



## MATHS

### BOOKS - CENGAGE MATHS (HINGLISH)

#### THREE DIMENSIONAL GEOMETRY

##### Solved Examples And Exercises

1. Find the angle between the line whose direction cosines are given by

$$l + m + n = 0 \text{ and } 2l^2 + 2m^2 - n^2 = 0.$$

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2. A line makes angles  $\alpha, \beta, \gamma$  and  $\delta$  with the diagonals of a cube. Show

$$\text{that } \cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma + \cos^2 \delta = 4/3.$$

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3.  $ABC$  is a triangle and  $A=(2,3,5), B=(-1,3,2)$  and  $C=(\lambda, 5, \mu)$ . If the median through  $A$  is equally inclined to the axes, then find the value of  $(\lambda, \mu)$

A.  $(10, 7)$

B.  $(7, 5)$

C.  $(7, 10)$

D.  $(5, 7)$

**Answer: C**



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4. A line  $OP$  through origin  $O$  is inclined at  $30^\circ$  and  $45^\circ \rightarrow OX$  and  $OY$ , respectively. Then find the angle at which it is inclined to  $OZ$ .



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5. If  $\alpha$ ,  $\beta$ , and  $\gamma$  are the angles which a directed line makes with the positive directions of the co-ordinates axes, then find the value of  $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma$ .

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6. If the sum of the squares of the distance of a point from the three coordinate axes is 36, then find its distance from the origin.

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7. If  $A(3, 2, -4)$ ,  $B(5, 4, -6)$  and  $C(9, 8, -10)$  are three collinear points, then find the ratio in which point  $C$  divides  $AB$ .

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8. Find the ratio in which the  $y - z$  plane divides the join of the points  $(-2, 4, 7)$  and  $(3, -5, 8)$ .

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9. A line passes through the points  $(6, -7, -1)$  and  $(2, -3, 1)$ . Find the direction cosines of the line if the line makes an acute angle with the positive direction of the  $x$ -axis.

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10. Find the angle between the lines whose direction cosines are connected by the relations  $l + m + n = 0$  and  $2lm + 2nl - mn = 0$ .

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11. Find the point where line which passes through point  $(1, 2, 3)$  and is parallel to line  $\vec{r} = \hat{i} + \hat{j} + 2\hat{k} + \lambda(\hat{i} - 2\hat{j} + 3\hat{k})$  meets the  $xy$ -plane.

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12. Find the equation of the line passing through the points  $(1, 2, 3)$  and  $(-1, 0, 4)$ .

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13. Find the equation of the line passing through the point  $(-1, 2, 3)$

and perpendicular to the lines

$$\frac{x}{2} = \frac{y-1}{-3} = \frac{z+2}{-2} \text{ and } \frac{x+3}{-1} = \frac{y+3}{2} = \frac{z-1}{3}.$$

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14. The line joining the points  $(-2, 1, -8)$  and  $(a, b, c)$  is parallel to the line whose direction ratios are  $6, 2,$  and  $3$ . Find the values of  $a, b$  and  $c$



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15. A parallelepiped is formed by planes drawn through the points  $P(6, 8, 10)$  and  $(3, 4, 8)$  parallel to the coordinate planes. Find the length of edges and diagonal of the parallelepiped.



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16. Find the angle between any two diagonals of a cube.



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17. Direction ratios of two lines are  $a, b, c$  and  $1/bc, 1/ca, 1/ab$ . Then the lines are \_\_\_\_\_.



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18. Find the equation of the line passing through the intersection of

$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} \text{ and } \frac{x-4}{5} = \frac{y-1}{2} = z$$

and also through the point  $(2, 1, -2)$ .

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19. The straight line  $\frac{x-3}{3} = \frac{y-2}{1} = \frac{z-1}{0}$  is (a) Parallel to x-axis

(b) Parallel to the y-axis (c) Parallel to the z-axis (d) Perpendicular to the z-axis

axis

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20. Find the equation of the plane containing the lines

$$\frac{x-5}{4} = \frac{y-7}{4} = \frac{z+3}{-5} \text{ and } \frac{x-8}{7} = \frac{y-4}{1} = \frac{z-5}{3}$$

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21. Find the equation of the plane passing through the points  $(1, 0, -1)$  and  $(3, 2, 2)$  and parallel to the line  $x - 1 = \frac{1 - y}{2} = \frac{z - 2}{3}$ .



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22. Find the equation of the sphere described on the joint of points  $A$  and  $B$  having position vectors  $2\hat{i} + 6\hat{j} - 7\hat{k}$  and  $-2\hat{i} + 4\hat{j} - 3\hat{k}$ , respectively, as the diameter. Find the center and the radius of the sphere.



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23. Find the radius of the circular section in which the sphere  $|\vec{r}| = 5$  is cut by the plane  $\vec{r} \cdot \hat{i} + \hat{j} + \hat{k} = 3\sqrt{3}$ .



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24. Find the equation of a sphere which passes through  $(1, 0, 0)$ ,  $(0, 1, 0)$  and  $(0, 0, 1)$ , and has radius as small as possible.

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25. Find the locus of a point which moves such that the sum of the squares of its distance from the points  $A(1, 2, 3)$ ,  $B(2, -3, 5)$  and  $C(0, 7, 4)$  is 120.

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26. Find the equation of the sphere which has centre at the origin and touches the line  $2(x + 1) = 2 - y = z + 3$ .

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27. Find the equation of the sphere which passes through  $(10, 0)$ ,  $(0, 1, 0)$  and  $(0, 0, 1)$  and whose centre lies on the plane

$$3x - y + z = 2.$$

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28. Find the equation of a sphere whose centre is  $(3, 1, 2)$  radius is 5.

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29. Find the equation of the sphere passing through  $(0, 0, 0)$ ,  $(1, 0, 0)$ ,  $(-1, 1, 0)$  and  $(0, 0, 1)$ .

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30. Find the image of the line  $\frac{x-1}{9} = \frac{y-2}{-1} = \frac{z+3}{-3}$  in the plane  $3x - 3y + 10z - 26 = 0$ .

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**31.** Find the equations of the bisectors of the angles between the planes  $2x - y + 2z + 3 = 0$  and  $3x - 2y + 6z + 8 = 0$  and specify the plane which bisects the acute angle and the plane which bisects the obtuse angle.

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**32.** If the  $x$ -coordinate of a point  $P$  on the join of  $Q(22, 1)$  and  $R(5, 1, -2)$  is  $4$ , then find its  $z$ -coordinate.

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**33.** A sphere of constant radius  $k$ , passes through the origin and meets the axes at  $A$ ,  $B$  and  $C$ . Prove that the centroid of triangle  $ABC$  lies on the sphere  $9(x^2 + y^2 + z^2) = 4k^2$ .

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**34.** A variable plane passes through a fixed point  $(a, b, c)$  and cuts the coordinate axes at points  $A, B,$  and  $C$ . Show that the locus of the centre of the sphere  $OABC$  is  $\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = 2$ .

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**35.** Show that the plane  $2x - 2y + z + 12 = 0$  touches the sphere  $x^2 + y^2 + z^2 - 2x - 4y + 2z - 3 = 0$ .

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**36.** If  $O$  is the origin,  $OP = 3$  with direction ratios  $-1, 2,$  and  $-2$ , then find the coordinates of  $P$ .

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**37.** If  $P(x, y, z)$  is a point on the line segment joining  $Q(2, 2, 4)$  and  $R(3, 5, 6)$  such that the projections of  $\vec{OP}$  on the axes are

$13/5$ ,  $19/5$  and  $26/5$ , respectively, then find the ratio in which  $P$  divides  $QR$ .

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38. If  $\vec{r}$  is a vector of magnitude 21 and has direction ratios 2,  $-3$  and 6, then find  $\vec{r}$ .

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39. Find the distance of the point  $P(a, b, c)$  from the x-axis.

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40. A line makes angles  $\alpha$ ,  $\beta$  and  $\gamma$  with the coordinate axes. If  $\alpha + \beta = 90^\circ$ , then find  $\gamma$ .

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41. If a line makes angles  $\alpha$ ,  $\beta$  and  $\gamma$  with three-dimensional coordinate axes, respectively, then find the value of  $\cos 2\alpha + \cos 2\beta + \cos 2\gamma$ .

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42. Find the distance between the parallel planes  $x + 2y - 2z + 1 = 0$  and  $2x + 4y - 4z + 5 = 0$ .

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43. A ray of light passing through the point  $A(1, 2, 3)$ , strikes the plane  $xy + z = 12$  at  $B$  and on reflection passes through point  $C(3, 5, 9)$ . Find the coordinate of point  $B$ .

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**44.** The plane  $ax + by = 0$  is rotated through an angle  $\alpha$  about its line of intersection with the plane  $z = 0$ . Show that the equation to the plane in the new position is  $aby \pm z\sqrt{a^2 + b^2} \text{ and } \alpha = 0$ .

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**45.** Find the equation of a plane containing the line of intersection of the planes  $x + y + z - 6 = 0$  and  $2x + 3y + 4z + 5 = 0$  passing through  $(1, 1, 1)$ .

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**46.** Find the locus of a point, the sum of squares of whose distance from the planes  $x - z = 0$ ,  $x - 2y + z = 0$  and  $x + y + z = 0$  is 36

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47. Find the length and the foot of the perpendicular from the point  $(7, 14, 5)$  to the plane  $2x + 4y - z = 2$ . Also, find the image of the point  $P$  in the plane.



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48. Find the angle between the line  $\vec{r} = \hat{i} + 2\hat{j} - \hat{k} + \lambda(\hat{i} - \hat{j} + \hat{k})$  and the plane  $\vec{r} \cdot 2\hat{i} - \hat{j} + \hat{k} = 4$ .



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49. Find the equation of the projection of the line  $\frac{x-1}{2} = \frac{y+1}{-1} = \frac{z-3}{4}$  on the plane  $x + 2y + z = 9$ .



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50. Find the equation the plane which contain the line of intersection of the planes  $\vec{r} \hat{i} + 2\hat{j} + 3\hat{k} - 4 = 0$  and  $\vec{r} 2\hat{i} + \hat{j} - \hat{k} + 5 = 0$  and which is perpendicular to the plane  $\vec{r} (5\hat{i} + 3\hat{j} - 6\hat{k}) + 8 = 0$ .

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51. Find the vector equation of the line passing through  $(1, 2, 3)$  and parallel to the planes  $\vec{r} \hat{i} - \hat{j} + 2\hat{k} = 5$  and  $\vec{r} 3\hat{i} + \hat{j} + \hat{k} = 6$ .

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52. Find the distance of the point  $P(3, 8, 2)$  from the line  $\frac{1}{2}(x - 1) = \frac{1}{4}(y - 3) = \frac{1}{3}(z - 2)$  measured parallel to the plane  $3x + 2y - 2z + 15 = 0$ .

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53. Find the distance of the point  $(1, 0, -3)$  from the plane  $x - y - z = 9$  measured parallel to the line  $\frac{x - 2}{2} = \frac{y + 2}{2} = \frac{z - 6}{-6}$ .

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54. Show that  $ax + by + r = 0$ ,  $by + cz + p = 0$  and  $cz + ax + q = 0$  are perpendicular to  $x - y$ ,  $y - z$  and  $z - x$  planes, respectively.

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55. Reduce the equation of line  $x - y + 2z = 5$  and  $3x + y + z = 6$  in symmetrical form. Or Find the line of intersection of planes  $x - y + 2z = 5$  and  $3x + y + z = 6$ .

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56. Find the angle between the lines  $x - 3y - 4 = 0$ ,  $4y - z + 5 = 0$  and  $x + 3y - 11 = 0$ ,  $2y = z + 6 = 0$ .

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57. If the line  $x = y = z$  intersect the line  $s \in Ax + s \in By + s \in Cz = 2d^2$ ,  $s \in 2Ax + s \in 2By + s \in 2Cz = d^2$ , then find the value of  $\frac{\sin A}{2} \frac{\sin B}{2} \frac{\sin C}{2}$  where  $A, B, C$  are the angles of a triangle.

