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India's Number 1 Education App

## MATHS

## BOOKS - ZEN MATHS (KANNADA

## ENGLISH)

## ARITHMETIC PROGRESSIONS

## Illustrative Examples

1. Which of the following forms an A.P.?

$$
\text { a] } 5 \frac{1}{2}, 9 \frac{1}{2}, 13 \frac{1}{2}, 17 \frac{1}{2}, \ldots
$$

b] $\sqrt{3}, \sqrt{12},, \sqrt{27}, \sqrt{48}, \ldots$
c] $13,10,7,5 \ldots$

## D Watch Video Solution

2. Write the first 4 terms of an A.P. Where $a_{n}=4 n+3$.

## - Watch Video Solution

3. Write the next three terms of the A.P.
$(a+b),(a+1)+b,(a+1)+(b+1)$.

- Watch Video Solution

4. For the A.P $\frac{3}{2}, \frac{1}{2}, \frac{-1}{2}, \frac{-3}{2}, \ldots$ write the first term and common difference.

## - Watch Video Solution

5. The first three terms of an A.P. are $3 y-1,3 y+5$, and $5 y+1$. Find y .

## - Watch Video Solution

## 6. Is $\sqrt{3}, \sqrt{6}, \sqrt{9}, \sqrt{12}$ an A.P.? Give reason.

## D Watch Video Solution

7. What is the next term of the A.P.?
$\sqrt{7}, \sqrt{28}, \sqrt{63}, \ldots$

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To Find The Nth Term Of An A P Illustrative Examples

1. How many two digit numbers are divisible by $3 ?$

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2. If the nth term of the A.P. $-1,4,914, \ldots$ is

129 ,find the value of ' $n$ '.

## - Watch Video Solution

3. Write the nth term of the A.P.
$\frac{1}{m}, \frac{1+m}{m}, \frac{1+2 m}{m}, \ldots$
4. What is the common difference of an A.P. in which $a_{12}-a_{8}=24$ ?

## D Watch Video Solution

5. The fourth and eight terms of an A.P. are in
the ratio of $1: 2$ and tenth term is 30 . Find the common difference.

D Watch Video Solution
6. Find the three numbers of A.P. whose sum is

12 and product is 48.

## D Watch Video Solution

7. The 10th term of an A.P. is $(-4)$ and the
$22 n d$ term is $(-16)$. Find the 38 th term.

- Watch Video Solution

8. The angles of a triangle are in A.P. The greatest angle is twice the least. Find all the angles of the triangle.

## D Watch Video Solution

9. Find the sum of all 3 digit naturals which are divisible by 9.

D Watch Video Solution
10. Find the common difference of an A.P.
whose first term is $\frac{1}{2}$ and the 8 th term is $\frac{17}{6}$.
Also write its 4th term.

## D Watch Video Solution

11. In an A.P., 7 times the 7 th term is equal to 11
times 11th term. Find the 18 th term of the A.P.

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## Arithmetic Series Illustrative Examples

1. Find the sum of all two digit natural numbers which when divided by 3 yield 1 as remainder.

## D Watch Video Solution

2. Find the number of terms of the A.P. 54, 51,

48, .... So that their sum is 513.
3. How many three digit numbers are divisible by 7 ?

D Watch Video Solution
4. The sums of $n, 2 n, 3 n$ terms of an $A . P$.
are $S_{1}, S_{2}, S_{3}$ respectively.
Prove that : $S_{3}=3\left(S_{2}-S_{1}\right)$

D Watch Video Solution
5. If the $p^{t h}$ term of an A.P. is $\frac{1}{q}$ and $q^{\text {th }}$ term is
$\frac{1}{p}$, show that the sum of $p q$ terms is $\frac{(p q+1)}{2}$

## - Watch Video Solution

6. The sum of the first 8 terms of an A.P. is 100
and the sum of its first 19 terms is 551 . Find
the first term and the common difference of the AP.

## Textual Exercise Exercise 11

1. In which of the following situations, does
the list of numbers involved make arithmetic progression, and why ?

The taxi fare after each km when fare is Rs. 15
for the first km and Rs. 8 for each additional km.

