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## MATHS

## BOOKS - RS AGGARWAL MATHS (HINGLISH)

## CONTINUITY AND DIFFERENTIABILITY

## Solved Examples

1. Draw the graph of each of the following canstant functions:
(i) $\mathrm{f}(\mathrm{x})=2$ for all $x \in R$
(ii) $\mathrm{f}(\mathrm{x})=0$ for all $x \in R$
(iii) $\mathrm{f}(\mathrm{x})=-2$ for all $x \in R$

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2. Draw the graphs of the linear funcations (i) $f(x)=1-x$ (ii) $f(x)=2 x+1$
3. Draw the graph of the identity function $f: R \rightarrow R: f(x)=x$ for all $x \in R$.

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4. Draw the graphs of the polynomial funcations
(i) $f(x)=x^{2}$ (ii) $f(x)=1-x^{2}$
(iii) $f(x)=x^{3}-x$

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5. Draw the graph of the modulus function, defined by
$f: R \rightarrow R: f(x)=|x|=\left\{\begin{array}{l}x, \text { when } x \geq 0 \\ -x, \text { when } x<0\end{array}\right.$

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6. Draw the graph of the reciprocal function $f(x)=\frac{1}{x}$

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7. Explain square root function with graph

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8. Draw the graph of the rational function $f(x)=\frac{x^{2}-1}{x-1}$

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9. Draw the graph of the step funcation $f(x)=[x]$.

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10. Draw the graph of the step funcation $f(x)=[x]$.
11. Draw the graph of the signum function
$f(x)=\left\{\begin{array}{lll}\frac{|x|}{x} & \text { when } & x \neq 0 \\ 0 & \text { when } & x=0\end{array}\right.$

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12. $\begin{array}{lll}\text { Draw } & \text { the } \quad \text { graph of the function } \\ f(x)\end{array}\left\{\begin{array}{lll}x^{2}, & \text { when } & x<0 \\ x, & \text { when } & 0 \leq x \leq 1 \\ 1 / x, & \text { when } & 1 \leq x<\infty .\end{array}\right.$

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13. Draw the graph of the function $f(x)=|x|+|x-1|$

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14. Draw the graph of the exponential funcation.
(i) $f(x)=2^{x}$ (ii) $f(x)=\left(\frac{1}{3}\right)^{x}$

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15. Draw the graphs of the logaritmic functhmic functions.
(i) $\log _{a} x$, whena $>1$ (ii) $\log _{a} x$, when $0<a<1$

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16. On the same draw the graphs of $e^{x}$ and $\log _{e} x$.

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17. show that $f(x)=x^{3}$ is contiuous at $\mathrm{x}=2$
18. Show that $f(x)=[x]$, is not continuous at $\mathrm{x}=\mathrm{n}$, where is an interger

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19. Show that the funcation $f(x)= \begin{cases}x, & \text { if } \mathrm{x} \text { is an intger } \\ 0, & \text { if } \mathrm{x} \text { is not an integer }\end{cases}$ is discontinuous at each integral value of x .

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20. Discuss the continuity of $f(x)=\left\{\begin{array}{ll}2 x-1 & x<0 \\ 2 x+1 & x \geq 0\end{array}\right.$ at $x=0$

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21. Show that the funcation $f(x)=\left\{\begin{array}{lll}3 x-2, & \text { when } & x \leq 0 \\ x+1, & \text { when } & x>0\end{array}\right.$ is discontinuous at $\mathrm{x}=0$

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22. Show that the function $f(x)=\left\{\begin{array}{lll}\frac{x}{|x|}, & \text { when } & x \neq 0 \\ 1, & \text { when } & x=0\end{array}\right.$ is discontinuous at $\mathrm{x}=0$

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23. Examine the continuity of the funcation
$f(x)= \begin{cases}\frac{|\sin x|}{x}, & x \neq 0 \\ 1, & x=0 \text { at } x=0\end{cases}$

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24. Show that the function $f(x)=2 x-|x|$ is continuous at $x=0$.

