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## MATHS

# BOOKS - RS AGGARWAL MATHS (HINGLISH) 

Relations

## Example

1. Find $a$ and $b$, when $(a-1, b+5)=(2,3)$.

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2. Find $a$ and $b$, when $(2 a+b, 11)=(1, a-3 b)$.
3. If $\left(\frac{x}{3}+1, y-\frac{2}{3}\right)=\left(\frac{5}{3}, \frac{1}{3}\right)$, find the values of x and y .

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4. Express $\left\{(x, y): x^{2}+y^{2}=25\right.$, where $\left.x, y \in W\right\}$ as a set of ordered pairs.

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5. If $A=\{1,3,5\}$ and $B=\{2,3\}$ then find:
(i)
$A \times B$
(ii) $B \times A$
$(i i i)(A \times B) \cap(B \times$

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6. If $A=\{1,2,3\}, B=\{3,4\}$ and $C=\{4,5,6\}$ then find:
(i) $A \times(B \cap C)$
(ii) $(A \times B) \cap(A \times C)$
(iii) $A \times(B \cup C)$
(iv) $(A \times B) \cup(A \times C)$

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7. Let $A=\left\{x \in N: x^{2}-5 x+6=0\right\}, B=\{x \in W: 0 \leq x<2\}$ and $C=\{x \in N: x<3\}$. Verify that
(i) $A \times(B \cup C)=(A \times B) \cup(A \times C)$
(ii) $A \times(B \cap C)=(A \times B) \cap(A \times C)$

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8. If $(A \times B)=\{(3,2),(3,4),(5,2),(5,4)\}$, find A and B .

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9. If $(1,3),(2,5)$ and $(3,3)$ are the three elements of $A \times B$ and the total number of elements in $A \times B$ is 6 then the remaining elements of $A \times B$ are

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10. Let $A=\{a, b\}$. List all relations on A and find their number.

Hint $A \times A=\{(a, a),(a, b),(b, a),(b, b)\}$ and every subset of $A \times A$ is a relation on A .

So, their number $=2^{4}=16$.

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11. If $R$ is the set of all real numbers, what do the cartesian products
$R \times R$ and $R \times R \times R$ represent?

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12. If $(A \times A)$ has 9 elements two of which are $(-1,0)$ and $(0,1)$, find the set A and the remaining elements of $(A \times A)$.

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13. If $A=\{1,2\}$, find $A \times A \times A$.
A. $\{(1,1,1),(1,1,2),(1,2,1),(2,1,1),(2,1,2),(2,2,1),(2,2,2)\}$.
B. $\{(1,1,2),(1,2,1),(2,1,1),(2,1,2),(2,2,1),(2,2,2)\}$.
C. $\{(1,1,1),(1,1,2),(1,2,1),(2,1,1),(2,1,2),(2,2,1)\}$.
D. None of these

## Answer: A

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14. If $R$ is the set of all real numbers, what do the cartesian products $R \times R$ and $R \times R \times R$ represent?
15. Let $A=\{1,2\}, B=\{3,4\}$ and $C=\{4,5\}$.

We have
verify that $(A \times B) \times C=A \times(B \times C)$ and hence find $A \times B \times C$.

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16. Let A and B be two nonempty sets such that $n(A)=5, n(B)=6$ and $n(A \cap B)=3$.

Find (i) $n(A \times B),(i i) n(B \times A)$ and (iii) $n\{(A \times B) \cap(B \times A)\}$.

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17. Let $A=\{-2,-1,0,1,2\}$ and $B=\{0,1,4,9\}$.

Let $R=\{(-2,4),(-1,1),(0,0),(1,1),(2,4)\}$.
(i) Show that R is a relation from A to B .
(ii) Find dom (R), range (R) and co-domain of $R$.

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18. Let $A=\{1,2,3,5\}$ and $B=\{4,6,9\}$.

Define a relation from $A$ to $B$, given by
$R=\{(a, b): a \in A, b \in B$ and $(a-b)$ is odd $\}$.
(i) Write R in roster form.
(ii) Find dom (R) and range (R).