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2. Write first four terms of the AP, when the
first term a and the common difference $d$ are given as follows:
(i) $a=10, d=10$
(ii) $a=-2, d=0$
(iii) $\mathrm{a}=4, \mathrm{~d}=-3$
(iv) $a=-1, d=\frac{1}{2}$
(v) $a=-1.25, d=-0.25$

- Watch Video Solution

3. For the following A.P.S, write the first term and the common difference.
i] $3,1,-1,-3, \ldots$
ii] $-5,-1,3,7, \ldots$
iii] $\frac{1}{3}, \frac{5}{3}, \frac{9}{3}, \frac{13}{3}, \ldots$. iv] $0.6,1.7,2.8,3.9, .$.

## - Watch Video Solution

4. Which of the following are APs? If they form
an AP, find the common difference $d$ and write
three more terms.

## 2,4,8,16,...

## D Watch Video Solution

## Textual Exercise Exercise 12

1. Fill in the blanks in the following table, given
that $a$ is the first term, $d$ the common
difference and $a_{n} n^{\text {th }}$ term of the AP:

| (i) | $a$ | $d$ | $n$ | $a_{n}$ |
| :--- | :---: | :---: | :---: | :---: |
|  | 7 | 3 | 8 | $\ldots$ |
|  | -18 | $\ldots$ | 10 | 0 |
| (iv) | -18.9 | 2.5 | $\ldots$ | -5 |
| (v) | 3.5 | 0 | 105 | 3.6 |

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## 2. Find the

(i) 30th term of the AP 10,7,4,...
(ii) 11th term fo the AP: $-3,-\frac{1}{2}, 2 \ldots \ldots$.

## - Watch Video Solution

3. In the following AP's find the missing terms in the boxes.
(i) $2 . \quad, \quad, \quad 26$

Let the missing term bex.
(ii)


13,

(iii) 5,

$(i v)-4$, $\qquad$ , --_-...
,-.-....., 6' ,6.


- Watch Video Solution

4. Which term of the AP : $3,8,13,18, .$. is 78 ?

## D Watch Video Solution

5. Find the number of terms in each of the following A.Ps.
(i) $7,13,19, \ldots, 205$
(ii) $18,15 \frac{1}{2}, 13, \ldots,-47$

## - Watch Video Solution

6. Check whether -150 is a term of the AP : 11,8 ,

5, 2
7. Find the $31^{\text {th }}$ term of an AP whose $11^{\text {th }}$ term is 38 and the 16th term is 73.

- Watch Video Solution

8. An A.P. consists of 50 terms of which the 3rd term is 12 and the last term is 106 . Find the 29th term.

# 9. If the 3 rd and 9 th term of an A.P. are 4 and -8 

 respectively, which term is zero?- Watch Video Solution

10. The $17^{\text {th }}$ term of an AP exceeds its $10^{\text {th }}$ term by 7. Find the common difference.

- Watch Video Solution

11. Which term of the AP: $3,15,27,39, \ldots$. Will be 132 more than its $54^{\text {th }}$ term ?

## D Watch Video Solution

12. Two APs have the same common difference.

The difference between their $100^{\text {th }}$ terms is

100, what is the difference between their $1000^{\text {th }}$ terms ?
13. How many 3-digit numbers are divisible by
$7 ?$

## - Watch Video Solution

14. How many multiples of 4 lie between 10 and 250 ?

## - Watch Video Solution

15. For what values of ' $n$ ' are the $n$th terms of
A.Ps. $\quad 63,65,67, \ldots$ and $3,10,17, \ldots$ are equal?

## D Watch Video Solution

16. Determine the AP whose third term is 16 and the 7th term exceeds the 5th term by 12.

D Watch Video Solution
17. Find the $20^{\text {th }}$ term from end of the sequence 3,8,13 ...... 253.

## D Watch Video Solution

18. The sum of the $4^{\text {th }}$ and $8^{\text {th }}$ terms of an AP is 24 and the sum of the $6^{\text {th }}$ and $10^{\text {th }}$ terms is 44 .

Find the first three terms of the AP.

## D Watch Video Solution

19. Subba Rao started work in 1995 at an annual salary of Rs. 5000 and received an increment of Rs. 200 cash year. In which year did this income reach Rs. 7000 ?

## D Watch Video Solution

20. Ramkali saved Rs. 5 in the first week of a
year and then increased her weekly savings by
Rs. 1.75 . If in the $n^{\text {th }}$ week, her weekly savings
become Rs. 20.75, find $n$.