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58. The point of intersecting of the line passing through  $(0, 0, 1)$  and intersecting the lines  $x + 2y + z = 1$ ,  $-x + y - 2z = 2$  and  $x + y = 2$ ,  $x + z = 2$  with  $xy$ -plane is

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59. A horizontal plane  $4x - 3y + 7z = 0$  is given. Find a line of greatest slope passes through the point  $(2, 1, 1)$  in the plane  $2x + y - 5z = 0$ .



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60. Find the equation of the plane passing through the points  $(-1, 1, 1)$  and  $(1, -1, 1)$  and perpendicular to the plane  $x + 2y + 2z = 5$ .



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61. Find ten equation of the plane passing through the point  $(0, 7, -7)$  and containing the line  $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$ .



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62. If a plane meets the equations axes at  $A, B$  and  $C$  such that the centroid of the triangle is  $(1, 2, 4)$ , then find the equation of the plane.

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63. Find the equation of the plane which is parallel to the lines  $\vec{r} = \hat{i} + \hat{j} + \lambda(2\hat{i} + \hat{j} + 4\hat{k})$  and  $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$  and is passing through the point  $(0, 1, -1)$ .

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64. Prove that the plane  $\vec{r} \cdot (\hat{i} + 2\hat{j} - \hat{k}) = 3$  contains the line  $\vec{r} = \hat{i} + \hat{j} + \lambda(2\hat{i} + \hat{j} + 4\hat{k})$ .

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65. Find the vector equation of the following planes in Cartesian form:

$$\vec{r} = \hat{i} - \hat{j} + \lambda(\hat{i} + \hat{j} + \hat{k}) + \mu(\hat{i} - 2\hat{j} + 3\hat{k}).$$

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66. Show that the line of intersection of the planes

$\vec{r} \cdot \hat{i} + 2\hat{j} + 3\hat{k} = 0$  and  $\vec{r} \cdot (3\hat{i} + 2\hat{j} + \hat{k}) = 0$  is equally inclined to  $i$  and  $k$ . Also find the angle it makes with  $j$ .

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67. Find the equation of the plane passing through  $A(2, 2, -1)$ ,  $B(3, 4, 2)$  and  $C(7, 0, 6)$ . Also find a unit vector perpendicular to this plane.

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68. Find the equation of the plane such that image of point  $(1, 2, 3)$  in it is  $(-1, 0, 1)$ .

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69. The foot of the perpendicular drawn from the origin to a plane is  $(1, 2, -3)$ . Find the equation of the plane. or If  $O$  is the origin and the coordinates of  $P$  is  $(1, 2, -3)$ , then find the equation of the plane passing through  $P$  and perpendicular to  $OP$ .

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70. Find the angle between the planes  $2x + y - 2z + 3 = 0$  and  $\vec{r} \cdot 6\hat{i} + 3\hat{j} + 2\hat{k} = 5$ .

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71. Find the equation of the plane passing through  $(3, 4, -1)$ , which is parallel to the plane  $\vec{r} \cdot 2\hat{i} - 3\hat{j} + 5\hat{k} + 7 = 0$ .

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72. Find the distance of the point  $(-1, -5, -10)$  from the point of intersection of the line  $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{12}$  and plane  $x - y + z = 5$ .

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73. Find the equation of the plane passing through the point  $(-1, 3, 2)$  and perpendicular to each of the planes  $x + 2y + 3z = 5$  and  $3x + 3y + z = 0$ .

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74. Find the angle between the line  $\frac{x-1}{3} = \frac{y-1}{2} = \frac{z-1}{4}$  and the plane  $2x + y - 3z + 4 = 0$ .

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75. Find the distance between the line  $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z-2}{1}$  and the plane  $x + y + z + 3 = 0$ .

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76. The extremities of a diameter of a sphere lie on the positive y- and positive z-axes at distance 2 and 4, respectively. Show that the sphere passes through the origin and find the radius of the sphere.

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77. A plane passes through a fixed point  $(a, b, c)$ . Show that the locus of the foot of the perpendicular to it from the origin is the sphere  $x^2 + y^2 + z^2 - ax - by - cz = 0$ .

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78. Find the radius of the circular section of the sphere  $|\vec{r}| = 5$  by the plane  $\vec{r} \cdot \hat{i} + 2\hat{j} - \hat{k} = 4\sqrt{3}$ .

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79. A point  $P(x, y, z)$  is such that  $3PA = 2PB$ , where  $A$  and  $B$  are the point  $(1, 3, 4)$  and  $(1, -2, -1)$ , irrespectively. Find the equation to the locus of the point  $P$  and verify that the locus is a sphere.

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80. Find the shortest distance between lines

$$\vec{r} = (\hat{i} + 2\hat{j} + \hat{k}) + \lambda(2\hat{i} + \hat{j} + 2\hat{k}) \text{ and } \vec{r} = 2\hat{i} - \hat{j} - \hat{k} + \mu(2\hat{i} + \hat{j} + \hat{k})$$

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81. Find the shortest distance between the lines

$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} \text{ and } \frac{x-2}{3} = \frac{y-4}{4} = \frac{z-5}{5}.$$

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82. Determine whether the following pair of lines intersect or not. (1)

$$\vec{r} = \hat{i} - 5\hat{j} + \lambda(2\hat{i} + \hat{k}); \vec{r} = 2\hat{i} - \hat{j} + \mu(\hat{i} + \hat{j} - \hat{k}) \quad (2)$$

$$\vec{r} = \hat{i} + \hat{j} - \hat{k} + \lambda(3\hat{i} - \hat{j}); \vec{r} = 4\hat{i} - \hat{k} + \mu(2\hat{i} + 3\hat{k})$$

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83. Find the equation of plane which is at a distance  $\frac{4}{\sqrt{14}}$  from the origin and is normal to vector  $2\hat{i} + \hat{j} - 3\hat{k}$ .

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84. Find the unit vector perpendicular to the plane  $\vec{r} \cdot 2\hat{i} + \hat{j} + 2\hat{k} = 5$ .

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85. If the straight lines  $x = -1 + s, y = 3 - \lambda s, z = 1 + \lambda s$  and  $x = \frac{t}{2}, y = 1 + t, z = 2 - t$ , with parameters  $s$  and  $t$ , respectively, are coplanar, then find  $\lambda$ .

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86. Find the equation of a line which passes through the point  $(1, 1, 1)$  and intersects the lines

$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} \text{ and } \frac{x+2}{1} = \frac{y-3}{2} = \frac{z+1}{4}.$$



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87. Find the vector equation of a line passing through  $3\hat{i} - 5\hat{j} + 7\hat{k}$  and perpendicular to the plane  $3x - 4y + 5z = 8$ .



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88. Find the equation of the plane passing through the point  $(2, 3, 1)$  having  $(5, 3, 2)$  as the direction ratio of the normal to the plane.



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89. Find the equation of the plane through the points  $(23, 1)$  and  $(4, -5, 3)$  and parallel to the x-axis.



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90. Find the equation of the image of the plane  $x - 2y + 2z - 3 = 0$  in plane  $x + y + z - 1 = 0$ .

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91. Find the equation of a plane which passes through the point  $(1, 2, 3)$  and which is equally inclined to the planes  $x - 2y + 2z - 3 = 0$  and  $8x - 4y + z - 7 = 0$ .

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92. Find the equation of a plane which is parallel to the plane  $x - 2y + 2z = 5$  and whose distance from the point  $(1, 2, 3)$  is 1.

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93. Find the direction ratios of orthogonal projection of line  $\frac{x-1}{1} = \frac{y+1}{-2} = \frac{z-2}{3}$  in the plane  $x - y + 2z - 3 = 0$ . also find the direction ratios of the image of the line in the plane.



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94. Find the equation of the plane which passes through the point  $(1, 2, 3)$  and which is at the minimum distance from the point  $(-1, 0, 2)$ .



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95. Find the angle between the line  $\vec{r} = \left( \vec{i} + 2\vec{j} - \vec{k} \right) + \lambda \left( \vec{i} - \vec{j} + \vec{k} \right)$  and the normal to the plane  $\vec{r} \cdot \left( 2\vec{i} - \vec{j} + \vec{k} \right) = 4$ .



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96. Find the equation of the plane passing through the line

$$\frac{x-1}{5} = \frac{y+2}{6} = \frac{z-3}{4} \text{ and point } (4, 3, 7).$$



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97. Find the equation of the plane perpendicular to the line

$$\frac{x-1}{2} = \frac{y-3}{-1} = \frac{z-4}{2} \text{ and passing through the origin.}$$



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98. Find the equation of the plane passing through the straight line

$$\frac{x-1}{2} = \frac{y+2}{-3} = \frac{z}{5} \text{ and perpendicular to the plane}$$

$$x - y + z + 2 = 0.$$



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99. Find the equation of the line drawn through point  $(1, 0, 2)$  to meet the line  $\frac{x+1}{3} = \frac{y-2}{-2} = \frac{z-1}{-1}$  at right angles.

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100. If  $\vec{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \lambda(\hat{i} - \hat{j} + \hat{k})$  and  $\vec{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \mu(\hat{i} + \hat{j} - \hat{k})$  are two lines, then the equation of acute angle bisector of two lines is

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101. Find the coordinates of a point on the line  $\frac{x-1}{2} = \frac{y+1}{-3} = z$  at a distance  $4\sqrt{14}$  from the point  $(1, -1, 0)$ .

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**102.** Line  $L_1$  is parallel to vector  $\vec{\alpha} = -3\hat{i} + 2\hat{j} + 4\hat{k}$  and passes through a point  $A(7, 6, 2)$  and line  $L_2$  is parallel vector  $\vec{\beta} = 2\hat{i} + \hat{j} + 3\hat{k}$  and point  $B(5, 3, 4)$ . Now a line  $L_3$  parallel to a vector  $\vec{r} = 2\hat{i} - 2\hat{j} - \hat{k}$  intersects the lines  $L_1$  and  $L_2$  at points  $C$  and  $D$ , respectively, then find  $|\vec{CD}|$ .



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**103.** Find the values  $p$  so that line  $\frac{1-x}{3} = \frac{7y-14}{2p} = \frac{z-3}{2}$  and  $\frac{7-7x}{3p} = \frac{y-5}{1} = \frac{6-z}{5}$  are at right angles.



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**104.** Find the angle between the following pair of lines:

$$\vec{r} = 2\hat{i} - 5\hat{j} + \hat{k} + \lambda(3\hat{i} + 2\hat{j} + 6\hat{k}) \text{ and } \vec{r} = 7\hat{i} - 6\hat{k} + \mu(\hat{i} + 2\hat{j} + 2\hat{k})$$

$$\frac{x}{2} = \frac{y}{2} = \frac{z}{1} \text{ and } \frac{x-5}{4} = \frac{y-2}{1} = \frac{z-3}{8}$$



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105. Find the condition if lines  $x = ay + b, z = cy + d$  and  $x = a'y + b', z = c'y + d'$  are perpendicular.

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106. Find the acute angle between the lines  $\frac{x-1}{l} = \frac{y+1}{m} = \frac{z-1}{n}$  and  $\frac{x+1}{m} = \frac{y-3}{n} = \frac{z-1}{l}$  where  $l > m > n$ , are the roots of the cubic equation  $x^3 + x^2 - 4x = 4$ .

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107. Find the length of the perpendicular drawn from point  $(2, 3, 4)$  to line  $\frac{4-x}{2} = \frac{y}{6} = \frac{1-z}{3}$ .

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**108.** Find the coordinates of the foot of the perpendicular drawn from point  $A(1, 0, 3)$  to the join of points  $B(4, 7, 1)$  and  $C(3, 5, 3)$ .



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**109.** Find the vector equation of the line passing through  $(1, 2, 3)$  and parallel to the planes  $\vec{r} \cdot \hat{i} - \hat{j} + 2\hat{k}$  and  $\vec{r} \cdot 3\hat{i} + \hat{j} + \hat{k} = 6$ .



