# ©゙" doubtnut 

India's Number 1 Education App

## MATHS

## BOOKS - RS AGGARWAL MATHS

## (HINGLISH)

## COORDINATE GEOMETRY

## Solved Examples

1. Find the distance the points $A(7,13)$ and
$B(10,9)$.
A. 5
B. 6
C. 7
D. 8

Answer: A

## - Watch Video Solution

2. Find the distance between the points $P(-4,7)$
and $Q(2,-5)$.
A. 5
B. 6
C. 7
D. $6 \sqrt{5}$

Answer: D

## D Watch Video Solution

## 3. Find the distance of the point $(6,-6)$ from

the origin
A. $6 \sqrt{3}$
B. 6
C. $6 \sqrt{2}$
D. $3 \sqrt{2}$

Answer: C

D Watch Video Solution
4. Find the value of $y$ for which the distance between the points $A(3,-1)$ and $B(11, y)$ is 10 units.
A. -5
B. -6
C. 4
D. -7

## Answer: D

## D Watch Video Solution

5. If the point $P(k-1,2)$ is equidistant from
the points $A(3, k)$ and $B(k, 5)$, find the values of $k$.
A. $k=2$
B. $k=5$
C. $k=0$
D. $k=-1$

Answer: B

## D Watch Video Solution

6. Find the relation between $x$ and $y$ such that
the point $P(x, y)$ is equidistant from the points
$A(1,4)$ and $B(-1,2)$.

# 7. Find those points on $x$-axis, each of which is 

at a distance of 5 units from the point
$A(5,-3)$
A. $(0,1)$
B. $(-1,0)$
C. $(1,9)$
D. $(0,9)$
8. Find those points on the $y$-axis, each of which is at a distance of 13 units from the point $A(-5,7)$.
A. $(1,19)$
B. $(2,19)$
C. $(0,19)$
D. $(1,2)$
9. Find a point on y -axis which is equidistant from the points $(5,-2)$ and $(-3,2)$.

## D Watch Video Solution

10. Find the point on $Y$-axis which is equidistant from the points
$(-5,2)$ and $(9,-2)$.
A. $(0,-7)$
B. $(0,7)$
C. $(0,-5)$
D. $(0,5)$

Answer: A

## D Watch Video Solution

11. Find the coordinates of the point equidistant from three given points
$A(5,1), B(-3,-7)$ and $C(7,-1)$.
12. Points $A(-1, y)$ and $B(5,7)$ lie on a circle with centre $O(2,-3 y)$. Find the values of $y$. Hence, find the radius of the circle.
A. 2 units
B. 3 units
C. 4 units
D. 5 units

Answer: D
13. Find the centre of the circle passing through $(6,-6),(3,-7)$ and $(3,3)$.
A. $(3,1)$
B. $(-3,-1)$
C. $(-3,1)$
D. $(3,-2)$

Answer: D

- Watch Video Solution

14. The points $A(4,7), B(p, 3)$ and $C(7,3)$ are the vertices of a right triangle, right-angled at $B$,

Find the values of $p$.
A. 7
B. 3
C. 5
D. 4

Answer: D
15. Show that the points $(a, a),(-a,-a)$ and $(-\sqrt{3} a, \sqrt{3} a)$ are the vertices of an equilateral triangle. Also, find its area.

## D Watch Video Solution

16. Find the circumcenter of the triangle formed by the points $(-3,0),(1,-3)$ and $(4,1)$
A. $(1,-3)$
B. $(-3,0)$
C. $\left(\frac{1}{2}, \frac{1}{2}\right)$
D. $\left(\frac{1}{3}, \frac{1}{3}\right)$

Answer: C

## D Watch Video Solution

17. Show that the points $(1,1),(-1,5),(7,9)$ and
$(9,5)$ taken in that order are the vertices of a rectangle.
18. Show that the points $A(3,5), B(6,0), C(1,-3)$ and $D(-2,2)$ are the vertices of a square $A B C D$.

## D Watch Video Solution

19. If $P(2,-1), Q(3,4), R(-2,3)$ and
$S(-3,-2)$ be four points in a plane, show that $P Q R S$ is a rhombus but not a square.

Find the area of the rhombus.
20. Prove that points $A(1,1), B(-2,7)$ and $C(3$,

- 3) are collinear.


## D Watch Video Solution

21. Find the coordinates of the point which divides the line segment joining the points
$A(4,-3)$ and $B(9,7)$ in the ratio: 3:2.

- Watch Video Solution

22. Find the coordinates of the midpoint of
the line segment joining the points $A(-5,4)$ and $B(7,-8)$.
A. $(-1,2)$
B. $(1,-2)$
C. $(2,-4)$
D. $(1,1)$

Answer: B

- Watch Video Solution

23. Find the coordinates of the points of trisection of the line segment joining the points $A(-5,6)$ and $B(4,-3)$.

## D Watch Video Solution

24. Find the co-ordinates of a point $P$ on the
line segment joining $A(1,2)$ and $B(6,7)$
such that $A P=\frac{2}{5} A B$.
A. $(3,4)$
B. $(5,4)$
C. $(7,4)$
D. $(3,5)$

## Answer: A

## D Watch Video Solution

25. Point $P$ divides the line segment joining the
points $A(2,1)$ and $B(5,-8)$ such that
$A P / A B=1 / 3$. If $P$ lies on the line
$2 x-y+k=0$, find the value of k .
A. -7
B. -8
C. -9
D. -11

Answer: B

D Watch Video Solution
26. In what ratio does the point $P(2,-5)$ divide
the line segment joining $A(-3,5)$ and $B(4,-9)$ ?
27. Find the ratio in which the point $P(x, 2)$
divides the line segment joining the points
$A(12,5)$ and $B(4,-3)$. Also find the value of $x$.

