



# MATHS

# **BOOKS - CENGAGE MATHS (HINGLISH)**

# **GRAPHS OF POLYNOMIAL AND RATIONAL FUNCTIONS**



**1.** Draw the rough sketch of the curve  $y = (x-1)^2(x-3)^3$ 

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**2.** Draw the rough sketch of the curve  $y = (x-1)^2(x-2)(x-3)^3$ .





**6.** Draw the graph of  $y = x^3 - x^2 + x - 2$  and find the number of real root(s) of the equation  $x^3 - x^2 + x - 2 = 0$ . Also locate the root.

7. Sketch the graph of the following functions y = f(x) and find the number of real roots of the corresponding equation f(x) = 0.

 $(i)f(x)=2x^3-9x^2+12x-(9/2)$   $(ii)f(x)=2x^3-9x^2+12x-3$ 



**8.** Draw the graph of  $y = x^4 + 2x^2 - 8x + 3$ 

Find the number of real roots of the equation  $x^4 + 2x^2 - 8x + 3 = 0$ .

Also find the sum of the integral parts of all real roots.

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- 9. Let a  $\,\in\,$  R and f :R
  ightarrow R be given by  $f(x)=x^5-5x+a$ , then
- (a) f(x) = 0 has three real roots if a > 4
- (b) f(x) = 0 has only one real root if a > 4
- (c) f(x) = 0 has three real roots if a < -4
- (d) f(x) = 0 has three real roots if -4 < a < 4



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11. Find the area bounded by the curves  $y = \sqrt{1 - x^2}$  and  $y = x^3 - x$  without using integration.

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12. Draw the graph of  $f(x) = 4x^3 - 3x$  and hence draw the graph of

$$g(x) = \cos^{-1}(4x^3 - 3x).$$



13.

$$f(x) = x^3 - 3x^2 + 6 \, orall x \in R \;\; ext{and} \;\; g(x) = \{(\; \max \, . \, f(t), x + 1 \leq t \leq x \;\;$$

Then find  $y=g(x) \;\; ext{for} \;\; x\in [\,-3,1].$ 

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14. Find the value of k if  $x^3 = 3x + a = 0$  has three real distinct roots.

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15. If t is a real number satisfying the equation  $2t^3 - 9t^2 + 30 - a = 0$ , then find the values of the parameter a for which the equation  $x + \frac{1}{x} = t$  gives six real and distinct values of x.

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Let

16. Let  $f(x)=x^3-9x^2+24x+c=0$  have three real and distinct roots lpha,eta and  $\lambda.$ 

(i) Find the possible values of c.

(ii) If  $[\alpha] + [\beta] + [\lambda] = 8$ , then find the values of c, where  $[\cdot]$  represents the greatest integer function.

(ii) If  $[\alpha] + [\beta] + [\lambda] = 7$ , then find the values of c, where  $[\cdot]$  represents the greatest integer function.s

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17. Draw the graph of 
$$f(x)=rac{x^2-x+1}{x^2+x+1}$$
 .

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18. Draw the graph of  $y=rac{x-1}{x^2}$  and hence the graph of  $y=rac{|x-1|}{x^2}.$ 

**19.** Write a possible rational function h with a hole at x = 5, a vertical asymptote at x = -1, a horizontal asymptote at y = 2 and x-intercept at x = 2.

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20. Write a rational function g with vertical asymptotes at x = 3 and x = -3,  
a horizontal asymptote at y = -4 and with no x-intercept.  
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21. Draw the graph of 
$$y = f(x) = \frac{x+1}{x^2+1}$$
  
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22. Draw the graph of the function  
 $f: R - \{-1, 1\} \rightarrow R. f(x) = \frac{x}{1-|x|}.$ 

**23.** Draw the graph of 
$$f(x)=rac{1}{x^2-2x+2}$$

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**24.** From the graph of 
$$y=x^2-4$$
, draw the graph of  $y=rac{1}{x^2-4}.$ 

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**25.** Draw the graph of 
$$y=x^2+rac{1}{x^2}, x
eq 0.$$

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**26.** Draw the graph of 
$$f(x) = \left| rac{x^2-2}{x^2-1} 
ight|$$

27. Draw the graph of  $y = \frac{1 - x^2}{1 + x^2}$  and hence draw the graph of  $y = \cos^{-1} \cdot \frac{1 - x^2}{1 + x^2}$ . View Text Solution

**28.** Write a rational function f with a slant asymptote y = x + 4, a vertical asymptote at x = 5 and one of the zeros at x = 2.



**31.** Draw the graph of y=

$$rac{x^3}{3(x+1)}.$$

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**32.** Draw the graph of 
$$y = rac{1}{x} + rac{1}{x-2}$$
.

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**33.** Find the greatest value of 
$$f(x)rac{1}{2ax-x^2-5a^2}\in [-3,5]$$

depending upon the parameter a.

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Exercise

1. Draw the graph of  $y=(x-1)ig(x^2-x+1ig).$ 





3. Draw the graphs of

(i) 
$$y = x^2(x-1)|x-2|$$

(ii) 
$$y = x^3(x-1)|x-2|$$

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4. Write a possible rational function f that has a vertical asymptote at x =

2, a horizontal asymptote y = 3 and a zero at x = -5. Also draw the graph of

the function.

5. Draw the graph of  $y=f(x)=rac{x^2}{x^2+1}.$ 

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**6.** Draw graph of 
$$y=rac{x^2-6x+4}{x^2+2x+4}$$

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7. Draw the graph of 
$$f(x)=rac{x^2-8x+15}{x^2-2x}$$

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**8.** Draw the graph of 
$$f(x) = rac{5x^2}{\left(x-1
ight)^3}$$

**9.** Draw the graph of  $y=x+rac{1}{x}$ 

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**10.** Draw graph of 
$$y = rac{1}{x^2} - x.$$

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11. Draw graph of 
$$y=rac{x^3-2x^2}{3{(x+1)}^2}.$$

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12. Draw graph of 
$$y=rac{x^3-5x}{x^2+1}.$$

13. Given  $C_1 < C_2 < C_3 < C_4 < C_5$  and the function y = f(x) is twice differentiable .

f'(x) > 0 for  $x \in (C_2, C_4)$ ,  $f'(C_2) = f'(C_4) = 0$  and f'(x) < 0 for all the remaining values. Also  $f''(C_1) = f''(C_3) = f''(C_5) = 0$  and f''(x) > 0 for  $x \in (C_1, C_3) \cup (C_5, \infty)$  and f''(x) < 0 for remaining values. Answer the following:

(i) What is the minimum number of asymptotes parallel to the x-axis for y=f(x)?

(ii) What is the maximum number of asymptotes parallel to the x-axis of y = f(x) ?

(iii) If the range of y = f(x) is  $[a, b], a, b \in R$ , then what is the minimum number of asymptotes parallel to the x-axis of y = f(x)? (iv) If the range of y = f(x) is non-finite interval, then what is the

maximum number of asymptotes parallel to the x-axis ?

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