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**110.** Find the value of  $m$  for which the straight line  $3x - 2y + z + 3 = 0 = 4x + 3y + 4z + 1$  is parallel to the plane  $2x - y + mz - 2 = 0$ .



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111. Show that the lines  $\frac{x - a + d}{\alpha - \delta} = \frac{y - a}{\alpha} = \frac{z - a - d}{\alpha + \delta}$  and  $\frac{x - b + c}{\beta - \gamma} = \frac{y - b}{\beta} = \frac{z - b - c}{\beta + \gamma}$  are coplanar.

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112. Find the equation of line  $x + y - z - 3 = 0 = 2x + 3y + z + 4$  in symmetric form. Find the direction of the line.

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113. Find the vector equation of line passing through the point  $(1, 2, -4)$  and perpendicular to the two lines:

$$\frac{x - 8}{3} = \frac{y + 19}{-16} = \frac{z - 10}{7} \text{ and } \frac{x - 15}{3} = \frac{y - 29}{8} = \frac{z - 5}{-5}$$

A.  $\vec{r} = (\hat{i} + 2\hat{j} - 4\hat{k}) + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$

B.  $\vec{r} = (\hat{i} + 2\hat{j} + 4\hat{k}) + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$

C.  $\vec{r} = (\hat{i} - 2\hat{j} + 4\hat{k}) + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$

$$D. \vec{r} = (\hat{i} + 2\hat{j} + 4\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - 6\hat{k})$$

**Answer: A**



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**114.** Find the vector equation of line passing through  $A(3, 4 - 7)$  and  $B(1, -1, 6)$ . Also find its Cartesian equations.



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**115.** Find Cartesian and vector equation of the line which passes through the point  $(-2, 4, -5)$  and parallel to the line given by

$$\frac{x + 3}{3} = \frac{y - 4}{5} = \frac{z + 8}{6}.$$



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**116.** Find the equation of a line which passes through the point  $(2, 3, 4)$  and which has equal intercepts on the axes.

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**117.** Find the points where line  $\frac{x - 1}{2} = \frac{y + 2}{-1} = \frac{z}{1}$  intersects  $xy, yz$  and  $zx$  planes.

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**118.** A mirror and source of light are situated at the origin  $O$  and a point on  $OX$  respectively. A ray of light from the source strikes the mirror and is reflected. If the DRs of the normal to the plane of mirror are  $1, -1, 1$ , then DCs for the reflected ray are :

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**119.** The Cartesian equation of a line is  $\frac{x-3}{2} = \frac{y+1}{-2} = \frac{z-3}{5}$ . Find the vector equation of the line.

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**120.** The Cartesian equations of a line are  $6x - 2 = 3y + 1 = 2z - 2$ . Find its direction ratios and also find a vector equation of the line.

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**121.** A line passes through the point with position vector  $2\hat{i} - 3\hat{j} + 4\hat{k}$  and is in the direction of  $3\hat{i} + 4\hat{j} - 5\hat{k}$ . Find the equations of the line in vector and Cartesian forms.

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122. Find the plane of the intersection of

$$x^2 + y^2 + z^2 + 2x + 2y + 2 = 0 \text{ and } 4x^2 + 4y^2 + 4z^2 + 4x + 4y + 4z - 1 = 0$$

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123. If the lines

$$\frac{x-1}{-3} = \frac{y-2}{2k} = \frac{z-3}{-2} \text{ and } \frac{x-1}{3k} = \frac{y-5}{1} = \frac{z-6}{-5} \text{ are at right}$$

angle, then find the value of  $k$ .

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124. Find the angle between the lines

$$2x = 3y = -z \text{ and } 6x = -y = -4z$$

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**125.** Find the length of the perpendicular drawn from the point  $(5, 4, -1)$  to the line  $\vec{r} = \hat{i} + \lambda(2\hat{i} + 9\hat{j} + 5\hat{k})$ , where  $\lambda$  is a parameter.



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**126.** The equations of motion of a rocket are  $x = 2t, y = -4t$  and  $z = 4t$ , where time  $t$  is given in seconds, and the coordinates of a moving points in kilometers. What is the path of the rocket? At what distance will be the rocket from the starting point  $O(0, 0, 0)$  in  $10s$ ?



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**127.** Find the shortest distance between the lines  $\vec{r} = (1 - \lambda)\hat{i} + (\lambda - 2)\hat{j} + (3 - 2\lambda)\hat{k}$  and  $\vec{r} = (\mu + 1)\hat{i} + (2\mu + 1)\hat{k}$ .



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128. Find the image of the point  $(1, 2, 3)$  in the line

$$\frac{x - 6}{3} = \frac{y - 7}{2} = \frac{z - 7}{-2}.$$

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129. If the lines  $\frac{x - 1}{2} = \frac{y + 1}{3} = \frac{z - 1}{4}$  and  $\frac{x - 3}{1} = \frac{y - k}{2} = \frac{z}{1}$  intersect, then find the value of  $k$ .

A.  $\frac{3}{2}$

B.  $\frac{9}{2}$

C.  $-\frac{2}{9}$

D.  $-\frac{3}{2}$

**Answer: b**

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**130.** Find the shortest distance between the z-axis and the line,  
 $x + y + 2z - 3 = 0, 2x + 3y + 4z - 4 = 0.$

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**131.** The lines which intersect the skew lines  
 $y = mx, z = c; y = -mx, z = -c$  and the x-axis lie on the surface:  
 (a.)  $cz = mxy$  (b.)  $xy = cmz$  (c.)  $cy = mxz$  (d.) none of these

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**132.** Distance of the point  $P(\vec{p})$  from the line  $\vec{r} = \vec{a} + \lambda \vec{b}$  is a.

$$\left| \left( \vec{a} - \vec{p} \right) + \frac{\left( \left( \vec{p} - \vec{a} \right) \vec{b} \right) \vec{b}}{\left| \vec{b} \right|^2} \right| \quad \text{b.}$$

$$\left( \vec{b} - \vec{p} \right) + \frac{\left( \left( \vec{p} - \vec{a} \right) \cdot \vec{b} \right) \vec{b}}{\left| \vec{b} \right|^2} \quad \text{c.}$$

$$\left( \vec{a} - \vec{p} \right) + \frac{\left( \left( \vec{p} - \vec{b} \right) \cdot \vec{b} \right) \vec{b}}{\left| \vec{b} \right|^2} \quad \text{d. none of these}$$

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**133.** The direction ratios of a normal to the plane through  $(1, 0, 0)$  and  $(0, 1, 0)$ , which makes an angle of  $\frac{\pi}{4}$  with the plane  $x + y = 3$ , are a.  $\langle 1, \sqrt{2}, 1 \rangle$  b.  $\langle 1, 1, \sqrt{2} \rangle$  c.  $\langle 1, 1, 2 \rangle$  d.  $\langle \sqrt{2}, 1, 1 \rangle$

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**134.** The centre of the circle given by  $\vec{r} \cdot \hat{i} + 2\hat{j} + 2\hat{k} = 15$  and  $\left| \vec{r} - (\hat{j} + 2\hat{k}) \right| = 4$  is a.  $(0, 1, 2)$  b.  $(1, 3, 5)$  c.  $(-1, 3, 4)$  d. none of these

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**135.** Two systems of rectangular axes have the same origin. If a plane cuts them at distance  $a, b, c$  and  $a', b', c'$  from the origin, then a.

$$\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} + \frac{1}{a'^2} + \frac{1}{b'^2} + \frac{1}{c'^2} = 0 \quad \text{b.}$$

$$\frac{1}{a^2} - \frac{1}{b^2} - \frac{1}{c^2} + \frac{1}{a'^2} - \frac{1}{b'^2} - \frac{1}{c'^2} = 0 \quad \text{c.}$$

$$\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} - \frac{1}{a'^2} - \frac{1}{b'^2} - \frac{1}{c'^2} = 0 \quad \text{d.}$$

$$\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} + \frac{1}{a'^2} + \frac{1}{b'^2} + \frac{1}{c'^2} = 0$$



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**136.** The plane which passes through the point  $(3, 2, 0)$  and the line

$$\frac{x-3}{1} = \frac{y-6}{5} = \frac{z-4}{4} \quad \text{is a. } x-y+z=1 \quad \text{b. } x+y+z=5 \quad \text{c.}$$

$$x+2y-z=1 \quad \text{d. } 2x-y+z=5$$



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137. The lines  $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$  and  $\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$  are coplanar if a.  $k = 1$  or  $-1$  b.  $k = 0$  or  $-3$  c.  $k = 3$  or  $-3$  d.  $k = 0$  or  $-1$



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138. The point of intersection of the lines  $\frac{x-5}{3} = \frac{y-7}{-1} = \frac{z+2}{1}$  and  $\frac{x+3}{-36} = \frac{y-3}{2} = \frac{z-6}{4}$  is (A)  $\left(21, \frac{5}{3}, \frac{10}{3}\right)$  (B)  $(2, 10, 4)$  (C)  $(-3, 3, 6)$  (D)  $(5, 7, -2)$



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139. A tetrahedron has vertices  $P(1, 2, 1)$ ,  $Q(2, 1, 3)$ ,  $R(-1, 1, 2)$  and  $O(0, 0, 0)$ . The angle between the faces OPQ and PQR is :



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140. The radius of the circle in which the sphere  $x^2 + y^2 + z^2 + 2z - 2y - 4z - 19 = 0$  is cut by the plane  $x + 2y + 2z + 7 = 0$  is a. 2 b. 3 c. 4 d. 1

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141. A sphere of constant radius  $2k$  passes through the origin and meets the axes in  $A, B,$  and  $C$ . The locus of a centroid of the tetrahedron  $OABC$  is a.  $x^2 + y^2 + z^2 = 4k^2$  b.  $x^2 + y^2 + z^2 = k^2$  c.  $2(k^2 + y^2 + z^2) = k^2$  d. none of these

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142. A plane passes through a fixed point  $(a, b, c)$ . The locus of the foot of the perpendicular to it from the origin is a sphere of radius a.  $\frac{1}{2}\sqrt{a^2 + b^2 + c^2}$  b.  $\sqrt{a^2 + b^2 + c^2}$  c.  $a^2 + b^2 + c^2$  d.  $\frac{1}{2}(a^2 + b^2 + c^2)$

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**143.** Equation of the plane containing the straight line  $\frac{x}{2} = \frac{y}{3} = \frac{z}{4}$  and perpendicular to the plane containing the straight lines  $\frac{x}{2} = \frac{y}{4} = \frac{z}{2}$  and  $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$  is

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**144.** The equation of the plane through the intersection of the planes  $x + 2y + 3z - 4 = 0$  and  $4x + 3y + 2z + 1 = 0$  and passing through the origin is (a)  $17x + 14y + 11z = 0$  (b)  $7x + 4y + z = 0$  (c)  $x + 14 + 11z = 0$  (d)  $17x + y + z = 0$

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**145.** The plane  $4x + 7y + 4z + 81 = 0$  is rotated through a right angle about its line of intersection with the plane  $5x + 3y + 10z = 25$ . The equation of the plane in its new position is a.  $x - 4y + 6z = 106$  b.  $x - 8y + 13z = 103$  c.  $x - 4y + 6z = 110$  d.  $x - 8y + 13z = 105$

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146. The vector equation of the plane passing through the origin and the

line of intersection of the planes  $\vec{r} \cdot \vec{a} = \lambda$  and  $\vec{r} \cdot \vec{b} = \mu$  is a.

$\vec{r} \cdot \lambda \vec{a} - \mu \vec{b} = 0$    b.  $\vec{r} \cdot \lambda \vec{b} - \mu \vec{a} = 0$    c.  $\vec{r} \cdot \lambda \vec{a} + \mu \vec{b} = 0$    d.