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19. Let $R=\left\{\left(x, x^{3}\right): x\right.$ is a prime number less than 10$\}$.
(i) Write R in roster form.
(ii) Find dom (R) and range (R).

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20. Let $R=\{(x, y): \quad \mathrm{x}$ and y are integers and $x y=4\}$.
(i) Write R in roster form.
(ii) Find dom (R) and range (R).

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21. Let $A=\{1,2,3,4,5\}$. Define a relation R from A to a A by
$R=\{(x, y): y=2 x-3\}$.
(i) Depict R using arrow diagram.
(ii) Find dom (R) and range (R).

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22. Let $A=\{(1,2,3,4,5\}$ and $B=\{1,4,5\}$.

Let $R$ be a relation 'is less than' from $A$ to $B$.
(i) List the elements of R.
(ii) Find the domain, co-domain and range of R .
(iii) Depict the above relation by an arrow diagram.
23. Let $A=\{x, y, z\}$ and $B=\{1,2\}$. Find the number of relations from A to $B$.

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24. Let $A=\{1,2,3\}$ and $R=\{(1,2),(2,2),(3,1),(3,2)\}$. Show that R is a binary relation on A . Find its domoin and range.

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25. Let $N$ be the set of all natural numbers. Let $R=\{(a, b): a, b \in N$ and $2 a+b=10\}$. Show that R is a binary relation on N . Find its domain, range and co-domain.

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26. Let $A$ be the set of first ten natural number. Let $R$ be a binary relaion on A, defined by
$R=\{(a, b): a, b \in A$ and $a+2 b=10\}$.
Express R and $R^{-1}$ as sets of ordered pairs.
Show that (i) dom (R)=range $\left(R^{-1}\right)$ (ii) range $(R)=\operatorname{dom}\left(R^{-1}\right)$.

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27. Let $R$ be a relation on the set $Q$ of all rationals defined by $R=\{(a, b): a, b \in Q$ and $a-b \in Z\}$. Show that R is an equivalence relation.

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28. Let $n$ be a fixed positive integer. Define a relation $R$ on $Z$ as follows:
$(a, b) R a-b$ is divisible by $n$. Show that $R$ is an equivalence relation on $Z$.
29. Show that set of all parallel lines in any plane is an equivalence relation.

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30. Show that the relation is congruent to on the set of all triangles in a plane is an equivalence relation

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31. Let $R=\left\{(a, b): a, b \in N\right.$ and $\left.a=b^{2}\right\}$, Show that R satisfies none of reflexivity, symmetry and transitivity.

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32. Let a relation $R_{1}$ on the set R of real numbers be defined as $(a, b) \in R_{11}+a b>0$ for all $a, b \in R$. Show that $R_{1}$ is reflexive and
symmetric but not transitive.

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33. Prove that the relation R on the set $N x N$ defined by $(a, b) R(c, d) a+d=b+c$ for all $(a, b),(c, d) \in N x N$ is an equivalence relation.

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## Exercise 2 A

1. Find the values of $a$ and $b$, when:
(i) $(a+3, b-2)=(5,1)$
(ii) $(a+b, 2 b-3)=(4,-5)$
(iii) $\left(\frac{a}{3}+1, b-\frac{1}{3}\right)=\left(\frac{5}{3}, \frac{2}{3}\right)$
(iv) $(a-2,2 b+1)=(b-1, a+2)$
2. If A $\{0,1\}$ and $\mathrm{B}=\{1,2,3\}$, show that $A \times B \neq B \times A$.

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3. If $\mathrm{P}=\{\mathrm{a}, \mathrm{b}\}$ and $\mathrm{Q}=\{\mathrm{x}, \mathrm{y}, \mathrm{z}\}$, show that $P \times Q \neq Q \times P$.

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4. If $A=\{2,3,5\}$ and $B=\{5,7\}$, find:
(i) $A \times B$
(ii) $B \times A$
(iii) $A \times A$
(iv) $B \times B$
5. If $A=\{x \in N: x \leq 3\}$ and $B=\{x \in W, x<2\}$, find $(A \times B)$ and $(B \times A)$. Is $(A \times B)=(B \times A)$ ?