## Textual Exercise Exercise 13

1. Find the sum of the following Aps:
(i) 2, 7, 12, ........, to 10 terms.
(ii) $-37,-33,-29, \ldots . . . . .$, , to 12 terms.
(iii) 0.6, 1.7, 2.8,....., to 100 terms
(iv) $\frac{1}{15}, \frac{1}{12}, \frac{1}{10}, \ldots \ldots$, ,to 11 terms
2. Find the sums given below:
$7+10 \frac{1}{2}+14+\ldots+84$.

## D Watch Video Solution

## 3. In an A.P:

(i) Given $a=5, d=3, a_{n}=50$, find n and $S_{n}$.
(ii) Given $a=7, a_{13}=35$, find 'd' and $S_{13}$.
(iii) Given $a_{12}=37, d=3$, find a and $S_{12}$.
(iv) Given $a_{3}=15, S_{10}=125$, find 'd' and $a_{10}$.
(v) Given $d=5, S_{9}=75$, find 'a' and $a_{9}$.
(vi) Given $a=2, d=8, S_{n}=90$, find ' n ' and $a_{n}$.
(vii) Given $a=8, I=a_{n}=62, S_{n}=210$, find ' n ' and ' d '.
(viii) Given $a_{n}=4=I, d=2, S_{n}=-14$,
find ' $n$ ' and 'a'.
(ix) Given $a=3, n=8, S_{n}=192$, find 'd'.
(x) Given $I=28, S_{n}=144$, and there are a total 9 terms find 'a' .
4. How many terms of the A.P : $9,1725, \ldots$ must be taken to give sum of 636 ?

## D Watch Video Solution

5. The first of an A.P is 5 , the last term is 45 and the sum is 400 . Find the number of terms and the common difference.

## D Watch Video Solution

6. The first and the last terms of an A.P are 17 and 350 respectively. If the common difference
is 9 , how many terms are there and what is
their sum ?

## - Watch Video Solution

7. Find the sum of first 22 terms of an A.P in which $\mathrm{d}=7$ and 22 nd term is 149 .
8. Find the sum of first terms of an A.P whose second and third terms are 14 and 18 respectively.
( Watch Video Solution
9. If the sum of first 7 terms of an A.P is 49 and
that of 17 terms is 289 , find the sum of first $n$
terms.

- Watch Video Solution

10. Show that $a_{1}, a_{2}, \ldots, a_{n}, \ldots$ form an A.P
where an is defined as below : (i) $a_{n}=3+4 n$
(ii) $a_{n}=9-5 n$.

Also find the sum of the first 15 terms in each case.

## - Watch Video Solution

11. If the sum of the first $n$ terms of an A.P. is
$4 n-n^{2}$ what is the first term? What is the sum of the first two terms? What is the second term? Find the 3rd, 10th, and the nth terms.
12. Find the sum of the first 40 positive integers divisible by 6 .

## - Watch Video Solution

13. Find the sum of the first 15 multiples of 8.

- Watch Video Solution

14. Find the sum of the odd numbers between 0 and 50.

## D Watch Video Solution

15. A contract on construction job specific a penalty for delay of completion beyond a certain date as follows : Rs. 200 for the first day, Rs. 250 for the second day, Rs. 300 for the third day, etc., the penalty for each succeeding day being Rs. 50 more than for the preceding
day. How much money the contractor has to
pay as penalty, if he has delayed the work by 30 days?

## D Watch Video Solution

16. A sum of Rs. 700 to be used to give seven
cash prizes to students of a school for thir overall academic performance. If each prize is

Rs. 20 less than its preceding prize, find the value of each of the prizes.
17. In a school, students thought of planting trees in an around the school to reduce air pollution. It was decided that the number of trees, that each section of each class will plant, will be the same as the class. In which they are studying e.g., a section of Class I will plant 1 tree, a section of Class II will plant 2 trees and so on till Class XII. There are three sections of each class. How many trees will be planted by the students?
18. A spiral is made up of successive semicircles, with centres alternately at $A$ and $B$, starting with centre at $A$, of radii $0.5 \mathrm{~cm}, 1.0$ $\mathrm{cm}, 1.5 \mathrm{~cm}, 2.0 \mathrm{~cm}, . .$. as shown in Fig. 54. What is the total length of such a spiral made up to thirteen consecutive semicircles ? (Take $\pi=\frac{22}{7}$ )

19. 200 logs are stacked in the following manner : 20 logs in the bottom row, 19 in the next row, 18 in the row next to it and so on. In how many rows are the 200 logs placed and how many logs are in the top row?