$\vec{r} \cdot \lambda \vec{b} + \mu \vec{a} = 0$



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147. The lines  $\vec{r} = \vec{a} + \lambda(\vec{b} \times \vec{c})$  and  $\vec{r} = \vec{b} + \mu(\vec{c} \times \vec{a})$  will

intersect if a.  $\vec{a} \times \vec{c} = \vec{b} \times \vec{c}$    b.  $\vec{a} \cdot \vec{c} = \vec{b} \cdot \vec{c}$    c.  $\vec{b} \times \vec{a} = \vec{c} \times \vec{a}$    d.

none of these



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148. The projection of the line  $\frac{x+1}{-1} = \frac{y}{2} = \frac{z-1}{3}$  on the plane

$x - 2y + z = 6$  is the line of intersection of this plane with the plane a.

$2x + y + 2 = 0$    b.  $3x + y - z = 2$    c.  $2x - 3y + 8z = 3$    d. none of these



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149. The direction cosines of a line satisfy the relations  $\lambda(l + m) = n$  and  $mn + nl + lm = 0$ . The value of  $\lambda$ , for which the two lines are perpendicular to each other, is a. 1 b. 2 c.  $1/2$  d. none of these



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150. The intercepts made on the axes by the plane the which bisects the line joining the points  $(1, 2, 3)$  and  $(-3, 4, 5)$  at right angles are a.  $\left(-\frac{9}{2}, 9, 9\right)$  b.  $\left(\frac{9}{2}, 9, 9\right)$  c.  $\left(9, -\frac{9}{2}, 9\right)$  d.  $\left(9, \frac{9}{2}, 9\right)$



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151. The pair of lines whose direction cosines are given by the equations  $3l + m + 5n = 0$  and  $6mn - 2nl + 5lm = 0$  are a. parallel b. perpendicular c. inclined at  $\cos^{-1}\left(\frac{1}{6}\right)$  d. none of these

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152. If the distance of the point  $P(1, -2, 1)$  from the plane  $x + 2y - 2z = \alpha$ , where  $\alpha > 0$ , is 5, then the foot of the perpendicular from  $P$  to the plane is
- a.  $\left(\frac{8}{3}, \frac{4}{3}, -\frac{7}{3}\right)$    b.  $\left(\frac{4}{3}, -\frac{4}{3}, \frac{1}{3}\right)$    c.  $\left(\frac{1}{3}, \frac{2}{3}, \frac{10}{3}\right)$    d.  $\left(\frac{2}{3}, -\frac{1}{3}, -\frac{5}{3}\right)$

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153. A line with positive direction cosines passes through the point  $P(2, -1, 2)$  and makes equal angles with the coordinate axes. The line meets the plane  $2x + y + z = 9$  at point  $Q$ . The length of the line segment  $PQ$  equals

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154. The value of  $k$  such that  $\frac{x-4}{1} = \frac{y-2}{1} = \frac{z-k}{2}$  lies in the plane  $2x - 4y + z = 7$  is (A) 7 (B) -7 (C) no real value (D) 4



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155. The equation of the plane passing through lines

$\frac{x-4}{1} = \frac{y-3}{1} = \frac{z-2}{2}$  and  $\frac{x-3}{2} = \frac{y-2}{-4} = \frac{z}{5}$  is a.

11x - y - 3z = 35 b. 11x + y - 3z = 35 c. 11x - y + 3z = 35 d. none

of these



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156. The line through  $\hat{i} + 3\hat{j} + 2\hat{k}$  and  $\perp$  to the line

$\vec{r} = (\hat{i} + 2\hat{j} - \hat{k}) + \lambda(2\hat{i} + \hat{j} + \hat{k})$  and  $\vec{r} = (2\hat{i} + 6\hat{j} + \hat{k}) + \mu(\hat{i} + 2\hat{j} - \hat{k})$

is a.  $\vec{r} = (\hat{i} + 2\hat{j} - \hat{k}) + \lambda(-\hat{i} + 5\hat{j} - 3\hat{k})$  b.

$\vec{r} = \hat{i} + 3\hat{j} + 2\hat{k} + \lambda(\hat{i} - 5\hat{j} + 3\hat{k})$  c.

$\vec{r} = \hat{i} + 3\hat{j} + 2\hat{k} + \lambda(\hat{i} + 5\hat{j} + 3\hat{k})$  d.

$\vec{r} = \hat{i} + 3\hat{j} + 2\hat{k} + \lambda(-\hat{i} - 5\hat{j} - 3\hat{k})$



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157. The equation of the plane through the line of intersection of the planes  $ax + by + cz + d = 0$  and  $a'x + b'y + c'z + d' = 0$  parallel to the line  $y = 0$  and  $z = 0$  is

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158. The three planes  $4y + 6z = 5$ ,  $2x + 3y + 5z = 5$  and  $6x + 5y + 9z = 10$  (a) meet in a point (b) have a line in common (c) form a triangular prism (d) none of these

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159. Given  $\vec{\alpha} = 3\hat{i} + \hat{j} + 2\hat{k}$  and  $\vec{\beta} = \hat{i} - 2\hat{j} - 4\hat{k}$  are the position vectors of the points  $A$  and  $B$  Then the distance of the point  $\hat{i} + \hat{j} + \hat{k}$  from the plane passing through  $B$  and perpendicular to  $AB$  is (a) 5 (b) 10 (c) 15 (d) 20

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160. The shortest distance between the lines

$$\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{1} \text{ and } \frac{x+3}{-3} = \frac{y+7}{2} = \frac{z-6}{4}$$

is a.  $\sqrt{30}$  b.  $2\sqrt{30}$  c.  $5\sqrt{30}$  d.  $3\sqrt{30}$

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161.  $L_1$  and  $L_2$  are two lines whose vector equations are

$$L_1: \vec{r} = \lambda \left( (\cos \theta + \sqrt{3}) \hat{i} + (\sqrt{2} \sin \theta) \hat{j} + (\cos \theta - \sqrt{3}) \hat{k} \right)$$

$$L_2: \vec{r} = \mu \left( a \hat{i} + b \hat{j} + c \hat{k} \right), \text{ where } \lambda \text{ and } \mu \text{ are scalars and } \alpha \text{ is the acute angle between } L_1 \text{ and } L_2.$$

If the angle  $\alpha$  is independent of  $\theta$ , then the value of  $\alpha$  is

a.  $\frac{\pi}{6}$  b.  $\frac{\pi}{4}$  c.  $\frac{\pi}{3}$  d.  $\frac{\pi}{2}$

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162. Value of  $\lambda$  such that the line  $\frac{x-1}{2} = \frac{y-1}{3} = \frac{z-1}{\lambda}$  is  $\perp$  to

normal to the plane  $2\vec{i} + 3\vec{j} + 4\vec{k} = 0$  is a.  $-\frac{13}{4}$  b.  $-\frac{17}{4}$  c. 4 d. none of these



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163. Equation of the plane passing through the points  $(2, 2, 1)$  and  $(9, 3, 6)$ , and  $\perp$  to the plane  $2x + 6y + 6z - 1 = 0$  is a.  $3x + 4y + 5z = 9$  b.  $3x + 4y - 5z = 9$  c.  $3x + 4y - 5z = 9$  d. none of these



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164. The equation of the plane which passes through the point of intersection of lines  $\frac{x-1}{3} = \frac{y-2}{1} = \frac{z-3}{2}$ , and  $\frac{x-3}{1} = \frac{y-1}{2} = \frac{z-2}{3}$  at greatest distance from point  $(0, 0, 0)$  is a.  $4x + 3y + 5z = 25$  b.  $4x + 3y = 5z = 50$  c.  $3x + 4y + 5z = 49$  d.  $x + 7y - 5z = 2$



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165. If the foot of the perpendicular from the origin to plane is  $P(a, b, c)$ , the equation of the plane is a.  $\frac{x}{a} = \frac{y}{b} = \frac{z}{c} = 3$  b.  $ax + by + cz = 3$  c.  $ax + by + cz = a^2 + b^2 + c^2$  d.  $ax + by + cz = a + b + c$



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166. Equation of a line in the plane  $\pi = 2x - y + z - 4 = 0$  which is perpendicular to the line  $l$  whose equation is  $\frac{x-2}{1} = \frac{y-2}{-1} = \frac{z-3}{-2}$  and which passes through the point of intersection of  $l$  and  $\pi$  is (A)

$$\frac{x-2}{1} = \frac{y-1}{5} = \frac{z-1}{-1} \quad \text{(B)} \quad \frac{x-1}{3} = \frac{y-3}{5} = \frac{z-5}{-1} \quad \text{(C)}$$

$$\frac{x+2}{2} = \frac{y+1}{-1} = \frac{z+1}{1} \quad \text{(D)} \quad \frac{x-2}{2} = \frac{y-1}{-1} = \frac{z-1}{1}$$



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167. The intercept made by the plane  $\vec{r} \cdot \hat{n} = q$  on the x-axis is a.  $\frac{q}{\hat{i} \cdot \hat{n}}$  b.

$$\frac{\hat{i} \cdot \vec{n}}{q} \quad \text{c.} \quad \frac{\hat{i} \cdot \vec{n}}{q} \quad \text{d.} \quad \frac{q}{|\vec{n}|}$$



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**168.** The coordinates of the foot of the perpendicular drawn from the origin to the line joining the point  $(-9, 4, 5)$  and  $(10, 0, -1)$  will be a.  $(-3, 2, 1)$  b.  $(1, 2, 2)$  c.  $4, 5, 3$  d. none of these

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**169.** The point on the line  $\frac{x-2}{1} = \frac{y+3}{-2} = \frac{z+5}{-2}$  at a distance of 6 from the point  $(2, -3, -5)$  is a.  $(3, -5, -3)$  b.  $(4, -7, -9)$  c.  $0, 2, -1$  d. none of these

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**170.** Let  $A(1, 1, 1)$ ,  $B(2, 3, 5)$  and  $C(-1, 0, 2)$  be three points, then equation of a plane parallel to the plane  $ABC$  which is at distance 2 is a.  $2x - 3y + z + 2\sqrt{14} = 0$  b.  $2x - 3y + z - \sqrt{14} = 0$  c.  $2x - 3y + z + 2 = 0$  d.  $2x - 3y + z - 2 = 0$

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171. Let  $A(\vec{a})$  and  $B(\vec{b})$  be points on two skew lines  $\vec{r} = \vec{a} + \lambda\vec{p}$  and  $\vec{r} = \vec{b} + u\vec{q}$  and the shortest distance between the skew lines is 1, where  $\vec{p}$  and  $\vec{q}$  are unit vectors forming adjacent sides of a parallelogram enclosing an area of  $1/2$  units. If angle between  $AB$  and the line of shortest distance is  $60^\circ$ , then  $AB =$  a.  $\frac{1}{2}$  b. 2 c. 1 d.

$$\lambda R = \{10\}$$

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172. Consider three planes  $P_1: x - y + z = 1$ ,  $P_2: x + y - z = -1$  and  $P_3: x - 3y + 3z = 2$  Let  $L_1, L_2$  and  $L_3$  be the lines of intersection of the planes  $P_2$  and  $P_3, P_3$  and  $P_1$  and  $P_1$  and  $P_2$  respectively. Statement 1: At least two of the lines  $L_1, L_2$  and  $L_3$  are non-parallel The three planes do not have a common point

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**173.** Consider the planes  $3x - 6y - 2z - 15 = 0$  and  $2x + y - 2z - 5 = 0$

Statement 1: The parametric equations of the line intersection of the given planes are  $x = 3 + 14t, y = 2t, z = 15t$ .

Statement 2: The vector  $14\hat{i} + 2\hat{j} + 15\hat{k}$  is parallel to the line of intersection of the given planes.