## - Watch Video Solution

28. Find the ratio in which the point $P(11, y)$
divides the line segment joining the points
$A(15,5)$ and $B(9,20)$. Also find the value of y.

## - Watch Video Solution

29. If the point $C(-1,2)$ divides internally
the line segment joining $A(2,5)$ and $B$ in ratio $3: 4$, find the coordinates of $B$.

D Watch Video Solution
30. Find the lengths of the medians of a $A B C$
whose vertices are $A(7,-3), B(5,3)$ and
$C(3,-1)$.

## - Watch Video Solution

31. The three vertices of a parallelogram $A B C D$
taken in order are $\mathrm{A}(3,-4), \mathrm{B}(-1,-3)$ and $\mathrm{C}(-6,2)$.
Find the coordinates of the fourth vertex D .
32. If $(3,3),(6, y),(x, 7)$ and $(5,6)$ are the vertices of a parallelogram taken in order, find the value of $x$ and $y$.

## D Watch Video Solution

33. Let $D(3,-2), E(-3,1)$ and $F(4,-3)$ be the midpoints of the sides $B C, C A$ and $A B$ respectively of $\triangle A B C$. Then, find the coordinates the vertices $A, B$ and $C$.
34. The coordinates of one end point of a diameter of a circle are $(4,-1)$ and the coordinates of the centre of the circle are
$(1,-3)$. Find the coordinates of the other end of the diameter.

## D Watch Video Solution

35. Find the centroid of $\triangle A B C$ whose vertices are $A(-3,0), B(5,-2)$, and $C(-8,5)$.
36. Two vertices of a $\Delta A B C$ are given by $\mathrm{A}(6$,
4) and $B(-2,2)$, and its centroid is $G(3,4)$. Find
the coordinates of the third vertex $C$ of
$\triangle A B C$.

## - Watch Video Solution

37. Find the area of $\triangle A B C$ whose vertices are
$A(2,7), B(3,-1)$ and $C(-5,6)$.
38. Find the values of $k$ so that the area of the triangle with vertices (1, -1), (-4, 2k) and ( $-k,-5$ ) is 24 sq. units.

## D Watch Video Solution

39. If $A(4,-6), B(3,-2) a n d C(5,2)$ are
the vertices of $A B C$, then verify the fact that
a median of a triangle $A B C$ divides it into two triangles of equal areas.
40. Find the area of the triangle formed by joining the midpoints of the sides of the triangle whose vertices are $\mathrm{A}(2,2), \mathrm{B}(4,4)$ and $C(2,6)$.

## - Watch Video Solution

41. Find the area of a quadrilateral $A B C D$
whose vertices are $A(-4,8), B(-3,-4), C(0,-5)$ and
$D(5,6)$.
42. Find the area of a parallelogram $A B C D$ if
three of its vertices are
$A(2,4), B(2+\sqrt{3}, 5)$ and $C(2,6)$.
A. $(2 \sqrt{3})$
B. $(3 \sqrt{4})$
C. $(4 \sqrt{5})$
D. $(6 \sqrt{5})$

Answer: A
43. If the points
$A(1,-2), B(2,3), \quad C(-3,2) \quad$ and
$D(-4,-3)$ are the vertices of parallelogram $A B C D$, then taking $A B$ as the base, find the height of the parallelogram.

## D Watch Video Solution

44. Show that the points $A(-1,1), B(5,7)$ and
$C(8,10)$ are collinear.

## - Watch Video Solution

45. Show that points $A(a, b+c), B(b, c+a)$,
$C(c, a+b)$ are collinear.

## - Watch Video Solution

46. If the area of $\triangle A B C$ with vertices
$A(x, y), B(1,2)$ and $C(2,1)$ is 6 square units, then prove that $\mathrm{x}+\mathrm{y}=15$ or $\mathrm{x}+\mathrm{y}+9=0$.
47. Find the value of $k$ for which the points
$\mathrm{A}(\mathrm{k}+1,2 \mathrm{k}), \mathrm{B}(3 \mathrm{k}, 2 \mathrm{k}+3)$ and $\mathrm{C}(5 \mathrm{k}-1,5 \mathrm{k})$ are collinear.

## D Watch Video Solution

48. If the points $A(-1,-4), B(b, c)$ and
$C(5,-1)$ are collinear and $2 b+c=4$, find
the values of $b$ and $c$.

- Watch Video Solution

49. If $R(x, y)$ is a point on the line segment joining the points $P(a, b) a n d Q(b, a)$, then prove that $x+y=a+b$

## D Watch Video Solution

## Exercise 6 A

1. Find the distance between the points :
(i) $A(9,3)$ and $B(15,11)$ (ii) $A(7,-4)$ and $B(-5,1)$
(iii) $A(-6,-4)$ and $B(9,-12)$ (iv) $A(1,-3)$ and $B(4,-6)$
(v) $P(a+b, a-b)$ and $Q(a-b, a+b)$
(vi) $\mathrm{P}(\mathrm{a} \sin \alpha, \mathrm{a} \cos \alpha)$ and $\mathrm{Q}(\mathrm{a} \cos \alpha,-\mathrm{a} \sin \alpha)$

## D Watch Video Solution

2. Find the distance of each of the following points from the origin:
(i) $\mathrm{A}(5,-12)$ (ii) $\mathrm{B}(-5,5)$ (iii) $\mathrm{C}(-4,-6)$.