## D Watch Video Solution

20. In a potato race, a bucket is placed at the starting point, which is 5 m from the first
potato, and the other potatoes are placed 3 m apart in a straight line. There are ten potatoes in the line (fig.).

Quman
A competitor starts from the bucket, picks up
the nearest potato, runs back with it, drops it
in the bucket, runs back to pick up the nest potato, runs to the bucket to drop it in, and she continues in the same way until all the potatoes are in the bucket. What is the total distance the competitor has to run ? [Hint : To pick up the first potato and the second potato,
the total distance (in metres) run by $a$ competitor is $2 \times 5+2 \times(5+3)$ ]

## - Watch Video Solution

## Textual Exercise Exercise 14

1. Which term of the A.P.: $121,117,113, \ldots$. is its first negative term?
2. The sum of the third and the seventh terms of an A.P. is 6 and the product is 8 . Find the sum of first sixteen terms of the A.P.

## D Watch Video Solution

3. A tadcler has rungs 25 cm apart. The rungs
decrease uniformly in length from 45 cm at the bottom to 25 cm at the top. If the top and the bottom runs are $2 \frac{1}{2} \mathrm{~m}$ apart, what is length of the wood required for the rungs?
4. The houses of a row are numbered consectively from 1 to 49 . show that there is a value of $x$ such that the sum of the houses preceding the house numbered x is equal to the sum of the numbers of the houses following it. Find this value of $x$.
5. A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid concrete.

Each stop has a rise of $1 / 2 \mathrm{~m}$ and a tread of
$1 / 2 \mathrm{~m}$ calculate the total volume of concrete required to build the terrace.

D Watch Video Solution

Zen Additional Questions Multiple Choice
Questions Mcqs

1. The first $n^{t h}$ term of a AP is given by
A. $a_{n}=a+n d$
B. $a_{n}=a+(n-1) d$
C. $a_{n}=a-(n-1) d$

$$
\text { D. } a_{n}=2 a+(n-1) d
$$

Answer: B

# 2. The $7^{\text {th }}$ term of the AP $3,6,9, \ldots$ is given by 

A. 21
B. 14
C. 28
D. 30

Answer: A
3. The sum of to $n$ terms of AP $1+3+5 \ldots .$.
is given by

> A. $2 n^{2}+1$
> B. $n^{2}$
> C. $2 n^{2}-1$
> D. $3 n+1$

Answer: B

D Watch Video Solution
4. For any arithmetic progression, $a_{n}$ is equivalent to
A. $S_{n}-S_{n+1}$
B. $S_{n+1}-S_{n}$
C. $S_{n+1}-S_{n-1}$
D. $S_{n}-S_{n-1}$

Answer: D

D Watch Video Solution
5. The next two terms of $\sqrt{2}, \sqrt{8}, \sqrt{18}, \ldots$. are

> A. $\sqrt{32}, \sqrt{50}$
> B. $\sqrt{8}, \sqrt{10}$
> C. $\sqrt{32}, \sqrt{10}$
> D. $\sqrt{32}, \sqrt{12}$

Answer: A
( Watch Video Solution
6. The first term of an AP is a and the $n^{\text {th }}$ term
is b , the $d=$

$$
\begin{aligned}
& \text { A. } \frac{a-b}{n} \\
& \text { B. } \frac{b-a}{n} \\
& \text { C. } \frac{b-a}{n-1} \\
& \text { D. } \frac{b-a}{n+1}
\end{aligned}
$$

Answer: C

- Watch Video Solution


## 7. What is the formula to find the sum of AP to

 $n$ terms?$$
\begin{aligned}
& \text { А. } S_{n}=\frac{n}{2}[a+(n-1) d] \\
& \text { B. } S_{n}=\frac{n}{2}[2 a+n d] \\
& \text { С. } S_{n}=\frac{n}{2}[a+(n+1) d] \\
& \text { D. } S_{n}=\frac{n}{2}[2 a+(n-1) d]
\end{aligned}
$$

## Answer: D

## D Watch Video Solution

8. In an AP, $S_{n}=3 n+5$ then, the value of $d$ is:
A. 3
B. 5
C. -5
D. 8

Answer: C

- Watch Video Solution

9. For an AP, the correct statement among the
following is:
A. $S_{3}=S_{2}+d$
B. $S_{3}=S_{2} \times d$
C. $S_{3}=S_{2}+a_{2}$
D. $S_{3}=S_{2}+a_{3}$

