$
- B.  $[-4, 4]$
- C.  $[-2, 2]$
- D.  $[-4, -2] \cup [2, 4]$

**Answer: c**



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113. A non-zero vector  $\vec{a}$  is such that its projections along vectors

$\frac{\hat{i} + \hat{j}}{\sqrt{2}}$ ,  $\frac{-\hat{i} + \hat{j}}{\sqrt{2}}$  and  $\hat{k}$  are equal, then unit vector along  $\vec{a}$  is

A.  $\frac{\sqrt{2}\hat{j} - \hat{k}}{\sqrt{3}}$

B.  $\frac{\hat{j} - \sqrt{2}\hat{k}}{\sqrt{3}}$

C.  $\frac{\sqrt{2}}{\sqrt{3}}\hat{j} + \frac{\hat{k}}{\sqrt{3}}$

D.  $\frac{\hat{j} - \hat{k}}{\sqrt{2}}$

Answer: a



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114. Position vector  $\hat{k}$  is rotated about the origin by angle  $135^\circ$  in such a way that the plane made by it bisects the angle between  $\hat{i}$  and  $\hat{j}$ . Then its

new position is  $\pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$  b.  $\pm \frac{\hat{i}}{2} \pm \frac{\hat{j}}{2} - \frac{\hat{k}}{\sqrt{2}}$  c.  $\frac{\hat{i}}{\sqrt{2}} - \frac{\hat{k}}{\sqrt{2}}$  d. none of these

A.  $\pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$

B.  $\pm \frac{\hat{i}}{2} \pm \frac{\hat{j}}{2} - \frac{\hat{k}}{\sqrt{2}}$

C.  $\frac{\hat{i}}{\sqrt{2}} - \frac{\hat{k}}{\sqrt{2}}$

D. none of these

**Answer: d**



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115. In a quadrilateral  $ABCD$ ,  $\vec{AC}$  is the bisector of the  $(\vec{AB} \wedge \vec{AD})$  which

is  $\frac{2\pi}{3}$ ,  $15 \left| \vec{AC} \right| = 2 \left| \vec{AB} \right| = 5 \left| \vec{AD} \right|$  then  $\cos(\vec{BA} \wedge \vec{CD})$  is

A.  $\cos^{-1} \frac{\sqrt{14}}{7\sqrt{2}}$

B.  $\cos^{-1} \frac{\sqrt{21}}{7\sqrt{3}}$

C.  $\cos^{-1} \frac{2}{\sqrt{7}}$

$$D. \cos^{-1} \frac{2\sqrt{7}}{14}$$

**Answer: c**



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**116.** In fig. 2.33 AB, DE and GF are parallel to each other and AD, BG and EF are parallel to each other. If  $CD:CE = CG:CB = 2:1$  then the value of area ( $\triangle AEG$ ): area( $\triangle ABD$ ) is equal to



A.  $7/2$

B. 3

C. 4

D.  $9/2$

**Answer: b**



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117. Vectors  $\vec{a}$  in the plane of  $\vec{b} = 2\hat{i} + \hat{j}$  and  $\vec{c} = \hat{i} - \hat{j} + \hat{k}$  is such that it is equally inclined to  $\vec{b}$  and  $\vec{d}$  where  $\vec{d} = \hat{j} + 2\hat{k}$  the value of  $\vec{a}$  is

A.  $\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$

B.  $\frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}}$

C.  $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$

D.  $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$

Answer: b



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118. Let  $ABCD$  be a tetrahedron such that the edges  $AB, AC$  and  $AD$  are mutually perpendicular. Let the area of triangles  $ABC, ACD$  and  $ADB$  be 3, 4 and 5 sq. units, respectively. Then the area of triangle  $BCD$  is  $5\sqrt{2}$  b. 5 c.

$\frac{\sqrt{5}}{2}$  d.  $\frac{5}{2}$

A.  $5\sqrt{2}$

B. 5

C.  $\frac{\sqrt{5}}{2}$

D.  $\frac{5}{2}$

**Answer: a**

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119. Let  $\vec{f}(t) = [t]\hat{i} + (t - [t])\hat{j} + [t + 1]\hat{k}$ , where  $[.]$  denotes the greatest integer function. Then the vectors  $\vec{f}(5/4)$  and  $\vec{f}(t)$ , 0

A. parallel to each other

B. perpendicular to each other

C. inclined at  $\frac{\cos^{-1}2}{\sqrt{7}(1-t^2)}$

D. inclined at  $\frac{\cos^{-1}(8+t)}{9\sqrt{1+t^2}}$

**Answer: d**



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**120.** If  $\vec{a}$  is parallel to  $\vec{b} \times \vec{c}$ , then  $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{c})$  is equal to

A.  $|\vec{a}|^2(\vec{b} \cdot \vec{c})$

B.  $|\vec{b}|^2(\vec{a} \cdot \vec{c})$

C.  $|\vec{c}|^2(\vec{a} \cdot \vec{b})$

D. none of these

**Answer: a**



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**121.** The three vectors  $\hat{i} + \hat{j}, \hat{j} + \hat{k}, \hat{k} + \hat{i}$  taken two at a time form three planes, The three unit vectors drawn perpendicular to these planes form a parallelepiped of volume:

A.  $1/3$

B. 4

C.  $(3\sqrt{3})/4$

D.  $4\sqrt{3}$

Answer: d

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122. If  $\vec{d} = \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$  is a non zero vector and

$\left| (\vec{d} \cdot \vec{c})(\vec{a} \times \vec{b}) + (\vec{d} \cdot \vec{a})(\vec{b} \times \vec{c}) + (\vec{d} \cdot \vec{b})(\vec{c} \times \vec{a}) \right| = 0$  then (A)

$|\vec{a}| + |\vec{b}| + |\vec{c}| = |\vec{d}|$  (B)  $|\vec{a}| = |\vec{b}| = |\vec{c}|$  (C)  $\vec{a}, \vec{b}, \vec{c}$  are coplanar (D)

$\vec{a} + \vec{c} = 2\vec{b}$

A.  $|\vec{a}| = |\vec{b}| = |\vec{c}|$

B.  $|\vec{a}| + |\vec{b}| + |\vec{c}| = |\vec{d}|$

C.  $\vec{a}, \vec{b}$  and  $\vec{c}$  are coplanar



D. none of these

**Answer: c**

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123. If  $|\vec{a}| = 2$  and  $|\vec{b}| = 3$  and  $\vec{a} \cdot \vec{b} = 0$ , then  $(\vec{a} \times (\vec{a} \times (\vec{a} \times (\vec{a} \times \vec{b}))))$  is equal to the given diagonal is  $\vec{c} = 4\hat{k} = 8\hat{k}$  then , the volume of a parallelepiped is

A.  $48\hat{b}$

B.  $-48\hat{b}$

C.  $48\hat{a}$

D.  $-48\hat{a}$

**Answer: a**

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124. If two diagonals of one of its faces are  $6\hat{i} + 6\hat{k}$  and  $4\hat{j} + 2\hat{k}$  and of the edges not containing the given diagonals is  $\vec{c} = 4\hat{j} - 8\hat{k}$ , then the volume of a parallelepiped is

A. 60

B. 80

C. 100

D. 120

**Answer: d**



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125. The volume of a tetrahedron formed by the coterminus edges  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  is 3. Then the volume of the parallelepiped formed by the coterminus edges  $\vec{a} + \vec{b}$ ,  $\vec{b} + \vec{c}$  and  $\vec{c} + \vec{a}$  is

A. 6

B. 18

C. 36

D. 9

**Answer: c**



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**126.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three mutually orthogonal unit vectors , then the triple product  $[\vec{a} + \vec{b} + \vec{c} \vec{a} + \vec{b} \vec{b} + \vec{c}]$  equals

A. 0

B. 1 or -1

C. 1

D. 3

**Answer: b**



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127. vector  $\vec{c}$  are perpendicular to vectors  $\vec{a} = (2, -3, 1)$  and  $\vec{b} = (1, -2, 3)$  and satisfies the condition  $\vec{c} \cdot (\hat{i} + 2\hat{j} - 7\hat{k}) = 10$  then vector  $\vec{c}$  is equal to

A. 7,5,1

B. (-7, -5, -1)

C. 1,1,-1

D. none of these

Answer: a



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128. Given  $\vec{a} = x\hat{i} + y\hat{j} + 2\hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j}$ ,  $\vec{a} \perp \vec{b}$ ,  $\vec{a} \cdot \vec{c} = 4$  then

A.  $[\vec{a}\vec{b}\vec{c}]^2 = |\vec{a}|$

B.  $[\vec{a}\vec{b}\vec{c}] = |\vec{a}|$

$$C. [\vec{a}\vec{b}\vec{c}] = 0$$

$$D. [\vec{a}\vec{b}\vec{c}] = 0$$

Answer: d



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129. Let  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  be three non zero vectors such that  $\vec{c}$  is a unit vector perpendicular to both

$\vec{a}$  and  $\vec{b}$ . If the angle between  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{6}$ , then  $\left| \begin{matrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{matrix} \right|^2$  is equal

to

A. 0

B. 1

C.  $\frac{1}{4}(a_1^2 + a_2^2 + a_3^2)(b_1^2 + b_2^2 + b_3^2)$

D.  $\frac{3}{4}(a_1^2 + a_2^2 + a_3^2)(b_1^2 + b_2^2 + b_3^2)$

**Answer: c**



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**130.** Let  $\vec{r}, \vec{a}, \vec{b}$  and  $\vec{c}$  be four non-zero vectors such that

$\vec{r} \cdot \vec{a} = 0, |\vec{r} \times \vec{b}| = |\vec{r}| |\vec{b}|, |\vec{r} \times \vec{c}| = |\vec{r}| |\vec{c}|$  then

$[\vec{a} \ \vec{b} \ \vec{c}] =$

A.  $|a||b||c|$

B.  $-|a||b||c|$

C. 0

D. none of these

**Answer: c**



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131. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are such that  $[\vec{a}\vec{c}\vec{c}] = 1$ ,  $\vec{c} = \lambda\vec{a} \times \vec{b}$ , angle between  $\vec{a}$  and  $\vec{b}$  is  $2\pi/3$ ,  $|\vec{a}| = \sqrt{2}|\vec{b}| = \sqrt{3}$  and  $|\vec{c}| = \frac{1}{\sqrt{3}}$  then the angle between  $\vec{a}$  and  $\vec{b}$  is

A.  $\frac{\pi}{6}$

B.  $\frac{\pi}{4}$

C.  $\frac{\pi}{3}$

D.  $\frac{\pi}{2}$

Answer: b



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132. If  $4\vec{a} + 5\vec{b} + 9\vec{c} = 0$  then  $(\vec{a} \times \vec{b}) \times [(\vec{b} \times \vec{c}) \times (\vec{c} \times \vec{a})]$  is equal to

A. a vector perpendicular to the plane of  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$

B. a scalar quantity

C.  $\vec{0}$

D. none of these

**Answer: c**



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133. Value of  $[\vec{a} \times \vec{b}, \vec{a} \times \vec{c}, \vec{d}]$  is always equal to

A.  $(\vec{a} \cdot \vec{d})[\vec{a}\vec{b}\vec{c}]$

B.  $(\text{veca} \cdot \text{vecc})[\text{veca vecb vecd}]$

C.  $(\vec{a} \cdot \vec{b})[\vec{a}\vec{b}\vec{d}]$

D. none of these

**Answer: a**



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134. Let  $\hat{a}$  and  $\hat{b}$  be mutually perpendicular unit vectors. Then for an arbitrary  $\vec{r}$ .

A.  $\vec{r} = (\vec{r} \cdot \hat{a})\hat{a} + (\vec{r} \cdot \hat{b})\hat{b} + (\vec{r} \cdot (\hat{a} \times \hat{b}))(\hat{a} \times \hat{b})$

B.  $\vec{r} = (\vec{r} \cdot \hat{a}) - (\vec{r} \cdot \hat{b})\hat{b} - (\vec{r} \cdot (\hat{a} \times \hat{b}))(\hat{a} \times \hat{b})$

C.  $\vec{r} = (\vec{r} \cdot \hat{a})\hat{a} - (\vec{r} \cdot \hat{b})\hat{b} - (\vec{r} \cdot (\hat{a} \times \hat{b}))(\hat{a} \times \hat{b})$

D. none of these

Answer: a



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135. Let  $\vec{a}$  and  $\vec{b}$  be unit vectors that are perpendicular to each other. I.

then  $[\vec{a} + (\vec{a} \times \vec{b})\vec{b} + (\vec{a} \times \vec{b})\vec{a} \times \vec{b}]$  will always be equal to

A. 1

B. 0

C. -1

D. none of these

Answer: a



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136.  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $|\vec{a}| = 1$ ,  $|\vec{b}| = 4$  and  $\vec{a} \cdot \text{Vec}b = 2$ . If  $\vec{c} = (2\vec{a} \times \vec{b}) - 3\vec{b}$  then find angle between  $\vec{b}$  and  $\vec{c}$ .