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6. If $A=\{1,3,5\}, B=\{3,4\}$ and $C=\{2,3\}$, verify that:
(i) $A \times(B \cup C)=(A \times B) \cup(A \times C)$
(ii) $A \times(B \cap C)=(A \times B) \cap(A \times C)$

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7. 

$A=\{x \in W: x<2\}, B=\{x \in N: 1<x \leq 4\}$ and $C=\{3,5\}$.
Verify that:
(i) $A \times(B \cup C)=(A \times B) \cup(A \times C)$
(ii) $A \times(B \cap C)=(A \times B) \cap(A \times C)$

Hint $A=\{0,1\}, B=\{2,3,4\}$ and $C=\{3,5\}$.
8. If $A \times B=\{(-2,3),(-2,4),(0,3),(0,4),(3,3),(3,4)\}$, find $A$ and $B$.

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9. Let $A=\{2,3\}$ and $B=\{4,5\}$. Find $(A \times B)$. How many subsets will $(A \times B)$ have?

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10. Let

$$
A \times B=\{(a, b): b=3 a-2\} .
$$

$(x,-5)$ and $(2, y)$ belong to $A \times B$, find the values of x and y .
11. Let A and B be two sets such that $n(A)=3$ and $n(B)=2$.

If $a \neq b \neq c$ and $(a, 0),(b, 1),(c, 0)$ are in $A \times B$, find A and B .

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12. Let $A=\{-2,2\}$ and $B=\{0,3,5\}$. Find : (i) $A \times B$ (ii) $B \times A$
(iii) $B \times B$ (iv) $A \times A$

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13. If $A=\{5,7\}$, find $(i) A \times A$ and (ii) $A \times A \times A$.

## - Watch Video Solution

14. Let $A=\{-3,-1\}, B=\{1,3\}$ and $C=\{3,5\}$. Find:
(i) $A \times B$
(ii) $(A \times B) \times C$
(iii) $B \times C$
$A \times(B \times C)$

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## Exercise 2 B

1. For any sets $A$ and $B$, prove that
$(A \times B) \cap(B \times A)=(A \cap B) \times(B \cap A)$.

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2. If $A$ and $B$ are nonempty sets, prove that
$A \times B=B \times A \Leftrightarrow A=B$.

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3. 

$A \times B \subseteq C \times D$ and $A \times B \neq \phi, \quad$ prove that $A \times C \subseteq B \times D$.

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4. If $A$ and $B$ be two sets such that $n(A)=3, n(B)=4$ and $n(A \cap B)=2$ then find:
(i)
$n(A \times B)$
(ii) $n(B \times A)$
$(i i i) n\{(A \times B) \cap(B \times A)\}$

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5. Sets $A$ and $B$ have $n$ elements in common. How many elements will $(A \times B)$ and $(B \times A)$ have in common?

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6. Let $A=\{1,2\}$ and $B=\{2,3\}$. Then, write down all possible subsets of $A \times B$.

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7. Let $A=\{a, b, c, d\}, B=\{c, d, e\}$ and $C=\{d, e, f, g\}$. Then verify each of the following identities:
(i) $A \times(B \cap C)=(A \times B) \cap(A \times C)$
(ii) $A \times(B-C)=(A \times B)-(A \times C)$
(iii) $(A \times B) \cap(B \times A)=(A \cap B) \times(A \cap B)$

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## Exercise 2 C

1. Let $A$ and $B$ be two nonempty sets.
(i) What do you mean by a relation from A to B ?
(ii) What do you mean by the domain and range of a relation?

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2. Find the domain and range of each of the relations given below:
(i) $R=\{(-1,1),(1,1),(-2,4),(2,4),(3,9)\}$
(ii) $R=\left\{\left(x, \frac{1}{x}\right): x\right.$ is an integer, $\left.0<x<5\right\}$
(iii) $R=\{(x, y): x+2 y=8$ and $x, y \in N\}$
(iv) $R=\{(x, y): y=|x-1|, x \in Z$ and $|x| \leq 3\}$

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3. Let $A=\{1,3,5,7\}$ and $B=\{2,4,6,8\}$.