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25. Prove that $f(x)=\left\{\begin{array}{ll}|x|+3 & ; x \leq-3 \\ -2 x & ;-3<x<3 \\ 6 x+2 & ; x \geq 3\end{array}\right.$ is continuous at $x=-3$ and $x=3$.
26. If the function $f(x)=\left\{\begin{array}{l}k x+5, \text { when } x \leq 2 \\ x-1, \text { when } x>2\end{array}\right.$ is continuous at $\mathrm{x}=2$ then $\mathrm{k}=$ ?
A. $k=-1$
B. $k=-2$
C. $k=-3$
D. $k=-4$

## Answer: B

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27. Find the value of the constant $k$ so that the function given below is continuous at $x=0 . f(x)=\left\{\frac{1-\cos 2 x}{2 x^{2}}, x \neq 0 k, x=0\right.$
28. Find the values of $k$ for which $f(x)=\left\{\begin{array}{ll}\frac{1-\cos 4 x}{8 x^{2}} & \text { when } x \neq 0 \\ k & \text { when } x=0\end{array}\right.$ is continuous at $x=0$.

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29. 

Let
$f(x)=\left\{\frac{1-\cos 4 x}{x^{2}}, \quad\right.$ if $\quad x<0 a, \quad$ if $\quad x=0 \frac{\sqrt{x}}{\sqrt{16+\sqrt{x}}-4}$,
Determine the value of $a$ so that $f(x)$ is continuous at $x=0$.

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30. If the following function $f(x)$ is continuous at $x=0$, find the values of $a, b$ and $c$.
$f(x)=\left\{\begin{array}{cl}\frac{\sqrt{x+b x^{2}}-\sqrt{x}}{b x^{\frac{3}{2}}} & \text { if } x>0 \\ c & \text { if } x=0 \\ \frac{\sin (a+1) x+\sin x}{x} & \text { if } x<0\end{array}\right.$
31. If the function $f(x)$ given by $f(x)=\left\{\begin{array}{ll}3 a x+b & \text { if } x>1 \\ 11 & \text { if } x=1 \\ 5 a x-2 b & \text { if } x<1\end{array}\right.$ is continuous at $x=1$ then find the values of $a$ and $b$.
A. $a=5, b=2$
B. $a=4, b=3$
C. $a=2, b=1$
D. $a=3, b=2$

## Answer: D

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32. for what value of $k$ is the funcation.
$f(x)=\left\{\begin{array}{lll}k\left(x^{2}-2 x\right), & \text { if } & x \leq 0 \\ 4 x+1, & \text { if } & x>0\end{array}\right.$
(i) continuous at $\mathrm{x}=0$ ? (ii) continuous at $\mathrm{x}=1$ ?
(iii) continuous at $\mathrm{x}=-1$ ?

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33. If the function $f(x)=\left\{\begin{array}{cl}\frac{\sin ^{2} a x}{x^{2}}, & \text { when } x \neq 0 \\ \mathrm{k}, & \text { when } x=0\end{array}\right.$ is continuous at $\mathrm{x}=$ 0 then $\mathrm{k}=$ ?

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34. If the function $f(x)=\frac{(3 x+4 \tan x)}{x}$ continuous at $\mathrm{x}=0$ ? If not, hwo may the funcation be defined to make it continuous at this point?

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35. Show that the function $f(x)$ given by

$$
f(x)=\left\{\frac{e^{1 / x}-1}{e^{1 / x}+1}, \text { when } x \neq 00, \quad \text { when } x=0\right.
$$

discontinuous at $x=0$.
36. Let $f(x)=\left\{\begin{array}{lll}x & \text { if } & x \geq 1 \\ x^{2} & \text { if } & x<1\end{array}\right.$ is f a continuous function ? Why ?

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37. Prove that $f(x)=|x|$ is continuous at $x=0$.