A.  $\frac{\pi}{3}$

B.  $\frac{\pi}{6}$

C.  $\frac{3\pi}{4}$

D.  $\frac{5\pi}{6}$

Answer: d



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137. Then for any arbitrary vector

$\vec{a}$ ,  $\left(\left(\left(\vec{a} \times \vec{b}\right) + \left(\vec{a} \times \vec{b}\right)\right) \times \left(\vec{b} \times \vec{c}\right)\right)\left(\vec{b} - \vec{c}\right)$  is always equal to

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138. If  $\vec{a} \cdot \vec{b} = \beta$  and  $\vec{a} \times \vec{b} = \vec{c}$ , then  $\vec{b}$  is

A.  $\frac{(\beta\vec{a} - \vec{a} \times \vec{c})}{|\vec{a}|^2}$

B.  $\frac{(\beta\vec{a} + \vec{a} \times \vec{c})}{|\vec{a}|^2}$

C.  $\frac{(\beta\vec{c} + \vec{a} \times \vec{c})}{|\vec{a}|^2}$

D.  $\frac{(\beta\vec{c} + \vec{a} \times \vec{c})}{|\vec{a}|^2}$

Answer: a

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139. If  $a(\vec{\alpha} \times \vec{\beta}) = b(\vec{\beta} \times \vec{\gamma}) + c(\vec{\gamma} \times \vec{\alpha}) = \vec{0}$  and at least one of  $a, b$  and  $c$  is non zero then vectors  $\vec{\alpha}, \vec{\beta}, \vec{\gamma}$  are (A) parallel (B) coplanar (C) mutually perpendicular (D) none of these

A. parallel

B. coplanar

C. mutually perpendicular

D. none of these

Answer: b



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140. If  $(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c}) = \vec{b}$ , where  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non zero vectors then (A)  $\vec{a}, \vec{b}$  and  $\vec{c}$  can be coplanar (B)  $\vec{a}, \vec{b}$  and  $\vec{c}$  must be coplanar (C)  $\vec{a}, \vec{b}$  and  $\vec{c}$  cannot be coplanar (D) none of these

A.  $\vec{a}, \vec{b}$  and  $\vec{c}$  can be coplanar

B.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  must be coplanar

C.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  cannot be coplanar

D. none of these

**Answer: c**



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**141.** If  $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = \frac{1}{2}$  for some non zero vector  $\vec{r}$  and  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non coplanar, then the area of the triangle whose vertices are  $A(\vec{a})$ ,  $B(\vec{b})$  and  $C(\vec{c})$  is (A)  $\left| \left[ \vec{a} \vec{b} \vec{c} \right] \right|$  (B)  $|\vec{r}|$  (C)  $\left| \left[ \vec{a} \vec{b} \vec{r} \right] \vec{r} \right|$  (D) none of these

A.  $\left| \left[ \vec{a} \vec{b} \vec{c} \right] \right|$

B.  $|\vec{r}|$

C.  $\left| \left[ \vec{a} \vec{b} \vec{c} \right] \vec{r} \right|$

D. none of these

**Answer: c**



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**142.** A vector of magnitude 10 along the normal to the curve  $3x^2 + 8xy + 2y^2 - 3 = 0$  at its point  $P(1, 0)$  can be  $6\hat{i} + 8\hat{j}$  b.  $-8\hat{i} + 3\hat{j}$  c.  $6\hat{i} - 8\hat{j}$   
d.  $8\hat{i} + 6\hat{j}$

A.  $6\hat{i} + 8\hat{j}$

B.  $-8\hat{i} + 3\hat{j}$

C.  $6\hat{i} - 8\hat{j}$

D.  $8\hat{i} + 6\hat{j}$

**Answer: a**



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143. If  $\vec{a}$  and  $\vec{b}$  are two unit vectors inclined at an angle  $\pi/3$  then  $\left\{ \vec{a} \times (\vec{b} + \vec{a} \times \vec{b}) \right\} \cdot \vec{b}$  is equal to

A.  $\frac{-3}{4}$

B.  $\frac{1}{4}$

C.  $\frac{3}{4}$

D.  $\frac{1}{2}$

Answer: a



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144. If  $\vec{a}$  and  $\vec{b}$  are orthogonal unit vectors, then for a vector  $\vec{r}$  non-coplanar with  $\vec{a}$  and  $\vec{b}$  vector  $\vec{r} \times \vec{a}$  is equal to

A.  $[\vec{r} \vec{a} \vec{b}] \vec{b} - (\vec{r} \cdot \vec{b})(\vec{b} \times \vec{a})$

B.  $[\vec{r} \vec{a} \vec{b}](\vec{a} + \vec{b})$

C.  $[\vec{r} \vec{a} \vec{b}] \vec{a} + (\vec{r} \cdot \vec{a}) \vec{a} \times \vec{b}$

D. none of these

**Answer: a**



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**145.** If  $\vec{a} + \vec{b}, \vec{c}$  are any three non- coplanar vectors then the equation

$$[\vec{b} \times \vec{c} \vec{c} \times \vec{a} \vec{a} \times \vec{b}] x^2 + [\vec{a} + \vec{b} \vec{b} + \vec{c} \vec{c} + \vec{a}] x + 1 + [\vec{b} - \vec{c} \vec{c} - \vec{c} - \vec{a} \vec{a} - \vec{b}] = 0$$

has roots

A. real and distinct

B. real

C. equal

D. imaginary

**Answer: c**



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146. Solve the simultaneous vector equations for  $\vec{x}$  and  $\vec{y}$ :

$$\vec{c}x + \vec{c} \times \vec{c}y = \vec{c}a \text{ and } \vec{c}y + \vec{c} \times \vec{c}x = \vec{c}b, \vec{c} \cdot \vec{c} = 1$$

$$\text{A. } \vec{x} = \frac{\vec{b} \times \vec{c} + \vec{a} + (\vec{c} \cdot \vec{a})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

$$\text{B. } \vec{x} = \frac{\vec{c} \times \vec{b} + \vec{b} + (\vec{c} \cdot \vec{a})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

$$\text{C. } \vec{y} = \frac{\vec{a} \times \vec{c} + \vec{b} + (\vec{c} \cdot \vec{b})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

D. none of these

Answer: b

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147. The condition for equations  $\vec{r} \times \vec{a} = \vec{b}$  and  $\vec{r} \times \vec{c} = \vec{d}$  to be consistent is

$$\text{A. } \vec{b} \cdot \vec{c} = \vec{a} \cdot \vec{d}$$

B.  $\vec{a} \cdot \vec{b} = \vec{c} \cdot \vec{d}$

C.  $\vec{b} \cdot \vec{c} + \vec{a} \cdot \vec{d} = 0$

D.  $\vec{a} \cdot \vec{b} + \vec{c} \cdot \vec{d} = 0$

**Answer: c**



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148. If  $\vec{a} = 2\hat{i} + 3\hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$  and  $\vec{c} = -3\hat{i} + \hat{j} + 2\hat{k}$ , then  $[\vec{a}\vec{b}\vec{c}] =$



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149. If

$\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} + 2\hat{k}$ ,  $\vec{c} = \hat{i} + \hat{j} + 2\hat{k}$  and  $(1 + \alpha)\hat{i} + \beta(1 + \alpha)\hat{j} + \gamma(1 + \alpha)\hat{k}$

A.  $-2, -4, -\frac{2}{3}$

B.  $2, -4, \frac{2}{3}$

C.  $-2, 4, \frac{2}{3}$

D. 2, 4,  $-\frac{2}{3}$

**Answer: a**



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**150.** Let  $\vec{a}(x) = (\sin x)\hat{i} + (\cos x)\hat{j}$  and  $\vec{b}(x) = (\cos 2x)\hat{i} + (\sin 2x)\hat{j}$  be two variable vectors ( $x \in R$ ). Then  $\vec{a}(x)$  and  $\vec{b}(x)$  are

- A. collinear for unique value of  $x$
- B. perpendicular for infinite values of  $x$ .
- C. zero vectors for unique value of  $x$
- D. none of these

**Answer: b**



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151. For any vectors

$\vec{a}$  and  $\vec{b}$ ,  $(\vec{a} \times \hat{i}) + (\vec{b} \times \hat{i}) + (\vec{a} \times \hat{j}) + (\vec{b} \times \hat{j}) + (\vec{a} \times \hat{k}) + (\vec{b} \times \hat{k})$  is always equal to

- A.  $\vec{a} \cdot \vec{b}$
- B.  $2\vec{a} \cdot \text{Vecb}$
- C. zero
- D. none of these

Answer: b



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152. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non coplanar vectors and  $\vec{r}$  is any vector in space, then  $(\vec{r} \times \vec{b}) + (\vec{r} \times \vec{c}) + (\vec{b} \times \vec{c}) \times (\vec{r} \times \vec{a}) + (\vec{c} \times \vec{a}) \times (\vec{r} \times \vec{b}) =$

- (A)  $[\vec{a}\vec{b}\vec{c}]$  (B)  $2[\vec{a}\vec{b}\vec{c}]\vec{r}$  (C)  $3[\vec{a}\vec{b}\vec{c}]\vec{r}$  (D)  $4[\vec{a}\vec{b}\vec{c}]\vec{r}$

- A.  $[\vec{a}\vec{b}\vec{c}]\vec{r}$

B.  $2[\vec{a}\vec{b}\vec{c}]\vec{r}$

C.  $3[\vec{a}\vec{b}\vec{c}]\vec{r}$

D. none of these

**Answer: b**



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153. If  $\vec{P} = \frac{\vec{b} \times \vec{c}}{[\vec{a}\vec{b}\vec{c}]}$ ,  $\vec{Q} = \frac{\vec{c} \times \vec{a}}{[\vec{a}\vec{b}\vec{c}]}$  and  $\vec{R} = \frac{\vec{a} \times \vec{b}}{[\vec{a}\vec{b}\vec{c}]}$ , where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are

three non-coplanar vectors then the value of the expression

$(\vec{a} + \vec{b} + \vec{c}) \cdot (\vec{Q} + \vec{Q} + \vec{R})$  is

A. 3

B. 2

C. 1

D. 0

**Answer: a**



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154.  $A(\vec{a})$ ,  $B(\vec{b})$  and  $C(\vec{c})$  are the vertices of triangle ABC and  $R(\vec{r})$  is any point in the plane of triangle ABC, then  $\vec{r}$ ,  $(\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})$  is always equal to

A. zero

B.  $[\vec{a}\vec{b}\vec{c}]$

C.  $-[\vec{a}\vec{b}\vec{c}]$

D. none of these

**Answer: b**



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155. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar vectors and  $\vec{a} \times \vec{c}$  is perpendicular to  $\vec{a} \times (\vec{b} \times \vec{c})$ , then the value of  $[\vec{a} \times (\vec{b} \times \vec{c})] \times \vec{c}$  is equal to

A.  $[\vec{a}\vec{b}\vec{c}]\vec{c}$

B.  $[\vec{a}\vec{b}\vec{c}]\vec{b}$

C.  $\vec{0}$

D.  $[\vec{a}\vec{b}\vec{c}]\vec{a}$

**Answer: c**



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156. If  $V$  be the volume of a tetrahedron and  $V'$  be the volume of another tetrahedron formed by the centroids of faces of the previous tetrahedron and  $V = KV'$ , then  $K$  is equal to 9 b. 12 c. 27 d. 81

A. 9

B. 12

C. 27

D. 81

**Answer: c**



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157.  $\left[ (\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c}) (\vec{b} \times \vec{c}) \times (\vec{c} \times \vec{a}) (\vec{c} \times \vec{a}) \times (\vec{a} \times \vec{b}) \right]$  is equal to

( where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non - zero non- colanar vectors).

A.  $[\vec{a}\vec{b}\vec{c}]^2$

B.  $[\vec{a}\vec{b}\vec{c}]^3$

C.  $[\vec{a}\vec{b}\vec{c}]^4$

D.  $[\vec{a}\vec{b}\vec{c}]$

**Answer: c**



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158.

If

$\vec{r} = x_1(\vec{a} \times \vec{b}) + x_2(\vec{b} \times \vec{a}) + x_3(\vec{c} \times \vec{d})$  and  $4[\vec{a}\vec{b}\vec{c}] = 1$  then  $x_1 + x_2 + x_3$

is equal to

A.  $\frac{1}{2}\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

B.  $\frac{1}{4}\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

C.  $2\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

D.  $4\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

**Answer: d**



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**159.** If the vectors  $\vec{a}$  and  $\vec{b}$  are perpendicular to each other then a vector  $\vec{v}$  in terms of  $\vec{a}$  and  $\vec{b}$  satisfying the equations  $\vec{v} \cdot \vec{a} = 0$ ,  $\vec{v} \cdot \vec{b} = 1$  and  $[\vec{v} \ \vec{a} \ \vec{b}] = 1$  is

A.  $\frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^2}$

B.  $\frac{\vec{b}}{|\vec{b}|} + \frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^2}$

C.  $\frac{\vec{b}}{|\vec{b}|} + \frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|}$

D. none of these

Answer: a

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160. If  $\vec{a}' = \hat{i} + \hat{j}$ ,  $\vec{b}' = \hat{i} - \hat{j} + 2\hat{k}$  and  $\vec{c}' = 2\hat{i} = \hat{j} - \hat{k}$  then the altitude of the parallelepiped formed by the vectors,  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  having base formed by  $\vec{b}$  and  $\vec{c}$  is ( where  $\vec{a}'$  is reciprocal vector  $\vec{a}$ , , etc.

A. 1

B.  $3\sqrt{2}/2$

C.  $1/\sqrt{6}$

D.  $1/\sqrt{2}$

Answer: d



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161. If  $\vec{a} = \hat{i} + \hat{j}$ ,  $\vec{b} = \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{k} + \hat{i}$  then in the reciprocal system of vectors  $\vec{a}, \vec{b}, \vec{c}$  reciprocal  $\vec{a}$  of vector  $\vec{a}$  is

A.  $\frac{\hat{i} + \hat{j} + \hat{k}}{2}$

B.  $\frac{\hat{i} - \hat{j} + \hat{k}}{2}$

C.  $\frac{-\hat{i} - \hat{j} + \hat{k}}{2}$

D.  $\frac{\hat{i} + \hat{j} - \hat{k}}{2}$

Answer: d



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162. If unit vectors  $\vec{a}$  and  $\vec{b}$  are inclined at an angle  $2\theta$  such that

$|\vec{a} - \vec{b}| < 1$  and  $0 \leq \theta \leq \pi$ , then  $\theta$  lies in the interval

- A.  $[0, \pi/6)$
- B.  $(5\pi/6, \pi]$
- C.  $[\pi/6, \pi/2]$
- D.  $(\pi/2, 5\pi/6]$

Answer: a,b



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163.  $\vec{b}$  and  $\vec{c}$  are non-collinear if *[Math Processing Error]* then

- A.  $x = 1$
- B.  $x = -1$
- C.  $y = (4n + 1)\frac{\pi}{2}, n \in I$

$$D. y(2n + 1)\frac{\pi}{2}, n \in I$$

Answer: a,c



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164. Unit vectors  $\vec{a}$  and  $\vec{b}$  are perpendicular, and unit vector  $\vec{c}$  is inclined at an angle  $\theta$  to both  $\vec{a}$  and  $\vec{b}$ . If  $\alpha\vec{a} + \beta\vec{b} + \gamma(\vec{a} \times \vec{b})$  then.