Let $R=\{(x, y): x \in A, y \in B$ and $x>Y\}$.
(i) Write R in roster form.
(ii) Find dom (R) and range (R).
(iii) Depict R by an arrow diagram.

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4. If $R$ is a relation from set $A=\{2,4,5\}$ to set $B=\{1,2,3,4,6,8\}$ defined by $x R y \Leftrightarrow x$ divides $y$. Write $R$ as a set of ordered pairs Find the domain and the range of $R$.

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5. A relation $R$ is defined from a set $A=\{2,3,4,5\} \rightarrow a$ set $B=\{3,6,7,10\}$ as follows: $(x, y) \in R \Leftrightarrow x$ is relatively prime to $y$. Express $R$ as a set of ordered pairs and determine its domain and range.

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6. $A=\{1,2,3,5\}$ and $B=\{4,6,9\} A$ relation $R$ is defined from $A$ to $B$ by $R=\{$ $(\mathrm{x}, \mathrm{y})$ : the difference between x \& y is odd\}. Writer R in roster form.

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7. Let $R=\{(x, y): x+3 y=12, x \in N$ and $y \in N\}$.
(i) Write R in roster form.
(ii) Find dom (R) and range (R).

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8. Let $A=\{1,2,3,4,5,6\}$. Define a relation $R$ on set A by $R=\{(x, y): y=x+1\}$ Depict this relation using an arrow diagram Write down the domain, co domain and range of $R$.

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9. Determine the domain and range of the relation $R$ defined by $R=\{(x, x+5): x \in\{0,1,2,3,4,5\}\}$.

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10. Let $A=\{1,2,3,4,6\}$. Let R be the relation on A defined by $\{(a \dot{b}): a, b \in A$, bis exactly divisible by a\}.(i) Write R in roster form(ii) Find the domain of $R$ (iii) Find the range of $R$.

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11. Let R be the relation on Z defined by $R=\{(a, b): a, b \in Z$, $a b$ is an integer\}.Find the domain and range of R .

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12. If $R=\left\{(x, y): x^{2}+y^{2} \leq 4 ; x, y \in Z\right\}$ is a relation on $Z$, write the domain of $R$.

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13. Let $A=\{2,3\}$ and $B=\{3,5\}$.
(i) Find $(A \times B)$ and $n(A \times B)$.
(ii) How many relations can be defined from A to B ?

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14. Let $A=\{3,5\}$ and $B=\{7,9\}$.
$R=\{(a, b): a \in A, b \in B$ and $(a-b)$ is odd $\}$.
Show that $R$ is an empty relation from $A$ to $B$.
Hint The difference of two odd numbers cannot be odd.

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Exercise 2 D

1. Let $A$ and $B$ be two nonempty sets.
(i) What do you mean by a relation from A to B ?
(ii) What do you mean by the domain and range of a relation?

## (D) Watch Video Solution

2. Let $A=\{2,3,5\}$ and $R=\{(2,3),(2,5),(3,3),(3,5)\}$.

Show that R is a binary relation on A . Find its domain and range.

## (D) Watch Video Solution

3. 

Let
$A=\{0,1,2,3,4,5,6,7,8\}$ and let $R=\{(a, b): a, b \in A$ and $2 a+3 b$ Express $R$ as a set of ordered pairs. Show that $R$ is a binary relation on $A$.

Find its domain and range.

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4. If R is a binary relation on a set A , define $R^{-1}$ on A .

Let $R=\{(a, b): a, b \in W$ and $3 a+2 b=15\}$ where W is the set of whole numbers.

Express R and $R^{-1}$ as sets of ordered pairs. Show that (i) dom ( R )=range ( $R^{-1}$ ) (ii) range $(\mathrm{R})=\operatorname{dom}\left(R^{-1}\right)$.

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5. What is an equivalence relation?

Show that the relation of'similarity' on the set S of all triangle in a plane is an equivalence relation.

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6. Let $R=\{(a, b): a, b \in Z$ and $(a-b)$ is even $\}$.

Then, show that $R$ is an equivalence relation on $Z$.