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38. Discuses the continity of the funcation
$f(x)=\left\{\begin{array}{lll}2 x-1, & \text { if } & x<0 \\ 2 x+1, & \text { if } & x \geq 0\end{array}\right.$

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39. Discuss the continuity of the function
$f(x)=\left\{\begin{array}{lll}\frac{\sin x}{x}, & \text { if } & x<0 \\ (x+1), & \text { if } & x \geq 0\end{array}\right.$

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40. Find all points of discontinuity of $f$, where $f$ is defined by $f(x)=\left\{\frac{|x|}{x}, \quad\right.$ if $x \neq 00, \quad$ if $x=0$

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41. prove that $f(x)$ is a continuous funcation where $f(x)\left\{\begin{array}{lll}\frac{x^{4}-16}{x-2}, & \text { if } & x \neq 2 \\ 32, & \text { if } & x=2\end{array}\right.$

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42. Determine the value of the constant $k$ so that the function $f(x)=\left\{k x^{2}, \quad\right.$ if $x \leq 23, \quad$ if $x>2$ is continuous.

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43. If $f(x)=1$ if $x<3$; $a x+b$ if $3<x<5$ and 7 if $x>5$ Then find the values of $a$ and $b$ for which $f(x)$ is continuous function
44. Show that the function $f(x)=\sqrt{x^{4}+3}$ is continuous at each point.

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45. Show that the function $f(x)=|\sin x+\cos x|$ is continuous at $x=\pi$

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46. Show that $f(x)=x^{2}$ is differentiable at $x=1$ and find $f^{\prime}(1)$.

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47. Show that $f(x)=[x]$ is not differentiable at $x=1$.
48. (i) Show that $f(x)=x^{4 / 3}$ is differentiable at $x=0$, and hence find $f^{\prime}(0)$.
(ii) Show that $g(x)=x^{3 / 2}$ is not differentiable at $x=0$

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49. 

Show
tha the
function
$f(x)=\{(1+x$, if $x \leq 2),,(5-x$, if $x>2)$ is not differentiable at $x=2$.

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50. Let $f(x)=\left\{\begin{aligned} &(1+\sin x), \text { when } 0 \leq x<\frac{\pi}{2} \\ & 1, \text { when } \\ & x<0\end{aligned}\right.$

Show that $f^{\prime}(0)$ does not exist.

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51. Let $f(x)=m x+c$ and $f(0)=f^{\prime}(0)=1$. Find $f(2)$.

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## 52.

Show
that
the
function
$f(x)=\left\{x \frac{\sin 1}{x}\right.$, when $x \neq 00 \quad$ when $x=0$ is continuous but not differentiable at $x=0$.

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53. Show that $f(x)=|x-2|$ is continuous but not differentiable at $x=2$.

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1. Show that $f(x)=x^{2}$ is continuous at $\mathrm{x}=2$ lt

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2. Show that $f(x)=\left(x^{2}+3 x+4\right)$ is continuous at $\mathrm{x}=1$

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3. Prove that $f(x)=\left\{\frac{x^{2}-x-6}{x-3}\right.$ when $x \neq 3 ; 5$ when $x=3$, is continuous at $\mathrm{x}=3$.

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4. $f(x)=\left\{\begin{array}{ll}\frac{x^{2}-25}{x-5}, & \text { when } x \neq 5 \\ 10, & \text { when } x=5\end{array}\right.$ is continuous at $\mathrm{x}=5$

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5. $f(x)=\left\{\begin{array}{ll}\frac{\sin 3 x}{x}, & \text { when } x \neq 0 \\ 1, & \text { when } x=0\end{array}\right.$ is discontinuous at $\mathrm{x}=0$.

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6. Let $f(x)=\left\{\frac{1-\cos x}{x^{2}} 1\right.$. Show that $f(x)$ is discontinuous at $x=0$.