A.  $\alpha = \beta$

B.  $\gamma^2 = 1 - 2\alpha^2$

C.  $\gamma^2 = -\cos 2\theta$

D.  $\beta^2 = \frac{1 + \cos 2\theta}{2}$

Answer: a,b,c,d



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165. If vectors  $\vec{a}$  and  $\vec{b}$  are two adjacent sides of parallelogram then the vector representing the altitude of the parallelogram which is

perpendicular to  $\vec{a}$  is (A)  $\vec{b} + \frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$  (B)  $\frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2}$  (C)  $\vec{b} - \frac{\vec{b} \cdot \vec{a}}{(|\vec{a}|)^2}$  (D)

$$\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$$

$$\text{A. } \frac{(\vec{a} \cdot \vec{b})}{|\vec{a}|^2} \vec{a} - \vec{b}$$

$$\text{B. } \frac{1}{|\vec{a}|^2} \{ |\vec{a}|^2 \vec{b} - (\vec{a} \cdot \vec{b}) \vec{a} \}$$

$$\text{C. } \frac{\vec{a} \times (\vec{a} \times \vec{b})}{|\vec{a}|^2}$$

$$\text{D. } \frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$$

Answer: a,b,c



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166. If  $\vec{c} \times \vec{a} \times (\vec{b} \times \vec{c})$  is perpendicular to  $(\vec{a} \times \vec{b}) \times \vec{c}$ , we may have

A.  $(\vec{a} \cdot \vec{b})|\vec{b}|^2 = (\vec{a} \cdot \vec{b})(\vec{b} \cdot \vec{c})$

B.  $\vec{a} \cdot \vec{b} = 0$

C.  $\vec{a} \cdot \vec{c} = 0$

D.  $\vec{b} \cdot \vec{c} = 0$

Answer: a,c

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167. If  $\vec{p} = \frac{\vec{b} \times \vec{c}}{[\vec{a} \ \vec{b} \ \vec{c}]}$ ,  $\vec{q} = \frac{\vec{c} \times \vec{a}}{[\vec{a} \ \vec{b} \ \vec{c}]}$ ,  $\vec{r} = \frac{\vec{a} \times \vec{b}}{[\vec{a} \ \vec{b} \ \vec{c}]}$  where  $\vec{a}, \vec{b}, \vec{c}$  are

three non-coplanar vectors, then the value of the expression

$(\vec{a} + \vec{b} + \vec{c}) \cdot (\vec{p} + \vec{q} + \vec{r})$  is

A.  $x[\vec{a}\vec{b}\vec{c}] + \frac{[\vec{p}\vec{q}\vec{r}]}{x}$  has least value 2

B.  $x^2[\vec{a}\vec{b}\vec{c}]^2 + \frac{[\vec{p}\vec{q}\vec{r}]}{x^2}$  has least value  $(3/2^{2/3})$

C.  $[\vec{p}\vec{q}\vec{r}] > 0$

D. none of these

**Answer: a,c**



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168.  $a_1, a_2, a_3 \in \mathbb{R} - \{0\}$  and  $a_1 + a_2 \cos 2x + a_3 \sin^2 x = 0$  for all  $x$  in  $\mathbb{R}$

then

A. vectors  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$  and  $\vec{b} = 4\hat{i} + 2\hat{j} + \hat{k}$  are perpendicular to

each other

B. vectors  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$  and  $\vec{b} = \hat{i} + \hat{j} + 2\hat{k}$  are parallel to each

each other

C. if vector  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$  is of length  $\sqrt{6}$  units, then one of the

ordered triplet  $(a_1, a_2, a_3) = (1, -1, -2)$

D. if  $2a_1 + 3a_2 + 6a_3 + 6a_3 = 26$ , then  $|\vec{a}\hat{i} + a_2\hat{j} + a_3\hat{k}| = 2\sqrt{6}$



Answer: a,b,c,d



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169. If  $\vec{a}$  and  $\vec{b}$  are two vectors and angle between them is  $\theta$ , then

A.  $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2 = |\vec{a}|^2 |\vec{b}|^2$

B.  $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2, \text{ if } \theta = \pi/4$

C.  $\vec{a} \times \vec{b} = (\vec{a} \cdot \text{Vec}b)\hat{n}$  ( where  $\hat{n}$  is a normal unit vector ) if  $\theta = \pi/4$

D.  $(\vec{a} \times \vec{b}) \cdot (\vec{a} + \vec{b}) = 0$

Answer: a,b,c,d



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170. Let  $\vec{a}$  and  $\vec{b}$  be two non- zero perpendicular vectors. A vector  $\vec{r}$  satisfying the equation  $\vec{r} \times \vec{b} = \vec{a}$  can be

$$\text{A. } \vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

$$\text{B. } 2\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

$$\text{C. } |\vec{a}|\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

$$\text{D. } |\vec{b}|\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

Answer: a,b,cd,



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171. If vector  $\vec{b} = (\tan\alpha, -12\sqrt{\sin\alpha/2})$  and  $\vec{c} = (\tan\alpha, \tan\alpha - \frac{3}{\sqrt{\sin\alpha/2}})$  are

orthogonal and vector  $\vec{a} = (13, \sin 2\alpha)$  makes an obtuse angle with the z-

axis, then the value of  $\alpha$  is  $\alpha = (4n + 1)\pi + \tan^{-1}2$  b.  $\alpha = (4n + 1)\pi - \tan^{-1}2$

c.  $\alpha = (4n + 2)\pi + \tan^{-1}2$  d.  $\alpha = (4n + 2)\pi - \tan^{-1}2$

A.  $\alpha = (4n + 1)\pi + \tan^{-1}2$

$$B. \alpha = (4n + 1)\pi - \tan^{-1}2$$

$$C. \alpha = (4n + 2)\pi + \tan^{-1}2$$

$$D. \alpha = (4n + 2)\pi - \tan^{-1}2$$

**Answer: b,d**



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**172.** Let  $\vec{r}$  be a unit vector satisfying

$$\vec{r} \times \vec{a} = \vec{b}, \text{ where } |\vec{a}| = \sqrt{3} \text{ and } |\vec{b}| = \sqrt{2}$$

$$A. \vec{r} = \frac{2}{3}(\vec{a} + \vec{a} \times \vec{b})$$

$$B. \vec{r} = \frac{1}{3}(\vec{a} + \vec{a} \times \vec{b})$$

$$C. \vec{r} = \frac{2}{3}(\vec{a} - \vec{a} \times \vec{b})$$

$$D. \vec{r} = \frac{1}{3}(-\vec{a} + \vec{a} \times \vec{b})$$

**Answer: b,d**



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173. If  $\vec{a}$  and  $\vec{b}$  are unequal unit vectors such that

$$(\vec{a} - \vec{b}) \times [(\vec{b} + \vec{a}) \times (2\vec{a} + \vec{b})] = \vec{a} + \vec{b}$$
 then angle  $\theta$  between  $\vec{a}$  and  $\vec{b}$  is

A. 0

B.  $\pi/2$

C.  $\pi/4$

D.  $\pi$

Answer: b,d



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174. If  $\vec{a}$  and  $\vec{b}$  are two unit vectors perpendicular to each other and

$$\vec{c} = \lambda_1 \vec{a} + \lambda_2 \vec{b} + \lambda_3 (\vec{a} \times \vec{b}),$$
 then which of the following is (are) true ?

A.  $\lambda_1 = \vec{a} \cdot \vec{c}$

B.  $\lambda_2 = |\vec{b} \times \vec{c}|$

$$C. \lambda_3 = |(\vec{a} \times \vec{b}) \times \vec{c}|$$

$$D. \lambda_1 \vec{a} + \lambda_2 \vec{b} + \lambda_3 (\vec{a} \times \vec{b})$$

**Answer: a,d**

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175. If vectors  $\vec{a}$  and  $\vec{b}$  are non collinear then  $\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|}$  is (A) a unit vector  $\in$  the plane of  $\vec{a}$  and  $\vec{b}$  (B)  $\in$  the plane of  $\vec{a}$  and  $\vec{b}$  (C) equally inclined to  $\vec{a}$  and  $\vec{b}$  (D) perpendicular to  $\vec{a} \times \vec{b}$

A. a unit vector

B. in the plane of  $\vec{a}$  and  $\vec{b}$

C. equally inclined to  $\vec{a}$  and  $\vec{b}$

D. perpendicular to  $\vec{a} \times \vec{b}$

**Answer: b,c,d**

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176. If  $\vec{a}$  and  $\vec{b}$  are non-zero vectors such that  $|\vec{a} + \vec{b}| = |\vec{a} - 2\vec{b}|$  then

A.  $2\vec{a} \cdot \vec{b} = |\vec{b}|^2$

B.  $\vec{a} \cdot \vec{b} = |\vec{b}|^2$

C. least value of  $\vec{a} \cdot \vec{b} + \frac{1}{|\vec{b}|^2 + 2}$  is  $\sqrt{2}$

D. least value of  $\vec{a} \cdot \vec{b} + \frac{1}{|\vec{b}|^2 + 2}$  is  $\sqrt{2} - 1$

Answer: a,d



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177. Let  $\vec{a}, \vec{b}$  and  $\vec{c}$  be non-zero vectors and

$\vec{V}_1 = \vec{a} \times (\vec{b} \times \vec{c})$  and  $\vec{V}_2 = (\vec{a} \times \vec{b}) \times \vec{c}$ . vectors  $\vec{V}_1$  and  $\vec{V}_2$  are equal .

Then

A.  $\vec{a}$  and  $\vec{b}$  are orthogonal

B.  $\vec{a}$  and  $\vec{c}$  are collinear

C.  $\vec{b}$  and  $\vec{c}$  are orthogonal

D.  $\vec{b} = \lambda(\vec{a} \times \vec{c})$  when  $\lambda$  is a scalar

**Answer: b,d**



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**178.** Vectors  $\vec{A}$  and  $\vec{B}$  satisfying the vector equation

$\vec{A} + \vec{B} = \vec{a}$ ,  $\vec{A} \times \vec{B} = \vec{b}$  and  $\vec{A} \cdot \vec{a} = 1$ . Vectors  $\vec{a}$  and  $\vec{b}$  are given vectors, are

A.  $\vec{A} = \frac{(\vec{a} \times \vec{b}) - \vec{a}}{a^2}$

B.  $\vec{B} = \frac{(\vec{b} \times \vec{a}) + \vec{a}(a^2 - 1)}{a^2}$

C.  $\vec{A} = \frac{(\vec{a} \times \vec{b}) + \vec{a}}{a^2}$

D.  $\vec{B} = \frac{(\vec{b} \times \vec{a}) - \vec{a}(a^2 - 1)}{a^2}$

Answer: b,c,

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179. A vector  $\vec{d}$  is equally inclined to three vectors  $\vec{a} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = 2\hat{i} + \hat{j}$  and  $\vec{c} = 3\hat{j} - 2\hat{k}$ . Let  $\vec{x}$ ,  $\vec{y}$  and  $\vec{z}$  be three vectors in the plane of  $\vec{a}$ ,  $\vec{b}$ ;  $\vec{b}$ ,  $\vec{c}$ ;  $\vec{c}$ ,  $\vec{a}$ , respectively. Then

A.  $\vec{x} \cdot \vec{d} = -1$

B.  $\vec{y} \cdot \vec{d} = 1$

C.  $\text{vecz} \cdot \text{vecd} = 0$

D.  $\text{vecr} \cdot \text{vecd} = 0$ , " where "  $\text{vecr} = \lambda \text{vecx} + \mu \text{vecy} + \delta \text{vecz}$

Answer: c.d

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180. Vectors perpendicular to  $\hat{i} - \hat{j} - \hat{k}$  and in the plane of  $\hat{i} + \hat{j} + \hat{k}$  and  $-\hat{i} + \hat{j} + \hat{k}$  are (A)  $\hat{i} + \hat{k}$  (B)  $2\hat{i} + \hat{j} + \hat{k}$  (C)  $3\hat{i} + 2\hat{j} + \hat{k}$  (D)  $-4\hat{i} - 2\hat{j} - 2\hat{k}$

A.  $\hat{i} + \hat{k}$

B.  $2\hat{i} + \hat{j} + \hat{k}$

C.  $3\hat{i} + 2\hat{j} + \hat{k}$

D.  $-4\hat{i} - 2\hat{j} - 2\hat{k}$

Answer: b,d

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181. If the sides  $\vec{AB}$  of an equilateral triangle ABC lying in the xy-plane is  $3\hat{i}$  then the side  $\vec{CB}$  can be (A)  $-\frac{3}{2}(\hat{i} - \sqrt{3})$  (B)  $\frac{3}{2}(\hat{i} - \sqrt{3})$  (C)  $-\frac{3}{2}(\hat{i} + \sqrt{3})$  (D)  $\frac{3}{2}(\hat{i} + \sqrt{3})$

A.  $-\frac{3}{2}(\hat{i} - \sqrt{3}\hat{j})$

$$B. -\frac{3}{2}(\hat{i} - \sqrt{3}\hat{j})$$

$$C. -\frac{3}{2}(\hat{i} + \sqrt{3}\hat{j})$$

$$D. \frac{3}{2}(\hat{i} + \sqrt{3}\hat{j})$$

**Answer: b,d**



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**182.** Let  $\hat{a}$  be a unit vector and  $\hat{b}$  a non zero vector non parallel to  $\vec{a}$ . Find the angles of the triangle two sides of which are represented by the vectors.  $\sqrt{3}(\hat{a} \times \vec{b})$  and  $\vec{b} - (\hat{a} \cdot \vec{b})\hat{a}$

$$A. \tan^{-1}(\sqrt{3})$$

$$B. \tan^{-1}(1/\sqrt{3})$$

$$C. \cot^{-1}(0)$$

$$D. \tan^{-1}(1)$$

**Answer: a,b,c**

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183.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unimodular and coplanar. A unit vector  $\vec{d}$  is perpendicular to them,  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = \frac{1}{6}\hat{i} - \frac{1}{3}\hat{j} + \frac{1}{3}\hat{k}$ , and the angle between  $\vec{a}$  and  $\vec{b}$  is  $30^\circ$  then  $\vec{c}$  is

- A.  $(\hat{i} - 2\hat{j} + 2\hat{k})/3$
- B.  $(-\hat{i} + 2\hat{j} - 2\hat{k})/3$
- C.  $(-\hat{i} + 2\hat{j} - \hat{k})/3$
- D.  $(-2\hat{i} - 2\hat{j} + \hat{k})/3$

Answer: a,b

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184. If  $\vec{a} + 2\vec{b} + 3\vec{c} = \vec{0}$  then  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} =$

- A.  $2(\vec{a} \times \vec{b})$

B.  $6(\vec{b} \times \vec{c})$

C.  $3(\vec{c} \times \vec{a})$

D.  $\vec{0}$

Answer: c,d



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185. Let  $\vec{a}$  and  $\vec{b}$  be two non-collinear unit vectors. If  $\vec{u} = \vec{a} - (\vec{a} \cdot \vec{b})\vec{b}$  and  $\vec{v} = \vec{a} \times \vec{b}$ , then  $|\vec{v}|$  is