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**174.** The length of projection of the line segment joining the points  $(1, 0, -1)$  and  $(-1, 2, 2)$  on the plane  $x + 3y - 5z = 6$  is equal to

a. 2  
 b.  $\sqrt{\frac{271}{53}}$  c.  $\sqrt{\frac{472}{31}}$  d.  $\sqrt{\frac{474}{35}}$

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**175.** If  $P_1: \vec{r} \cdot \vec{n}_1 - d_1 = 0$   $P_2: \vec{r} \cdot \vec{n}_2 - d_2 = 0$  and  $P_3: \vec{r} \cdot \vec{n}_3 - d_3 = 0$  are three non-coplanar vectors, then three lines  $P_1 = 0, P_2 = 0; P_2 = 0, P_3 = 0; P_3 = 0, P_1 = 0$  are

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176. Perpendiculars are drawn from points on the line  $\frac{x+2}{2} = \frac{y+1}{-1} = \frac{z}{3}$  to the plane  $x+y+z=3$ . The feet of

perpendiculars lie on the line (a)  $\frac{x}{5} = \frac{y-1}{8} = \frac{z-2}{-13}$  (b)

$\frac{x}{2} = \frac{y-1}{3} = \frac{z-2}{-5}$  (c)  $\frac{x}{4} = \frac{y-1}{3} = \frac{z-2}{-7}$  (d)

$\frac{x}{2} = \frac{y-1}{-7} = \frac{z-2}{5}$



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177. The point P is the intersection of the straight line joining the points  $Q(2, 3, 5)$  and  $R(1, -1, 4)$  with the plane  $5x - 4y - z = 1$ . If S is the foot of the perpendicular drawn from the point  $T(2, 1, 4)$  to QR, then the length of the line segment PS is (A)  $\frac{1}{\sqrt{2}}$  (B)  $\sqrt{2}$  (C) 2 (D)  $2\sqrt{2}$



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**178.** A line  $l$  passing through the origin is perpendicular to the lines  $l_1: (3+t)\hat{i} + (-1+2t)\hat{j} + (4+2t)\hat{k}$ ,  $\infty < t < \infty$ ,  $l_2: (3+s)\hat{i} + (3+2s)\hat{j} + (4+s)\hat{k}$ ,  $\infty < s < \infty$ , then the coordinates of the point on  $l_2$  at a distance of  $\sqrt{17}$  from the point of intersection of  $l$  &  $l_1$  is/are:

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**179.** Two lines  $L_1: x = 5, \frac{y}{3-\alpha} = \frac{z}{-2}$  and  $L_2: x = \alpha, \frac{y}{-1} = \frac{z}{2-\alpha}$  are coplanar. Then  $\alpha$  can take value (s) a. 1 b. 2 c. 3 d. 4

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**180.** The projection of point  $P(\vec{p})$  on the plane  $\vec{r} \cdot \vec{n} = q$  is  $(\vec{s})$ , then

- a.  $\vec{s} = \frac{\left(q - \vec{p} \cdot \vec{n}\right) \vec{n}}{|\vec{n}|^2}$       b.  $\vec{s} = \vec{p} + \frac{\left(q - \vec{p} \cdot \vec{n}\right) \vec{n}}{|\vec{n}|^2}$       c.
- $\vec{s} = \vec{p} - \frac{\left(\vec{p} \cdot \vec{n}\right) \vec{n}}{|\vec{n}|^2}$       d.  $\vec{s} = \vec{p} - \frac{\left(q - \vec{p} \cdot \vec{n}\right) \vec{n}}{|\vec{n}|^2}$

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181. The angle between  $i$  line of the intersection of the plane  $\vec{r} \cdot \hat{i} + 2\hat{j} + 3\hat{k} = 0$  and  $\vec{r} \cdot 3\hat{i} + 3\hat{j} + \hat{k} = 0$  is a.  $\cos^{-1}\left(\frac{1}{3}\right)$  b.  $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$  c.  $\cos^{-1}\left(\frac{2}{\sqrt{3}}\right)$  d. none of these

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182. From the point  $P(a, b, c)$ , let perpendiculars  $PL$  and  $PM$  be drawn to  $YOZ$  and  $ZOX$  planes, respectively. Then the equation of the plane  $OLM$  is a.  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 0$  b.  $\frac{x}{a} + \frac{y}{b} - \frac{z}{c} = 0$  c.  $\frac{x}{a} - \frac{y}{b} - \frac{z}{c} = 0$  d.  $\frac{x}{a} - \frac{y}{b} + \frac{z}{c} = 0$

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183. The plane  $\vec{r} \cdot \vec{n} = q$  will contain the line  $\vec{r} = \vec{a} + \lambda \vec{b}$ , if a.  $b \cdot n \neq 0, a \cdot n \neq q$  b.  $b \cdot n = 0, a \cdot n \neq q$  c.  $b \cdot n = 0, a \cdot n = q$  d.  $b \cdot n \neq 0, a \cdot n = q$

b.  $n \neq 0$ , a.  $n = q$



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**184.** Consider triangle  $AOB$  in the  $x - y$  plane, where  $A \equiv (1, 0, 0)$ ,  $B \equiv (0, 2, 0)$  and  $O \equiv (0, 0, 0)$ . The new position of  $O$ ,

when triangle is rotated about side  $AB$  by  $90^\circ$  can be a.  $\left(\frac{4}{5}, \frac{3}{5}, \frac{2}{\sqrt{5}}\right)$

b.  $\left(\frac{-3}{5}, \frac{\sqrt{2}}{5}, \frac{2}{\sqrt{5}}\right)$  c.  $\left(\frac{4}{5}, \frac{2}{5}, \frac{2}{\sqrt{5}}\right)$  d.  $\left(\frac{4}{5}, \frac{2}{5}, \frac{1}{\sqrt{5}}\right)$



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**185.** Let  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = 2\hat{i} - \hat{k}$ , then the point of intersection of the lines  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$  and  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  is a.  $(3, -1, 1)$  b.

$(3, 1, -1)$  c.  $(-3, 1, 1)$  d.  $(-3, -1, -1)$



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**186.** The line  $\frac{x+6}{5} = \frac{y+10}{3} = \frac{z+14}{8}$  is the hypotenuse of an isosceles right-angled triangle whose opposite vertex is  $(7, 2, 4)$ . Then

which of the following is not the side of the triangle? a.

$\frac{x-7}{2} = \frac{y-2}{-3} = \frac{z-4}{6}$       b.  $\frac{x-7}{3} = \frac{y-2}{6} = \frac{z-4}{2}$       c.

$\frac{x-7}{3} = \frac{y-2}{5} = \frac{z-4}{-1}$       d. none of these



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**187.** The equation of the plane which passes through the line of intersection of planes  $\vec{r} \cdot \vec{n}_1 = q_1$ ,  $\vec{r} \cdot \vec{n}_2 = q_2$  and the is parallel to the

line of intersection of planers  $\vec{r} \cdot \vec{n}_3 = q_3$  and  $\vec{r} \cdot \vec{n}_4 = q_4$  is



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**188.** The coordinates of the point  $P$  on the line

$\vec{r} = (\hat{i} + \hat{j} + \hat{k}) + \lambda(-\hat{i} + \hat{j} - \hat{k})$  which is nearest to the origin is

a.  $\left(\frac{2}{4}, \frac{4}{3}, \frac{2}{3}\right)$       b.  $\left(-\frac{2}{3}, -\frac{4}{3}, \frac{2}{3}\right)$       c.  $\left(\frac{2}{3}, -\frac{4}{3}, \frac{2}{3}\right)$       d. none of these

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**189.** The ratio in which the line segment joining the points whose position vectors are  $2\hat{i} - 4\hat{j} - 7\hat{k}$  and  $-3\hat{i} + 5\hat{j} - 8\hat{k}$  is divided by the plane whose equation is  $\hat{r}\hat{i} - 2\hat{j} + 3\hat{k} = 13$  is a. 13:12 internally b. 12:25 externally c. 13:25 internally d. 37:25 internally

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**190.** The number of planes that are equidistant from four non-coplanar points is a. 3 b. 4 c. 7 d. 9

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**191.** In a three-dimensional coordinate system,  $P$ ,  $Q$ , and  $R$  are images of a point  $A(a, b, c)$  in the  $x - y$ ,  $y - z$  and  $z - x$  planes, respectively. If  $G$  is the centroid of triangle  $PQR$ , then area of triangle  $AOG$  is ( $O$  is the origin) (A) 0 (B)  $a^2 + b^2 + c^2$  (C)  $\frac{2}{3}(a^2 + b^2 + c^2)$  (D) none of these



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**192.** A plane passing through  $(1, 1, 1)$  cuts positive direction of coordinates axes at  $A, B$  and  $C$ , then the volume of tetrahedron  $OABC$  satisfies a.  $V \leq \frac{9}{2}$  b.  $V \geq \frac{9}{2}$  c.  $V = \frac{9}{2}$  d. none of these



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**193.** If lines  $x = y = z$  and  $x = \frac{y}{2} = \frac{z}{3}$  and third line passing through  $(1, 1, 1)$  form a triangle of area  $\sqrt{6}$  units, then the point of intersection of third line with the second line will be a.  $(1, 2, 3)$  b.  $2, 4, 6$  c.  $\frac{4}{3}, \frac{6}{3}, \frac{12}{3}$  d. none of these



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**194.** The point of intersection of the line passing through  $(0, 0, 1)$  and intersecting the lines  $x + 2y + z = 1$ ,  $-x + y - 2z = 2$  and

$x + y = 2, x + z = 2$  with  $xy$  plane is a.  $\left(\frac{5}{3}, -\frac{1}{3}, 0\right)$  b.  $(1, 1, 0)$  c.  $\left(\frac{2}{3}, \frac{1}{3}, 0\right)$  d.  $\left(-\frac{5}{3}, \frac{1}{3}, 0\right)$

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195. Shortest distance between the lines  $\frac{x-1}{1} = \frac{y-1}{1} = \frac{z-1}{1}$  and  $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{1}$  is equal to a.  $\sqrt{14}$  b.  $\sqrt{7}$  c.  $\sqrt{2}$  d. none of these

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196. Distance of point  $P(\vec{p})$  from the plane  $\vec{r} \cdot \vec{n} = 0$  is a.  $\left| \frac{\vec{p} \cdot \vec{n}}{|\vec{n}|} \right|$  b.  $\frac{|\vec{p} \times \vec{n}|}{|\vec{n}|}$  c.  $\frac{|\vec{p} \cdot \vec{n}|}{|\vec{n}|}$  d. none of these

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197. The reflection of the point  $\vec{a}$  in the plane  $\vec{r} \cdot \vec{n} = q$  is a.

$$\vec{a} + \frac{\left(\vec{q} - \vec{a} \cdot \vec{n}\right)}{|\vec{n}|}$$

b.

$$\vec{a} + 2 \left( \frac{\left(\vec{q} - \vec{a} \cdot \vec{n}\right)}{|\vec{n}|} \right) \vec{n}$$

c.

$$\vec{a} + \frac{2\left(\vec{q} + \vec{a} \cdot \vec{n}\right)}{|\vec{n}|^2} \vec{n}$$

d. none of these



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198. Line  $\vec{r} = \vec{a} + \lambda \vec{b}$  will not meet the plane  $\vec{r} \cdot \vec{n} = q$ , if a.

$$\vec{b} \cdot \vec{n} = 0, \vec{a} \cdot \vec{n} = q \quad \text{b.} \quad \vec{b} \cdot \vec{n} \neq 0, \vec{a} \cdot \vec{n} \neq q \quad \text{c.} \quad \vec{b} \cdot \vec{n} = 0, \vec{a} \cdot \vec{n} \neq q \quad \text{d.}$$

$$\vec{b} \cdot \vec{n} \neq 0, \vec{a} \cdot \vec{n} = q$$



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199. If a line makes an angle of  $\frac{\pi}{4}$  with the positive direction of each of x-axis and y-axis, then the angle that the line makes with the positive

direction of the z-axis is a.  $\frac{\pi}{3}$  b.  $\frac{\pi}{4}$  c.  $\frac{\pi}{2}$  d.  $\frac{\pi}{6}$



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**200.** A parallelepiped  $S$  has base points  $A, B, C$  and  $D$  and upper face points  $A', B', C',$  and  $D'$ . The parallelepiped is compressed by upper face  $A'B'C'D'$  to form a new parallelepiped  $T$  having upper face points  $A, B, C$  and  $D$ . The volume of parallelepiped  $T$  is 90 percent of the volume of parallelepiped  $S$ . Prove that the locus of  $A$  is a plane.