D Watch Video Solution
3. Find all possible values of x for which for distance between the points $\mathrm{A}(\mathrm{x},-1)$ and $\mathrm{B}(5,3)$ is 5 units.

## - Watch Video Solution

4. Find the values of $y$ for which the distance
between the points $P(2,-3)$ and $Q(10, y)$ is 10 units.
5. Find the values of $x$ for which the distance between the points $P(x, 4)$ and $Q(9,10)$ is 10 units.
( Watch Video Solution
6. If the point $A(x, 2)$ is equidistant from the points $B(8,-2)$ and $C(2,-2)$, find the value of $x$.

Also, find the length of $A B$.
7. If the point $A(0,2)$ is equidistant from the points $B(3, p)$ and $C(p, 5)$, find $p$. Also, find the length of $A B$.

## - Watch Video Solution

8. Find the point on $x$-axis which is equidistant from the points $(-2,5)$ and $(2,-3)$.
9. Find points on the x-axis, each of which is at a distance of 10 units from the point $A(11,-8)$.

D Watch Video Solution
10. Find the point on the $y$-axis which is equidistant from the points $A(6,5)$ and $B(-4,3)$.

D Watch Video Solution
11. If the point $P(x, y)$ is equidistant from the points $A(5,1)$ and $B(-1,5)$, prove that $3 x=2 y$.

## D Watch Video Solution

12. If $P(x, y)$ is a point equidistant from the points $A(6,-1)$ nad $B(2,3)$, show that $x-y-3$.

## D Watch Video Solution

13. Find the coordinates of the point equidistant from three given points $A(5,3)$, $B(5,-5)$ and $C(1,-5)^{\prime}$

## D Watch Video Solution

14. If the points $A(4,3)$ and $B(x, 5)$ lie on a circle with the centre $O(2,3)$, find the value of $x$.

## D Watch Video Solution

15. If the point $\mathrm{C}(-2,3)$ is equidistant from the points $A(3,-1)$ and $B(x, 8)$, find the values of $x$. Also, find the distance $B C$.

## - Watch Video Solution

16. If the point $P(2,2)$ is equidistant from the points $A(-2, k)$ and $B(-2 k,-3)$, find $k$. Also, find the length of AP.
17. (i) If the point ( $x, y$ ) is equidistant from the points $(a+b, b-a)$ and $(a-b, a+b)$, prove that $b x=$ ay.
(ii) If the distances of $\mathrm{P}(\mathrm{x}, \mathrm{y})$ from $\mathrm{A}(5,1)$ and $B(-1,5)$ are equal then prove that $3 x=2 y$.

## - Watch Video Solution

18. Using the distance formula, show that the given points are collinear.
(i) $(1,-1),(5,2)$ and $(9,5)$ (ii) $(6,9),(0,1)$ and $(-6$,
-7)
(iii) $(-1,-1),(2,3)$ and $(8,11)$ (iv) $(-2,5),(0,1)$ and (2, -3).

## D Watch Video Solution

19. Show that the points $A(7,10), B(-2,5)$ and
$C(3,-4)$ are the vertices of an isosceles right triangle.

D Watch Video Solution
20. Show that the points $A(3,0), B(6,4)$ and
$C(-1,3)$ are the vertices of an isosceles right triangle.

## D Watch Video Solution

21. If $A(5,2), B(2,-2)$ and $C(-2, t)$ are the vertices
of a right triangle with $\angle B=90^{\circ}$ then find
the value of $t$.
22. Prove that the points $A(2,4), B(2,6)$ and $C(2$
$+\sqrt{3}, 5)$ are the vertices of an equilateral triangle.
( Watch Video Solution
23. Show that the points $(-3,-3),(3,3)$ and
$(-3 \sqrt{3}, 3 \sqrt{3})$ are the vertices of an equilateral triangle.
24. The points $A(-5,6), B(3,0)$ and $C(9,8)$ are
the vertices of an isosceles right-angled triangle. Calculate its area.
A. 30
B. 50
C. 100
D. None of these

Answer: B
25. Show that the points $\mathrm{O}(0,0)$,
$A(3, \sqrt{3})$ and $B(3,-\sqrt{3})$ are the vertices of an equilateral triangle. Find the area of this triangle.

## D Watch Video Solution

26. Show that the following points are the vertices of a square:
(i) $A(3,2), B(0,5), C(-3,2)$ and $D(0,-1)$
(ii) $A(6,2), B(2,1), C(1,5)$ and $D(5,6)$
(iii) $A(0,-2), B(3,1), C(0,4)$ and $D(-3,1)$

## - Watch Video Solution

27. Show that the points $A(-3,2), B(-5,-5), C(2$,
$-3)$ and $D(4,4)$ are the vertices of a rhombus.
Find the area of this rhombus.

## - Watch Video Solution

28. Show that the points $A(3,0), B(4,5), C(-1,4)$
and $D(-2,-1)$ are the vertices of a rhombus. Find its area.

## Watch Video Solution

29. Show that the points $A(6,1), B(8,2), C(9,4)$
and $D(7,3)$ are the vertices of a rhombus. Find
its area.
A. 6 sq units
B. 3 sq units
C. $3 / 2$ sq units
D. 1 sq units

## - Watch Video Solution

30. Show that the points $A(2,1), B(5,2), C(6,4)$
and $D(3,3)$ are the angular points of a parallelogram. Is this figure a rectangle?