A.  $|\vec{u}|$

B.  $|\vec{u}| + |\vec{u} \cdot \vec{b}|$

C.  $|\vec{u}| + |\vec{u} \cdot \vec{a}|$

D. none of these

Answer: b,d



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186. if  $\vec{a} \times \vec{b} = \vec{c}$ ,  $\vec{b} \times \vec{c} = \vec{a}$ , where  $\vec{c} \neq \vec{0}$  then

A.  $|\vec{a}| = |\vec{c}|$

B.  $|\vec{a}| = |\vec{b}|$

C.  $|\vec{b}| = 1$

D.  $|\vec{a}| = |\vec{b}| = |\vec{c}| = 1$

Answer: a,c



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187. Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be three non-coplanar vectors and  $\vec{d}$  be a non-zero, which is perpendicular to

$(\vec{a} + \vec{b} + \vec{c})$ . Now  $\vec{d} = (\vec{a} \times \vec{b})\sin x + (\vec{b} \times \vec{c})\cos y + 2(\vec{c} \times \vec{a})$ . Then

A.  $\frac{\vec{d} \cdot (\vec{a} + \vec{c})}{[\vec{a}\vec{b}\vec{c}]} = 2$

$$\text{B. } \frac{\vec{d} \cdot (\vec{a} + \vec{c})}{[\vec{a}\vec{b}\vec{c}]} = -2$$

C. minimum value of  $x^2 + y^2$  is  $\pi^2/4$

D. minimum value of  $x^2 + y^2$  is  $5\pi^2/4$

**Answer: b,d**



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**188.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three unit vectors such that

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{1}{2}\vec{b}, \text{ then } (\vec{b} \text{ and } \vec{c} \text{ being non parallel})$$

A. angle between  $\vec{a}$  and  $\vec{b}$  is  $\pi/3$

B. angle between  $\vec{a}$  and  $\vec{c}$  is  $\pi/3$

C. angle between  $\vec{a}$  and  $\vec{b}$  is  $\pi/2$

D. angle between  $\vec{a}$  and  $\vec{c}$  is  $\pi/2$

**Answer: b,c**



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189. If in triangle ABC,  $\vec{AB} = \frac{\vec{u}}{|\vec{u}|} - \frac{\vec{v}}{|\vec{v}|}$  and  $\vec{AC} = \frac{2\vec{u}}{|\vec{u}|}$ , where  $|\vec{u}| \neq |\vec{v}|$ ,

then

- A.  $1 + \cos 2A + \cos 2B + \cos 2C = 0$
- B.  $\sin A = \cos C$
- C. projection of AC on BC is equal to BC
- D. projection of AB on BC is equal to AB

Answer: a,b,c



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190.  $[\vec{a} \times \vec{b} \quad \vec{c} \times \vec{d} \quad \vec{e} \times \vec{f}]$  is equal to

- A.  $[\vec{a}\vec{b}\vec{d}][\vec{c}\vec{e}\vec{f}] - [\vec{a}\vec{b}\vec{c}][\vec{d}\vec{e}\vec{f}]$
- B.  $[\vec{a}\vec{b}\vec{e}][\vec{f}\vec{c}\vec{d}] - [\vec{a}\vec{b}\vec{f}][\vec{e}\vec{c}\vec{d}]$

$$C. [\vec{c}\vec{d}\vec{a}][\vec{b}\vec{e}\vec{f}] - [\vec{a}\vec{d}\vec{b}][\vec{a}\vec{e}\vec{f}]$$

$$D. [\vec{a}\vec{c}\vec{e}][\vec{b}\vec{d}\vec{f}]$$

Answer: a,b,c



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191. The scalars  $l$  and  $m$  such that  $l\vec{a} + m\vec{b} = \vec{c}$ , where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are given vectors, are equal to

$$A. l = \frac{(\vec{c} \times \vec{b}) \cdot (\vec{a} \times \vec{b})}{(\vec{a} \times \vec{b})^2}$$

$$B. l = \frac{(\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$$

$$C. m = \frac{(\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})^2}$$

$$D. m = \frac{(\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$$



Answer: a,c



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192. If  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) \cdot (\vec{a} \times \vec{d}) = 0$  then which of the following may be true ?

A.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{d}$  are necessarily coplanar

B.  $\vec{a}$  lies in the plane of  $\vec{c}$  and  $\vec{d}$

C.  $\vec{b}$  lies in the plane of  $\vec{a}$  and  $\vec{d}$

D.  $\vec{c}$  lies in the plane of  $\vec{a}$  and  $\vec{d}$

Answer: b,c,d



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193. A, B, C and D are four points such that

$\vec{AB} = m(2\hat{i} - 6\hat{j} + 2\hat{k})$ ,  $\vec{BC} = (a\hat{i} - 2\hat{j})$  and  $\vec{CD} = n(-6\hat{i} + 15\hat{j} - 3\hat{k})$ . If CD

intersects AB at some points E, then

A.  $m \geq 1/2$

B.  $n \geq 1/3$

C.  $m = n$

D.  $m < n$

Answer: a,b



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194. If the vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non-coplanar and  $l, m, n$  are distinct scalars such that

$$[l\vec{a} + m\vec{b} + n\vec{c} \quad l\vec{b} + m\vec{c} + n\vec{a} \quad l\vec{c} + m\vec{a} + n\vec{b}] = 0 \text{ then}$$

A.  $l + m + n = 0$

B. roots of the equation  $lx^2 + mx + n = 0$  are equal

C.  $l^2 + m^2 + n^2 = 0$

$$D. l^3 + m^2 + n^3 = 3lmn$$

Answer: a,b,d



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195. Let  $\vec{\alpha} = a\hat{i} + b\hat{j} + c\hat{k}$ ,  $\vec{\beta} = b\hat{i} + c\hat{j} + a\hat{k}$  and  $\vec{\gamma} = c\hat{i} + a\hat{j} + b\hat{k}$  be three coplanar vectors with  $a \neq b$ , and  $\vec{v} = \hat{i} + \hat{j} + \hat{k}$ . Then  $\vec{v}$  is perpendicular to

A.  $\vec{\alpha}$

B.  $\vec{\beta}$

C.  $\vec{\gamma}$

D. none of these

Answer: a,b,c



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196. If vectors  $\vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$ ,  $\vec{B} = \hat{i} + \hat{j} + 5\hat{k}$  and  $\vec{C}$  form a left handed system then  $\vec{C}$  is (A)  $11\hat{i} - 6\hat{j} - \hat{k}$  (B)  $-11\hat{i} + 6\hat{j} + \hat{k}$  (C)  $-11\hat{i} + 6\hat{j} - \hat{k}$  (D)  $-11\hat{i} + 6\hat{j} - \hat{k}$

A.  $11\hat{i} - 6\hat{j} - \hat{k}$

B.  $-11\hat{i} - 6\hat{j} - \hat{k}$

C.  $-11\hat{i} - 6\hat{j} + \hat{k}$

D.  $-11\hat{i} + 6\hat{j} - \hat{k}$

Answer: b,d



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197. If

$\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$ ,  $\vec{b} = y\hat{i} + z\hat{j} + x\hat{k}$  and  $\vec{c} = z\hat{i} + x\hat{j} + y\hat{k}$ , then  $\vec{a} \times (\vec{b} \times \vec{c})$  is

A. parallel to  $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$

B. orthogonal to  $\hat{i} + \hat{j} + \hat{k}$

C. orthogonal to  $(y + z)\hat{i} + (z + x)\hat{j} + (x + y)\hat{k}$

D. orthogonal to  $x\hat{i} + y\hat{j} + z\hat{k}$

**Answer: a,b,c,d**



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**198.** If  $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \times \vec{b}) \times \vec{c}$  then

A.  $(\vec{c} \times \vec{a}) \times \vec{b} = \vec{0}$

B.  $\vec{c} \times (\vec{a} \times \vec{b}) = \vec{0}$

C.  $\vec{b} \times (\vec{c} \times \vec{a}) = \vec{0}$

D.  $\vec{c} \times \vec{a} \times \vec{b} = \vec{b} \times (\vec{c} \times \vec{a}) = \vec{0}$

**Answer: a,c,d**



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199. A vector  $\vec{d}$  is equally inclined to three vectors  $\vec{a} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = 2\hat{i} + \hat{j}$  and  $\vec{c} = 3\hat{j} - 2\hat{k}$ . Let  $\vec{x}$ ,  $\vec{y}$  and  $\vec{z}$  be three vectors in the plane of  $\vec{a}$ ,  $\vec{b}$ ;  $\vec{b}$ ,  $\vec{c}$ ;  $\vec{c}$ ,  $\vec{a}$ , respectively. Then

A.  $\vec{z} \cdot \vec{d} = 0$

B.  $\vec{x} \cdot \vec{d} = 1$

C.  $\vec{y} \cdot \vec{d} = 32$

D.  $\vec{r} \cdot \vec{d} = 0$ , where  $\vec{r} = \lambda\vec{x} + \mu\vec{y} + \gamma\vec{z}$

Answer: a,d

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200. A parallelogram is constructed on the vectors  $\vec{a} = 3\vec{\alpha} - \vec{\beta}$ ,  $\vec{b} = \vec{\alpha} + 3\vec{\beta}$ . If  $|\vec{\alpha}| = |\vec{\beta}| = 2$  and angle between  $\vec{\alpha}$  and  $\vec{\beta}$  is  $\frac{\pi}{3}$  then the length of a diagonal of the parallelogram is (A)  $4\sqrt{5}$  (B)  $4\sqrt{3}$  (C)  $4\sqrt{7}$  (D) none of these

A.  $4\sqrt{5}$

B.  $4\sqrt{3}$

C.  $4\sqrt{7}$

D. none of these

**Answer: b,c**

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**201.** Statement 1: Vector  $\vec{c} = -5\hat{i} + 7\hat{j} + 2\hat{k}$  is along the bisector of angle between  $\vec{a} = \hat{i} + 2\hat{j} + 2\hat{k}$  and  $\vec{b} = 8\hat{i} + \hat{j} - 4\hat{k}$ .

Statement 2 :  $\vec{c}$  is equally inclined to  $\vec{a}$  and  $\vec{b}$ .

A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. Statement 1 is true and Statement 2 is false

D. Statement 1 is false and Statement 2 is true.

**Answer: b**



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**202.** Statement 1: A component of vector  $\vec{b} = 4\hat{i} + 2\hat{j} + 3\hat{k}$  in the direction perpendicular to the direction of vector  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$  is  $\frac{1}{\sqrt{3}}$ .

Statement 2: A component of vector  $\vec{b}$  in the direction of  $\vec{a}$  is  $\frac{1}{\sqrt{3}}$ .

A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. Statement 1 is true and Statement 2 is false

D. Statement 1 is false and Statement 2 is true.



**Answer: c**



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**203.** Statement 1: Distance of point D( 1,0,-1) from the plane of points A(

1,-2,0) , B ( 3, 1,2) and C( -1,1,-1) is  $\frac{8}{\sqrt{229}}$

Statement 2: volume of tetrahedron formed by the points A,B, C and D is

$$\frac{\sqrt{229}}{2}$$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

**Answer: d**





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204. Let  $\vec{r}$  be a non-zero vector satisfying  $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = 0$  for given non-zero vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$

Statement 1:  $[\vec{a} - \vec{b}, \vec{b} - \vec{c}, \vec{c} - \vec{a}] = 0$

Statement 2:  $[\vec{a}, \vec{b}, \vec{c}] = 0$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

**Answer: b**



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**205.** Statement 1: If  $a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  are three mutually perpendicular unit vectors then  $a_1\hat{i} + b_1\hat{j} + c_1\hat{k}$ ,  $a_2\hat{i} + b_2\hat{j} + c_2\hat{k}$  and  $a_3\hat{i} + b_3\hat{j} + c_3\hat{k}$  may be mutually perpendicular unit vectors.

Statement 2 : value of determinant and its transpose are the same.

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

**Answer: a**



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206. Statement 1:  $\vec{A} = 2\hat{i} + 3\hat{j} + 6\hat{k}$ ,  $\vec{B} = \hat{u} + \hat{j} - 2\hat{k}$  and  $\vec{C} = \hat{i} + 2\hat{j} + \hat{k}$  then

$$|\vec{A} \times (\vec{A} \times (\vec{A} \times \vec{B})) \cdot \vec{C}| = 243$$

$$\text{Statement 2: } |\vec{A} \times (\vec{A} \times (\vec{A} \times \vec{B})) \cdot \vec{C}| = |\vec{A}|^2 |[\vec{A}\vec{B}\vec{C}]|$$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

Answer: d



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207. Statement 1:  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three mutually perpendicular unit vectors and  $\vec{d}$  is a vector such that  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are non-coplanar. If

$$[\vec{d}\vec{b}\vec{c}] = [\vec{d}\vec{a}\vec{b}] = [\vec{d}\vec{c}\vec{a}] = 1, \text{ then } \vec{d} = \vec{a} + \vec{b} + \vec{c}$$

Statement 2:  $[\vec{d}\vec{b}\vec{c}] = [\vec{d}\vec{a}\vec{b}] = [\vec{d}\vec{c}\vec{a}] \Rightarrow \vec{d}$  is equally inclined to  $\vec{a}, \vec{b}$  and  $\vec{c}$ .