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**201.** Find the equation of the plane containing the lines  $2x-y+z-3=0, 3x+y+z=5$  and at a distance of  $\frac{1}{\sqrt{6}}$  from the point  $(2,1,-1)$ .



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**202.** A plane which perpendicular to two planes  $2x - 2y + z = 0$  and  $x - y + 2z = 4$  passes through the point  $(1, -2, 1)$  is:



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203. Let  $P(3, 2, 6)$  be a point in space and  $Q$  be a point on line  $\vec{r} = (\hat{i} - \hat{j} + 2\hat{k}) + \mu(-3\hat{i} + \hat{j} + 5\hat{k})$ . Then the value of  $\mu$  for which the vector  $\vec{PQ}$  is parallel to the plane  $x - 4y + 3z = 1$  is a.  $1/4$  b.  $-1/4$  c.  $1/8$  d.  $-1/8$

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204. If the lines  $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$  and  $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1}$  intersect, then  $k$  is equal to (1)  $-1$  (2)  $\frac{2}{9}$  (3)  $\frac{9}{2}$  (4)  $0$

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205. Statement 1: A plane passes through the point  $A(2, 1, -3)$ . If distance of this plane from origin is maximum, then its equation is  $2x + y - 3z = 14$ . Statement 2: If the plane passing through the point

$A(\vec{a})$  is at maximum distance from origin, then normal to the plane is vector  $\vec{a}$ .

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**206.** If the distance between the plane  $Ax - 2y + z = d$ . and the plane containing the \_\_\_\_\_ lies

$$\frac{x+1}{2} = \frac{y-2}{3} = \frac{z-3}{4} \text{ and } \frac{x-2}{3} = \frac{4-3}{4} = \frac{z-4}{5} \text{ is } \sqrt{6}, \text{ then}$$

$|d|$  is

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**207.** Prove that the volume of tetrahedron bounded by the planes

$$\vec{r} \cdot m\hat{j} + n\hat{k} = 0, \vec{r} \cdot n\hat{k} + l\hat{i} = 0, \vec{r} \cdot l\hat{i} + m\hat{j} = 0, \vec{r} \cdot l\hat{i} + m\hat{j} + n\hat{k} = \pi s \frac{2l}{3ln}$$

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**208.** If a variable plane forms a tetrahedron of constant volume  $64k^3$  with the co-ordinate planes, then the locus of the centroid of the tetrahedron is:

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**209.** Prove that for all values of  $\lambda$  and  $\mu$ , the planes  $\frac{2x}{a} + \frac{y}{b} + \frac{2z}{c} - 1 + \lambda \left( \frac{x}{a} - \frac{2y}{b} - \frac{z}{c} - 2 \right) = 0$  and  $\frac{4x}{a} + \frac{3y}{b} - 5 + \mu \left( \frac{5y}{b} - \frac{4z}{c} + 3 \right) = 0$  intersect on the same line.

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**210.** If  $P$  is any point on the plane  $lx + my + nz = p$  and  $Q$  is a point on the line  $OP$  such that  $OP \cdot OQ = p^2$ , then find the locus of the point  $Q$ .

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**211.** A variable plane  $lx + my + nz = p$  (where  $l, m, n$  are direction cosines of normal) intersects the coordinate axes at points  $A, B$  and  $C$ , respectively. Show that the foot of the normal on the plane from the origin is the orthocenter of triangle  $ABC$  and hence find the coordinate of the circumcentre of triangle  $ABC$ .



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**212.**  $P$  is a point and  $PM$  and  $PN$  are the perpendicular from  $P$  to  $z - x$  and  $x - y$  planes. If  $OP$  makes angles  $\theta, \alpha, \beta$  and  $\gamma$  with the plane  $OMN$  and the  $x - y, y - z$  and  $z - x$  planes, respectively, then prove that  $\cos^2 \theta = \cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma$ .



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**213.** Let a plane  $ax + by + cz + 1 = 0$ , where  $a, b, c$  are parameters, make an angle  $60^\circ$  with the line  $x = y = z$ ,  $45^\circ$  with the line  $x = y - z = 0$  and  $\theta$  with the plane  $x = 0$ . The distance of the plane

from point  $(2, 1, 1)$  is 3 units. Find the value of  $\theta$  and the equation of the plane.

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214. Let

$x - y \sin \alpha - z \sin \beta = 0, x \sin \alpha + y \sin \beta - z \sin \gamma = 0$  and  $x \sin \beta + y \sin \gamma - z \sin \alpha = 0$

be the equations of the planes such that

$\alpha + \beta + \gamma = \pi/2$  (where  $\alpha, \beta$  and  $\gamma \neq 0$ ). Then show that there is a

common line of intersection of the three given planes.

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215. The position vectors of the four angular points of a tetrahedron

OABC are  $(0, 0, 0); (0, 0, 2), (0, 4, 0)$  and  $(6, 0, 0)$  respectively. A point P

inside the tetrahedron is at the same distance  $r$  from the four plane faces

of the tetrahedron. Find the value of  $r$

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216. Find the distance of the point  $(-2, 3, -4)$  from the line

$$\frac{x+2}{3} = \frac{2y+3}{4} = \frac{3z+4}{5} \quad \text{measured parallel to the plane}$$

$$4x + 12y - 3z + 1 = 0.$$



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217. The plane  $4x + 7y + 4z + 81 = 0$  is rotated through a right angle

about its line of intersection with the plane  $5x + 3y + 10z = 25$ . The

equation of the plane in its new position is a.  $x - 4y + 6z = 106$  b.

$x - 8y + 13z = 103$  c.  $x - 4y + 6z = 110$  d.  $x - 8y + 13z = 105$



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218. If  $(a, b, c)$  is a point on the plane  $3x + 2y + z = 7$ , then find the

least value of vector method.  $a^2 + b^2 + c^2$ , using vector method.



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**219.** Let the equation of the plane containing the line  $x - y - z - 4 = 0 = x + y + 2z - 4$  and is parallel to the line of intersection of the planes  $2x + 3y + z = 1$  and  $x + 3y + 2z = 2$  be  $x + Ay + Bz + C = 0$  Compute the value of  $|A + B + C|$ .

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**220.** Let  $a_1, a_2, a_3, \dots$  be in *A. P.* and  $h_1, h_2, h_3, \dots$  in *H. P.* If  $a_1 = 2 = h_1$ , and  $a_{30} = 25 = h_{30}$  then  $a_7 h_{24} + a_{14} + a_{17} =$

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**221.** If the angle between the plane  $x - 3y + 2z = 1$  and the line  $\frac{x - 1}{2} = \frac{y - 1}{1} = \frac{z - 1}{-3}$  is  $\theta$ , then find the value of  $\cos \theta$ .

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**222.** The length of projection of the line segment joining the points  $(1, 0, -1)$  and  $(-1, 2, 2)$  on the plane  $x + 3y - 5z = 6$  is equal to a. 2

b.  $\sqrt{\frac{271}{53}}$  c.  $\sqrt{\frac{472}{31}}$  d.  $\sqrt{\frac{474}{35}}$



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**223.** Find the equation of a plane passing through  $(1, 1, 1)$  and parallel to the lines  $L_1$  and  $L_2$  direction ratios  $(1, 0, -1)$  and  $(1, -1, 0)$  respectively. Find the volume of the tetrahedron formed by origin and the points where this plane intersects the coordinate axes.



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**224.** Find the equation of the plane passing through the points  $(2, 1, 0)$ ,  $(5, 0, 1)$  and  $(4, 1, 1)$  If P is the point  $(2, 1, 6)$  then find point Q such that PQ is perpendicular to the above plane and the mid point of PQ lies on it.



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225. For the line  $\frac{x-1}{1} = \frac{y-2}{2} = \frac{z-3}{3}$ , which one of the following is incorrect? a. it lies in the plane  $x - 2y + z = 0$  b. it is same as line  $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$  c. it passes through  $(2, 3, 5)$  d. it is parallel to the plane  $x - 2y + z - 6 = 0$

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226. The value of  $m$  for which straight line  $3x - 2y + z + 3 = 0 = 4x - 3y + 4z + 1$  is parallel to the plane  $2x - y + mz - 2 = 0$  is a.  $-2$  b.  $8$  c.  $-18$  d.  $11$

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227. Let the equations of a line and plane be  $\frac{x+3}{2} = \frac{y-4}{3} = \frac{z+5}{2}$  and  $4x - 2y - z = 1$ , respectively, then a. the

line is parallel to the plane b. the line is perpendicular to the plane c. the line lies in the plane d. none of these

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228. The length of the perpendicular from the origin to the plane passing through the point  $a$  and containing the line  $\vec{r} = \vec{b} + \lambda \vec{c}$  is a.

$$\frac{\left[ \vec{a} \vec{b} \vec{c} \right]}{\left| \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} \right|}$$

b.

$$\frac{\left[ \vec{a} \vec{b} \vec{c} \right]}{\left| \vec{a} \times \vec{b} + \vec{b} \times \vec{c} \right|}$$

c.

$$\frac{\left[ \vec{a} \vec{b} \vec{c} \right]}{\left| \vec{b} \times \vec{c} + \vec{c} \times \vec{a} \right|}$$

d.

$$\frac{\left[ \vec{a} \vec{b} \vec{c} \right]}{\left| \vec{c} \times \vec{a} + \vec{a} \times \vec{b} \right|}$$

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229. In a three-dimensional  $xyz$  space, the equation  $x^2 - 5x + 6 = 0$  represents a. Points b. planes c. curves d. pair of straight lines

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230. The line  $\frac{x-2}{3} = \frac{y+1}{2} = \frac{z-1}{-1}$  intersects the curve  $xy = c^2, z = 0$  if  $c$  is equal to a.  $\pm 1$  b.  $\pm 1/3$  c.  $\pm \sqrt{5}$  d. none of these

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231. A unit vector parallel to the intersection of the planes

$$\vec{r} \cdot \hat{i} - \hat{j} + \hat{k} = 5 \text{ and } \vec{r} \cdot 2\hat{i} + \hat{j} - 3\hat{k} = 4$$

a.  $\frac{2\hat{i} + 5\hat{j} - 3\hat{k}}{\sqrt{38}}$  b.  $\frac{-2\hat{i} + 5\hat{j} - 3\hat{k}}{\sqrt{38}}$  c.  $\frac{2\hat{i} + 5\hat{j} - 3\hat{k}}{\sqrt{38}}$  d.  $\frac{-2\hat{i} - 5\hat{j} - 3\hat{k}}{\sqrt{38}}$

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232. Let  $L_1$  be the line  $\vec{r}_1 = 2\hat{i} + \hat{j} - \hat{k} + \lambda(i + 2\hat{k})$  and let  $L_2$  be the line  $\vec{r}_2 = 3\hat{i} + \hat{j} + \mu(i + \hat{j} - \hat{k})$ . Let  $\pi$  be the plane which contains the line  $L_1$  and is parallel to  $L_2$ . The distance of the plane  $\pi$  from the origin is a.  $\sqrt{6}$  b.  $1/7$  c.  $\sqrt{2/7}$  d. none of these

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**233.** The distance of point  $A(-2, 3, 1)$  from the line  $PQ$  through  $P(-3, 5, 2)$ , which makes equal angles with the axes is a.  $2/\sqrt{3}$  b.  $14/\sqrt{3}$  c.  $16/\sqrt{3}$  d.  $5/\sqrt{3}$

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**234.** The Cartesian equation of the plane  $\vec{r} = (1 + \lambda - \mu)\hat{i} + (2 - \lambda)\hat{j} + (3 - 2\lambda + 2\mu)\hat{k}$  is a.  $2x + y = 5$  b.  $2x - y = 5$  c.  $2x + z = 5$  d.  $2x - z = 5$

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**235.** Statement 1: there exists a unique sphere which passes through the three non-collinear points and which has the least radius. Statement 2: The centre of such a sphere lies on the plane determined by the given three points.