## - Watch Video Solution

31. Show that $A(1,2), B(4,3), C(6,6)$ and $D(3,5)$
are the vertices of a parallelogram. Show that
$A B C D$ is not a rectangle.
32. Show that the following points are the vertices of a rectangle.
(i) $A(-4,-1), B(-2,-4), C(4,0)$ and $D(2,3)$
(ii) $A(2,-2), B(14,10), C(11,13)$ and $D(-1,1)$
(iii) $A(0,-4), B(6,2), C(3,5)$ and $D(-3,-1)$

## D Watch Video Solution

33. Show that $\triangle A B C$ with vertices $\mathrm{A}(-2,0)$, $\mathrm{B}(0,2)$ and $\mathrm{C}(2,0)$ is similar to $\triangle D E F$ with
vertices $D(-4,0), F(4,0)$ and $E(0,4)$.

## - Watch Video Solution

34. Show that $\triangle A B C$, where
$A(-2,0), B(2,0), C(0,2)$ and $\triangle P Q R$
where $P(-4,0), Q(4,0)$ and $R(0,4)$ are similar triangles.

- Watch Video Solution

1. Find the coordinates of the point which divides the join of $A(-1,7)$ and $B(4,-3)$ in the ratio $2: 3$.
A. $\left(\frac{10}{3}, \frac{-20}{3}\right)$
B. $\left(2, \frac{8}{3}\right)$
C. $(3,1)$
D. $(1,3)$

## Answer: D

2. Find the coordinates of the points of trisection of the line segment joining the points $A(7,-2)$ and $B(1,5)$.

## D Watch Video Solution

3. If the coordinates of points $A$ and $B$ are ( -2 ,
-2 ) and (2, -4) respectively, find the coordinates
of the point P such that $A P=\frac{3}{7} A B$, where P lies on the line segment $A B$.
4. Point A lies on the line segment PQ joining
$P(6,-6)$ and $Q(-4,-1)$ in such a way that $\frac{P A}{P Q}=\frac{2}{5}$. If the point A also lies on the line $3 x+k(y+1)=0$, find the value of $k$.

## - Watch Video Solution

5. Points $P, Q, R$ and $S$ divide the line segment joining the points $A(1,2)$ and $B(6,7)$ in five equal parts. Find the coordinates of the point P.
A. $P(3,4)$
B. $P(4,5)$
C. $P(2,3)$
D. $P(2,1)$

Answer: C

## D Watch Video Solution

6. Points $P, Q$ and $R$ in that order are dividing a line segment joining $A(1,6)$ and $B(5,-2)$, in four equal parts. Find the coordinates of $P, Q$ and $R$.

## - Watch Video Solution

7. The line segment joining the points $A(3,-4)$ and $\mathrm{B}(1,2)$ is trisected at the points $\mathrm{P}(\mathrm{p},-2)$ and $Q\left(\frac{5}{3}, q\right)$. Find the values of p and q .

## - Watch Video Solution

8. Find the coordinates of the midpoint of the
line segment joining
(i) $A(3,0)$ and $B(-5,4)$ (ii) $P(-11,-8)$ and $Q(8,-2)$.
9. If $(2, p)$ is the midpoint of the line segment
joining the points $A(6,-5)$ and $B(-2,11)$,
find the value of $p$.
A. $p=3$
B. $p=5$
C. $p=-2$
D. $p=8$
10. The midpoint of the line segment joining
$A(2 a, 4)$ and $B(-2,3 b)$ is $C(1,2 a+1)$. Find the values of $a$ and $b$.

## - Watch Video Solution

11. The line segment joining $A(-2,9)$ and $B(6,3)$
is a diameter of a circle with centre $C$. Find the coordinates of C .

## Watch Video Solution

12. Find the coordinates of a point $A$, where $A B$ is a diameter of a circle with centre $C(2,-3)$ and the other end of the diameter is $\mathrm{B}(1,4)$.

## - Watch Video Solution

13. In what ratio does the point $P(2,5)$ divide the join of $A(8,2)$ and $B(-6,9)$ ?

## - Watch Video Solution

14. Find the ratio in which the point $P\left(\frac{3}{4}, \frac{5}{12}\right)$ divides the line segment joining the points $A\left(\frac{1}{2}, \frac{3}{2}\right)$ and $B(2,-5)$.

## - Watch Video Solution

15. Find the ratio in which the point $P(m, 6)$ divides the join of $A(-4,3)$ and $B(2,8)$.

Also, find the value of $m$.
A. $\frac{-2}{5}$
B. $\frac{2}{5}$
C. -2
D. Nome of these

Answer: A

## D Watch Video Solution

16. Find the ratio in which the point $(-3, k)$ divides the join of $A(-5,-4)$ and $B(-2,3)$. Also, find the value of $k$.
17. In what ratio is the line segment joining
$A(2,-3)$ and $B(5,6)$ divided by the $x$-axis? Also,
find the coordinates of the point of division.

## D Watch Video Solution

18. In what ratio is the line segment joining the points $A(-2,-3)$ and $B(3,7)$ divided by the $y-$ axis? Also, find the coordinates of the point of division.

## Watch Video Solution

19. In what ratio does the line $x-y-2=0$ divide the line segment joining the points $A(3,-1)$ and $B(8,9)$ ?

- Watch Video Solution

20. Find the lengths of the medians of a
$\Delta A B C$ whose vertices are $\mathrm{A}(0,-1), \mathrm{B}(2,1)$ and
$C(0,3)$.