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

**Answer: b**



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**208.** Consider three vectors  $\vec{a}, \vec{b}$  and  $\vec{c}$

$$\text{Statement 1: } \vec{a} \times \vec{b} = \left( (\hat{i} \times \vec{a}) \cdot \vec{b} \right) \hat{i} + \left( (\hat{j} \times \vec{a}) \cdot \vec{b} \right) \hat{j} + \left( (\hat{k} \times \vec{a}) \cdot \vec{b} \right) \hat{k}$$

$$\text{Statement 2: } \vec{c} = \left( \hat{i} \cdot \vec{c} \right) \hat{i} + \left( \hat{j} \cdot \vec{c} \right) \hat{j} + \left( \hat{k} \cdot \vec{c} \right) \hat{k}$$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

**Answer: a**

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**209.** Let  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  be three unit vectors such that  $\vec{u} + \vec{v} + \vec{w} = \vec{a}$ ,  $\vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}$ ,  $(\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}$ ,  $\vec{a} \cdot \vec{u} = 3/2$ ,  $\vec{a} \cdot \vec{v} = 7/4$  and

Vector  $\vec{u}$  is

A.  $\vec{a} - \frac{2}{3}\vec{b} + \vec{c}$

B.  $\vec{a} + \frac{4}{3}\vec{b} + \frac{8}{3}\vec{c}$

$$C. 2\vec{a} - \vec{b} + \frac{1}{3}\vec{c}$$

$$D. \frac{4}{3}\vec{a} - \vec{b} + \frac{2}{3}\vec{c}$$

**Answer: b**



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**210.** Let  $\vec{u}, \vec{v}$  and  $\vec{w}$  be three unit vectors such that  $\vec{u} + \vec{v} + \vec{w} = \vec{a}$ ,  $\vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}$ ,  $(\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}$ ,  $\vec{a} \cdot \vec{u} = 3/2$ ,  $\vec{a} \cdot \vec{v} = 7/4$  and

Vector  $\vec{u}$  is

$$A. 2\vec{a} - 3\vec{c}$$

$$B. 3\vec{b} - 4\vec{c}$$

$$C. -4\vec{c}$$

$$D. \vec{a} + \vec{b} + 2\vec{c}$$

**Answer: c**



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211. Let  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  be three unit vectors such that  $\vec{u} + \vec{v} + \vec{w} = \vec{a}$ ,  $\vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}$ ,  $(\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}$ ,  $\vec{a} \cdot \vec{u} = 3/2$ ,  $\vec{a} \cdot \vec{v} = 7/4$  and

Vector  $\vec{u}$  is

A.  $\frac{2}{3}(2\vec{c} - \vec{b})$

B.  $\frac{1}{3}(\vec{a} - \vec{b} - \vec{c})$

C.  $\frac{1}{3}\vec{a} - \frac{2}{3}\vec{b} - 2\vec{c}$

D.  $\frac{4}{3}(\vec{c} - \vec{b})$

Answer: d



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212. Vectors  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^\circ$  with each other. If  $\vec{x} \times (\vec{y} \times (\vec{z} \times \vec{x})) = \vec{b}$  and  $\vec{x} \times \vec{y} = \vec{c}$ ,  $f \in d\vec{x}, \vec{y}, \vec{z}$  in terms of  $\vec{a}, \vec{b}$  and  $\vec{c}$ .



$$A. \frac{1}{2} [(\vec{a} - \vec{b}) \times \vec{c} + (\vec{a} + \vec{b})]$$

$$B. \frac{1}{2} [(\vec{a} + \vec{b}) \times \vec{c} + (\vec{a} - \vec{b})]$$

$$C. \frac{1}{2} [- (\vec{a} + \vec{b}) \times \vec{c} + (\vec{a} + \vec{b})]$$

$$D. \frac{1}{2} [(\vec{a} + \vec{b}) \times \vec{c} - (\vec{a} + \vec{b})]$$

**Answer: d**

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**213.** Vectors  $\vec{x}, \vec{y}, \vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^\circ$  with each other. If  $\vec{x} \times (\vec{y} \times (\vec{z} \times \vec{x})) = b\vec{n}$  and  $\vec{x} \times \vec{y} = \vec{c}$ ,  $f \in d\vec{x}, \vec{y}, \vec{z}$  in terms of  $\vec{a}, \vec{b}$  and  $\vec{c}$ .

$$A. \frac{1}{2} [(\vec{a} + \vec{c}) \times \vec{b} - \vec{b} - \vec{a}]$$

$$B. \frac{1}{2} [(\vec{a} - \vec{c}) \times \vec{b} + \vec{b} + \vec{a}]$$

$$C. \frac{1}{2} [(\vec{a} - \vec{b}) \times \vec{c} + \vec{b} + \vec{a}]$$

$$D. \frac{1}{2} [(\vec{a} - \vec{c}) \times \vec{a} + \vec{b} - \vec{a}]$$

**Answer: c**



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**214.** Vectors  $\vec{x}, \vec{y}, \vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^\circ$  with each other. If  $\vec{x} \times (\vec{y} \times (\vec{z} \times \vec{x})) = \vec{b}$  and  $\vec{x} \times \vec{y} = \vec{c}$ ,  $f \in d\vec{x}, \vec{y}, \vec{z}$  in terms of  $\vec{a}, \vec{b}$  and  $\vec{c}$ .

A.  $\frac{1}{2} [(\vec{a} - \vec{c}) \times \vec{c} - \vec{b} + \vec{a}]$

B.  $\frac{1}{2} [(\vec{a} - \vec{b}) \times \vec{c} + \vec{b} - \vec{a}]$

C.  $\frac{1}{2} [\vec{c} \times (\vec{a} - \vec{b}) + \vec{b} + \vec{a}]$

D. none of these

**Answer: b**



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215. If  $\vec{x} \times \vec{y} = \vec{a}$ ,  $\vec{y} \times \vec{z} = \vec{b}$ ,  $\vec{x} \cdot \vec{b} = \gamma$ ,  $\vec{x} \cdot \vec{y} = 1$  and  $\vec{y} \cdot \vec{z} = 1$  then find  $x, y, z$  in terms of  $\vec{a}, \vec{b}$  and  $\gamma$ .

A.  $\frac{1}{|\vec{a} \times \vec{b}|^2} [\vec{a} \times (\vec{a} \times \vec{b})]$

B.  $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} \times \vec{b} - \vec{a} \times (\vec{a} \times \vec{b})]$

C.  $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} \times \vec{b} + \vec{a} \times (\vec{a} \times \vec{b})]$

D. none of these

Answer: b



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216. If  $\vec{x} \times \vec{y} = \vec{a}$ ,  $\vec{y} \times \vec{z} = \vec{b}$ ,  $\vec{x} \cdot \vec{b} = \gamma$ ,  $\vec{x} \cdot \vec{y} = 1$  and  $\vec{y} \cdot \vec{z} = 1$  then find  $x, y, z$  in terms of  $\vec{a}, \vec{b}$  and  $\gamma$ .

A.  $\frac{\vec{a} \times \vec{b}}{\gamma}$

B.  $\vec{a} + \frac{\vec{a} \times \vec{b}}{\gamma}$

C.  $\vec{a} + \vec{b} + \frac{\vec{a} \times \vec{b}}{\gamma}$

D. none of these

**Answer: a**

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**217.** If  $\vec{x} \times \vec{y} = \vec{a}$ ,  $\vec{y} \times \vec{z} = \vec{b}$ ,  $\vec{x} \cdot \vec{b} = \gamma$ ,  $\vec{x} \cdot \vec{y} = 1$  and  $\vec{y} \cdot \vec{z} = 1$  then find  $x, y, z$  in terms of  $\vec{a}, \vec{b}$  and  $\gamma$ .

A.  $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} + \vec{b} \times (\vec{a} \times \vec{b})]$

B.  $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} + \vec{b} - \vec{a} \times (\vec{a} \times \vec{b})]$

C.  $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} + \vec{b} + \vec{a} \times (\vec{a} \times \vec{b})]$

D. none of these

**Answer: c**



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218. Given two orthogonal vectors  $\vec{A}$  and  $\vec{B}$  each of length unity. Let  $\vec{P}$  be the vector satisfying the equation  $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$ . then

$(\vec{P} \times \vec{B}) \times \vec{B}$  is equal to

A.  $\vec{P}$

B.  $-\vec{P}$

C.  $2\vec{B}$

D.  $\vec{A}$

Answer: b



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219. Given two orthogonal vectors  $\vec{A}$  and  $\vec{B}$  each of length unity. Let  $\vec{P}$  be the vector satisfying the equation  $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$ . then

$\vec{P}$  is equal to

A.  $\frac{\vec{A}}{2} + \frac{\vec{A} \times \vec{B}}{2}$

B.  $\frac{\vec{A}}{2} + \frac{\vec{B} \times \vec{A}}{2}$

C.  $\frac{\vec{A} \times \vec{B}}{2} - \frac{\vec{A}}{2}$

D.  $\vec{A} \times \vec{B}$

Answer: b



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220. Given two orthogonal vectors  $\vec{A}$  and  $\vec{B}$  each of length unity. Let  $\vec{P}$  be the vector satisfying the equation  $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$ . then which of the following statements is false ?

A. vectors  $\vec{P}$ ,  $\vec{A}$  and  $\vec{P} \times \vec{B}$  are linearly dependent.

B. vectors  $\vec{P}$ ,  $\vec{B}$  and  $\vec{P} \times \vec{B}$  are linearly independent

C.  $\vec{P}$  is orthogonal to  $\vec{B}$  and has length  $\frac{1}{\sqrt{2}}$ .

D. none of these

**Answer: d**

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**221.** Let  $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$ ,  $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and  $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$ . Let  $\vec{a}_1$  be the projection of  $\vec{a}$  on  $\vec{b}$  and  $\vec{a}_2$  be the projection of  $\vec{a}_1$  on  $\vec{c}$ . Then  $\vec{a}_2$  is equal to

A.  $\frac{943}{49} (2\hat{i} - 3\hat{j} - 6\hat{k})$

B.  $\frac{943}{49^2} (2\hat{i} - 3\hat{j} - 6\hat{k})$

C.  $\frac{943}{49} (-2\hat{i} + 3\hat{j} + 6\hat{k})$

D.  $\frac{943}{49^2} (-2\hat{i} + 3\hat{j} + 6\hat{k})$

**Answer: b**

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222. Let  $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$ ,  $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and  $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$ . Let  $\vec{a}_1$  be the projection of  $\vec{a}$  on  $\vec{b}$  and  $\vec{a}_2$  be the projection of  $\vec{a}_1$  on  $\vec{c}$ . Then  $\vec{a}_1 \cdot \vec{b}$  is equal to

A. -41

B. -41/7

C. 41

D. 287

**Answer: a**



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223. Let  $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$ ,  $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and  $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$ . Let  $\vec{a}_1$  be the projection of  $\vec{a}$  on  $\vec{b}$  and  $\vec{a}_2$  be the projection of  $\vec{a}_1$  on  $\vec{c}$ . Then which of the following is true ?



A.  $\vec{a}$  and  $\vec{a}_2$  are collinear

B.  $\vec{a}_1$  and  $\vec{c}$  are collinear

C.  $\vec{a}, \vec{a}_1$  and  $\vec{b}$  are coplanar

D.  $\vec{a}, \vec{a}_1$  and  $\vec{a}_2$  are coplanar

**Answer: c**



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**224.** Consider a triangular pyramid ABCD the position vectors of whose angular points are  $A(3, 0, 1), B(-1, 4, 1), C(5, 3, 2)$  and  $D(0, -5, 4)$ . Let G be the point of intersection of the medians of the triangle BCT. The length of the vector  $\vec{AG}$  is

A.  $\sqrt{17}$

B.  $\sqrt{51}/3$

C.  $3/\sqrt{6}$

D.  $\sqrt{59}/4$

**Answer: b**



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**225.** Consider a triangular pyramid ABCD the position vectors of whose angular points are  $A(3, 0, 1)$ ,  $B(-1, 4, 1)$ ,  $C(5, 3, 2)$  and  $D(0, -5, 4)$ . Let G be the point of intersection of the medians of the triangle BCT. The length of the vector  $\overrightarrow{AG}$  is

A. 24

B.  $8\sqrt{6}$

C.  $4\sqrt{6}$

D. none of these

**Answer: c**



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**226.** Consider a triangular pyramid ABCD the position vectors of whose angular points are  $A(3, 0, 1)$ ,  $B(-1, 4, 1)$ ,  $C(5, 3, 2)$  and  $D(0, -5, 4)$ . Let G be the point of intersection of the medians of the triangle BCT. The length of the vector  $AG$  is

A.  $14/\sqrt{6}$

B.  $2/\sqrt{6}$

C.  $3/\sqrt{6}$

D. none of these

**Answer: a**



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**227.** Vertices of a parallelogram taken in order are A, (2, -1, 4), B (1, 0, -1), C (1, 2, 3) and D.

The distance between the parallel lines AB and CD is

A.  $\sqrt{6}$

B.  $3\sqrt{6/5}$

C.  $2\sqrt{2}$

D. 3

**Answer: c**



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**228.** Vertices of a parallelogram taken in order are A, ( 2,-1,4 ) , B (1,0,-1) , C ( 1,2,3) and D.

Distance of the point P ( 8, 2,-12) from the plane of the parallelogram is

A.  $\frac{4\sqrt{6}}{9}$

B.  $\frac{32\sqrt{6}}{9}$

C.  $\frac{16\sqrt{6}}{9}$

D. none

**Answer: b**



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**229.** Vertices of a parallelogram taken in order are A, ( 2,-1,4) , B (1,0,-1) , C ( 1,2,3) and D.

The distance between the parallel lines AB and CD is

A. 14, 4,2

B. 2,4,14

C. 4,2,14

D. 2,14,4

**Answer: d**



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**230.** Let  $\vec{r}$  is a positive vector of a variable point in cartesian OXY plane such that  $\vec{r} \cdot (10\hat{j} - 8\hat{i} - \vec{r}) = 40$  and

$$p_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}, p_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}.$$

A tangent line is drawn to the curve  $y = \frac{8}{x^2}$  at the point A with abscissa 2. The drawn line cuts x-axis at a point B

- A. 9
- B.  $2\sqrt{2} - 1$
- C.  $6\sqrt{6} + 3$
- D.  $9 - 4\sqrt{2}$

**Answer: d**



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**231.** Let  $\vec{r}$  is a positive vector of a variable point in cartesian OXY plane such that  $\vec{r} \cdot (10\hat{j} - 8\hat{i} - \vec{r}) = 40$  and

$p_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}, p_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}$ . A tangent line is drawn to the curve  $y = \frac{8}{x^2}$  at the point A with abscissa 2. The drawn line cuts x-axis at a point B

- A. 2
- B. 10
- C. 18
- D. 5

**Answer: c**



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**232.** Let  $\vec{r}$  is a positive vector of a variable point in cartesian OXY plane

such that  $\vec{r} \cdot (10\hat{j} - 8\hat{i} - \vec{r}) = 40$  and

$p_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}, p_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}$ . A tangent line is drawn to the curve  $y = \frac{8}{x^2}$  at the point A with abscissa 2. The drawn line cuts x-axis at a point B

A. 1

B. 2

C. 3

D. 4

Answer: c



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233.  $\vec{AB}$ ,  $\vec{AC}$  and  $\vec{AD}$  are three adjacent edges of a parallelepiped. The diagonal of the parallelepiped passing through A and directed away from it is vector  $\vec{a}$ . The vector of the faces containing vertices A, B, C and A, B, D are  $\vec{b}$  and  $\vec{c}$ , respectively, i.e.  $\vec{AB} \times \vec{AC}$  and  $\vec{AD} \times \vec{AB} = \vec{c}$  the

projection of each edge AB and AC on diagonal vector  $\vec{a}$  is  $\frac{|\vec{a}|}{3}$

vector  $\vec{AB}$  is

$$\text{A. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$$



$$\text{B. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

$$\text{C. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

D. none of these

**Answer: a**



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**234.** Ab, AC and AD are three adjacent edges of a parallelepiped. The diagonal of the parallelepiped passing through A and directed away from it is vector  $\vec{a}$ . The vector of the faces containing vertices A, B, C and

A, B, D are  $\vec{b}$  and  $\vec{c}$ , respectively, i.e.  $\vec{AB} \times \vec{AC} = \vec{b}$  and  $\vec{AD} \times \vec{AB} = \vec{c}$  the

projection of each edge AB and AC on diagonal vector  $\vec{a}$  is  $\frac{|\vec{a}|}{3}$  vector AC is

$$\text{A. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$$

$$\text{B. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

$$\text{C. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

D. none of these

**Answer: b**

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**235.** Ab, AC and AD are three adjacent edges of a parallelepiped. The diagonal of the parallelepiped passing through A and directed away from it is vector  $\vec{a}$ . The vector of the faces containing vertices A, B, C and A, B, D are  $\vec{b}$  and  $\vec{c}$ , respectively, i.e.  $\vec{AB} \times \vec{AC} = \vec{b}$  and  $\vec{AD} \times \vec{AB} = \vec{c}$  the projection of each edge AB and AC on diagonal vector  $\vec{a}$  is  $\frac{|\vec{a}|}{3}$  vector  $\vec{AD}$  is

$$\text{A. } \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$$

B.  $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

C.  $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

D. none of these

Answer: c

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238. 