Answer: D

D Watch Video Solution
10. In an AP, the seventh term is 4 and the common difference is -4 . Which is the first term?
A. 18
B. 12
C. 28
D. 20

## Answer: C

11. $2 m, m+10$ and $3 m+2$ form the terms of an AP, then the value of $m$ is:
A. 6
B. -6
C. 21
D. 15

Answer: A
( Watch Video Solution
12. The angles of quadrilateral are in the ratio
$3: 5: 9: 13$. Find all the angles of the quadrilateral.
A. $60^{\circ}, 20^{\circ}$
B. $100^{\circ}, 40^{\circ}$
C. $120^{\circ}, 60^{\circ}$
D. $90^{\circ}, 30^{\circ}$

Answer: C

- Watch Video Solution

13. Which term of the AP $3,8,13,18, \ldots$ is 258 ?
A. 36
B. 52
C. 24
D. 50

Answer: B
14. If the $59^{\text {th }}$ term of an AP is 449 and $449^{\text {th }}$ term is 59 , then

$$
\text { A. } a_{501}=0
$$

B. $a_{508}=0$
C. $a_{502}=0$
D. $a_{509}=0$

## Answer: D

D Watch Video Solution
15. If the $n-t h$ term of an arithmetic progression $a_{n}=24-3 n$ then its $2 n d$ term is
A. 18
B. 15
C. 0
D. 2

Answer: A
16. If the $n$-th term of an arithmetic progression is $5 n+3$, then 3 rd term of the arithmetic progression is
A. 11
B. 18
C. 12
D. 13

Answer: B

- Watch Video Solution

17. In an arithmetic progression, if $a=2 n+1$,
then the common difference of the given progression is
A. 0
B. 1
C. 2
D. 3

Answer: C

- Watch Video Solution


## Zen Additional Questions Very Short Answer Vsa

 Questions1. Find ' $d$ ' in the following arithmetic progressions:
i] 2, 5, 8, 11, 14
ii] $-3,-1,1,3, \ldots . .$.
iii] $0,-8,-16, \ldots . .$.
iv] $\frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \ldots$.

- Watch Video Solution


## 2.

a] first term is 0 and common difference 3
b] first term is -3 and common difference -1
c] first term is 4 and common difference -2 .

## D Watch Video Solution

3. Express these terms of an A.P. in terms of
' $a$ ' and 'd'.

## - Watch Video Solution

4. Write the next three terms of the given arithmetic progression:
i] $3,-2,-7, \ldots .$.
ii] $0,5,10, \ldots$.
iii] $119,136,157, \ldots$..

## - Watch Video Solution

5. If $a=5, d=2$, find
i] $T_{5}$ ii] $T_{10}$ iii] $T_{100}$

- Watch Video Solution

6. Write the common difference of the arithmetic progression whose nth term is
a] $n^{2}+5$
b] $2 n^{2}-6$

- Watch Video Solution

7. Find the 10 th term of an arithmetic progression whose first term is ' d ' and common difference is ' b '.
8. What is common difference of an AP in which $a_{21}-a_{7}=84$ ?

- Watch Video Solution

9. For what value of $k$ will
$k+9,2 k-1,2 k+7$ be consecutive terms of a AP.
10. Find the sum of first twenty terms of Arithmetic series $2+7+12+\cdots$ using suitable formula.

## D Watch Video Solution

11. Write the formula to find the sum of first $n$ terms of an Arithmetic progression, whose first term is a and the last term is $a_{n}$.

## D <br> Watch Video Solution

## Zen Additional Questions Short Answer Sa Type 1

## Questions

1. Write the $n^{\text {th }}$ term of the AP:
a] $13,8,3,-2, \ldots$.
b] $\sqrt{2}, 3 \sqrt{2}, 5 \sqrt{2}, \ldots .$.
c] $121,117,113, \ldots$.
d] $\frac{3}{4}, \frac{5}{4}, \frac{7}{4}, \ldots$.
e] $-15,-10,-5,0, \ldots \ldots$.