D Watch Video Solution
21. Find the centroid of $\triangle A B C$ whose vertices are $A(-1,0), B(5,-2)$ and $C(8,2)$.

## D Watch Video Solution

22. If $\mathrm{G}(-2,1)$ is the centroid of a $\Delta A B C$ and two of its vertices are $A(1,-6)$ and $B(-5,2)$, find the third vertex of the triangle.
23. Find the third vertex of a $\triangle A B C$ if two of
its vertices are $B(-3,1)$ and $C(0,-2)$, and its centroid is at the origin.

## - Watch Video Solution

24. Show that the points $A(3,1), B(0,-2), C(1,1)$
and $D(4,4)$ are the vertices of a parallelogram
ABCD.
25. If the points $P(a,-11), Q(5, b), R(2,15)$ and $S(1,1)$ are the vertices of a parallelogram $P Q R S$, find the values of a.
A. 5
B. 3
C. 4
D. 2

Answer: C

- Watch Video Solution

26. If three consecutive vertices of $a$ parallelogram are $(1,-2),(3,6)$ and $(5,10)$, find its fourth vertex.

## D Watch Video Solution

27. In what ratio does $y$-axis divide the line segment joining the points $(-4,7)$ and $(3,-7)$ ?
28. If the point $P\left(\frac{1}{2}, y\right)$ lies on the line
segment joining the points $A(3,-5)$ and $B(-7,-9)$
the find the ratio in which $P$ divides $A B$. Also,
find the value of $y$.

## - Watch Video Solution

29. Find the ratio in which the line segment joining the points $A(3,-3)$ and $B(-2,7)$ is divided by $x$-axis. Also, find the point of division.
30. The base $Q R$ of an equilateral triangle $P Q R$ lies on $x$-axis. The coordinates of the point $Q$ are $(-4,0)$ and origin is the midpoint of the base. Find the coordinates of the points $P$ and $R$.

$$
\begin{aligned}
& \text { A. } P(0,5 \sqrt{4}) \operatorname{or} P(0,-5 \sqrt{4}) \text { and } R(3,2) \\
& \text { B. } P(0,4 \sqrt{3}) \operatorname{or} P(0,-4 \sqrt{3}) \text { and } R(4,0) \\
& \text { C. } P(0,3 \sqrt{2}) \operatorname{or} P(0,-3 \sqrt{2}) \text { and } R(3,1) \\
& \text { D. } P(0,2 \sqrt{5}) \operatorname{or} P(0,-2 \sqrt{5}) \text { and } R(3,5)
\end{aligned}
$$

Answer: B

## - Watch Video Solution

31. The base $B C$ of an equilateral triangle $A B C$,
lies on $y$-axis. The coordinates of point $C$ are
$(0,-3)$. The origin is the midpoint of the base.
Find the coordinates of the points $A$ and $B$.

## - Watch Video Solution

32. Find the ratio in which the point $P(-1, y)$
lying on the line segment joining points $A(-3$,
$10)$ and $B(6,-8)$ divides it. Also, find the value of
y.

## - Watch Video Solution

33. $A B C D$ is rectangle formed by the points
$A(-1,-1), B(-1,4), C(5,4)$ and $D(5,-1)$. If $P, Q, R$ and
$S$ be the midpoint of $A B, B C, C D$ and $D A$ respectively, show that PQRS is a rhombus.
34. The midpoint $P$ of the line segment joining the points $A(-10,4)$ and $B(-2,0)$ lies on the line segment joining the points $C(-9,-4)$ and $D(-4$, y). Find the ratio in which $P$ divides CD. Also find the value of $y$.

## - Watch Video Solution

35. A line intersects the $Y$ - axis at the points $P$ and $Q$, respectively. If $(2,-5)$ is the mid- point of
$P Q$, then the coordinates of $P$ and $Q$ are , respectively

## D Watch Video Solution

36. In what ratio does the point $\left(\frac{24}{11}, y\right)$ divide the line segment joining the points
$P(2,-2)$ and $Q(3,7)$ ? Also find the value of
$y$.

$$
\begin{aligned}
& \text { A. } 2: 8 ; y=-\frac{9}{11} \\
& \text { B. } 2: 9 ; y=-\frac{4}{11}
\end{aligned}
$$

> C. $5: 9 ; y=-\frac{3}{11}$
> D. $1: 9 ; y=-\frac{7}{11}$

Answer: B

## D Watch Video Solution

37. The midpoints of the sides $B C, C A$ and $A B$ of
a $\Delta A B C$ are $\mathrm{D}(3,4), \mathrm{E}(8,9)$ and $\mathrm{F}(6,7)$ respectively. Find the coordinates of the vertices of the triangle.
38. If two vertices of a parallelogram are
$(3,2),(-1,0)$ and the diagonals cut at
$(2,-5)$, find the other vertices of the parallelogram.
( Watch Video Solution

Exercise 6 C

1. Find the area of $\triangle A B C$ whose vertices are :
(i) $\mathrm{A}(1,2), \mathrm{B}(-2,3)$ and $\mathrm{C}(-3,-4)$
(ii) $A(-5,7), B(-4,-5)$ and $C(4,5)$
(iii) $A(3,8), B(-4,2)$ and $C(5,-1)$
(iv) $A(10,-6), B(2,5)$ and $C(-1,3)$

## D Watch Video Solution

2. Find the are of quadrilateral $A B C D$ whose vertices are $A(3,-1), B(9,-5), C(14,0)$ and $D(9$, 19).
3. 

$P(-5,-3), Q(-4,-6), R(2,-3)$
and $S(1,2)$ are the vertices of a quadrilateral
$P Q R S$, find its area.