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239. Given two vectors  $\vec{a} = -\hat{i} + \hat{j} + 2\hat{k}$  and  $\vec{b} = -\hat{i} - 2\hat{j} - \hat{k}$



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240. Given two vectors  $\vec{a} = -\hat{i} + 2\hat{j} + 2\hat{k}$  and  $\vec{b} = -2\hat{i} + \hat{j} + 2\hat{k}$



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241. 



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242. Volume of parallelepiped formed by vectors  $\vec{a} \times \vec{b}$ ,  $\vec{b} \times \vec{c}$  and  $\vec{c} \times \vec{a}$  is 36 sq. units.



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243. If  $\vec{a}$  and  $\vec{b}$  are any two unit vectors, then find the greatest positive integer in the range of  $\frac{3|\vec{a} + \vec{b}|}{2} + 2|\vec{a} - \vec{b}|$

integer in the range of  $\frac{3|\vec{a} + \vec{b}|}{2} + 2|\vec{a} - \vec{b}|$



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244. Let  $\vec{u}$  be a vector on rectangular coordinate system with sloping angle  $60^\circ$  suppose that  $|\vec{u} - \hat{i}|$  is geometric mean of  $|\vec{u}|$  and  $|\vec{u} - 2\hat{i}|$ , where  $\hat{i}$  is the unit vector along the x-axis. Then find the value of  $(\sqrt{2} + 1)|\vec{u}|$



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245. Find the absolute value of parameter  $t$  for which the area of the triangle whose vertices are  $A(-1, 1, 2)$ ;  $B(1, 2, 3)$  and  $C(5, 1, 1)$  is minimum.

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246. If

$$\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}, \vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}, \vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k} \text{ and } [3\vec{a} + \vec{b} = \vec{c}3\vec{c}]$$

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247. Let  $\vec{a} = \alpha\hat{i} + 2\hat{j} - 3\hat{k}$ ,  $\vec{b} = \hat{i} + 2\alpha\hat{j} - 2\hat{k}$  and  $\vec{c} = 2\hat{i} - \alpha\hat{j} + \hat{k}$ . Find the value of  $6\alpha$ . Such that  $\{(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c})\} \times (\vec{c} \times \vec{a}) = 0$

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**248.** If  $\vec{x}, \vec{y}$  are two non-zero and non-collinear vectors satisfying  $[(a-2)\alpha^2 + (b-3)\alpha + c]\vec{x} + [(a-2)\beta^2 + (b-3)\beta + c]\vec{y} + [(a-2)\gamma^2 + (b-3)\gamma + c]\vec{z}$  are three distinct real numbers, then find the value of  $(a^2 + b^2 + c^2 - 4)$ .

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**249.** Let  $\vec{u}$  and  $\vec{v}$  be unit vectors such that  $\vec{u} \times \vec{v} + \vec{u} = \vec{w}$  and  $\vec{w} \times \vec{u} = \vec{v}$ . Find the value of  $[\vec{u}\vec{v}\vec{w}]$

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**250.** The volume of the tetrahedron whose vertices are the points with position vectors  $\hat{i} - 5\hat{j} + 10\hat{k}$ ,  $-\hat{i} - 3\hat{j} + 7\hat{k}$ ,  $5\hat{i} - \hat{j} + \lambda\hat{k}$  and  $7\hat{i} - 4\hat{j} + 7\hat{k}$  is 11 cubic units then the value of  $\lambda$  is (A) 7 (B) 1 (C) -7 (D) -1

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251.

Given

that

$$\vec{u} = \hat{i} + 2\hat{j} + 3\hat{k}, \vec{v} = 2\hat{i} + \hat{k} + 4\hat{k}, \vec{w} = \hat{i} + 3\hat{j} + 3\hat{k} \text{ and } (\vec{u} \cdot \vec{R} - 15)\hat{i} + (\vec{c} \cdot \vec{R} - 30)\hat{j}$$

. Then find the greatest integer less than or equal to  $|\vec{R}|$ .

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252. Let a three- dimensional vector  $\vec{V}$  satisfy the condition ,

$$2\vec{V} + \vec{V} \times (\hat{i} + 2\hat{j}) = 2\hat{i} + \hat{k}. \text{ If } 3|\vec{V}| = \sqrt{m}. \text{ Then find the value of } m.$$

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253. If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors such that  $\vec{a} \cdot \vec{b} = 0 = \vec{a} \cdot \vec{c}$  and the angle

between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$ , then find the value of  $|\vec{a} \times \vec{b} - \vec{a} \times \vec{c}|$

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254. Let  $\vec{OA} = \vec{a}$ ,  $\vec{OB} = 10\vec{a} + 2\vec{b}$  and  $\vec{OC} = \vec{b}$ , where O, A and C are non-collinear points. Let P denote the area of quadrilateral OACB. And let q denote the area of parallelogram with OA and OC as adjacent sides. If  $p = kq$ , then find k.

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255. Find the work done by the force  $F = 3\hat{i} - \hat{j} - 2\hat{k}$  acting on a particle such that the particle is displaced from point  $A(-3, -4, 1)$  to  $B(-1, -1, -2)$ .

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256. From a point O inside a triangle ABC, perpendiculars OD, OE and OF are drawn to the sides BC, CA and AB, respectively. Prove that the perpendiculars from A, B and C to the sides EF, FD and DE are concurrent.

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257.  $A_1, A_2, \dots, A_n$  are the vertices of a regular plane polygon with  $n$  sides

and  $O$  is its centre. Show that 
$$\sum_{i=1}^{n-1} \left( \vec{OA}_i \times \vec{OA}_{i+1} \right) = (1 - n) \left( \vec{OA}_2 \times \vec{OA}_1 \right)$$

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258. If  $c$  is a given non-zero scalar, and  $\vec{A}$  and  $\vec{B}$  are given non-zero vectors such that  $\vec{A} \perp \vec{B}$ . Then find vector,  $\vec{X}$  which satisfies the equations

$\vec{A} \cdot \vec{X} = c$  and  $\vec{A} \times \vec{X} = \vec{B}$ .

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259.  $A, B, C$  and  $D$  are any four points in the space, then prove that

$$\left| \vec{AB} \times \vec{CD} + \vec{BC} \times \vec{AD} + \vec{CA} \times \vec{BD} \right| = 4 \text{ (area of } ABC \text{.)}$$

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260. If the vectors  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are coplanar show that

$$\begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \end{vmatrix} = 0$$

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261.  $\vec{A} = (2\vec{i} + \vec{k})$ ,  $\vec{B} = (\vec{i} + \vec{j} + \vec{k})$  and  $\vec{C} = 4\vec{i} - 3\vec{j} + 7\vec{k}$  determine a vector  $\vec{R}$  satisfying  $\vec{R} \times \vec{B} = \vec{C} \times \vec{B}$  and  $\vec{R} \cdot \vec{A} = 0$

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262. Determine the value of  $c$  so that for the real  $x$ , vectors  $c\hat{i} - 6\hat{j} - 3\hat{k}$  and  $x\hat{i} + 2\hat{j} + 2cx\hat{k}$  make an obtuse angle with each other.

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263.

Prove

that:

$$(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) + (\vec{a} \times \vec{c}) \times (\vec{d} \times \vec{b}) + (\vec{a} \times \vec{d}) \times (\vec{b} \times \vec{c}) = 2[\vec{b} \vec{c} \vec{d}] \vec{a}$$


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**264.** The position vectors of the vertices A, B and C of a tetrahedron ABCD are  $\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{k}$ ,  $\hat{i}$  and  $3\hat{i}$ , respectively. The altitude from vertex D to the opposite face ABC meets the median line through A of triangle ABC at a point E. If the length of the side AD is 4 and the volume of the tetrahedron is  $\frac{2\sqrt{2}}{3}$ , find the position vectors of the point E for all its possible positions


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**265.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be non-coplanar unit vectors, equally inclined to one another at an angle  $\theta$ . If  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} = p\vec{a} + q\vec{b} + r\vec{c}$ , find scalars p, q and r in terms of  $\theta$ .



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266. If  $\vec{a}, \vec{b}, \vec{c}$  are vectors such that  $|\vec{b}| = |\vec{c}|$  then  
$$\{(\vec{a} + \vec{b}) \times (\vec{a} + \vec{c})\} \times (\vec{b} \times \vec{c}) \cdot (\vec{b} + \vec{c}) =$$

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267. For any two vectors  $\vec{u}$  and  $\vec{v}$  prove that

$$(1 + |\vec{u}|^2)(1 + |\vec{v}|^2) = (1 - \vec{u} \cdot \vec{v})^2 + |\vec{u} + \vec{v} + \vec{u} \times \vec{v}|^2$$

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268. Let  $\vec{u}$  and  $\vec{v}$  be unit vectors. If  $\vec{w}$  is a vector such that

$\vec{w} + \vec{u} \times \vec{v} = \vec{v}$ , then prove that  $|\vec{w}| \leq 1/2$

and the equality holds if and only if  $\vec{u}$  is perpendicular to  $\vec{v}$ .

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269. find three-dimensional vectors,

$\vec{v}_1, \vec{v}_2$  and  $\vec{v}_3$  satisfying  $\vec{v}_1 \cdot \vec{v}_2 = -2, \vec{v}_1 \cdot \text{Vec}v_3 = 6, \vec{v}_2 \cdot \vec{v}_2 = 2\vec{v}_2 \cdot \text{Vec}v_3 = -5$

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270. Let  $V$  be the volume of the parallelepiped formed by the vectors,

$\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}, \vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ . if  $a_r, b_r, c_r$

are non-negative real numbers and

$$\sum_{r=1}^3 (a_r + b_r + c_r) = 3L \text{ show that } V \leq L^3$$

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271.  $\vec{u}, \vec{v}$  and  $\vec{w}$  are three nono-coplanar unit vectors and  $\alpha, \beta$  and  $\gamma$  are

the angles between  $\vec{u}$  and  $\vec{u}, \vec{v}$  and  $\vec{w}$  and  $\vec{w}$  and  $\vec{u}$ , respectively and

$\vec{x}, \vec{y}$  and  $\vec{z}$  are unit vectors along the bisectors of the angles  $\alpha, \beta$  and  $\gamma$ .

respectively, prove that  $[\vec{x} \times \vec{y} \vec{y} \times \vec{z} \vec{z} \times \vec{x}] = \frac{1}{16} [\vec{u} \vec{v} \vec{w}]^2 \frac{\sec^2 \alpha}{2} \frac{\sec^2 \beta}{2} \frac{\sec^2 \gamma}{2}$ .

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**272.** If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are distinct vectors such that  $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$  and  $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$ . Prove that  $(\vec{a} \times \vec{d}) \cdot (\vec{b} \cdot \vec{c}) \neq 0$ , i. e.,  $\vec{a} \cdot \vec{b} + \vec{d} \cdot \vec{c} \neq \vec{d} \cdot \vec{b} + \vec{a} \cdot \vec{c}$ .

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**273.**  $P_1$  and  $P_2$  are planes passing through origin,  $L_1$  and  $L_2$  are two lines on  $P_1$  and  $P_2$  respectively such that their intersection is the origin. Show that there exist points, A, B and C, whose permutation, A, B' and C' respectively, can be chosen such that (i) A is on  $L_1$ , B' and C' are not on  $L_1$  and C' is not on  $P_1$ , (ii) A is on  $L_2$ , B' is on  $P_2$  but not on  $L_2$  and C' is not on  $P_2$ .

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274. If the incident ray on a surface is along the unit vector  $\vec{v}$ , the reflected ray is along the unit vector  $\vec{w}$  and the normal is along the unit vector  $\vec{a}$  outwards, express  $\vec{w}$  in terms of  $\vec{a}$  and  $\vec{v}$



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275. Let  $\vec{A}$ ,  $\vec{B}$  and  $\vec{C}$  be vectors of length 3, 4 and 5 respectively. Let  $\vec{A}$  be perpendicular to  $\vec{B} + \vec{C}$ ,  $\vec{B}$  to  $\vec{C} + \vec{A}$  and  $\vec{C}$  to  $\vec{A} + \vec{B}$  then the length of vector  $\vec{A} + \vec{B} + \vec{C}$  is \_\_\_\_\_.



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276. The unit vector perpendicular to the plane determined by P (1,-1,2), C(3,-1,2) is \_\_\_\_\_.



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277. the area of the triangle whose vertices are A ( 1,-1,2) , B ( 1,2, -1) ,C ( 3, -1, 2) is \_\_\_\_\_.

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278. If  $\vec{A}, \vec{B}, \vec{C}$  are non-coplanar vectors then  $\frac{\vec{A} \cdot \vec{B} \times \vec{C}}{\vec{C} \times \vec{A} \cdot \vec{B}} + \frac{\vec{B} \cdot \vec{A} \times \vec{C}}{\vec{C} \cdot \vec{A} \times \vec{B}} =$

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279. If  $\vec{A} = (1, 1, 1)$  and  $\vec{C} = (0, 1, -1)$  are given vectors then find a vector  $\vec{B}$  satisfying equations  $\vec{A} \times \vec{B} = \vec{C}$  and  $\vec{A} \cdot \vec{B} = 3$

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280. Let  $\vec{b} = 4\hat{i} + 3\hat{j}$  and  $\vec{c}$  be two vectors perpendicular to each other in the xy-plane. Find all vectors in the same plane having projection 1 and 2

along  $\vec{b}$  and  $\vec{c}$  respectively.