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**236.** Statement 1: There exist two points on the  $\frac{x-1}{1} = \frac{y}{-1} = \frac{z+2}{2}$  which are at a distance of 2 units from point  $(1, 2, -4)$ . Statement 2: Perpendicular distance of point  $(1, 2, -4)$  from the line  $\frac{x-1}{1} = \frac{y}{-1} = \frac{z+2}{2}$  is 1 unit.

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**237.** Statement 1: The shortest distance between the lines  $\frac{x}{-3} = \frac{y-1}{1} = \frac{z+1}{-1}$  and  $\frac{x-2}{1} = \frac{y-3}{2} = \left(\frac{z+(13/7)}{-1}\right)$  is zero. Statement 2: The given lines are perpendicular.

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**238.** Find the number of sphere of radius  $r$  touching the coordinate axes.

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**239.** Find the distance of the z-axis from the image of the point  $M(2 - 3, 3)$  in the plane  $x - 2y - z + 1 = 0$ .

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**240.** A line with direction cosines proportional to 1,  $-5$ , and  $-2$  meets lines  $x = y + 5 = z + 1$  and  $x + 5 = 3y = 2z$ . The coordinates of each of the points of the intersection are given by a.  $(2, -3, 1)$  b.  $(1, 2, 3)$  c.  $(0, 5/3, 5/2)$  d.  $(3, -2, 2)$

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**241.** If the planes

$$\vec{r} \cdot \hat{i} + \hat{j} + \hat{k} = q_1, \vec{r} \cdot \hat{i} + 2a\hat{j} + \hat{k} = q_2 \text{ and } \vec{r} \cdot a\hat{i} + a^2\hat{j} + \hat{k} = q_3$$

intersect in a line, then the value of  $a$  is a. 1 b.  $1/2$  c. 2 d. 0

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**242.** The equation of a line passing through the point  $\vec{a}$  parallel to the plane  $\vec{r} \cdot \vec{n} = q$  and perpendicular to the line  $\vec{r} = \vec{b} + t\vec{c}$  is a.

$\vec{r} = \vec{a} + \lambda(\vec{n} \times \vec{c})$       b.  $(\vec{r} - \vec{a}) \times (\vec{n} \times \vec{c})$       c.

$\vec{r} = \vec{b} + \lambda(\vec{n} \times \vec{c})$       d. none of these

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**243.** A straight line  $L$  on the  $xy$ -plane bisects the angle between  $OX$  and  $OY$ . What are the direction cosines of  $L$ ? a.

$\langle (1/\sqrt{2}), (1/\sqrt{2}), 0 \rangle$       b.  $\langle (1/2), (\sqrt{3}/2), 0 \rangle$       c.  $\langle 0, 0, 1 \rangle$       d.  $\left\langle \begin{matrix} 2/3 \\ 2/3 \\ 1/3 \end{matrix} \right\rangle$

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**244.** Statement 1: Vector  $\vec{c} = 5\hat{i} + 7\hat{j} + 2\hat{k}$  is along the bisector of angle between  $\vec{a} = \hat{i} + 2\hat{j} + 2\hat{k}$  and  $\vec{b} = -8\hat{i} + \hat{j} - 4\hat{k}$ . Statement 2:  $\vec{c}$  is equally inclined to  $\vec{a}$  and  $\vec{b}$ .

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**245.** The equation of the line  $x + y + z - 1 = 0$ ,  $4x + y - 2z + 2 = 0$  written in the symmetrical form is

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**246.** The equation of two straight lines are  $\frac{x-1}{2} = \frac{y+3}{1} = \frac{z-2}{-3}$  and  $\frac{x-2}{1} = \frac{y-1}{-3} = \frac{z+3}{2}$ . Statement 1: the given lines are coplanar. Statement 2: The equations  $2x_1 - y_1 = 1$ ,  $x_1 + 3y_1 = 4$  and  $3x - 1 + 2y_1 = 5$  are consistent.

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**247.** Statement 1: Lines  $\vec{r} = \hat{i} + \hat{j} - \hat{k} + \lambda(3\hat{i} - \hat{j})$  and  $\vec{r} = 4\hat{i} - \hat{k} + \mu(2\hat{i} + \hat{j} + 3\hat{k})$  intersect. Statement 2:  $\vec{b} \times \vec{d} = 0$ , then lines  $\vec{r} = \vec{a} + \lambda\vec{b}$  and  $\vec{r} = \vec{c} + \lambda\vec{d}$  do not intersect.

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**248.** Statement 1: Line  $\frac{x-1}{1} = \frac{y-0}{2} = \frac{z-2}{-1}$  lies in the plane  $2x - 3y - 4z - 10 = 0$ . Statement 2: if line  $\vec{r} = \vec{a} + \lambda \vec{b}$  lies in the plane  $\vec{r} \cdot \vec{c} = n$  (where  $n$  is scalar), then  $\vec{b} \cdot \vec{c} = 0$ .

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**249.** What is the equation of the plane which passes through the z-axis and is perpendicular to the line  $\frac{x-a}{\cos \theta} = \frac{y+2}{\sin \theta} = \frac{z-3}{0}$ ? (A)  $x + y \tan \theta = 0$  (B)  $y + x \tan \theta = 0$  (C)  $x \cos \theta - y \sin \theta = 0$  (D)  $x \sin \theta - y \cos \theta = 0$

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**250.** Statement 1: let  $A(\vec{i} + \vec{j} + \vec{k})$  and  $B(\vec{i} - \vec{j} + \vec{k})$  be two points. Then point  $P(2\vec{i} + 3\vec{j} + \vec{k})$  lies exterior to the sphere with  $AB$  as its diameter. Statement 2: If  $A$  and  $B$  are any two points and  $P$  is a

point in space such that  $\vec{P} \vec{A} \vec{P} B > 0$ , then point  $P$  lies exterior to the sphere with  $AB$  as its diameter.

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**251.** Statement 1: Let  $\theta$  be the angle between the line  $\frac{x-2}{2} = \frac{y-1}{-3} = \frac{z+2}{-2}$  and the plane  $x+y-z=5$ . Then  $\theta = \sin^{-1}(1/\sqrt{51})$ . Statement 2: The angle between a straight line and a plane is the complement of the angle between the line and the normal to the plane.

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**252.** If the volume of tetrahedron  $ABCD$  is 1 cubic units, where  $A(0, 1, 2)$ ,  $B(-1, 2, 1)$  and  $C(1, 2, 1)$ , then the locus of point  $D$  is a.  
 $x+y-z=3$  b.  $y+z=6$  c.  $y+z=0$  d.  $y+z=-3$

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253. The equation of the plane which is equally inclined to the lines

$$\frac{x-1}{2} = \frac{y}{-2} = \frac{z+2}{-1} \text{ and } \frac{x+3}{8} = \frac{y-4}{1} = \frac{z}{-4} \text{ and passing}$$

through the origin is/are a.  $14x - 5y - 7z = 0$  b.  $2x + 7y - z = 0$  c.

$3x - 4y - z = 0$  d.  $x + 2y - 5z = 0$



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254. Which of the following lines lie on the plane  $x + 2y - z + 4 = 0$ ? a.

$\frac{x-1}{1} = \frac{y}{-1} = \frac{z-5}{1}$  b.  $x - y + z = 2x + y - z = 0$  c.

$\hat{r} = 2\hat{i} - \hat{j} + 4\hat{k} + \lambda(3\hat{i} + \hat{j} + 5\hat{k})$  d. none of these



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255. The equations of the plane which passes through  $(0, 0, 0)$  and which

is equally inclined to the planes

$x - y + z - 3 = 0$  and  $x + y = z + 4 = 0$  is/are a.  $y = 0$  b.  $x = 0$  c.

$x + y = 0$  d.  $x + z = 0$



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**256.** The  $x$ - $y$  plane is rotated about its line of intersection with the  $y$ - $z$  plane by  $45^\circ$ , then the equation of the new plane is/are a.  $z + x = 0$  b.  $z - y = 0$  c.  $x + y + z = 0$  d.  $z - x = 0$



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**257.** Consider the planes  $3x - 6y + 2z + 5 = 0$  and  $4x - 12 + 3z = 3$ . The plane  $67x - 162y + 47z + 44 = 0$  bisects the angle between the given planes which a. contains origin b. is acute c. is obtuse d. none of these



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**258.** A variable plane  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$  at a unit distance from origin cuts the coordinate axes at  $A, B$  and  $C$ . Centroid  $(x, y, z)$  satisfies the equation  $\frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = K$ . The value of  $K$  is (A) 9 (B) 3 (C)  $\frac{1}{9}$  (D)  $\frac{1}{3}$



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**259.** Let  $P = 0$  be the equation of a plane passing through the line of intersection of the planes  $2x - y = 0$  and  $3z - y = 0$  and perpendicular to the plane  $4x + 5y - 3z = 8$ . Then the points which lie on the plane  $P = 0$  is/are a.  $(0, 9, 17)$  b.  $(1/7, 21/9)$  c.  $(1, 3, -4)$  d.  $(1/2, 1, 1/3)$

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**260.** The equation of the line  $x + y + z - 1 = 0$ ,  $4x + y - 2z + 2 = 0$  written in the symmetrical form is

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**261.** A point  $P$  moves on a plane  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ . A plane through  $P$  and perpendicular to  $OP$  meets the coordinate axes at  $A$ ,  $B$  and  $C$ . If the planes through  $A$ ,  $B$  and  $C$  parallel to the planes  $x = 0$ ,  $y = 0$  and  $z = 0$ , respectively, intersect at  $Q$ , find the locus of  $Q$ .

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**262.** If the planes  $x - cy - bz = 0$ ,  $cx = y + az = 0$  and  $bx + ay - z = 0$  pass through a straight line, then find the value of  $a^2 + b^2 + c^2 + 2abc$

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**263.** Find the equation of the plane through the points  $(1, 0, -1)$ ,  $(3, 2, 2)$  and parallel to the line  $\frac{x-1}{1} = \frac{y-1}{-2} = \frac{z-2}{3}$ .

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**264.** A variable plane passes through a fixed point  $(\alpha, \beta, \gamma)$  and meets the axes at  $A$ ,  $B$ , and  $C$ . show that the locus of the point of intersection of the planes through  $A$ ,  $B$  and  $C$  parallel to the coordinate planes is  $\alpha x^{-1} + \beta y^{-1} + \gamma z^{-1} = 1$ .

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**265.** Show that the straight lines whose direction cosines are given by the equations  $al + bm + cn = 0$  and  $ul^2 + zm^2 = vn^2 + wn^2 = 0$  are parallel or perpendicular as  $\frac{a^2}{u} + \frac{b^2}{v} + \frac{c^2}{w} = 0$  or  $a^2(v + w) + b^2(w + u) + c^2(u + v) = 0$

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**266.** The perpendicular distance of a corner of uni cube from a diagonal not passing through it is

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**267.** If the direction cosines of a variable line in two adjacent points be  $l, M, n$  and  $l + \delta l, m + \delta m + n + \delta n$  the small angle  $\delta\theta$  as between the two positions is given by

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268. The image of the point  $(-1, 3, 4)$  in the plane  $x - 2y = 0$  is a.