- Watch Video Solution

4. Find the area of quadrilateral $A B C D$ whose vertices are $A(-3,-1), B(-2,-4), C(4,-1)$ and $D(3,4)$.
5. If $A(-7,5), B(-6,-7), C(-3,-8)$ and $D(2,3)$ are the vertices of a quadrilateral $A B C D$ then find the area of the quadrilateral.

## D Watch Video Solution

6. Find the area of the triangle formed by joining the midpoints of the sides of the triangle whose vertices are $A(2,1), B(4,3)$ and
$C(2,5)$.

## Watch Video Solution

7. $A(7,-3), B(5,3)$ and $C(3,-1)$ are the vertices of a $\triangle A B C$ and $A D$ is its median. Prove that the median AD divides $\triangle A B C$ into two triangles of equal areas.

## - Watch Video Solution

8. Find the area of $\triangle A B C$ with $A(1,-4)$ and midpoints of sides through $A$ being $(2,-1)$ and $(0,-1)$.
A. 19 sq units
B. 14 sq units
C. 13 sq units
D. 12 sq units

## Answer: D

## D Watch Video Solution

9. $A(6,1), B(8,2)$ and $C(9,4)$ are the vertices of a parallelogram $A B C D$. If $E$ is the midpoint of $D C$, find the area of $\triangle A D E$.

## - Watch Video Solution

10. (i) If the vertices of $\triangle A B C$ be $\mathrm{A}(1,-3), \mathrm{B}(4$,
p) and $C(-9,7)$ and its area is 15 square units, find the value of $p$.
(ii) The area of a triangle is 5 sq units. Two of its vertices are $(2,1)$ and ( $3,-2$ ). If the third vertex is $\left(\frac{7}{2}, y\right)$, find the value of $y$
11. Find the value of $k$ so that the area of the triangle with vertices $A(k+1,1), B(4,-3)$ and $C(7$, $-k)$ is 6 square units.

## D Watch Video Solution

12. For what value of $k(k>0)$ is the area of
the triangle with vertices $(-2,5),(k,-4)$ and ( $2 k$ $+1,10)$ equal to 53 square units?
13. Show that the following points are collinear:
(i) $A(2,-2), B(-3,8)$ and $C(-1,4)$
(ii) $A(-5,1), B(5,5)$ and $C(10,7)$
(iii) $A(5,1), B(1,-1)$ and $C(11,4)$
(iv) $\mathrm{A}(8,1), \mathrm{B}(3,-4)$ and $\mathrm{C}(2,-5)$

## D Watch Video Solution

14. Find the value of $x$ for which the points $A(x$,
2), $B(-3,-4)$ and $C(7,-5)$ are collinear.
15. For what value of $x$ are the points $A(-3,12)$, $B(7,6)$ and $C(x, 9)$ collinear?

## D Watch Video Solution

16. For what value of $y$ are the points $P(1,4)$,
$Q(3, y)$ and $R(-3,16)$ are collinear?

D Watch Video Solution
17. Find the value of $y$ for which the points $A(-3$, 9 ), $B(2, y)$ and $C(4,-5)$ are collinear.

## - Watch Video Solution

18. For what values of $k$ are the points $A(8,1)$, $B(3,-2 k)$ and $C(k,-5)$ collinear.

- Watch Video Solution

19. Find a relation between $x$ and $y$, if the points $A(2,1), B(x, y)$ and $C(7,5)$ are collinear.

D Watch Video Solution
20. Find a relation between $x$ and $y$, if the points $A(x, y), B(-5,7)$ and $C(-4,5)$ are collinear.

## D Watch Video Solution

21. Prove that the points $A(a, 0), B(0, b)$ and $C(1$,
1) are collinear, if $\frac{1}{a}+\frac{1}{b}=1$.

## D Watch Video Solution

22. If the points $P(-3,9), Q(a, b)$ and $R(4,-5)$ are
collinera and $a+b=1$, find the values of $a$ and b.

D Watch Video Solution
23. Find the area of $\triangle A B C$ with vertices $\mathrm{A}(0$,
$-1), B(2,1)$ and $C(0,3)$. Also, find the area of the triangle formed by joining the midpoints of its sides.

Show that the ratio of the areas of two triangles is 4:1.

## - Watch Video Solution

24. 

$a \neq b \neq c$, prove that $\left(a, a^{2}\right),\left(b, b^{2}\right),(0,0)$
will not be collinear.

## - Watch Video Solution

Exercise 6 D

1. Points $A(-1, y)$ and $B(5,7)$ lie on a circle with
centre $\mathrm{O}(2,-3 y)$. Find the values of y .

- Watch Video Solution

2. If the point $A(0,2)$ is equidistant from the points $B(3, p)$ and $C(p, 5)$, find $p$.

## - Watch Video Solution

3. $A B C D$ is rectangle whose three vertices are $B(4,0), C(4,3)$ and $D(0,3)$. Find the length of one of its diagonal.