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7. Let $A=\{1,2,3\}$ and $R=\left\{(a, b): a, b \in A\right.$ and $\left|a^{2}-b^{2}\right| \leq 5$.

Write $R$ as set of ordered pairs.

Mention whether R is (i) reflexive (ii) symmetric (iii) transitive.

Give reason in each case.

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8. 

$R=\{(a, b): a, b \in Z$ and $b=2 a-4\}$. If $(a,-2) \in R$ and $\left(4, b^{2}\right)$
Then, write the values of $a$ and $b$.

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9. If $R$ is a relation defined on the set $Z$ of integers by the rule $(x, y) \in R \Leftrightarrow x^{2}+y^{2}=9$, then write domain of $R$.

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10. Let $A$ be the set of first five natural numbers and let $R$ be a relationobn A defined as follows $(x, y) \in R \Leftrightarrow x \leq y$. Express
$R$ and $R^{-1}$ as sets of ordered pairs. Determine also The domain of $R^{-1}$ The range of $R$.

## - Watch Video Solution

11. A relation $R$ is defined on the set $Z$ of integers as: $(x, y) \in R x^{2}+y^{2}=25$. Express $\operatorname{Rand}^{-1}$ as the sets of ordered pairs and hence find their respective domains.

## - Watch Video Solution

12. Find $R^{-1}$, when
(i) $R=\{(1,2),(1,3),(2,3),(3,2),(4,5)\}$,
(ii) $R=\{(x, y): x, y \in N, x+2 y=8\}$.

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13. Let $A=\{a, b\}$. List all relations on A and find their number.

Hint $A \times A=\{(a, a),(a, b),(b, a),(b, b)\}$ and every subset of $A \times A$ is a relation on A .

So, their number $=2^{4}=16$.

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14. Let $R=\{(a, b): a, b \in N$ and $a<b\}$.

Show that R is a binary relation on N , which is neither reflexive nor symmetric. Show that R is transitive.

Hint Since $R \subset N \times N$, so it is a binary relation on $N$.

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## Exercise 2 E

1. Let $A$ and $B$ be two sets such that $n(A)=5, n(B)=3$ and $n(A \cap B)=2$.
(i)
$n(A \cup B) \quad(i i) n(A \times B) \quad(i i i) n\{(A \times B) \cap(B \times A)\}$
Hint (i) $n(A \cup B)=n(A)+n(B)-n(A \cap B)$.
(ii) $n(A \times B)=n(A) \cdot n(B)$
(iii) If $n(A \cap B)=m$ then $n\{(A \times B) \cap(B \times A)\}=2^{m}$.

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2. Find a and b when $(a-2 b, 13)=(7,2 a-3 b)$.

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3. If $A=\{1,2\}, \quad$ find $A \times A \times A$.

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4. If $A=\{2,3,4\}$ and $B=\{4,5\}$, draw an arrow diagram to represent $(A \times B)$.
5. If $A=\{3,4\}, B=\{4,5\}$ and $C=\{5,6\}$, find $A \times(B \times C)$.

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6. If $A \subseteq B, \quad$ prove that $A \times C=B \times C$.

## - Watch Video Solution

7. If $\operatorname{AandB}$ are any two non-empty sets, then prove that: $A \times B=B \times A A=B$.

## - Watch Video Solution

8. If $A=\{5\}$ and $B=\{5,6\}$ write down al possible subsets of $A \times B$.
9. Let $R=\left\{\left(x, x^{2}\right): x\right.$ is a prime number less than 10$\}$.
(i) Write R in roster form.
(ii) Find dom (R) and range (R).

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10. Let $A=\{1,2,3\}$ and $B=\{4\}$.

How many relations can be defined from A to B ?

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11. Let $A=\{3,4,5,6\}$ and $R=\{(a, b): a, b \in A$ and $a>b\}$.

Write R in roster form.

Find: dom ( R ) and range $(\mathrm{R})$.
Write $R^{-1}$ in roster form.
12. Let $R=\{(a, b): a, b \in N, a>b\}$.

Show that R is a binary relation which is neither reflexive, nor symmetric.
Show that R is transitive.

