

## MATHS

### BOOKS - RS AGGARWAL MATHS (HINGLISH)

## CONDITIONAL IDENTITIES INVOLVING THE ANGLES OF A TRIANGLE

#### Solved Examples

1. If  $A + B + C = \pi$ , prove that

$$\sin 2A + \sin 2B + \sin 2C = 4 \sin A \sin B \sin C.$$



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2. If  $A + B + C = \pi$ , prove that

$$\sin 2A - \sin 2B + \sin 2C = 4 \cos A \sin B \cos C.$$





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3. If  $A + B + C = \pi$ , prove that

$$\cos 2A + \cos 2B + \cos 2C = -1 - 4 \cos A \cos B \cos C.$$



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4. If  $A + B + C = \pi$ , prove that :

$$\cos 2A + \cos 2B - \cos 2C = 1 - 4 \sin A \sin B \cos C$$



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5. If  $A + B + C = \pi$ , prove that

$$\cos 4A + \cos 4B + \cos 4C = -1 + 4 \cos 2A \cos 2B \cos 2C.$$



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$$6. \sin A + \sin B - \sin C = 4 \sin\left(\frac{A}{2}\right) \sin\left(\frac{B}{2}\right) \cos\left(\frac{C}{2}\right)$$



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7. If  $A + B + C = \pi$ , prove that :  $\cos A + \cos B - \cos C = 4 \cos\left(\frac{A}{2}\right) \cos\left(\frac{B}{2}\right) \sin\left(\frac{C}{2}\right)$



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8. If  $A + B + C = \pi$ , prove that  
 $\sin^2 A + \sin^2 B + \sin^2 C = 2(1 + \cos A \cos B \cos C)$



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9. If  $A + B + C = 180^\circ$ , prove that :  
 $\cos^2 A + \cos^2 B - \cos^2 C = 1 - 2 \sin A \sin B \cos C$



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10. Prove that:  $\cos^2 A + \cos^2\left(A + \frac{2\pi}{3}\right) + \cos^2\left(A - \frac{2\pi}{3}\right) = \frac{3}{2}$



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11. If  $A + B + C = \pi$ , prove that  
 $\frac{\sin^2 A}{2} + \frac{\sin^2 B}{2} - \frac{\sin^2 C}{2} = 1 - 2 \frac{\cos A}{2} \frac{\cos B}{2} \frac{\sin C}{2}$ .



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12. If  $A + B + C = \pi$  then prove that  
 $\cos^2\left(\frac{A}{2}\right) + \cos^2\left(\frac{B}{2}\right) - \cos^2\left(\frac{C}{2}\right) = 2 \cos\left(\frac{A}{2}\right) \cos\left(\frac{B}{2}\right) \sin\left(\frac{C}{2}\right)$



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13. If  $A + B + C = 180^\circ$ , prove that :  
 $\cos^2, \frac{A}{2} + \cos^2, \frac{B}{2} - \cos^2, \frac{C}{2} = 2 + 2 \sin, \frac{A}{2} \sin, \frac{A}{2}, \sin, \frac{B}{2}, \sin, \frac{B}{2}, \sin, \frac{C}{2}$



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14. If  $\tan A + \tan B + \tan C = \tan A \tan B \tan C$  then



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15. If  $A + B + C = \pi$ , prove that :

$$\frac{\tan A}{2} \frac{\tan B}{2} + \frac{\tan B}{2} \frac{\tan C}{2} + \frac{\tan C}{2} \frac{\tan A}{2} = 1$$



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16.  $\cot B \cot C + \cot C \cot A + \cot A \cot B = 1$



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17. If  $A + B + C = \pi$ , prove that :

$$\cot \frac{A}{2} + \cot \frac{B}{2} + \cot \frac{C}{2} = \cot \frac{A}{2} \cot \frac{B}{2} \cot \frac{C}{2}$$



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## Exercise 16

1. If  $A + B + C = 180^0$ , prove that

$$\sin 2A + \sin 2B - \sin 2C = 4 \cos A \cos B \sin C$$



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2. If  $A + B + C = \pi$ , prove that

$$\cos 2A - \cos 2B - \cos 2C = -1 + 4 \cos A \sin B \sin C$$



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3. If  $A + B + C = \pi$ , prove that :

$$\cos 2A + \cos 2B - \cos 2C = 1 - 4 \sin A \sin B \cos C$$



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4. If  $A + B + C = \pi$ , prove that :

$$\sin A + \sin B + \sin C = 4 \cos\left(\frac{A}{2}\right) \cos\left(\frac{B}{2}\right) \cos\left(\frac{C}{2}\right)$$



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5. If  $A + B + C = \pi$  then prove that

$$\cos A + \cos B + \cos C = 1 + 4 \sin\left(\frac{A}{2}\right) \cdot \sin\left(\frac{B}{2}\right) \cdot \sin\left(\frac{C}{2}\right)$$



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$$6. \frac{\sin 2A + \sin 2B + \sin 2C}{\sin A + \sin B + \sin C} = 8 \sin\left(\frac{A}{2}\right) \sin\left(\frac{B}{2}\right) \sin\left(\frac{C}{2}\right)$$



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7. If  $A + B + C = \pi$ , prove that :

$$\sin(B + C - A) + \sin(C + A - B) + \sin(A + B - C) = 4 \sin A \sin B \sin C$$



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8. If  $A + B + C = \pi$ , prove that :

$$\frac{\cos A}{\sin b \sin C} + \frac{\cos B}{\sin C \sin A} + \frac{\cos C}{\sin A \sin B} = 2.$$



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9. If  $A + B + C = 180^\circ$ , prove that

$$\cos^2 A + \cos^2 B + \cos^2 C = 1 - 2 \cos A \cos B \cos C.$$



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10. If  $A + B + C = \pi$ , prove that

$$\sin^2 A - \sin^2 B + \sin^2 C = 2 \sin A \cos B \sin C$$



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**11.** If  $A + B + C = 180^\circ$ , Prove that  $\sin^2(A/2) + \sin^2(B/2) + \sin^2(C/2) = 1 - 2 \sin A/2 \sin B/2 \sin C/2$



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**12.** If  $A + B + C = \frac{\pi}{2}$  then  $\tan 2A + \tan 2B + \tan 2C =$



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