## - Watch Video Solution

4. If the point $P(k-1,2)$ is equidistant from the point $A(3, k)$ and $B(k, 5)$, find the values of $k$.

## - Watch Video Solution

5. Find the ratio in which the point $P(x, 2)$ divides the join of $A(12,5)$ and $B(4,-3)$.
A. $5: 3$
B. $3: 5$
C. 1:3
D. $3: 2$

Answer: B

## D Watch Video Solution

6. Prove that the diagonals of a rectangle
$A B C D$ with vertices $A(2,-1), B(5,-1), C(5,6)$ and
$D(2,6)$ are equal and bisect each other.

D Watch Video Solution
7. Find the lengths of the medians $A D$ and $B E$ of $\triangle A B C$ whose vertices are $\mathrm{A}(7,-3), \mathrm{B}(5,3)$ and $C(3,-1)$.

## - Watch Video Solution

8. If the point $C(k, 4)$ divides the join of $A(2,6)$
and $B(5,1)$ in the ratio $2: 3$ then find the value of $k$.
9. Find the point on $x$-axis which is equidistant from points $A(-1,0)$ and $B(5,0)$.

## - Watch Video Solution

10. Find the distance between the points
$\left(\frac{-8}{5}, 2\right)$ and $\left(\frac{2}{5}, 2\right)$

## D Watch Video Solution

11. Find the value of a so that the point $(3, a)$
lies on the line represented by $2 x-3 y=5$

## D Watch Video Solution

12. If the points $A(4,3)$ and $B(x, 5)$ lie on a circle with the centre $O(2,3)$, find the value of $x$.

## D Watch Video Solution

13. If $\mathrm{P}(\mathrm{x}, \mathrm{y})$ is equidistant from the points $\mathrm{A}(7$,
1) and $B(3,5)$, find the relation between $x$ and $y$.

## - Watch Video Solution

14. If the centroid of $\triangle A B C$ having vertices
$A(a, b), B(b, c)$ and $C(c, a)$ is the origin, then
find the value of $(a+b+c)$.

## - Watch Video Solution

15. Find the centroid of $\triangle A B C$ whose vertices are $A(2,2), B(-4,-4)$ and $C(5,-8)$.

## D Watch Video Solution

16. In what ratio does the point $C(4,5)$ divide the join of $A(2,3)$ and $B(7,8)$ ?

## D Watch Video Solution

17. If the points $A(2,3), B(4, k)$ and $C(6,-3)$ are collinear, find the value of $k$.

D Watch Video Solution

## Multiple Choice Questions Mcq

1. The distance of the point $P(-6,8)$ from the origin is
A. 8
B. $2 \sqrt{7}$
C. 6
D. 10

Answer: D

## D Watch Video Solution

## 2. The distance of the point $(-3,4)$ from $x$-axis

is
A. 3
B. -3
C. 4
D. 5

## Answer: C

## - Watch Video Solution

3. The point on $x$-axis which is equidistant from points $A(-1,0)$ and $B(5,0)$ is
A. $(0,2)$
B. $(2,0)$
C. $(3,0)$
D. $(0,3)$

Answer: B

## D Watch Video Solution

4. If $R(5,6)$ is the midpoint of the line segment
$A B$ joining the points $A(6,5)$ and $B(4,4)$ then $y$
equals
A. 5
B. 7
C. 12
D. 6

Answer: B

## D Watch Video Solution

5. If the point $C(k, 4)$ divides the join of $A(2,6)$
and $B(5,1)$ in the ratio $2: 3$ then find the value of $k$.
A. 16
B. $\frac{28}{5}$
C. $\frac{16}{5}$
D. $\frac{8}{5}$

Answer: C

## D Watch Video Solution

6. The perimeter of the triangle with vertices
$(0,4),(0,0)$ and $(3,0)$ is
A. $(7+\sqrt{5})$
B. 5
C. 10
D. 12

## Answer: D

## D Watch Video Solution

## 7. If $A(1,3), B(-1,2), C(2,5)$ and $D(x, 4)$ are the

 vertices of a parallelogram $A B C D$ then the value of $x$ isA. 3
B. 4
C. 0
D. $\frac{3}{2}$

Answer: B

## D Watch Video Solution

8. If the points $A(x, 2), B(-3,-4)$ and $C(7,-5)$ are collinear then the value of $x$ is ?
A. -63
B. 63
C. 60
D. -60

Answer: A

## D Watch Video Solution

9. The area of a triangle with vertices $A(5,0)$, $B(8,0)$ and $C(8,4)$ in square units is
A. 20
B. 12
C. 6
D. 16

Answer: C

## D Watch Video Solution

10. The area of $\Delta A B C$ with vertices $\mathrm{A}(\mathrm{a}, 0)$,
$O(0,0)$ and $B(0, b)$ in square units is
A. $a b$
B. $\frac{1}{2} a b$
C. $\frac{1}{2} a^{2} b^{2}$
D. $\frac{1}{2} b^{2}$

Answer: B

## D Watch Video Solution

11. If $P\left(\frac{a}{2}, 4\right)$ is the midpoint of the line segment joining the points $A(-6,5)$ and $B(-2,3)$
then the value of $a$ is
A. -8
B. 3
C. -4
D. 4

Answer: A

## D Watch Video Solution

12. $A B C D$ is a rectangle whose three vertices
are $B(4,0), C(4,3)$ and $D(0,3)$. The length of
one of its diagonals is
A. 5
B. 4
C. 3
D. 25

Answer: A

D Watch Video Solution
13. The coordinates of the point $P$ dividing the
line segment joining the points $A(1,3)$ and $B(4$,
6) in the ratio $2: 1$ is
A. $(2,4)$
B. $(3,5)$
C. $(4,2)$
D. $(5,3)$