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7. $f(x)=\left\{\begin{array}{ll}2-x, & \text { when } x<2 \\ 2+x, & \text { when } x \geq 2\end{array}\right.$ is discontinuous at $\mathrm{x}=2$

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8. $f(x)=\left\{(3-x\right.$, , when, $x \leq 0),,\left(x^{2}\right.$, when, $\left.x>0\right)$ is discontinuous at $x=0$

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9. Show that $\mathfrak{f}(x)=\{5 x-4, \backslash \backslash \backslash w h$ e $n \backslash 0$

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10. $f(x)=\{x-1$, when $1 \leq x<2 ; 2 x-3$, when $2 \leq x \leq 3$ is continuous at $x=2$.

## - Watch Video Solution

11. 

$$
f(x)=\{(\cos x, \text {, when, } x \geq 0,),(-\cos x, \text { when, } x<0)
$$

discontinuous at $\mathrm{x}=0$

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12. Show that $f(x)=\left\{\frac{|x-a|}{x-a}\right.$, when $x \neq a 1$, when $x=a$ is discontinuous at $x=a$
13. 

$f(x)=\{(-x$, when, $x<0),,(1$, when, $x=0),(x$, , when, $x>0)$ is discontinuous at $\mathrm{x}=0$

## - Watch Video Solution

14. If $f(x)=\left\{\sin \left(\frac{1}{x}\right), x \neq 00, x=0\right.$ then it is discontinuous at-

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15. $f(x)=\left\{(2 x\right.$, , when, $x<0),,(2$, , when, $x=2),\left(x^{2}\right.$, , when, $\left.x>2\right)$ is discontinuous at $\mathrm{x}=0$

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16. 

$f(x)=\{(-x$, when, $x<0),,(1$, , when, $x=0),(x$, , when, $x>0)$ is discontinuous at $\mathrm{x}=0$

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17. Determine the value of the constant $k$ so that the function
$f(x)=\left\{\begin{array}{ll}\frac{\sin 2 x}{5 x} & \text { if } x \neq 0 \\ k & \text { if } x=0\end{array}\right.$ is continuous at $x=0$.
A. $k=\frac{2}{5}$
B. $k=\frac{3}{5}$
C. $k=\frac{4}{5}$
D. $k=\frac{1}{5}$

## Answer: A

18. Find the value of k for which
$f(x)=\left\{\left(\frac{x^{2}-2 x-3}{x+1}\right.\right.$, when, $\left.x \neq-1,\right),(\lambda$, when, $x=-1)$ is continuous at $\mathrm{x}=-1$

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19. For what value of $k$ is the following function continuous at $x=2$ ?
$f(x)=\{2 x+1 ; x<2 k ; x=23 x-1 ; x>2\}$

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20. Determine the value of $k$ for which the following function is continuous at $x=3$. $f(x)=\left\{\frac{x^{2}=9}{x-3}, x \neq 3 k, x=3\right.$

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21. Find the value of $k$ so that the function $f$ defined by $f(x)=\left\{\begin{array}{l}\frac{k \cos x}{\pi-2 x}, \text { for } x \neq \frac{\pi}{2} \\ 3, \text { for } x=\frac{\pi}{2}\end{array}\right.$ is continuous at $x=\frac{\pi}{2}$
A. $k=6$
B. $k=5$
C. $k=4$
D. $k=3$

## Answer: $A$

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22. If $f(x)=x^{2} \sin ^{\prime} \frac{1}{x}$, where $x \neq 0$, then the value of the function f at $x=0$, so that the function is continuous at $x=0$ is

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23. Show that $f(x)=\left((x+1,, \quad\right.$ if $x \leq 2),\left(x^{2}+1\right),, \quad$ if $\left.\left.\quad x<1\right):\right\}$ is continuous at $\mathrm{x}=1$

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24. Show that $f(x)=\left\{\begin{array}{lll}x^{3}-3, & \text { if } & x \leq 2 \\ x^{2}+1, & \text { if } & x>2\end{array}\right.$ is continuous at $\mathrm{x}=2$

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25. If the function $f(x)= \begin{cases}5, & x \leq 2 \\ a x+b, & 2<x \leq 10 \\ 21, & x>10\end{cases}$
continuous, find the values of $a$ and $b$