- a.  $\left(-\frac{17}{3}, -\frac{19}{3}, 4\right)$    b.  $(15, 11, 4)$    c.  $\left(-\frac{17}{3}, -\frac{19}{3}, 1\right)$    d.  $\left(\frac{9}{5}, -\frac{13}{5}, 4\right)$

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269. The ratio in which the plane  $\vec{r} \cdot \vec{i} - 2\vec{j} + 3\vec{k} = 17$  divides the line joining the points  $-2\vec{i} + 4\vec{j} + 7\vec{k}$  and  $3\vec{i} - 5\vec{j} + 8\vec{k}$  is a. 1:5 b. 1:10 c. 3:5 d. 3:10

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270. Let  $L$  be the line of intersection of the planes  $2x + 3y + z = 1$  and  $x + 3y + 2z = 2$ . If  $L$  makes an angle  $\alpha$  with the positive x-axis, then  $\cos \alpha$  equals a.  $\frac{1}{2}$  b. 1 c.  $\frac{1}{\sqrt{2}}$  d.  $\frac{1}{\sqrt{3}}$

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271. The distance between the line  $\vec{r} = 2\hat{i} - 2\hat{j} + 3\hat{k} + \lambda(\hat{i} - \hat{j} + 4\hat{k})$  and the plane  $\vec{r} \cdot \hat{i} + 5\hat{j} + \hat{k} = 5$  is a.  $\frac{10}{3\sqrt{3}}$  b.  $\frac{10}{9}$  c.  $\frac{10}{3}$  d.  $\frac{3}{10}$



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272. If angle  $\theta$  between the line  $\frac{x+1}{1} = \frac{y-1}{2} = \frac{z-2}{2}$  and the plane  $2x - y + \sqrt{\lambda}z + 4 = 0$  is such that  $\sin\theta = 1/3$ , the value of  $\lambda$  is a.  $-\frac{3}{5}$  b.  $\frac{5}{3}$  c.  $-\frac{4}{3}$  d.  $\frac{3}{4}$



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273. The length of the perpendicular drawn from  $(1, 2, 3)$  to the line  $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$  is a. 4 b. 5 c. 6 d. 7



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**274.** A plane makes intercepts  $OA$ ,  $OB$  and  $OC$  whose measurements are  $a$ ,  $b$  and  $c$  on the  $OX$ ,  $OY$  and  $OZ$  axes. The area of triangle  $ABC$  is a.  $\frac{1}{2}(ab + bc + ca)$  b.  $\frac{1}{2}abc(a + b + c)$  c.  $\frac{1}{2}(a^2b^2 + b^2c^2 + c^2a^2)^{1/2}$  d.  $\frac{1}{2}(a + b + c)^2$



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**275.** The intersection of the spheres  $x^2 + y^2 + z^2 + 7x - 2y - z = 13$  and  $x^2 + y^2 + z^2 - 3x + 3y + 4z = 8$  is the same as the intersection of one of the spheres and the plane a.  $x - y - z = 1$  b.  $x - 2y - z = 1$  c.  $x - y - 2z = 1$  d.  $2x - y - z = 1$



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**276.** The shortest distance from the plane  $12x + 4y + 3z = 327$  to the sphere  $x^2 + y^2 + z^2 + 4x - 2y - 6z = 155$  is a. 39 b. 26 c.  $41 - \frac{4}{13}$  d.



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277. A line makes an angle  $\theta$  with each of the x-and z-axes. If the angle  $\beta$ , which it makes with the y-axis, is such that  $\sin^2 \beta = 3 \sin^2 \theta$ , then  $\cos^2 \theta$  equals a.  $\frac{2}{3}$  b.  $\frac{1}{5}$  c.  $\frac{3}{5}$  d.  $\frac{2}{5}$

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278. Find the equation of a straight line in the plane  $\vec{r} \cdot \vec{n} = d$  which is parallel to  $\vec{r} = \vec{a} + \lambda \vec{b}$  and passes through the foot of the perpendicular drawn from point

$P(\vec{a}) \rightarrow \vec{r} \cdot \vec{n} = d$  (where  $\vec{n} \cdot \vec{b} = 0$ ). a.

$\vec{r} = \vec{a} + \left( \frac{d - \vec{a} \cdot \vec{n}}{n^2} \right) \vec{n} + \lambda \vec{b}$  b.

$\vec{r} = \vec{a} + \left( \frac{d - \vec{a} \cdot \vec{n}}{n} \right) \vec{n} + \lambda \vec{b}$  c.

$\vec{r} = \vec{a} + \left( \frac{\vec{a} \cdot \vec{n} - d}{n^2} \right) \vec{n} + \lambda \vec{b}$  d.

$\vec{r} = \vec{a} + \left( \frac{\vec{a} \cdot \vec{n} - d}{n} \right) \vec{n} + \lambda \vec{b}$

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**279.** What is the nature of the intersection of the set of planes  $x + ay + (b + c)z + d = 0$ ,  $x + by + (a + a)z + d = 0$  and  $x + cy + (a + a)z + d = 0$

a. they meet at a point b. they form a triangular prism c. they pass through a line d. they are at equal distance from the origin

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**280.** Let  $P_1$  denote the equation of a plane to which the vector  $(\hat{i} + \hat{j})$  is normal and which contains the line whose equation is  $\vec{r} = \hat{i} + \hat{j} + \hat{k} + \lambda(\hat{i} - \hat{j} - \hat{k})$  and  $P_2$  denote the equation of the plane containing the line  $L$  and a point with position vector  $\hat{j}$ . Which of the following holds good? a. The equation of  $P_1$  is  $x+y=2$ . b. The equation of  $P_2$  is  $\vec{r} \cdot (i - 2j + k) = 2$  c. The acute angle between  $P_1$  and  $P_2$  is  $\cot^{-1} \sqrt{3}$  d. The angle between plane  $P_2$  and the line  $L$  is  $\tan^{-1} \sqrt{3}$

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**281.** Let  $PM$  be the perpendicular from the point  $P(1, 2, 3)$  to the  $x - y$  plane. If  $\vec{OP}$  makes an angle  $\theta$  with the positive direction of the  $z -$  axis and  $\vec{OM}$  makes an angle  $\phi$  with the positive direction of  $x -$  axis, where  $O$  is the origin and  $\theta$  and  $\phi$  are acute angles, then a.  $\cos \theta \cos \phi = 1/\sqrt{14}$  b.  $\sin \theta \sin \phi = 2/\sqrt{14}$  c.  $\tan \phi = 2$  d.  $\tan \theta = \sqrt{5}/3$

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**282.** If the plane  $\frac{x}{2} + \frac{y}{3} + \frac{z}{6} = 1$  cuts the axes of coordinates at points,  $A, B,$  and  $C$ , then find the area of the triangle  $ABC$ . a.  $18sq.$  unit b.  $36sq.$  unit c.  $3\sqrt{14}sq.$  unit d.  $2\sqrt{14}sq.$  unit

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**283.** For what value (s) of  $a$  will the two points  $(1, a, 1)$  and  $(-3, 0, a)$  lie on opposite sides of the plane  $3x + 4y - 12z + 13 = 0$ ?

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## Question Bank

1. Let the line  $L_1: \frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$  and  $L_2: \frac{x-2}{1} = \frac{y-3}{2} = \frac{z-k}{4}$  intersect at  $P$ . The least distance of  $P$  from the plane  $3x - 4y - 12z + 4 = 0$ , equals

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2. Consider two lines  $L_1: \frac{x-7}{3} = \frac{y-7}{2} = \frac{z-3}{1}$  and  $L_2: \frac{x-1}{2} = \frac{y+1}{4} = \frac{z+1}{3}$ . If a line  $L$  whose direction ratios are  $\langle 2, 2, 1 \rangle$  intersect the lines  $L_1$  and  $L_2$  at  $A$  and  $B$  then the distance  $AB$  is

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3. If the lines  $L_1: x - 2y + 4z = 0, 2x + y + z - 4 = 0$  and  $L_2: \frac{x-2}{2} = \frac{y}{1} = \frac{z-1}{2}$  are perpendicular, then  $a$  is equal to



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4. Line drawn perpendicular to plane  $x + 2y - 3z = 21$  at point  $A$  meets plane  $2x + ky + 5z = 8$  at point  $B$ . If mid point of  $AB$  is  $(1, -1, 2)$ , then  $k$  is equal to



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5. The equation of the plane which has the property that the point  $Q(5, 4, 5)$  is the reflection of point  $P(1, 2, 3)$  through that plane, is  $ax + by + cz = d$  where  $a, b, c, d \in N$ . Find the least value of  $(a + b + c + d)$ .



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6. Consider a plane  $\Pi: \vec{r} \cdot (2\hat{i} + \hat{j} - \hat{k}) = 5$ , a line  $L_1: \text{vecr} = 3\hat{i} - \hat{j} + 2\hat{k} + \lambda(2\hat{i} - 3\hat{j} - \hat{k})$  where  $\lambda \in R$  and a point  $A(3, -4, 1)$ . The line  $L_1$  intersects plane  $\Pi$  at  $Q$  and  $xy$  plane at  $R$ . If

the volume of tetrahedron  $OAQR$  ( $O$  is origin) is  $\frac{m}{n}$  where  $m$  and  $n$  are relatively prime positive integers, then find  $(3m - 5n)$ .

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7. If  $L: x - \frac{2}{a} = y - \frac{0}{b} = z - \frac{p}{c}$  where  $a, b \in I$  is a line parallel to the line of intersection of the plane  $x + y = 2$  and the  $x - y$  plane whose distance from the origin is  $3\sqrt{2}$  units (z-coordinate is positive of every point on the line), then find least value of  $|a + b + c + p|$

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8. If the angle between the plane  $x - 3y + 2z = 1$  and the line  $x - \frac{1}{2} = y - \frac{1}{1} = z - \frac{1}{-3}$  is  $\theta$ , then the value of  $\cos ec\theta$  is

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9. A plane  $P$  is perpendicular to the vector  $A = 2i + 3j + 6k$  and contains the terminal point of the vector  $\vec{B} = \hat{i} + 5\hat{j} + 3\hat{k}$ . The distance from the origin to the plane  $P$ , is

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10. The intersection of the planes  $2x - y - 3z = 8$  and  $x + 2y - 4z = 14$  is the line  $L$ . The value of  $a$  for which the line  $L$  is perpendicular to the line through  $(a, 2, 2)$  and  $(6, 11, -1)$  is

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11. Let  $Q$  be the foot of perpendicular from the origin to the plane  $4x - 3y + z + 13 = 0$  and  $R$  be a point  $(-1, 1, -6)$  on the plane. The length  $QR$  is

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12. If a line passing through  $A(1, 2, 3)$  and  $B(-1, 3, 5)$  meets the plane  $x + 3y + 5z - 3 = 0$  at  $C$ , then  $BC$  is equal to



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13. If direction ratios of the normal of the plane which contains the lines  $x - \frac{2}{3} = y - \frac{4}{2} = z - \frac{1}{1}$  and  $x - \frac{6}{3} = y + \frac{2}{2} = z - \frac{2}{1}$  are  $(a, 1, -26)$ , then  $a$  is equal to



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14. The point of intersection of the plane  $\vec{r} \cdot (2\hat{i} - \hat{j} + 3\hat{k}) = 6$  with the straight line passing through origin and perpendicular to the plane  $2x + y + z = 0$  is  $(p, q, r)$ . Then the value of  $(2p - 3q + r)$



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15. Shortest distance between  $\bar{z}$  -axis and the line  $x + y + 2z - 3 = 0 = 2x + 3y + 4z - 4$  is

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16. If the plane  $2x + y + 2z = 9$  intersects the co-ordinate axes in  $A, B$  and  $C$  and the co-ordinates of orthocentre of triangle  $ABC$  be  $(\alpha, \beta, \gamma)$ , then the value of  $\alpha + \beta + \gamma$  is

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17. If the plane  $2x - 2y - z - 11 = 0$  makes an angle  $\sin^{-1}(\lambda)$  with  $x$  - axis, then  $\lambda$  is equal to

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18. The vector  $\overline{AB} = 3\hat{i} + 4\hat{k}$  and  $ove \rightarrow owAC = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are the sides of a triangle  $ABC$ . The length of the median through  $A$  is

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19. The distance of the point  $(-1, -5, -10)$  from the point of intersection of the line  $\frac{x-2}{2} = \frac{y+1}{4} = \frac{z-2}{12}$  and the plane  $x - y + z = 5$  is

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20. Consider two lines in space as  $L_1: \vec{r}_1 = \hat{j} + 2\hat{k} + \lambda(3\hat{i} - \hat{j} - \hat{k})$  and  $L_2: \vec{r}_2 = 4\hat{i} + 3\hat{j} + 6\hat{k} + \mu(\hat{i} + 2\hat{k})$ . If the shortest distance between these lines is  $\sqrt{d}$  then  $d$  equals

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