- Watch Video Solution

2. Which term of the AP
a] $2,5,8, \ldots$. is 68 ?
b] $-3,-5,-7, \ldots$. is -101 ?
c] $21,42,63, \ldots \ldots$. is 420 ?
d] $80,76,72, \ldots \ldots$ is 0 ?

- View Text Solution

3. Check whether
a] -1 is a term of $33,31,29, \ldots \ldots$. .
b] 54 is a term of $3,9,15, \ldots \ldots \ldots$.
c] -10 is a term of $-3,-5,-7, \ldots \ldots$

D Watch Video Solution
4. The 10th term of $A P$ is 41 and 18 th term is
73. Find the 26th term.

## - Watch Video Solution

5. The 7th term of an AP is 32 and 13th term is 62. Find the progression.
6. In an AP, the 6th term is 12 and 8th term is
7. Find the nth term.

- Watch Video Solution

7. Which term of the AP 5, 15, 25 is 150 more than its 12 th term?

- Watch Video Solution

8. In an AP, the 18th term is 20 more than the

13th term. If the fourth term is 22 , find the AP.

- Watch Video Solution

9. Find the common difference of the AP in which 18 th term is 10 less than the 20th term.

- Watch Video Solution

10. The 24th term of an AP is twice its 10th term. Show that 72nd term is 4 times its 15th term.

## D Watch Video Solution

11. Find the sum of first:
a] 13 term of AP $2,6,10,14, \ldots$.
b] 20 terms of AP $-6,0,6,12, \ldots . .$.
c] 15 term of AP $18,16,14$,

## 12. Find the sum of

a] first 10 multiples of 8
b] first 25 multiples of 3
c] first 100 multiples of 2.

## D Watch Video Solution

13. Find the sum of
i] $41,36,31, \ldots . . .$. upto 10 terms
ii] $-26,-24,-22$, ..... upto 36 terms.
14. Find the sum of first $n$ odd natural numbers.

## D Watch Video Solution

15. Find the sum of first $n$ even numbers.

D Watch Video Solution
16. For what values of $n$, the $n$th terms of the
following sequences are equal:
$13,19,25, \ldots .$. and $69,68,67, \ldots .$.

## D Watch Video Solution

17. Determine $k$ such that
$(3 k-2),(4 k-6)$ and $(k+2)$ are three consecutive terms of AP.
18. How many two digits numerals are divisible by $6 ?$

## - Watch Video Solution

19. The first and last terms of an AP are 7 and
20. How many terms make the sum 420?

## - Watch Video Solution

20. Which term of an AP $3,8,13,18, \ldots .$. will be 55 more than 20th term?

## D Watch Video Solution

21. Find the common difference of an AP whose first term is 4 , last term is 49 and sum of all terms 265.

D Watch Video Solution
22. Three numbers which are in AP together make a 39 and their product is a 325 . Find the AP.

## D Watch Video Solution

23. The four sides of a quadrilateral form an

AP, taken in order. The difference in lengths
between each adjacent pair is 8 cm . If its perimeter is 168 cm , find the sides.
24. Find the Sum of $5+8+11+\ldots$ to 10 terms using formula.

D Watch Video Solution

Zen Additional Questions Short Answer Sa Type 2
Questions

1. Find the 12 th term from the end of AP 8, 10,

12, ..... , 130

## 2. Find the sum:

i] $28+31+$. . . . . . . . . . +100
ii] $28+26+\cdots \cdot . \cdot \cdots \cdot . \cdot+10$.
iii] $3+11+19+\ldots \ldots++803$.

## D Watch Video Solution

3. Find the sum of first 20 terms of an AP
whose nth term is $a_{n}=2-3 n$.

- Watch Video Solution

4. In an AP, the 5th term is 30 and 12th term is 65. What is the sum of first 20 terms?

## D Watch Video Solution

5. The first of an A.P is 5 , the last term is 45 and the sum is 400 . Find the number of terms and the common difference.

- Watch Video Solution

6. The sum of first $n$ terms of an $A P$ is
$3 n^{2}+4 n$. Find:
a] $a_{25}$
b] $a_{10}$

## - Watch Video Solution

7. Find the sum of all natural numbers between 50 and 500, which are divisible by 6 .

## - Watch Video Solution

8. 

Find
'x'
if
$1+4+7+10+\ldots \ldots .+x=287$.