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281. The components of a vector  $\vec{a}$  along and perpendicular to a non-zero vector  $\vec{b}$  are \_\_\_\_\_ and \_\_\_\_\_, respectively.



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282. A unit vector coplanar with  $\vec{i} + \vec{j} + 2\vec{k}$  and  $\vec{i} + 2\vec{j} + \vec{k}$  and perpendicular to  $\vec{i} + \vec{j} + \vec{k}$  is \_\_\_\_\_



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283. A non vector  $\vec{a}$  is parallel to the line of intersection of the plane determined by the vectors  $\hat{i}, \hat{i} + \hat{j}$  and the plane determined by the vectors  $\hat{i} - \hat{j}, \hat{i} + \hat{k}$  then angle between  $\vec{a}$  and  $\hat{i} - 2\hat{j} + 2\hat{k}$  is = (A)  $\frac{\pi}{2}$  (B)  $\frac{\pi}{3}$  (C)  $\frac{\pi}{6}$  (D)  $\frac{\pi}{4}$



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284. If  $\vec{b}$  and  $\vec{c}$  are any two mutually perpendicular unit vectors and  $\vec{a}$  is

any vector, then  $(\vec{a} \cdot \vec{b})\vec{b} + (\vec{a} \cdot \vec{c})\vec{c} + \frac{\vec{a} \cdot (\vec{b} \times \vec{c})}{|\vec{b} \times \vec{c}|^2}(\vec{b} \times \vec{c}) =$  (A) 0 (B)  $\vec{a}$  (C)

(D)  $2\vec{a}$

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285. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three vectors having magnitudes 1, 1 and 2 respectively. If  $\vec{a} \times (\vec{a} \times \vec{c}) + \vec{b} = \vec{0}$  then the acute angle between  $\vec{a}$  and  $\vec{c}$  is

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286. A, B, C and D are four points in a plane with position vectors,  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  respectively, such that

$(\vec{a} - \vec{d}) \cdot (\vec{b} - \vec{c}) = (\vec{b} - \vec{d}) \cdot (\vec{c} - \vec{a}) = 0$  then point D is the \_\_\_\_\_ of triangle ABC.

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287. If

$$\vec{A} = \lambda(\vec{u} \times \vec{v}) + \mu(\vec{v} \times \vec{w}) + \nu(\vec{w} \times \vec{u}) \text{ and } [\vec{u} \vec{v} \vec{w}] = \frac{1}{5} \text{ then } \lambda + \mu + \nu = \text{ (A) } 5$$

(B) 10 (C) 15 (D) none of these

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288. If  $\vec{a} = \hat{j} + \sqrt{3}\hat{k}$ ,  $\vec{b} = -\hat{j} + \sqrt{3}\hat{k}$  and  $\vec{c} = 2\sqrt{3}\hat{k}$  form a triangle, then the internal angle of the triangle between  $\vec{a}$  and  $\vec{b}$  is \_\_\_\_\_

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289. Let  $\vec{A}$ ,  $\vec{B}$  and  $\vec{C}$  be unit vectors such that  $\vec{A} \cdot \vec{B} = \vec{A} \cdot \vec{C} = 0$  and the angle between  $\vec{B}$  and  $\vec{C}$  be  $\pi/3$ . Then  $\vec{A} = \pm 2(\vec{B} \times \vec{C})$ .



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290. If  $\vec{x} \cdot \vec{a} = 0$ ,  $\vec{x} \cdot \vec{b} = 0$  and  $\vec{x} \cdot \vec{c} = 0$  for some non zero vector  $\vec{x}$  then show that  $[\vec{a} \vec{b} \vec{c}] = 0$



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291. For any three vectors,  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ ,  $(\vec{a} - \vec{b}) \cdot (\vec{b} - \vec{c}) \times (\vec{c} - \vec{a}) = 2\vec{a} \cdot \vec{b} \times \vec{c}$ .



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292. The scalar  $\vec{A} \cdot (\vec{B} + \vec{C}) \times (\vec{A} + \vec{B} + \vec{C})$  equals (A) 0 (B)  $[\vec{A} \vec{B} \vec{C}] + [\vec{B} \vec{C} \vec{A}]$  (C)  $[\vec{A} \vec{B} \vec{C}]$  (D) none of these

A. 0

B.  $[\vec{A} \vec{B} \vec{C}] + [\vec{B} \vec{C} \vec{A}]$

c.  $[\vec{A}\vec{B}\vec{C}]$

D. none of these

**Answer: a**



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**293.** For non zero vectors  $\vec{a}, \vec{b}, \vec{c}$

$$\left| (\vec{a} \times \vec{b}) \cdot \vec{c} \right| = |\vec{a}| |\vec{b}| |\vec{c}| \text{ holds iff}$$

A.  $\vec{a} \cdot \vec{b} = 0, \vec{b} \cdot \vec{c} = 0$

B.  $\vec{b} \cdot \vec{c} = 0, \vec{c} \cdot \vec{a} = 0$

C.  $\vec{c} \cdot \vec{a} = 0, \vec{a} \cdot \vec{b} = 0$

D.  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a} = 0$

**Answer: d**



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**294.** The volume of the parallelepiped whose sides are given by

$$\vec{OA} = 2i - 2j, \vec{OB} = i + j - k \text{ and } \vec{OC} = 3i - k$$

A.  $\frac{4}{13}$

B. 4

C.  $\frac{2}{7}$

D. 2

**Answer: d**



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**295.** Let  $\vec{a}, \vec{b}, \vec{c}$  be three noncoplanar vectors and  $\vec{p}, \vec{q}, \vec{r}$  are vectors

defined by the relations  $\vec{p} = (\vec{b} \times \vec{c}) / ([\vec{a} \ \vec{b} \ \vec{c}])$ ,  $\vec{q} =$

$(\vec{c} \times \vec{a}) / ([\vec{a} \ \vec{b} \ \vec{c}])$ ,  $\vec{r} = (\vec{a} \times \vec{b}) / ([\vec{a} \ \vec{b} \ \vec{c}])$

then the value of the expression  $(\vec{a} + \vec{b}) \cdot \vec{p} + (\vec{b} + \vec{c}) \cdot \vec{q} +$

$(\vec{c} + \vec{a}) \cdot \vec{r}$  is equal to (A) 0 (B) 1 (C) 2 (D) 3

A. 0

B. 1

C. 2

D. 3

Answer: d



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296. Let  $\vec{a} = \hat{i} - \hat{j}$ ,  $\vec{b} = \hat{j} - \hat{k}$ ,  $\vec{c} = \hat{k} - \hat{i}$ . If  $\hat{d}$  is a unit vector such that  $\vec{a} \cdot \hat{d} = 0 = [\vec{b}, \vec{c}, \hat{d}]$  then  $\hat{d}$  equals (A)  $-(\hat{i} + \hat{j} - 2\hat{k})/\sqrt{6}$  (B)  $(\hat{i} + \hat{j} - \hat{k})/\sqrt{3}$  (C)  $(\hat{i} + \hat{j} + \hat{k})/\sqrt{3}$  (D)  $-\hat{k}$

A.  $\pm \frac{\hat{i} + \hat{j} - 2\hat{k}}{\sqrt{6}}$

B.  $\pm \frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$

C.  $\pm \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$

D.  $\pm \hat{k}$



**Answer: a**



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**297.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non coplanar and unit vectors such that

$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\vec{b} + \vec{c}}{\sqrt{92}}$  then the angle between  $\vec{a}$  and  $\vec{b}$  is (A)  $\frac{3\pi}{4}$  (B)  $\frac{\pi}{4}$

(C)  $\frac{\pi}{2}$  (D)  $\pi$

A.  $3\pi/4$

B.  $\pi/4$

C.  $\pi/2$

D.  $\pi$

**Answer: a**



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298. Let  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  be vectors such that  $\vec{u} + \vec{v} + \vec{w} = 0$  if  $|\vec{u}| = 3$ ,  $|\vec{v}| = 4$  and  $|\vec{w}| = 5$  then  $\vec{u} \cdot \vec{v} + \vec{v} \cdot \vec{w} + \vec{w} \cdot \vec{u}$  is

A. 47

B. -25

C. 0

D. 25

Answer: b



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299. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors, then  $(\vec{a} + \vec{b} + \vec{c}) \cdot [(\vec{a} + \vec{b}) \times (\vec{a} + \vec{c})]$  equals

A. 0

B.  $[\vec{a}\vec{b}\vec{c}]$

C.  $2[\vec{a}\vec{b}\vec{c}]$

$$D. - [\vec{a}\vec{b}\vec{c}]$$

**Answer: d**



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**300.** Let  $\vec{p}, \vec{q}, \vec{r}$  be three mutually perpendicular vectors of the same magnitude. If a vector  $\vec{x}$  satisfies the equation

$$\vec{p} \times \{ \vec{x} - \vec{q} \} \times \vec{p} \} + \vec{q} \times \{ \vec{x} - \vec{r} \} \times \vec{q} \} + \vec{r} \times \{ \vec{x} - \vec{p} \} \times \vec{r} \} = \vec{0},$$

then  $\vec{x}$  is given by

A.  $\frac{1}{2}(\vec{p} + \vec{q} - 2\vec{r})$

B.  $\frac{1}{2}(\vec{p} + \vec{q} + \vec{r})$

C.  $\frac{1}{3}(\vec{p} + \vec{q} + \vec{r})$

D.  $\frac{1}{3}(2\vec{p} + \vec{q} - \vec{r})$

**Answer: b**



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**301.** Let  $\vec{a} = 2i + j - 2k$ , and  $b = i + j$  if  $c$  is a vector such that  $\vec{a} \cdot \vec{c} = |\vec{c}|$ ,  $|\vec{c} - \vec{a}| = 2\sqrt{2}$  and the angle between  $\vec{a} \times \vec{b}$  and  $\vec{c}$  is  $30^\circ$ , then  $|(\vec{a} \times \vec{b}) \times \vec{c}|$  is equal to

A.  $2/3$

B.  $3/2$

C. 2

D. 3

**Answer: b**



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**302.** Let  $\vec{a} = 2i + j + k$ ,  $\vec{b} = i + 2j - k$  and a unit vector  $\vec{c}$  be coplanar. If  $\vec{c}$  is perpendicular to  $\vec{a}$ . Then  $\vec{c}$  is

A.  $\frac{1}{\sqrt{2}}(-j + k)$

B.  $\frac{1}{\sqrt{3}}(i - j - k)$

$$C. \frac{1}{\sqrt{5}}(i - 2j)$$

$$D. \frac{1}{\sqrt{3}}(i - j - k)$$

**Answer: a**

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**303.** If the vectors  $\vec{a}, \vec{b}, \vec{c}$  form the sides BC, CA and AB respectively of a triangle ABC then (A)  $\vec{a} \cdot (\vec{b} \times \vec{c}) = \vec{0}$  (B)  $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{0}$  (C)  $\vec{a} \cdot \vec{b} = \vec{c} \cdot \vec{c} = \vec{a} \cdot \vec{a} \neq 0$  (D)  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \vec{0}$

$$A. \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = 0$$

$$B. \vec{a} \times \vec{b} = \vec{b} \times \vec{c} = \vec{c} \times \vec{a}$$

$$C. \vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a}$$

$$D. \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \vec{0}$$

**Answer: b**

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**304.** Let the vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  be such that  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = \vec{0}$ . Let  $P_1$  and  $P_2$  be planes determined by pairs of vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ ,  $\vec{d}$  respectively. Then the  $\angle$  between  $P_1$  and  $P_2$  is (A) 0 (B)  $\pi/4$  (C)  $\pi/3$  (D)  $\pi/2$

A. 0

B.  $\pi/4$

C.  $\pi/3$

D.  $\pi/2$

**Answer: a**



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**305.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit coplanar vectors, then the scalar triple product  $[2\vec{a} - \vec{b} \quad 2\vec{b} - \vec{c} \quad 2\vec{c} - \vec{a}]$  is

A. 0

B. 1

C.  $-\sqrt{3}$

D.  $\sqrt{3}$

**Answer: a**



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**306.** if  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  are unit vectors. Then  $|\hat{a} - \hat{b}|^2 + |\hat{b} - \hat{c}|^2 + |\hat{c} - \hat{a}|^2$  does not exceed

A. 4

B. 9

C. 8

D. 6

**Answer: b**



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307. If  $\vec{a}$  and  $\vec{b}$  are two unit vectors such that  $\vec{a} + 2\vec{b}$  and  $5\vec{a} - 4\vec{b}$  are perpendicular to each other then the angle between  $\vec{a}$  and  $\vec{b}$  is (A)  $45^\circ$

(B)  $60^\circ$  (C)  $\cos^{-1}\left(\frac{1}{3}\right)$  (D)  $\cos^{-1}\left(\frac{2}{7}\right)$

A.  $45^\circ$

B.  $60^\circ$

C.  $\cos^{-1}(1/3)$

D.  $\cos^{-1}(2/7)$

Answer: b



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308. Let  $\vec{V} = 2\hat{i} + \hat{j} - \hat{k}$  and  $\vec{W} = \hat{i} + 3\hat{k}$ . If  $\vec{U}$  is a unit vector, then the maximum value of the scalar triple product  $[\vec{U} \ \vec{V} \ \vec{W}]$  is



A. -1

B.  $\sqrt{10} + \sqrt{6}$

C.  $\sqrt{59}$

D.  $\sqrt{60}$

**Answer: c**



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**309.** The value of  $a$  so that the volume of parallelepiped formed by vectors

$\hat{i} + a\hat{j} + \hat{k}, \hat{j} + a\hat{k}, a\hat{i} + \hat{k}$  becomes minimum is (A)  $\sqrt{93}$  (B) 2 (C)  $\frac{1}{\sqrt{3}}$  (D) 3

A. -3

B. 3

C.  $1/\sqrt{3}$

D.  $\sqrt{3}$

**Answer: c**



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310. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{a} \cdot \vec{b} = 1$  and  $\vec{a} \times \vec{b} = \hat{j} - \hat{k}$  then  $\vec{b}$

A.  $\hat{i} - \hat{j} + \hat{k}$

B.  $2\hat{i} - \hat{k}$

C.  $\hat{i}$

D.  $2\hat{i}$

Answer: c



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311. The unit vector which is orthogonal to the vector  $5\hat{j} + 2\hat{k}$  and is coplanar with vectors  $2\hat{i} + \hat{j} + \hat{k}$  and  $\hat{i} - \hat{j} + \hat{k}$  is