Answer: B

## D Watch Video Solution

14. If the coordinates of one end of a diameter of a circle are $(2,3)$ and the coordinates of its
centre are $(-2,5)$, then the coordinates of the other end of the diameter are
A. $(-6,7)$
B. $(6,-7)$
C. $(4,2)$
D. $(5,3)$

Answer: A
( Watch Video Solution
15. In the given figure $P(5,-3)$ and $Q(3, y)$ are
the points of trisection of the line segment
joining $A(7,-2)$ and $B(1,-5)$. Then, $y$ equals

A. 2
B. 4
C. -4
D. $\frac{-5}{2}$
16. The midpoint of segment $A B$ is $P(0,4)$. If the coordinates of $B$ are $(-2,3)$, then the coordinates of $A$ are
A. $(2,5)$
B. $(-2,-5)$
C. $(2,9)$
D. $(-2,11)$

Answer: A
17. The point $P$ which divides the line segment
joining the points $A(2,5)$ and $B(5,2)$ in the
ratio $2: 3$ lies in the quadrant
A. 1
B. II
C. III
D. IV
18. If $A(-6,7)$ and $B(-1,-5)$ are two given points
then the distance $2 A B$ is
A. 13
B. 26
C. 169
D. 238

Answer: B
19. What point on the $X$-axis is equidistant from $(7,6)$ and $(-3,4)$ ?
A. $(0,4)$
B. $(-4,0)$
C. $(3,0)$
D. $(0,3)$

Answer: C

- Watch Video Solution

20. The distance of $P(3,4)$ from the $x$-axis is
A. 3 units
B. 4 units
C. 5 units
D. 1 unit

Answer: B

- Watch Video Solution

21. In what ratio does the $x$-axis divide the join of $A(2,-3)$ and $B(5,6)$ ?
A. $2: 3$
B. 3:5
C. 1:2
D. 2:1

Answer: C
( Watch Video Solution

## 22. In what ratio does the $Y$-axis divide the join

 of $(-4,2)$ and $(8,3)$ ?A. $3: 1$
B. $1: 3$
C. 2:1
D. 1:2

Answer: D
( Watch Video Solution
23. If $P(-1,1)$ is the midpoint of the line
segment joining $A(-3, b)$ and $B(1, b+4)$
then $b=$ ?
A. 1
B. -1
C. 2
D. 0

Answer: B
24. Determine the ratio in which the line
$2 x+y-4=0$ divides the line segment joining the points $A(2,-2)$ and $B(3,7)$.
A. $2: 5$
B. 2: 9
C. 2:7
D. $2: 3$

Answer: B

D Watch Video Solution
25. If $A(4,2), B(6,5)$ and $C(1,4)$ be the vertices
of $\triangle A B C$ and AD is a median, then the coordinates of $D$ are
A. $\left(\frac{5}{2}, 3\right)$
B. $\left(5, \frac{7}{2}\right)$
C. $\left(\frac{7}{2}, \frac{9}{2}\right)$
D. none of these

Answer: C

- Watch Video Solution

26. If $\mathrm{A}(-1,0), \mathrm{B}(5,-2)$ and $\mathrm{C}(8,2)$ are the vertices of a $\triangle A B C$ then its centroid is
A. $(12,0)$
B. $(6,0)$
C. $(0,6)$
D. $(4,0)$

Answer: D

- Watch Video Solution

27. Two vertices of $\Delta A B C$ are $\mathrm{A}(-1,4)$ and $\mathrm{B}(5$,
2) and its centroid is $G(0,-3)$. Then, the coordinates of $C$ are
A. $(4,3)$
B. $(4,15)$
C. $(-4,-15)$
D. $(-15,-4)$

## Answer: C

28. The points $A(-4,0), B(4,0)$ and $C(0,3)$ are the vertices of a triangle, which is
A. isosceles
B. equilateral
C. scalene
D. right angled

Answer: A
( Watch Video Solution
29. The points $P(0,6), Q(-5,3)$ and $R(3,1)$ are
the vertices of a triangle which is
A. equilateral
B. isosceles
C. scalene
D. right angled

Answer: D
( Watch Video Solution
30. Find the value of $k$ if the points $(2,3),(5, k)$
and $(6,7)$ are collinear .
A. $k=4$
B. $k=6$
C. $k=\frac{-3}{2}$
D. $k=\frac{11}{4}$

Answer: B

D Watch Video Solution
31. If the points $A(1,2), B(0,0)$ and $C(a, b)$ are collinear, then
A. $a=b$
B. $a=2 b$
C. $2 \mathrm{a}=\mathrm{b}$
D. $a+b=0$

Answer: C

D Watch Video Solution
32. The area of a triangle with vertices
$A(3,0), B(7,0)$ and $C(8,4)$ is
A. 14sq units
B. 28 sq units
C. 8 sq units
D. 6 sq units

Answer: C

D Watch Video Solution
33. If $A O B C$ is a ractangle whose three vertices are $A(0,3), O(0,0)$ and $B(5,0)$, then the length of its diagonal is
A. 5 units
B. 3 units
C. 4 units
D. $\sqrt{34}$ units

Answer: D

- Watch Video Solution

34. If the distance between the points $(4, p)$
and $(1,0)$ is 5 , then $p=$ ?

$$
\begin{aligned}
& \text { A. } p=4 \text { only } \\
& \text { B. } p=-4 \text { only } \\
& \text { C. } p= \pm 4 \\
& \text { D. } p=0
\end{aligned}
$$

Answer: C