D Watch Video Solution
9. Find the sum of all natural numbers between 1 and 1000 which are divisible by 3,

- Watch Video Solution

10. The sum of first 14 terms of an AP is 1505 and its first term is 10 . Find its tenth term.

## D Watch Video Solution

11. The sum of first 7 terms of an AP is 63 and
the sum of next 7 terms is 161 . Find $a_{28}$.

## D Watch Video Solution

12. Find the middle term of $A P$ :
$10,7,4, \ldots \ldots,-62$.

D Watch Video Solution
13. The seventh term of an arithmetic progression is four times itss second term and twelth term is 2 more than three times of its
fourth term. Find the progression.

D Watch Video Solution
14. A line segment is divided into four parts
forming an arithmetic progression. The sum of the lengths of 3 rd and 4 th parts is three times the sum of the lengths of first two part.

If the length of fourth part is $\mathbf{s} 14 \mathrm{~cm}$, find the total length of the line segment.
(D) Watch Video Solution

Zen Additional Questions Long Answer La Type
Questions

1. If the sum of n terms of A.P. is $\frac{1}{2}\left(3 n^{2}+7 n\right)$ , find its $n^{\text {th }}$ term and write its 25 th term.

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2. The sum of first 6 terms of an A.P. is 42 . If its

10th and 30th terms are in the ratio $1: 3$, find $a_{8}$ and $a_{12}$.

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3. In an arithmetic progression, thrice the second term is equivalent to eighth term and the sum of fourth term and the seventh term is 9 greater than the ninth term. Find the AP.

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4. In and AP, the sum of the first 10 terms is
-150 and sum of the next ten terms is -550 .

Find the AP.
5. A person saved Rs. 500 in the first month and increased his saving by Rs. 50 every month. What is his savings at the end of 5 years?

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6. In an arithmetic progression of 50 terms,
the sum of first ten terms is 210 and the sum
of last fifteen terms is 2565 . Find the arithmetic progression.
7. The ratio of 11th term to 18th term of an AP
is $2: 3$. Find the ratio of 5 th term to the 21 st term, also the ratio of the sum of the first 5 terms to the sum of the first 21 terms.

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8. Along a road lies an odd number of stones placed at intervals of 10 m . These stones have
to be assembled around the middle stone. A person can carry one stone at a time, A man
started the job with one of the end of the stones by carrying in them succession. In carrying all the stones, he covered a distance of 3 km . Find the number of stones.

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9. A thief runs away from a police station with
a uniform speed of $100 \mathrm{~m} /$ minute. After 1 minute a policeman runs behind the thief to
catch him. He goes at a speed of $100 \mathrm{~m} /$ minute in first minute and increases his speed by $10 \mathrm{~m} /$ minute in each succeeding minute. How many minutes will the policeman take to catch the thief?

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10. The digits of a positive number of three digits are in A.P. and their sum is 15 . The number obtained by reversing the digit is 594
less than the original number. Find the number.

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11. If the roots of the equation
$(b-c) x^{2}+(c-a) x+(a-b)=0$
are equal show that $a, b, c$ are in A.P.

D View Text Solution
12. The sum of the fourth and eighth terms of an arithmetic progression is 24 and the sum of the sixth and tenth terms is 44 . Find the first three terms of the Arithmetic progression.

## D View Text Solution

13. There are five terms in an arrithmetic progression. the Sum of these terms is 55 , and
the fourth term is five more than the sum of
the first two terms.Find the terms of the Arithmaetic progression.

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14. In an arithmetic progression sixth term is one more than twice the thrid term. Tha sum of the fourth and fifth terms is five times the secon term. Find the tenth term of the arithmatic progression.

Zen Additional Questions Hots Higher Order Thinking Skills Questions

1. If $m$ times the $m^{\text {th }}$ term of an A.P. is equal ton times the $n^{\text {th }}$ term and $m \neq n$, show that $(m+n)^{t h}$ term is zero.

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2. In a given AP, $p^{\text {th }}$ term is $q$ and $q^{\text {th }}$ term is p .

Show that the $n^{\text {th }}$ term is $(p+q-n)$.
3. If $S_{n}$ denotes sum of the first n times of an
A.P, then prove that $S_{30}=2\left[S_{20-S_{10}}\right.$.

D View Text Solution
4. Find the sum of the following:
$\left(1-\frac{1}{n}\right)+\left(1-\frac{2}{n}\right)+\left(1-\frac{3}{n}\right)+\ldots \ldots$.
upto $n$ terms.