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26. Find the value of ' $a$ ' for which the function $f$ defined as

$$
f(x)=\left\{\begin{array}{ll}
a \sin \left(\frac{\pi}{2}(x+1)\right) & x \leq 0 \\
\frac{\tan x-\sin x}{x^{3}} & x>0
\end{array} \text { is continuous at } x=0\right.
$$

27. Show that the function $f(x)=|x-3|, x \in \mid R$, is continuous but not differentiable at $x=3$.

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## Exercise 9 B

1. Show that the function $f(x)=\left\{\begin{array}{l}7 x+5, x \geq 0, \\ 5-3 x, x<0\end{array}\right.$ is a continuous function.

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2. Show that the funcation $f(x)=\left\{\begin{array}{lll}\sin x, & \text { if } & x<0 \\ x \mathrm{lt} & \text { if } & x \geq 0\end{array}\right.$ is continuous.
3. Show that the function $f(x)=\left\{\begin{array}{ll}\frac{x^{n}-1}{x-1}, & \text { when } x \neq 1 \\ n, & \text { when } x=1\end{array}\right.$ is continuous.

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4. Show that the $\sec x$ is a continuous function.

## D Watch Video Solution

5. Show that $\cos x$ is a continuous function

## - Watch Video Solution

6. Show that the function $f(x)=\left\{\begin{array}{ll}\frac{\sin x}{x} & \text { whenx } \neq 0 \\ 2 & \text { whenx }=0\end{array}\right.$ is continuous at each point except 0.

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7. Discuss the continuity of $f(x)=[x]$

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8. show that $f(x)=\left\{\begin{array}{lrr}(2 x-1), & \text { if } & x<2 \\ \frac{3 x}{2} & & \text { if } x \geq 2\end{array}\right.$ is continuous

## - Watch Video Solution

9. Show that $f(x)=\left\{\begin{array}{lll}x, & \text { if } & x \neq 0 \\ 1, & \text { if } & x=0\end{array}\right.$ is continuous at each point except 0.

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10. Locate the point of discontinuity of the function.
$f(x)=\left\{\begin{array}{llc}\left(x^{3}-x^{2}+2 x-2\right), & \text { if } & x \neq 1 \\ 4, & \text { if } & \text { if }=1\end{array}\right.$
11. Discuss the continuity of the function $f(x)=|x|+|x-1|$ in the interval [ -1,2]

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## Exercise 9 C

1. Show that $f(x)=x^{3}$ is continuous as well as differentiable at $\mathrm{x}=3$

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2. Show that $f(x)=(x-1)^{\frac{1}{3}}$ is not differentiable at $x=1$.

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3. show that a constant function is always differentiable.
4. Show that $f(x)=|x-5|$ is continuous but not differentiable at $x=5$.

## - Watch Video Solution

5. Let $f(x)= \begin{cases}(2 x-1), & \text { when } x \geq 1 \\ x, & \text { when } 0 \leq x \leq 1\end{cases}$

Show that $\mathrm{f}(\mathrm{x})$ is continuous but not differentiable at $\mathrm{x}=1$

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6. show that $\mathrm{f}(\mathrm{x})=|\mathrm{x}|$ is continuous but not differentiable at $\mathrm{x}=0$

## - Watch Video Solution

7. Show that the function $f(x)=\left\{\begin{array}{ll}1-x, & x<1 \\ x^{2}-1, & x \geq 1\end{array}\right.$ is continuous but not differnetiable at $\mathrm{x}=1$

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8. Let $f(x)=\left\{\begin{array}{lll}(2+x), & \text { if } & x \geq 0 \\ (2-x), & \text { if } & x<0\end{array}\right.$ show that $\mathrm{f}(\mathrm{x})$ not derivable at x $=0$

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9. Find the values of $a$ and $b$ so that the function $f(x)=\left\{x^{2}+3 x+a, b x 2\right.$, if $x \leq 1$ if $x>1$ is differentiable at each $x R$.