A.  $\frac{2\hat{i} - 6\hat{j} + \hat{k}}{\sqrt{41}}$

$$B. \frac{2\hat{i} - 3\hat{j}}{\sqrt{13}}$$

$$C. \frac{3\hat{i} - \hat{k}}{\sqrt{10}}$$

$$D. \frac{4\hat{i} + 3\hat{j} - 3\hat{k}}{\sqrt{34}}$$

Answer: c



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312. if  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-zero, non-coplanar vectors and

$$\vec{b}_1 = \vec{b} - \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}, \vec{b}_2 = \vec{b} + \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}, \vec{c}_1 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^2} \vec{a} + \frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^2} \vec{b}_1, \vec{c}_2 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^2} \vec{a} - \frac{\vec{b} \cdot \vec{c}}{|\vec{b}|^2} \vec{b}_1$$

, then the set of orthogonal vectors is

$$A. (\vec{a}, \vec{b}_1, \vec{c}_3)$$

$$B. (\vec{c}, \vec{b}_1, \vec{c}_2)$$

$$C. (\vec{a}, \vec{b}_1, \vec{c}_1)$$

$$D. (\vec{a}, \vec{b}_2, \vec{c}_2)$$

Answer: c



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313. Let  $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} + \hat{j} - \hat{k}$  A vector in the plane of  $\vec{a}$  and  $\vec{b}$  whose projections on  $\vec{c}$  is  $\frac{1}{\sqrt{3}}$  is

A.  $4\hat{i} - \hat{j} + 4\hat{k}$

B.  $3\hat{i} + \hat{j} - 3\hat{k}$

C.  $2\hat{i} + \hat{j} - 2\hat{k}$

D.  $4\hat{i} + \hat{j} - 4\hat{k}$

Answer: a



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314. Let two non collinear unit vectors  $\hat{a}$  and  $\hat{b}$  form an acute angle. A

point P moves so that at any time t the position vector  $\vec{OP}$  (where O is the origin) is given by  $\hat{a}\cos t + \hat{b}\sin t$ . When P is farthest from origin O, let

M be the length of  $\vec{OP}$  and  $\hat{u}$  be the unit vector along  $\vec{OP}$ . Then (A)

$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}} \quad \text{(B) } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}} \quad \text{(C)}$$

$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{\frac{1}{2}} \quad \text{(D) } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{\frac{1}{2}}$$

$$\text{A. } \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{1/2}$$

$$\text{B. } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{1/2}$$

$$\text{C. } \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{1/2}$$

$$\text{D. } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{1/2}$$

Answer: a



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315. If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are unit vectors such that  $(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 1$  and  $\vec{a} \cdot \vec{c} = \frac{1}{2}$  then (A)  $\vec{a}, \vec{b}, \vec{c}$  are non coplanar (B)  $\vec{b}, \vec{c}, \vec{d}$  are non coplanar (C)  $\vec{b}, \vec{d}$  are non paralel (D)  $\vec{a}, \vec{d}$  are paralel and  $\vec{b}, \vec{c}$  are paralel

A.  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non-coplanar

B.  $\vec{b}, \vec{c}$  and  $\vec{d}$  are non-coplanar

C.  $\vec{b}$  and  $\vec{d}$  are non-parallel

D.  $\vec{a}$  and  $\vec{d}$  are parallel and  $\vec{b}$  and  $\vec{c}$  are parallel

Answer: c



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316. Two adjacent sides of a parallelogram  $ABCD$  are given by

$\vec{AB} = 2\hat{i} + 10\hat{j} + 11\hat{k}$  and  $\vec{AD} = -\hat{i} + 2\hat{j} + 2\hat{k}$  The side  $AD$  is rotated by an

acute angle  $\alpha$  in the plane of the parallelogram so that  $AD$  becomes  $AD'$

If  $AD'$  makes a right angle with the side  $AB$ , then the cosine of the angle

$\alpha$  is given by  $\frac{8}{9}$  b.  $\frac{\sqrt{17}}{9}$  c.  $\frac{1}{9}$  d.  $\frac{4\sqrt{5}}{9}$

A.  $\frac{8}{9}$

B.  $\frac{\sqrt{17}}{9}$

C.  $\frac{1}{9}$

D.  $\frac{4\sqrt{5}}{9}$

**Answer: b**



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**317.** Let  $P$ ,  $Q$ ,  $R$  and  $S$  be the points on the plane with position vectors  $-2\hat{i} - \hat{j}$ ,  $4\hat{i}$ ,  $3\hat{i} + 3\hat{j}$  and  $-3\hat{i} + 2\hat{j}$  respectively. The quadrilateral  $PQRS$  must be a

A. Parallelogram, which is neither a rhombus nor a rectangle

B. square

C. rectangle, but not a square

D. rhombus, but not a square.

**Answer: a**



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**318.** Let  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} - \hat{j} - \hat{k}$  be three vectors. A vectors  $\vec{v}$  in the plane of  $\vec{a}$  and  $\vec{b}$ , whose projection on  $\vec{c}$  is  $\frac{1}{\sqrt{3}}$  is given by

A.  $\hat{i} - 3\hat{j} + 3\hat{k}$

B.  $-3\hat{i} - 3\hat{j} + \hat{k}$

C.  $3\hat{i} - \hat{j} + 3\hat{k}$

D.  $\hat{i} + 3\hat{j} - 3\hat{k}$

**Answer: c**



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319. Let  $\vec{PR} = 3\hat{i} + \hat{j} - 2\hat{k}$  and  $\vec{SQ} = \hat{i} - 3\hat{j} - 4\hat{k}$  determine diagonals of a parallelogram PQRS and  $\vec{PT} = \hat{i} + 2\hat{j} + 3\hat{k}$  be another vector. Then the volume of the parallelepiped determined by the vectors  $\vec{PT}$ ,  $\vec{PQ}$  and  $\vec{PS}$  is

- A. 5
- B. 20
- C. 10
- D. 30

**Answer: c**

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320. Let  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  be three non zero vectors such that  $\vec{c}$  is a unit vector perpendicular to both

$\vec{a}$  and  $\vec{b}$ . If the angle between  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{6}$ , then  $\left| \begin{matrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{matrix} \right|^2$  is equal

to

A. 0

B. 1

C.  $\frac{1}{4} (a_1^2 + a_2^2 + a_2^2) (b_1^2 + b_2^2 + b_2^2)$

D.  $\frac{3}{4} (a_1^2 + a_2^2 + a_2^2) (b_1^2 + b_2^2 + b_2^2) (c_1^2 + c_2^2 + c_2^2)$

**Answer: C**



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**321.** The number of vectors of unit length perpendicular to vectors

$\vec{a} = (1, 1, 0)$  and  $\vec{b} = (0, 1, 1)$  is a. one b. two c. three d. infinite

A. one

B. two

C. three

D. infinite

**Answer: b**



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**322.** Let  $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$  and  $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$  be three vectors. A vector in the plane of  $\vec{b}$  and  $\vec{c}$  whose projection on  $\vec{a}$  is of magnitude

$\sqrt{\left(\frac{2}{3}\right)}$  is (A)  $2\hat{i} + 3\hat{j} + 3\hat{k}$  (B)  $2\hat{i} + 3\hat{j} - 3\hat{k}$  (C)  $-2\hat{i} - \hat{j} + 5\hat{k}$  (D)  $2\hat{i} + \hat{j} + 5\hat{k}$

A.  $2\hat{i} + 3\hat{j} - 3\hat{k}$

B.  $2\hat{i} + 3\hat{j} + 3\hat{k}$

C.  $-2\hat{i} - \hat{j} + 5\hat{k}$

D.  $2\hat{i} + \hat{j} + 5\hat{k}$

**Answer: a,c**



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**323.** For three vectors  $\vec{u}$ ,  $\vec{v}$ ,  $\vec{w}$  which of the following expressions is not equal to any of the remaining three?

A.  $\vec{u} \cdot (\vec{v} \times \vec{w})$

B.  $(\vec{v} \times \vec{w}) \cdot \vec{u}$

C.  $\vec{v} \cdot (\vec{u} \times \vec{w})$

D.  $(\vec{u} \times \vec{v}) \cdot \vec{w}$

**Answer: c**



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**324.** Which of the following expressions are meaningful?  $\vec{u} \vec{v} \times \vec{w}$  b.  $\left( \vec{u} \vec{v} \right) \vec{w}$

c.  $\left( \vec{u} \vec{v} \right) \vec{w}$  d.  $\vec{u} \times \left( \vec{v} \vec{w} \right)$

A.  $\vec{u} \cdot (\vec{v} \times \vec{w})$

B.  $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$

C.  $(\vec{u} \cdot \vec{v})\vec{w}$

D.  $\vec{u} \times (\vec{v} \cdot \text{Vecw})$

**Answer: a,c**



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**325.** If  $\vec{a}$  and  $\vec{b}$  are two non collinear vectors and  $\text{vecu} = \text{vecu} \cdot \text{vecu} + \text{vecu} \cdot \text{vecb}$  and  $\text{vecv} = \text{vecu} \times \text{vecb}$  then  $|\text{vecv}|$  is (A)  $|\text{vecu}| \cdot (B) |\text{vecu}| + |\text{vecu} \cdot \text{vecb}|$  (C)  $|\text{vecu}| + |\text{vecu} \cdot \text{vecu}|$  (D) none of these

A.  $|\vec{u}|$

B.  $|\vec{u}| + |\vec{u} \cdot \text{Vecu}|$

C.  $|\vec{u}| + |\vec{u} \cdot \vec{b}|$

D.  $|\vec{u}| + \vec{u} \cdot (\vec{a} + \vec{b})$

**Answer: a,c**



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326. Vector  $\frac{1}{3}(2\hat{i} - 2\hat{j} + \hat{k})$  is

A. a unit vector

B. makes an angle  $\pi/3$  with vector  $(2\hat{i} - 4\hat{j} + 3\hat{k})$

C. parallel to vector  $\left(-\hat{i} + \hat{j} - \frac{1}{2}\hat{k}\right)$

D. perpendicular to vector  $3\hat{i} + 2\hat{j} - 2\hat{k}$

Answer: a,c,d



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327. Let  $\vec{a}$  be vector parallel to line of intersection of planes  $P_1$  and  $P_2$  through origin. If  $P_1$  is parallel to the vectors  $2\vec{j} + 3\vec{k}$  and  $4\vec{j} - 3\vec{k}$  and  $P_2$  is parallel to  $\vec{j} - \vec{k}$  and  $3\vec{i} + 3\vec{j}$ , then the angle between  $\vec{a}$  and  $2\vec{i} + \vec{j} - 2\vec{k}$  is :

A.  $\pi/2$

B.  $\pi/4$

C.  $\pi/6$

D.  $3\pi/4$

**Answer: b,d**



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**328.** The vectors which is/are coplanar with vectors  $\hat{i} + \hat{j} + 2\hat{k}$  and  $\hat{i} + 2\hat{j} + \hat{k}$  and perpendicular to the vector  $\hat{i} + \hat{j} + \hat{k}$  is /are  
(A)  $\hat{j} - \hat{k}$  (B)  $-\hat{i} + \hat{j}$  (C)  $\hat{i} - \hat{j}$  (D)  $-\hat{j} + \hat{k}$

A.  $\hat{j} - \hat{k}$

B.  $-\hat{i} + \hat{j}$

C.  $\hat{i} - \hat{j}$

D.  $-\hat{j} + \hat{k}$

**Answer: a,d**

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**329.** Let  $\vec{x}, \vec{y}$  and  $\vec{z}$  be three vectors each of magnitude  $\sqrt{2}$  and the angle between each pair of them is  $\frac{\pi}{3}$  if  $\vec{a}$  is a non-zero vector perpendicular to  $\vec{x}$  and  $\vec{y} \times \vec{z}$  and  $\vec{b}$  is a non-zero vector perpendicular to  $\vec{y}$  and  $\vec{z} \times \vec{x}$ , then

A.  $\vec{b} = (\vec{b} \cdot \vec{z})(\vec{z} - \vec{x})$

B.  $\vec{a} = (\vec{a} \cdot \vec{y})(\vec{y} - \vec{z})$

C.  $\vec{a} \cdot \vec{b} = -(\vec{a} \cdot \vec{y})(\vec{b} \cdot \vec{z})$

D.  $\vec{a} = (\vec{a} \cdot \vec{y})(\vec{z} - \vec{y})$

**Answer:** a,b,c

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**330.** Let  $\triangle PQR$  be a triangle. Let  $\vec{a} = \overrightarrow{QR}, \vec{b} = \overrightarrow{RP}$  and  $\vec{c} = \overrightarrow{PQ}$ . if  $|\vec{a}| = 12, |\vec{b}| = 4\sqrt{3}$  and  $\vec{b} \cdot \vec{c} = 24$  then



which of the following is (are) true ?

A.  $\frac{|\vec{c}|^2}{2} - |\vec{a}| = 12$

B.  $\frac{|\vec{c}|^2}{2} - |\vec{a}| = 30$

C.  $|\vec{a} \times \vec{b} + \vec{c} \times \vec{a}| = 48\sqrt{3}$

D.  $\vec{a} \cdot \vec{b} = -72$

Answer: a,c,d



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331. 



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332. 



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333. 

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334. If  $\vec{a}$  and  $\vec{b}$  are vectors in space given by  $\vec{a} = \frac{\hat{i} - 23\hat{j}}{\sqrt{5}}$   
 $\vec{b} = \frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}$  then the value of  $(2\vec{a} + \vec{b}) \cdot [(\vec{a} \times \vec{b}) \times (\vec{a} - 2\vec{b})]$ , is

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335. Let  $\vec{a} = -\hat{i} - \hat{k}$ ,  $\vec{b} = -\hat{i} + \hat{j}$  and  $\vec{c} = \hat{i} + 2\hat{j} + 3\hat{k}$  be three given vectors.  
If  $\vec{r}$  is a vector such that  $\vec{r} \times \vec{b} = \vec{c} \times \vec{d}$  and  $\vec{r} \cdot \vec{a} = 0$  then find the value of  
 $\vec{r} \cdot \vec{b}$ .

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336. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors satisfying

$$|\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2 = 9 \text{ then } |2\vec{a} + 5\vec{b} + 5\vec{c}| \text{ is}$$

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337. Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be three non coplanar unit vectors such that the angle between every pair of them is  $\frac{\pi}{3}$ . If  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} = p\vec{a} + q\vec{b} + r\vec{c}$  where p,q,r are scalars then the value of  $\frac{p^2 + 2q^2 + r^2}{q^2}$  is

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